

## **Circuit Theory and Electronics Fundamentals**

Masters of Aerospace Engineer, Técnico, University of Lisbon

Laboratory Report

Group 37

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# 1 Introduction

The objective of this laboratory assignment is to choose the best architecture of the circuit in order to build a Bandpass filter using OP AMP. This assignment allowed us to deal with important concepts such as OP AMP and its diverse utility in circuits. We did this while paying attention to the merit of the project designed. This merit is calculated exactly as the next equation:

$$M = \frac{1}{cost * (gaindeviation + centralfrequencydeviation + 1e - 6)} \quad (1)$$

Being the cost the following:

- cost = cost of resistors + cost of capacitors + cost of transistors
- cost of resistors = 1 monetary unit (MU) per kOhm
- cost of capacitors = 1 MU/ $\mu$ F
- cost of transistors = 0.1 MU per transistor

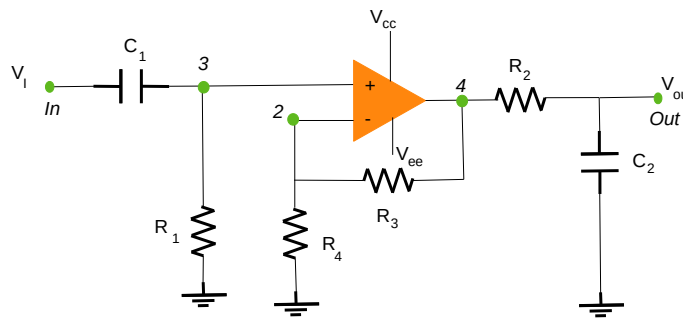


Figure 1: Main circuit

The constants values used are expressed in the following table.

Name - Value	
C1	2.200000e-07
C2	1.100000e-07
R1	1.000000e+03
R2	1.000000e+03
R3	1.000000e+05
R4	1.000000e+03
Vcc	1.000000e+01

Table 1: Inicial Values

In Section 2, a theoretical analysis of the circuit is presented. In Section 3, the circuit is analysed by simulation, and in Section 4 the results are compared to the theoretical results obtained in Section 2. Next in Section 5 we show the cost and merit attributed to our circuit. To finish, the conclusions of this study are

outlined in Section 6.

## 2 Theoretical Analysis

In this section we will analyse theoretical our bandpass filter using OP AMP.

To do so, and because there were several things to be analysed, we divided the theoretical analysis in the following subsections that explain the different sectors that our circuit has and also each one will be detailed separately.

### 2.1 Transfer function computation

Name - Value	
LowFreq BandPass	4.545455e+03
HighFreq BandPass	9.090909e+03
Central Freq	6.428243e+03

Table 2: BANDPASS FREQUENCY

Name - Value	
Central Freq (Hz)	1.023087e+03
Gain Central Freq (dB)	3.656460e+01

Table 3: WO FREQUENCY GAIN

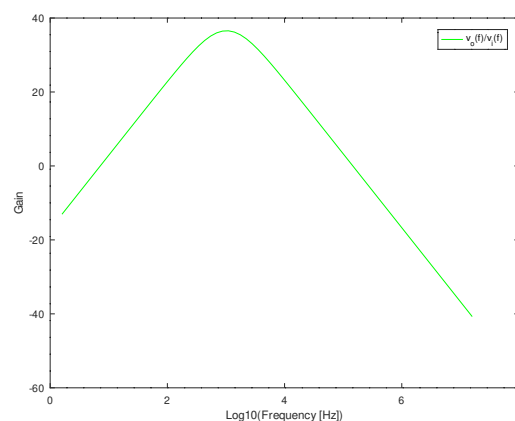


Figure 2: Gain

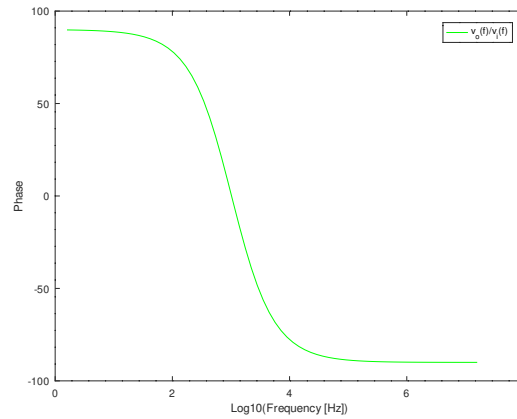


Figure 3: Phase

## 2.2 Input and Output Impedances

Name - Value	
Z in	1.000000e+03 + -7.071068e+02j
Z out	6.666667e+02 + -4.714045e+02j

Table 4: IMPEDANCES

In this section, a theoretical analysis of the circuit shown in section 1 was conducted. The OP Amp was considered ideal (internal impedance between  $v_+$  and  $v_-$  is infinite, which means no current flows through it and  $v_{os}=0$  or in other words  $v_+ = v_-$ ). So, in order to build a bass pand filter, a capactor was connected in series (C1) with the input voltage which will function as a high pass filter (for low frequencies, the impedance goes to infinity and the capacitor is basically an open circuit) and other capacitor (C2) was connected in parallel with the output voltage, functioning as a low pass filter (for high impedances, the impedance goes to 0 and the capacitor is basically a short circuit). To sum up, this circuit consists of a high pass filter, a signal amplifier and a low pass filter in series.

