

15.19

fredag 23 december 2022

15:57

$$a) \quad 2y \cdot \frac{dy}{dx} = 3x^2 \quad y' = \frac{dy}{dx}$$

$$\int 2y \, dy = \int 3x^2 \, dx$$

$$y^2 + A = x^3 + B \Leftrightarrow y^2 = x^3 + \underbrace{(B-A)}_C$$

$$y^2 = x^3 + C \quad y = \pm \sqrt{x^3 + C}$$

$$2 = \sqrt{1 + C} \quad C = 3$$

$$\text{Sv: } y = \sqrt{x^3 + 3}$$

b)

$$\int 3y^2 \, dy = \int 2x \, dx$$

$$y^3 = x^2 + C \quad y = (x^2 + C)^{1/3}$$

$$2 = (1 + C)^{1/3} \quad C = 7$$

$$\text{Sv: } y = \sqrt[3]{x^2 + 7}$$

c)

$$\int y \, dy = \int 3x^2 \, dx$$

$$\frac{y^2}{2} = x^3 + C \quad y = \sqrt{2(x^3 + C)} \quad 2 = \sqrt{2(1 + C)} \quad C = 1$$

$$\text{Sv: } y = \sqrt{2(x^3 + 1)}$$

d)

$$\int y^2 \, dy = \int 2x \, dx$$

$$\frac{y^3}{3} = x^2 + C \quad y = (3(x^2 + C))^{1/3} \quad 2 = (3(1 + C))^{1/3}$$

$$C = 5/3$$

$$\text{Sv: } y = \sqrt[3]{3x^2 + 5}$$