

### **Announcements**

- Presentation topics due 02/07
- Homework 2 due 02/13

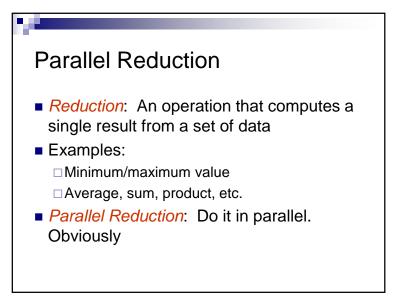
# Agenda

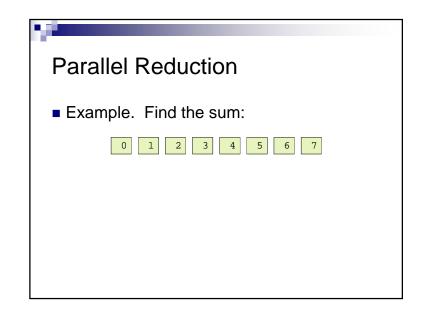
- Finish atomic functions from Monday
- Parallel Algorithms
  - □ Parallel Reduction
  - □Scan
  - ☐ Stream Compression
  - □ Summed Area Tables

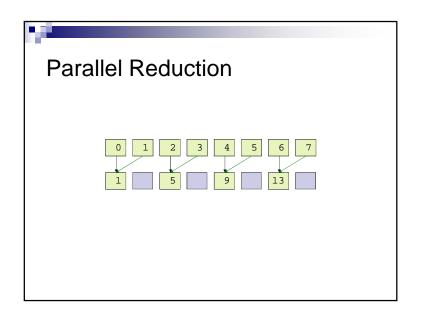
### **Parallel Reduction**

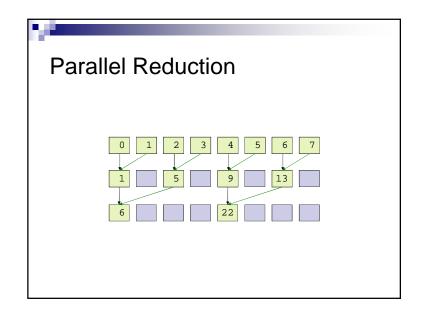
- Given an array of numbers, design a parallel algorithm to find the sum.
- Consider:
  - □ Arithmetic intensity: compute to memory access ratio

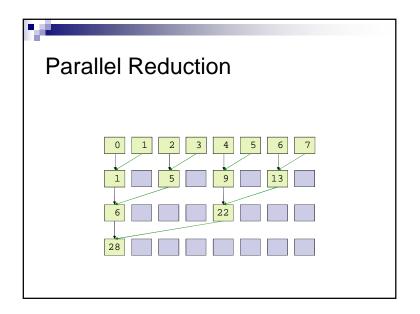
# Parallel Reduction Given an array of numbers, design a parallel algorithm to find: The sum The maximum value The product of values The average value How different are these algorithms?

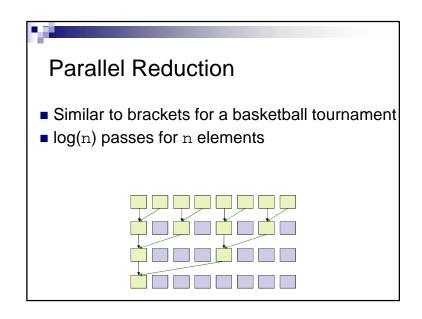


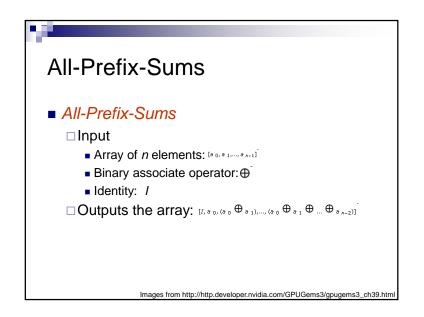












### All-Prefix-Sums

- Example
  - □ If ⊕ is addition, the array
    - **•** [3 1 7 0 4 1 6 3]
  - □ is transformed to
    - **•** [0 3 4 11 11 15 16 22]
- Seems sequential, but there is an efficient parallel solution

