

# Introduction to genetic algorithms

## Insights for IA

TEAM 2

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# Background

# Why GA?

Asses point to point, genetic algorithm is parralel, we dont need additional information about the problem.

# Quadratic Optimization

## Gradient descent

The process could be enlightened by extension.

# Chromosome, gen, allele and locus

Figure: Chromosome representation



# Codification

Binary, real...

Individuals with better features have major probability of have offspring.

# Introduction to genetic algorithm

A GA is a program, composed of strings that swap information!.



# Swaping operators

The selection provided the parents that will be interchange information, with the crossover and mutation operator.

# Genetic algorithm

## Implementation

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### Algorithm 1: Canonical genetic algorithm

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initialization of population;

**while** *not fill stoping criteria* **do**

    Select Parents ;

    Crossover pairs of parents ;

    Mutate Offspring ;

    Update population ;

**end**

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# Schema

Constructed over the alphabet  $\{0, 1, *\}$  it is an abstract representation of a chromosome. Where  $*$  is metasyMBOL (taking either 1 or 0).

# Schema

If we have the following schema \* \* \* we could represent  $2^3$  possible instances, for example 111 or 100 and so on. 10101 could be represented by:

- 10101
- \*0101
- 1\*101
- \*\*101
- 1\*\*01
- \*\*\*01
- \*\*\*\*\*

in a total of  $\sum_{i=0}^k \binom{n}{i} = 2^n$  where  $k$  is the number of wildcards.

- Order:  $o(H)$  the number of fixed position; or the length of the schema minus the number of  $*$ 's.
- Length:  $l(H)$  is the number of bits that composed H.
- Defining length:  $\delta(H)$  The distance among the first and last fixed position.

# Inheritance

Features that remain of parents to offsprings.

# Selection

## Proportional selection

Select possible chromosomes as parents, according its fitness.

$$P_{x_i} = \frac{f_i(t)}{\sum_j^n f_j(t)} \quad (1)$$

after of get we can choose a random number among 0 and the sum of total fitness in population, this strategy is denominated wheel strategy.

# Mutation and crossover

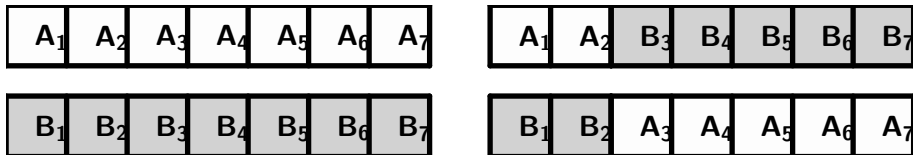
The crossover and mutation as operators of the evolutionary process, in the search process, one is exploration and the another exploitation of search space.



# Crossover

fix one point

Figure: Crossover in single point (2-index)



the offspring born choosing a random locus, in two parents, and after concatenate  $\alpha_a$  and  $\alpha_b$  and the locus is equal to  $\pi$  then the offspring will be  $\alpha_a[:\pi]$  concatenate with  $\alpha_b[\pi:]$ .

# Crossover

## Inheritance-compactibility

When we consider a schema  $H$

# Crossover-inheritance

We can define the probability of that the crossover occur among two parents  $P_c$ , and the probability of a schema will be destroyed as  $p_d$  (related with the vulnerability) We can define that the probability of a schem will be destroyed by  $P_c * P_{dl}$

$$P_s = (1 - P_c) \frac{\delta(H)}{l(H) - 1} \quad (2)$$

Therefore the probability that a schema survive will be  $1 - P_d$ .

# Mutation-inheritance

All bits in a string have  $P_{mu}$  of undergoes a mutation, therefore the probability of not mutate is  $1 - P_{mu}$  then for the number of fixed bits we have  $o(H)$  that the probability of complete schema survival to mutation will be

$$P_m = (1 - P_{mu})^{o(H)} \quad (3)$$

# Crossover-Mutation-Inheritance

The probability of a schema survive to crossover and mutation will be:

$$P_{sur} = [(1 - p_c) \frac{\delta(H)}{L(H) - 1}] (1 - p_{mu})^{o(H)} \quad (4)$$

# Schema theorem

## Inheritance in generations

First we need take in mind the settings:

- Binary codification
- $N_{t-1} = 0$  (There are not parents in the next generation)
- Roulette wheel (proportional selection)
- Crossover in a single point
- Uniform mutation

# Schema theorem

Population(t)	Fitness $f(x)$
$x_1 = 1010$	$f(x_1)$
$x_2 = 0101$	$f(x_2)$
$\vdots$	$\vdots$
$x_n = 1110$	$f(x_n)$
$\sum_i^n f(x_i) = F(t)$	

We can ranking that  $\frac{f(x_i)}{F(t)} > \dots > \frac{f(x_j)}{F(t)}$  and select pairs to crossover.

# Schema theorem

$m(H, t)$  number of strings that match with  $H$  schema in  $t$  generation.

Chromosome	Schema ( $H = 1*01$ )	$f(H, t)$
$x_1 = 1011$	0	-
$x_2 = 1001$	1	$f(x_2)$
$x_3 = 0011$	0	-
$x_4 = 1101$	1	$f(x_4)$
$m(H, t) = 2$		$\frac{f(x_2) + f(x_4)}{2}$



# Schema theorem

## Goal

Determine the **probability** that  $H$  survive in the evolutionary process.  
The average probability of individuals that  $Match(H, x_i) = 1$  be selected in the  $t$ -generation to crossover is :

$$\frac{f(H, t)}{F(t)} \quad (5)$$

# Schema theorem

if for instance we have  $n$  individuals in the population, the probability of my first parent will be a *match* will be  $m(H, t) \frac{f(H, t)}{F(t)}$  and therefore for the  $n$  parents selections we have:

$$m(H, t) \frac{f(H, t)}{F(t)} (n) \quad (6)$$

will be the number of individuals that match that will be selected.

# Schema theorem

In the next generation:

$$m(H, t + 1) = m(H, t) \frac{f(H, t)}{F(t)} (n) \quad (7)$$

The average fitness of the population will be  $\bar{F}(t) = \frac{F(t)}{n}$  rewriting we have:

$$m(H, t + 1) = m(H, t) \frac{f(H, t)}{\bar{F}(t)} \quad (8)$$

This means that schemas with higher fitness of average tend to be selected more.

# Schema theorem

## Lower-bound

Why is low bound? because in some cases we assume for instance crossover with another not belonging schemas.

$$E[m(H, t + 1)] \geq m(H, t) \frac{f(H, t)}{\bar{F}(t)} [(1 - p_c) \frac{\delta(H)}{L(H) - 1}] (1 - p_{mu})^{o(H)} \quad (9)$$

# Implicit parallelism

Process  $3^n$  schemate, with only  $n$  as input.

# Deap library

# Mutation

# Mutation

## Shuffle indices



# genetic TSP

# Elitism process

$\mu + \lambda$  algorithm

# Genetic algorithms in ML

Here there are important remarks are used to avoid greedy algorithms for instance:

- Decision trees
- K-means
- Tuning hyperparameters in Neural Networks.

# Memetic algorithms

# References

# Following techniques to research

Simulated annealing, tabú search... ant PSO and ant-colony.

