

# 分子のグラフ表現と機械学習

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2020年10月20日(火)：日本化学会 第10回CSJ化学フェスタ2020  
データサイエンスの世界をのぞいてみませんか？

たきがわ いちがく

瀧川一学

<https://itakigawa.github.io/>

北海道大学 化学反応創成研究拠点 (WPI-ICReDD)

# 本日の内容

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GNN(Graph Neural Networks)でグラフ表現された分子を  
入力にして機械学習するやり方をのぞいてみませんか？

- 機械学習とは？
- 分子のグラフ表現
- 準備：深層学習のココロ (forwardとbackward)
- Graph Neural Networksとは？
- 自分でやってみるための情報
- おまけ：  
最近の話 (計算限界、分子生成、事前学習、...)

# 本日の内容

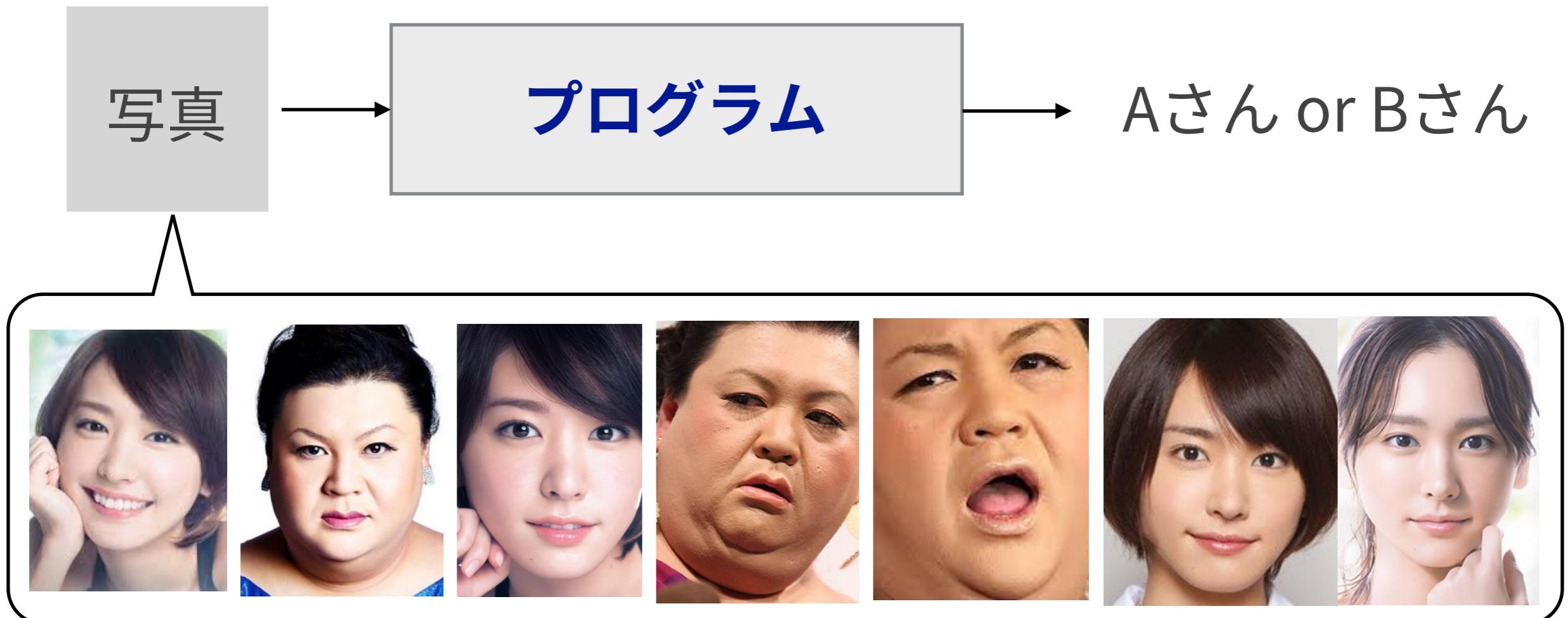
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GNN(Graph Neural Networks)でグラフ表現された分子を  
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# 機械学習の出番

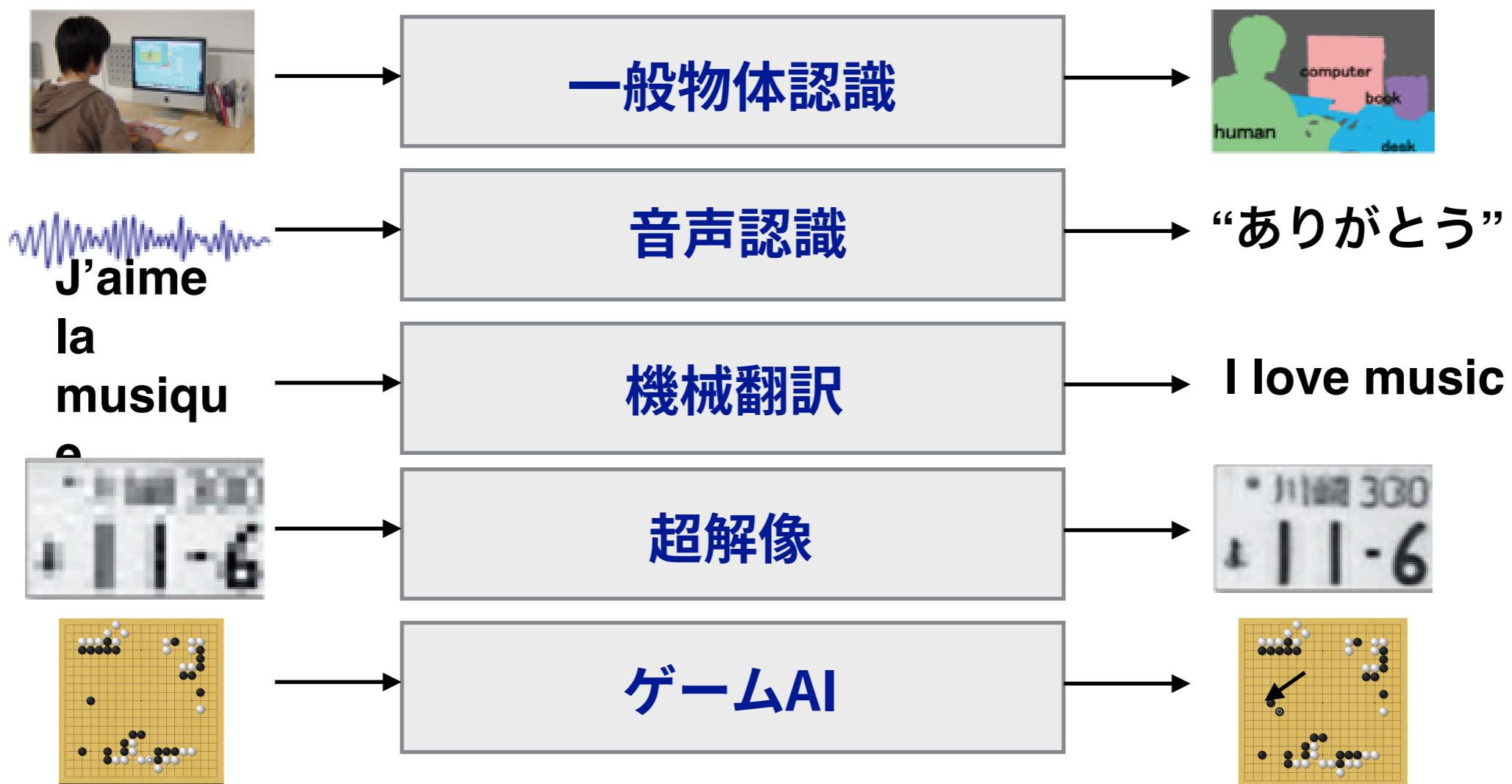
AさんとBさんの写真を分けるプログラムを作りたい



人間なら簡単に解けるけど手順は自分でも説明できない...

