# Algorithms for Bioinformatics

# Pairwise Sequence Alignment

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#### **Outline**

- Comparing Sequences
- Visualize alignments
- Alignments as an optimisation problem
  - Problem definition and complexity
  - Substitution matrices
  - Gap penalties
  - Implementing objective function
- Global Alignment Algorithms with Dynamic Programming
  - Needleman-Wunsch
- Local Alignment Algorithms with Dynamic Programming
  - Smith-Waterman
- Exercises

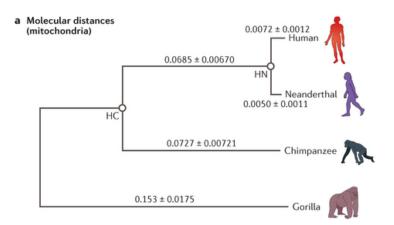
## Inferring function and Phylogenetics

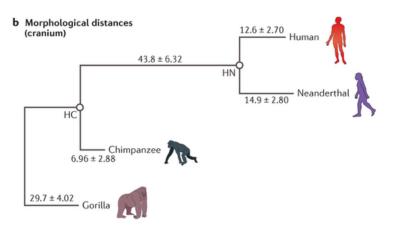
 Bioinformatics provides tools to help researchers to infer the function of the genes and the respective proteins. It relies on the assumption that biological sequences with high similarity share similar functions.

Phylogenetics is the division of biology that studies evolutionary divergence and relationship between organisms, based on two important important concepts:

- Similarity. Measures the resemblance and differences between organisms without taking into account any contextualization.
- Homology. Investigates the common ground between the organisms and if they share any ancestral characteristics. Find the point in the evolutionary tree that they started to diverge.
- Sequences with high degree of similarity have high probability of being homologous and share similar function. The higher the similar the higher the probability.

#### **Phylogenetics**





Nature Reviews | Genetics

Depending on the nature of the characters different evolutionary rates can be observed:

- Molecular sequences have a nearly constant rate in these close species.
- Morphological characteristics evolve in a different way.

Bayesian molecular clock dating of species divergences in the genomics era Mario dos Reis, Philip C. J. Donoghue & Ziheng Yang Nature Reviews Genetics 17, 71-80 (2016) doi:10.1038/nrg.2015.8

#### **Sequence Similarity**

Seq1: TATACTTCAGGAACTAATTCTGAAGCATCA

Seq2: TATACTAAAGGAACTAATGCTAAAGCATGA

Seq3: TATCCTCCAGGCATTATTCTTGGACCTTCT

- Oiven Sequence 1, which of the other two sequences is most similar?
  - Sequence similarity can be measured by counting the number of symbols that you need to change in one sequence (query) in order to transform it in the other sequence (target).
  - The distance between two sequences allows to quantify their similarity and how related their biological function may be. We expect that similar sequences will have similar functions.
  - This measure of distance also provides an indication of homology which helps us to know the evolutionary relationship between sequences.
  - Sequence similarity is the basis of phylogenetics studies.

#### **Sequence Similarity**

- Distance can be calculated by:
  - Hamming distance
  - Edit distance
- Hamming distance is a dissimilarity measure that corresponds to minimum number of symbols that are different between the two sequences.

```
Q:ATTACGAT
| | | Hamming distance is 3
T:ATCAGGTT
```

- This is a limited distance measure since it requires sequences to have the same length, can not perform edit operations.
- Distance between sequences of different length must be calculated with edit distance.

#### **Sequence Similarity**

- The edit distance between the query and the target sequence corresponds to the minimum number of editing operations (and associated costs) to transform one sequence into the other.
- Operations can be:
  - Substitution by replacing one symbol by the other



Deletion by deleting one symbol in the query sequence.



Insertion by inserting one symbol in the query sequence.



- Sequence alignment is a way of arranging the biological sequences to identify regions of similarity. Such regions may indicate a functional, structural, or evolutionary relationships between the sequences, that can be either DNA, RNA or protein.
- From a computational view an alignment is a procedure to align similar symbols keeping the same order.
- Alignments may be classified as either global or local.
- A global alignment aligns two sequences from beginning to end, aligning each letter in each sequence only once. An alignment is always produced. Indicated for sequences that share significant similarity over most of their extents.
- A local alignment maximizes the alignment of the parts of the sequences that share similarity. Finds the best aligned subsequence. An alignment may not be produced if no sufficient similarity is found.
- Global alignments are performed with the Needleman–Wunsch algorithms and local alignments with the Smith–Waterman algorithm.

