

# Data Security and Encryption

数据安全与加密

Xitian Huang

6 August 2022

# Data Leak

## Shanghai National Police Database

- <https://breached.to/>
- Info ~1 Billion Chinese Citizens
- 10 BTC (200,000 USD or 1,300,000 RMB)

# 2022 - SHGA Shanghai Gov National Police database

by ChinaDan - Thursday June 30, 2022 at 08:55 AM

ChinaDan



BreachForums User

MEMBER

Posts: 5  
Threads: 1  
Joined: Jun 2022  
Reputation: 183

June 30, 2022, 08:55 AM (This post was last modified: July 3, 2022, 10:25 AM by Muffin. *Edit Reason: Locked by staff due to all # the spam*)

In 2022, the Shanghai National Police (SHGA) database was leaked. This database contains many TB of data and information on Billions of Chinese citizens.

Sell: Shanghai GOV (SHGA.gov.cn) National Police Database

Host: <http://oss-cn-shanghai-shga-d01-a.ops.ga.sh/>  
Data leaked from these tables:

----TABLES----

person\_address\_label\_info\_slave QFpD25bKTJ2eQBxcbe2Aaw 90 0 546148916 0 172.2gb  
172.2gb  
nb\_theme\_address\_merge\_tracks\_slave -bUMVB1uRRusUbbqZepEpA 300 0 37483779369 4  
22.4tb 22.4tb  
nb\_theme\_address\_case\_dwd\_test 7COIWTt7QU-YPwWub8z\_SQ 150 0 22375506 1749307 25.2gb  
25.2gb  
nb\_theme\_address\_company\_dwd-total fpnmEYB9SI6WevHnZIEwIA 150 0 1842856 0 2.8gb  
2.8gb  
nb\_theme\_address\_case\_dwd-total 7X8oNqULQnWFLpzHDaUTbg 150 0 1214119253 0 1tb 1tb  
nb\_theme\_address\_company\_dwd\_test g5f614LGQcGL3oQ60N2Bbw 150 0 2017931 0 4.3gb  
4.3gb  
person\_address\_label\_info\_master t64pp9WnS3maY9jBjzTtiw 90 0 969830088 0 282.8gb  
282.8gb

## Data Details:

Databases contain information on 1 Billion Chinese national residents and several billion case records including:

- Name
- Address
- Birthplace
- National ID Number
- Mobile number
- All Crime / Case details

1 Billion Chinese national residents and several billion case records



**UPDATE: Per request, sample size increased to 750k (250k for each of the 3 main index): <https://gofile.io/d/sCggGC>**

Staff update: Due to the chances of the file being reported to gofile, uploaded the sample to our servers: [https://cdn.breached.to/shga\\_sample\\_750k.tar.gz](https://cdn.breached.to/shga_sample_750k.tar.gz)

**PRICE: I am selling all of this data for 10BTC (\$200k USD)**

省长沙市浏阳市", "IDNO": "430181199712035426", "IDTYPE": "01", "QUERY\_STRING": " 湖南省长沙市浏阳市 24 97 1997 ", "R  
省商丘市虞城县", "EDEGREE": "初中", "HEIGHT": "160", "IDNO": "411425198807157221", "IDTYPE": "01", "NATION": "汉", "PHOTO  
省淮安市盱眙县", "EDEGREE": "学龄前儿童", "ESCU": "未服兵役", "HHPLACE": "江苏省盱眙县管仲镇祖窑村井西组11号", "IDNO": "320830  
省天水市秦安县", "HHPLACE": "甘肃省秦安县兴国镇青年西路地税局家属楼2号楼1单元502室", "IDNO": "620522198601090011", "IDTYPE  
省白银市白银区", "IDNO": "620402199005110462", "IDTYPE": "01", "QUERY\_STRING": " 甘肃省白银市白银区 31 90 1990 ", "R  
壮族自治区南宁地区宾阳县", "IDNO": "452123198504281021", "IDTYPE": "01", "QUERY\_STRING": " 广西壮族自治区南宁地区宾阳县  
省黄冈地区黄梅县", "HEIGHT": "158", "IDNO": "42213019430810196x", "IDTYPE": "01", "PROF": "粮农", "QUERY\_STRING": " 湖北  
省温州市苍南县", "HHPLACE": "浙江省苍南县灵溪镇联进村182-183号", "IDNO": "330327194711033513", "IDTYPE": "01", "NATION": "  
福建省福州市晋安区", "IDNO": "350111191001070158", "IDTYPE": "01", "QUERY\_STRING": " 福建省福州市晋安区 111 10 1910 ",  
市长宁区", "EDEGREE": "高中", "HEIGHT": "163.0", "HHPLACE": "上海市闵行区龙吴路5599弄171号301室", "IDNO": "31010519670627  
省黄冈地区黄冈县", "HEIGHT": "166", "IDNO": "422121197102214026", "IDTYPE": "01", "PROF": "临工", "QUERY\_STRING": " 湖北  
省淄博市沂源县", "IDNO": "370323198709010021", "IDTYPE": "01", "QUERY\_STRING": " 山东省淄博市沂源县 34 87 1987 ", "R  
省锦州市太和区", "HEIGHT": "157", "IDNO": "210711195210044028", "IDTYPE": "01", "PROF": "菜农", "QUERY\_STRING": " 辽宁省  
西壮族自治区桂林市象山区", "IDNO": "450304190302060515", "IDTYPE": "01", "QUERY\_STRING": " 广西壮族自治区桂林市象山区 1  
省六安地区六安市", "HHPLACE": "安徽省六安市裕安区徐集镇裕兴村王院墙组", "IDNO": "342401197804273638", "IDTYPE": "01", "NATI  
壮族自治区河池地区凤山县", "IDNO": "452727198909250029", "IDTYPE": "01", "QUERY\_STRING": " 广西壮族自治区河池地区凤山县  
省常州市金坛县", "IDNO": "320422197405231111", "IDTYPE": "01", "QUERY\_STRING": " 江苏省常州市金坛县 47 74 1974 ", "R  
省泰安市肥城县", "IDNO": "370922197010194236", "IDTYPE": "01", "QUERY\_STRING": " 山东省泰安市肥城县 51 70 1970 ", "R  
省蚌埠市五河县", "ESCU": "未服兵役", "HEIGHT": "156.0", "IDNO": "340322192805122024", "IDTYPE": "01", "MARR": "丧偶", "NAT  
市南开区", "IDNO": "120104197706054941", "IDTYPE": "01", "QUERY\_STRING": " 天津市南开区 44 77 1977 ", "RNAME": "强白  
省达川地区大竹县", "HHPLACE": "四川省大竹县高明乡大良村4组", "IDNO": "513029199409176738", "IDTYPE": "01", "NATION": "汉",  
省合肥市长丰县", "HHPLACE": "安徽省长丰县岗集镇井沿村老庄组12号", "IDNO": "34012119880720850x", "IDTYPE": "01", "NATION": "  
省秦皇岛市青龙满族自治县", "IDNO": "13032119760401426x", "IDTYPE": "01", "QUERY\_STRING": " 河北省秦皇岛市青龙满族自治县  
省上蔡县", "IDNO": "412825198905288519", "IDTYPE": "01", "QUERY\_STRING": " 河南省上蔡县 32 89 1989 ", "RNAME": "刘义