# Scan

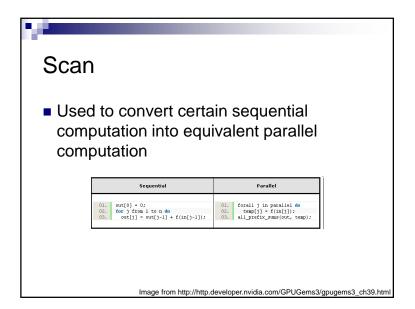
- *Scan*: all-prefix-sums operation on an array of data
- Exclusive Scan: Element j of the result does not include element j of the input:
  - In: [3 1 7 0 4 1 6 3] ■ Out: [0 3 4 11 11 15 16 22]
- *Inclusive Scan* (*Prescan*): All elements including *j* are summed
  - In: [3 1 7 0 4 1 6 3] ■ Out: [3 4 11 11 15 16 22 25]

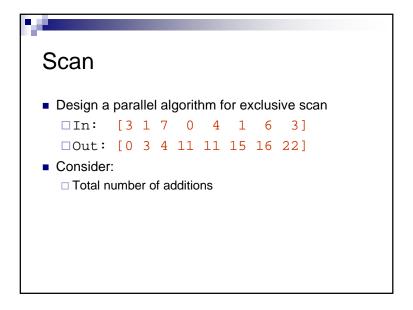
# Scan

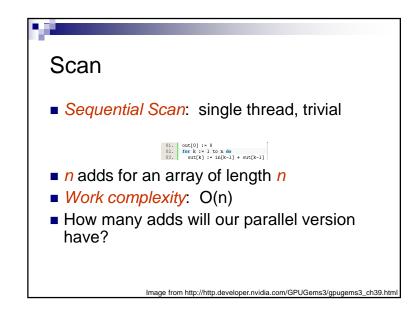
- How do you generate an exclusive scan from an inclusive scan?
  - Input: [3 1 7 0 4 1 6 3]
    Inclusive: [3 4 11 11 15 16 22 25]
    Exclusive: [0 3 4 11 11 15 16 22]
    // Shift right, insert identity
- How do you go in the opposite direction?

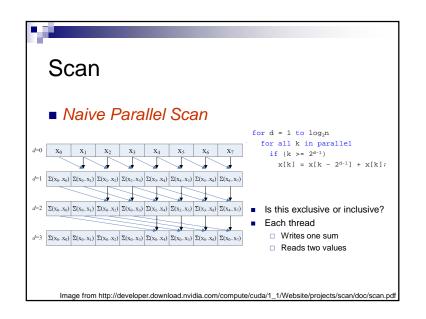
## Scan

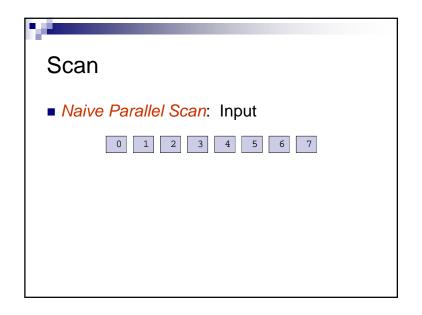
- Use cases
  - □ Stream compaction
  - □ Summed-area tables for variable width image processing
  - □ Radix sort
  - □ ...

