

# Heuristics Analysis

## Optimal Plans:

### Problem 1:

*Load(C1, P1, SFO)*

*Fly(P1, SFO, JFK)*

*Unload(C1, P1, JFK)*

*Load(C2, P2, JFK)*

*Fly(P2, JFK, SFO)*

*Unload(C2, P2, SFO)*

### Problem 2:

*Load(C1, P1, SFO)*

*Fly(P1, SFO, JFK)*

*Unload(C1, P1, JFK)*

*Load(C2, P2, JFK)*

*Fly(P2, JFK, SFO)*

*Unload(C2, P2, SFO)*

*Load(C3, P3, ATL)*

*Fly(P3, ATL, SFO)*

*Unload(C3, P3, SFO)*

### Problem 3:

*Load(C1, P1, SFO)*

*Fly(P1, SFO, ATL)*

*Load(C3, P1, ATL)*

*Fly(P1, ATL, JFK)*

*Unload(C3, P1, JFK)*

*Unload(C1, P1, JFK)*

*Load(C2, P2, JFK)*

*Fly(P2, JFK, ORD)*

*Load(C4, P2, ORD)*

*Fly(P2, ORD, SFO)*

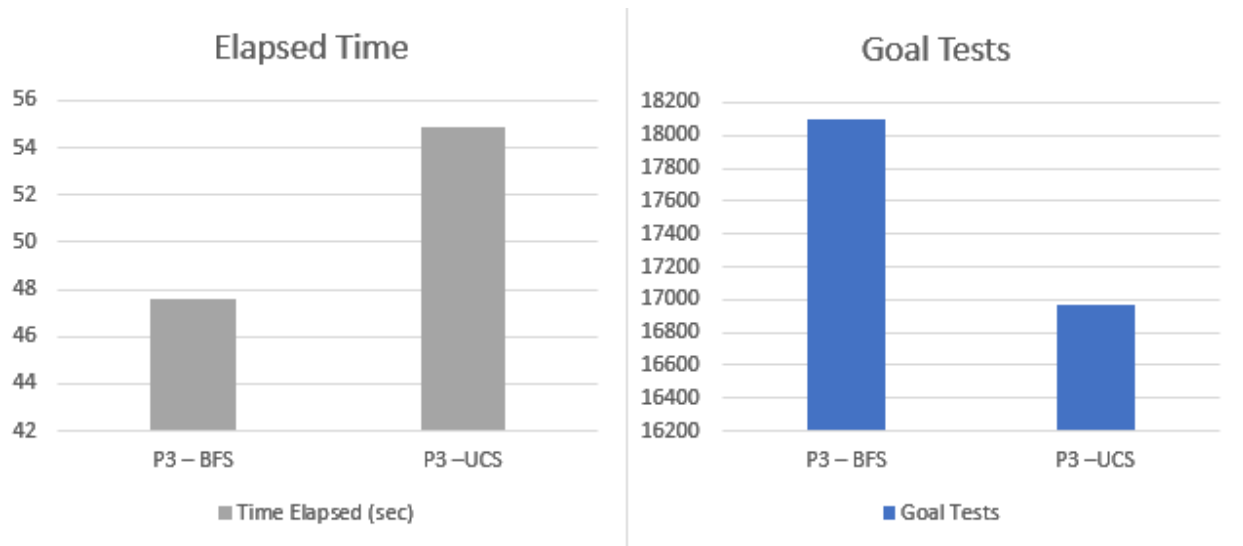
*Unload(C4, P2, SFO)*

*Unload(C2, P2, SFO)*

## Uninformed Search

The best non-heuristic search was *BFS*. *DFGS* performed better on all other metrics but produced sub-optimal solutions with a length two order of magnitudes larger than the optimal plan length.

On elapsed time and node expansions *BFS* performed better than *UCS*. *UCS* performed marginally better than *BFS* on the goal tests metric.



## Heuristic Search – A\* with levelsum vs ignore preconditions

The best heuristic for all of the problems was *ignore preconditions*, it performed better on both the optimality and time metrics.

*Level sum* could produce either optimal or sub-optimal solutions for problem 3 depending on the order of literals in the initial state. For problems 1 and 2 it produced an optimal solutions and required less node expansions and goal tests but required an order of magnitude more time than *ignore preconditions* to complete.

## Heuristic vs Non-heuristic Search

Comparing heuristic to non-heuristic search techniques, A\* search with *ignore preconditions* heuristic performed best overall for all problems. It required roughly a quarter of the goal tests and node expansions and a third of the time of *BFS*.

DFGS does not find optimal solutions because it searches each path to its end and terminates once any solution, that is, a path that reaches all goals is found. So only if the first possible solution happens to be optimal it would reach it.

The graph search version of A\* is optimal given *ignore preconditions* heuristic is consistent. In any case the use of a good heuristic provides enormous savings compared to uninformed search such as *BFS*.

The metrics table for the informed and uninformed searches shows that A\* with either heuristic dominates any uninformed search method by any criteria.

Comparing informed searches we see *levelsum* dominates *ignore preconditions* by node expansions and goal tests but is being dominated by the time complexity criteria.

*Ignore preconditions* iterates the goals and for each looks up its state, that is  **$O(\text{goals} \times \log \text{states})$**  python list index operation is  $O(\log n)$ . *Level sum* iterates the goals and for each iterates planning graph state levels. That is  **$O(\text{goals} \times \text{levels} \times \text{states})$**  making *ignore preconditions* an order of magnitude faster.

A\* expands nodes with minimal  $f(n) = g(n) + h(n)$ , it is optimal yet its space complexity is still prohibitive but much better than *BFS* having exponential space complexity.

Complete Metrics Table

	Plan Length	Optimal	Time Elapsed (sec)	Node Expansions	Goal Tests	New Nodes
P1 – BFS	6	Yes	.027	43	56	180
P1 –DFGS	12	No	.009	12	13	48
P1 –UCS	6	Yes	.034	55	57	224
P2 – BFS	9	Yes	8.72	3343	4609	30509
P2 –DFGS	466	No	2.44	476	477	4253
P2 –UCS	9	Yes	11.9	4604	4606	41828
P3 – BFS	12	Yes	47.6	14663	18098	129631
P3 –DFGS	1442	No	13.9	1511	1512	12611
P3 –UCS	12	Yes	54.9	16963	16965	149136
P1 – A* h1	6	Yes	.034	55	57	224
P1 – A* ignore_precond	6	Yes	.026	41	43	170
P1 – A* pg_levelsum	6	Yes	.896	11	13	50
P2 – A* h1	9	Yes	11.5	4604	4606	41828
P2 – A* ignore_precond	9	Yes	3.54	1310	1312	11979
P2 – A* pg_levelsum	9	Yes	93.9	94	96	925
P3 – A* h1	12	Yes	52.9	16963	149136	16965
P3 – A* ignore_precond	12	Yes	14.6	4444	4446	39227
P3 – A* pg_levelsum	12	Yes	434	314	316	2894