9 52 1952 "", "RNAME": "陈太全", "SEX": "男", "NATION": "汉", "MARR": "已婚", "NPLACE": "天津镇高升村大阳组16号", "PHOTO": "http://oss-cn-shanghai-shga-d01-a-1253460112534601/aa.sh/shaa-rvzp/CSJ/JIANGSU\_JZZ/5173", "RNAME": "白利花", "SEX": "女", "NATION": "汉", "MARR": "未婚", "NPLACE": "江苏宿迁市宿城区", "PHOTO": "http://oss-cn-shanghai-shga-d01-a-1253460112534601/aa.sh/shaa-rvzp/CSJ/JIANGSU\_JZZ/5173", "MES": "撤逃人员 寻衅滋事案", "LABS": "交通违法 实有入口 常住人口", "IDNO": "31010619771127号1801室", "NAME": "甘继海", "SEX": "男"}, {"ty": "河南封丘县", "QUERY\_STRING": "河南封丘县", "RNAME": "张萌", "SEX": "女", "NATION": "汉", "MARR": "已婚", "NPLACE": "河南封丘县", "PHOTO": "http://oss-cn-shanghai-shga-d01-a-1253460112534601/aa.sh/shaa-rvzp/CSJ/JIANGSU\_JZZ/511991", "RNAME": "林市蛟河市 辽宁 20 01 2001", "SEX": "女", "NATION": "汉", "MARR": "未婚", "NPLACE": "辽宁林市蛟河市", "PHOTO": "http://oss-cn-shanghai-shga-d01-a-1253460112534601/aa.sh/shaa-rvzp/CSJ/JIANGSU\_JZZ/511991"}, {"ty": "关注人员\_涉毒关注人员", "QUERY\_STRING": "关注人员\_涉毒关注人员", "RNAME": "王雷", "SEX": "男", "NATION": "汉", "MARR": "已婚", "NPLACE": "江苏沭阳县", "PHOTO": "http://oss-cn-shanghai-shga-d01-a-1253460112534601/aa.sh/shaa-rvzp/CSJ/JIANGSU\_JZZ/5170", "RNAME": "王雷", "SEX": "男", "NATION": "汉", "MARR": "已婚", "NPLACE": "江苏沭阳县", "PHOTO": "http://oss-cn-shanghai-shga-d01-a-1253460112534601/aa.sh/shaa-rvzp/CSJ/JIANGSU\_JZZ/5170"}]

津镇高升村大阳组16号 51 70 1970 "", "RNAME": "王雷", "SEX": "男", "NATION": "汉", "MARR": "已婚", "NPLACE": "江苏沭阳县", "PHOTO": "http://oss-cn-shanghai-shga-d01-a-1253460112534601/aa.sh/shaa-rvzp/CSJ/JIANGSU\_JZZ/5170", "MES": "关注人员\_涉毒关注人员", "LABS": "AB000633", "NATION": "汉", "NPLACE": "上海市金山区", "PHOTO": "http://oss-cn-shanghai-shga-d01-a-1253460112534601/aa.sh/shaa-rvzp/CSJ/JIANGSU\_JZZ/5170", "RNAME": "王雷", "SEX": "男", "NATION": "汉", "MARR": "已婚", "NPLACE": "江苏沭阳县", "PHOTO": "http://oss-cn-shanghai-shga-d01-a-1253460112534601/aa.sh/shaa-rvzp/CSJ/JIANGSU\_JZZ/5170"}]

10时26分,王斌(男,户籍地址:上海市徐汇区梅陇六村6号401室,现住地址:上海市闵行区罗秀路1339弄29号801室,身份证号:310115198811107215)报警称:其在本市普陀区枣阳路465弄21号门口与一男子发生纠纷,被该男子殴打。接报后,民警立即赶赴现场处置,并将涉嫌殴打他人的男子带回派出所进一步调查。

20时许,报案人罗友军来所报案,2014年11月29日15时许,其在本市普陀区枣阳路465弄21号门口与一男子发生纠纷,被该男子殴打。接报后,民警立即赶赴现场处置,并将涉嫌殴打他人的男子带回派出所进一步调查。

13:05:57,手机号:15317001758,报警人在仓汇路1345弄东门口,称:苏A278A1 挪车","CASE\_TYPE":null,"CASE\_STATE":null,"ORGANIZER\_POLICE\_TYPE":null,"ORGANIZER":>{"ORGANIZER\_NAME": "上海市公安局徐汇分局漕河泾派出所", "ORGANIZER\_ID": "310115198811107215"}, "case\_address": "上海市徐汇区漕河泾开发区漕宝路1345弄东门口", "case\_time": "2014-11-29T13:05:57", "case\_desc": "挪车", "case\_detail": "报警人在仓汇路1345弄东门口发现一辆苏A278A1的白色轿车停在人行道上,影响行人通行,遂报警要求挪车。", "case\_resolution": "民警到达现场后,发现该车已驶离,未造成任何损失,因此未采取进一步措施。", "case\_status": "已处理", "case\_type": "交通事故", "case\_update": null}