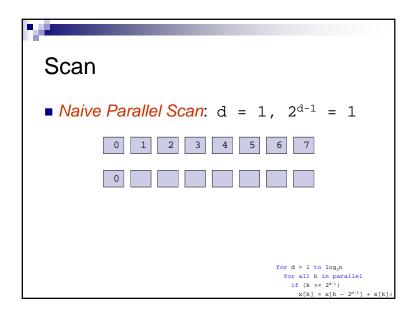


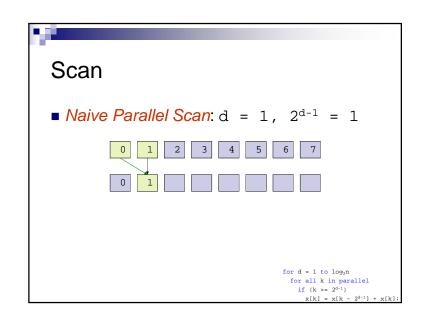


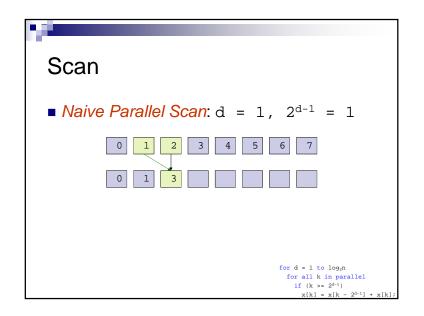


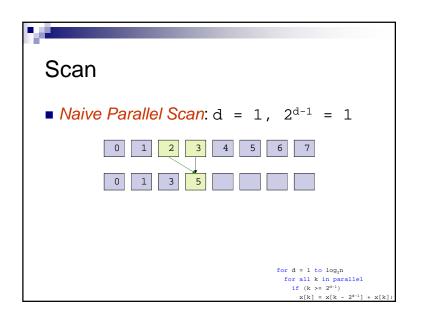


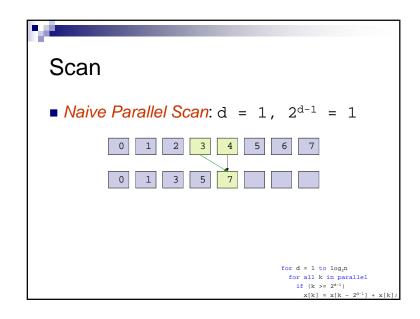


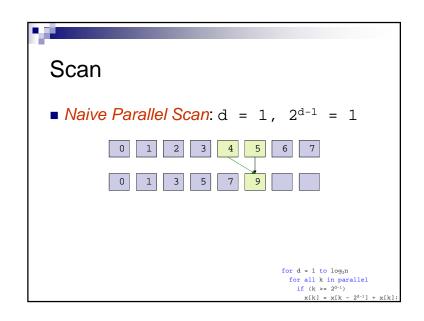


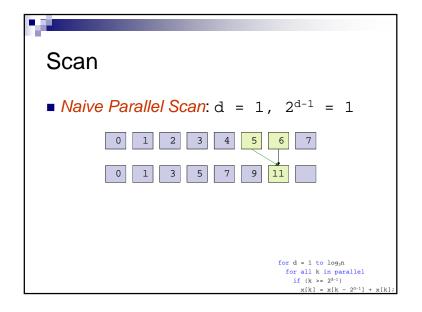


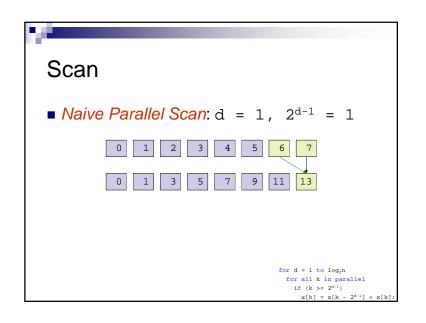


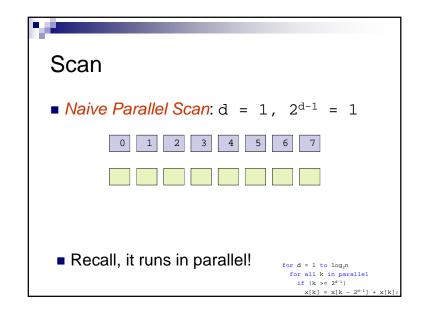


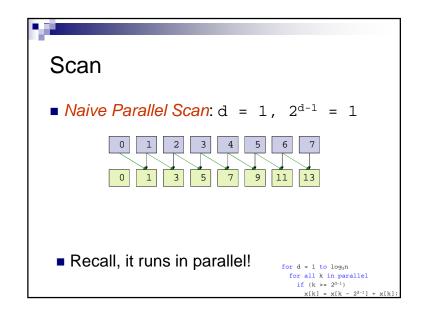


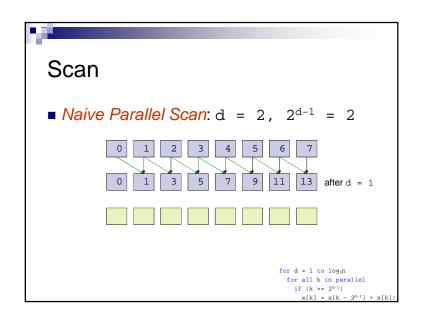


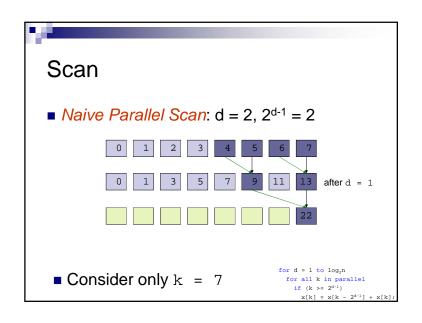


