

## Section 3.1

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“Learning is not child’s play; we cannot learn without pain.”

- Aristotle

## Where's the $p$ -value?

Let  $\pi$  denote some population proportion of interest and suppose a 99% confidence interval for  $\pi$  is calculated to be  $(0.5, 0.8)$ . Also, suppose that we want to test  $H_0 : \pi = 0.79$  vs.  $H_a : \pi \neq 0.79$ .

(1) What can you say for sure about the corresponding  $p$ -value?

- A The corresponding  $p$ -value will be greater than 5%.
- B The corresponding  $p$ -value will be equal to 1%.
- C The corresponding  $p$ -value will greater than 1%.
- D The corresponding  $p$ -value will less than 1%.

## What's the confidence interval?

Suppose we are constructing a confidence interval using repeated tests of significance. Using two-sided tests each time with the following null hypotheses, we obtain these  $p$ -values.

Null	p-value	Null	p-value
Proportion = 0.45	0.014	Proportion = 0.53	0.787
Proportion = 0.46	0.032	Proportion = 0.54	0.572
Proportion = 0.47	0.062	Proportion = 0.55	0.373
Proportion = 0.48	0.126	Proportion = 0.56	0.142
Proportion = 0.49	0.371	Proportion = 0.57	0.077
Proportion = 0.50	0.598	Proportion = 0.58	0.042
Proportion = 0.51	0.733	Proportion = 0.59	0.021
Proportion = 0.52	0.986	Proportion = 0.60	0.003

(2) Give an approximate 90% CI in the form (*lower*, *upper*).

A (0.47, 0.58)

C (0.48, 0.56)

B (0.47, 0.57)

D (0.46, 0.57)

Let  $\pi$  denote some population proportion of interest and suppose a 95% confidence interval for  $\pi$  is calculated to be (0.25, 0.55).

(3) Give one plausible value for  $\pi$ .

A 0.20

B 0.56

C 0.13

D 0.95

E None of the above.

Let  $\pi$  denote some population proportion of interest and suppose a 95% confidence interval for  $\pi$  is calculated to be (0.25, 0.55).

(4) Make a guess for what the two-sided  $p$ -value would be if you hypothesized that  $\pi = 0.58$ .

A 0.99

B 0.01

C 0.25

D 0.50

E None of the above.

A representative sample to estimate some population proportion  $\pi$  produces the sample proportion  $\hat{p} = 0.54$ . A test of  $H_0 : \pi = 0.51$  against the alternative  $\pi \neq 0.51$  gives a  $p$ -value of  $p = 0.16$ .

(5) What can you say about the  $p$ -value one would obtain for the null hypothesis  $H_0 : \pi = 0.52$ ?

- A It would be smaller than  $p = 0.16$  because  $\hat{p} = 0.54$  is closer to  $\pi_0 = 0.52$  than it is to  $\pi_0 = 0.51$ .
- B It would be larger than  $p = 0.16$  because  $\hat{p} = 0.54$  is closer to  $\pi_0 = 0.52$  than it is to  $\pi_0 = 0.51$ .
- C It would be the same because  $\hat{p}$  has remained the same.
- D You would have to run the test or a simulation to decide.

A representative sample to estimate some population proportion  $\pi$  produces the sample proportion  $\hat{p} = 0.54$ . A test of  $H_0 : \pi = 0.51$  against the alternative  $\pi \neq 0.51$  gives a  $p$ -value of  $p = 0.16$ .

(6) What can you say about the  $p$ -value one would obtain for the null hypothesis  $H_0 : \pi = 0.57$ ?

- A It would be smaller than  $p = 0.16$  because  $\hat{p} = 0.54$  is less than  $\pi_0 = 0.57$ .
- B It would be larger than  $p = 0.16$  because the  $z$ -score for 0.57 is positive.
- C It would be similar to  $p = 0.16$  because 0.57 is the same distance from 0.54 as 0.51 is.
- D You would have to run the test or a simulation to decide.



A representative sample to estimate some population proportion  $\pi$  produces the sample proportion  $\hat{p} = 0.54$ . A test of  $H_0 : \pi = 0.51$  against the alternative  $\pi \neq 0.51$  gives a  $p$ -value of  $p = 0.16$ .

(7) Assuming a two-tailed alternative, which of the following null hypotheses do you think will give a  $p$ -value smaller than  $p = 0.16$ ?

A  $H_0 : \pi = 0.64$ .

B  $H_0 : \pi = 0.53$

C  $H_0 : \pi = 0.47$ .

D B and C but not A.

E A and C but not B.

Teenage hearing loss has increased significantly in America over the past several years. A 95% CI using the interval of plausible values method is given by  $(0.16, 0.23)$ .

(8) Which of the following could be the 99% CI based on the same sample?

A  $(0.13, 0.22)$

B  $(0.18, 0.21)$

C  $(0.14, 0.25)$

D  $(0.16, 0.27)$

E None of the above.

## Key Terms and Ideas to Understand in Section 3.2 and 3.3

- Confidence level
- Margin-of-error
- Center of CI
- Multiplier
- Standard error of  $\hat{p}$
- Standard error of  $\bar{x}$
- 2 SD Method for CIs