16时51分,报警人王正芳使用13817262927拨打110报警称:其前夫钱龙详(身份证证:310225195711201217)在外欠债,无法归还。接报后,民警立即赶赴现场处置,并将涉嫌欠债不还的男子带回派出所进一步调查。

17时9时许,报警人张丽萍110报称:于2006年1月4日晚20时至次日上午8时间,受害单位(东沟镇东塘路771号上海东际塑料制品有限公司)仓库被盗。接报后,民警立即赶赴现场处置,并将涉嫌盗窃的男子带回派出所进一步调查。

17时42分,报警人使用13818080572报警称:在 瑞和路168号 8号楼门口 2辆轿车相撞。双方理赔中心理赔","CASE\_TYPE":null,"CASE\_STATE":null,"ORGANIZER\_POLICE\_TYPE":null,"ORGANIZER": {""ORGANIZER\_NAME": "上海市公安局徐汇分局漕河泾派出所", """ORGANIZER\_ID": "310115198811107215"}, "case\_address": "上海市徐汇区漕河泾开发区漕宝路168号", "case\_time": "2014-11-29T17:42:00", "case\_desc": "交通事故", "case\_detail": "两辆轿车在瑞和路168号8号楼门口发生碰撞,造成车辆损坏,双方协商赔偿事宜。", "case\_resolution": "民警到达现场后,双方达成协议,由保险公司进行理赔,未造成人员受伤。", "case\_status": "已处理", "case\_type": "交通事故", "case\_update": null}

15时许,我所民警接群众匿名举报称:本市徐汇区嘉善路171弄11号棋牌室内有人以打麻将方式进行赌博。","CASE\_TYPE":null,"CASE\_STATE":null,"ORGANIZER\_POLICE\_TYPE":null,"ORGANIZER": {""ORGANIZER\_NAME": "上海市公安局徐汇分局漕河泾派出所", """ORGANIZER\_ID": "310115198811107215"}, "case\_address": "上海市徐汇区嘉善路171弄11号", "case\_time": "2014-11-29T15:00:00", "case\_desc": "治安扰民", "case\_detail": "群众匿名举报称棋牌室内有赌博行为,民警立即前往核查,未发现明显违法行为,仅口头警告并责令整改。", "case\_resolution": "民警口头警告并责令整改,未采取进一步措施。", "case\_status": "已处理", "case\_type": "治安扰民", "case\_update": null}

7时48日许,接指挥中心110报警,龙水北路960弄15号501室纠纷。我所处警到达现场,报警人称楼上601室是群居有十几人,经常吵闹,严重影响居民休息。接报后,民警立即赶赴现场处置,并将涉嫌噪音扰民的男子带回派出所进一步调查。

1时10分吉接110报警称昆明路1266号门口夜排当吵闹.民警到现场劝阻. ","CASE\_TYPE":null,"CASE\_STATE":null,"ORGANIZER\_POLICE\_TYPE":null,"ORGANIZER": {""ORGANIZER\_NAME": "上海市公安局徐汇分局漕河泾派出所", """ORGANIZER\_ID": "310115198811107215"}, "case\_address": "上海市徐汇区昆明路1266号", "case\_time": "2014-11-29T01:10:00", "case\_desc": "治安扰民", "case\_detail": "群众举报称昆明路1266号门口有噪音扰民现象,民警立即前往核查,未发现明显违法行为,仅口头警告并责令整改。", "case\_resolution": "民警口头警告并责令整改,未采取进一步措施。", "case\_status": "已处理", "case\_type": "治安扰民", "case\_update": null}

09时05分,报警人使用13482626327报警称:在 龙水南路201号龙华汽配城内菜场内2号岗亭处 警察走后,有摆摊人员要卖淫嫖娼。接报后,民警立即赶赴现场处置,并将涉嫌卖淫嫖娼的男子带回派出所进一步调查。

22时08分,报警人使用13122394577报警称:在 新源路"盛越(谐音)"宾馆301号房间 举报上址有2人正在进行卖淫嫖娼。接报后,民警立即赶赴现场处置,并将涉嫌卖淫嫖娼的男子带回派出所进一步调查。

12时00分,报警人使用38821518报警称:在 浦东大道2220号1楼104室上安大厦 报警人被打rn报警人被打,带所处理。接报后,民警立即赶赴现场处置,并将涉嫌殴打他人的男子带回派出所进一步调查。

14:28:42,手机号:13764916279,报警人在杨泰路2188号门口 通道处,称:挪车 粤GG1743","CASE\_TYPE":null,"CASE\_STATE":null,"ORGANIZER\_POLICE\_TYPE":null,"ORGANIZER": {""ORGANIZER\_NAME": "上海市公安局徐汇分局漕河泾派出所", """ORGANIZER\_ID": "310115198811107215"}, "case\_address": "上海市徐汇区漕河泾开发区漕宝路2188号", "case\_time": "2014-11-29T14:28:42", "case\_desc": "交通事故", "case\_detail": "报警人在杨泰路2188号门口发现一辆粤GG1743的白色轿车停在人行道上,影响行人通行,遂报警要求挪车。", "case\_resolution": "民警到达现场后,发现该车已驶离,未造成任何损失,因此未采取进一步措施。", "case\_status": "已处理", "case\_type": "交通事故", "case\_update": null}

16时21分,报警人使用13918193166报警称:在金山区朱泾镇西林街51号中国农业银行门口上址有人打架,民警到场处理,并调取监控录像。接报后,民警立即赶赴现场处置,并将涉嫌打架斗殴的男子带回派出所进一步调查。