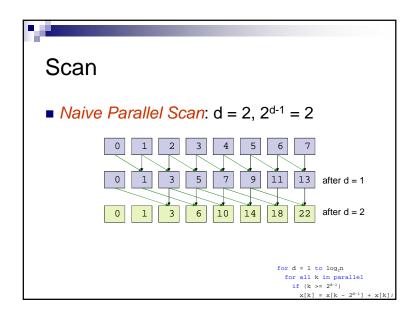


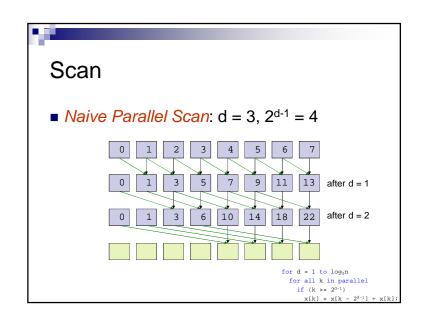


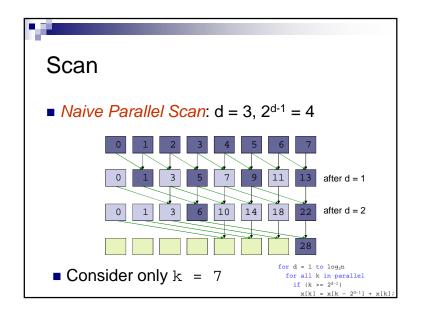


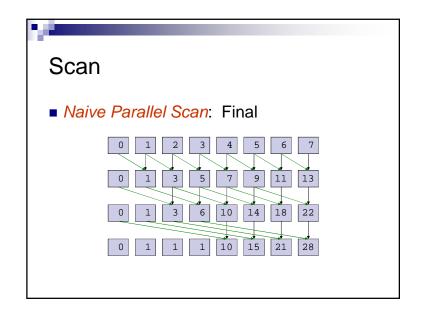


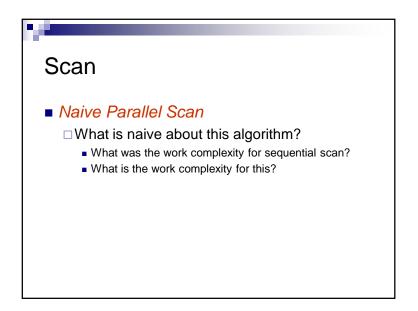


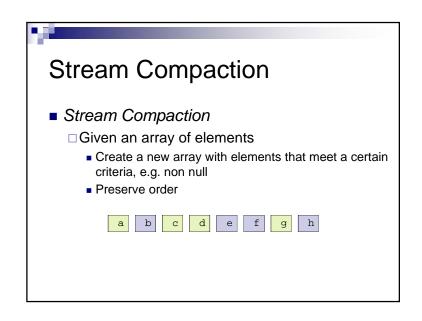


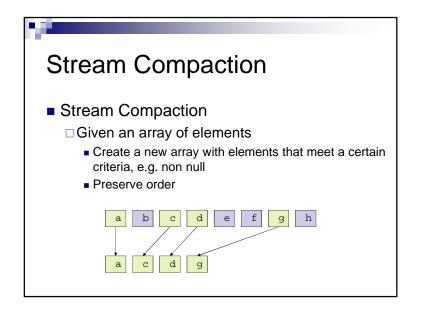


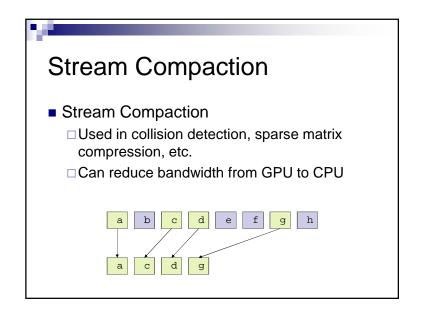


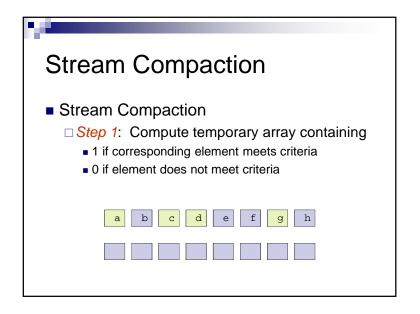


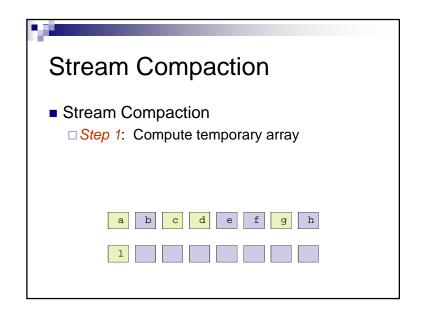


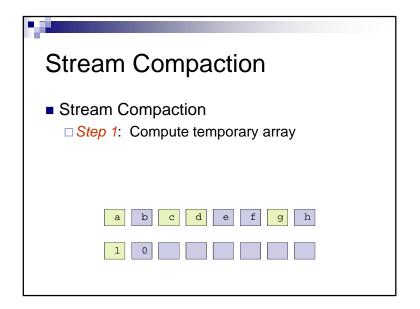


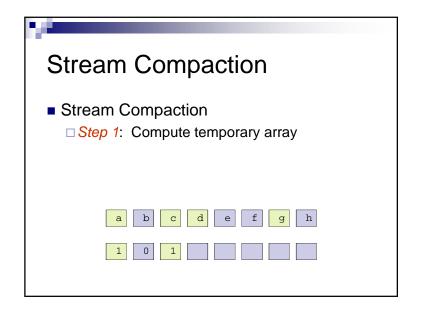


