

a)

$$f(t) = (2 + 3t^2) \theta(t) =$$

$$= 2\theta(t) + 3t^2\theta(t)$$

$$\underbrace{2\theta(t)}_{g(t)} \downarrow \mathcal{L}g(s) = \frac{1}{s}$$

$$\underbrace{3t^2\theta(t)}_{h(t)} \downarrow \mathcal{L}h(s) = \frac{2}{s^3}$$

$$\mathcal{L}f(s) = \frac{2}{s} + \frac{6}{s^3} = \frac{2(s^2 + 3)}{s^3}$$

d)

$$f(t) = t^2 e^{3t} \theta(t)$$

$$\mathcal{L}f(s) = \frac{2}{(s-3)^3}$$

e)

$$f(t) = (\cos 2t - \sin 2t) \theta(t)$$

$$\mathcal{L}f(s) = \frac{s}{s^2 + 4} - \frac{2}{s^2 + 4} = \frac{s-2}{s^2 + 4}$$