0:28:56,手机号:13052027987,报警人在天通庵路654号,称:赔偿纠纷 请民警到场处理。赔偿纠纷 ,民警到场调解,并调取监控录像。接报后,民警立即赶赴现场处置,并将涉嫌赔偿纠纷的男子带回派出所进一步调查。

12时28分,事主110报警称:杭州路宁武路电动自行车被窃。民警到现场后经了解系报警人自己未锁电动自行车停在路边后被盗。接报后,民警立即赶赴现场处置,并将涉嫌盗窃的男子带回派出所进一步调查。

13时20分,我所民警在漕河泾派出所现场建筑(甲 310115198811107215)在该处抓获2名犯罪嫌疑人予以刑事拘留。接报后,民警立即赶赴现场处置,并将涉嫌盗窃的男子带回派出所进一步调查。

nameinfo": [{"name": "黄\*"}]}, "FIRST\_TIME": "159\*\*\*\*5906", "LAST\_TIME": "159\*\*\*\*5906"},  
{"name": "李灵芝女士"}]}, "FIRST\_TIME": "154", "IDENTITY\_VALUE": "18926754681", "LAST\_TIME": "154"},  
nameinfo": [{"name": "曾\*\*"}]}, "FIRST\_TIME": "135\*\*\*\*8875", "LAST\_TIME": "135\*\*\*\*8875"},  
nameinfo": [{"name": "任\*\*"}]}, "FIRST\_TIME": "183\*\*\*\*5084", "LAST\_TIME": "183\*\*\*\*5084"},  
[{"name": "邹声虎"}]}, "FITYPE": "mobile", "IDENTITY\_VALUE": "18798532"},  
[{"name": "田女士"}]}, "FIRST\_TIME": "154608", "IDENTITY\_VALUE": "15062048023", "LAST\_TIME": "154608"},  
nameinfo": [{"name": "高素霞"}]}, "FIRST\_TIME": "15695189162", "LAST\_TIME": "15695189162"},  
nameinfo": [{"name": "余世杰"}]}, "FIRST\_TIME": "13461187266", "LAST\_TIME": "13461187266"},  
nameinfo": [{"name": "冯庆成"}]}, "FIRST\_TIME": "13656373688", "LAST\_TIME": "13656373688"},  
nameinfo": [{"name": "贾艳芳"}]}, "FIRST\_TIME": "15293353385", "LAST\_TIME": "15293353385"},  
,"ADDRESS": "小牛津幼儿园(航顺晓镇东南)(迎秋西里28栋3单元8号)", "SOURCE": "shga\_wa.ods\_nb\_app\_icpoof\_delivery", "\_type": "a",  
,"ADDRESS": "宜昌市湖北省宜昌市夷陵区长江市场香山凤凰城", "SOURCE": "shga\_wa.ods\_nb\_app\_icpoof\_delivery", "\_type": "a",  
,"ADDRESS": "西乡(金海路金海商务大厦2栋512)", "SRC\_ID": "0b2554", "SOURCE": "shga\_wa.ods\_nb\_app\_icpoof\_delivery", "\_type": "a",  
,"ADDRESS": "广东省东莞市清溪镇清溪镇铁松铁矢岭河边东路11号", "SOURCE": "shga\_wa.ods\_nb\_app\_icpoof\_delivery", "\_type": "a",  
,"ADDRESS": "山东省烟台市烟台市文昌路街道莱州中医院", "SRC\_ID": "0b2554", "SOURCE": "shga\_wa.ods\_nb\_app\_icpoof\_delivery", "\_type": "a",  
,"SRC\_ADDRESS": "贵州省黔东南苗族侗族自治州岑巩县大有", "ADDRESS": "嘉德·金鼎广场(六号楼三单元302)", "SRC\_ID": "43f0348c5", "SOURCE": "shga\_wa.ods\_nb\_app\_icpoof\_delivery", "\_type": "a", "sort": 1},  
,"ADDRESS": "江苏省连云港市海州区江苏省连云港市海州区江苏省", "SOURCE": "shga\_wa.ods\_nb\_app\_icpoof\_expressdelivery", "\_type": "a",  
,"ADDRESS": "河南省平顶山市平顶山市文峰路龙博城", "SRC\_ID": "0b2554", "SOURCE": "shga\_wa.ods\_nb\_app\_icpoof\_delivery", "\_type": "a", "sort": 1},  
,"ADDRESS": "山东省枣庄市枣庄市海滕机床有限公司地址:滕州市", "SOURCE": "shga\_wa.ods\_nb\_app\_icpoof\_delivery", "\_type": "a", "sort": [33198],  
,"ADDRESS": "甘肃省陇南市武都区甘肃省陇南市武都区城关镇甘肃", "SOURCE": "shga\_wa.ods\_nb\_app\_icpoof\_delivery", "\_type": "a", "sort": [33198]}

# Encryption Cryptography 密码学



Symmetric Encryption



Private Key 私钥



Asymmetric Encryption



Public Key 公钥  
Private Key 私钥



## Number Theory

# Mathematical Preliminaries

Modular Arithmetic 同余

$$a \equiv b \pmod{n}$$

$$a \pmod{n} \equiv b$$

$$32 \pmod{12} \equiv ?$$

$$32 \equiv 8 \pmod{12}$$

"congruent"  
~~≡~~

$$\begin{array}{r} & 2 \\ 12 & \overline{)32} \\ & 24 \\ & \hline & 8 \end{array}$$

2 years  
months  
Remainder

# Mathematical Preliminaries

## Prime number 素数/质数

1,2,3,5,7,11,13,17,19,23,29...

Infinitely many!