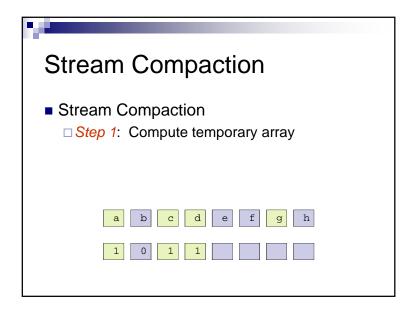


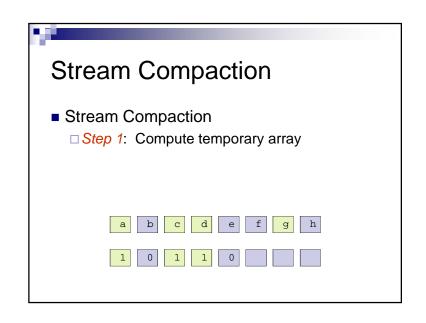


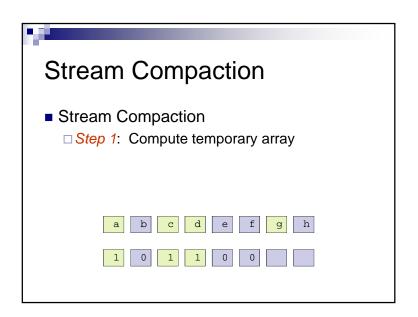


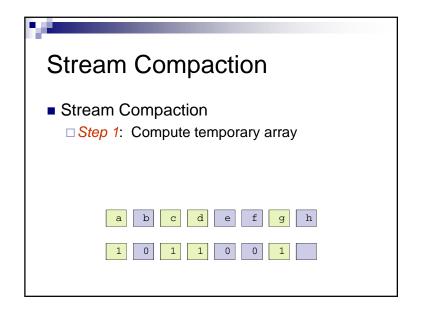


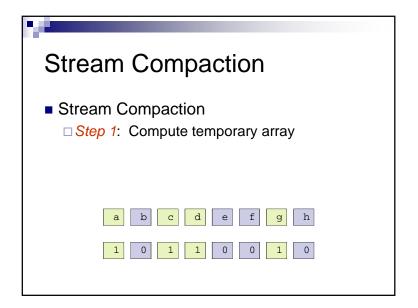


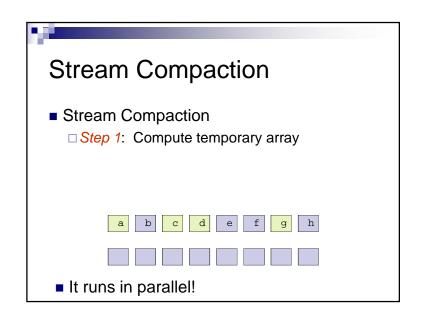


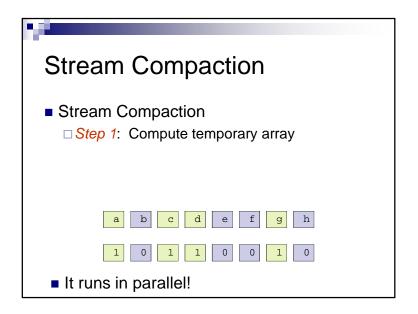


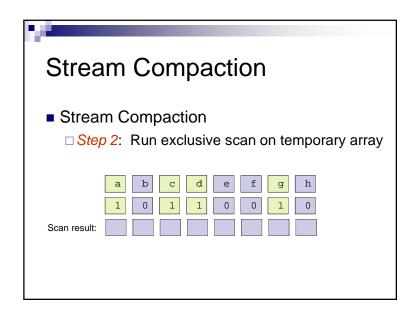


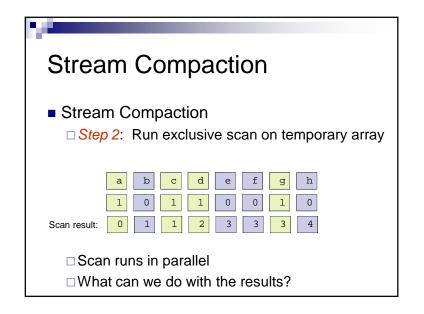


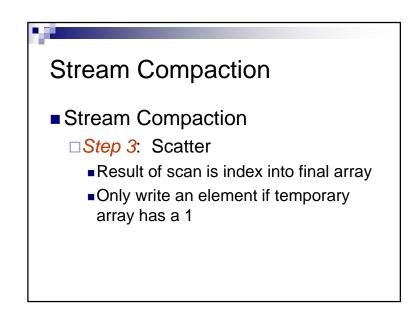


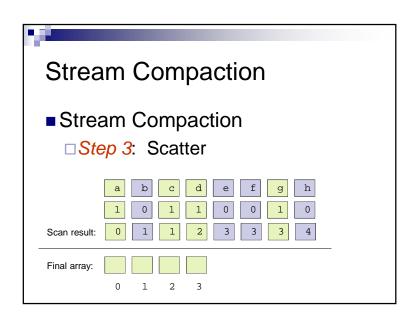


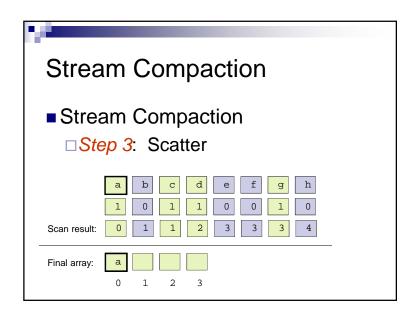


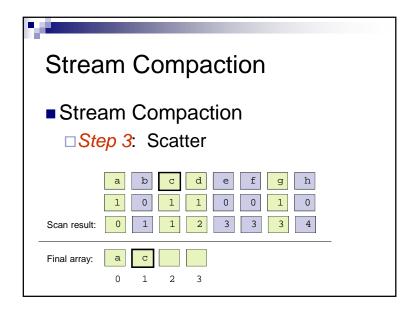