# 機械学習：新しいプログラミングのパラダイム

機械学習 = 多量の入出力の見本例からプログラムを自動的に作成する(いいかげんな)技術



# 今日の例：分子の活性や物性の予測 (QSAR/QSPR)



入出力の  
見本例

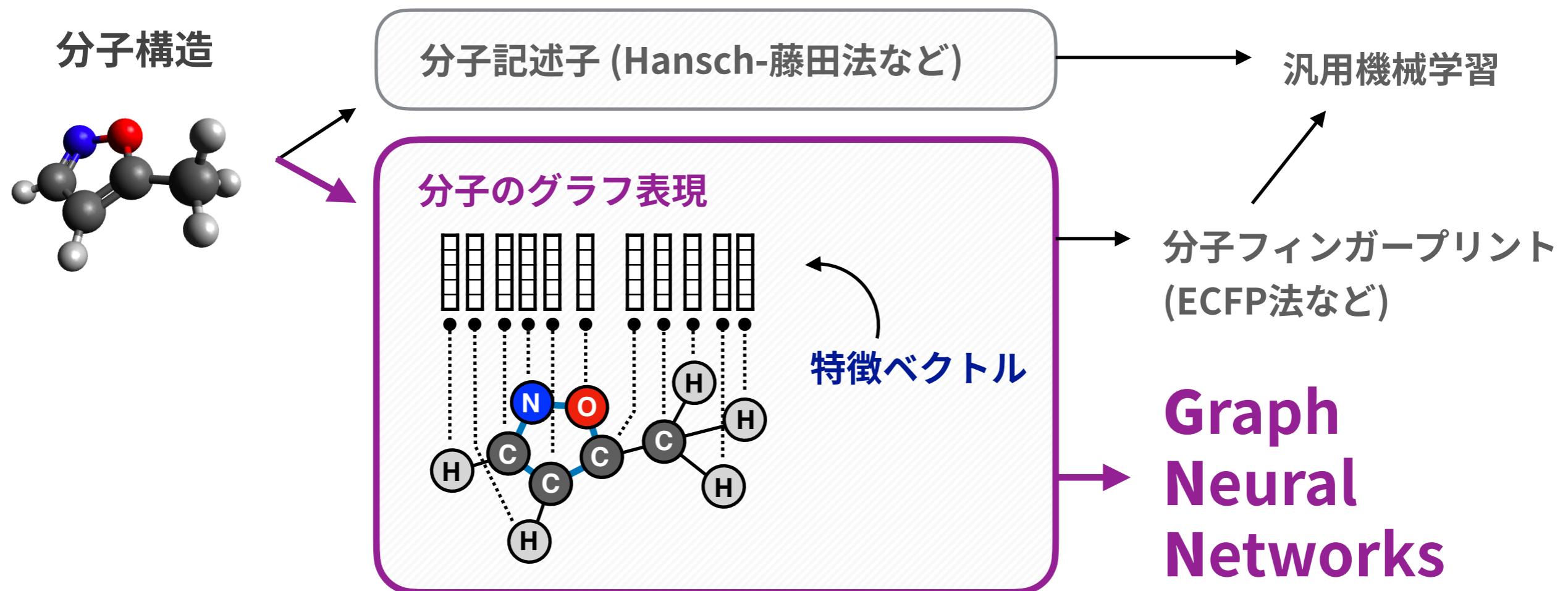


⋮

# 分子のグラフ表現とGraph Neural Networks (GNNs)

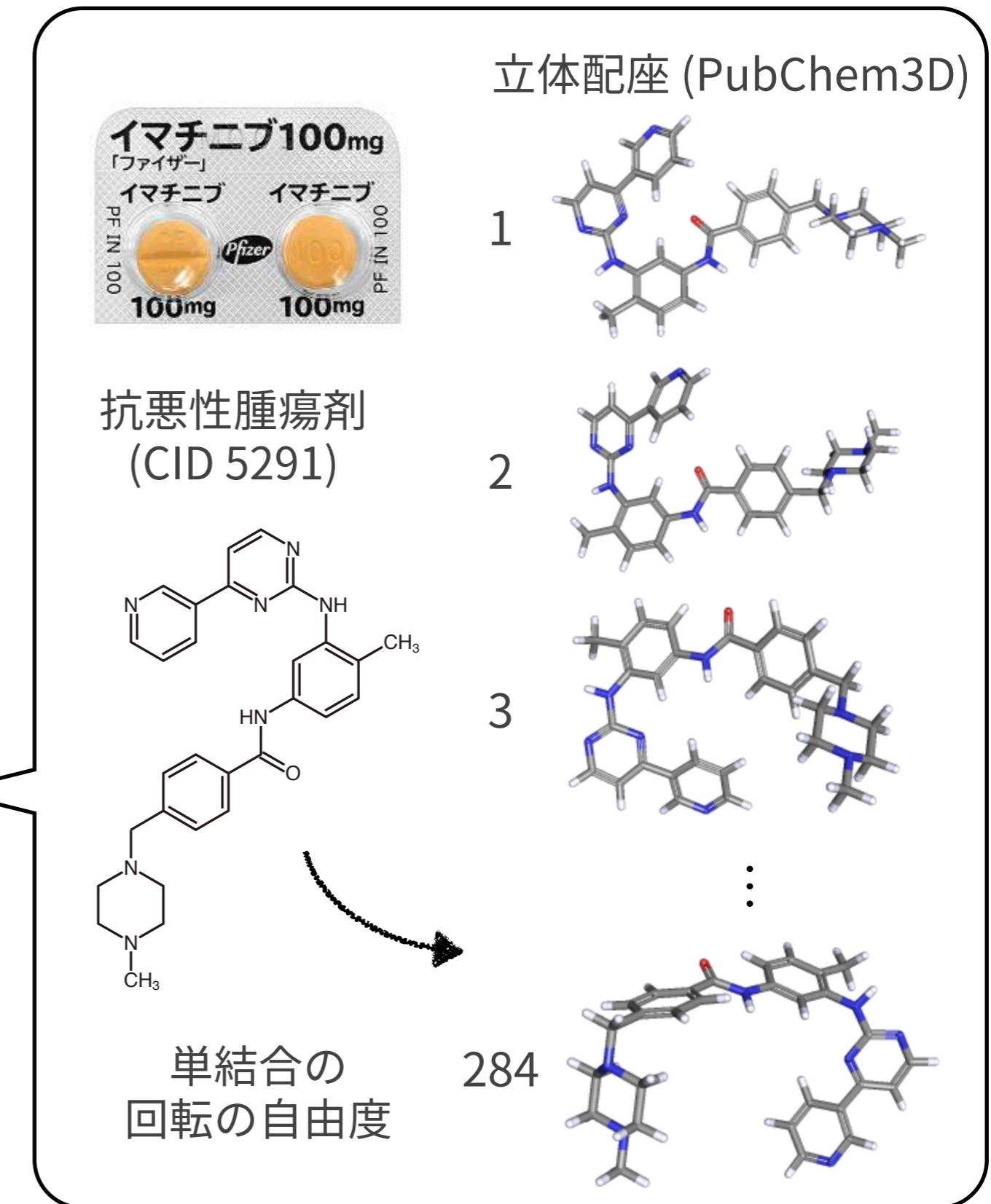
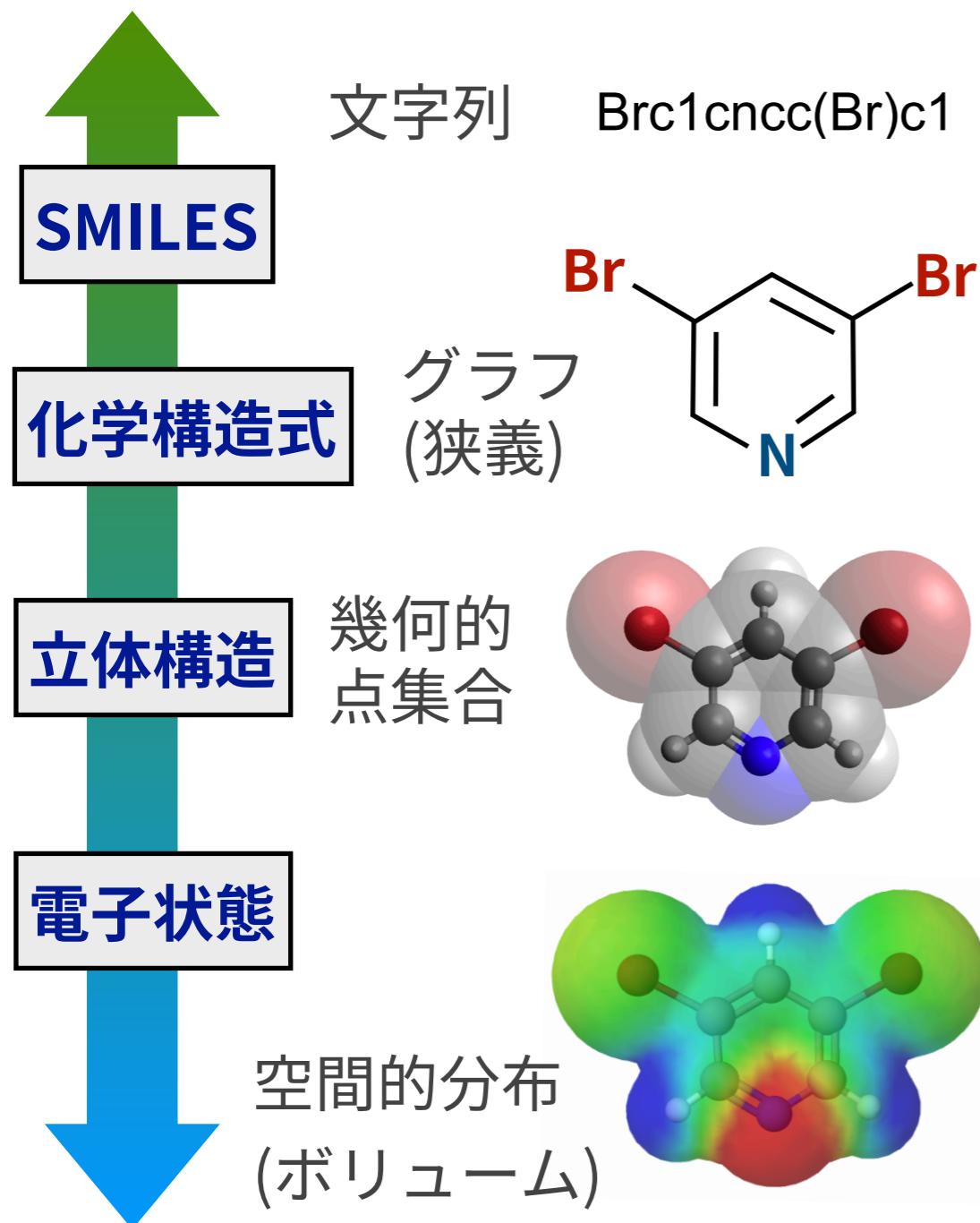