There are many ways to align two sequences.

Q: CTGTCGCTGCACG

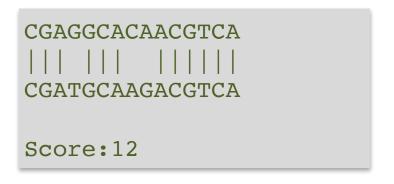
T: TGCCGTG

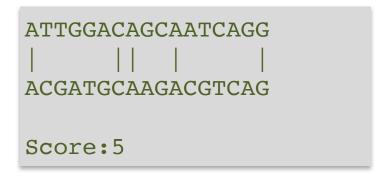
```
global:
CTGTCGCTGCACG
-TG-C-C-G--TG
```

```
local:
CTGTCGCTGCACG
-TG-CCGTG----
```

```
local:
CTGTCGCTGCACG
-TGCCG-T---G
```

- We need a way to obtain the biological meaning of an alignment. A scoring system can be used to evaluate and quantify the quality of the alignment. Possible scoring system:
  - 1 for a match between symbols
  - 0 for a mismatch





- Simple alignment score do not take into account the physico-chemical properties of amino-acids or the biological sequence information such as the structural and evolutionary relationship between the amino-acids.
- Given the properties of the amino-acids in proteins some mismatches are more acceptable than others. Substitution matrices give a score for each substitution of one amino-acid by another.

Example: NP\_004013 with NP\_004014 are dystrophin isoforms, but the first sequence is missing about 100 residues starting at residue 948 (some exons have been spliced out of the

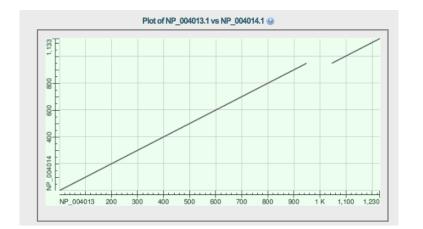
corresponding mRNA).

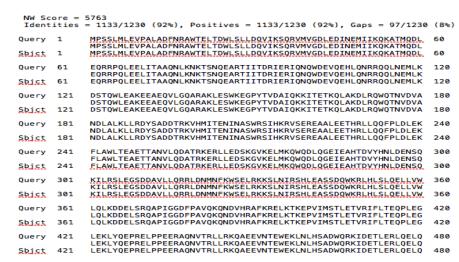


Compare two sequences across their entire span (Needleman-Wunsch)

https://blast.ncbi.nlm.nih.gov/

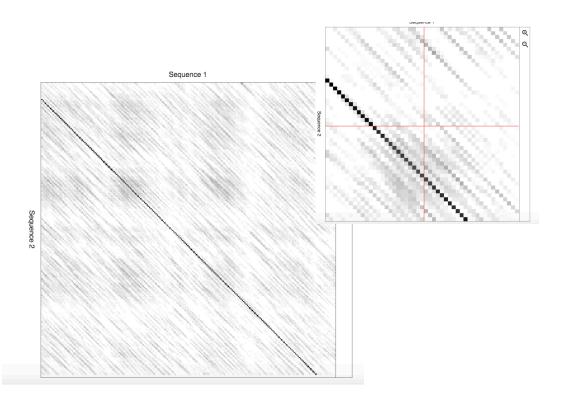
Job title: ref NP_004013  (1230 letters	Wunsch alignment of two seque	nces
RID 4K5VACD3114 (Expires of Query ID NP 004013.1  Description dystrophin isoform D140 Molecule type amino acid Query Length 1230		

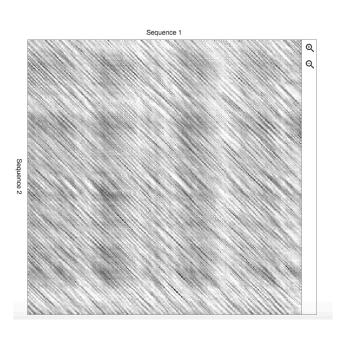




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The dotlet tool compares sequences by the diagonal plot method.





- Sequences with higher similarity show a darker diagonal.
- Lack of diagonal indicates low similarity.

