# WDM PASSIVE STAR - PROTOCOLS AND PERFORMANCE ANALYSIS

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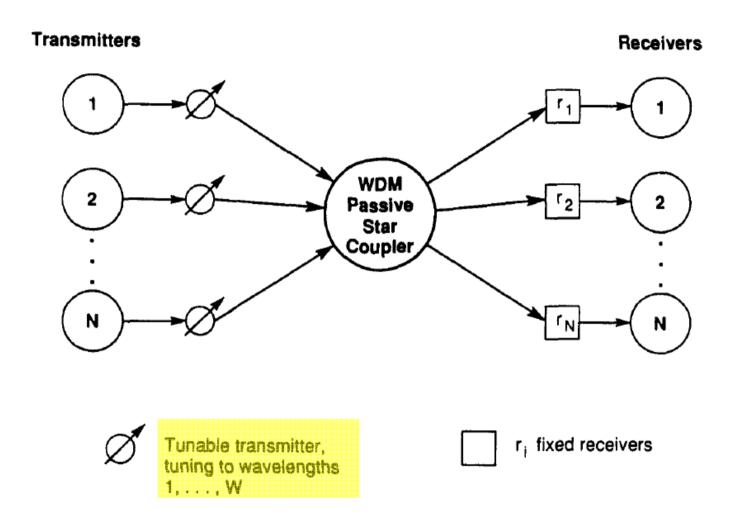


Figure 1:N Nodes interconnected through a WDM star.

#### 2. The Model

In this paper we analyze a communication system consisting of N nodes, interconnected by a WDM star using W ( $1 \le W \le N$ ) identical channels. The channels are obtained by wavelength

Node i has a buffer capacity of  $L_i$  packets. Time is divided into slots of fixed size, and all nodes are synchronized to the beginnings of the slots. At the beginning of each time slot, node i (provided that its buffer is not full) generates a new packet with probability  $\lambda_i$ . The packet transmission time is one slot. The packet is destined to node m with probability  $d_{im}$ , ( $\sum_{m=1}^{N} d_{im} = 1$  for i = 1, ..., N).

Let  $R_i$  denote the set of wavelengths that node i can simultaneously receive from,  $|R_i| = r_i$ . This leads to the division of the N nodes into W (not necessarily disjoint) sets  $A_1, ..., A_W$  according to their transmission channel, with  $A_i = \{m|1 \le m \le N, i \in T_m\}$  and W (not necessarily disjoint) sets  $B_1, ..., B_W$  according to their reception channel

#### 4. Random TDMA

### 4.1 Protocol Description

Each node follows a slot transmission schedule trans, with trans[i] determining the channel on which node i will be allowed to transmit. If node i is not scheduled for transmission, trans[i] = 0.

At the beginning of each slot, a busy node i with trans[i] = k > 0 is given permission to transmit on channel k to any of the nodes in the set  $B_k$  (the set of nodes that receive on channel k).

Node i can choose from its buffer any of the packets whose destination is in the set  $B_k$ , and it will transmit successfully if it has such a packet.

The following algorithm constructs the collision free transmission schedule *trans*:

1. 
$$\Omega = \{1, 2, ..., W\}, \hat{A}_j = A_j \text{ for } j = 1, ..., W.$$

- 2. Choose at random one channel in the set  $\Omega$ , say channel k.
- 3. Choose at random one node among the nodes in set  $\hat{A}_k$ , say node i.
- 4. trans[i] = k,  $\hat{A}_{j} = \hat{A}_{j} - \{i\} \text{ for } j = 1, ..., W; \quad \Omega = \Omega - \{k\}.$
- 5. If  $\Omega \neq \emptyset$  goto 2.

## 5. Numerical Results

As a specific example we investigated a system consisting of 8 nodes interconnected through 4 channels, and we performed both a validation of

System 3: Each transmitter can tune to all four wavelengths and each node has one receiver, one for each wavelength. The transmitters' and receivers' wavelengths are given by:

$$T_i = \{1, 2, 3, 4\}, i = 1, ..., 8,$$
  
 $R_i = \{1\}, i = 1, 2, R_i = \{2\}, i = 3, 4, R_i = \{3\}, i = 5, 6, R_i = \{4\}, i = 7, 8.$ 

System Performance: Once the approximation has been validated, we investigate the system behavior as a function of the system load, the channel access protocol and the system hardware design. The results are depicted in Figures 4-6.

For the performance calculations we chose a homogeneous system with packet generation probability  $\lambda_i = b/N$ , buffer size  $L_i = 4$  and  $d_{im} = 0$  for m = i,  $d_{im} = \frac{1}{N-1}$  for  $m \neq i$ .

system load b (the sum of the nodes' packet generation probabilities).

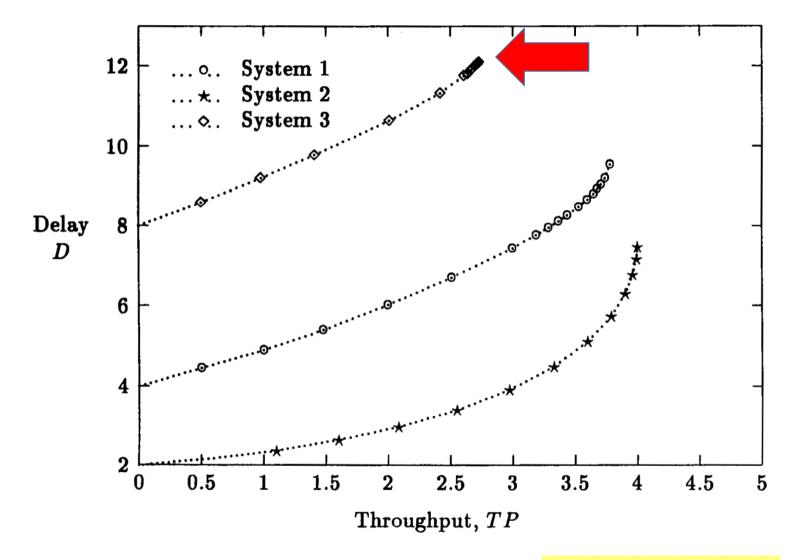


Figure 5: Average packet delay versus system throughput, N=8, W=4,  $L_i=4$ , random TDMA protocol.