

# Iris-OS Documentation

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## Abstract

This document describes formally the OS verification framework based on the Iris program logic. The latest versions of Iris document and the Iris Coq formalization can be found in the git repository at <https://gitlab.mpi-sws.org/FP/iris-coq/>.

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# 1 Language

## 1.1 Definitions

**Syntax.** The language is a simplified version of C. It consists of *Prim* (primitives), *Expr* (expressions), *Type* (types) and *Val* (values).

Memory address  $l : Addr \triangleq b \# o$  where block address  $b \in \mathbb{N}$ , offset  $o \in \mathbb{Z}^+$ .

$$\begin{aligned}
\tau : Type &::= \tau_{\text{void}} \mid \tau_{\text{null}} \mid \tau_{\text{int8}} \mid \tau_{\text{int32}} \mid * \tau \mid \tau \times \tau \\
v : Val &::= \text{void} \mid \text{null} \mid i \in [0, 2^8) \mid i \in [0, 2^{32}) \mid l \mid (v, v) \\
p : Prim &::= \text{cli} \mid \text{sti} \\
e : Expr &::= v \mid x \mid e \oplus e \mid !e \mid !_\tau e \mid \&e \mid e.1 \mid e.2 \\
&\quad \text{skip} \mid p \mid e \leftarrow e \mid \text{if}(e) \{e\} \text{ else } \{e\} \mid \text{while}_e(e) \{e\} \mid \\
&\quad \text{return } e \mid f(e_1, \dots, e_n) \mid e; e \mid \text{alloc}_\tau(e)
\end{aligned}$$

The relationship between  $!e$  and  $!_\tau e$ : The former one is in source, and the later one is “instantiated” with type information and used in inference rules. It is part of the efforts of removing lexical analysis from core program logic.

Note: the C program is usually more restrictive by differentiating statements and expressions. For simplicity and expressivity, we merged them together into a coherent expression *Expr* without loss of generality.

**Program.** A program is considered to be a set of functions *Function*, each identified by its name. Each function is a triple of return type  $\tau_{ret}$ , parameter declarations  $(x_1 : \tau_1, \dots)$ , and function body  $e$ .

**Evaluation Context.** To make the evaluation order explicit and reusable by the WP-BIND rule, we define evaluation context.

$$\begin{aligned}
K : \text{ECTX} &\triangleq \bullet \mid \bullet \oplus e \mid v \oplus \bullet \mid !\bullet \mid \&\bullet \mid \bullet.1 \mid \bullet.2 \mid \\
&\quad \bullet \leftarrow e \mid l \leftarrow \bullet \mid \text{if}(\bullet) \{e\} \text{ else } \{e\} \mid \text{while}_e(\bullet) \{e\} \mid \\
&\quad \text{return } \bullet \mid f(v_1, \dots, \bullet, e_1, \dots) \mid \text{alloc}_\tau(\bullet) \mid \bullet; e
\end{aligned}$$

## 1.2 Semantics

**Model.** Define continuation  $\text{CONT} \triangleq [K]$ , and stack  $\text{STACK} \triangleq [\text{CONT}]$ .

We define byte-size value and memory model:

$$v_{\text{byte}} : Val_{\text{byte}} \triangleq \frac{1}{2} \mid i \in [0, 2^8) \mid l_{\{0|1|2|3\}} \mid \text{null}$$

We define state  $\sigma : State \triangleq (\text{heap} : [l \mapsto v_{\text{byte}}], \text{text} : [x \mapsto Function], \text{stack} : \text{STACK})$ ,

You may notice the difference between *Val* and *Val<sub>byte</sub>*, it is intentional to create a layer of abstraction for easier manipulation of spatial assertions and also a clean, unified language syntax.