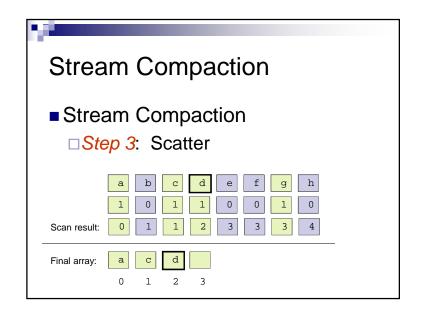


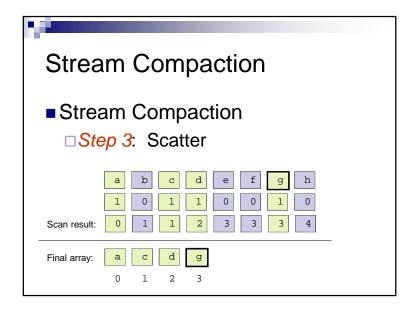




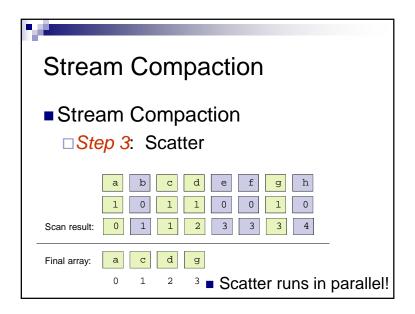






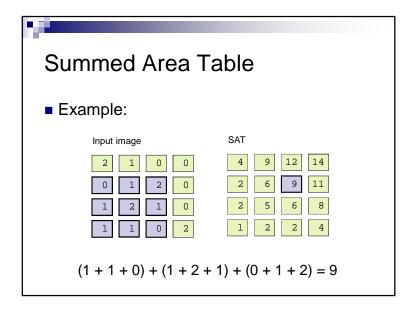


# Stream Compaction Stream Compaction Step 3: Scatter a b c d e f g h 1 0 1 1 0 0 1 0 Scan result: 0 1 1 2 3 3 4 Final array: 0 1 2 3 Scatter runs in parallel!



# Summed Area Table

■ Summed Area Table (SAT): 2D table where each element stores the sum of all elements in an input image between the lower left corner and the entry location.