- In their simplest forms, dotplot matrices place dots in the cells where the characters in the two sequences coincide.
- Write a function that given the number of rows and columns creates a numerical matrix.

```
1. def create mat(nrows, ncols):
2.
       """ create matrix given dimensions: number of rows and columns filled wit
  h zeros"""
3.
       mat = []
       for i in range(nrows):
4.
5.
           mat.append([])
6.
           for j in range(ncols):
7.
               mat[i].append(0)
8.
       return mat
```

 The algorithm can be noisy. In order to reduce the noise, filter alignments by a minimum of matches. Apply a scanning window around each position and count the number of matching characters; if they pass a *stringency* threshold keep the alignment.

```
1. def extended dotplot (seq1, seq2, window, stringency):
2.
       """ extended dotplot with window and stringency parameters """
3.
       mat = create mat(len(seq1), len(seq2))
       start = int(window/2)
4.
5.
       for i in range(start, len(seq1) - start):
            for j in range(start, len(seq2)-start):
6.
                matches = 0
7.
                1 = j - start
8.
9.
                for k in range(i-start, i+start+1):
10.
                         if seq1[k] == seq2[1]: matches += 1
11.
                         1 += 1
12.
                         if matches >= stringency: mat[i][j] = 1
13.
       return mat
14.
15.def test():
16.
      s1 = "CGATATAGATT"
17.
      s2 = "TATATAGTAT"
18.
      mat1 = dotplot(s1, s2)
19.
      print dotplot(mat1, s1, s2)
20.
21.
      print("")
      mat2 = extended dotplot(s1, s2, 5, 4)
22.
      print dotplot(mat2, s1, s2)
23.
```

- In pairwise sequence alignment we try to arrange two sequences so that the number of matching characters is maximised. The order of the characters in the sequences cannot be altered.
- There are many solutions for a given input. Thus, this is an optimisation problem where we try to find the best solution among the possible ones.
- In order to select the best solution we need to define a proper objective function.

Input: two sequences (in a well defined alphabet) and an objective function.

Output: optimal pairing of the characters in each sequence; gaps are placed in each sequence to maximise the objective function.

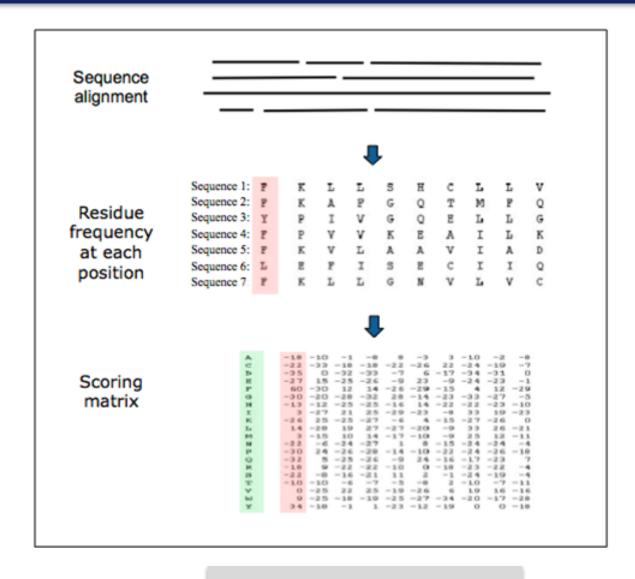
- The problem is highly complex. Consider for simplicity and as an example two sequences of length n.
- The maximum length of the whole alignment is *2n*, obtained by placing gaps all over one of the sequences.
- The total number of solutions is 120 billion solutions!

$$\binom{2n}{n} = \frac{(2n)!}{n!^2}$$
 approximately

Brute-force approaches will not work.

- The objective function attributes a value for each of the solutions. This is also called *score*.
- In this case we have a maximisation problem where we want to find the highest value for the most similar sequences and the lowest values for the most distant or less similar sequences.
- As we have seen before we can use a simple scheme of given 1 to a match and 0 to a mismatch. This will be an additive objective function. From the biological point of view this may not be the most appropriate function.
- Mutations typically affect adjacent positions. It would be important to discriminate between matches, mismatches and gaps. While the first contributes to a better alignment (positive contribution) this is not the case for the other two (negative contribution).