$$\begin{array}{c}
\text{ES-BINOP} \\
\frac{\llbracket \text{oplus} \rrbracket(v_1, v_2) = v'}{(v_1 \oplus v_2, \sigma) \rightarrow_{Expr} (v', \sigma)} \\
\\
\text{ES-DEREF-TYPED} \\
\frac{\vdash_{\text{tychk}} v : \tau \quad \sigma \vdash l \mapsto \text{encode}(v)}{(!_{\tau} l, \sigma) \rightarrow_{Expr} (v, \sigma)} \\
\\
\text{ES-FST} \\
((v_1, v_2).1, \sigma) \rightarrow_{Expr} (v_1, \sigma) \\
\\
\text{ES-SND} \\
((v_1, v_2).2, \sigma) \rightarrow_{Expr} (v_2, \sigma) \\
\\
\text{ES-ASSIGN} \\
(l \leftarrow v, \sigma) \rightarrow_{Expr} (\text{skip}, \sigma[l \mapsto \text{encode}(v)]) \\
\\
\text{ES-SEQ} \\
(v; e, \sigma) \rightarrow_{Expr} (e, \sigma) \\
\\
\text{ES-ALLOC} \\
\frac{\vdash_{\text{tychk}} v : \tau \quad \forall o'. \sigma(b, o') = \perp}{(\text{alloc}_{\tau}(v), \sigma) \rightarrow_{Expr} (b \# o, \sigma[b \# o \mapsto v])} \\
\\
\text{ES-WHILE-TRUE} \\
(\text{while}_e(\text{true}) \{s\}, \sigma) \rightarrow_{Expr} (s; \text{while}_e(e) \{s\}, \sigma) \\
\\
\text{ES-WHILE-FALSE} \\
(\text{while}_e(\text{false}) \{s\}, \sigma) \rightarrow_{Expr} (\text{skip}, \sigma) \\
\\
\text{ES-BIND'} \\
\frac{\text{is\_jump}(e) = \text{False} \quad (e, \sigma) \rightarrow_{Expr} (e', \sigma')}{((k :: ks)e, \sigma) \rightarrow_{Expr} ((k :: ks)e', \sigma')}
\end{array}$$

Figure 1: Semantics rules

**Small-Step Operational Semantics.** We define the HNF small step semantics for both non-jumping expression  $((e, \sigma) \rightarrow_{Expr} (e', \sigma'))$  and jumping expressions  $((e, s : \text{STACK}) \rightarrow_{\text{jump}}^{\sigma} (e', s' : \text{STACK}))$ , and then combine them together  $((e, \sigma, s) \rightarrow_{\text{cur}} (e', \sigma', s'))$ .

XXX: Define  $\sigma \vdash l \mapsto v_{\text{byte}}$

### 1.3 Type System and Environment

**Local Typing Rules.** The types are defined in §1.1, and all values in  $v$  can be *locally* typed trivially (since  $v$  is introduced to reflect type structure in some sense). Nevertheless, due to the fact that language of study is weakly-typed in the vein of C, we still have some “weird” rules worth documenting.

Here we define local typing judgment  $\vdash_{\text{tychk}} v : \tau$  for values.

$$\begin{array}{c}
\text{TYCHK-VOID} \quad \text{TYCHK-NULL} \quad \text{TYCHK-INT8} \quad \text{TYCHK-INT32} \\
\vdash_{\text{tychk}} \text{void} : \tau_{\text{void}} \quad \vdash_{\text{tychk}} \text{null} : \tau_{\text{null}} \quad \vdash_{\text{tychk}} i \in [0, 2^8) : \tau_{\text{int8}} \quad \vdash_{\text{tychk}} i \in [0, 2^{32}) : \tau_{\text{int32}} \\
\\
\text{TYCHK-NULL-PTR} \quad \text{TYCHK-PTR} \quad \text{TYCHK-PROD} \\
\forall \tau. \vdash_{\text{tychk}} \text{null} : * \tau \quad \forall \tau, l. \vdash_{\text{tychk}} l : * \tau \quad \frac{\vdash_{\text{tychk}} v_1 : \tau_1 \quad \vdash_{\text{tychk}} v_2 : \tau_2}{\vdash_{\text{tychk}} (v_1, v_2) : \tau_1 \times \tau_2}
\end{array}$$

**Typing Environment** When variables are introduced, we will need an environment  $\Gamma : Env \triangleq [x \mapsto (\tau, l)]$  to “unfold” the meaning of variables.