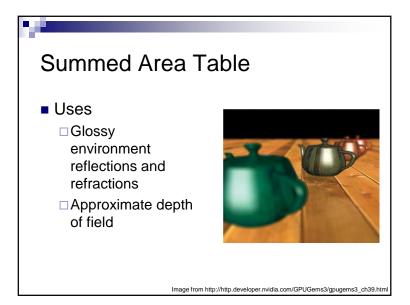


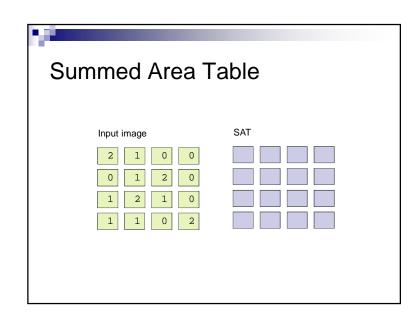
### Summed Area Table

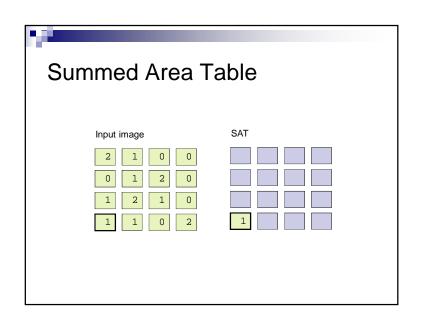
- Benefit
  - □ Used to perform different width filters at every pixel in the image in constant time per pixel□ Just sample four pixels in SAT:

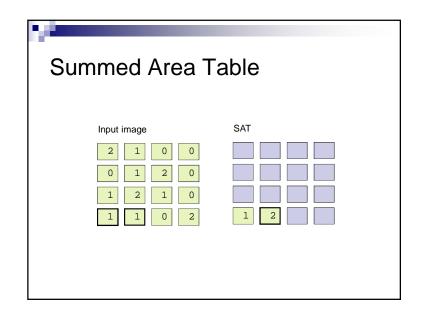
$$s_{filter} = \frac{s_{ur} - s_{ul} - s_{lr} + s_{ll}}{w \times h},$$

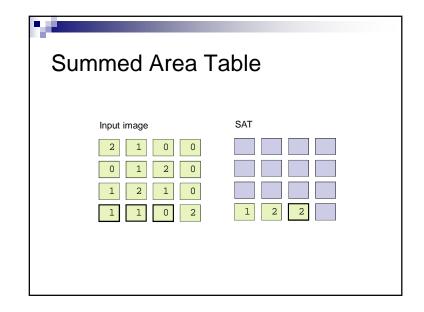
Image from http://http.developer.nvidia.com/GPUGems3/gpugems3\_ch39.htm

