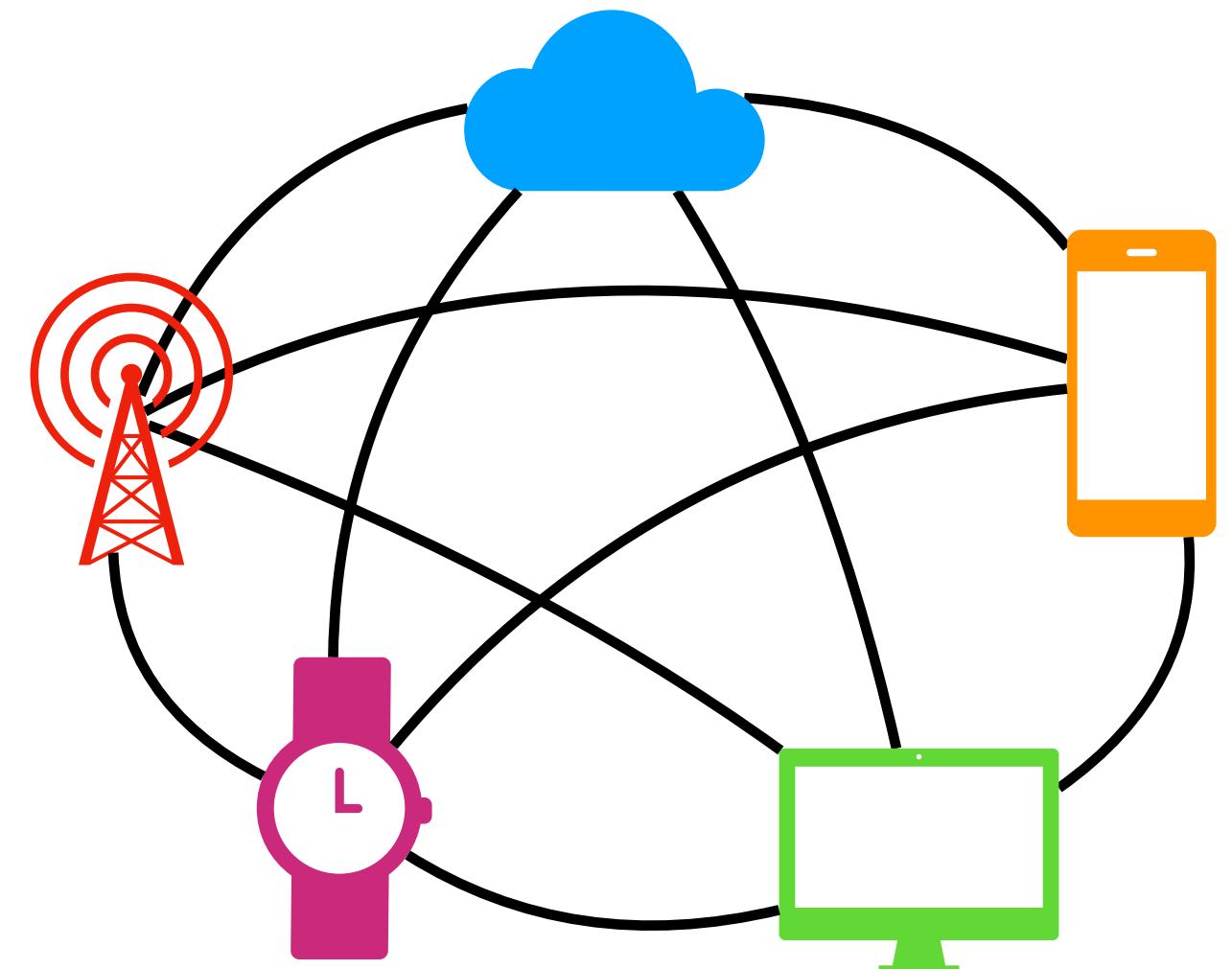
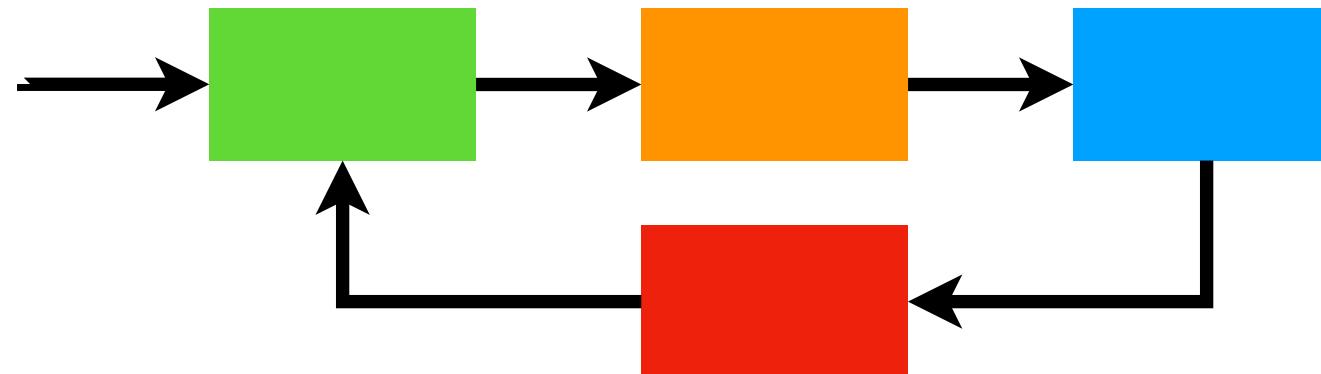


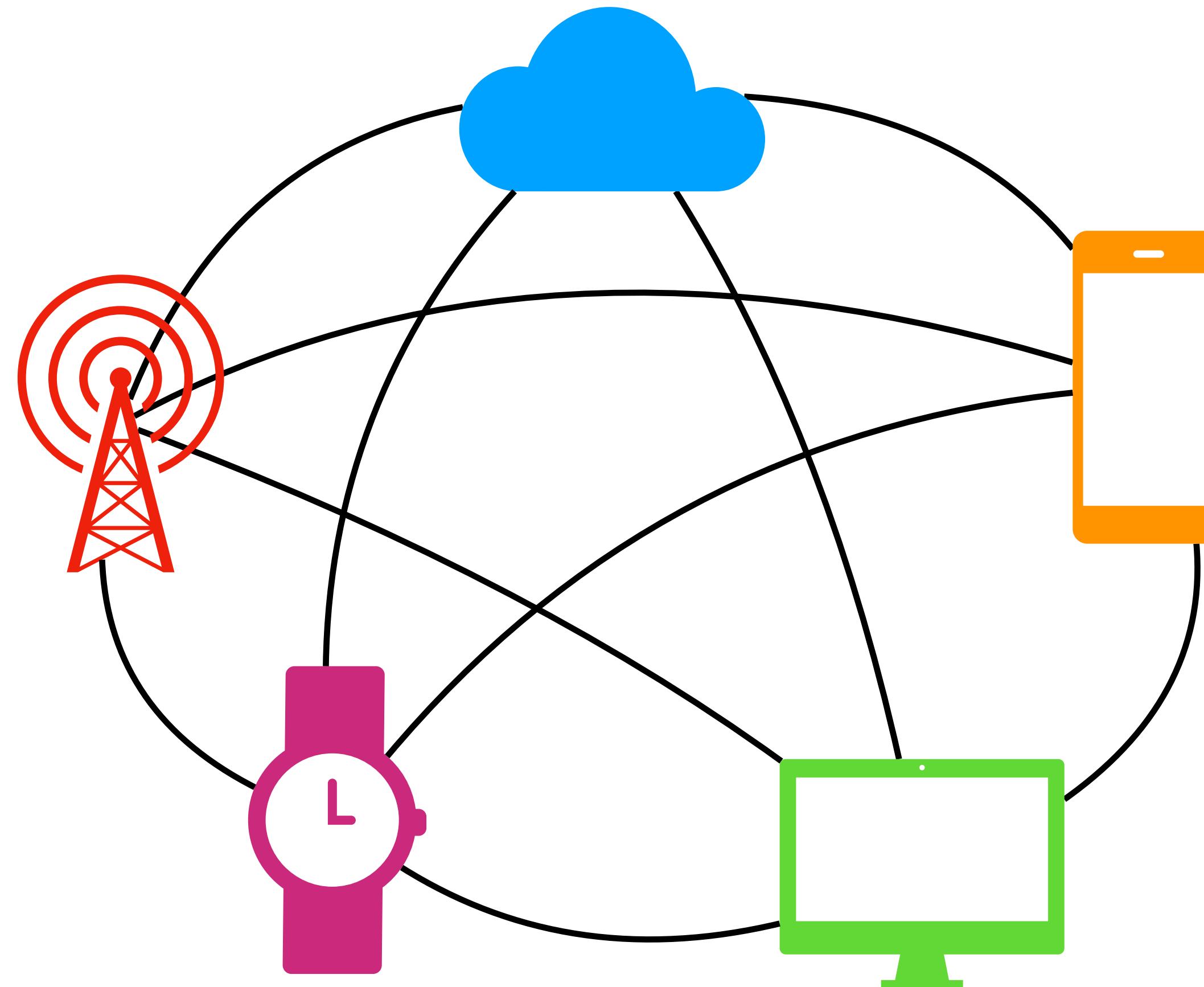


Packet Priority Assignment for Wireless Control Systems of Multiple Physical Systems

Wenchen Wang, Daniel Mosse, and Alessandro V. Papadopoulos

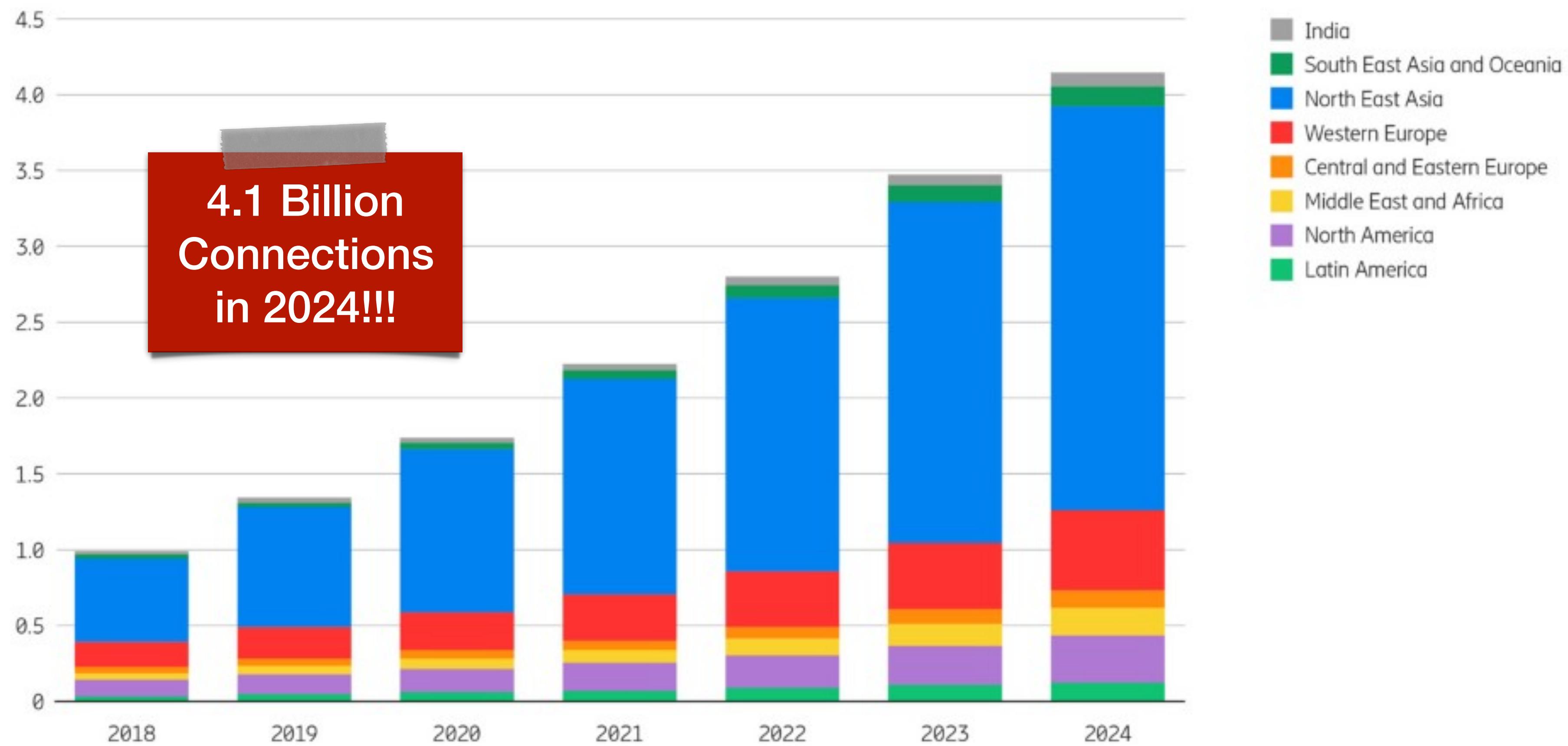


Interconnected World Made of Computing Systems



IoT Connections

Cellular IoT connections per region (billion)





Whoops, something went wrong...

Netflix Streaming Error

We're having trouble playing this title right now. Please try again later or select a different title.

