

N2.3

$$\frac{1}{\mu_n} = n^{-1} \sum_{i=1}^n x_i^{-1}$$

$n \rightarrow \infty \Rightarrow$ converges to $\frac{1}{\mu}$ que

$$\frac{1}{n} \sum_{i=1}^n x_i^{-1}$$

$$\Rightarrow P_n\left(\frac{1}{\mu_n}\right) \rightarrow N\left(\mu_x, \frac{\sigma_x^2}{n}\right) \quad x_n = \frac{1}{\mu_n};$$

$$\left\langle \frac{1}{x} \right\rangle \mu_x = \mu_{x_n}; \quad \sigma_{x_n}^2 = \frac{\sigma_x^2}{n} = \frac{1}{n} \left[\left\langle \frac{1}{x^2} \right\rangle - \left(\left\langle \frac{1}{x} \right\rangle \right)^2 \right]$$

$$\Rightarrow P_n\left(\frac{1}{\mu_n}\right) \rightarrow \frac{\sqrt{n}}{\sqrt{\left\langle \frac{1}{x^2} \right\rangle - \left(\left\langle \frac{1}{x} \right\rangle \right)^2}} \cdot \exp \left[-n \frac{\left(\frac{1}{\mu_n} - \left\langle \frac{1}{x} \right\rangle \right)^2}{2 \left(\left\langle \frac{1}{x^2} \right\rangle - \left(\left\langle \frac{1}{x} \right\rangle \right)^2 \right)} \right]$$

$$P_n(\mu_n) = P_n\left(\frac{1}{\mu_n}\right) \cdot \left| \frac{\partial \frac{1}{\mu}}{\partial \mu} \right| = \frac{1}{\mu_n^2} P_n\left(\frac{1}{\mu_n}\right)$$

$$P_n(\mu) = \frac{1}{\mu_n^2} \cdot \frac{\sqrt{n}}{\sqrt{\left\langle \frac{1}{x^2} \right\rangle - \left(\left\langle \frac{1}{x} \right\rangle \right)^2}} \cdot \exp \left[-n \frac{\left(\frac{1}{\mu_n} - \left\langle \frac{1}{x} \right\rangle \right)^2}{2 \left(\left\langle \frac{1}{x^2} \right\rangle - \left(\left\langle \frac{1}{x} \right\rangle \right)^2 \right)} \right]$$