# Key Exchange Symmetric Encryption



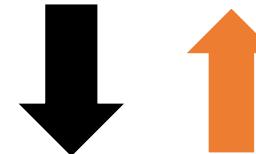
M139WJ

Alice ← → Bob

13 01 03 09 23 10



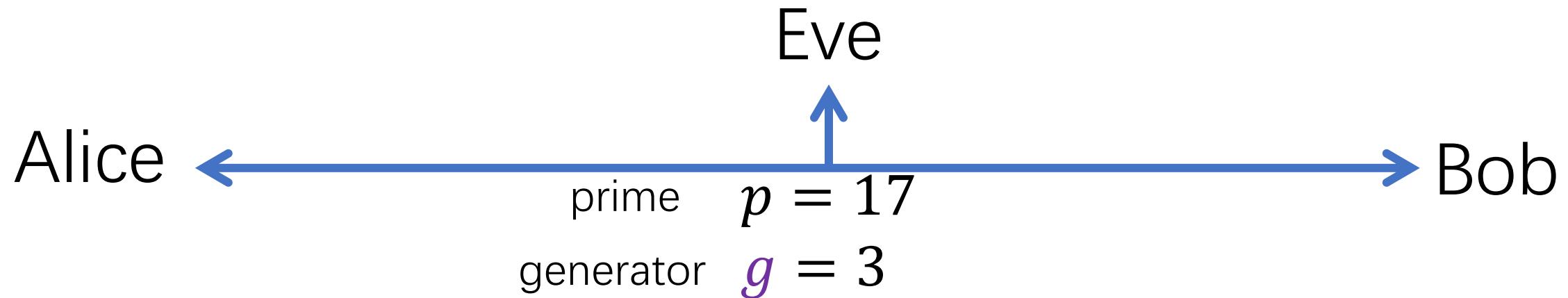
26 02 06 18 46 20