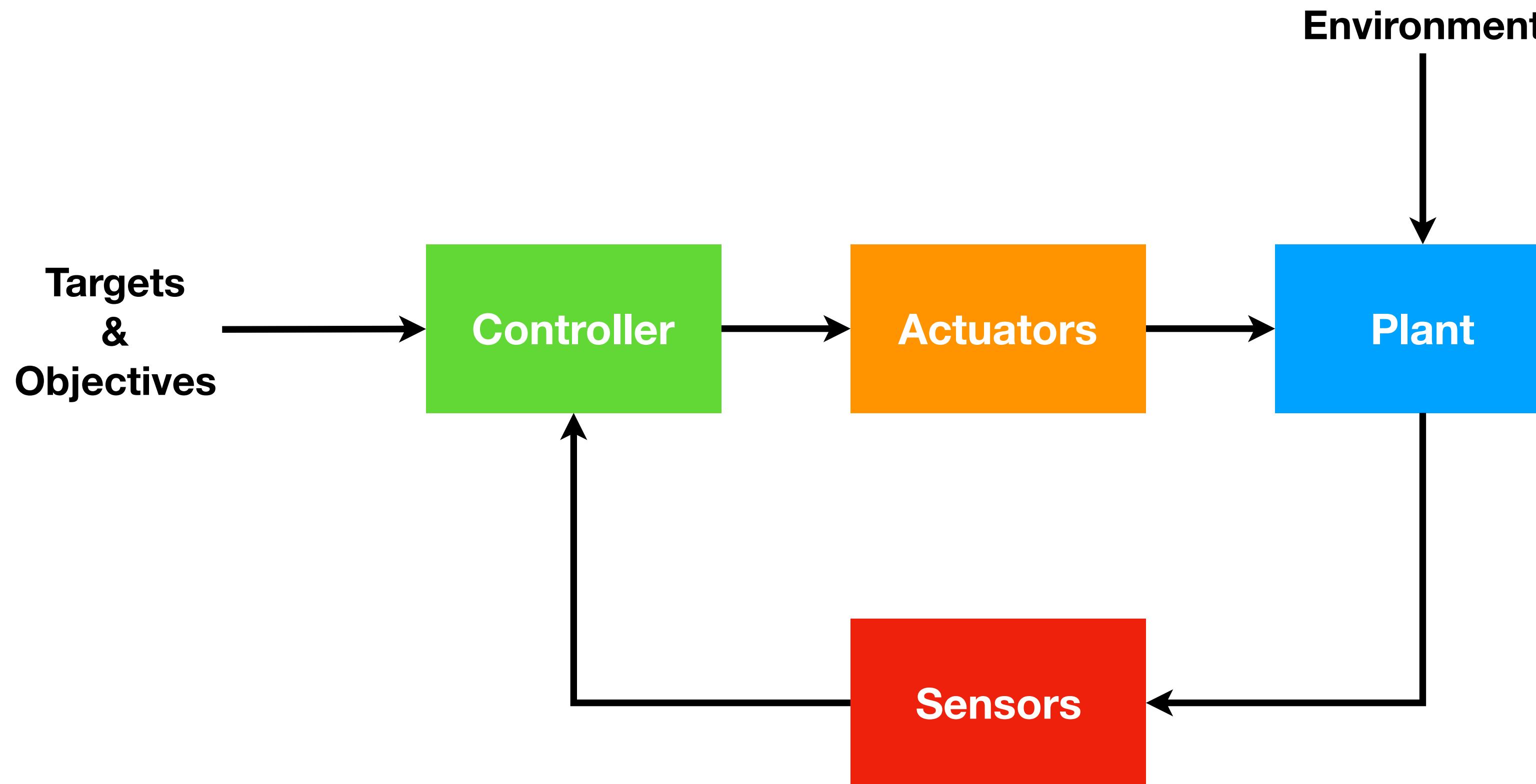


Photo-illustration: iStockphoto

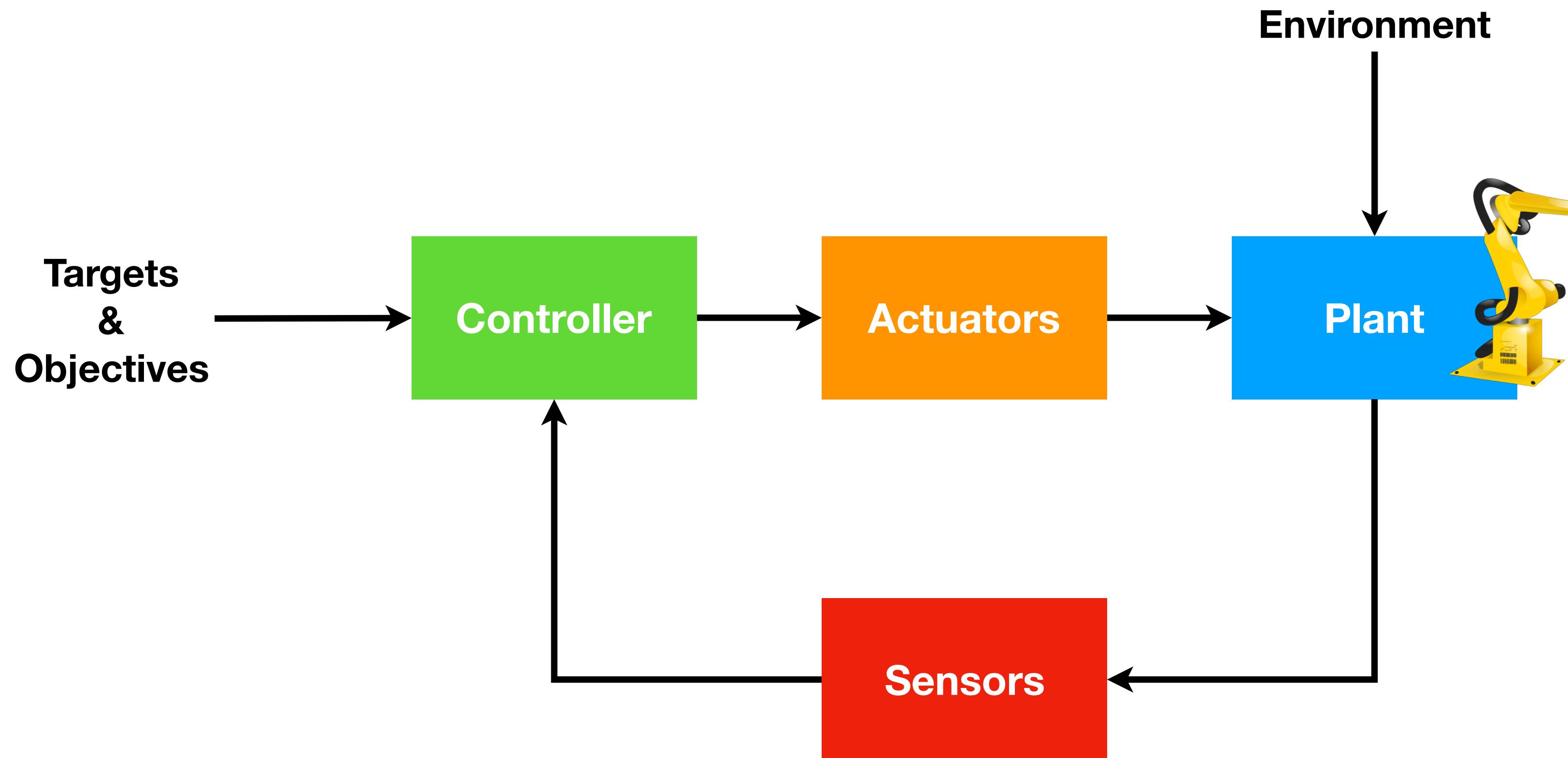


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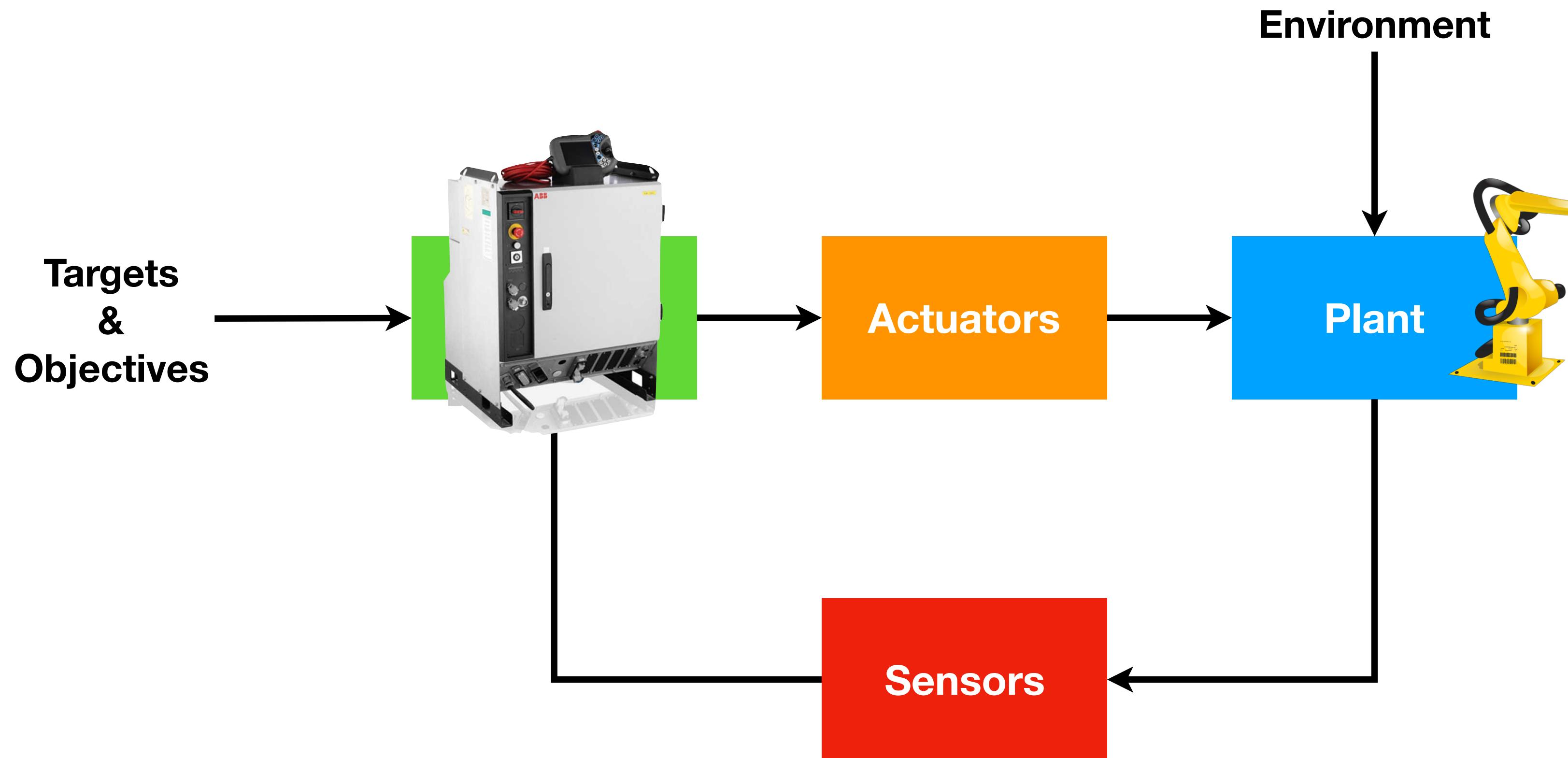
Wired Control System



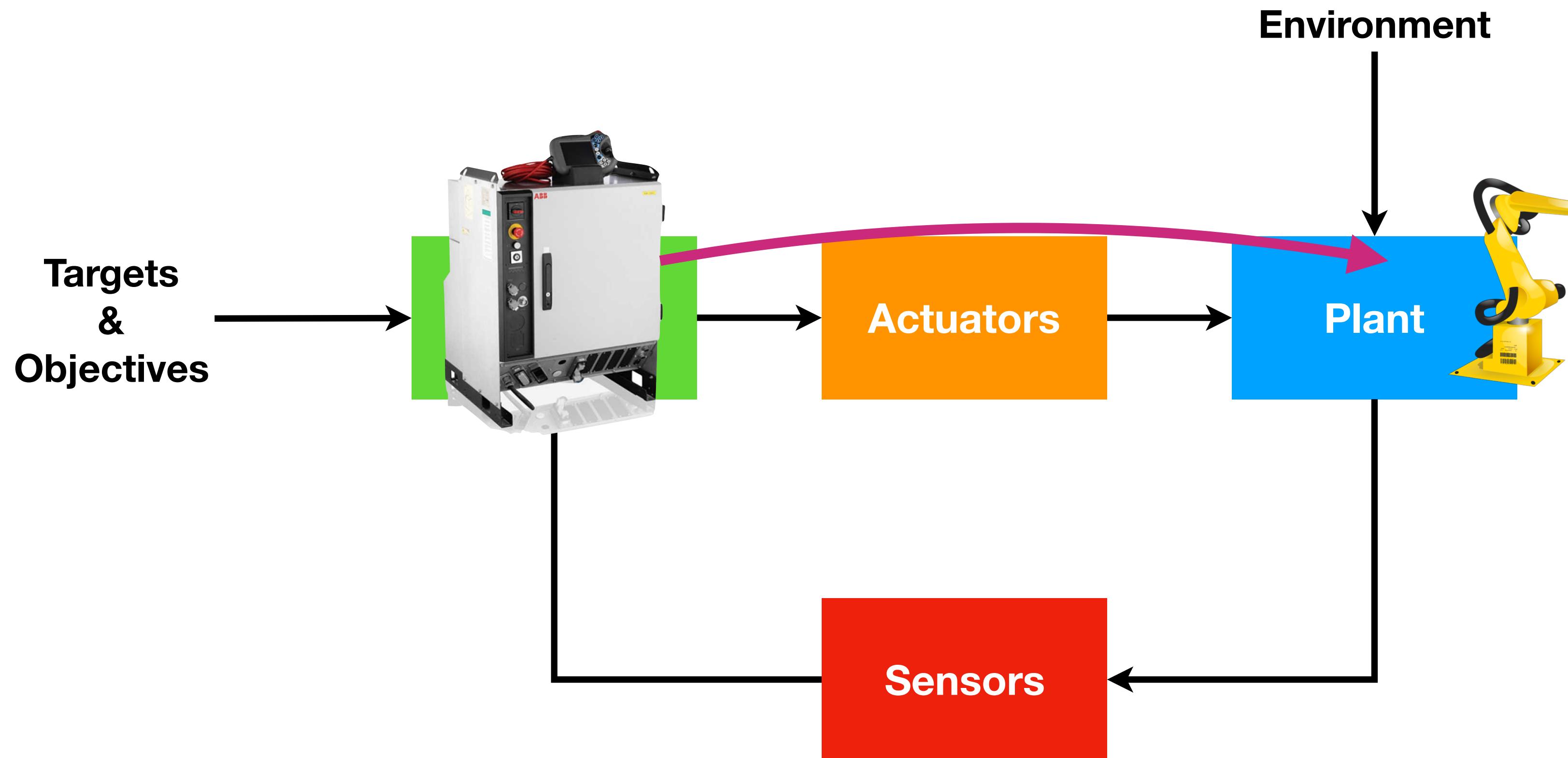
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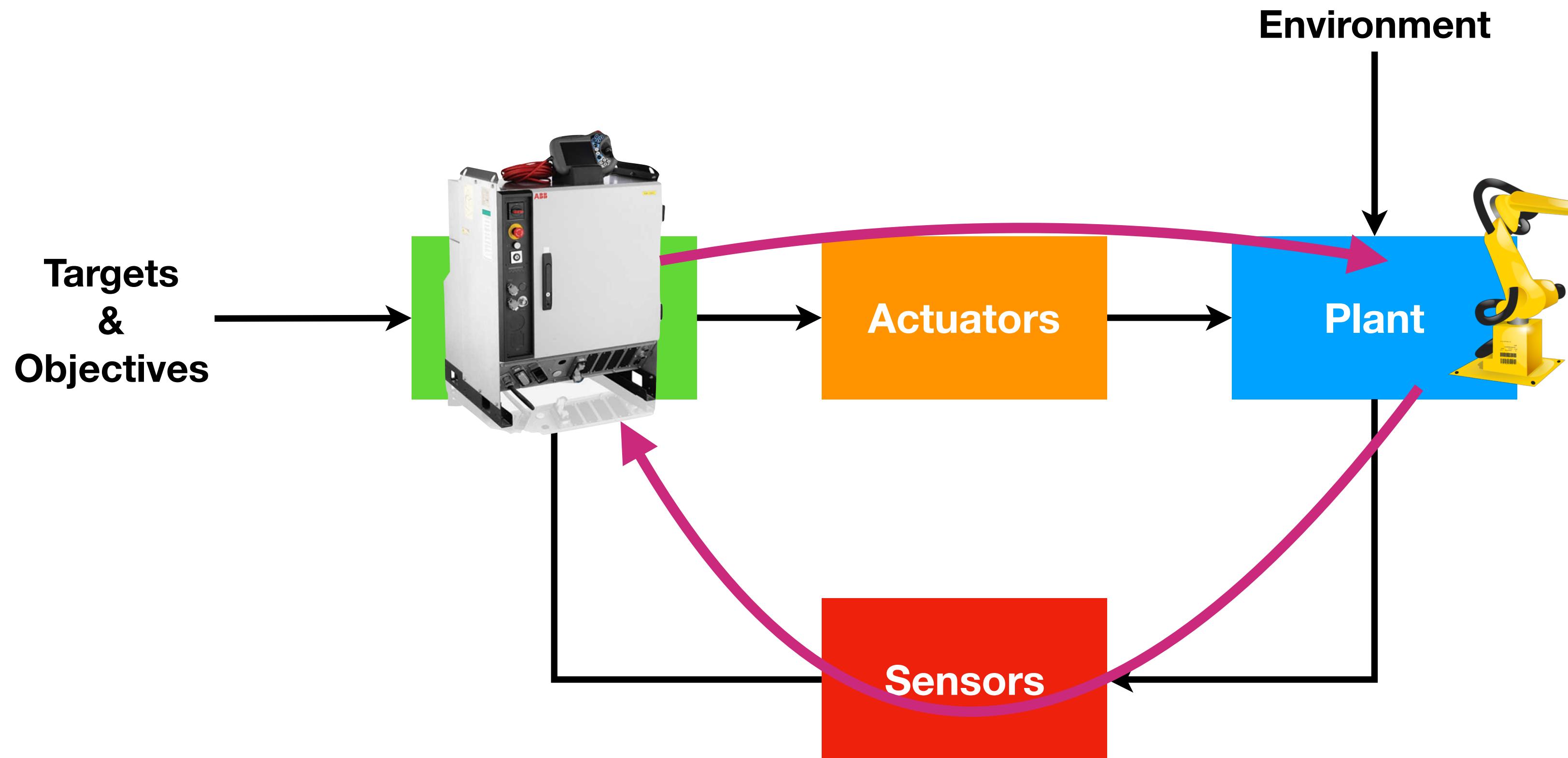
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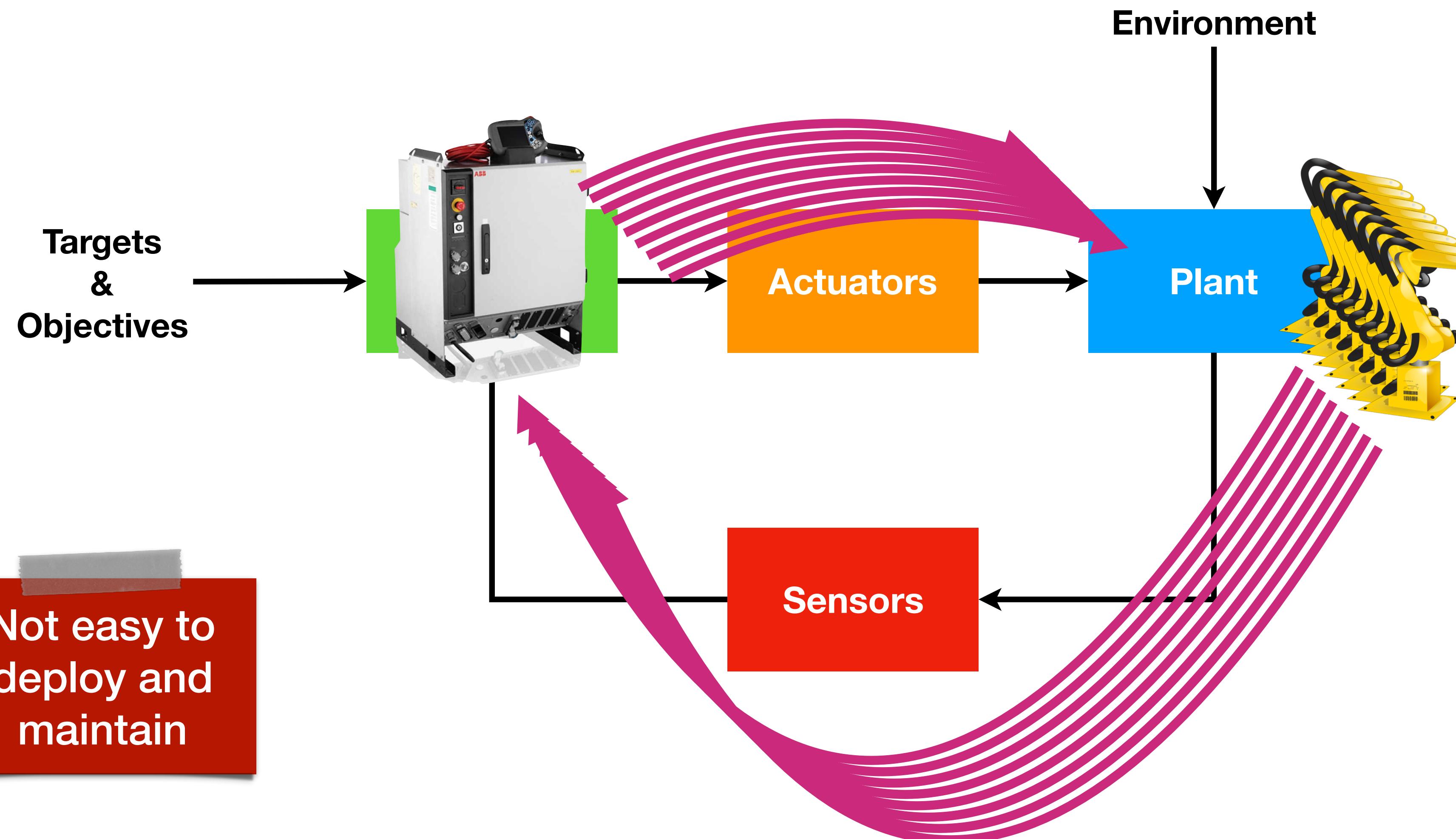
Wired Control System