色々やり方あるけれど今日はGNNをのぞいてみませんか？



**動機：GNNは広いモダリティを統一的に扱うことができる**

# GNNで扱えるモダリティは **狭義の「グラフ」より広い**



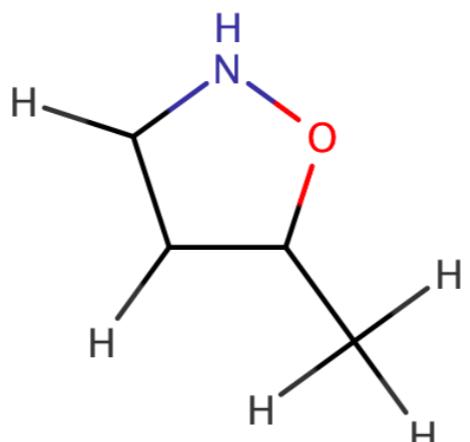
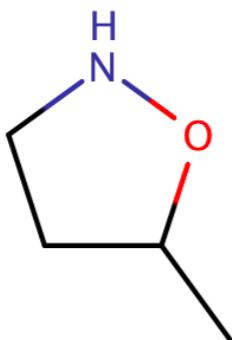
# 分子表現

1次元

CC1CCN<sup>O</sup>1

Canonical SMILES

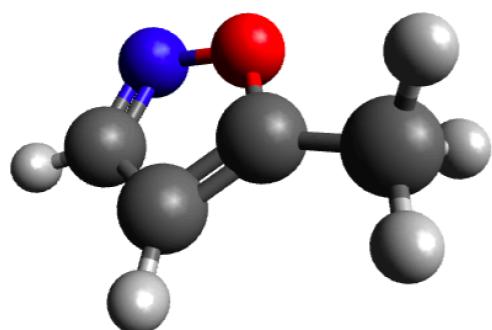
2次元



水素(Implicit)

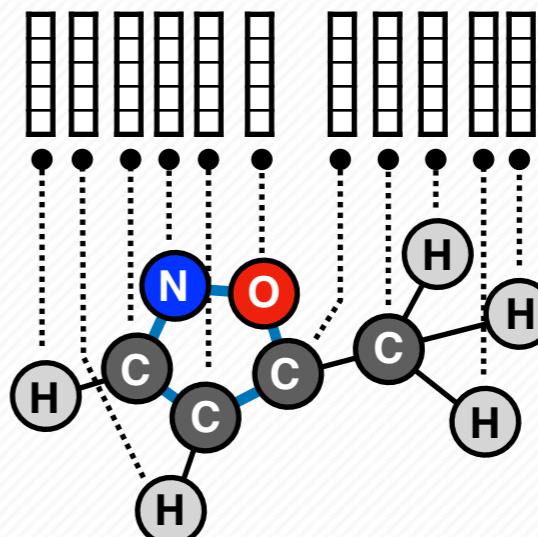
水素(Explicit)

3次元



MOL形式

分子のグラフ表現



特徴ベクトル

|         |    |         |   |         |   |     |
|---------|----|---------|---|---------|---|-----|
| 11      | 11 | 0       | 0 | 0       | 0 | 999 |
| 0.0264  |    | 1.4944  |   | 0.0287  | C |     |
| -0.0850 |    | 0.0111  |   | 0.0449  | C |     |
| -1.0957 |    | -0.8588 |   | -0.2308 | C |     |
| -0.5082 |    | -2.1326 |   | -0.0113 | C |     |
| 0.7433  |    | -2.0451 |   | 0.3632  | N |     |
| 1.0156  |    | -0.6777 |   | 0.3997  | O |     |
| 0.8032  |    | 1.8213  |   | -0.6702 | H |     |
| -0.9230 |    | 1.9401  |   | -0.2734 | H |     |
| 0.2923  |    | 1.8782  |   | 1.0190  | H |     |
| -2.1005 |    | -0.6271 |   | -0.5415 | H |     |
| -0.9559 |    | -3.1113 |   | -0.1136 | H |     |
| 1       | 2  | 1       | 0 | 0       | 0 | 0   |
| 1       | 9  | 1       | 0 | 0       | 0 | 0   |
| 2       | 6  | 1       | 0 | 0       | 0 | 0   |
| 3       | 4  | 1       | 0 | 0       | 0 | 0   |
| 3       | 2  | 2       | 0 | 0       | 0 | 0   |
| 4       | 5  | 2       | 0 | 0       | 0 | 0   |
| 5       | 6  | 1       | 0 | 0       | 0 | 0   |
| 7       | 1  | 1       | 0 | 0       | 0 | 0   |
| 8       | 1  | 1       | 0 | 0       | 0 | 0   |
| 10      | 3  | 1       | 0 | 0       | 0 | 0   |
| 11      | 4  | 1       | 0 | 0       | 0 | 0   |

原子核のxyz

化学結合

# 実際の分子グラフデータを見てみよう

---

## QM9 Dataset (Ramakrishnan+ 2014)

133,885 分子： C, N, O, Fの組合せから成る9原子(H以外)までの分子の安定3D構造と15種の物性値を計算 (B3LYP/6-31G(2df,p) level)

SCIENTIFIC DATA 

OPEN  
SUBJECT CATEGORIES  
» Quantum chemistry  
» Density functional theory

Quantum chemistry structures and properties of 134 kilo molecules

Raghunathan Ramakrishnan<sup>1</sup>, Pavlo O. Dral<sup>2,3</sup>, Matthias Rupp<sup>1</sup> & O. Anatole von Lilienfeld<sup>1,4</sup>

