

## JUNYUAN PRIMARY SCHOOL

Welcome to P3 and P4 Math Alive Workshop for Parents Fri, 8 April 2022



## JUNYUAN PRIMARY SCHOOL

### A note to P4 parents:

This workshop is similar to last year's "P3 and P4 Math Alive" Workshop.

If you have attended last year, feel free to excuse yourself from today's workshop or go ahead and attend this as a refresher workshop.



The material shared in today's workshop is under the property of Junyuan Primary School, Mathematics Department.

Please <u>do not</u> take any photos or videos throughout the sharing.

Thank you for your understanding.

## 1 km = 1000 m Math Alive!

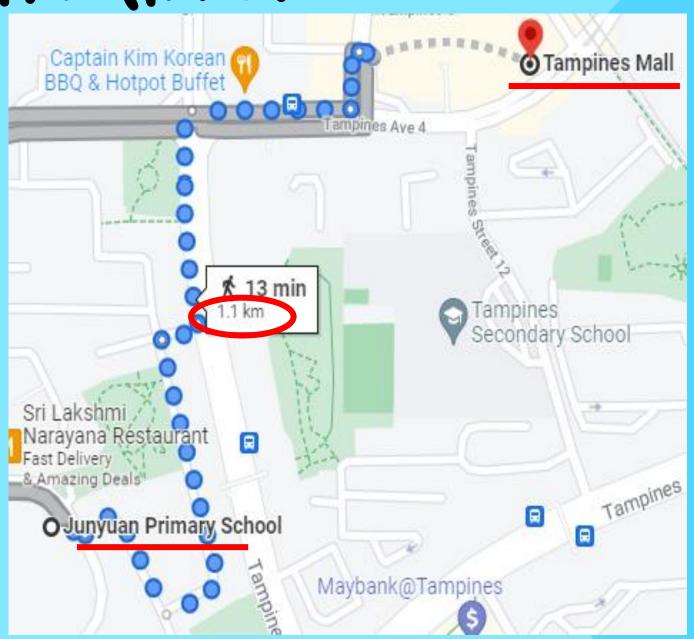


via Tampines Ave 5

Mostly flat



The distance from JYPS to Tampines Mall is about 1 km. Time taken is 13 min.



## Math Alive!

How heavy is Mr A?

Ans: 102 kg



Mr A jogs every morning and he is 12 kg lighter now. How heavy is he now?

Ans:

102 kg - 12 kg = 90 kg

## Math Alive!



















#### How much is the amount shown?

Ans: \$189

Mr B wants to buy a bicycle that costs \$200. How much more money does he need?

Ans:

\$200 - \$189 = \$11

## Math Alive!

Miss X bought a pizza for the family and cut it equally into 6 pieces.

Her son ate  $\frac{1}{3}$  of the pizza.

Her daughter ate a slice of the pizza.

What fraction of the pizza was left?



#### Ans:

$$\frac{1}{3} = \frac{2}{6}$$
 (son ate 2 slices)

$$2 + 1 = 3$$
 (total slices eaten)

$$\frac{3}{6} = \frac{1}{2}$$
 (left)

## **Outline of Workshop**

- 1) Introduction to Metacognition in Problem Solving using STAR approach
- 2) Problem Solving using Model Drawing strategy
- 3) Problem Solving using Restate the Problem strategy
- 4) Q & A

### Singapore Mathematics Framework

Mathematics Curriculum Framework

Belief, appreciation, confidence, motivation, interest and perseverance

Proficiency in carrying out operations and algorithms, visualising space, handling data and using mathematical tools

Awareness, monitoring and Metacognition regulation of thought processes Attitudes Mathematical Processes Problem Solving Skills Concepts

Competencies in abstracting and reasoning, representing and communicating, applying and modelling

Understanding of the properties and relationships, operations and algorithms

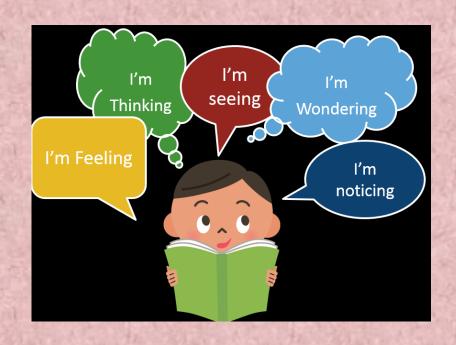
## Metacognition

### **Definition**

Think about one's own thinking – To be critically aware of one's thinking and learning.