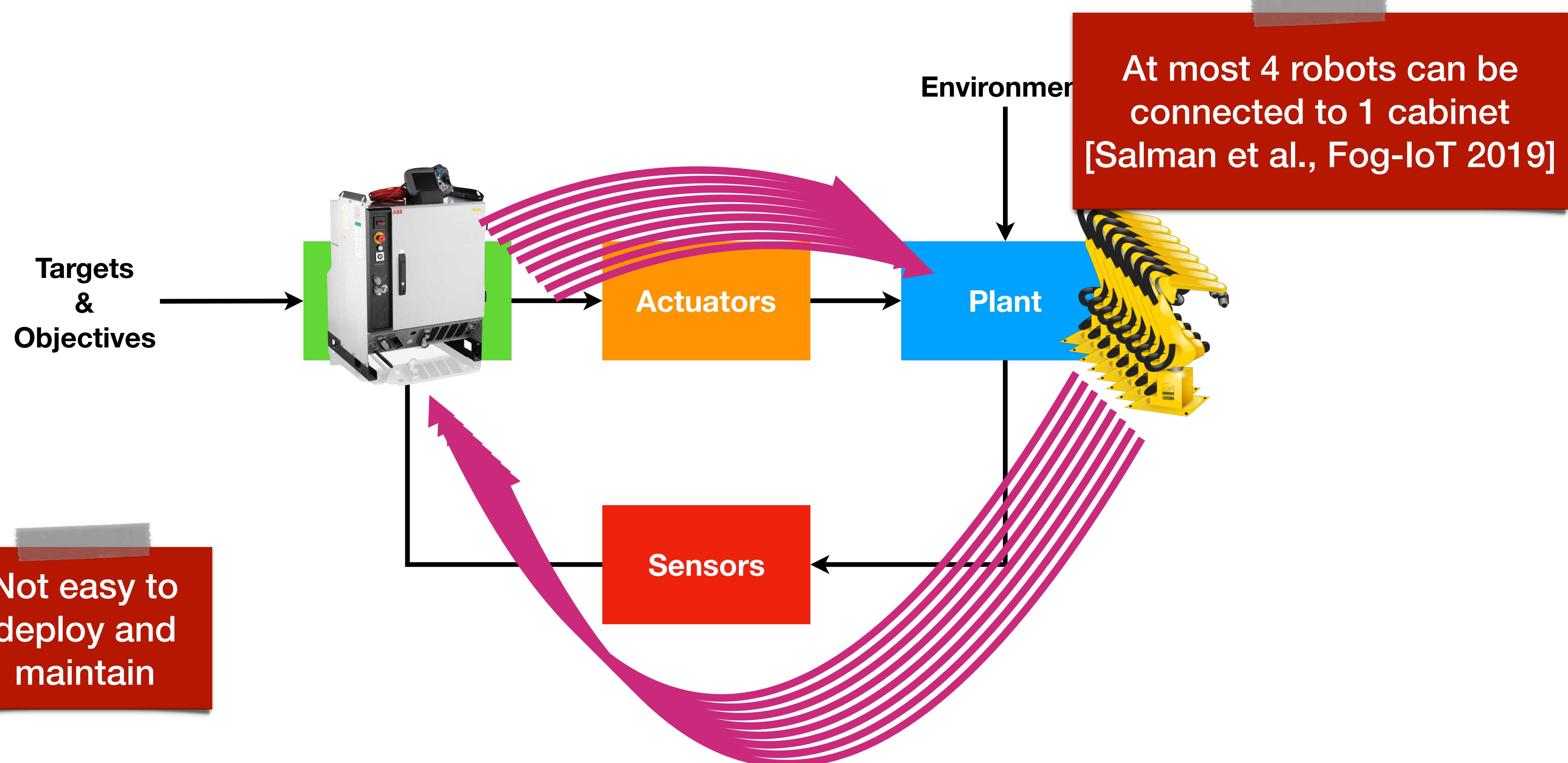
Wired Control System



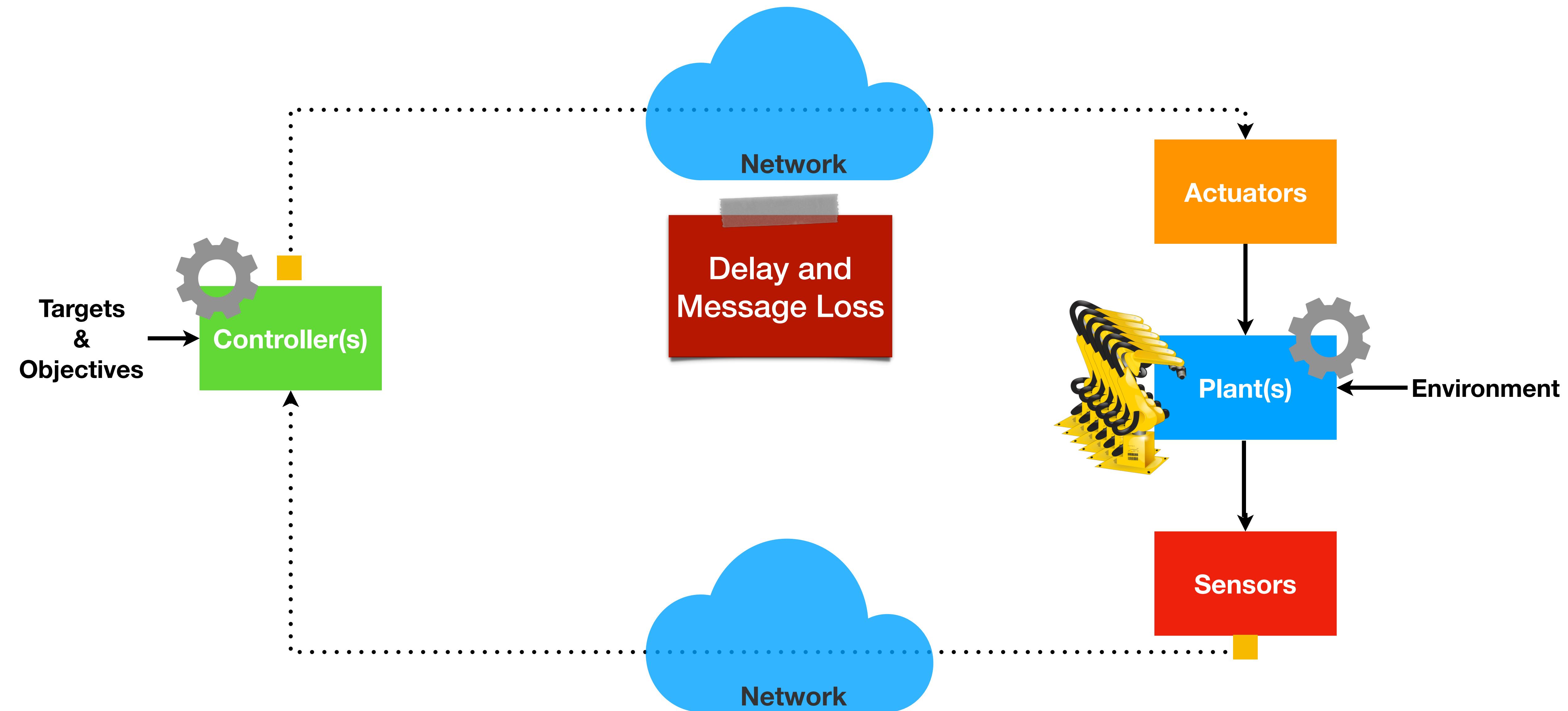
Wired Control System



Wired Control System



Wireless Control System (WCS)



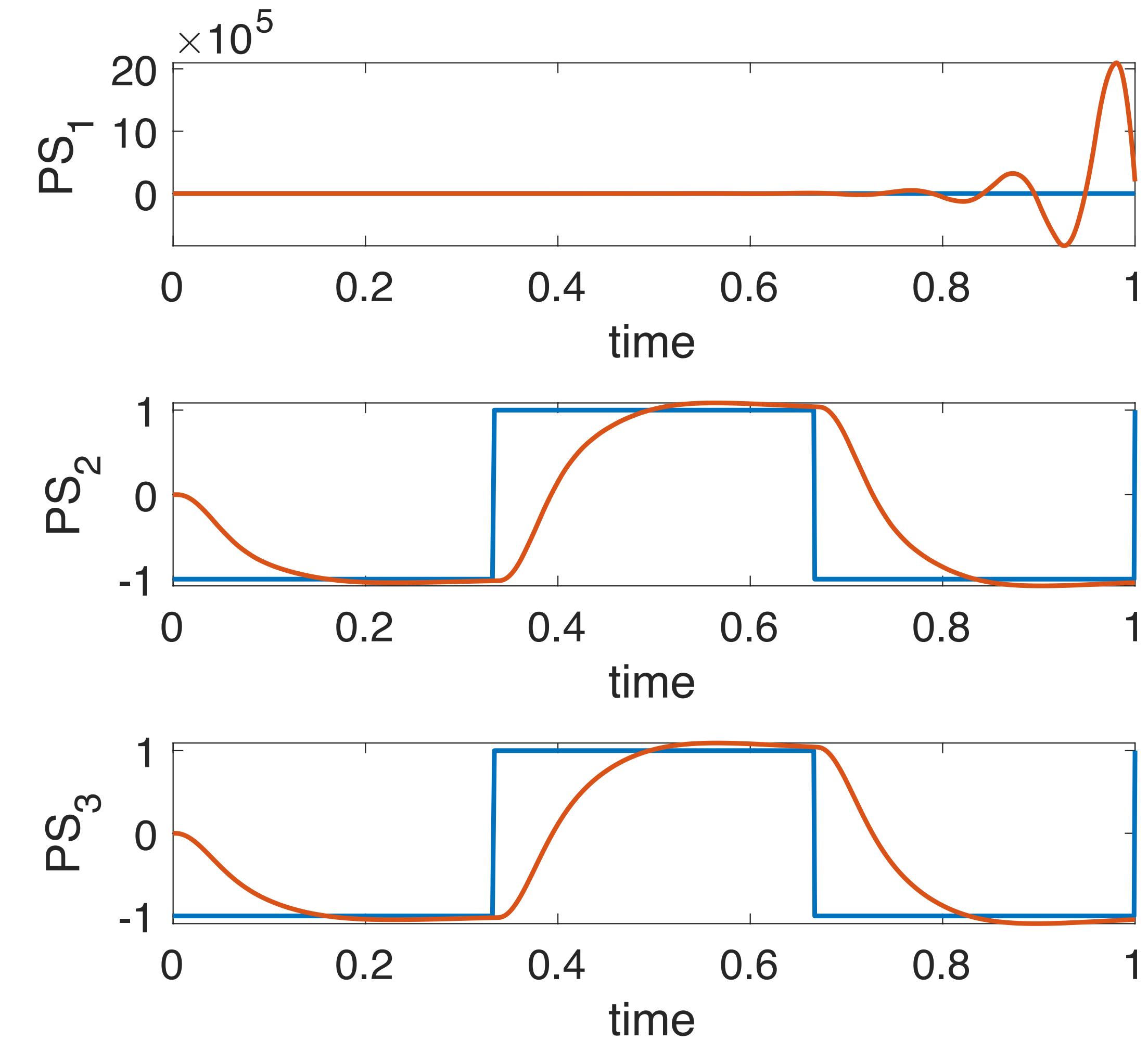
Major Challenges of WCS

- **Instability**

- ▶ When the physical system is unstable, the plant or the device can be damaged and leads to serious safety issues and financial loss.

- **Performance Degradation**

- ▶ Induced additional error
 - Network-induced error



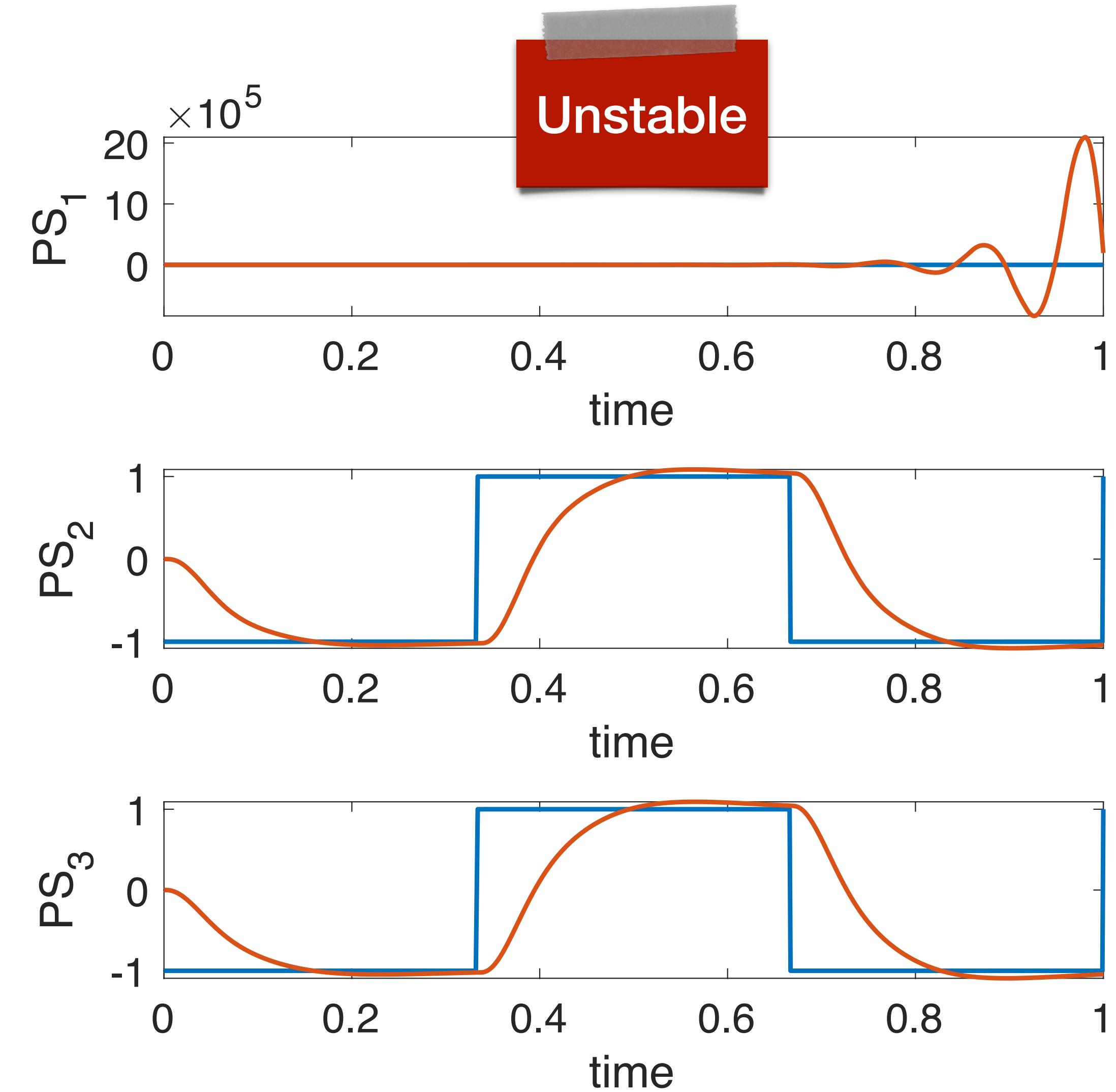
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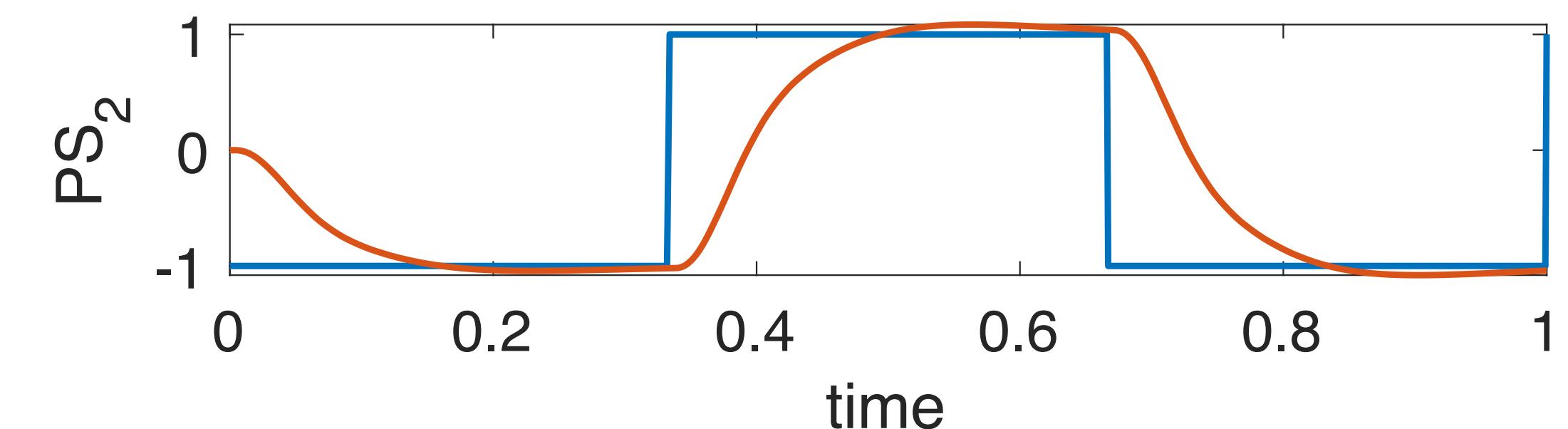
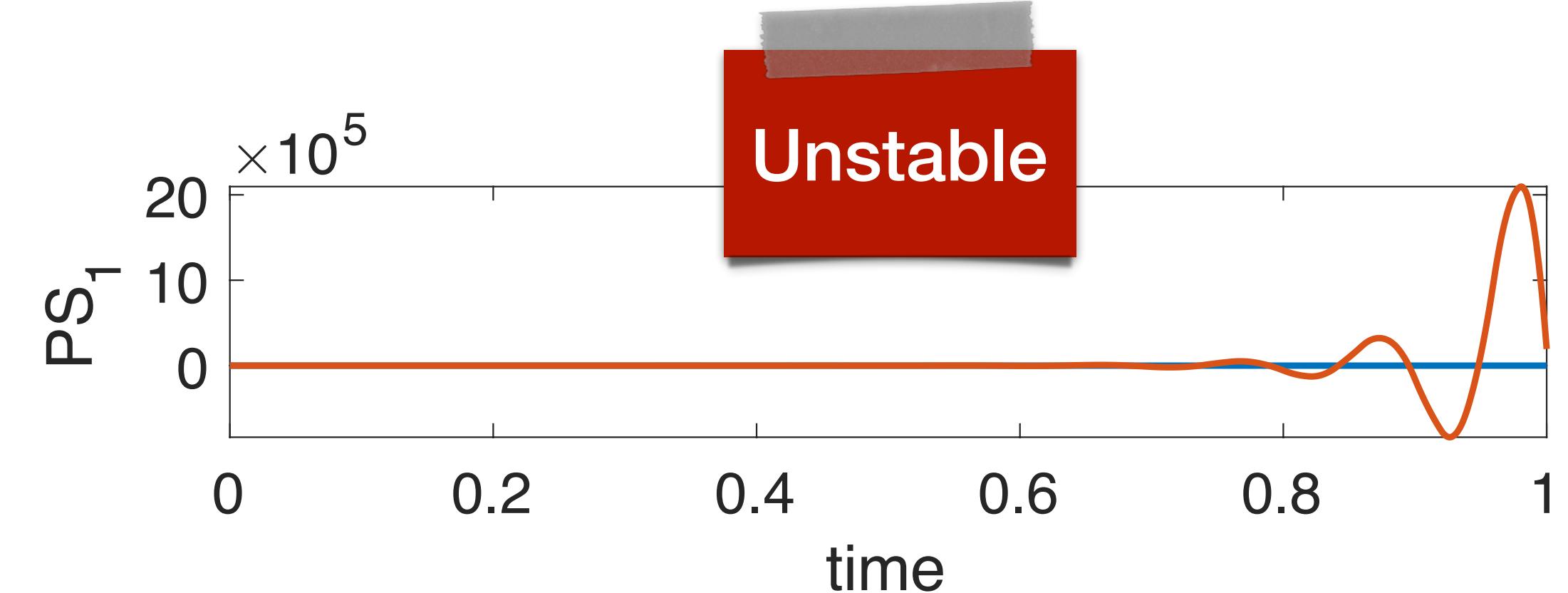
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Major Challenges of WCS

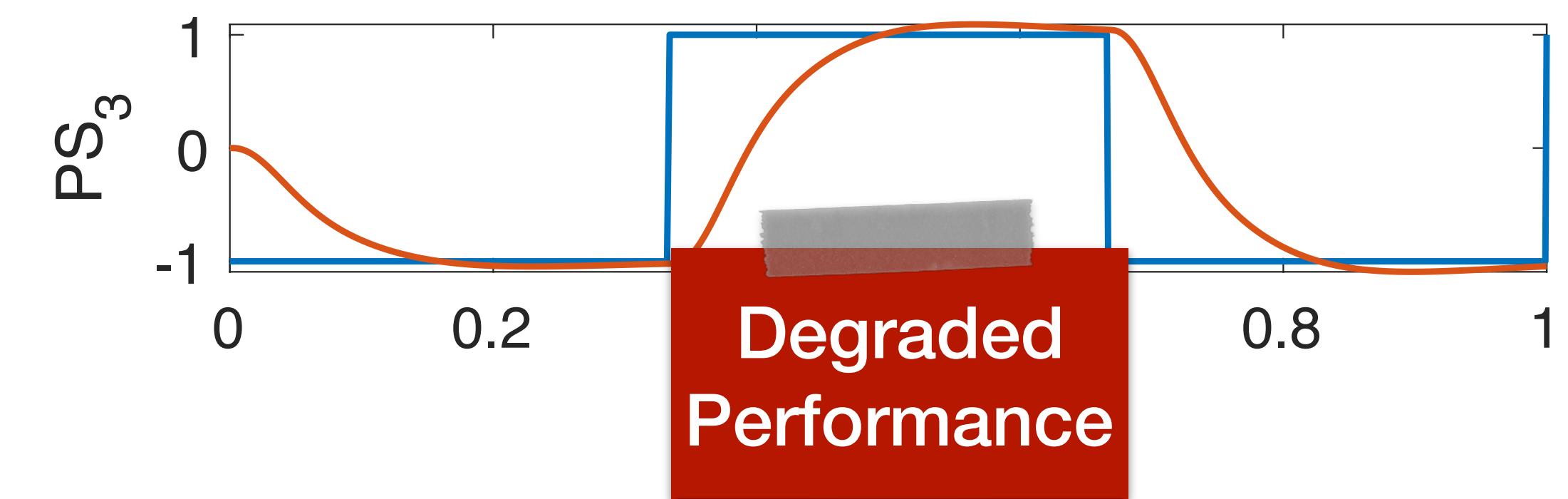
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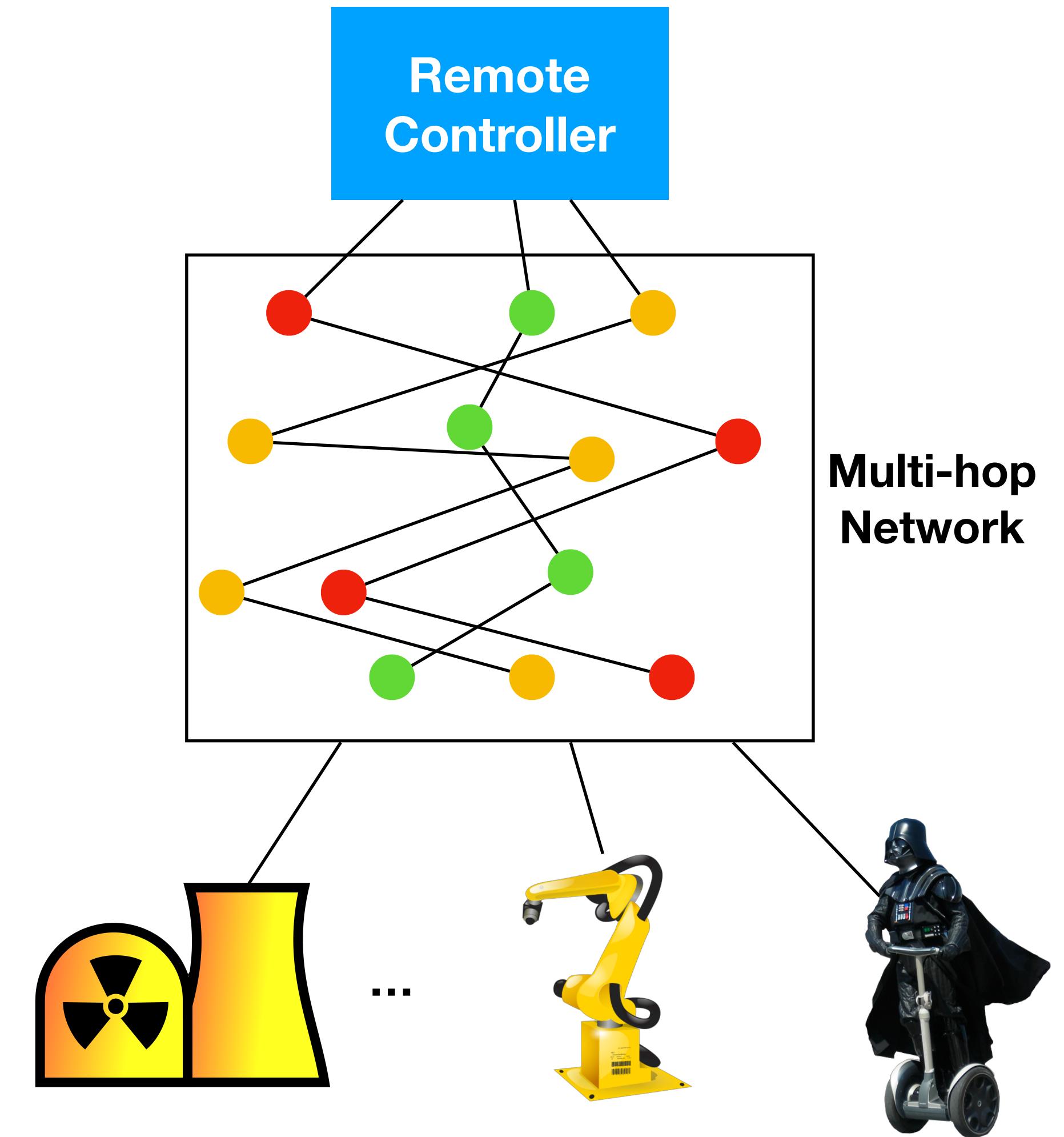
- **Performance Degradation**