*Sci Data* 1, 140022 (2014). <https://doi.org/10.1038/sdata.2014.22>

# 実際の分子グラフデータを見てみよう

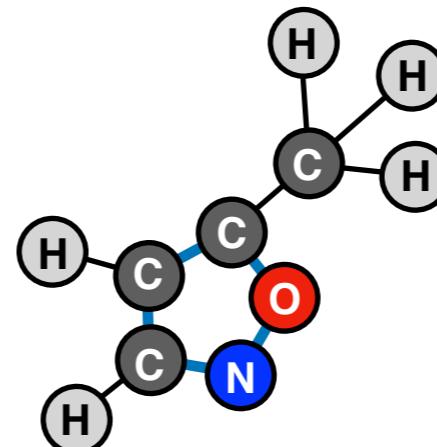
```
import matplotlib.pyplot as plt  
import networkx as nx  
import torch_geometric as pyg
```

```
data = pyg.datasets.QM9(root='/tmp/QM9')  
print('分子グラフの数:', len(data))
```

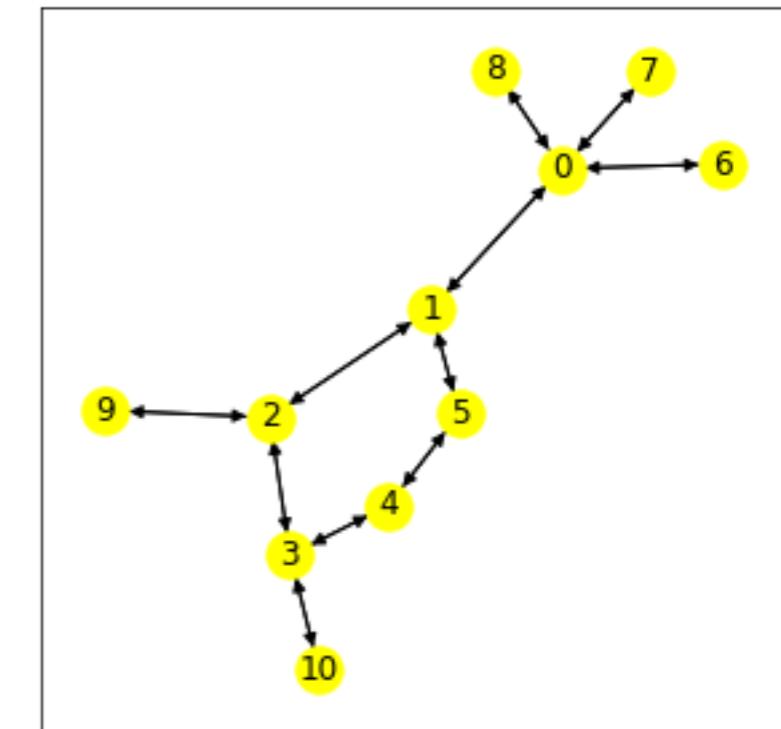
分子グラフの数: 130831

```
mol = data[717] ← 718番目の  
mol.name  
'gdb_727'
```

この分子の  
molを観察



```
g = pyg.utils.convert.to_networkx(mol)  
fig, ax = plt.subplots(figsize=(5, 5))  
nx.draw_networkx(g, node_color="yellow")  
fig.show()
```



# 実際の分子グラフデータを見てみよう

mol.y

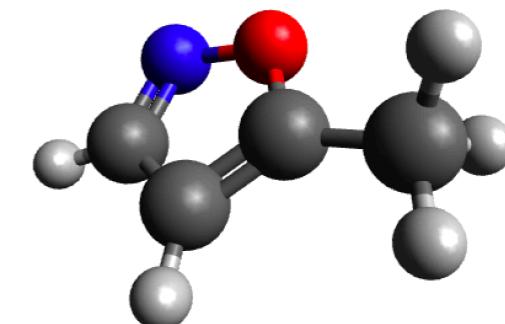
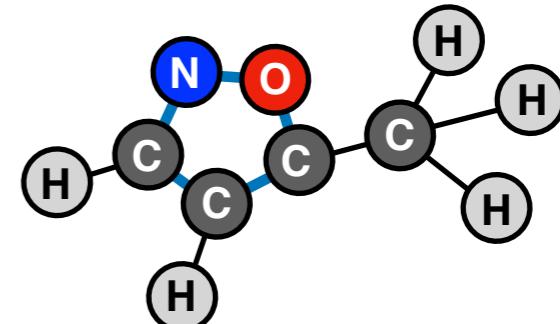
```
tensor([[ 3.1194e+00,  4.8060e+01, -6.8763e+00, -1.9320e-01,  6.6831e+00,
         4.8378e+02,  2.3288e+00, -7.7632e+03, -7.7631e+03, -7.7631e+03,
        -7.7640e+03,  1.8293e+01, -4.7811e+01, -4.8092e+01, -4.8349e+01,
       -4.4744e+01,  9.2803e+00,  3.5644e+00,  2.6172e+00]])
```

```
import pandas as pd
pd.Series(mol.y.numpy()[0])
```

|    |              |   |
|----|--------------|---|
| 0  | 3.119400     | Dipole moment                                     |
| 1  | 48.060001    | Isotropic polarizability                          |
| 2  | -6.876316    | Highest occupied molecular orbital (HOMO) energy  |
| 3  | -0.193201    | Lowest unoccupied molecular orbital (LUMO) energy |
| 4  | 6.683115     | Gap between HOMO and LUMO                         |
| 5  | 483.779388   | Electronic spatial extent                         |
| 6  | 2.328750     | Zero point vibrational energy                     |
| 7  | -7763.241699 | Internal energy at 0K                             |
| 8  | -7763.098633 | Internal energy at 298.15K                        |
| 9  | -7763.073242 | Enthalpy at 298.15K                               |
| 10 | -7764.022949 | Free energy at 298.15K                            |
| 11 | 18.292999    | Heat capacity at 298.15K                          |
| 12 | -47.811089   | Atomization energy at 0K                          |
| 13 | -48.092346   | Atomization energy at 298.15K                     |
| 14 | -48.349361   | Atomization enthalpy at 298.15K                   |
| 15 | -44.743744   | Atomization free energy at 298.15K                |
| 16 | 9.280260     | Rotational constant A                             |
| 17 | 3.564360     | Rotational constant B                             |
| 18 | 2.617160     | Rotational constant C                             |

タテに表示

これらのDFT計算値を  
(DFTしないで)予測するタスク



# 実際の分子グラフデータを見てみよう

```
mol.edge_index
```

```
tensor([[ 0,  0,  0,  0,  1,  1,  1,  2,  2,  2,  3,  3,  3,  4,  4,  5,  5,  6,
         7,  8,  9, 10],
        [ 1,  6,  7,  8,  0,  2,  5,  1,  3,  9,  2,  4, 10,  3,  5,  1,  4,  0,
         0,  0,  2,  3]])
```

```
for id, (s, t) in enumerate(zip(*mol.edge_index)):
    print(f'Edge: {id}, node[{s}] -> node[{t}]')
```

```
Edge: 0, node[ 0 ] -> node[ 1 ]
```

```
Edge: 1, node[ 0 ] -> node[ 6 ]
```

```
Edge: 2, node[ 0 ] -> node[ 7 ]
```

```
Edge: 3, node[ 0 ] -> node[ 8 ]
```

```
Edge: 4, node[ 1 ] -> node[ 0 ]
```