## 3 Simulation Analysis

In this section, Ngspice was used in order to simulate the Bandpass Filter. A brief description of the circuit modeled in NGspice is going to be presented and a comparison between the values obtained in NGspice and the ones in Octave is going to be done as well. In order to do that, we used the model  $\mu A741$  from Texas In-struments to represent the OP AMP. The measurement of these parameters and the overall performance of the circuit is represented in the beggining of the 5.

### 3.1 Circuit simulation

We started the simulation by designing the circuit in NGspce, having as start point the circuit presented in Section 1. Then, the results were calculated and are represented in the following table:

Name - Value	
Gain	36.5323
Central Frequency	1000
Gain deviation	32.9164
Central frequency deviation	0

Table 5: Results NGSpice

Consequently, the phase and the gain were computed. Is also important to remember that the main goal of this assignment was to design a band pass filter, meaning that this filter should cut both low an very high frequencies.

The following graphs represent the results obtained from simulation in NGSpice of the gain and phase:

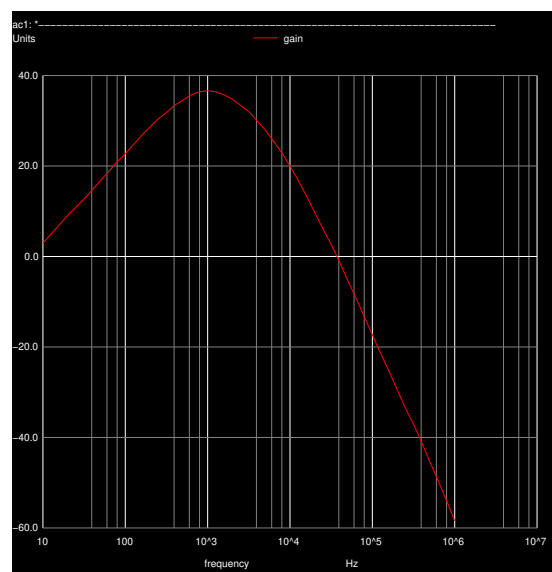


Figure 4: Gain

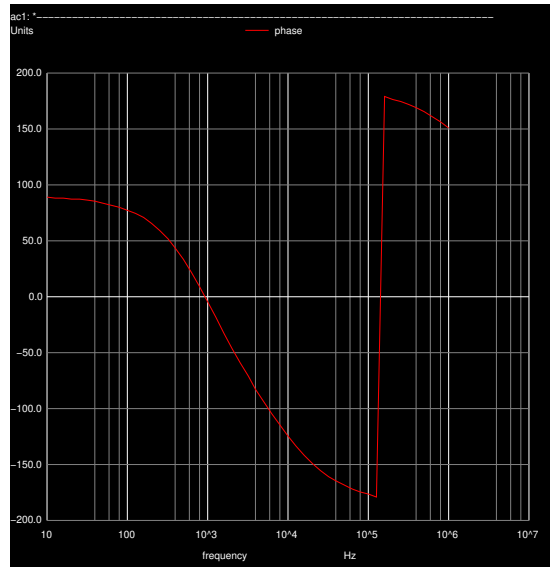


Figure 5: Phase

### 3.2 Input and Output Impedances

The following table represents the input impedance obtained from simulation in NGSpice:

Name - Value	
Zin	999.002 + -7.3282 j

Table 6: Zin

The result obtained for the input impedance, considering the value in Ohm's, is quite high, which turns out to be very beneficial for the gain, because the voltage in node 2 must be as similar to  $V_{in}$  as possible. Using a voltage divider, the only way to achieve this was to have a very high resistance value.

The following table represents the output impedance obtained from simulation in NGSpice:

Name - Value	
Zo	0.0522978 + -7.23396 j

Table 7: Zout

In regard to the output impedance, an opposite deduction to the one made for the input impedance is needed. Using again a voltage divider, the output impedance must be as low as possible, in order for the output voltage to be as high as possible.