In Iris-OS, variables are all unfolded before the running the function body, which saves the program logic from caring about the lexical environment. During this unfolding, we will replace variables with either their location (left-hand side) or the dereference of their location (right-hand side). And we will also produce a pointer arithmetic expression when processing the left-hand side expression, which requires type inference  $\vdash_{\text{tyinf}} e : \tau$  (since it is standard and trivial, we will leave

out the details here).

Then we define the rules for “interpreting” left-hand side expression  $\langle\langle e \rangle\rangle_{\text{LHS}}$  and right-hand side expression  $\langle\langle e \rangle\rangle_{\text{RHS}}$ . In all rules below, a  $\Gamma$  is implicitly captured, and if any operation on  $\Gamma$  failed, then the rule will be returning “invalid” in implementation.

$$\begin{aligned}
\langle\langle e_1 \leftarrow e_2 \rangle\rangle_{\text{LHS}} &= \langle\langle e_1 \rangle\rangle_{\text{LHS}} \leftarrow e_2 \\
\langle\langle x \rangle\rangle_{\text{LHS}} &= \Gamma(x).l \\
\langle\langle !e \rangle\rangle_{\text{LHS}} &= \langle\langle e \rangle\rangle_{\text{RHS}} \\
\langle\langle e.1 \rangle\rangle_{\text{LHS}} &= \langle\langle e \rangle\rangle_{\text{LHS}} \\
\langle\langle e.2 \rangle\rangle_{\text{LHS}} &= \langle\langle e \rangle\rangle_{\text{LHS}} + \text{sizeof}(\tau) \quad \text{if } \vdash_{\text{tyinf}} \langle\langle e \rangle\rangle_{\text{LHS}} : *(\tau_1 \times \tau_2) \\
\langle\langle l \rangle\rangle_{\text{LHS}} &= l
\end{aligned}$$

$$\begin{aligned}
\langle\langle e_1 \leftarrow e_2 \rangle\rangle_{\text{RHS}} &= e_1 \leftarrow \langle\langle e_2 \rangle\rangle_{\text{RHS}} \\
\langle\langle x \rangle\rangle_{\text{RHS}} &= !_{\Gamma(x).t} \Gamma(x).l \\
\langle\langle !e \rangle\rangle_{\text{RHS}} &= !_\tau \langle\langle e \rangle\rangle_{\text{RHS}} \quad \text{if } \vdash_{\text{tyinf}} e : *\tau
\end{aligned}$$

The cases not covered are defined recursively (and trivially)

## 2 Program Logic

This section describes how to build a program logic for the C language (*c.f.* §1) on top of the base logic of Iris.

### 2.1 Extended Assertions

Using the standard Iris assertions and the ownership of ghost heap resource, we can define some basic custom assertions:

$$\begin{aligned} l \mapsto_q v : t &\triangleq l \mapsto_q \text{encode}(v) \wedge \vdash_{\text{tychk}} v : t \\ l \mapsto v : t &\triangleq l \mapsto_1 v : t \\ l \mapsto_q - : t &\triangleq \exists v. l \mapsto_q v : t \end{aligned}$$

### 2.2 Weakest Precondition

Finally, we can define the core piece of the program logic, the assertion that reasons about program behavior: Weakest precondition, from which Hoare triples will be derived.

**Defining weakest precondition.** While we have fixed the program state  $\sigma$  in language definition, but it can be any state, as long as it has a predicate  $S : \text{State} \rightarrow iProp$  that interprets the physical state as an Iris assertion. For our heap state,

$$S(\sigma) \triangleq \text{Own}(\bullet \text{fmap}(\lambda v. (1, \text{agv}), \sigma.\text{heap})) * \text{Own}(\bullet \sigma.\text{text}) * \text{Own}((\frac{1}{2}, \sigma.\text{stack}))$$