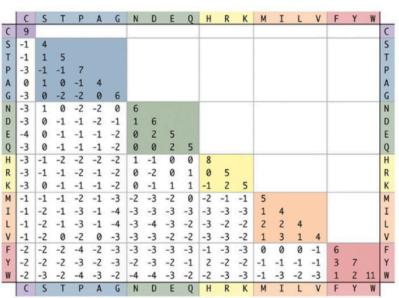
- For DNA/RNA typical values include:
  - Match: +2 or +3
  - Mismatch and gap: -3 or -2
- For protein sequences we have a different alphabets. Aminoacids share physico-chemical properties that allow to group them. So a mismatch between R and A is very different than a mismatch between R and K.
- Substitution matrices capture the different scores between each amino acid pair. It assigns a value for each pair of possible symbols in the alphabet (either amino acid or nucleic acids) excluding gaps.
- For proteins they are calculated based on the probability of finding a given pair of aligned amino-acids in a good alignment over the probability of obtaining such pairing by chance.
- From the biological point of view the introduction of a gap has a bigger impact.
   A gap penalty function defines how to penalize a gap or series of gaps.



Adapted from: EBI Train Online

#### **BLOSUM**

- BLOSUM (BLOcks SUbstitution Matrix) matrix is a substitution matrix used for sequence alignment of proteins. It is based on frequencies of substitutions in blocks of local alignments in related proteins (BLOCKS database).
- Each matrix is tailored to a particular evolutionary distance.
- Example: the scores in the BLOSUM62 matrix are derived using sequences sharing no more than 62% identity.



www.memim.com

# **Affine gap penalty**

- Typical gap penalties have values ranging from -12 to -7 in protein sequences and -3 or -2 in DNA/RNA.
- The gap opening should have a larger penalty. The affine gap penalty model give a different penalty for the opening of the gap and for its extension:
  - $affine\_gap(len) = g + r^*len$ , where g is the cost of gap opening, r the cost of each gap and len the extension of the gap (in symbols).

- The objective function takes into account both substitution matrix and gap penalty.
- Develop a function to implement a substitution matrix given the alphabet, a value for match and a value for mismatch.

```
1. def create submat (match, mismatch, alphabet):
       """ substitution matrix as dictionary """
3.
       sm = \{\}
       for c1 in alphabet:
4.
           for c2 in alphabet:
5.
                if (c1 == c2):
6.
7.
                    sm[c1+c2] = match
8.
                else:
9.
                    sm[c1+c2] = mismatch
10.
            return sm
1. sm = create submat(1, 0 , "ACGT")
2. print (sm)
```

 In practice for protein substitution matrices it is easier to read from a table on an existing file. blosum62.mat provided in the class. Assume the matrix is symmetric and first row contains the symbols in the alphabet.

```
1. def read submat file (filename):
       """read substitution matrix from file """
2.
3.
       sm = \{ \}
       f = open(filename, "r")
4.
5.
       line = f.readline()
       tokens = line.split("\t")
6.
7.
       ns = len(tokens)
8.
       alphabet = []
       for i in range(0, ns):
9.
            alphabet.append(tokens[i][0])
10.
       for i in range(0,ns):
11.
12.
            line = f.readline();
13.
            tokens = line.split("\t");
14.
            for j in range(0, len(tokens)):
                k = alphabet[i]+alphabet[j]
15.
16.
                sm[k] = int(tokens[j])
17.
       return sm
```

Write a function that provides the score of a column alignment or position,
 i.e. between characters c1 and c2. Assume a constant gap penalty g and substitution matrix sm.

```
1. def score_pos (c1, c2, sm, g):
2.    """score of a position (column)"""
3.    if c1 == "-" or c2=="-":
4.        return g
5.    else:
6.        return sm[c1+c2]
```

Write the test code for the alignments:

```
-CAGTGCATG-ACATA

TCAG-GC-TCTACAGA

Match = 2 and Mismatch = -2; gap = -3
```

```
1. def test_DNA():
2.     sm = create_submat(2,-2,"ACGT")
3.     seq1 = "-CAGTGCATG-ACATA"
4.     seq2 = "TCAG-GC-TCTACAGA"
5.     g = -3
6.     print(score_align(seq1, seq2, sm, g))
7.
```