Cipher-text



Eve



$$g^a \bmod p = A$$

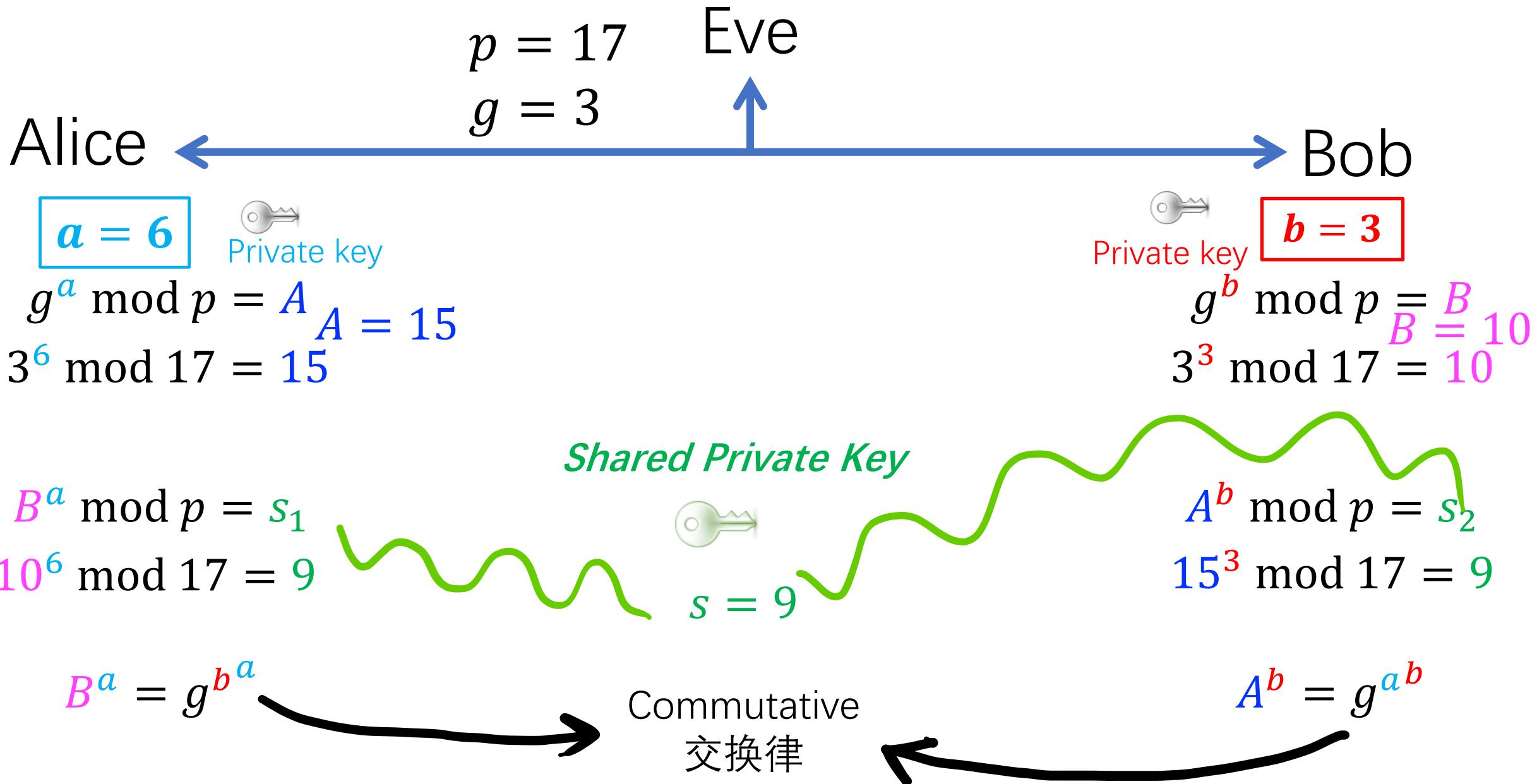


Easy

$$g? \bmod p = A$$

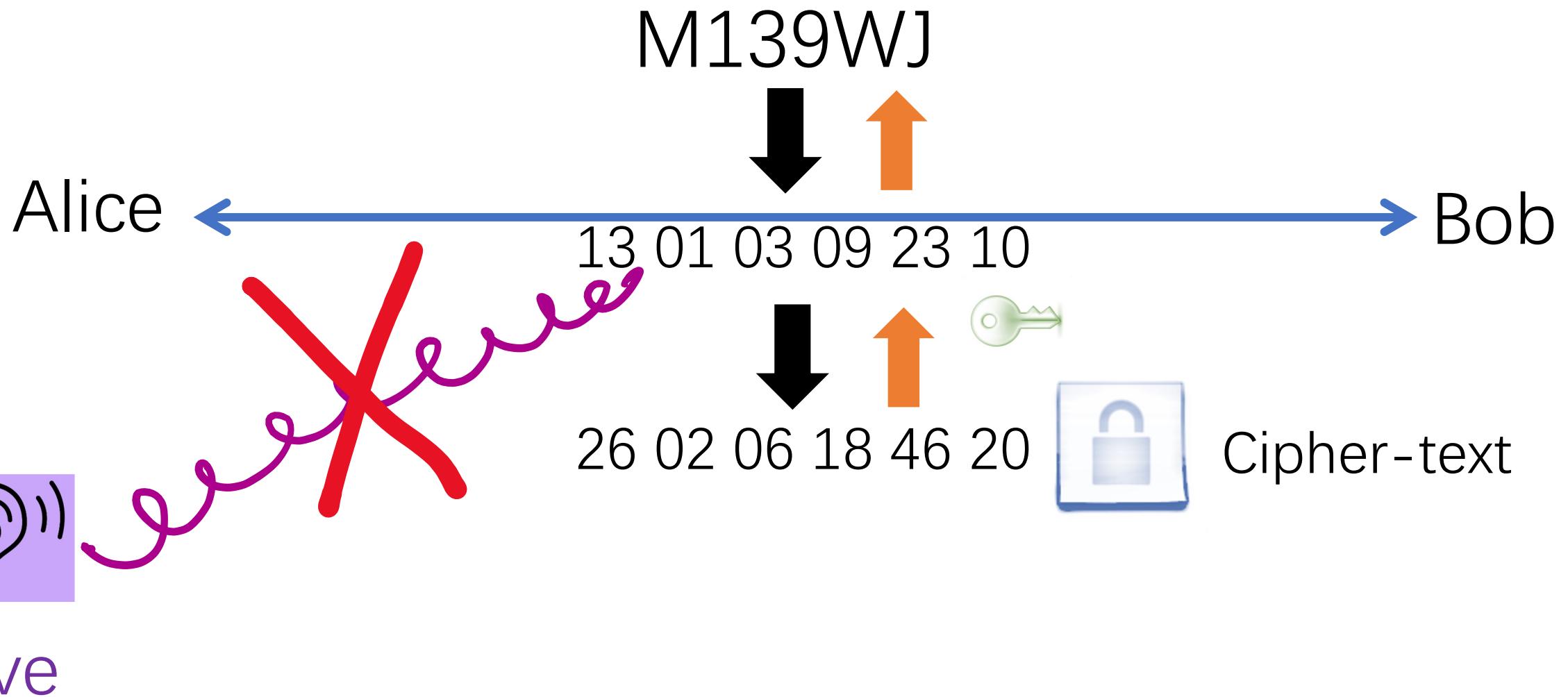
Hard      Discrete Logarithm  
trial and error