$$\begin{aligned} wp &\triangleq \mu wp. \lambda \mathcal{E}, E_{\text{cur}}, \Phi, \Phi_{\text{ret}}. \\ &(\exists v. \text{to\_val}(E_{\text{cur}}) = v \wedge \Vdash_{\mathcal{E}} \Phi(v)) \vee \\ &(\exists v. \text{to\_ret\_val}(E_{\text{cur}}) = v \wedge \Vdash_{\mathcal{E}} \Phi_{\text{ret}}(v)) \vee \\ &\left( \text{to\_val}(E_{\text{cur}}) = \perp \wedge \text{to\_ret\_val}(E_{\text{cur}}) = \perp \wedge \right. \\ &\quad \forall \sigma. S(\sigma) \stackrel{\mathcal{E}}{\equiv} *^{\emptyset} \\ &\quad \text{red}(e, \sigma) * \triangleright \forall E'_{\text{cur}}, \sigma'. (E_{\text{cur}}, \sigma \rightarrow E'_{\text{cur}}, \sigma') \stackrel{\emptyset}{\equiv} *^{\mathcal{E}} \\ &\quad \left. S(\sigma') * wp(\mathcal{E}, E'_{\text{cur}}, \Phi, \Phi_{\text{ret}}) \right) \end{aligned}$$

Here are some conventions:

- If we leave away the mask, we assume it to default to  $\top$ .
- We will leave  $\dagger$  out when writing  $E_{\text{cur}}$  in WP.
- $\Phi$  in post-condition might or might not take a value parameter, depending on the context.

**Laws of weakest precondition.** The following rules can all be derived:

$$\begin{array}{c}
\text{WP-VALUE} \quad \Phi(v) \vdash \text{wp}_{\mathcal{E}} v \{\Phi\} \qquad \text{WP-SKIP} \quad \triangleright \text{wp}_{\mathcal{E}} e \{\Phi\} \vdash \text{wp}_{\mathcal{E}} v; e \{\Phi\} \\
\\
\text{WP-RET} \quad \text{stack}(k' :: ks) * (\text{stack}(ks) \multimap \text{wp}_{\mathcal{E}} k'(v) \{\Phi\}) \vdash \text{wp}_{\mathcal{E}} k(\text{return } v) \{\Phi\} \\
\\
\text{WP-STRONG-MONO} \quad \frac{\mathcal{E}_1 \subseteq \mathcal{E}_2}{((\forall v. \Phi(v) \models_{\mathcal{E}_2} \Psi(v)) \wedge (\forall v. \Phi_{\text{ret}}(v) \models_{\mathcal{E}_2} \Psi_{\text{ret}}(v))) * \text{wp}_{\mathcal{E}_1} E_{\text{cur}} \{\Phi\} \vdash \text{wp}_{\mathcal{E}_2} E_{\text{cur}} \{\Psi\} \Psi_{\text{ret}}} \\
\\
\text{FUP-WP} \quad \models_{\mathcal{E}} \text{wp}_{\mathcal{E}} E_{\text{cur}} \{\Phi\} \vdash \text{wp}_{\mathcal{E}} E_{\text{cur}} \{\Phi\} \qquad \text{WP-FUP} \quad \text{wp}_{\mathcal{E}} E_{\text{cur}} \{x. \models_{\mathcal{E}} \Phi(x)\} x. \models_{\mathcal{E}} \Phi_{\text{ret}}(x) \vdash \text{wp}_{\mathcal{E}} e \{\Phi\} \\
\\
\text{WP-BIND} \quad \frac{\text{is\_jump}(e) = \text{False}}{\text{wp}_{\mathcal{E}} e \{x. \text{wp}_{\mathcal{E}} k(x) \{\Phi\}\} \vdash \text{wp}_{\mathcal{E}} k(e) \{\Phi\}} \qquad \text{WP-OP} \quad \frac{\llbracket \text{oplus} \rrbracket(v_1, v_2) = v'}{\Phi(v') \vdash \text{wp}_{\mathcal{E}} v_1 \oplus v_2 \{\Phi\}} \\
\\
\text{WP-ASSIGN} \quad \frac{\vdash_{\text{tychk}} v : \tau' \quad \sqrt{(\tau \leftarrow \tau')}}{l \mapsto - : \tau * (l \mapsto v : \tau \multimap \Phi) \vdash \text{wp}_{\mathcal{E}} l \leftarrow v \{\Phi\}} \qquad \text{WP-LOAD} \quad l \mapsto_q v : \tau * (l \mapsto_q v : \tau \multimap \Phi(v)) \vdash \text{wp}_{\mathcal{E}} !_{\tau} l \{\Phi\} \\
\\
\text{WP-SEQ} \quad \frac{\text{is\_jump}(e_1) = \text{False}}{\text{wp}_{\mathcal{E}} e_1 \{v, \text{wp}_{\mathcal{E}} v; e_2 \{\Phi\}\} \vdash \text{wp}_{\mathcal{E}} e_1; e_2 \{\Phi\}} \qquad \text{WP-WHILE-TRUE} \quad \frac{\text{wp}_{\mathcal{E}} s; \text{while}_e(e) \{s\} \{\Phi\}}{\text{wp}_{\mathcal{E}} \text{while}_e(\text{true}) \{s\} \{\Phi\}} \\
\\
\text{WP-WHILE-FALSE} \quad \frac{\Phi(\text{void})}{\text{wp}_{\mathcal{E}} \text{while}_e(\text{false}) \{s\} \{\Phi\}} \\
\\
\text{WP-WHILE-INV} \quad \frac{\forall \Phi. (I * (\forall v. (v = \text{false} * Q(\text{void})) \vee (v = \text{true} * I)) \multimap \Phi(v)) \multimap \text{wp } e \{\Phi\} \quad \forall \Phi. (I * (I \multimap \Phi(\text{void}))) \multimap \text{wp } s \{\Phi\}}{I \vdash \text{wp while}_e(e) \{s\} \{Q\}} \\
\\
\text{WP-FST} \quad \triangleright \Phi(v_1) \vdash \text{wp}_{\mathcal{E}} (v_1, v_2).1 \{\Phi\} \qquad \text{WP-SND} \quad \triangleright \Phi(v_2) \vdash \text{wp}_{\mathcal{E}} (v_1, v_2).1 \{\Phi\} \\
\\
\text{WP-ALLOC} \quad \frac{\vdash_{\text{tychk}} v : \tau}{(\forall l. l \mapsto v : \tau \multimap \Phi(l)) \vdash \text{wp}_{\mathcal{E}} \text{alloc}_{\tau}(v) \{\Phi\}} \\
\\
\text{WP-CALL} \quad f \mapsto_{\text{text}} (ps, e) * \text{stack}(ks) * \triangleright (\text{stack}(k :: ks) \multimap \text{wp}_{\mathcal{E}} \text{instantiate}(ps, ls, e) \{\Phi\}) \vdash \text{wp}_{\mathcal{E}} k(f(vs)) \{\Phi\}
\end{array}$$