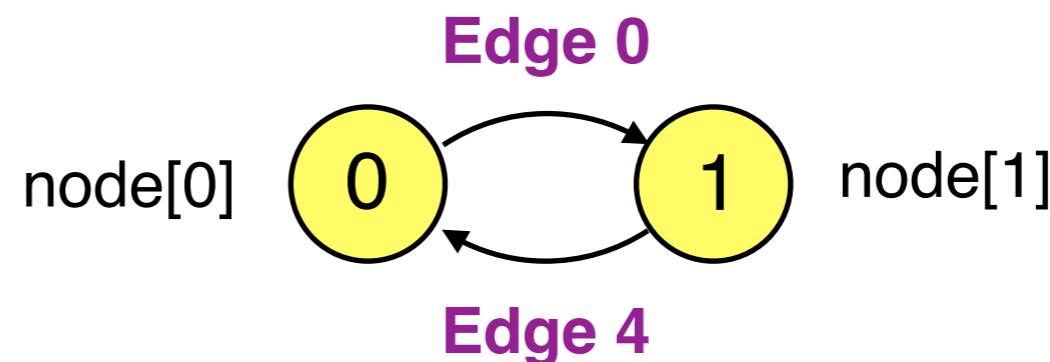
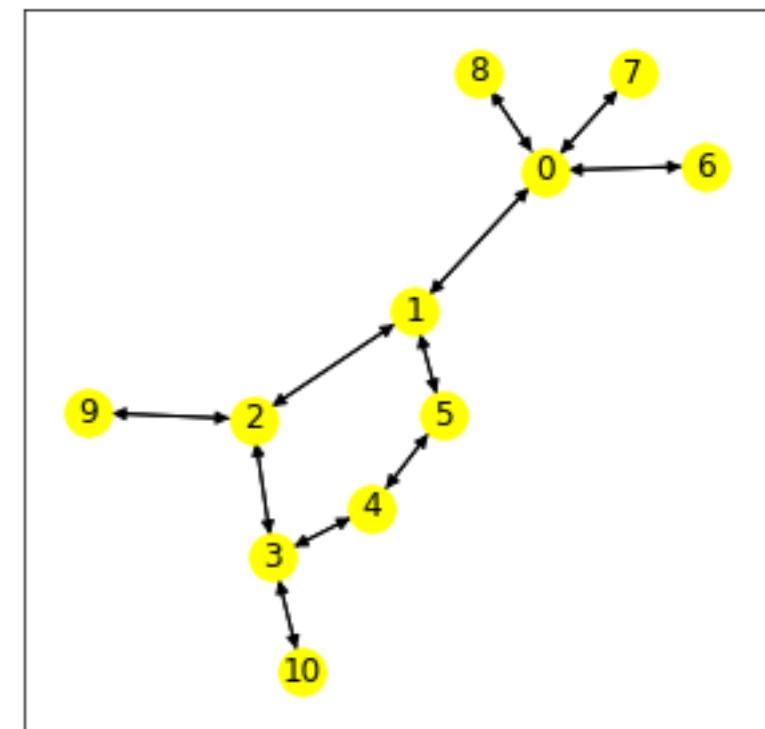
```
Edge: 5, node[ 1 ] -> node[ 2 ]
```

```
:
```

```
Edge: 20, node[ 9 ] -> node[ 2 ]
```

```
Edge: 21, node[10] -> node[ 3 ]
```

辺の向きも  
考慮できる



# 実際の分子グラフデータを見てみよう

mol.z 頂点の原子番号

```
tensor([6, 6, 6, 6, 7, 8, 1, 1, 1, 1, 1])
```

## mol.x 頂点の特徴ベクトル(11次元)

```
tensor([[0., 1., 0., 0., 0., 6., 0., 0., 0., 0., 0., 3.],  
       [0., 1., 0., 0., 0., 6., 0., 0., 0., 0., 0., 0.],  
       [0., 1., 0., 0., 0., 6., 0., 0., 0., 0., 0., 1.],  
       [0., 1., 0., 0., 0., 6., 0., 0., 0., 0., 0., 1.],  
       [0., 0., 1., 0., 0., 7., 0., 0., 0., 0., 0., 0.],  
       [0., 0., 0., 1., 0., 8., 0., 0., 0., 0., 0., 0.],  
       [1., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0., 0.],  
       [1., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0., 0.],  
       [1., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0., 0.],  
       [1., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0., 0.],  
       [1., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0., 0.]])
```

## mol.pos 頂点の位置ベクトル (3次元)

```
tensor([[ 0.0264,  1.4944,  0.0287],  
       [-0.0850,  0.0111,  0.0449],  
       [-1.0957, -0.8588, -0.2308],  
       [-0.5082, -2.1326, -0.0113],  
       [ 0.7433, -2.0451,  0.3632],  
       [ 1.0156, -0.6777,  0.3997],  
       [ 0.8032,  1.8213, -0.6702],  
       [-0.9230,  1.9401, -0.2734],  
       [ 0.2923,  1.8782,  1.0190],  
       [-2.1005, -0.6271, -0.5415],  
       [-0.9559, -3.1113, -0.1136]])
```

## 辺の特徴ベクトル(4次元)

`mol.edge_attr`

**Single**  
**Double**  
**Triple**  
**Aromatic**

# (one-hot encoding)

# 実際の分子グラフデータを見てみよう

mol.z 頂点の原子番号

```
tensor([6, 6, 6, 6, 7, 8, 1, 1, 1, 1])
```

mol.x 頂点の特徴ベクトル (11次元)

```
tensor([[0., 1., 0., 0., 0., 6., 0., 0., 0., 0., 3.],
       [0., 1., 0., 0., 0., 6., 0., 0., 0., 0., 0.],
       [0., 1., 0., 0., 0., 6., 0., 0., 0., 0., 1.],
       [0., 1., 0., 0., 0., 6., 0., 0., 0., 0., 1.],
       [0., 0., 1., 0., 0., 7., 0., 0., 0., 0., 0.],
       [0., 0., 0., 1., 0., 8., 0., 0., 0., 0., 0.],
       [1., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0.],
       [1., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0.],
       [1., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0.],
       [1., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0.],
       [1., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0.]])
```

mol.pos 頂点の位置ベクトル (3次元)

```
tensor([[ 0.0264,  1.4944,  0.0287],
       [-0.0850,  0.0111,  0.0449],
       [-1.0957, -0.8588, -0.2308],
       [-0.5082, -2.1326, -0.0113],
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       [ 1.0156, -0.6777,  0.3997],
       [ 0.8032,  1.8213, -0.6702],
       [-0.9230,  1.9401, -0.2734],
       [ 0.2923,  1.8782,  1.0190],
       [-2.1005, -0.6271, -0.5415],
       [-0.9559, -3.1113, -0.1136]])
```

辺の特徴ベクトル (4次元)

mol.edge\_attr

```
tensor([[1., 0., 0., 0.],
       [1., 0., 0., 0.],
       [1., 0., 0., 0.],
       [1., 0., 0., 0.],
       [1., 0., 0., 0.],
       [1., 0., 0., 0.],
       [0., 1., 0., 0.],
       [1., 0., 0., 0.],
       [0., 1., 0., 0.],
       [1., 0., 0., 0.],
       [1., 0., 0., 0.],
       [1., 0., 0., 0.],
       [1., 0., 0., 0.],
       [1., 0., 0., 0.],
       [1., 0., 0., 0.],
       [1., 0., 0., 0.],
       [1., 0., 0., 0.],
       [1., 0., 0., 0.],
       [1., 0., 0., 0.],
       [1., 0., 0., 0.],
       [1., 0., 0., 0.],
       [1., 0., 0., 0.],
       [1., 0., 0., 0.]]))
```

Single  
Double  
Triple  
Aromatic

(one-hot  
encoding)

# 実際の分子グラフデータを見てみよう

mol.x

頂点の特徴ベクトル (11次元)

```
tensor([[0., 1., 0., 0., 0., 6., 0., 0., 0., 0., 3.],  
       [0., 1., 0., 0., 0., 6., 0., 0., 0., 0., 0.],  
       [0., 1., 0., 0., 0., 6., 0., 0., 0., 0., 1.],  
       [0., 1., 0., 0., 0., 6., 0., 0., 0., 0., 1.],  
       [0., 0., 1., 0., 0., 7., 0., 0., 0., 0., 0.],  
       [0., 0., 0., 1., 0., 8., 0., 0., 0., 0., 0.],  
       [1., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0.],  
       [1., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0.],  
       [1., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0.],  
       [1., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0.],  
       [1., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0.]])
```

0  
1  
2  
3  
4  
5  
6  
7  
8  
9  
10

H C N O F  
(one-hot  
encoding)