### **Process**

- Monitor one's own thinking and one's existing state of knowledge
- Self-regulate one's learning through goal setting, self-monitoring and self instruction



## Metacognition

### How to develop metacognitive awareness

- Exposure to general problem solving skills
- Thinking aloud using the strategies and methods taught
- Attempting problems that require planning and evaluation
- -Seeking alternative ways to solve a problem
- -Checking reasonableness of answers

## Metacognition

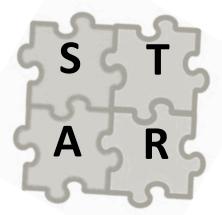
### STAR approach

- S ee what is given
- Think of a plan
- A ct on my plan
- R elook and check

### JUNYUAN PRIMARY SCHOOL MATHEMATICS



**P3** 



NAME:					

CLASS: P3 -

### See (What is given?)

#### Think (What is my plan?)

Can I use Model Drawing?

Can I look for a pattern?

Can I work backwards?

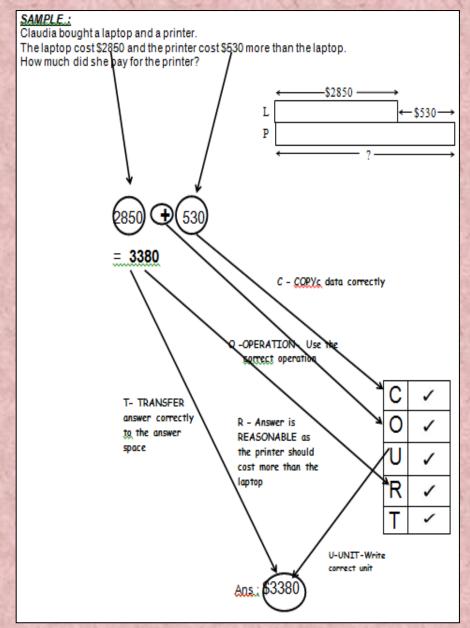
Can I use Guess and Check?

Other heuristic(s) I can use:

#### Act(What do I need to do?)

Relook(Reflect and Check)

## **CHECKING Strategy Using**



C-O-U-R-T

C — Copy data correctly

O — Operation sign

**U** — Unit of measurement

R — Reasonableness of answer

**T** — Transfer answer correctly

### Problem Solving using Model Drawing

- 1. Part-Whole Model
- 2. Comparison Model (2 Variables)
- 3. Comparison Model (3 Variables)
- 4. Unitary Method
- 5. Stacking Model
- 6. Fraction of a Set
- 7. Before and After

# Q1: Model Drawing (Part-Whole) – Find Total

Aaron has 452 cards. Benedict has 373 cards. How many cards do they have altogether?

See (What is given?)

Aaron  $\rightarrow$  452

Benedict → 373

Altogether?

Think (What is my plan?)

✓ Can I use Model Drawing?

Can I look for a pattern?

Can I work backwards?

Can I use Guess and Check?

Other heuristic(s) I can use:

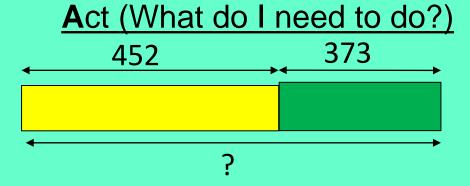
# Q1: Model Drawing (Part-Whole) – Find Total

See (What is given?)

Aaron  $\rightarrow$  452

Benedict → 373

Altogether?



<u>Method</u> 452 + 373 = 825

They have 825 cards altogether.

# Q1: Model Drawing (Part-Whole) – Find Total

Aaron has 452 cards. Benedict has 373 cards. How many cards do they have altogether?

<u>Act</u>

<u>Method</u>

452 + 373 = 825

Relook (Reflect and Check)



# Q2: Model Drawing (Part-Whole) – Find Part

Rachel and Sally have 263 hair clips altogether. Sally has 91 hair clips.
How many hair clips does Rachel have?