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Problem Formulation

- Shared multi-hop network
 - ▶ Different paths p_1, p_2, \dots, p_m
 - ▶ Each path with delay D_j
 - ▶ TDMA fixed topology
 - ▶ Time-varying delivery ratio dr_j



N Physical Systems (PSs)

Different Requirements, Shared Network



LO-Critical
HI-Frequency

Demand

time



HI-Critical
HI-Frequency

Demand

time



HI-Critical
LO-Frequency

Demand

time

Different Requirements, Shared Network



LO-Critical
HI-Frequency

Demand

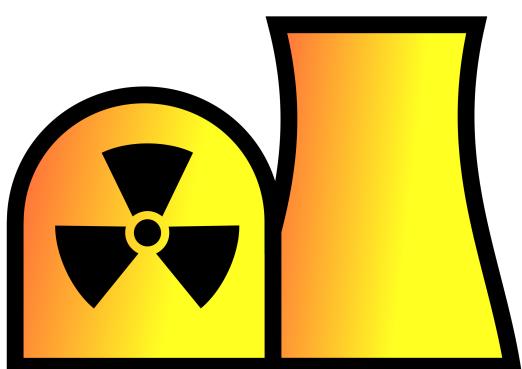
time



HI-Critical
HI-Frequency

Demand

time



HI-Critical
LO-Frequency

Demand

time

Different Requirements, Shared Network



LO-Critical
HI-Frequency

Demand

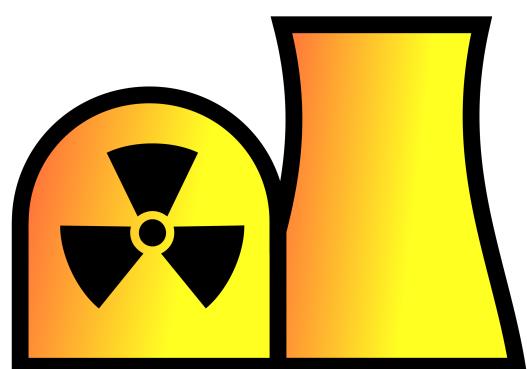
time



HI-Critical
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time

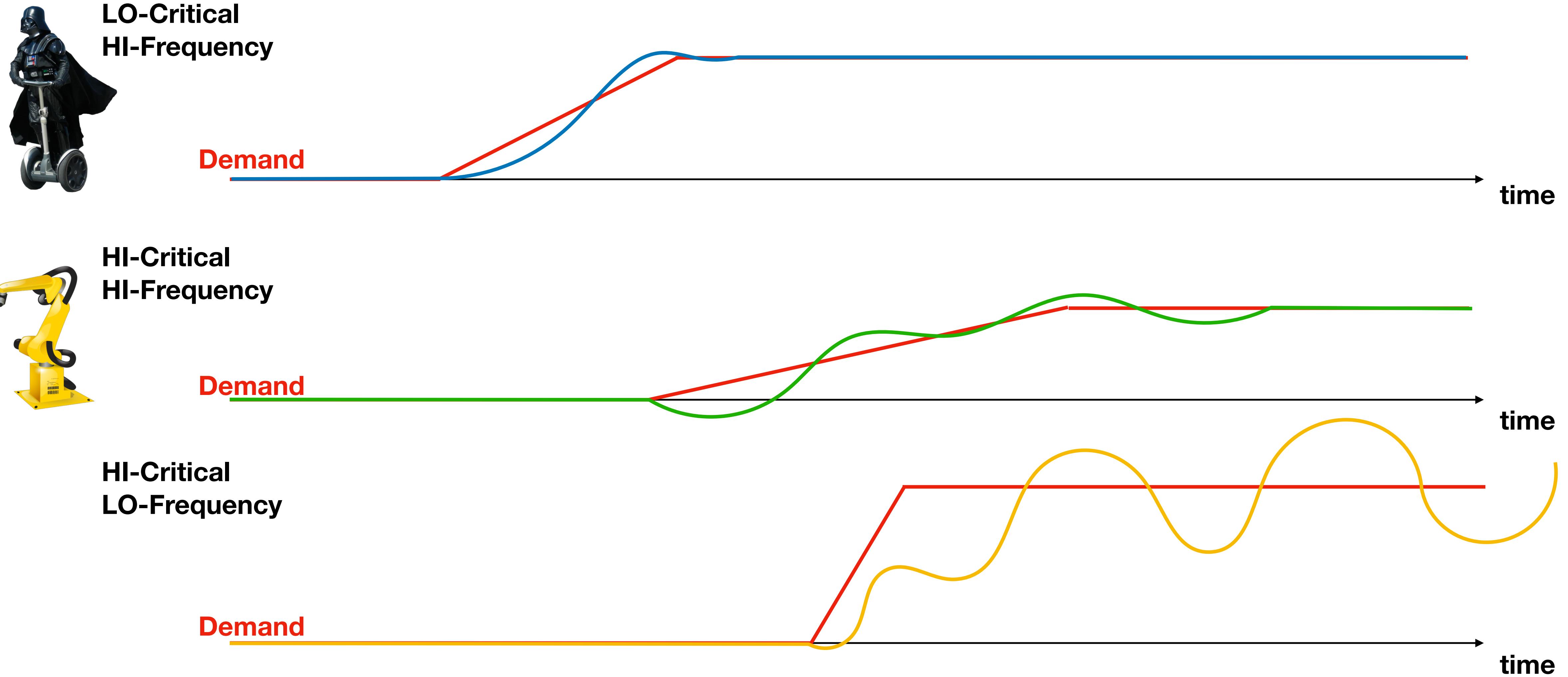


HI-Critical
LO-Frequency

Demand

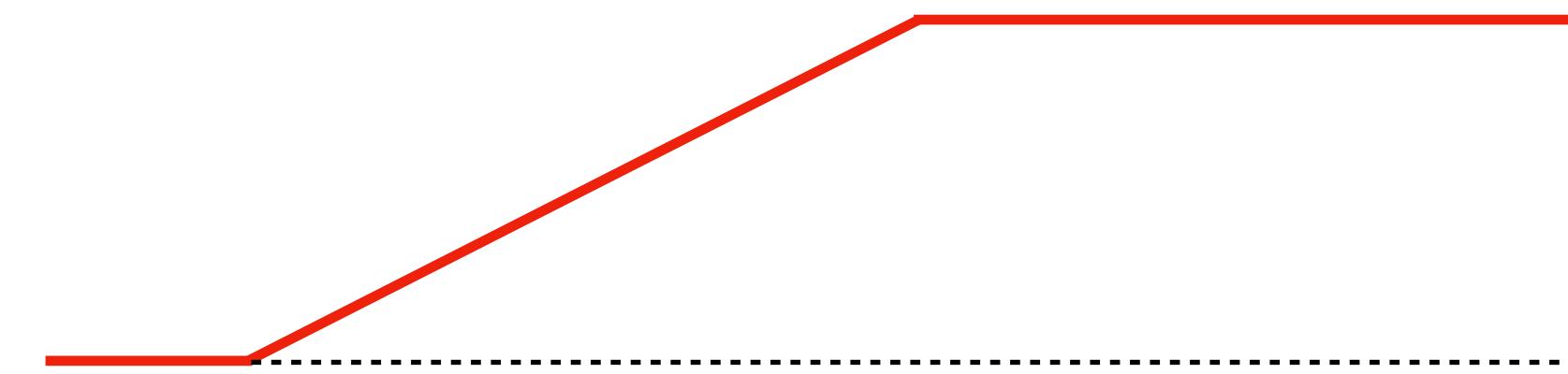
time

Different Requirements, Shared Network



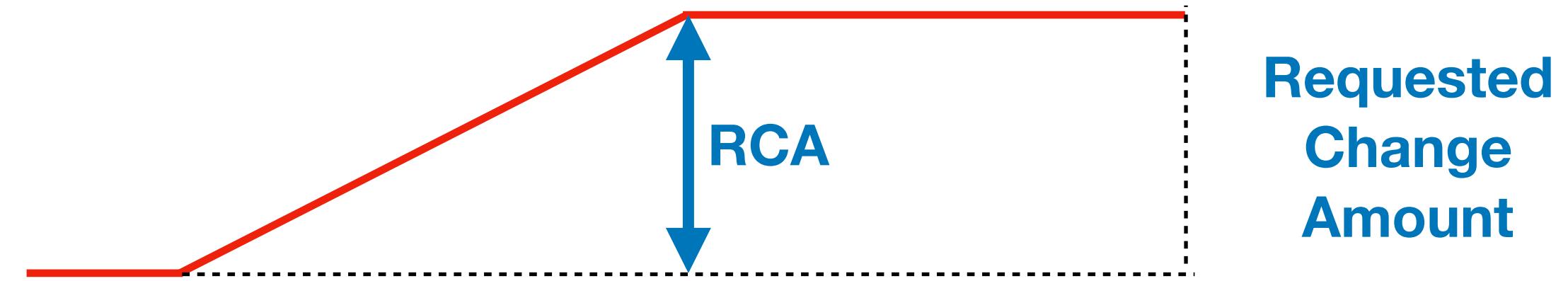
Problem Formulation

- The control is more or less difficult based on
 - ▶ **Setpoint (or reference) tracking**
 - ▶ **Nonlinearity** of the controlled system
 - ▶ **Reliability** of the communication path



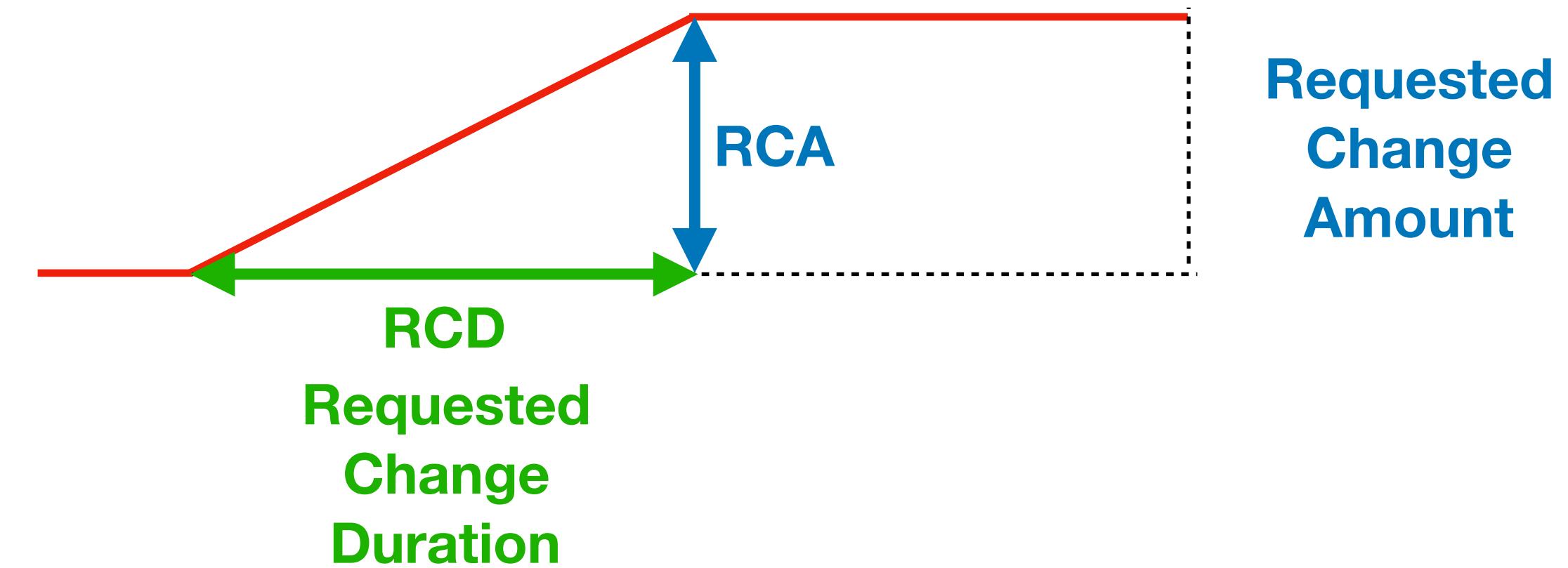
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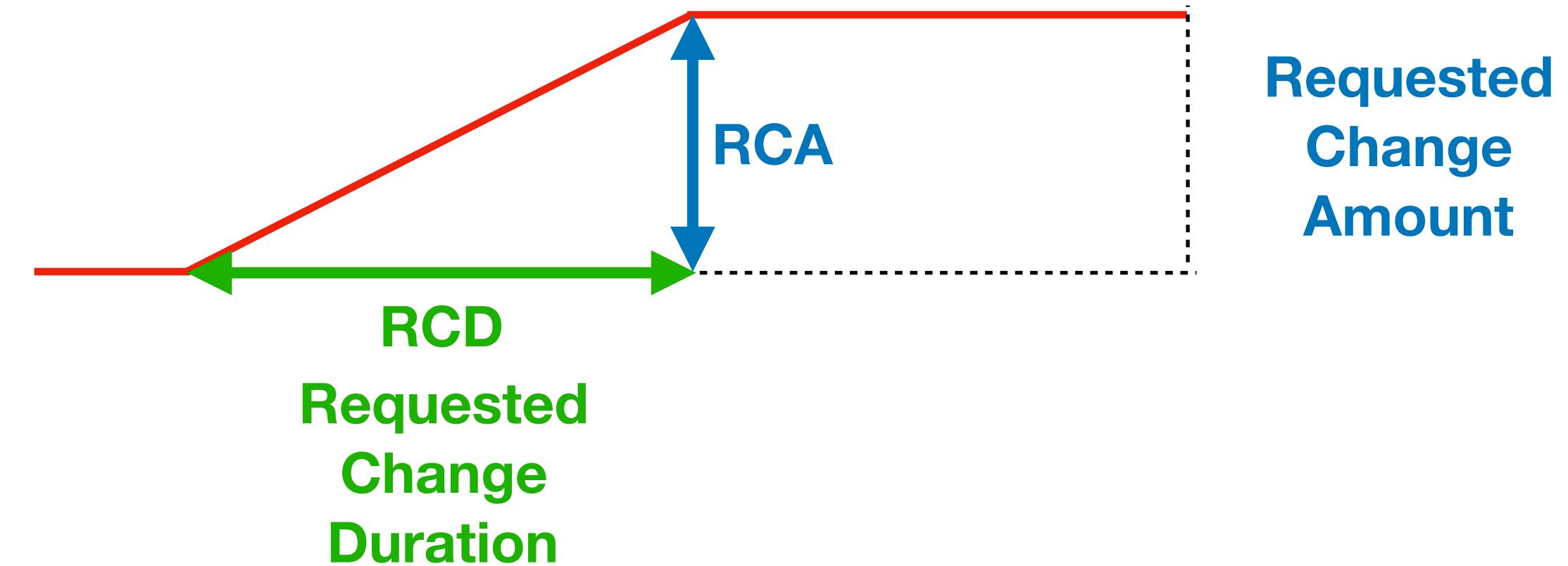
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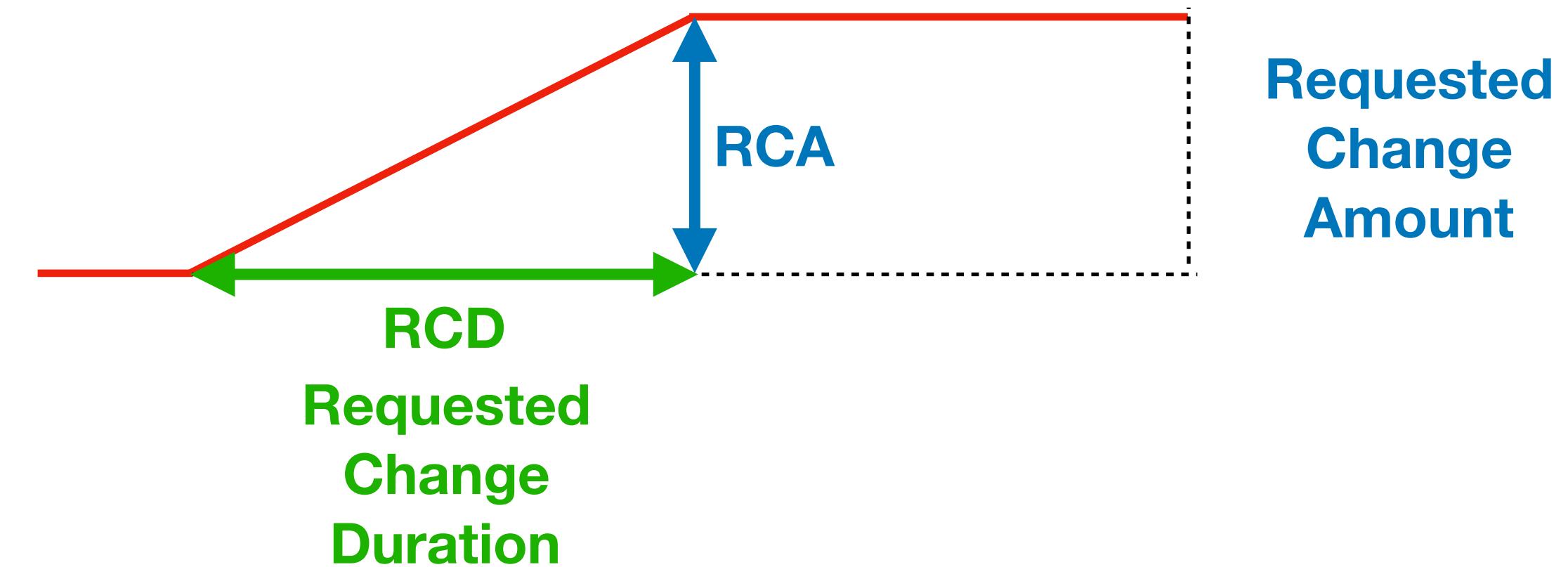
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 - ▶ Control **performance degradation**
 - ▶ Induced by the **wireless realization**
 - ▶ Without redesigning the control system