## 4 Comparison

In this section a global comparison of the two approaches is created, with the chosen values for the constants. The following table represents the comparison between the results obtained from Octave and from simulation in NGSpice:

Name - Value	
C1	2.200000e-07
C2	1.100000e-07
R1	1.000000e+03
R2	1.000000e+03
R3	1.000000e+05
R4	1.000000e+03
Vcc	1.000000e+01

Table 8: Octave

Name - Value	
Gain	36.5323
Central Frequency	1000
Gain deviation	32.9164
Central frequency deviation	0

Table 9: NGSpice

Table 10: Cost and Merit

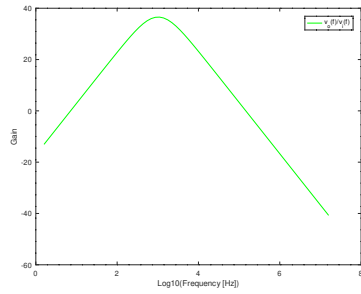
Name - Value	
Gain	36.5323
Central Frequency	1000
Gain deviation	32.9164
Central frequency deviation	0

Table 11: Results NGSpice

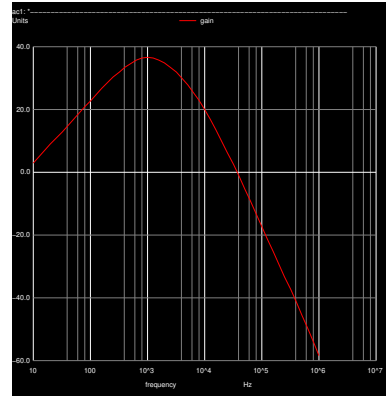
As seen in the previous table, as requested, we were able to compute the passband frequency in a simulation analysis using the measure function and the central frequency in the theoretical analysis as explained in Section 2. We have to consider that the OP-AMP model chosen is far more complex in Ngspice than in Octave. The different calculation methods lead to the difference between both methods, being that the calculated and simulated impedances have the same issues.

Next we present both theoretical and simulation graphs of the frequency response of the gain and the phase side by side.



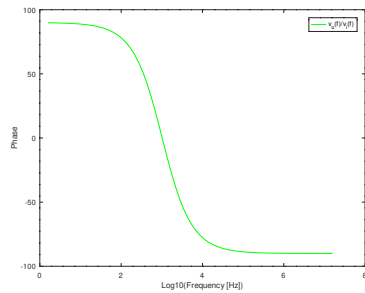


(a) OCTAVE

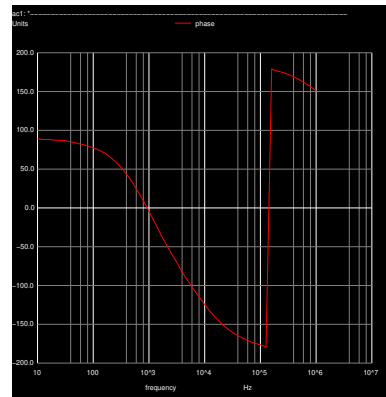


(b) NGSPICE

Figure 6: Gain



(a) OCTAVE



(b) NGSPICE

Figure 7: vo1f

In general, in terms of the graphs, we achieved satisfactory results. When an initial comparison of the gain response is executed, using the shape of the graph, isn't difficult to realise that they have a similar behaviour. As seen in the upper graphs, in the initial section, there is a constant slope of +20dB/dec. After that, exists a small pass band, that is also the region where the central frequency is achieved, and a last part with a slope of -20dB/dec.

When it comes to the lower graphs, in the phase response, both plots differ. This is because our theoretical model does not predict the existence of capacitors in the OP AMP, as it idealises the gain as being purely real, i.e, there's no shift in phase. In reality, because the OP AMP has two capacitors, it is expected that in the phase frequency response plot each would introduce a shift of  $-90^\circ$ , making the overall phase to go down to  $-270^\circ = +90^\circ$ . As we can observe from the initial table of this Section ( 4) we have small relative errors

for the values of interest (the impedances, the total gain and the central frequency). This somehow proves that, even though the OPAMPs are made of dozens of components, some of them non-linear, we can predict with a fairly simple model its behaviour.

## 5 Merit Results

From the results obtained through the Ngspice simulation and considering we used the data shown in table 1, we can compute the merit using the formula given in the lab assignment, represented in the Introduction.

The values of cost and merit are represented in the next table:

Name - Value	
Cost	2.639850e+02
Merit	1.428277e-04

Table 12: Octave

Name - Value	
Cost	263.985
Merit	0.000115082

Table 13: NGspice

Table 14: Cost and Merit

To obtain the best values for the circuit, we've used the matlab simulink to optimize them for the best merit.

## 6 Conclusion

In this laboratory assignment, the goal specified in the introduction has been achieved with a great merit. All analyses have been performed both theoretically using the Octave maths tool and by circuit simulation using the Ngspice tool. When comparing these last two we conclude that there aren't any disparity between the results and therefore no errors associated. So, we conclude that the architecture that we used can be validated.