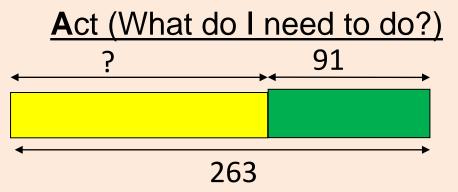
See (What is given?)
Rachel & Sally → 263
Sally → 91
Rachel ?

Think (What is my plan?)

✓ Can I use Model Drawing?
 Can I look for a pattern?
 Can I work backwards?
 Can I use Guess and Check?
 Other heuristic(s) I can use:

# Q2: Model Drawing (Part-Whole) – Find Part

See (What is given?)
Rachel & Sally → 263
Sally → 91
Rachel ?



Rachel has 172 paper clips.

# Q2: Model Drawing (Part-Whole) – Find Part

Rachel and Sally have 263 hair clips altogether. Sally has 91 hair clips.

How many hair clips does Rachel have?

Act Method

263 - 91 = 172

Relook (Reflect and Check)



# Q3: Model Drawing (Comparison with 2 variables) – Finding Difference

Hotel Pan Pacific Singapore charges \$330 per night. Hotel Amara Singapore charges \$198 per night. How much will Fes save if he decides to stay in Amara Singapore instead of Pan Pacific Singapore for three nights?

See (What is given?)
Pan Pacific → \$330
Amara → \$198
Save?

Think (What is my plan?)

✓ Can I use Model Drawing?
 Can I look for a pattern?
 Can I work backwards?
 Can I use Guess and Check?
 Other heuristic(s) I can use:

# Q3: Model Drawing (Comparison with 2 variables) – Finding Difference

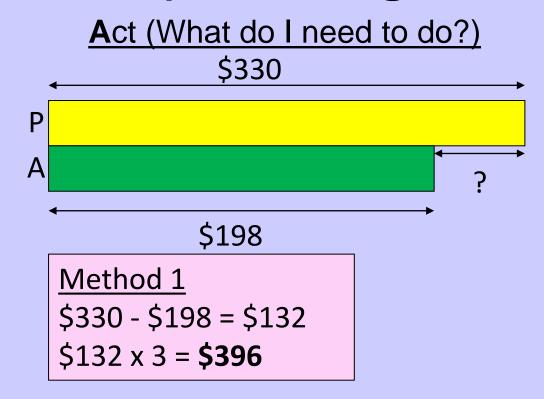
See (What is given?)

Pan Pacific → \$330

Amara  $\rightarrow$  \$198

Save?

Fes will save **\$396**.



# Q3: Model Drawing (Comparison with 2 variables) – Finding Difference

Hotel Pan Pacific Singapore charges \$330 per night. Hotel Amara Singapore charges \$198 per night. How much will Fes save if he decides to stay in Amara Singapore instead of Pan Pacific Singapore for three nights?

#### Act

Method 2

\$330 x 3 = \$990

\$198 x 3 = \$594

\$990 - \$594 = **\$396** 

#### Relook (Reflect and Check)

**\$396** + \$594 = \$990

\$594 ÷ 3 = \$198

\$990 ÷ 3 = \$330 ✓ ok

Fes will save \$396.

С	<b>✓</b>		
0	<b>\</b>		
U	<b>\</b>		
R	<b>✓</b>		
Т	<b>✓</b>		

# Q4: Model Drawing (Comparison with 2 variables – Unequal Distribution)

At a factory, Worker A and Worker B sorted 1886 plastic bottles altogether. Worker B sorted 988 more bottles than Worker A. How many bottles did Worker A sort?

#### See (What is given?)

 $A + B \rightarrow 1886$ 

 $B \rightarrow 988$  more than A

Qn: *A*?

#### Think (What is my plan?)

✓ Can I use Model Drawing?

Can I look for a pattern?

Can I work backwards?

Can I use Guess and Check?

Other heuristic(s) I can use:

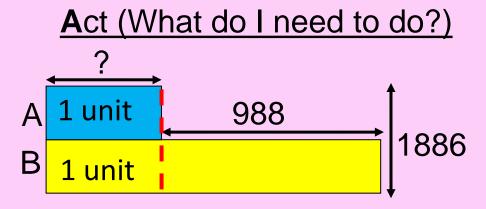
## Q4: Model Drawing (Comparison with 2 variables – Unequal Distribution)

See (What is given?)