原子番号  
(one-hot  
encoding)

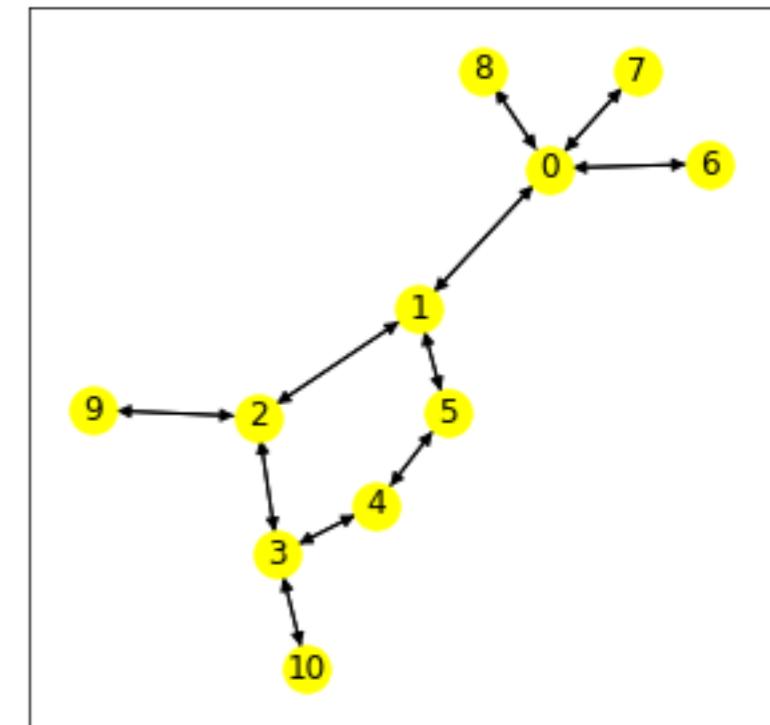
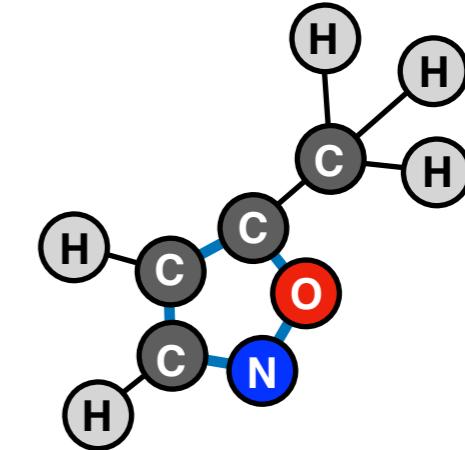
aromatic? (0/1)

sp? (0/1)

sp<sup>2</sup>? (0/1)

sp<sup>3</sup>? (0/1)

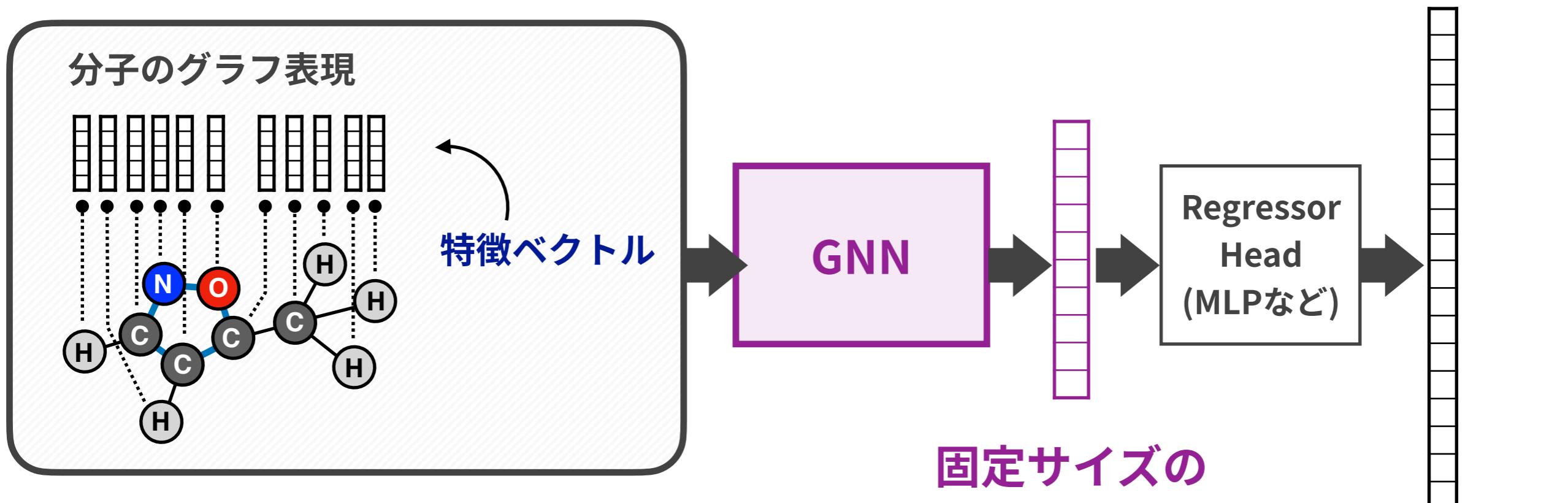
結合するHの数



これ以外にもいろいろ有りえることに注意

# GNNがやること

可変サイズの分子グラフから「固定サイズのベクトル表現」への変換を学習



**mol.x** 頂点の特徴ベクトル (11次元)

**mol.pos** 頂点の位置ベクトル (3次元)

**mol.edge\_attr** 辺の特徴ベクトル (4次元)

**mol.edge\_index** 辺と結合原子ペアの対応

**mol.y**

DFT計算値  
(19次元)

# 本日の内容

---

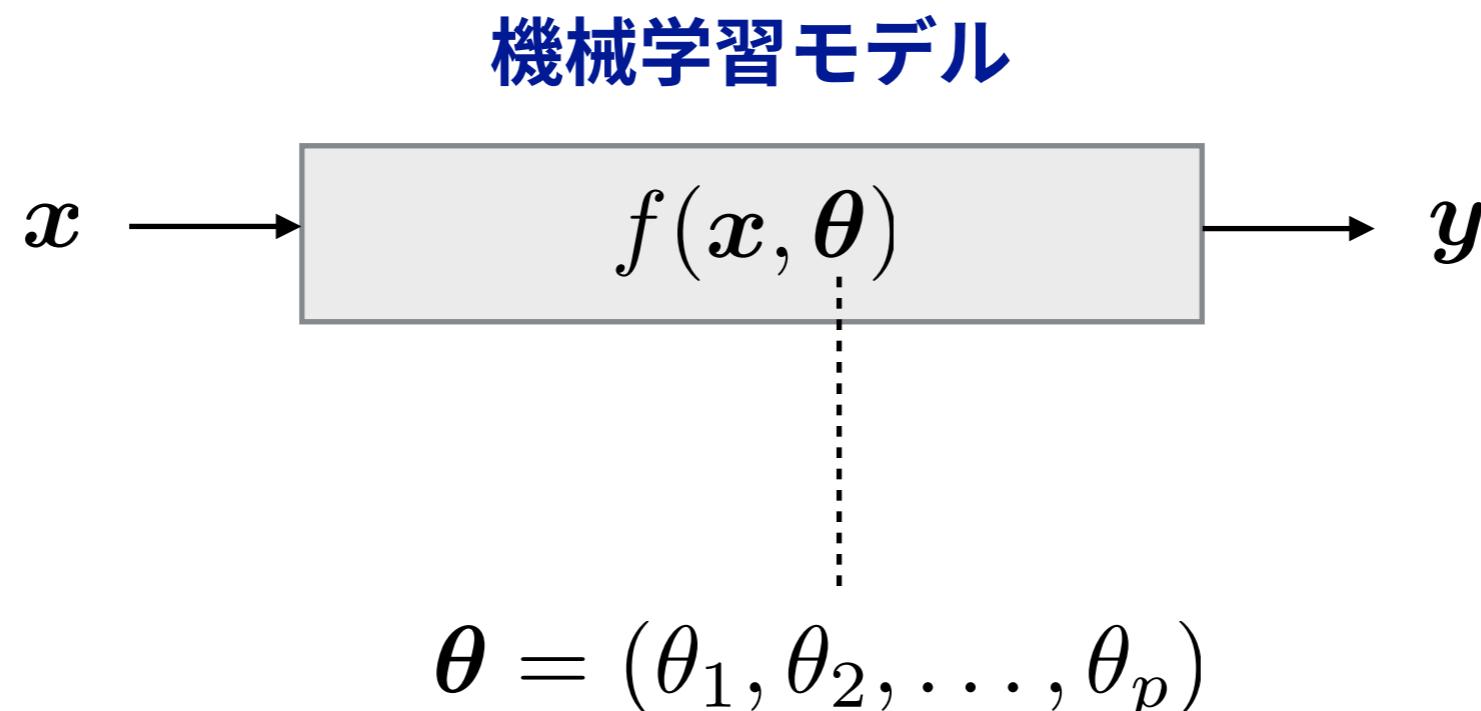
GNN(Graph Neural Networks)でグラフ表現された分子を  
入力にして機械学習するやり方をのぞいてみませんか？