## 3 OS and Virtualization

This section discusses the system features as part of the formalization. The first part, OS, mainly include interrupt and simulation. The second part, virtualization, mainly include virtual memory model and the memory allocator on top of that.

### 3.1 Interrupt

Interrupt is a hardware features, thus we will only write down its abstract specification without proving it. However, in the OS's perspective, multi-level interrupt will enable us to open/close OS-global invariants for different level of priorities.

### 3.2 Simulation

Simulation piggybacks on the WP-based program logic through two special kinds of assertions: spec state witnessing assertion and spec code assertion.

With this, we can give refinement style proofs for certain kernel APIs.

### 3.3 VMM

We will first write down the abstract spec for page table primitives: `insert`, `lookup`, and `delete`. They will change the locally owned page table content, which is modelled by a `gmap`.

On top of that, supposing that the physical heap memory is shared across the processes, and our language provides related operations. We can combine these operation with page table access to virtualize an exclusively owned, sequentially allocated memory space. The relevant operations will be `mem_init`, `mem_read` and `mem_write`.

Since our final client is a high-level language, we want to expose an object allocator interface built on top of the local virtual memory. The new operations for runtime to use will be `mem_alloc`, `mem_free`. `mem_init` will be called at the initialization time of the system.



## 4 Misc

This section contained some key formal developments claimed but not yet mechanized in Coq for reference.