Problem Formulation

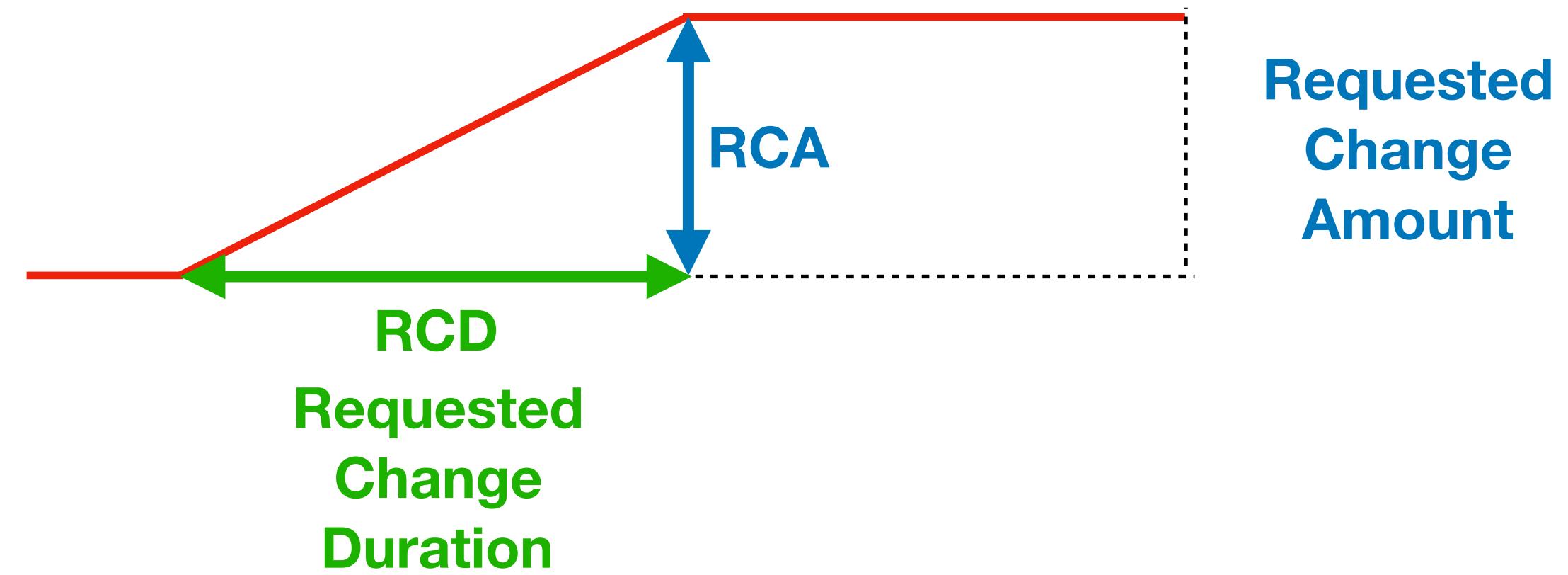
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$$RMSE_i = \sqrt{\frac{1}{T_{trans}} \sum_{t=0}^{T_{trans}} \|y_i^W(t) - y_i^{WL}(t)\|^2}$$

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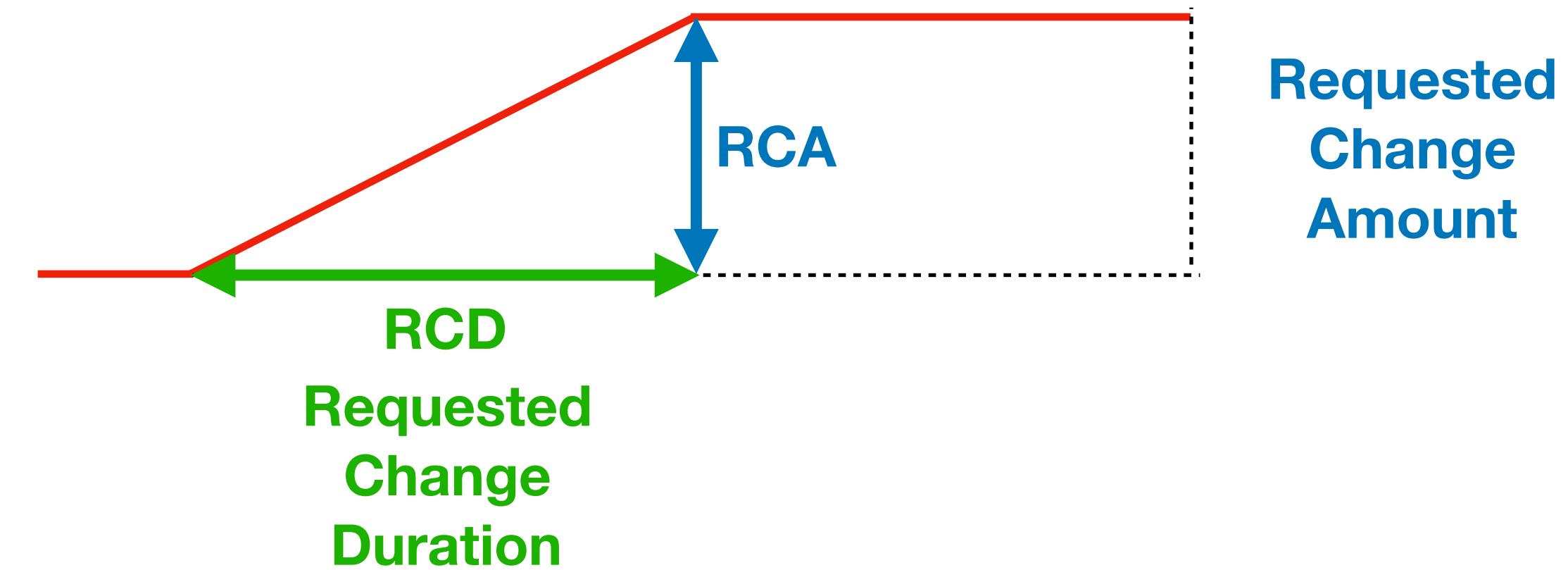


$$RMSE_i = \sqrt{\frac{1}{T_{trans}} \sum_{t=0}^{T_{trans}} \|y_i^W(t) - y_i^{WL}(t)\|^2}$$

A blue arrow points from the text 'Wired' to the term $y_i^{WL}(t)$ in the equation.

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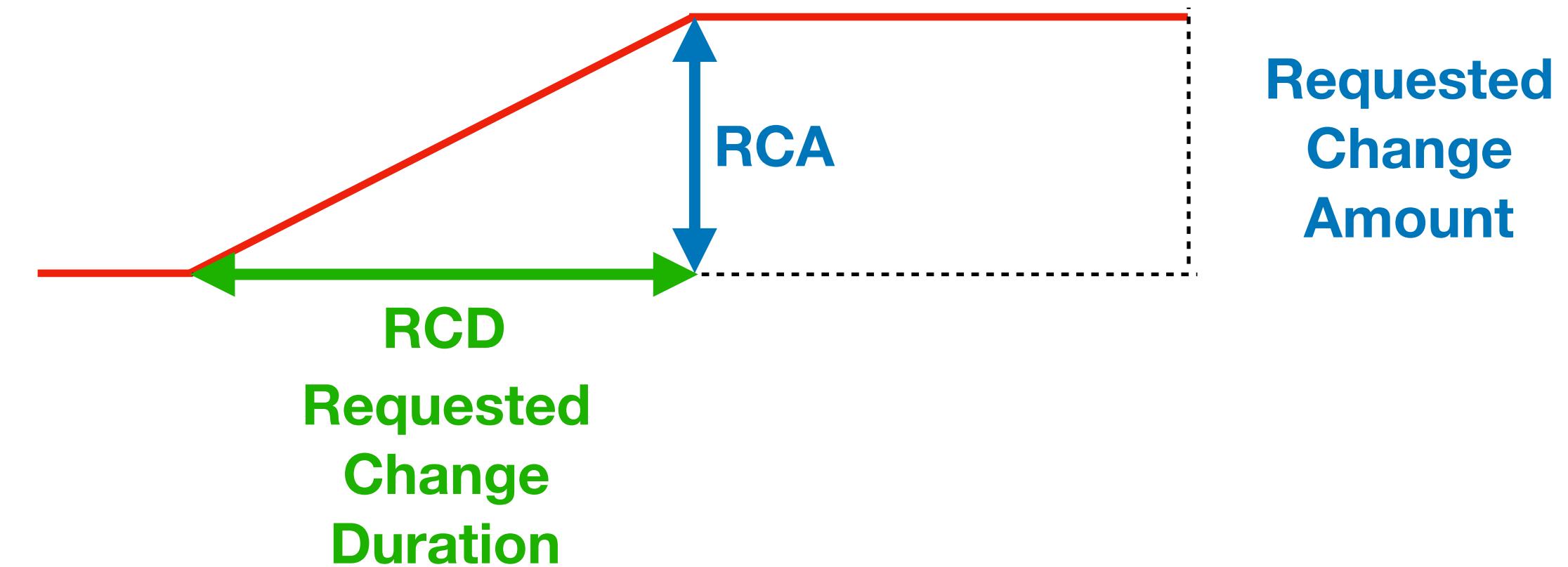


$$RMSE_i = \sqrt{\frac{1}{T_{trans}} \sum_{t=0}^{T_{trans}} \|y_i^W(t) - y_i^{WL}(t)\|^2}$$

The equation represents the Root Mean Square Error (RMSE) for the i -th output. It calculates the average squared difference between the **Wired** signal ($y_i^W(t)$) and the **Wireless** signal ($y_i^{WL}(t)$) over T_{trans} transmission instances. The terms $y_i^W(t)$ and $y_i^{WL}(t)$ are highlighted with blue and pink boxes respectively, with arrows pointing to them from the labels 'Wired' and 'Wireless' above the timeline.

Problem Formulation

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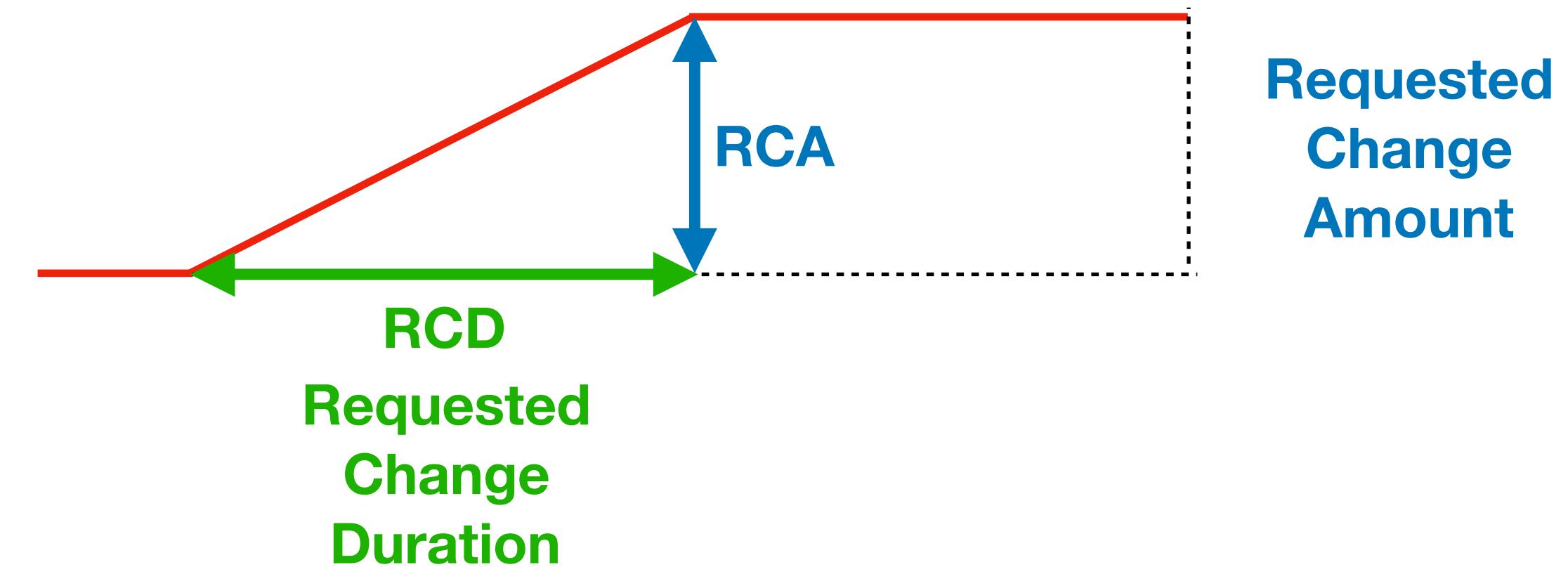
$$RMSE_i = \sqrt{\frac{1}{T_{trans}} \sum_{t=0}^{T_{trans}} \|y_i^W(t) - y_i^{WL}(t)\|^2}$$

Annotations for the equation:

- A green circle highlights the term $\frac{1}{T_{trans}}$.
- A green arrow points from the term T_{trans} to the label "Transient" at the bottom.
- A blue arrow points from the term $y_i^W(t)$ to the label "Wired" above it.
- A red arrow points from the term $y_i^{WL}(t)$ to the label "Wireless" above it.

Problem Formulation

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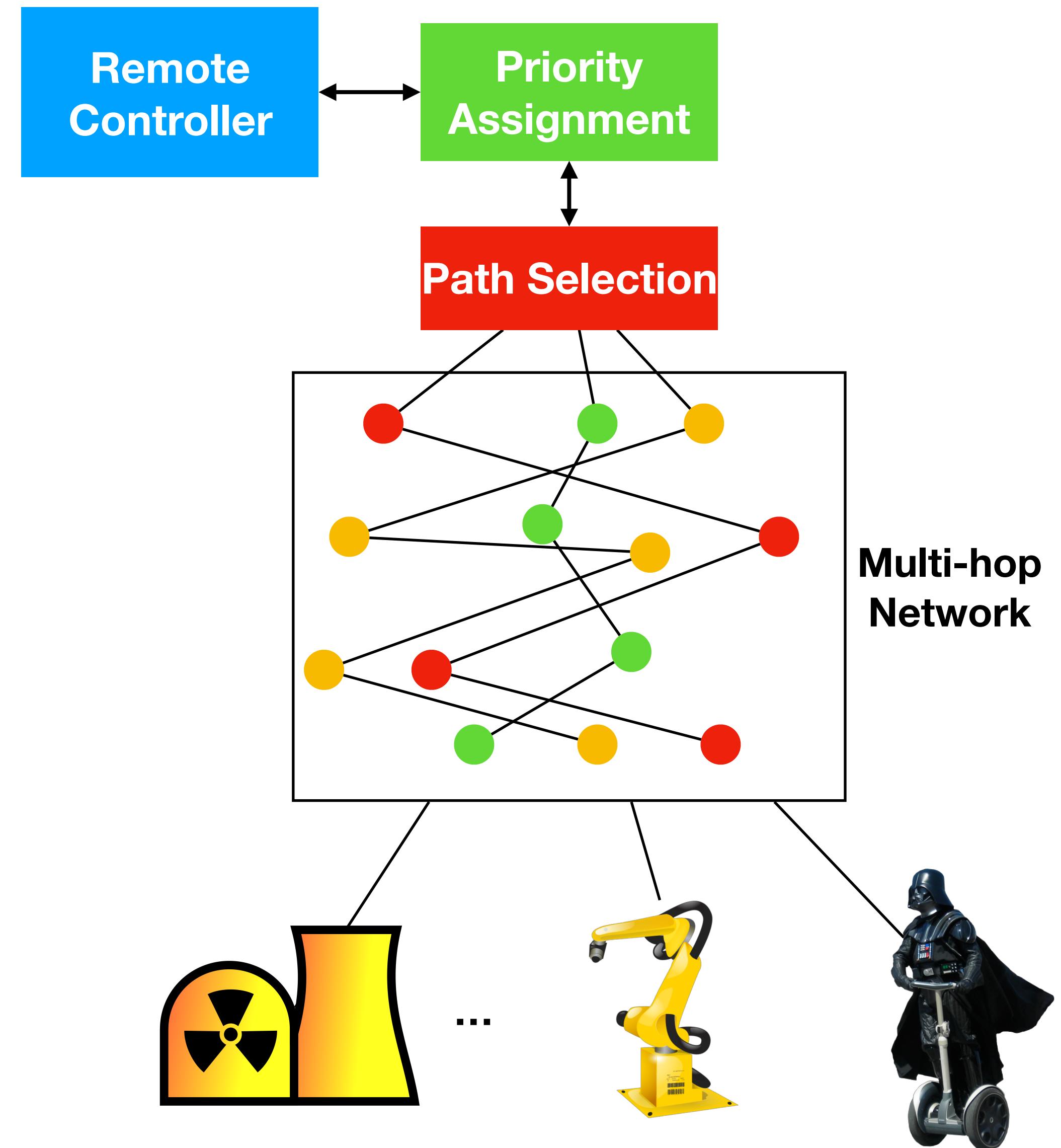
Annotations for the equation:

- A green arrow labeled "Transient" points to the summation index $t=0$.
- A blue arrow labeled "Wired" points to the term $y_i^W(t)$.
- A red arrow labeled "Wireless" points to the term $y_i^{WL}(t)$.

$\forall i \in \text{Physical Systems}$

Solution: Dynamic Packet Priority Assignment

- **Priority Assignment**
 - ▶ Static heuristic (baseline)
 - ▶ Dynamic heuristic
 - ▶ PID Dynamic heuristic
- **Path Selection**
 - ▶ Network Path Quality Determination

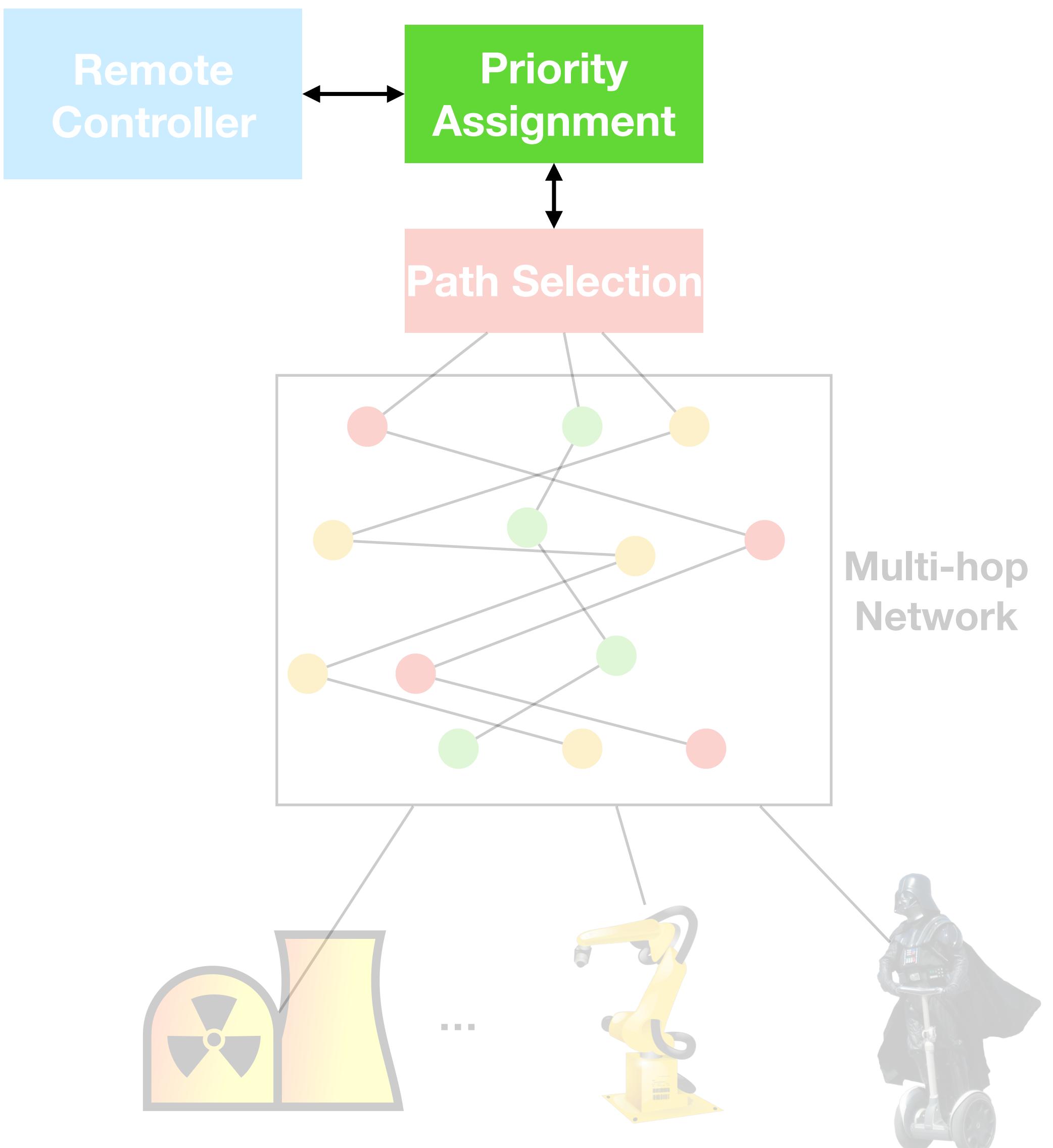


Static Heuristic - Baseline

- Offline analysis
 - ▷ Assuming no packet loss
 - ▷ For different requested changes in demand
- For all PS i compute

$$rRMSE_i(T_{sim}) = \sqrt{\frac{1}{T_{sim}} \sum_{j=0}^{T_{sim}} \|r_i(j) - y_i(j)\|^2}$$