 $A + B \rightarrow 1886$ 

 $B \rightarrow 988$  more than A

Qn: *A*?



1886 - 988 = 898  
2 units = 898  
1 unit = 898 
$$\div$$
 2  
= **449**

Worker A sorted 449 bottles in the morning.

# Q4: Model Drawing (Comparison with 2 variables – Unequal Distribution)

At a factory, Worker A and Worker B sorted 1886 plastic bottles altogether. Worker B sorted 988 more bottles than Worker A. How many bottles did Worker A sort?

#### Act

1886 - 988 = 898

2 units = 898

1 unit  $= 898 \div 2$ 

= 449

#### Relook (Reflect and Check)

1 unit = 449

 $2 \text{ units} = 449 \times 2$ 

= 898

 $898 + 988 = 1886 \checkmark ok$ 

Worker A sorted <u>449</u> bottles in the morning.

С	✓		
0	<b>✓</b>		
U	<b>\</b>		
R	<b>✓</b>		
Т	<b>✓</b>		



# Q5: Model Drawing (Comparison with 3 variables)

Mr Li saved \$5304 in January. He saved \$1509 more in February than in January. He also saved \$357 more in March than in February. How much did he save in March?

#### See (What is given?)

 $J \rightarrow $5304$ 

 $F \rightarrow $1509$  more than J

 $M \rightarrow $357$  more than F

Qn: M saved?

#### Think (What is my plan?)

✓ Can I use Model Drawing?

Can I look for a pattern?

Can I work backwards?

Can I use Guess and Check?

Other heuristic(s) I can use:

### Q5: Model Drawing (Comparison with 3 variables)

#### See (What is given?)

 $J \rightarrow $5304$ 

 $F \rightarrow $1509$  more than J

 $M \rightarrow $357$  more than F

Qn: M saved?

### Act (What do I need to do?) \$5304 \$1509 F \$357 M \$5304 + \$1509 = \$6813 \$6813 + \$357 = **\$7170**

$$$5304 + $1509 = $6813$$
  
 $$6813 + $357 = $7170$ 

He saved \$7170 in March.

# Q5: Model Drawing (Comparison with 3 variables)

Mr Li saved \$5304 in January. He saved \$1509 more in February than in January. He also saved \$357 more in March than in February. How much did he save in March?

#### **Act**

\$5304 + \$1509 = \$6813

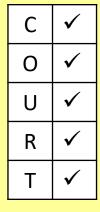
\$6813 + \$357 = **\$7170** 

Relook (Reflect and Check)

**\$7170** - \$357 = \$6813

\$6813 - \$1509 = \$5304 ✓ok

He saved \$7170 in March.



# Q6: Model Drawing (Comparison with 3 variables – *Hidden Part*)

Jimmy paid \$3480 for a <u>laptop</u>, <u>camera and printer</u>. The <u>laptop</u> cost \$450 more than the <u>camera</u>. The <u>camera</u> cost \$300 more than the <u>printer</u>. How much did he pay for the <u>laptop</u>?

#### See (What is given?)

$$L + C + P \rightarrow $3480$$

$$L \to $450 + C$$

$$C \to $300 + P$$

Qn: Laptop?

#### Think (What is my plan?)

✓ Can I use Model Drawing?

Can I look for a pattern?

Can I work backwards?

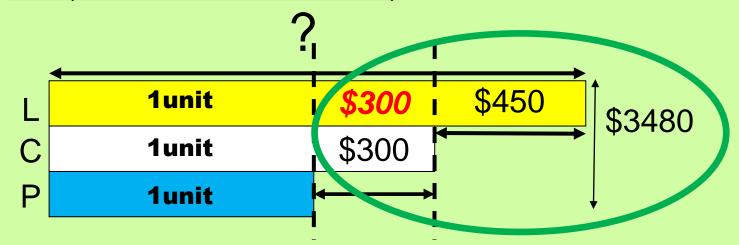
Can I use Guess and Check?

Other heuristic(s) I can use:

### Q6: Model Drawing

### (Comparison with 3 variables – *Hidden Part*)

Act (What do I need to do?)



$$3u = $2430$$

$$1u = $2430 \div 3 = $810$$

Laptop 
$$\rightarrow$$
 \$810 + \$300 + \$450 = **\$1560**

He paid **\$1560** for the laptop.