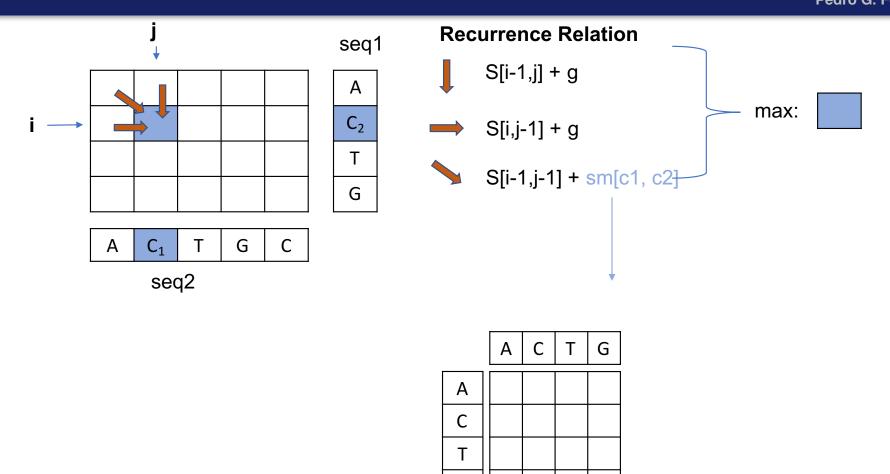
#### Affine gap score

```
def score affinegap (seq1, seq2, sm, g, r):
2.
       res = 0
3.
       ingap1 = False
4.
       ingap2 = False
       for i in range(len(seq1)):
5.
            if seq1[i]=="-":
6.
7.
                if ingap1: res += r
8.
                else:
9.
                    ingap1 = True
10.
                    res += g
11.
            elif seq2[i]=="-":
                if ingap2: res += r
12.
13.
                else:
14.
                    ingap2 = True
15.
                    res += q
16.
            else:
                if ingap1: ingap1 = False
17.
18.
                if ingap2: ingap2 = False
19.
                res += sm[seq1[i] + seq2[i]]
20.
       return res
```

- Dynamic Programming is a general-purpose class of optimisation algorithms based on divide-and-conquer strategy.
- The optimal alignment of two sequences is based on the optimal alignment of its sub-sequences.
- Two sequences A and B of size n and m:
  - \*  $A = a_1 a_2 ... a_n$
  - \*  $B = b_1b_2....b_m$
  - \* Build matrix S where rows indices are elements from A and columns indices are elements from B
  - \* S has n+1 and m+1 dimensions
  - \* Add extra column and extra row in the beginning to represent gaps in all positions of the sequences.
- Fill matrix S so that in each position the element indicates the score of the optimal alignment of the sub-sequences of A and B, considering all the symbols from the beginning until the character represented in the row from A and column from B.
- S<sub>i,j</sub> represents the alignment of a<sub>1</sub>...a<sub>i</sub> and b<sub>1...</sub>b<sub>j</sub>

- Main ideia: fill matrix S cell by cell, using the value of adjacent cells to reach the target cell.
- This means using the previously calculated scores for smaller alignment to calculate the score of the current alignment.
- Recurrence relation:
  - $\circ$   $S_{i,j} = \max(S_{i-1,j-1} + sm(a_i, b_j), S_{i-1,j} + g, S_{i,j-1} + g)$  for all 0 < i <= n and 0 < j <= m
  - $\circ$  sm(c1,c2) substitution score between c1 and c2; g is constant gap penalty.
- Matrix is filled left to right and top to bottom. To calculate S<sub>i,j</sub> you need to have calculated: S<sub>i-1,j</sub> S<sub>i,j-1</sub> S<sub>i-1,j-1</sub>.
- The recurrence relation states that:
  - An alignment is obtained by composition of other alignments.
  - Add an extra column to the previous alignment and compute the new score by adding the previous score with the one from the added column.

#### **Dynamic Programming: Recurrence Relation**



- Recurrence relation:
  - $S_{i,j} = \max(S_{i-1,j-1} + \text{sm}(a_i, b_j), S_{i-1,j} + g, S_{i,j-1} + g)$  for all 0 < i <= n and 0 < j <= m

G

Substitution

matrix

o sm(c1,c2) - substitution score between c1 and c2; g is constant gap penalty.30

- Three ways to add columns to previous alignment (based on recurrence formula):
  - Add column with symbols from both sequences;
  - Add symbol from first sequence and gap;
  - Add gap and symbol from second sequence;
- o Initialize the matrix:
  - $\circ$  Fill first row and column: multiply the number of columns or rows by g;  $S_{i,0} = i * g$

			Sequence B									
				$b_1$	$b_2$	$b_3$	$b_4$	$b_5$				
			gap	Н	G	w	Α	G				
		gap	0	-8	-16	-24	-32	-40				
	$a_1$	Р	-8	-2	-10	-18	-25	-33				
Sequence	$a_2$	Н	-16	0	-4	-12	-20	-27				
Α	$a_3$	S	-24	-8	0	-7	-11	-19				
	$a_4$	W	-32	-16	-8	11	3	-5				
	a <sub>5</sub>	G	-40	-24	-10	3	11	9				