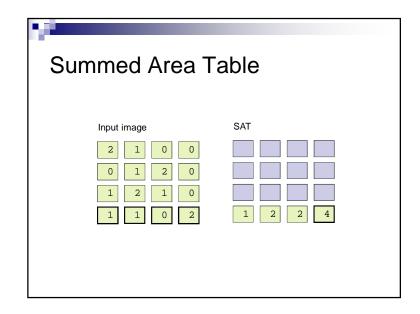


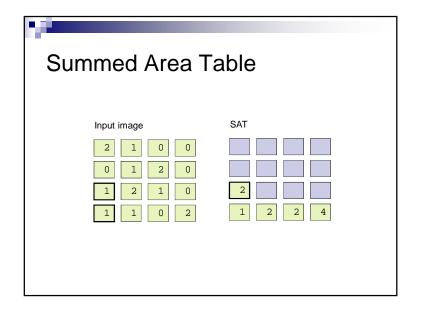


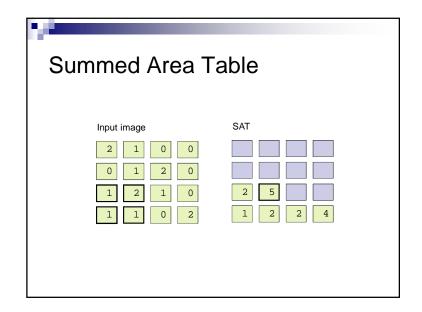


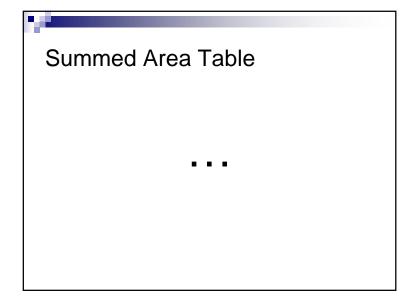


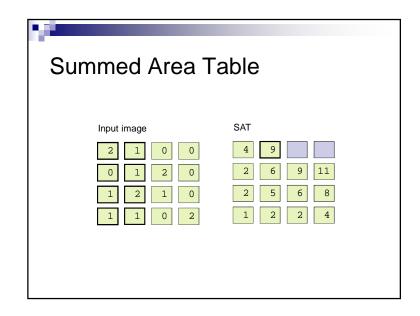


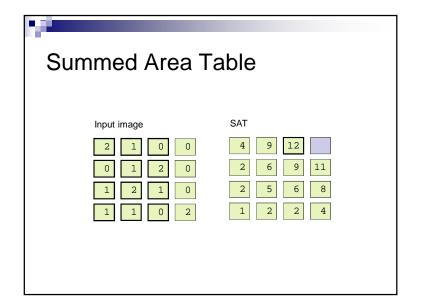


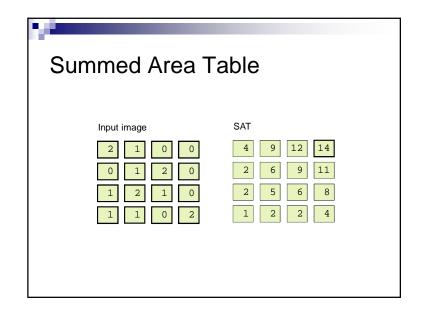






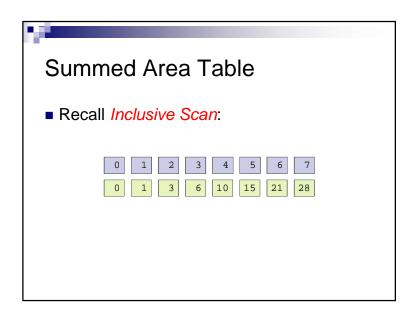






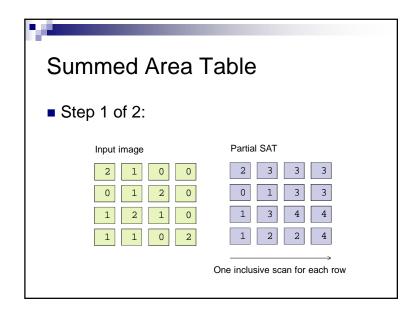
Summed Area Table

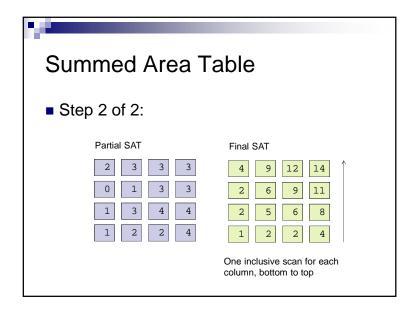
How would implement this on the GPU?



**Summed Area Table** 

How would compute a SAT on the GPU using inclusive scan?





## Summary

- Parallel reductions and scan are building blocks for many algorithms
- An understanding of parallel programming and GPU architecture yields efficient GPU implementations