

# Tabla de Propiedades y algunas Transformadas de Fourier

|    | $f(t) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} F(\omega) e^{j\omega t} d\omega$   | $F(\omega) = \int_{-\infty}^{+\infty} f(t) e^{-j\omega t} dt$                              |
|----|--|--|
| 1  | $a_1 f_1(t) + a_2 f_2(t)$  | $a_1 F_1(\omega) + a_2 F_2(\omega)$  |
| 2  | $f(at), a \neq 0$  | $\frac{1}{ a } F\left(\frac{\omega}{a}\right)$   |
| 3  | $f(t \mp t_0)$   | $e^{\mp j\omega t_0} F(\omega)$  |
| 4  | $e^{\pm j\omega_0 t} f(t)$   | $F(\omega \mp \omega_0)$   |
| 5  | $f(t) \cdot \cos(\omega_0 t)$  | $\frac{1}{2} F(\omega - \omega_0) + \frac{1}{2} F(\omega + \omega_0)$                      |
| 6  | $f(t) \cdot \sen(\omega_0 t)$  | $\frac{1}{2j} F(\omega - \omega_0) - \frac{1}{2j} F(\omega + \omega_0)$                    |
| 7  | $F(t)$   | $2\pi f(-\omega)$  |
| 8  | $\frac{d^n f(t)}{dt^n}, n \in \mathbb{N}$  | $(j\omega)^n F(\omega)$  |
| 9  | $\int_{-\infty}^t f(t') dt'$   | $\frac{1}{j\omega} F(\omega) + \pi F(0) \delta(\omega)$                                    |
| 10 | $(-jt)^n f(t), n \in \mathbb{N}$   | $\frac{d^n F(\omega)}{d\omega^n}$  |
| 11 | $\frac{f(t)}{-jt}$   | $\int_{-\infty}^{\omega} F(\omega') d\omega'$  |
| 12 | $f_1(t) * f_2(t)$  | $F_1(\omega) \cdot F_2(\omega)$  |
| 13 | $f_1(t) \cdot f_2(t)$  | $\frac{1}{2\pi} F_1(\omega) * F_2(\omega)$   |
| 14 | $\int_{-\infty}^{\infty} f_1(t) \overline{f_2(t)} dt$  | $\frac{1}{2\pi} \int_{-\infty}^{\infty} F_1(\omega) \cdot \overline{F_2(\omega)} d\omega$  |
| 15 | $e^{-at} u(t)$   | $\frac{1}{a + j\omega}$  |
| 16 | $e^{-a t }$  | $\frac{2a}{a^2 + \omega^2}$  |
| 17 | $e^{-at^2}, a \neq 0$  | $\sqrt{\frac{\pi}{a}} e^{-\frac{\omega^2}{4a}}$  |
| 18 | $A \cdot p_{2T}(t)$  | $2AT \text{sinc}(\omega T)$  |
| 19 | $\Delta(t) = \begin{cases} A \left(1 - \frac{ t }{T}\right), &  t  < T \\ 0, &  t  > T \end{cases}$  | $AT \text{sinc}^2\left(\frac{\omega T}{2}\right)$  |
| 20 | $\frac{t^{n-1}}{(n-1)!} e^{-at} u(t)$  | $\frac{1}{(j\omega + a)^n}$  |
| 21 | $e^{-at} \sen \omega_0 t \cdot u(t)$   | $\frac{\omega_0}{(a + j\omega)^2 + \omega_0^2}$  |
| 22 | $e^{-at} \cos \omega_0 t \cdot u(t)$   | $\frac{a + j\omega}{(a + j\omega)^2 + \omega_0^2}$   |
| 23 | $k \delta(t)$  | $k$  |
| 24 | $k$  | $2\pi k \delta(\omega)$  |
| 25 | $\text{sgn}(t)$  | $\frac{2}{j\omega}$  |
| 26 | $u(t)$   | $\frac{1}{j\omega} + \pi \delta(\omega)$   |
| 27 | $\cos \omega_0 t$  | $\pi [\delta(\omega - \omega_0) + \delta(\omega + \omega_0)]$                              |
| 28 | $\sen \omega_0 t$  | $j\pi [\delta(\omega + \omega_0) - \delta(\omega - \omega_0)]$                             |
| 29 | $e^{\pm j\omega_0 t}$  | $2\pi \delta(\omega \mp \omega_0)$   |
| 30 | $\sum_{n=-\infty}^{\infty} C_n e^{jn\omega_0 t}, C_n = \frac{1}{T} \int_{-T/2}^{T/2} f(t) e^{-jn\omega_0 t} dt, \omega_0 = \frac{2\pi}{T}$ | $2\pi \sum_{n=-\infty}^{\infty} C_n \delta(\omega - n\omega_0)$                            |
| 31 | $\sum_{n=-\infty}^{\infty} \delta(t - nT)$   | $\omega_0 \sum_{n=-\infty}^{\infty} \delta(\omega - n\omega_0), \omega_0 = \frac{2\pi}{T}$ |
| 32 | $t^n, n \in \mathbb{N}$  | $2\pi j^n \frac{d^n \delta(\omega)}{d\omega^n}$  |