### 4.1 Properties of Evaluation Context

Our expression  $Expr$  is a recursively defined algebraic data type, which can be generalized into the following form:

$$e : Expr ::= Expr_1(A_1, e^{r_1}) \mid \dots \mid Expr_n(A_n, e^{r_n}) \mid v$$

Here,  $Expr_i$  is tag for  $i$ -th class of expression,  $A_i$  is its arbitrary non-recursive payload, and  $e^{r_i}$  means it has  $r_i \in \mathbb{N}$  recursive occurrences.

It is apparent that ECTX is a direct translation of  $Expr$  plus some ordering considerations, though in actual Coq development we don't mechanize this fact. But we will make it explicit here to support some stronger claims than what we can do in Coq.

For some abstract  $Expr$  like above, its ECTX should be a sum of sub-ECTX $_i$  for each  $Expr_i$ . When  $r_i = 0$ , ECTX $_i$  doesn't exist, now we consider  $r_i > 0$ , define

$$k_i : ECTX_i ::= ECTX_{i1}(A_i, e^{r_i-1}) \mid ECTX_{i2}(A_i, v^1, e^{r_i-2}) \mid \dots \mid ECTX_{ir_i}(A_i, v^{r_i-1})$$

**Theorem 4.1.** For any  $e, e' : Expr$  and  $k_{im}, k_{jn} : ECTX$ ,

$$k_{im}(e) = k_{jn}(e') \vdash i = j$$

*Proof.* Trivial. □

**Theorem 4.2.** For any  $e, e' : Expr$  and  $k_{im}, k_{in} : ECTX_i$ ,

$$k_{im}(e) = k_{in}(e') \vdash (m = n \wedge e = e') \vee (m \neq n \wedge (\exists v. \text{to\_val}(e) = v \vee \exists v. \text{to\_val}(e) = v))$$

*Proof.* When  $m = n$ , by injectivity; When  $m \neq n$ , we can expand the equation like below without loss of generality:

$$\begin{aligned} Expr_i(A_i, v_1, \dots, v_{m-1}, e, e_{m+1}, \dots, e_{r_i-1}) = \\ Expr_i(A'_i, v'_1, \dots, v'_{m-1}, v'_m, \dots, e', \dots) \end{aligned}$$

So  $e = v'_m$  by injectivity. □

As you may observe, the expression space spanned by  $k(e)$  for any  $k, e$  is not the entire expression space as an ADT. Instead, it is a subset of  $Expr$  which represents well-formed ones that can appear as an immediate form according to some well-defined evaluation order. We call such  $e$  is *well-formed*.

Here we prove two lemmas about the syntactic structure on paper:

**Lemma 4.3.**  $\forall e : Expr, k : \text{CONT}. \text{is\_enf}(e) \rightarrow \text{unfill}(k(e)) = (k, e)$

*Proof.* Let's prove inductively w.r.t  $k$ . When  $k$  is empty, since  $e$  is in normal form, so unfill it will only return the same thing. And inductively, since fill and unfill should cancel out, the final conclusion is proved trivially as well. □

**Lemma 4.4.** *Induction scheme for Expr:*

$$\begin{aligned} \forall P : \text{Expr} \rightarrow \text{Prop}. (\forall e. \text{is\_enf}(e) \rightarrow P(e)) \rightarrow \\ (\forall e, k : \text{CONT}. \text{to\_val}(e) = \perp \rightarrow \text{well\_formed}(e) \rightarrow P(e) \rightarrow P(k(e))) \rightarrow \\ (\forall e. \text{to\_val}(e) = \perp \rightarrow \text{well\_formed}(e) \rightarrow P(e)) \end{aligned}$$

*Proof.* We want to *inductively* prove that for any non-value, *well-formed*  $e$ ,  $P(e)$  holds. Note that  $P$  here can be any proposition.

The base case is when  $e$  is in normal form, which corresponds to the first condition; The inductive case is that for any well-formed  $e'$  that is not in normal form, it must be of the form  $k(e)$  for some  $k, e$ . With each proved given sufficient inductive assumption, we know that any well-formed  $e$  must satisfy  $P$ .  $\square$