

# Statistical Modeling and Inference for Climate Applications

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## 1. Bayesian Inference

- Hierarchical Model

$$\text{Data} = Y(\mathbf{s}_i, t)$$

$$\text{Process} = \alpha(\mathbf{s}_i, t)$$

$$\text{Parameters} = \boldsymbol{\theta}$$

$$\begin{aligned} [\text{Data}, \text{Process}, \text{Parameters}] &= [\text{Data}|\text{Process}, \text{Parameters}] \\ &\times [\text{Process}|\text{Parameters}] \\ &\times [\text{Parameters}] \end{aligned}$$

- Posterior Distribution

$$[\boldsymbol{\theta}|\mathbf{Y}] \propto \int [\mathbf{Y}|\boldsymbol{\alpha}, \boldsymbol{\theta}] [\boldsymbol{\alpha}|\boldsymbol{\theta}] [\boldsymbol{\theta}] d\boldsymbol{\alpha}$$

## 2. Spatial Models

Model the joint distribution for the spatial field  $\mathbf{Y}_t$

- Covariance model  
Model  $Cov(Y(\mathbf{s}_i, t), Y(\mathbf{s}_j, t))$  as a function of spatial distance
- Spatial random effects  
Model  $Y(\mathbf{s}_i, t)$  as a linear combination of a low-dimensional random vector and spatial basis functions.
- Conditionally-specified model  
Specify conditional distributions given neighboring values

$$Y(\mathbf{s}_i, t)|\mathbf{y}_t(N_i)$$

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