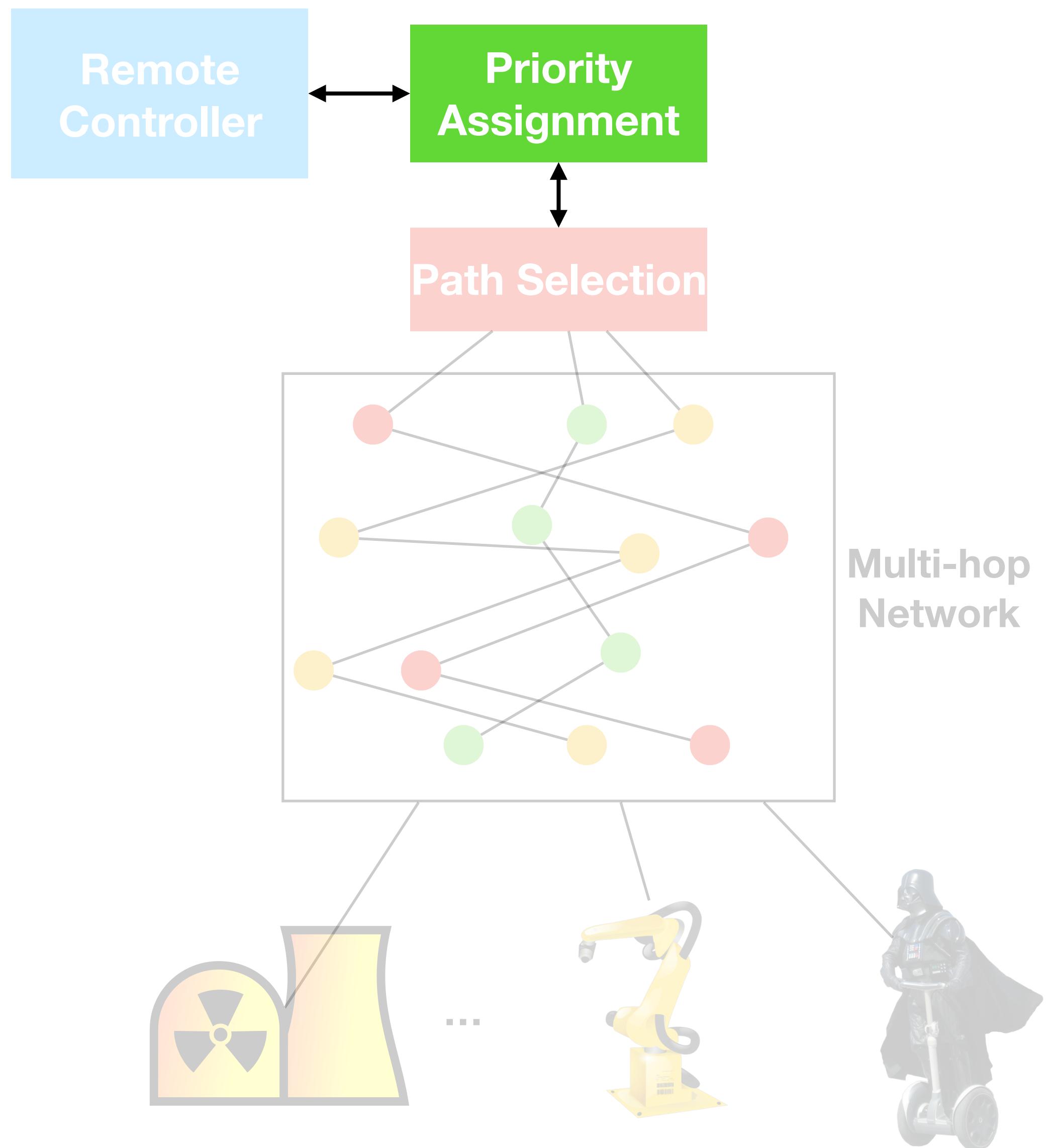
- Assign the priorities that minimise the average $rRMSE_i(T_{sim})$
- Do not change the priorities online



Dynamic Heuristic

- At every time t , for all PS i compute
- Sort the PS i by $rRMSE_i(t)$
- Assign the highest priority to the PS with highest value of $rRMSE_i(t)$

$$rRMSE_i(t) = \sqrt{\frac{1}{t} \sum_{j=0}^t \|r_i(j) - y_i(j)\|^2}$$



PID Dynamic Heuristic

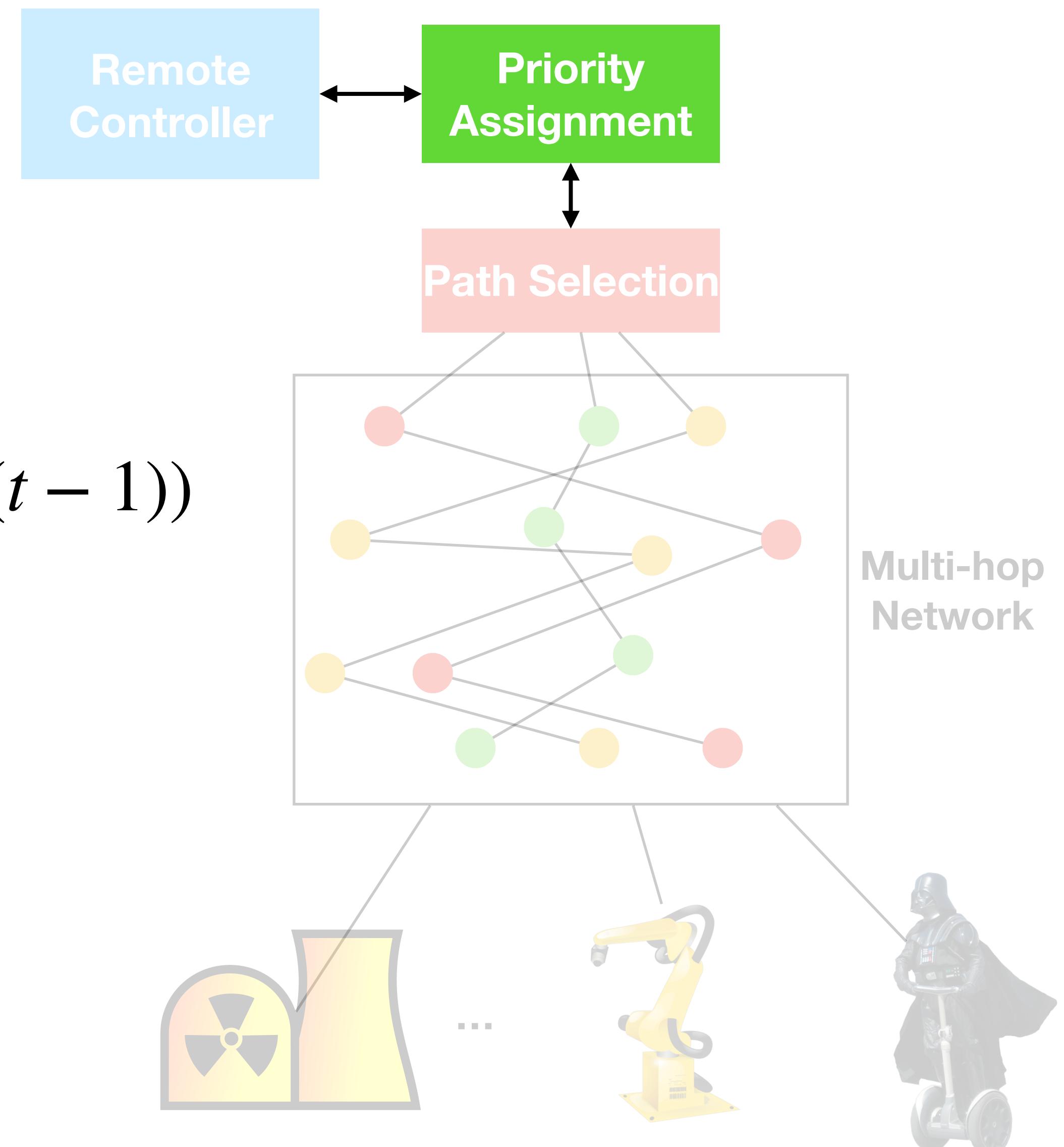
- We define the tracking error as

$$e_i(t) = |r_i(t) - y_i(t)|$$

- The priority for every PS i is computed as

$$\pi_i(t) = K_P \left(e_i(t) + \frac{\lambda}{t} \sum_{i=1}^t e_i(t) \right) + K_D (e_i(t) - e_i(t-1))$$

- strange formula, isn't it?
 - It is a **PID controller!**



PID Dynamic Heuristic

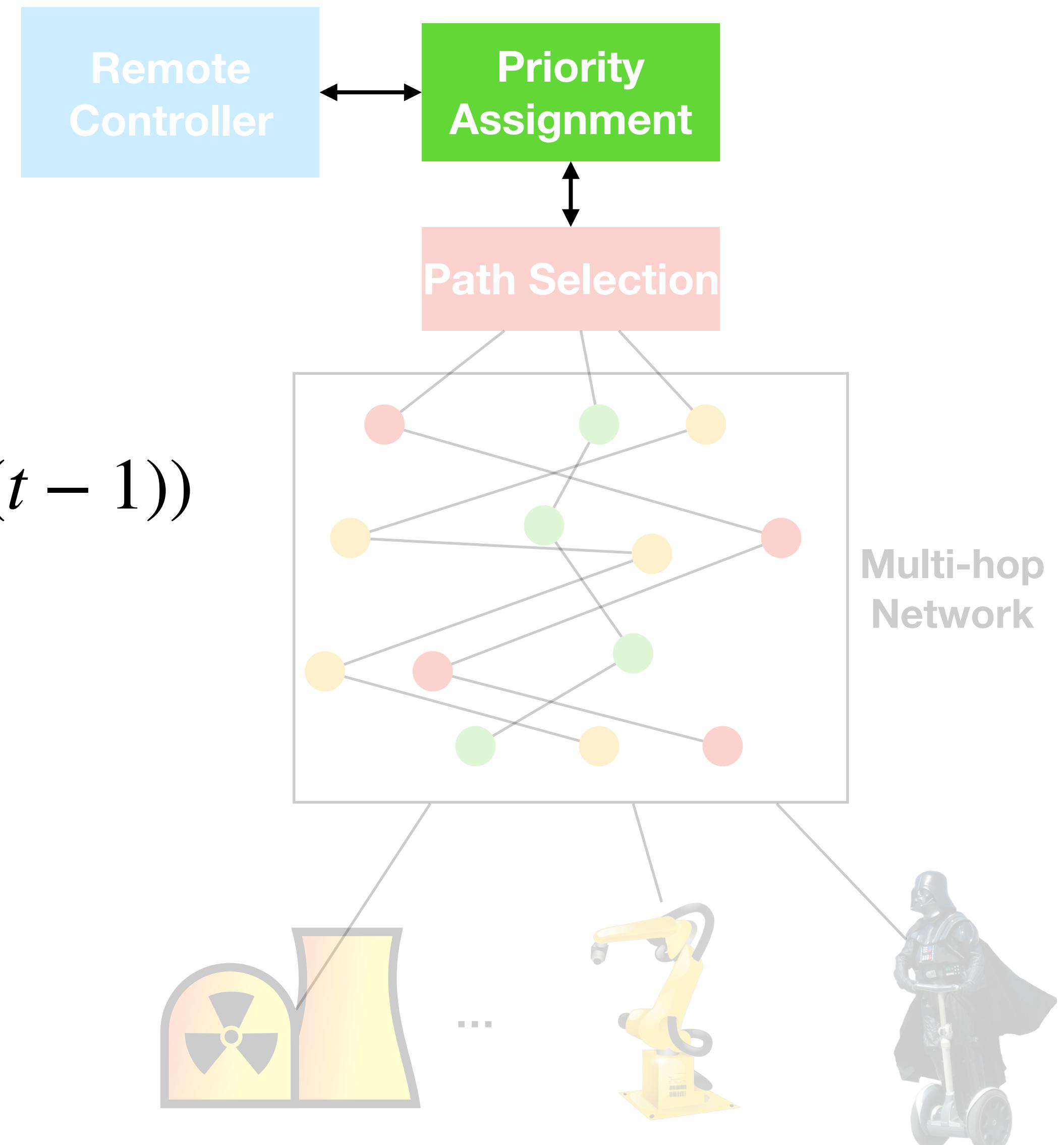
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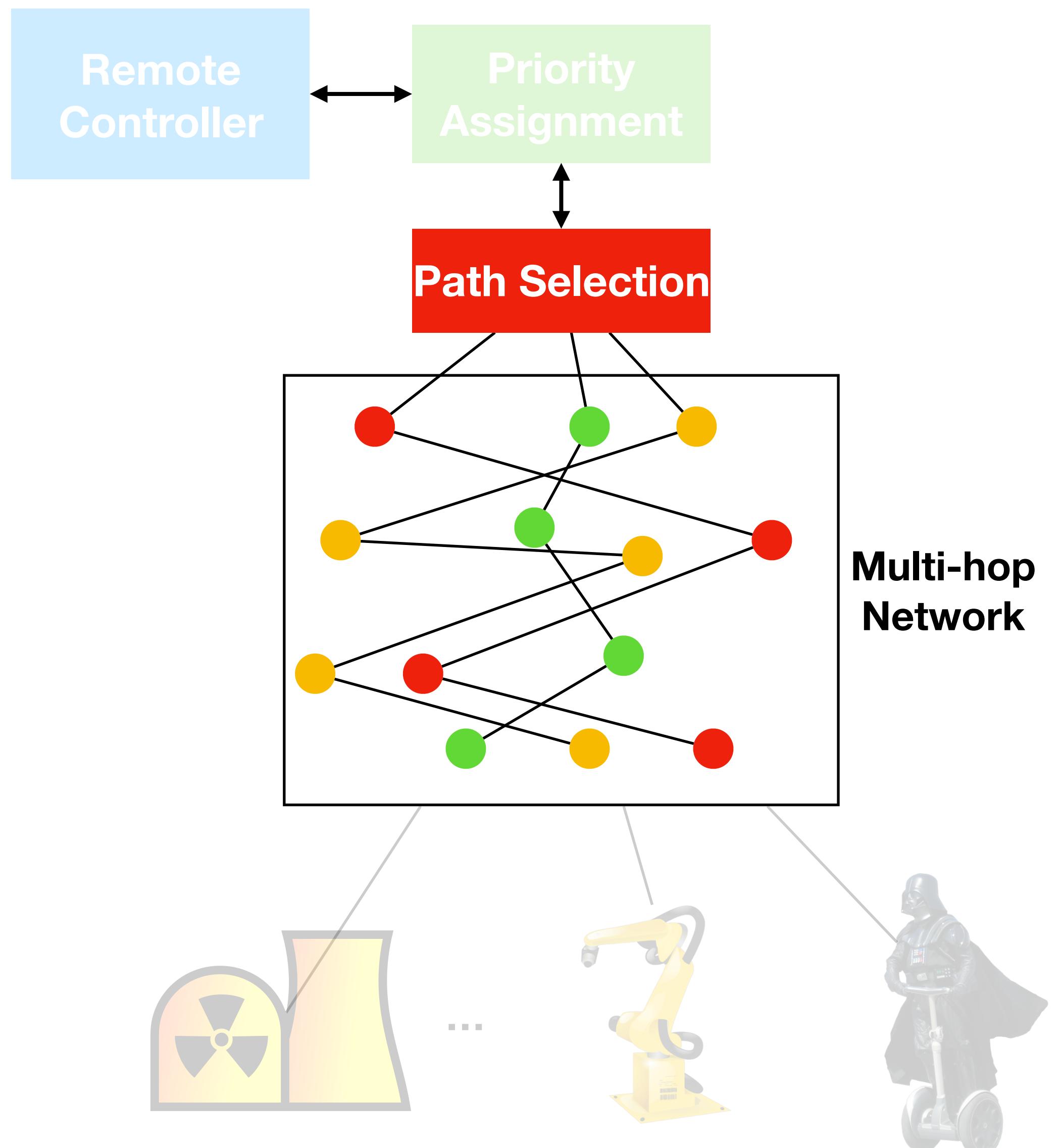
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The Path Quality Model: PQModel