One-way Function



# Key Exchange Symmetric Encryption

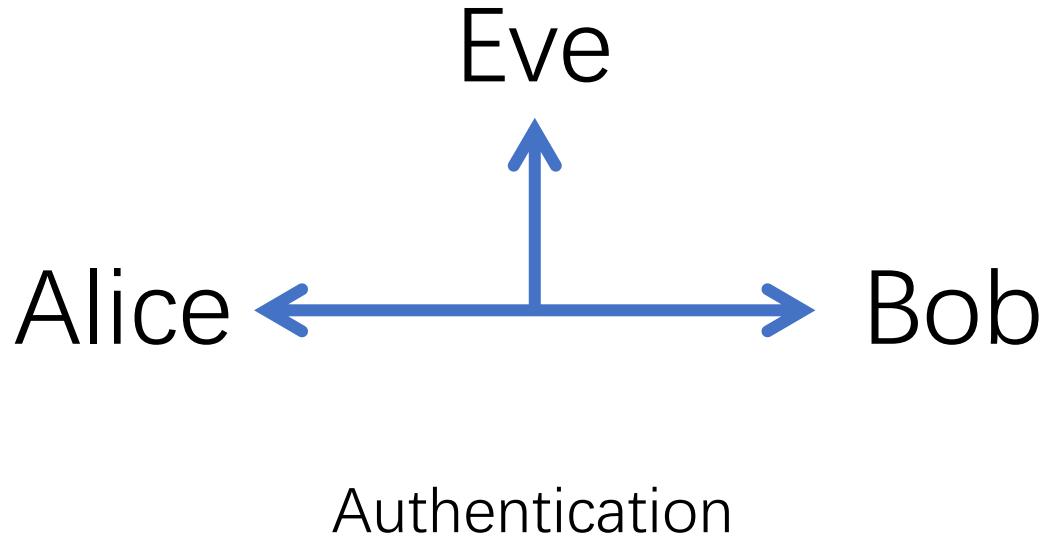
Diffie-Hellman key exchange  
1976



# Key Exchange Symmetric Encryption

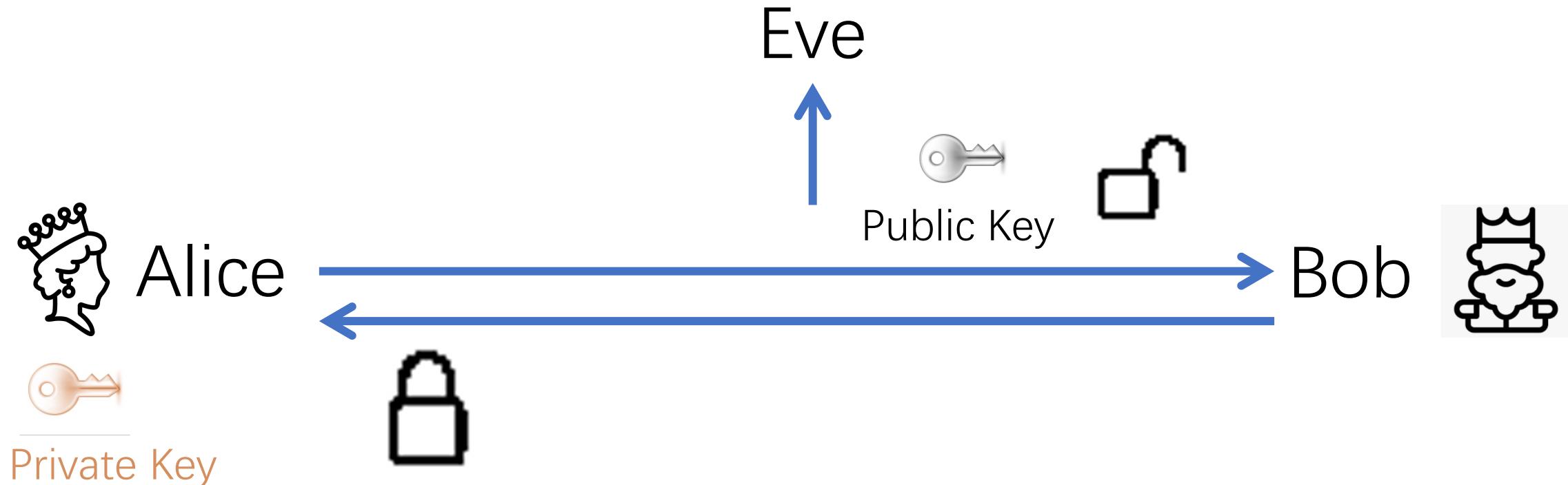


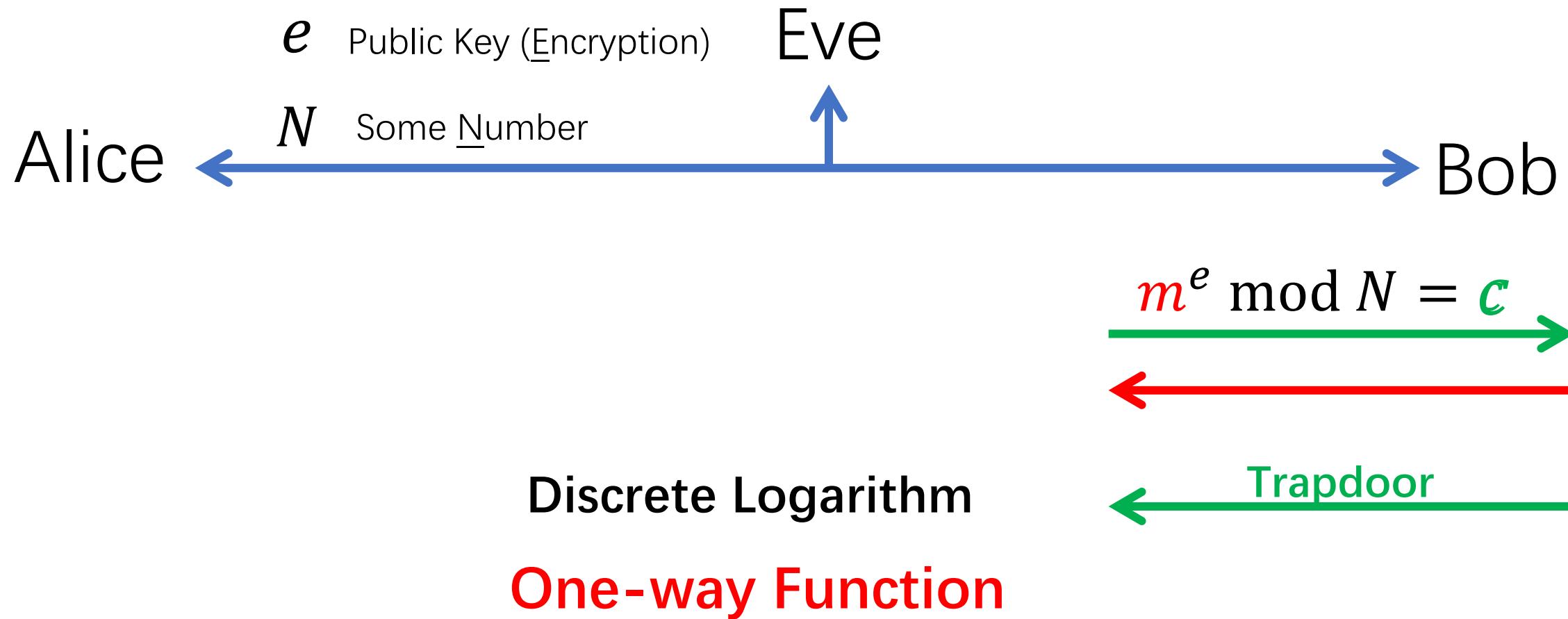
Too many keys



# Asymmetric Encryption

Public Key 公钥  
Private Key 私钥





Trapdoor One-way Function

# Factorization of Numbers

$$46 = 2 \times 23$$



$$6895601 = 1931 \times 3571$$



**Uniquely** decomposed into **prime** numbers

**Fundamental theorem of arithmetic**  
**Unique factorization theorem**

# Leonhard Euler

(15 April 1707 – 18 September 1783)

