Introduction to Machine Learning - Exercise 1 Due Date: November 17th 22:00, 2019

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$1 \quad \mathbf{ERM}$

1.1

As mentioned in the class, a learning algorithm receives as input a training set S sampled from an unknown distribution \mathcal{D} and labeled by some target function f. Since the learner does not know what \mathcal{D} and f are, we use a training set of examples, which acts as a snapshot of the world that is available to the learner. In ERM we would like to find a solution that works well on that data.

An axis aligned classifier in the plane is a classifier that assigns the value 1 to a point if and only if it is inside a certain rectangle. Formally, given real numbers $a_1 \leq b_1, a_2 \leq b_2$, define the classifier $h_{(a_1,b_1,a_2,b_2)}$ by

$$h_{(a_1,b_1,a_2,b_2)}(x_1,x_2) = \left\{ \begin{array}{ll} 1 & \text{if } a_1 \leq x_1 \leq b_1 \ and \ a_2 \leq x_2 \leq b_2 \\ 0 & \text{otherwise} \end{array} \right.$$

Let A be the algorithm that returns the smallest rectangle enclosing all positive examples in the training set. Explain whether A is an ERM or not.

1.2

Let \mathcal{H} be the hypothesis space of binary classifiers over a domain \mathcal{X} . Let \mathcal{D} be an unknown distribution over \mathcal{X} , and let f be the target hypothesis in \mathcal{H} . Denote $h \in \mathcal{H}$. Let us define the *true error* of h as,

$$L_{\mathcal{D}}(h) = \mathbb{P}_{x \sim \mathcal{D}}[h(x) \neq f(x)]$$

Let us define the *empirical error* of h over the training set S as,

$$L_S(h) = \frac{1}{m} \sum_{i=1}^{m} \mathbb{1}_{[h(x) \neq f(x)]}$$

where m is the number of training examples.

Show that the expected value of $L_S(h)$ over the choice of S equals $L_D(h)$, namely,

$$\mathbb{E}_{S \sim \mathcal{D}} \big[L_s(h) \big] = L_{\mathcal{D}}(h)$$

2 Sound Compression

In this part of the exercise we will use the k-means algorithm for sound compression, i.e. you should implement the k-means algorithm on the **amplitude values** and then replace each value by its centroid.

You should implement the k-means algorithm as described in class (slide no. 40 in recitation 1 presentation). You will train your algorithm and report results using the sample.wav as shown in Figure 1. For visualization, you can use Praat (http://www.fon.hum.uva.nl/praat/)

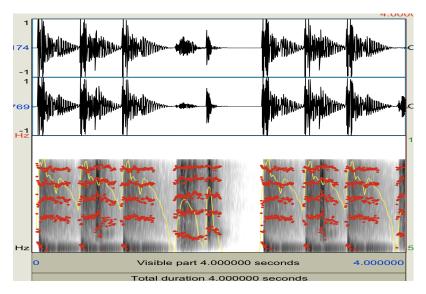


Figure 1: sample.wav

The centroids initialization will be provided to you in a text file which will be received as an argument to your program. The run command to your program should be:

```
$ python ex_1.py <wav file> <centroinds_init>
For example:
$ python ex_1.py sample.wav cents1.txt
```

The following snippet contains commands for reading and writing sound files as well as reading the centroids initialization:

```
sample,centroids = sys.argv[1],sys.argv[2]
fs, y = scipy.io.wavfile.read(sample) #reading
x=np.array(y.copy())
centroids=np.loadtxt(centroids)

#your code goes here#
...
...
scipy.io.wavfile.write("compressed.wav", fs, np.array(new_values, dtype=np.int16))#saving
```

You should get something similar results to the following,

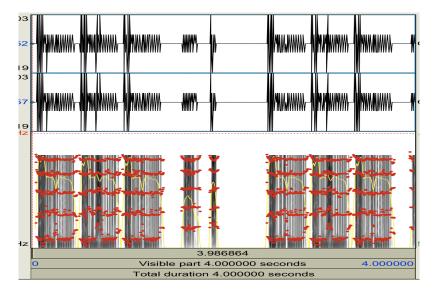


Figure 2: K=5

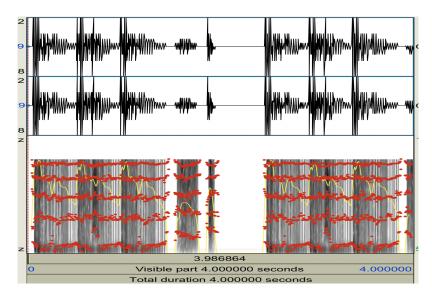


Figure 3: K=10

Reproducibility. Originally, the initial centroids in k-means are randomly generated. For reproducible purposes, we provided you with cents1.txt and cents3.txt for centroid initialization, you should use it and compare your output with output1.txt and output3.txt! Please note that given these pre-defined values, your sequence of centroid updates should be deterministic and not random in any way.

Note: in case when 2 centroids are evenly close to a certain point, the one with the lower index

"wins".

Your code should run for 30 iterations or until convergence. Your program should create output.txt, consisting of your centroids after each centroid update step as follows: For example, when using cents3.txt:

```
[iter 0]:[-4189. -4171.],[ 4. -2.],[3. 2.],[4. 3.],[4543. 4517.]
[iter 1]:[-7645. -7603.],[-494. -718.],[-243. 24.],[780. 802.],[7851. 7858.]
...
[iter 18]:[-24823. -24965.],[-7598. -7574.],[ 10. -11.],[7645. 7638.],[24409. 24914.]
[iter 19]:[-24823. -24965.],[-7598. -7574.],[ 10. -11.],[7645. 7638.],[24409. 24914.]
The full requested output is at output3.txt
use the following print-line to match outputs:
    print(f"[iter {iter}]:{','.join([str(i) for i in new_z])}")
```

As you can see the algorithm converged and stopped(same centroids). For consistency, after each centroids update, use the round() function on each dimension. We define convergence when the centroids don't update. You can assume both the sound and the centroids initialization files will be at the same working directory as your running file.

The sample.wav was taken from here: https://www.youtube.com/watch?v=7vQ831z0528 (Lucille Crew - Something).

3 What to submit?

You should submit the following files:

- A txt file, named details.txt with your name and ID.
- A PDF file named ex_1.pdf with your answers to 1.1 and 1.2.
- Python 3.6 code for question 2. Your main function should reside in a file called ex_1.py. The main function prints the centroids as explained above.
- A txt file named output2.txt Your program's output when using the cents2.txt for initialization.
- A PDF report including the following plots: (i) The average loss value (i.e. the distance between each point to its closest centroid) as a function of the iterations (you can stop at 10) for k = 2, 4, 8, 16. Your report should include the implementation details (number of iterations, how you chose your centroids, did you run multiple run each time?, etc.)
- Part of your grade will consist of automatic checks using the Submit system. Make sure your output matches the expected output, check your mail after submitting.
- <u>Note</u>: your code should load n sound and a centroids initialization files located in the same folder as your main script. Make sure you use relative paths.

```
Overall: ex_1.py, ex_1.pdf, details.txt, output2.txt and report.pdf
```