- After we determine the priority of the measurement packets
- Includes
 - Network delay
 - Network reliability
- We compute the path quality for all the paths as

$$PQ = D_{net} + \alpha n_{loss} \Delta_{csp}$$

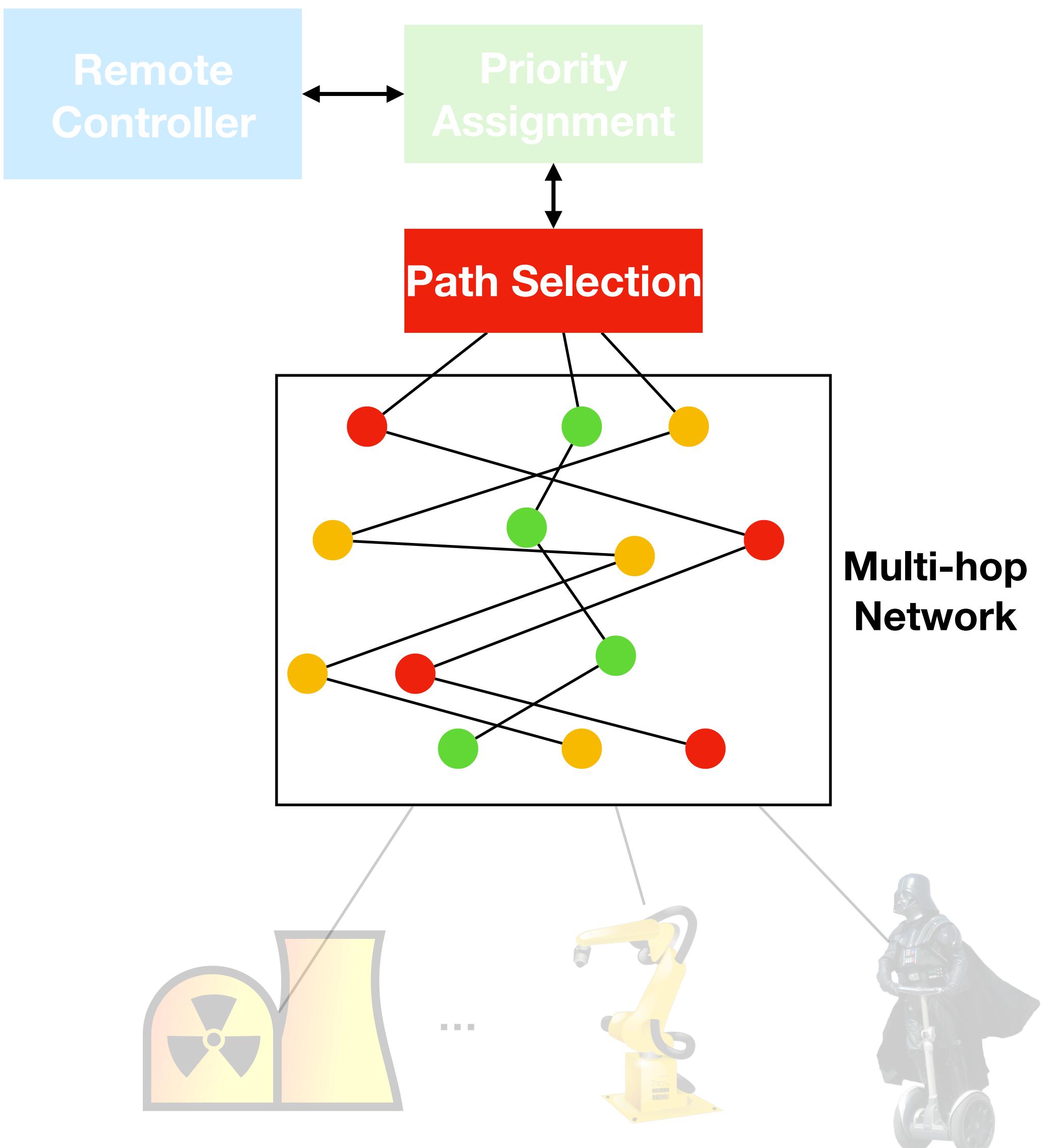


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End-to-end delay

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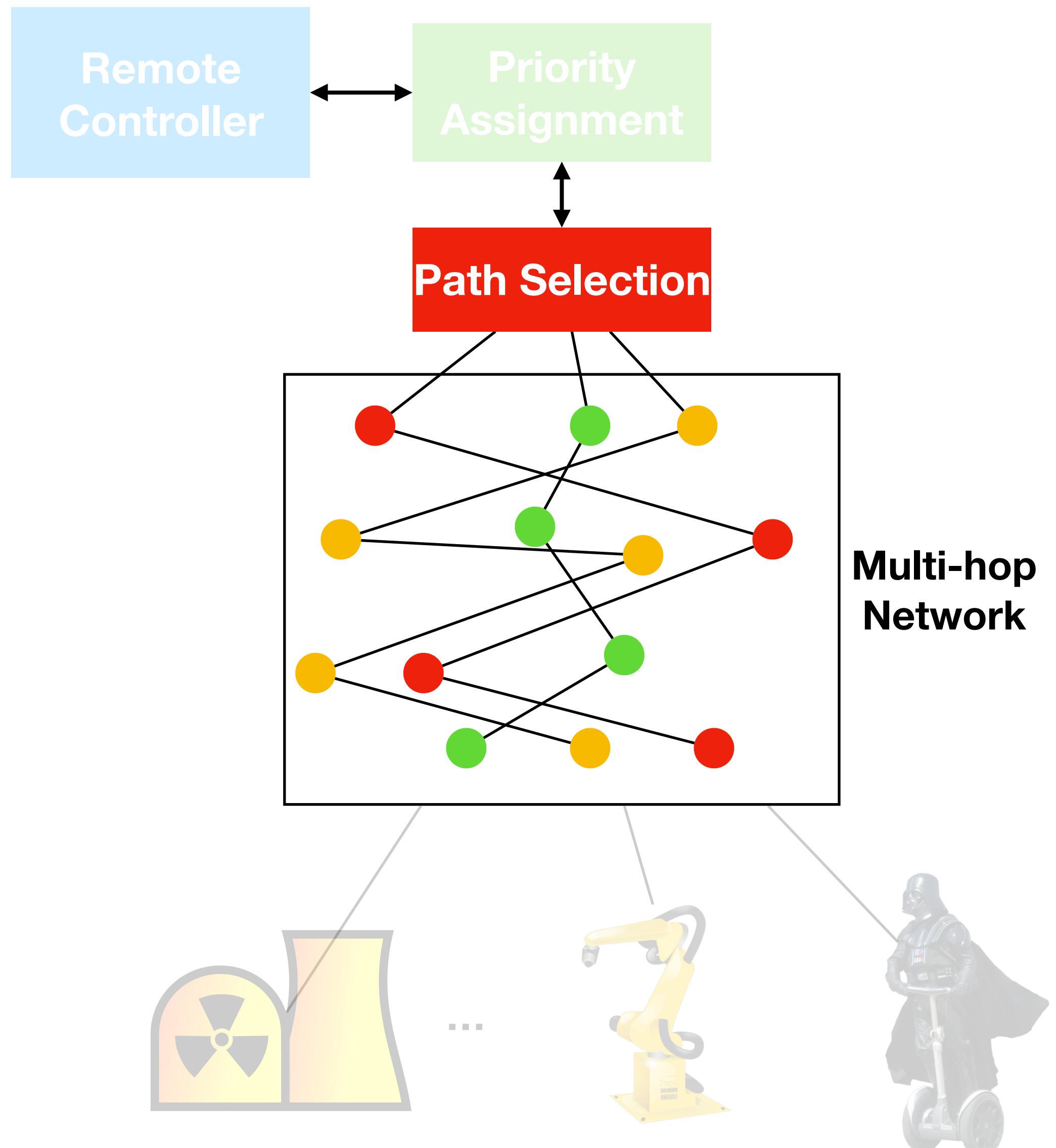


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End-to-end delay Control Sampling Period



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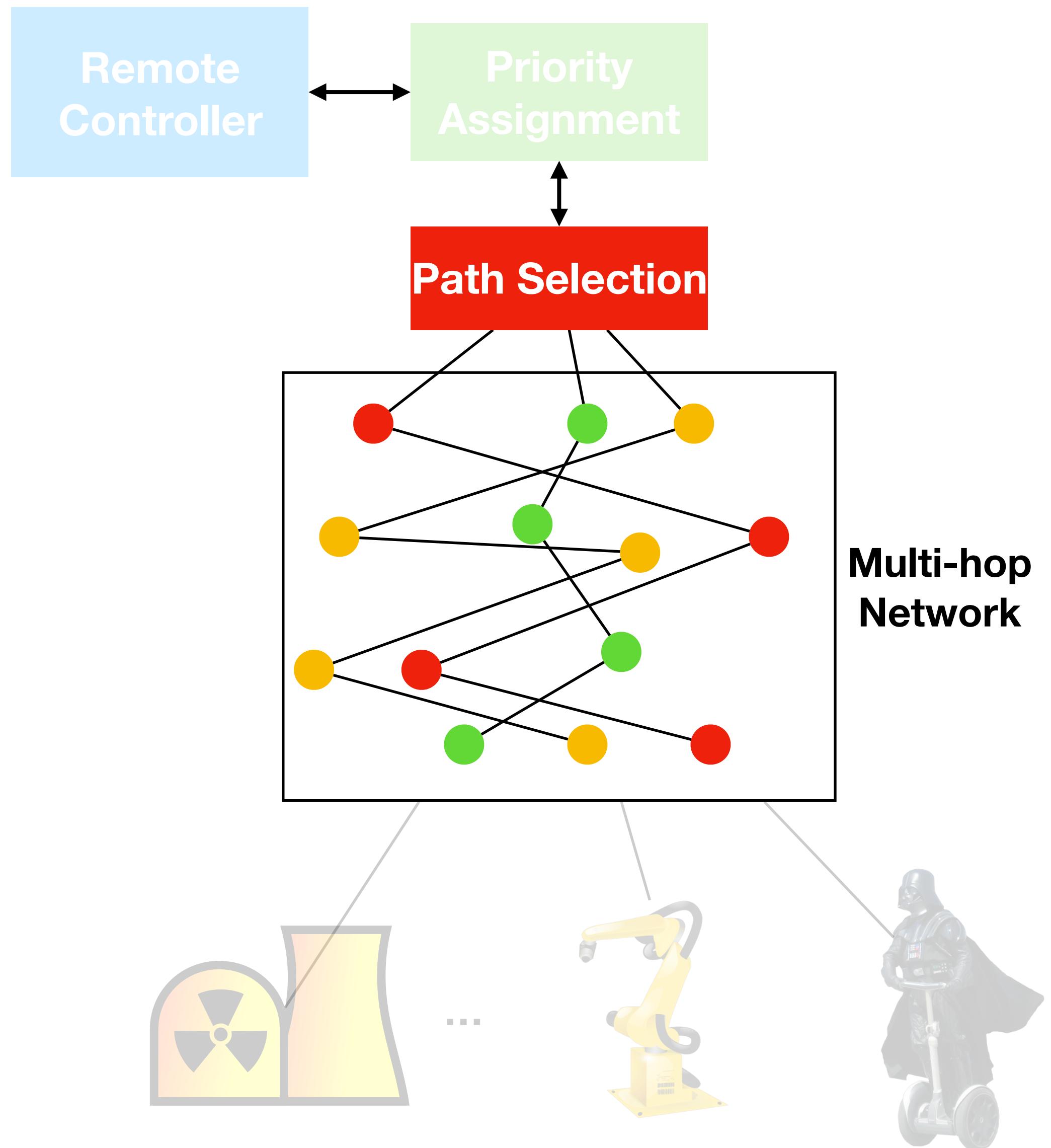
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End-to-end delay

Control Sampling Period

Consecutive Packet losses



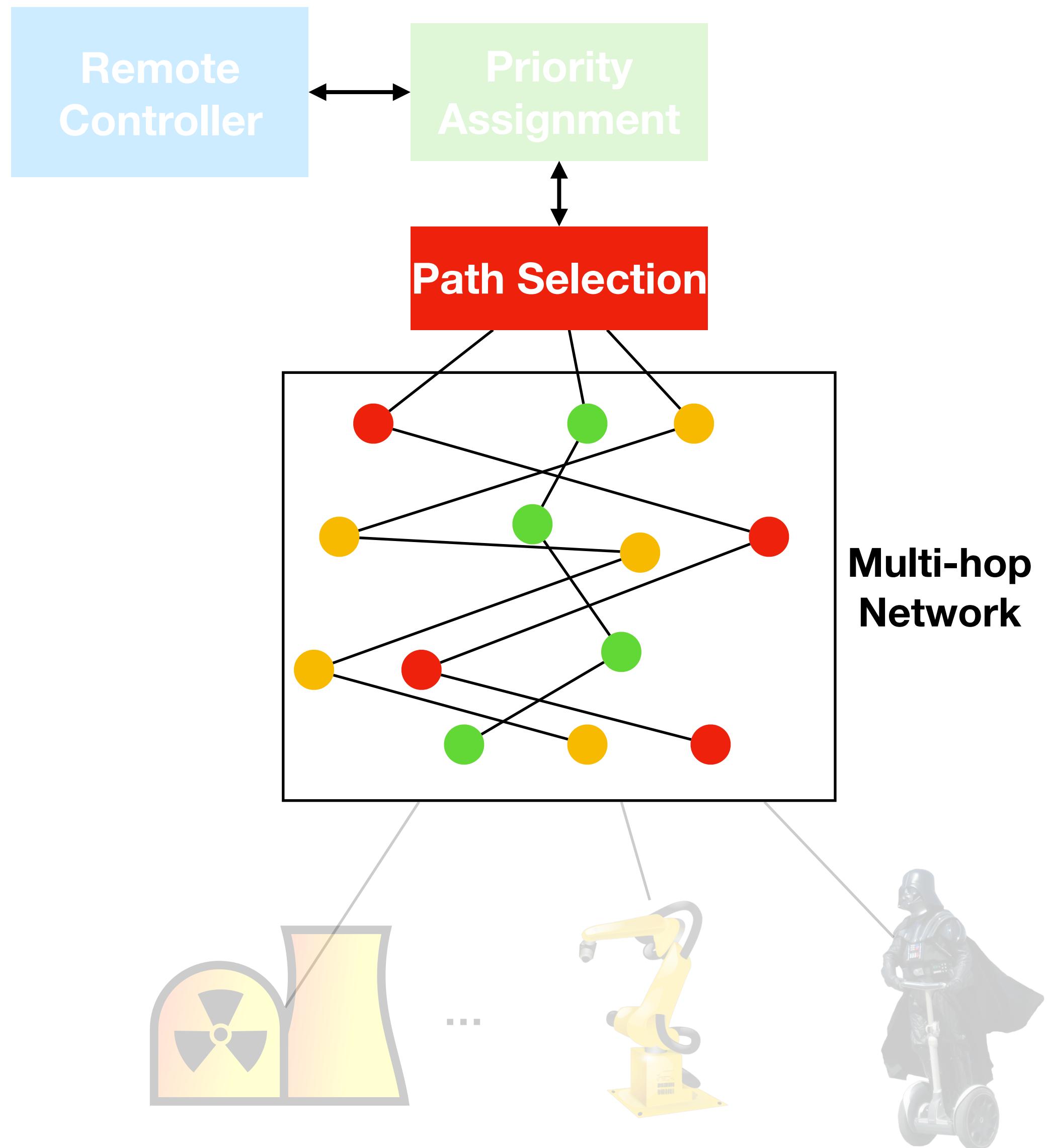
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Design parameter Consecutive Packet losses

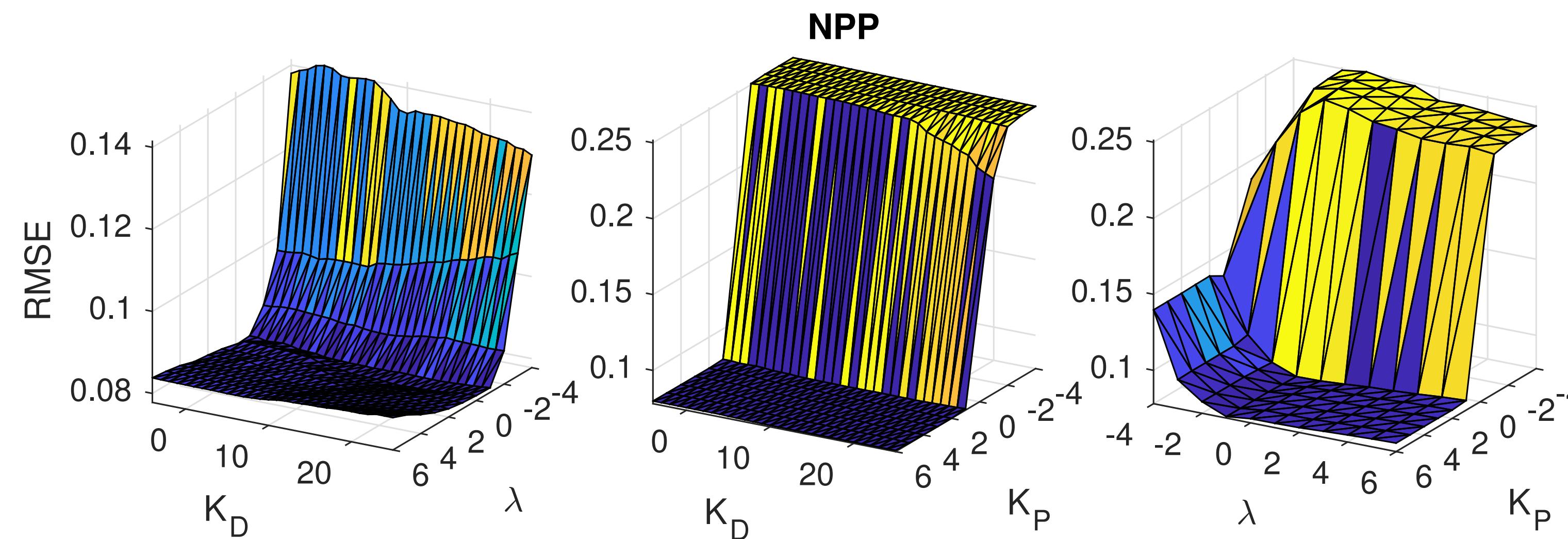
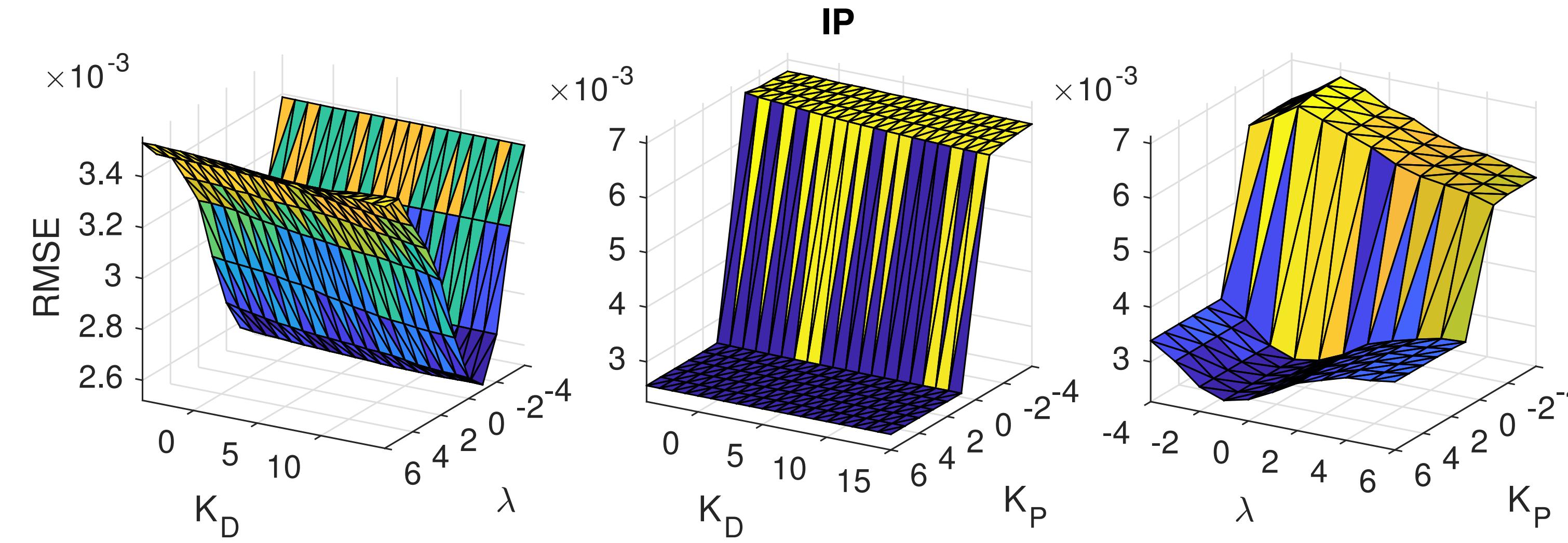