S matrix for the Needleman-Wunsch

Substitution matrix BLOSUM62 and g = -8

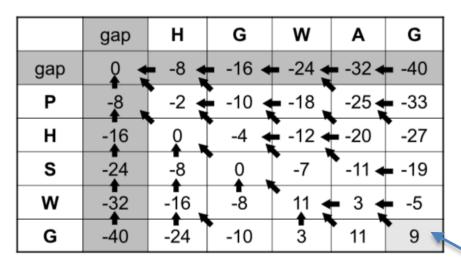
	C	S	Т	P	A	G	N	D	Е	Q	Н	R	K	М	I	L	٧	F	Y	W
С	9																			
S	-1	4																		
Т	-1	1	5																	
P	-3	-1	-1	7																
A	0	1	0	-1	4															
G	-3	0	-2	-2	0	6														
N	-3	1	0	-2	-2	0	6													
D	-3	0	-1	-1	-2	-1	1	6												
Е	-4	0	-1	-1	-1	-2	0	2	5											
Q	-3	0	-1	-1	-1	-2	0	0	2	5										
Н	-3	-1	-2	-2	-2	-2	1	-1	0	0	8									
R	-3	-1	-1	-2	-1	-2	0	-2	0	1	0	5								
K	-3	0	-1	-1	-1	-2	0	-1	1	1	-1	2	5							
М	-1	-1	-1	-2	-1	-3	-2	-3	-2	0	-2	-1	-1	5						
Ι	-1	-2	-1	-3	-1	-4	-3	-3	-3	-3	-3	-3	-3	1	4					
L	-1	-2	-1	-3	-1	-4	-3	-4	-3	-2	-3	-2	-2	2	2	4				
٧	-1	-2	0	-2	0	-3	-3	-3	-2	-2	-3	-3	-2	1	3	1	4			
F	-2	-2	-2	-4	-2	-3	-3	-3	-3	-3	-1	-3	-3	0	0	0	-1	6		
Υ	-2	-2	-2	-3	-2	-3	-2	-3	-2	-1	2	-2	-2	-1	-1	-1	-1	3	7	
W	-2	-3	-2	-4	-3	-2	-4	-4	-3	-2	-2	-3	-3	-1	-3	-2	-3	1	2	11
	С	S	Т	Р	A	G	N	D	E	0	Н	R	K	М	I	L	٧	F	Y	W

Best alignment score

Example:

 $S_{1,1} = \max(S_{0,0} + sm("H","P"), S_{0,1} + g, S_{1,0} + g) = \max(0-2, -8-8, -8-8) = -2$ 

- The previous procedure is sufficient to calculate the score of the best alignment but not the alignment it self. We need to keep track of the decisions that define the path to reach from the beginning of the sequences to the best alignment.
- Keep a matrix called trace-back (T) to keep all the three possible (3 symbol alphabet) moves at each cell. From T we can recover the alignment. Start from the lower-right cell and trace-back to upper-left cell. Moves:
  - Diagonal: add characters from both sequences.
  - Vertical: add character from first sequence and gap to the second.
  - Horizontal: add gap from the first sequence and character from the second.



From Bioinformatics Algorithms, Rocha & Ferreira

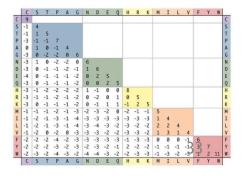
 The process of recovering the optimal alignment from the trace-back information in the Needleman-Wunsch.

	gap	Н	G	W	Α	G
gap	0 <	-8	16 ◆	-24	<b>-</b> -32 <b>&lt;</b>	<b>-</b> -40
Р	-8	-2	-10	<b>-</b> -18	-25∢	<b>-</b> -33
Н	-16	Q	-4	-12	-20	-27
S	-24	-8	0	-7	-11 ∢	<b>-</b> -19
w	-32	-16	-8	11	<b>-</b> 3 <b>&lt;</b>	<b>-</b> -5
G	-40	-24	-10	3	11	9

Best alignment:

Score of the best alignment:

