

## Question 1 of 16

Find the sum of the coefficients of the polynomial obtained after expanding and collecting the terms of the product:

$$(1 - 3x + 3x^2)^{743}(1 + 3x - 3x^2)^{744}$$

**SUBMIT ANSWER**

*and proceed to next question*

## Question 2 of 16

You roll two dice.

What is the probability the difference between the high and low roll is exactly 4, to four decimal places?

**SUBMIT ANSWER**

*and proceed to next question*

**PREVIOUS**

### Question 3 of 16

Suppose there is an asset  $X$  whose current value is \$90, and we know its value in one year will be \$100. There is an option that pays \$1 when  $X$  hits \$97 for the first time.

Compute the value of this option to 4 decimal places.

**SUBMIT ANSWER**

*and proceed to next question*

**PREVIOUS**

## Question 4 of 16

Let  $X$  and  $Y$  be two standard independent normal variables, i.e.,  $X \sim N(0,1)$ ,  $Y \sim N(0,1)$ , and  $\rho(X,Y) = -0.72$ .

Calculate  $E[3X+Y|X-Y=1]$

**SUBMIT ANSWER**

*and proceed to next question*

**PREVIOUS**

## Question 5 of 16

(Part 1 of 2) - Students from two schools participated in a tournament. Each contestant played each other contestant once. There were ten times as many students from school A but they were able to win only 4.5 times as many points as the students from school B.

a) How many students from school B participated?

**SUBMIT ANSWER**

*and proceed to next question*

**PREVIOUS**

## Question 6 of 16

(Part 2 of 2) - Students from two schools participated in a tournament. Each contestant played each other contestant once. There were ten times as many students from school A but they were able to win only 4.5 times as many points as the students from school B.

b) How many points did they win?

**SUBMIT ANSWER**

*and proceed to next question*

**PREVIOUS**

## Question 7 of 16

Suppose the current price of a stock is \$100. The price has probability 70% of increasing to \$110 and probability 30% of declining to \$90 in one year. Assume the risk-free rate is 5%.

Calculate the value of a call option struck at \$100 that matures in one year to four decimal places.

**SUBMIT ANSWER**

*and proceed to next question*

**PREVIOUS**

## Question 8 of 16

Suppose  $X$ , and  $Y$  are independent Brownian Motions that at time 0 are both equal to 1. Consider the first time,  $T$ , the  $Y$  process hits 0.

What is the probability that  $X(T) > 0$ ?

**SUBMIT ANSWER**

*and proceed to next question*

**PREVIOUS**



## Question 9 of 16

A player A tosses 100 coins. B tosses 99 coins. B wins if he has at least as many heads as A.

What is the probability that B wins?

**SUBMIT ANSWER**

*and proceed to next question*

**PREVIOUS**

## Question 10 of 16

The number 123456789(10)(11)(12)(13)(14) is written in the base 15, that is the number is equal (in the base 10) to

$$14 + 13 \cdot 15 + 12 \cdot 15^2 + 11 \cdot 15^3 + \dots + 2 \cdot 15^{12} + 15^{13}$$

Without using computers, calculators or other computation devices, calculate the remainder upon dividing this number by 7.

**SUBMIT ANSWER**

*and proceed to next question*

**PREVIOUS**

## Question 11 of 16

There is a 6-faced fair die.

What is the expected number of throws before getting three same numbers in a row?

**SUBMIT ANSWER**

*and proceed to next question*

**PREVIOUS**

## Question 12 of 16

The population of an endangered species at year  $N$  is denoted by

$$P_N$$

Assume

$$P_0 = 100$$

$P$  updates by the rule

$$P_{n+1} = 2 * P_n$$

with probability  $1/2$

,

$$P_{n+1} = 0$$

with probability  $1/2$ .

What is the expected time until the species dies out?

**SUBMIT ANSWER**

*and proceed to next question*

**PREVIOUS**

## Question 13 of 16

A family has two children. The genders of the first-born and second-born are independent (with boy and girl equally likely). The seasons in which the children were born in are independent, with all 4 seasons (winter, spring, summer, fall) equally likely.

Find the probability to 4 decimal places that both children are girls, given that at least one of the two is a girl who was born in winter.

**SUBMIT ANSWER**

*and proceed to next question*

**PREVIOUS**

## Question 14 of 16

Without using computers, calculators or other computation devices, find the integer part of  $X$  (i.e.  $[X]$ ) where  $X$  is given by the following sum:

$$X = \sum_{i=4}^{1,000,000} \frac{1}{\sqrt[3]{i}}$$

**SUBMIT ANSWER**

*and proceed to next question*

**PREVIOUS**

## Question 15 of 16

(Part 1 of 2) - There are 3 random variables  $X$ ,  $Y$  and  $Z$ . The correlation between  $X$  and  $Y$  is 0.8 and correlation between  $X$  and  $Z$  is 0.5.

Calculate the minimum correlation between  $Y$  and  $Z$ , to four decimal places.

**SUBMIT ANSWER**

*and proceed to next question*

**PREVIOUS**

## Question 16 of 16

(Part 2 of 2) - There are 3 random variables  $X$ ,  $Y$  and  $Z$ . The correlation between  $X$  and  $Y$  is 0.8 and correlation between  $X$  and  $Z$  is 0.5.

Calculate the maximum correlation between  $Y$  and  $Z$ , to four decimal places.

**SUBMIT ANSWER**

*(Last question! Answering this will complete the challenge.)*

**PREVIOUS**