# Q6: Model Drawing (Comparison with 3 variables – *Hidden Part*)

#### Relook (Reflect and Check)

```
$1560 - $450 = $1110 (A camera)
```

$$$1110 - $300 = $810 (A printer)$$



### **Q7: Unitary Method (Find Total)**

Alex ran 234 m. Roy jogged thrice the distance ran by Alex. What was the total distance run by both Alex and Roy?

#### See (What is given?)

Alex  $\rightarrow$  234 m

Roy → 3x the distance ran by Alex

**Qn: Total distance ran?** 

#### Think (What is my plan?)

✓ Can I use Model Drawing?
Can I look for a pattern?

Can I work backwards?

Can I use Guess and Check?

Other heuristic(s) I can use:

### **Q7: Unitary Method (Find Total)**

#### See (What is given?)

Alex  $\rightarrow$  234 m

Roy → 3x the distance ran by Alex

Qn: Total distance ran?

#### Method 1

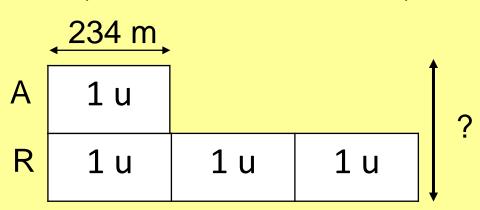
1 u = 234 m

 $3 u = 3 \times 234 m$ 

= 702 m

234 m + 702 m = 936 m

#### Act (What do I need to do?)



#### Method 2

1 u = 234 m

 $4 u = 4 \times 234 m$ 

= 936 m

They ran <u>936 m</u> altogether.

### **Q7: Unitary Method (Find Total)**

Alex ran 234 m. Roy jogged thrice the distance ran by Alex. What is the total distance ran by both Alex and Roy?

```
Act

Method 1

234 m x 3 = 702 m

234 m + 702 m

= 936 m
```

```
Relook (Reflect and Check)

Total \rightarrow 936 m

Roy \rightarrow936 - 234 = 702m

Alex \rightarrow 702m ÷ 3

= 234m \checkmark ok
```

They ran <u>936 m</u> altogether.

### **Q8: Unitary Method**

A bookshop sold 212 pencils and pens in a day. The number of pens sold was thrice the number of pencils sold. How many pencils were sold?

#### See (What is given?)

Pencils and Pens → 212

Pens → 3x as many as Pencils

Qn: ? Pencils were sold

#### Think (What is my plan?)

✓ Can I use Model Drawing?

Can I look for a pattern?

Can I work backwards?

Can I use Guess and Check?

Other heuristic(s) I can use:

### **Q8: Unitary Method**

### See (What is given?)

pencils and pens → 212 pens → 3x as many as pencils

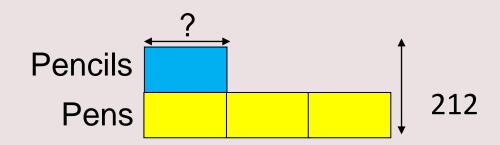
Qn: ? Pencils were sold

#### Method

$$4 u = 212$$

$$1 u = 212 \div 4$$

### Act (What do I need to do?)



53 pencils were sold.

### **Q8: Unitary Method**

A bookshop sold 212 pencils and pens in a day. The <u>number of pens sold</u> was thrice the <u>number of pencils sold</u>. How many <u>pencils were sold</u>?

#### <u>Act</u>

#### Method

$$1 u = 212 \div 4$$

### Relook (Reflect and Check)

$$1 u = 53$$

$$4 u = 4 \times 53$$

С	<b>✓</b>
0	<b>✓</b>
U	<b>√</b>
R	<b>✓</b>
Т	<b>√</b>

# Q9: Model Drawing (Stacking Model)

A pair of shoes and 3 bags cost \$60. The pair of shoes cost twice as much as the bag. Find the cost of the pair of shoes.

#### See (What is given?)

 $1S + 3B \rightarrow $60$ 

 $1S \rightarrow 1B \times 2$ 

Qn: 1S?

#### Think (What is my plan?)

Can I use Part-Whole Model Drawing?

