

COMPUTER SCIENCE TRIPOS Part IA – 2016 – Paper 2

1 Digital Electronics (IJW)

- (a) Consider a 4-input Boolean function that outputs a binary 1 whenever an odd number of its inputs are binary 1.

(i) Using Boolean logic or otherwise, show how the above function can be implemented using only 2-input XOR gates. [4 marks]

(ii) Show how the above function may alternatively be implemented using one 4-input decoder, and a minimum number of 4-input NOR and 4-input NAND gates. [3 marks]

- (b) Consider the following Boolean expression

$$F = \overline{B}.\overline{C} + \overline{A}.B.C + A.C.\overline{D}$$

(i) Show that F can be represented by the following Product of Sums (POS) form

$$F = (\overline{B} + C).(\overline{A} + \overline{C} + \overline{D}).(A + B + \overline{C})$$

[3 marks]

(ii) Show how F can be implemented in a 2-level form using OR gates followed by an AND gate. Remember to indicate any NOT gates required, since only uncomplemented input variables are available. [2 marks]

- (c) Consider your implementation in part (b)(ii).

(i) Assume that the gates have finite propagation delay. Describe in detail what happens at the output F when the inputs $\{A, B, C, D\}$ change from $\{1, 1, 0, 1\}$ to $\{1, 1, 1, 1\}$. [4 marks]

(ii) Using a Karnaugh map or otherwise, determine the other single input variable change that will give rise to a similar problem to that observed in part (c)(i). [2 marks]

(iii) Using a Karnaugh map or otherwise, determine a modified POS expression for F that will eliminate the problems observed in parts (c)(i) and (c)(ii). [2 marks]