- 機械学習とは？
- 分子のグラフ表現
- 準備：深層学習のココロ (forwardとbackward)
- Graph Neural Networksとは？
- 自分でやってみるための情報
- おまけ：  
最近の話 (計算限界、分子生成、事前学習、...)

# 機械学習のモデル

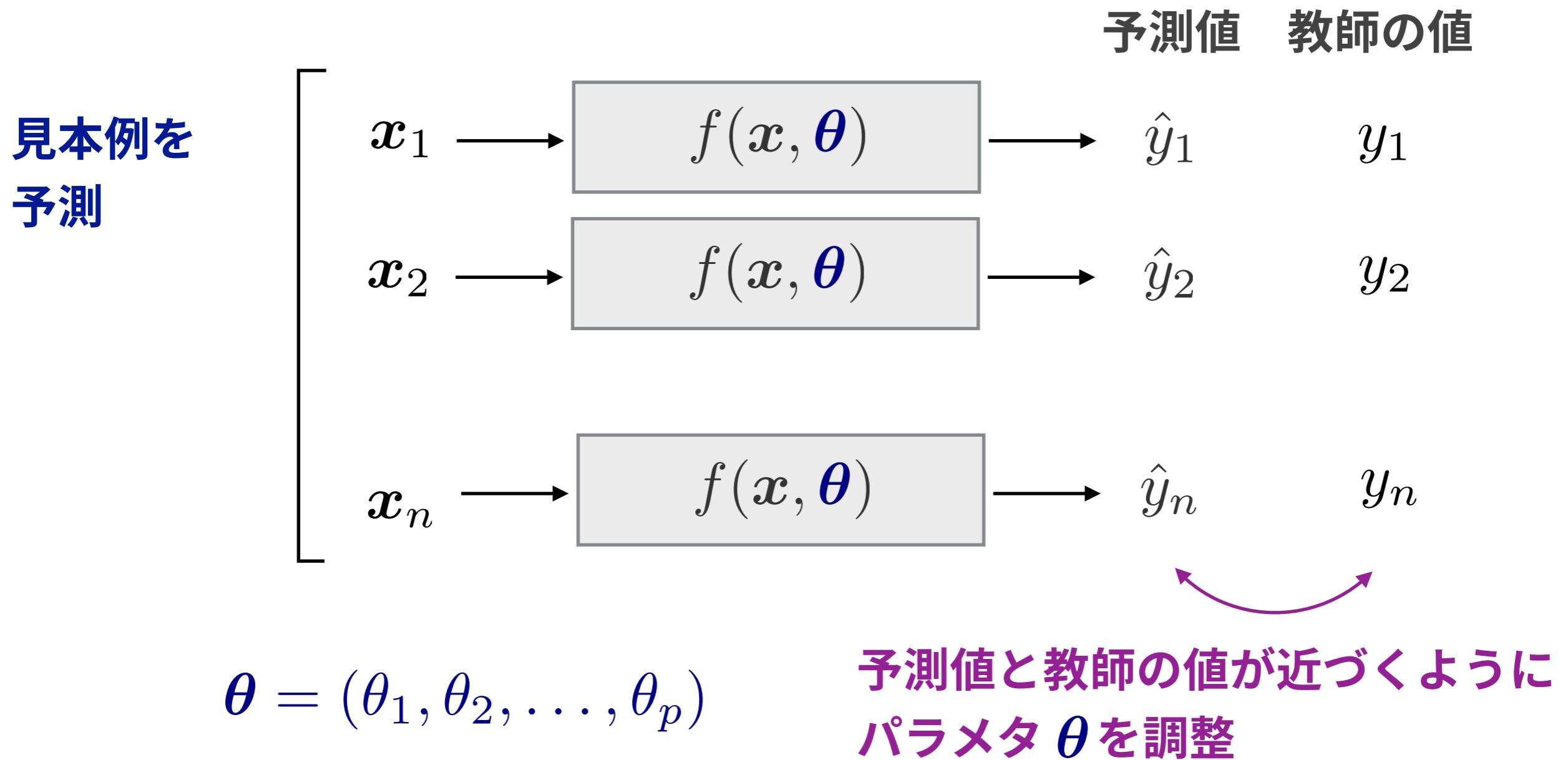
---

機械学習 = 多量の入出力の見本例からプログラムを自動的に作成する(いいかげんな)技術



多数のパラメタの値を動かして  
出力が望む値になるようにする

# モデルの学習 = パラメタの値を最適にする



# モデルの学習 = パラメタの値を最適にする

予測値と教師の値が近づくように  
パラメタ  $\theta$  を調整

関数  $\text{loss}(\theta)$  の値が小さくなる  
ようにパラメタ  $\theta$  を調整

パラメタ調整のやりかた：

- $\theta$  をランダム値で初期化
- $\text{loss}(\theta)$  の値が小さくなるように  $\theta$  をちょっとだけ変える

$$\begin{bmatrix} \theta_1 \\ \theta_2 \\ \vdots \\ \theta_p \end{bmatrix} \leftarrow \begin{bmatrix} \theta_1 \\ \theta_2 \\ \vdots \\ \theta_p \end{bmatrix} + 0.01 \times \begin{bmatrix} \Delta\theta_1 \\ \Delta\theta_2 \\ \vdots \\ \Delta\theta_p \end{bmatrix}$$

くりかえし

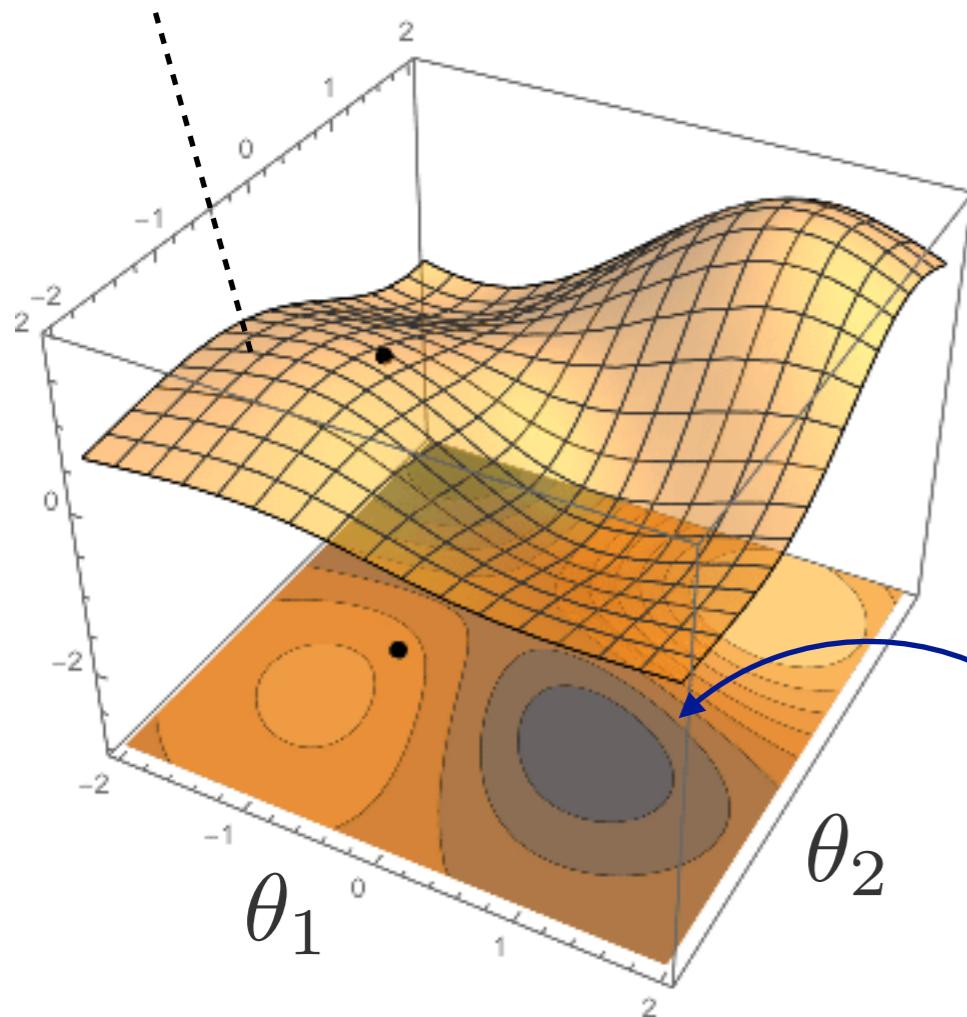
学習率  
(step size)