Can I use Comparison Model Drawing?

Can I use Stacking method? ✓

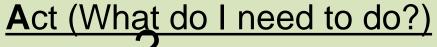
Can I act it out?

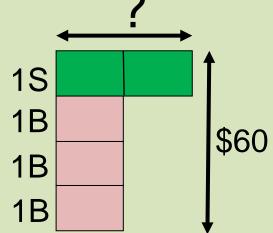
Can I use Guess and Check?

Can I use Working Backwards?

Other heuristic(s) I can use:

# Q9: Model Drawing (Stacking Model)





$$5u = $60$$

$$1u = $60 \div 5 = $12$$

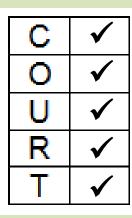
The pair of shoes cost **\$24**.

### Q9: Model Drawing (Stacking Model)

#### Relook (Reflect and Check)

$$$24 + $12 + $12 + $12 = $60$$





# Q10: Model Drawing (Stacking Model)

Mr Koh paid \$1145 for a dining table and 4 chairs.

The table cost \$270 more than each chair.

What was the cost of each chair?

### See (What is given?)

 $1T + 4C \rightarrow $1145$ 

 $1T \rightarrow 1C + $270$ 

Qn: 1C?

#### Think (What is my plan?)

Can I use Part-Whole Model Drawing?

Can I use Comparison Model Drawing?

Can I use Stacking method? ✓

Can I act it out?

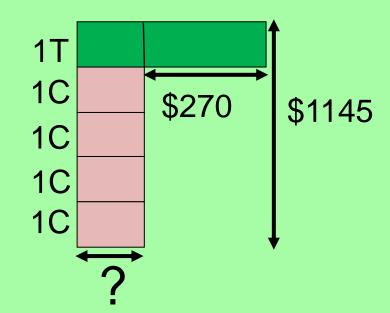
Can I use Guess and Check?

Can I use Working Backwards?

Other heuristic(s) I can use:

## Q10: Model Drawing (Stacking Model)

Act (What do I need to do?)

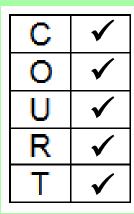


A chair cost **\$175**.

## Q10: Model Drawing (Stacking Model)

#### Relook (Reflect and Check)

Table -> \$175 + \$270  
= \$445  
4 chairs -> 4 x \$175  
= \$700  
Total cost -> \$445 + \$700  
= \$1145 
$$\checkmark$$
 ok



### Q11: Model Drawing (Fraction of a Set)

Annie baked 252 cookies  $\frac{4}{7}$  of the cookies were chocolate cookies and the <u>rest</u> were <u>butter cookies</u>. How many <u>butter cookies</u> did she bake?

### See (What is given?)

Total → 252 cookies

Chocolate  $\rightarrow \frac{4}{7}$  of the cookies

Rest → Butter cookies

Qn: Number of butter cookies?

Think (What is my plan?)

Model drawing ✓

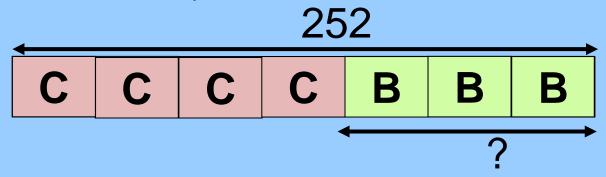
Working backwards

Restate the problem

**Stacking Method** 

# Q11: Model Drawing (Fraction of a Set)

Act (What do I need to do?)



$$7 u = 252$$
  
 $1 u = 252 \div 7 = 36$   
 $3 u = 36 \times 3 = 108$ 

She baked 108 butter cookies.

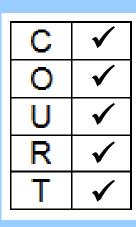
### Q11: Model Drawing (Fraction of a Set)

Relook (Reflect and Check)

$$108 \div 3 = 36$$

$$36 \times 7 = 252$$

√ok



### Q12: Model Drawing (Fraction of a Set)

Mrs Liz had a birthday party.  $\frac{3}{5}$  of the children were girls. There were 36 boys at the party. How many children were there altogether?

### See (What is given?)

Girls  $\rightarrow \frac{3}{5}$  of the children

Boys  $\rightarrow$  36

Qn: total number of children?