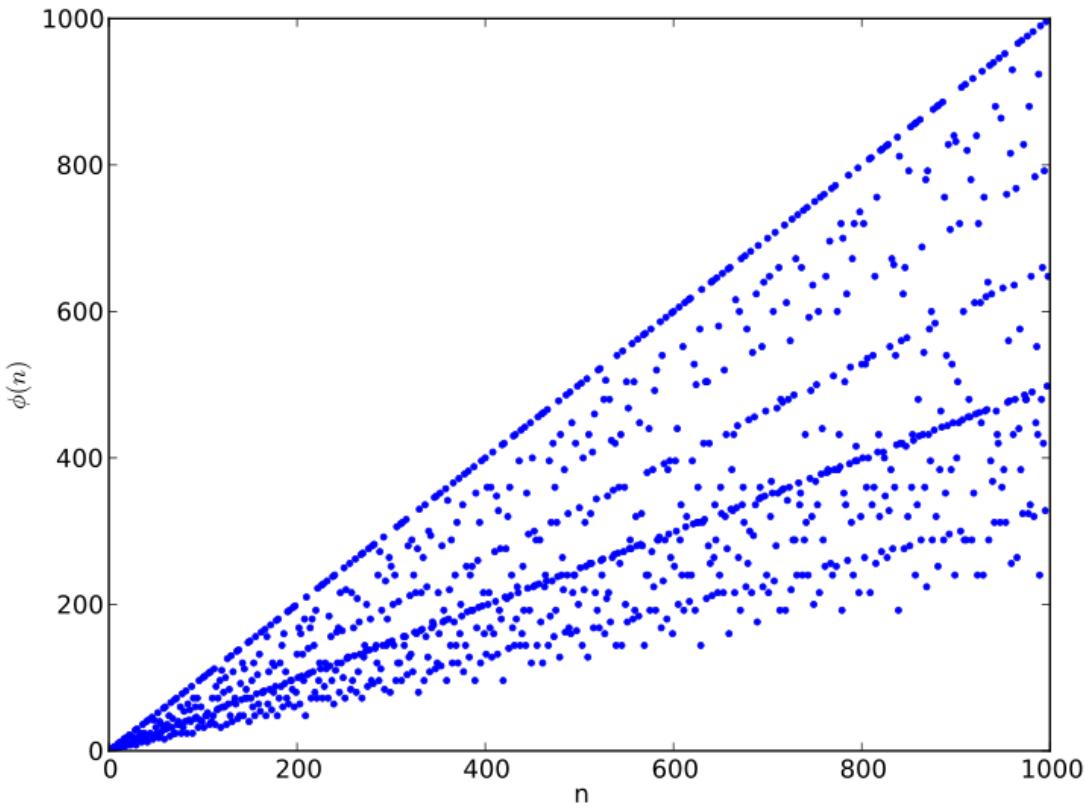
- Euler's function  $\phi$
- Euler's theorem



- Euler's function  $\phi$

$$\phi(9) = \#\{1, 2, 3, 4, 5, 6, 7, 8, 9\} = 6$$

*coprime*



primes  $p, q$

$$pq = N$$

$$\begin{aligned}\phi(N) &= \phi(pq) = \phi(p)\phi(q) \\ &= (p-1)(q-1)\end{aligned}$$

- Euler's theorem

$$m^{\phi(n)} \equiv 1 \pmod{n} \quad (m, n \text{ coprime})$$

$$m^{k\phi(n)} \equiv 1 \pmod{n}$$

$$m^{k\phi(n)+1} \equiv m \pmod{n}$$

Some number  $n$

Public Key  $e$

Alice

Eve

Bob

$$m^e \equiv c \pmod{n}$$

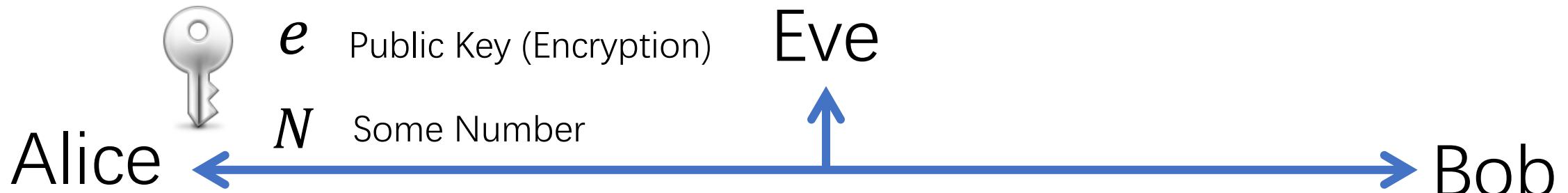
$$c^d \equiv m \pmod{n}$$

$$(m^e)^d \equiv m \pmod{n}$$

$$k\phi(n) + 1 = ed$$

$$ed \equiv 1 \pmod{\phi(n)}$$

Trapdoor  
One-way Function



$$N = pq$$

$$221 = 13 \times 17$$

$$\begin{aligned}\phi(N) &= \phi(pq) = \phi(p)\phi(q) \\ &= (p-1)(q-1)\end{aligned}$$

$$\phi(221) = 12 \times 16 = 192$$

$$e = 5$$

$$c^d \bmod N = m$$

$$163^{77} \bmod 221 = 11$$

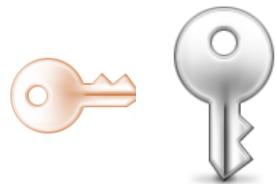
$$\begin{array}{c} m^e \bmod N = c \\ \xleftarrow{\hspace{1cm}} \\ 11^5 \bmod 221 = 163 \end{array}$$

$$d = 77$$



Private Key (Decryption)

$$ed \equiv 1 \pmod{\phi(n)}$$



# Asymmetric Encryption

RSA Logarithm  
1977

Ron Rivest  
Adi Shamir  
Leonard Adleman

Discrete Logarithm  
Prime Factorization

→ **One-way Function**

Euler's Function  
Euler's Theorem

→ **Trapdoor**

# Edward Snowden

(1983/6/21 --- )



PRISM(棱镜计划)



# Secret Documents Reveal N.S.A. Campaign Against Encryption

Documents show that the N.S.A. has been waging a war against encryption using a battery of methods that include working with industry to weaken encryption standards, making design changes to cryptographic software, and pushing international encryption standards it knows it can break. [Related Article »](#)

Excerpt from 2013 Intelligence Budget Request

Bullrun Briefing Sheet

Diffie–Hellman key exchange  
1976

1969 at GCHQ  
James Ellis  
Clifford Cocks  
Malcolm Williamson



RSA Logarithm  
1977

1973 at GCHQ  
Clifford Cocks

(Revealed in 1997)



# MATHS

Number Theory

# No Privacy On Internet