

Lec 6, HW 1

- $\alpha_i (y_i w^T x_i - 1 + \xi_i) = 0$
- $\beta_i \xi_i = 0$

1. $\alpha_i = 0 \Rightarrow y_i w^T x_i \geq 1$

$$\alpha_i = 0 \Rightarrow \beta_i = c$$

$$\Rightarrow \xi_i = 0$$

$$\Rightarrow y_i w^T x_i - 1 \geq 0$$

2. $0 < \alpha_i < c \Rightarrow y_i w^T x_i = 1$

$$0 < \alpha_i < c \Rightarrow y_i w^T x_i - 1 + \xi_i = 0, \beta_i > 0$$

$$\Rightarrow y_i w^T x_i - 1 + \xi_i = 0, \xi_i = 0$$

$$\Rightarrow y_i w^T x_i - 1 = 0$$

3. $\alpha_i = c \Rightarrow y_i w^T x_i \leq 1$

$$\alpha_i = c \Rightarrow y_i w^T x_i - 1 + \xi_i = 0$$

$$\Leftrightarrow y_i w^T x_i = 1 - \xi_i$$

$$\Rightarrow y_i w^T x_i \leq 1$$

4. $y_i w^T x_i > 1 \Rightarrow \alpha_i = 0$

$$y_i w^T x_i > 1 \Rightarrow y_i w^T x_i - 1 + \xi_i \geq y_i w^T x_i - 1 > 0$$

$$\Rightarrow \alpha_i = 0 \quad \because \alpha_i (y_i w^T x_i - 1 + \xi_i) = 0$$

5. $y_i w^T x_i < 1 \Rightarrow \alpha_i = c$

$$y_i w^T x_i < 1 \Rightarrow 0 \leq y_i w^T x_i - 1 + \xi_i < \xi_i$$

$$\Rightarrow 0 \neq \xi_i$$

$$\Rightarrow \beta_i = 0$$

$$\Rightarrow \alpha_i = c$$

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