From Bioinformatics Algorithms, Rocha & Ferreira



#### **Needleman-Wunsch Algorithm**

Fill matrices S and T (1 for diagonal, 2 for vertical and 3 for horizontal).

```
def needleman Wunsch (seq1, seq2, sm, q):
2.
       """Global Alignment"""
3.
       S = [[0]]
4.
       T = [[0]]
5.
       # initialize gaps in rows
6.
       for j in range (1, len(seq2)+1):
           S[0].append(g * j)
7.
8.
           T[0].append(3)
       # initialize gaps in cols
9.
10.
       for i in range(1, len(seq1)+1):
11.
           S.append([g * i])
12.
           T.append([2])
       # apply the recurrence to fill the matrices
13.
14.
       for i in range(0, len(seq1)):
15.
            for j in range(len(seq2)):
16.
                s1 = S[i][j] + score pos (seq1[i], seq2[j], sm, q);
17.
                s2 = S[i][j+1] + q
18.
                s3 = S[i+1][j] + q
19.
                S[i+1].append(max(s1, s2, s3))
20.
                T[i+1].append(max3t(s1, s2, s3))
21.
       return (S, T)
22.
23. def max3t (v1, v2, v3):
24.
       """Provides the integer to fill in T"""
25.
       if v1 > v2:
26.
           if v1 > v3: return 1
27.
           else: return 3
28.
       else:
29.
           if v2 > v3: return 2
30.
           else: return 3
```

#### **Needleman-Wunsch Algorithm**

- Recover the optimal alignment from T and A and B.
- Starts bottom right corner.
- Diagonal symbol in T adds symbols form A and B to the alignment.
- A vertical cell in T leads to move to previous low and adds to the alignment a symbol from A in the respective row and gap from
   B. Vice-versa if horizontal cell.

```
1. def recover align (T, seq1, seq2):
2.
       # alignment are two strings
       res = ["", ""]
       i = len(seq1)
5.
       j = len(seq2)
6.
       while i>0 or j>0:
           if T[i][j]==1:
7.
               res[0] = seq1[i-1] + res[0]
8.
               res[1] = seq2[j-1] + res[1]
9.
10.
                i -= 1
11.
                i -= 1
12.
           elif T[i][i] == 3:
13.
                res[0] = "-" + res[0]
14.
                res[1] = seq2[j-1] + res[1]
15.
                i -= 1
16.
           else:
17.
                res[0] = seq1[i-1] + res[0]
                res[1] = "-" + res[1]
18.
                i -= 1
19.
20.
       return res
```

#### **Needleman-Wunsch Algorithm**

```
1. def print mat (mat):
2.
       for i in range(0, len(mat)):
3.
           print(mat[i])
4.
5. def test global alig():
       sm = read submat file("blosum62.mat")
6.
       seq1 = "PHSWG"
7.
       seq2 = "HGWAG"
8.
9.
       res = needleman Wunsch (seq1, seq2, sm, -8)
10.
       S = res[0]
11.
       T = res[1]
       print("Score of optimal alignment:", S[len(seq1)][len(seq2)])
12.
       print mat(S)
13.
       print mat(T)
14.
15.
       alig = recover align(T, seq1, seq2)
16.
       print(aliq[0])
17.
       print(aliq[1])
```

- In the local alignment we are interested in the best partial alignment of the sub-sequences from the two sequences, which maximize the objective function (score).
- The *Smith-Waterman* is the algorithm for local sequence alignment. This algorithm reformulates the recurrence relation used in the DP.
- If the best of the three alternatives leads to a negative score, this means that in that position we need to restart the alignment from this position onwards, ignoring the previous parts of the sequences.
- Recurrence relation:
  - $\circ$   $S_{i,j} = \max(S_{i-1,j-1} + sm(a_i, b_j), S_{i-1,j} + g, S_{i,j-1} + g, 0)$  for all 0 < i <= n and 0 < j <= m
  - $\circ$  sm(c1,c2) substitution score between c1 and c2; g is constant gap penalty.

- Initialization of matrix S: first row and column filled with zero.
- The best alignment can occur in any cell of the matrix, corresponding to the highest score value in S.
- Multiple alternative best alignments may occur.

	gap	Н	G	W	Α	G
gap	0	0	0	0	0	0
Р	0	0	0	0	0	0
Н	0	8	0	0	0	0
S	0	0	8	0	1	0
W	0	0	0	19	11	3
G	0	0	6	11	19	17

#### **Examples:**

```
S_{1,1} = max (S_{0,0} + sm("H","P"), S_{0,1} + g, S_{1,0} + g, 0) = max(0-2, -8-8, -8-8, 0) = 0

S_{4,3} = max (S_{3,2} + sm("H","P"), S_{3,3} + g, S_{4,2} + g, 0) = max(8+11, 0-8, 0-8, 0) = 19
```