Think (What is my plan?)

Model drawing ✓

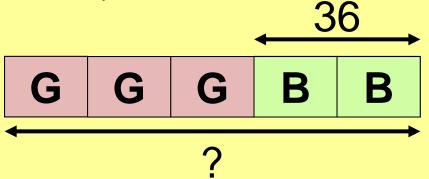
Working backwards

Restate the problem

**Stacking Method** 

## Q12: Model Drawing (Fraction of a Set)

Act (What do I need to do?)



$$2 u = 36$$
  
 $1 u = 36 \div 2 = 18$   
 $5 u = 18 \times 5 = 90$ 

There were **90** children altogether.

# Q12: Model Drawing (Fraction of a Set)

Relook (Reflect and Check)

$$90 \div 5 = 18$$

$$18 \times 2 = 36$$

√ok



## Q13: Model Drawing (Before and After) – Make Equal

Samy has 250 erasers and Darryl has 64 erasers. How many erasers must Samy give to Darryl so that both have the same number of erasers?

### See (What is given?)

 $S \rightarrow 250$ 

 $D \rightarrow 64$ 

S give ? to D so that S = D

#### Think (What is my plan?)

✓ Can I use Model Drawing?

Can I look for a pattern?

Can I work backwards?

Can I use Guess and Check

Other heuristic(s) I can use:

# Q13: Model Drawing (Before and After) – Make Equal

### See (What is given?)

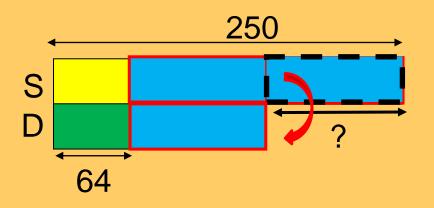
 $S \rightarrow 250$ 

 $D \rightarrow 64$ 

S give ? to D so that

$$S = D$$

#### Act (What do I need to do?)



Samy must give Darryl **93** erasers.

# Q13: Model Drawing (Before and After) – Make Equal

Samy has 250 erasers and Darryl has 64 erasers. How many erasers must Samy give to Darryl so that both have the same number of erasers?

**A**ct

$$186 \div 2 = 93$$

Relook (Reflect and Check)

$$314 \div 2 = 157$$

$$250 - 93 = 157$$

Samy must give Darryl **93** erasers.

С	<b>√</b>
0	<b>\</b>
C	<b>√</b>
R	<b>✓</b>
Т	<b>√</b>

### **Q14: Restate the Problem**

The total cost of 1 box of mangoes and 1 box of papayas is \$32. The total cost of 1 box of mangoes and 3 boxes of papayas is \$56. What is the cost of 3 boxes of papayas?

### See (What is given?)

 $1 M + 1P \rightarrow $32$ 

 $1 M + 3P \rightarrow $56$ 

**Qns: 3P?** 

Think (What is my plan?)
Model drawing
Working backwards
Restate the problem ✓
Stacking Method

### **Q14: Restate the Problem**

The total cost of 1 box of mangoes and 1 box of papayas is \$32. The total cost of 1 box of mangoes and 3 boxes of papayas is \$56. What is the cost of 3 boxes of papayas?

#### Act (What do I need to do?)

$$1 M + 1P \rightarrow $32$$

$$1 M + 3P \rightarrow $56$$

$$2P \rightarrow $56 - $32 = $24$$

$$1P \rightarrow $24 \div 2 = $12$$

$$3P \rightarrow $12 \times 3 = $36$$

The cost of 3 boxes of papayas cost **\$36**.

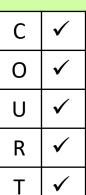
### **Q14: Restate the Problem**

The total cost of 1 box of mangoes and 1 box of papayas is \$32. The total cost of 1 box of mangoes and 3 boxes of papayas is \$56. What is the cost of 3 boxes of papayas?

#### Relook (Reflect and Check)

√ok

The cost of 3 boxes of papayas cost **\$36**.







### **Other Matters**

- 1) Kindly scan the QR code to provide your feedback for the workshop.
  - https://forms.moe.edu.sg/forms/JqyEQJ
- 2) Slides shared will be uploaded onto the school website next week.





# Thank you for attending our presentation

