

$$M = \begin{bmatrix} -fxr_{11} + oxr_{31} & -fxr_{12} + oxr_{32} & -fxr_{13} + oxr_{33} & -fxT_x + oxT_z \\ -fy r_{21} + oy r_{31} & -fy r_{22} + oy r_{32} & -fy r_{23} + oy r_{33} & -fyT_y + oyT_z \\ r_{31} & r_{32} & r_{33} & T_z \end{bmatrix}$$

$$\vec{M} = \gamma M \quad \text{where } |\gamma| = \sqrt{r_{31}^2 + r_{32}^2 + r_{33}^2} = |\gamma|$$

computed rotation matrix R , rows and columns are unit vectors and their dot product is zero

and we know $T_z \neq 0$ since we are in flat space, compute γ and so find original Π

$$q_1 = [m_{11} \ m_{12} \ m_{13}]$$

$$q_2 = [m_{21} \ m_{22} \ m_{23}]$$

$$q_3 = [m_{31} \ m_{32} \ m_{33}]$$

~~matrix~~

$$\begin{bmatrix} \bar{r}_1 \\ \bar{r}_2 \\ \bar{r}_3 \end{bmatrix}$$

$$r_1 \cdot r_1 \quad r_2 \cdot r_2 \quad r_3 \cdot r_3$$

$$= |r_1|^2 = |r_2|^2 = |r_3|^2 = 1$$

$$= \bar{r}_1 \cdot \bar{r}_2 = \bar{r}_1 \cdot \bar{r}_3 = \bar{r}_2 \cdot \bar{r}_3 = 0$$

$q_1 \cdot q_3$

by characteristics of rotation matrix

$$-fx r_{31} r_{11} + ox r_{31}^2 - fx r_{12} r_{32} + oy r_{32}^2 - fx r_{23} r_{33} + oy r_{33}^2$$

$$-fx(r_{31} r_{11} + r_{32} r_{12} + r_{33} r_{23}) + ox(r_{31}^2 + r_{32}^2 + r_{33}^2)$$

0

$$\bar{q}_1 \cdot \bar{q}_3 = 0x \quad \text{similarly } \bar{q}_2 \cdot \bar{q}_3 = 0y$$