Case studies

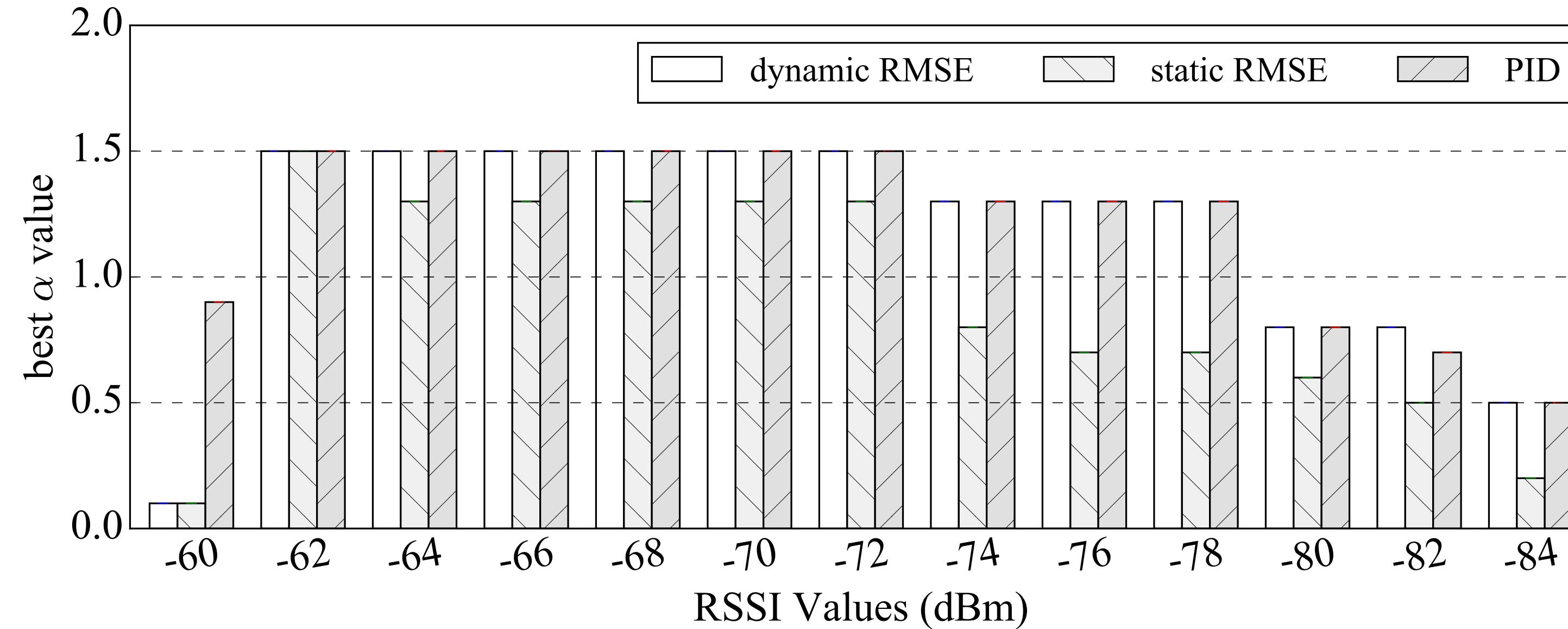
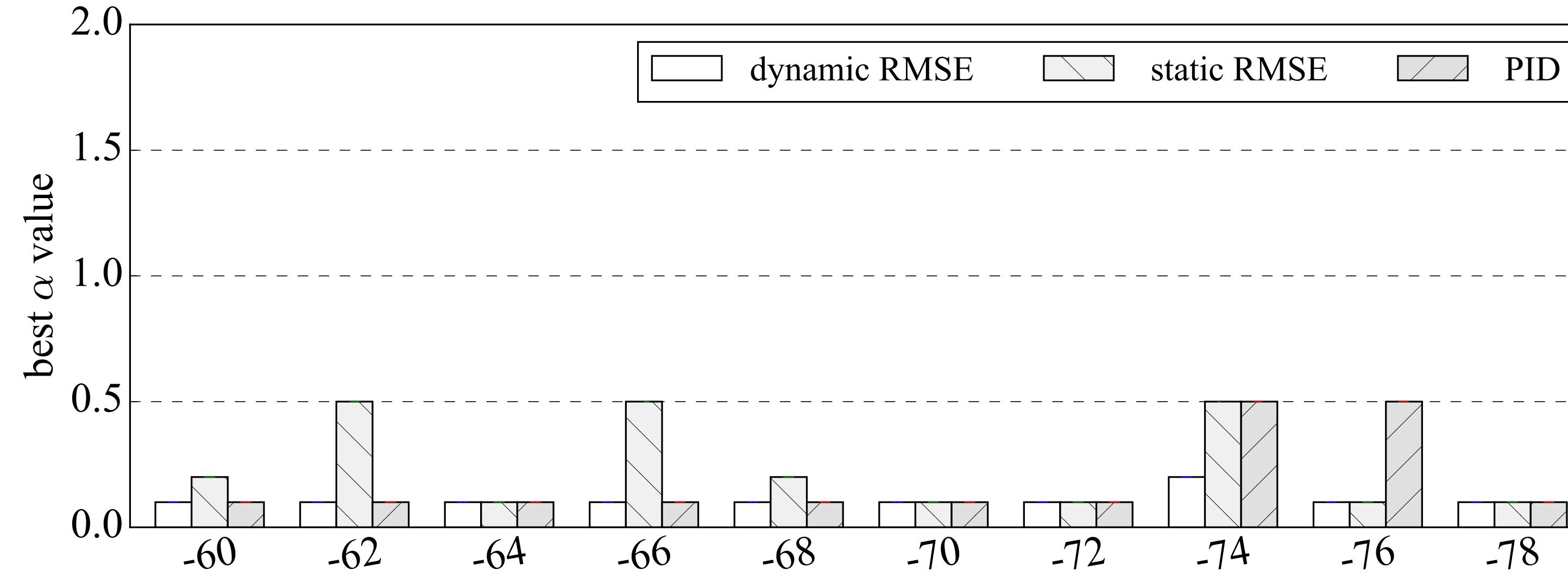


Parameters	Inverted Pendula (IP)	Nuclear Power Plant (NPP)	
Sampling period T_s	0.01s	0.1s	
Simulation time T_{sim}	100s	300s	
RCA	$(6 + 4l)$ meters	$(2 + 2l)$ MWatts	$l=0, \dots, 4$
RCD	$5j$ seconds	$15j$ seconds	$j=1, \dots, 8$
ST change	[0s, T_{sim} -RCD]	[0s, T_{sim} -RCD]	

PID Tuning



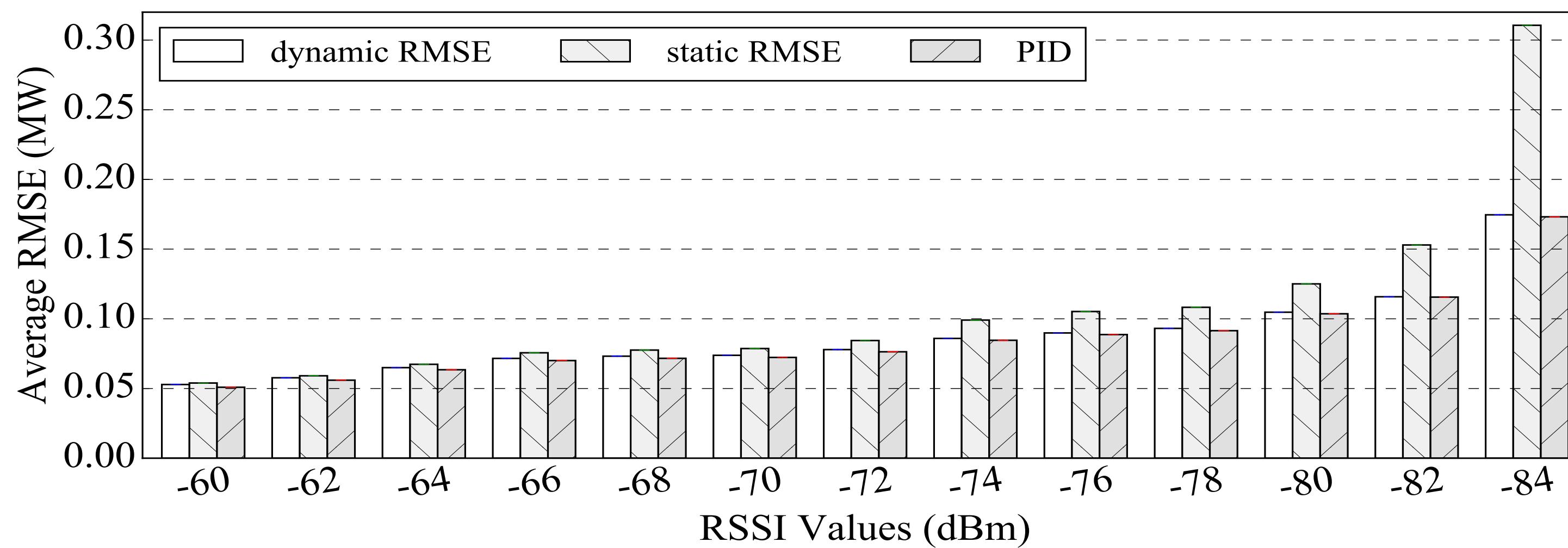
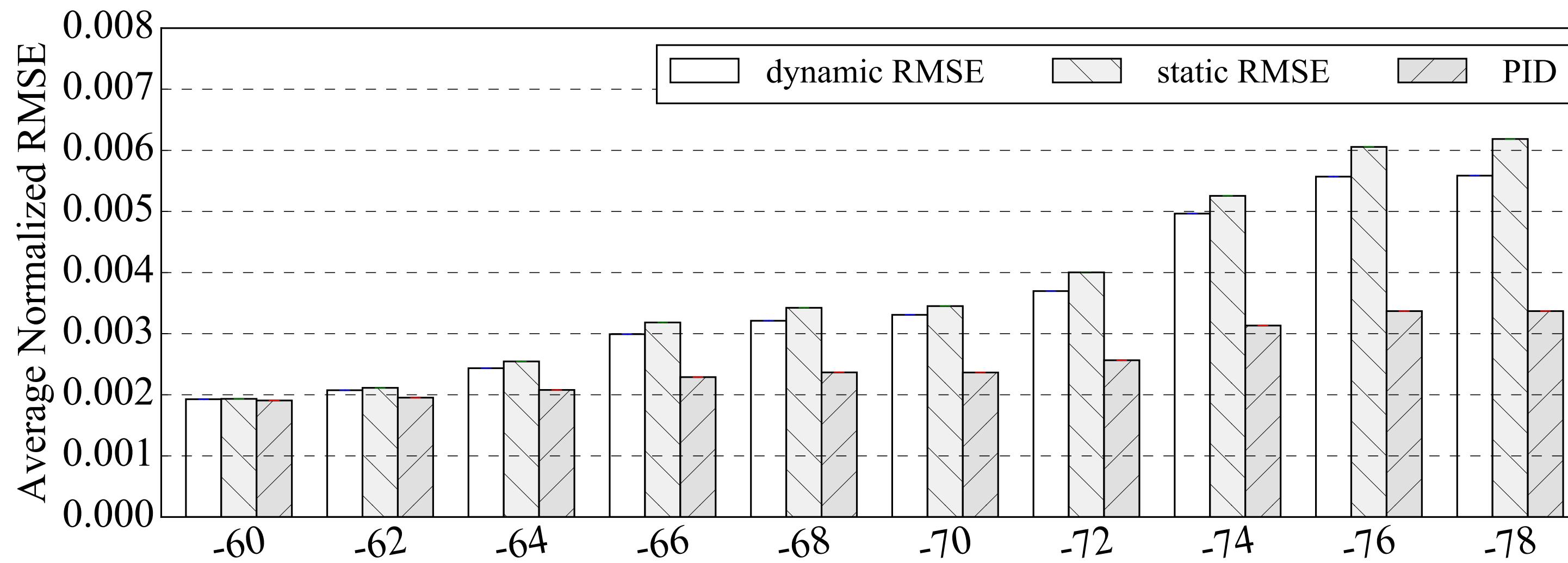
α Tuning



The IP is more sensitive to large delays

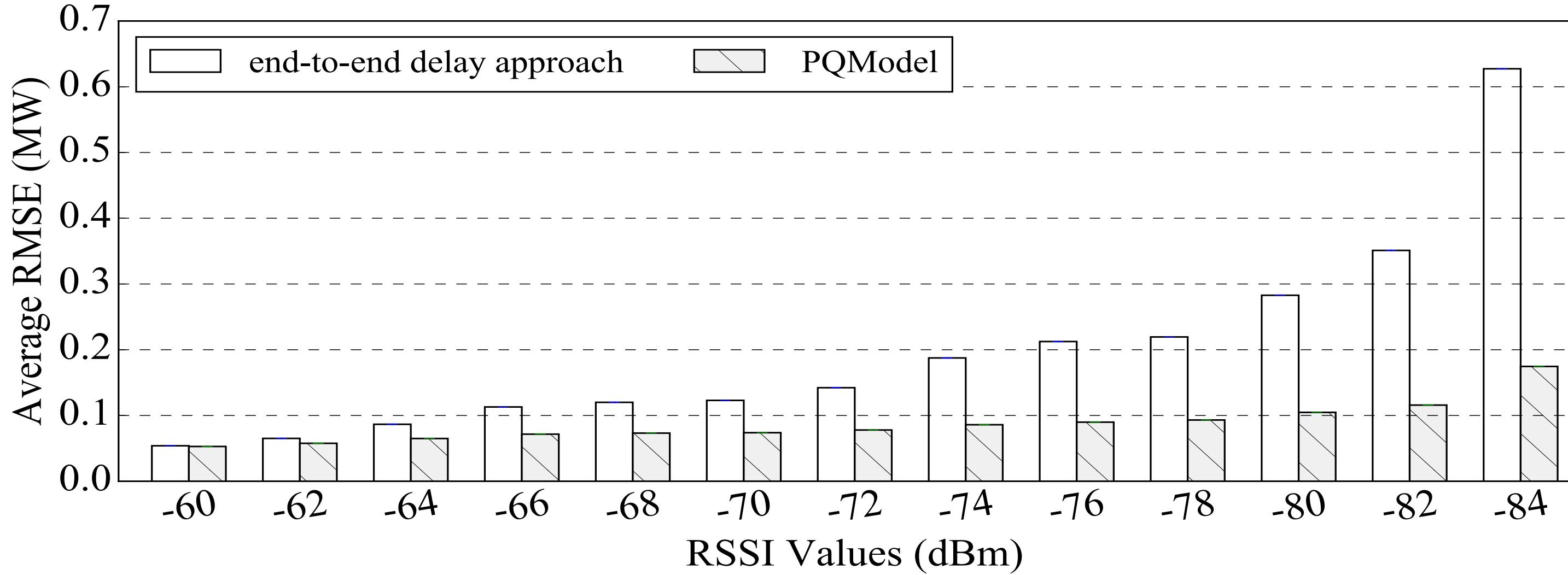
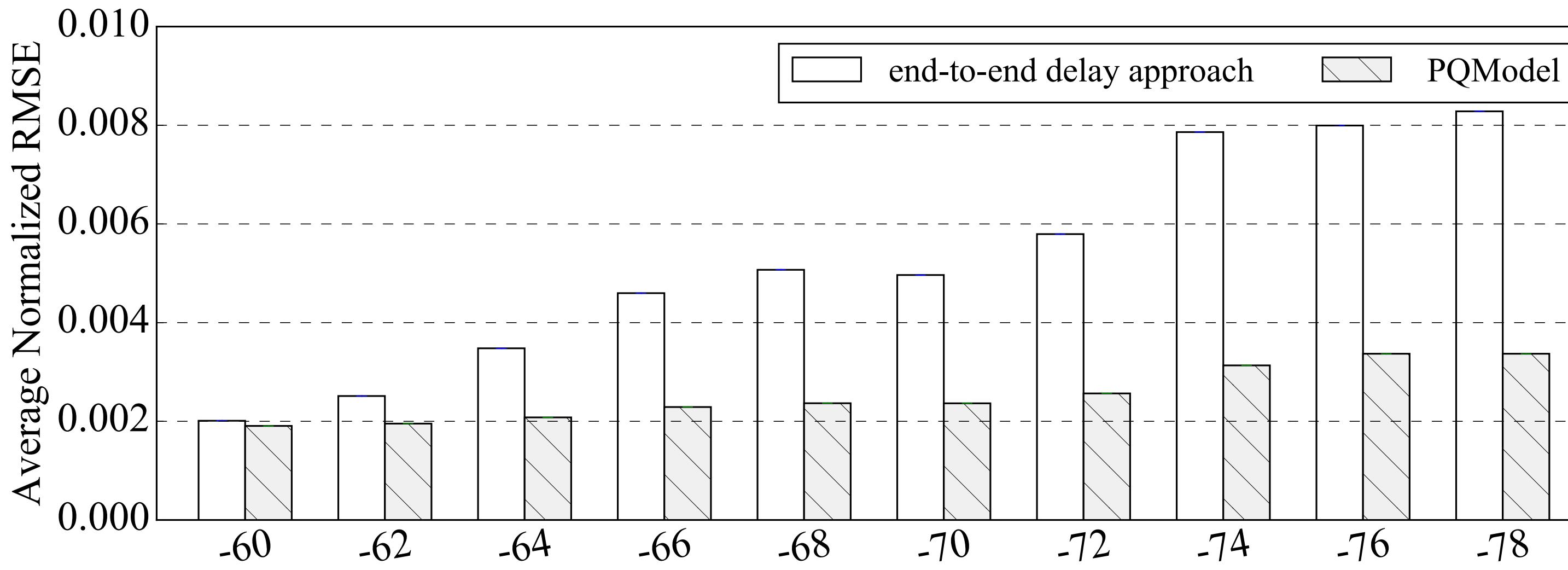
α decreases with high network interference

Comparison of the Different Heuristics



PID provides better and more stable performance

Improvement With PQModel



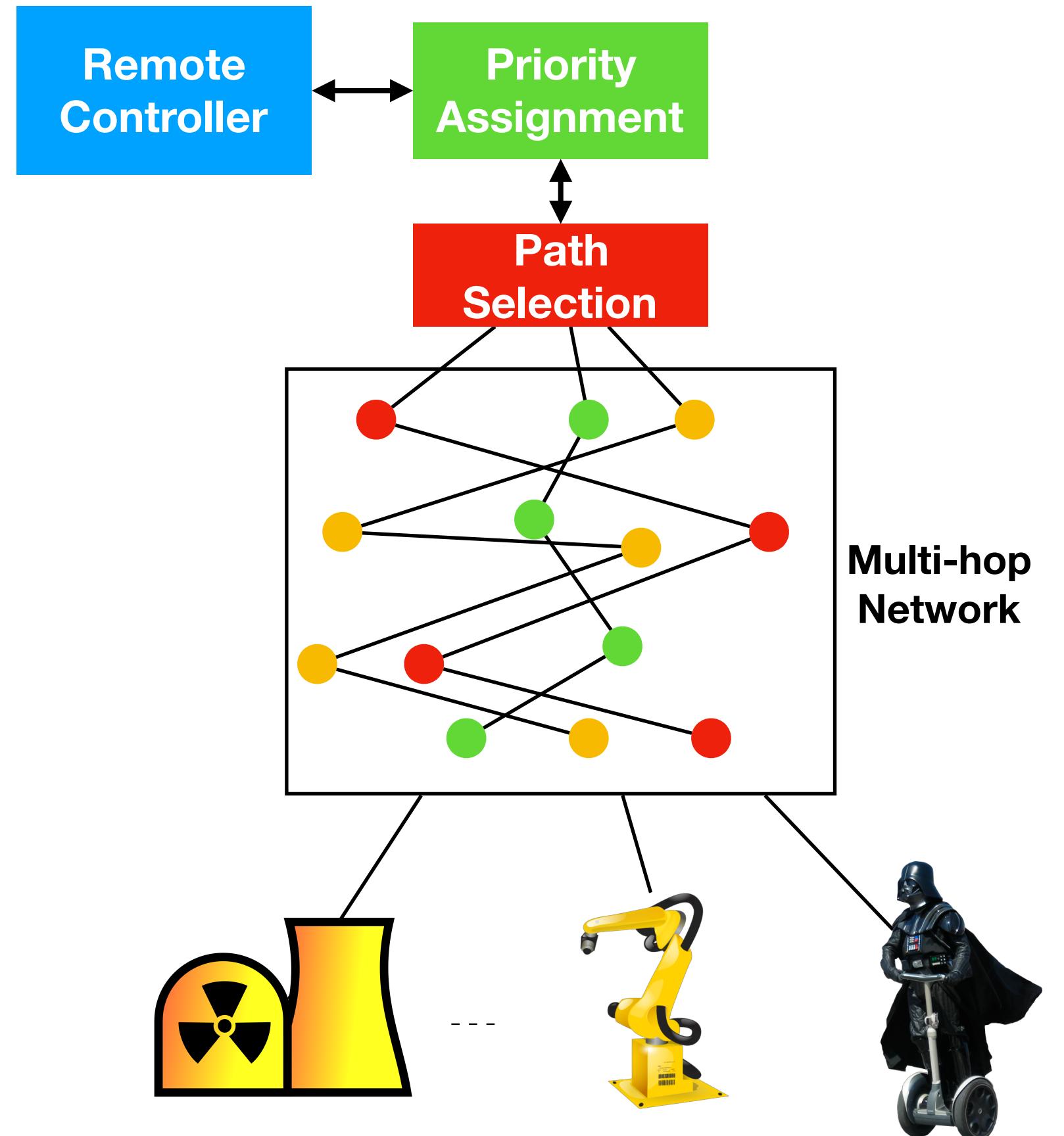
The PQ model
outperforms
end-to-end
approaches

Conclusion

- We explored the interaction between dynamic packet scheduling and the control system performance in WCS
 - ▶ Highly nonlinear systems are not heavily explored in the literature
- Three heuristics for packet priority assignment
 - ▶ PID: most promising
- Path quality model
 - ▶ Tradeoff between delay and reliability



Questions?



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