From Bioinformatics Algorithms, Rocha & Ferreira

- The trace-back matrix T contains four possible values: three previous values (diagonal, vertical, horizontal) and an extra value to the cases where the alignment is terminated (correspond to cells in S with 0).
- The recovery process starts on the cell with highest value and proceeds until the upper left corner is reached.

	gap	Н	G	W	Α	G				
gap	0	0	0	0	0	0				
Р	0	0	0	0	0	0				
Н	0	8	0	0	0	0				
S	0	0	8	0	1	0				
W	0	0	0	19	<b>-</b> 11 <b>&lt;</b>	<b>-</b> 3				
G	0	0	6	/11	19	17				
		/ Best alignments:								
			HSW HSWG HGW HGWA							

#### **Smith-Waterman Algorithm**

Fill matrices S and T (1 for diagonal, 2 for vertical and 3 for horizontal and 0 for termination).

```
def smith Waterman (seq1, seq2, sm, g):
        """Local alignment"""
2.
3.
        S = [[0]]
       T = [[0]]
4.
5.
        maxscore = 0
6.
        # first row filled with zero
7.
        for j in range (1, len(seq2)+1):
8.
            S[0].append(0)
9.
            T[0].append(0)
10.
        # first column filled with zero
11.
        for i in range (1, len(seq1)+1):
12.
            S.append([0])
13.
            T.append([0])
        for i in range(0, len(seq1)):
14.
15.
            for j in range(len(seq2)):
16.
                s1 = S[i][j] + score pos (seq1[i], seq2[j], sm, g);
17.
                s2 = S[i][j+1] + q
18.
                s3 = S[i+1][j] + q
19.
                b = max(s1, s2, s3)
20.
                if b <= 0:
21.
                    S[i+1].append(0)
22.
                    T[i+1].append(0)
23.
                else:
24.
                    S[i+1].append(b)
25.
                    T[i+1].append(max3t(s1, s2, s3))
26.
                    if b > maxscore:
27.
                        maxscore = b
28.
        return (S, T, maxscore)
```

#### **Smith-Waterman Algorithm**

```
1. def recover align local (S, T, seq1, seq2):
2.
       """recover one of the optimal alignments"""
       res = ["", ""]
3.
       """determine the cell with max score"""
4.
5.
       i, j = max mat(S)
       """terminates when finds a cell with zero"""
6.
7.
       while T[i][j]>0:
8.
           if T[i][i]==1:
               res[0] = seq1[i-1] + res[0]
9.
10.
               res[1] = seq2[j-1] + res[1]
               i = 1
11.
                i -= 1
12.
           elif T[i][j] == 3:
13.
14.
               res[0] = "-" + res[0];
15.
               res[1] = seq2[j-1] + res[1]
16.
               i −= 1
17.
            elif T[i][j] == 2:
18.
                res[0] = seq1[i-1] + res[0]
19.
                res[1] = "-" + res[1]
20.
                i -= 1
21.
       return res
```

#### **Smith-Waterman Algorithm**

```
1. def test local aliq():
2.
       sm = read submat file("blosum62.mat")
       seq1 = "PHSWG"
3.
      seq2 = "HGWAG"
4.
5.
       res = smith Waterman(seq1, seq2, sm, -8)
6.
       S = res[0]
7.
       T = res[1]
       print("Score of optimal alignment:", res[2])
8.
9.
       print mat(S)
10.
       print mat(T)
       alinL= recover align local(S, T, seq1, seq2)
11.
       print(alinL[0])
12.
13.
    print(alinL[1])
```

# **Exercises and Weekly Assignment**

- Write a function that given two sequences creates a dot plot by filling the matrix with 1s where there is a match and 0s where there is a mismatch. Fill the function dotplot() in dotplots.py.
- Write a function that given the dotplot matrix and the two respective input sequences does the pretty printing of the matrix. Fill the function print\_dotplot() in dotplots.py.
- Test the respective functions above.

# **Exercises and Weekly Assignment**

- Write a function score\_align that given two sequences calculates the overall score. Use the function score\_pos() to score every pair of symbols from the two sequences. Sum this scores and return its value. Assume sequences have equal length. Complete function score\_align() in sequence\_alignments.py.
- Write a function max\_mat() that receives as input a matrix with numbers and returns the indices where the maximum value is found. Complete in sequence\_alignments.py.