

N4.2

$$\langle x_f | U(T) | x_i \rangle = \sqrt{\frac{m}{2\pi i \hbar T}} \exp\left(\frac{i S_{cl}(P_i)}{\hbar}\right) - \text{сб. энергии}$$

~~U(x_f, t_f; x_i, t_i)~~

$$U(x_f, t_f; x_i, t_i) = \sqrt{\frac{1}{2\pi i \hbar}} \frac{\partial^2 S_{cl}}{\partial x_f \partial x_i} e^{i S_{cl}/\hbar}$$

$$S_{cl} = \frac{m}{2T} (x_a - x_b)^2$$

$$\frac{\partial S_{cl}}{\partial x_a} = \frac{m}{T} (x_a - x_b)$$

$$\frac{\partial^2 S_{cl}}{\partial x_a \partial x_b} = \frac{m}{T} \Rightarrow U = \sqrt{\frac{m}{2\pi i \hbar T}} \exp\left(\frac{i S_{cl}}{\hbar}\right)$$

$$\stackrel{!!!}{F(T)} = \sqrt{\frac{m}{2\pi i \hbar T}}$$

N4.1

$$U(x_f, t_f; x_i, t_i) = \frac{m\omega}{2\sin(\omega T)} \left[(x_a^2 + x_b^2) \cos(\omega T) - 2x_a x_b \right] T = t_f - t_i$$

$$\frac{\partial^2 S_{cl}}{\partial x_a \partial x_b} = \frac{m\omega}{2\sin \omega T} [-2] = -\frac{m\omega}{\sin \omega T}$$

$$\Rightarrow U = \sqrt{\frac{1}{2\pi i \hbar} \frac{-m\omega}{\sin \omega T}} e^{i S_{cl}/\hbar} \Rightarrow F = \sqrt{\frac{i m \omega}{2\pi \hbar \sin \omega T}}$$