# 勾配降下法 (Gradient Descent)

- loss( $\theta$ ) の値が小さくなるように  $\theta$  をちょっとだけ変える

$$\begin{bmatrix} \theta_1 \\ \theta_2 \end{bmatrix} \leftarrow \begin{bmatrix} \theta_1 \\ \theta_2 \end{bmatrix} + 0.01 \times \begin{bmatrix} f'_1(\theta_1, \theta_2) \\ f'_2(\theta_1, \theta_2) \end{bmatrix}$$

loss( $\theta_1, \theta_2$ )



勾配ベクトル

$$f'_1(\theta_1, \theta_2) = \frac{\partial \text{loss}(\theta_1, \theta_2)}{\partial \theta_1}$$

$$f'_2(\theta_1, \theta_2) = \frac{\partial \text{loss}(\theta_1, \theta_2)}{\partial \theta_2}$$

偏微分

$\theta_1$  や  $\theta_2$  を  
少し動かしたときの  
loss( $\theta_1, \theta_2$ ) の変化量

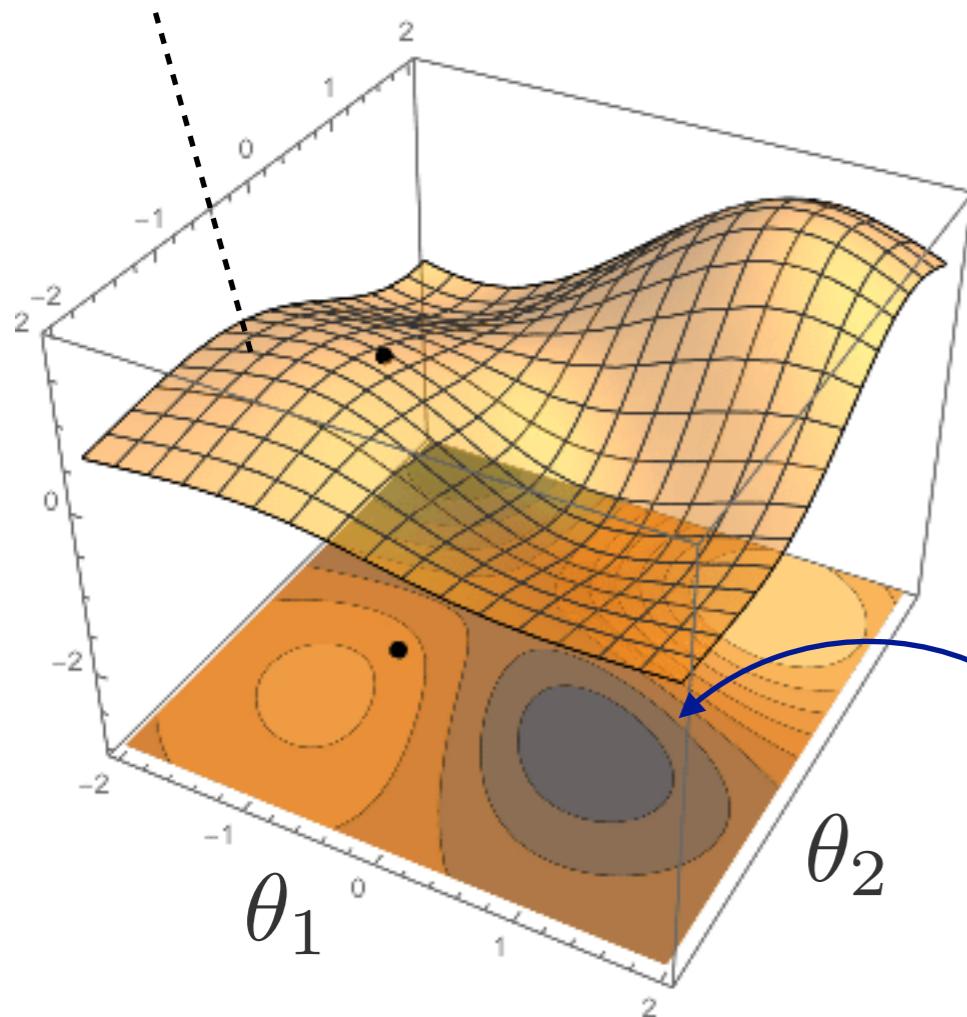
勾配ベクトルに比例する量をちょっと引くと  
最寄りの極小値に向かうことがわかっている

# 勾配降下法 (Gradient Descent)

- loss( $\theta$ ) の値が小さくなるように  $\theta$  をちょっとだけ変える

$$\begin{bmatrix} \theta_1 \\ \theta_2 \end{bmatrix} \leftarrow \begin{bmatrix} \theta_1 \\ \theta_2 \end{bmatrix} + 0.01 \times \begin{bmatrix} f'_1(\theta_1, \theta_2) \\ f'_2(\theta_1, \theta_2) \end{bmatrix}$$

loss( $\theta_1, \theta_2$ )



勾配ベクトル

$$f'_1(\theta_1, \theta_2) = \frac{\partial \text{loss}(\theta_1, \theta_2)}{\partial \theta_1}$$

$$f'_2(\theta_1, \theta_2) = \frac{\partial \text{loss}(\theta_1, \theta_2)}{\partial \theta_2}$$

偏微分

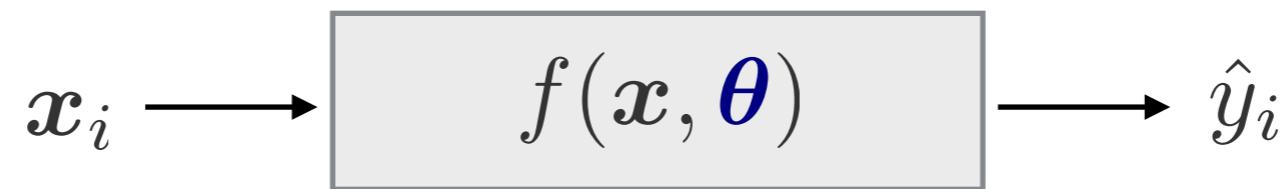
$\theta_1$  や  $\theta_2$  を  
少し動かしたときの  
loss( $\theta_1, \theta_2$ ) の変化量

勾配ベクトルに比例する量をちょっと引くと  
最寄りの極小値に向かうことがわかっている

# 計算グラフと自動微分：複雑なモデルの勾配の計算

---

機械学習モデル



小さくしたい尺度

$$\text{loss}(\theta) = \sum_{i=1}^n (\hat{y}_i - y_i)^2$$

$$= \sum_{i=1}^n (f(x_i, \theta) - y_i)^2$$

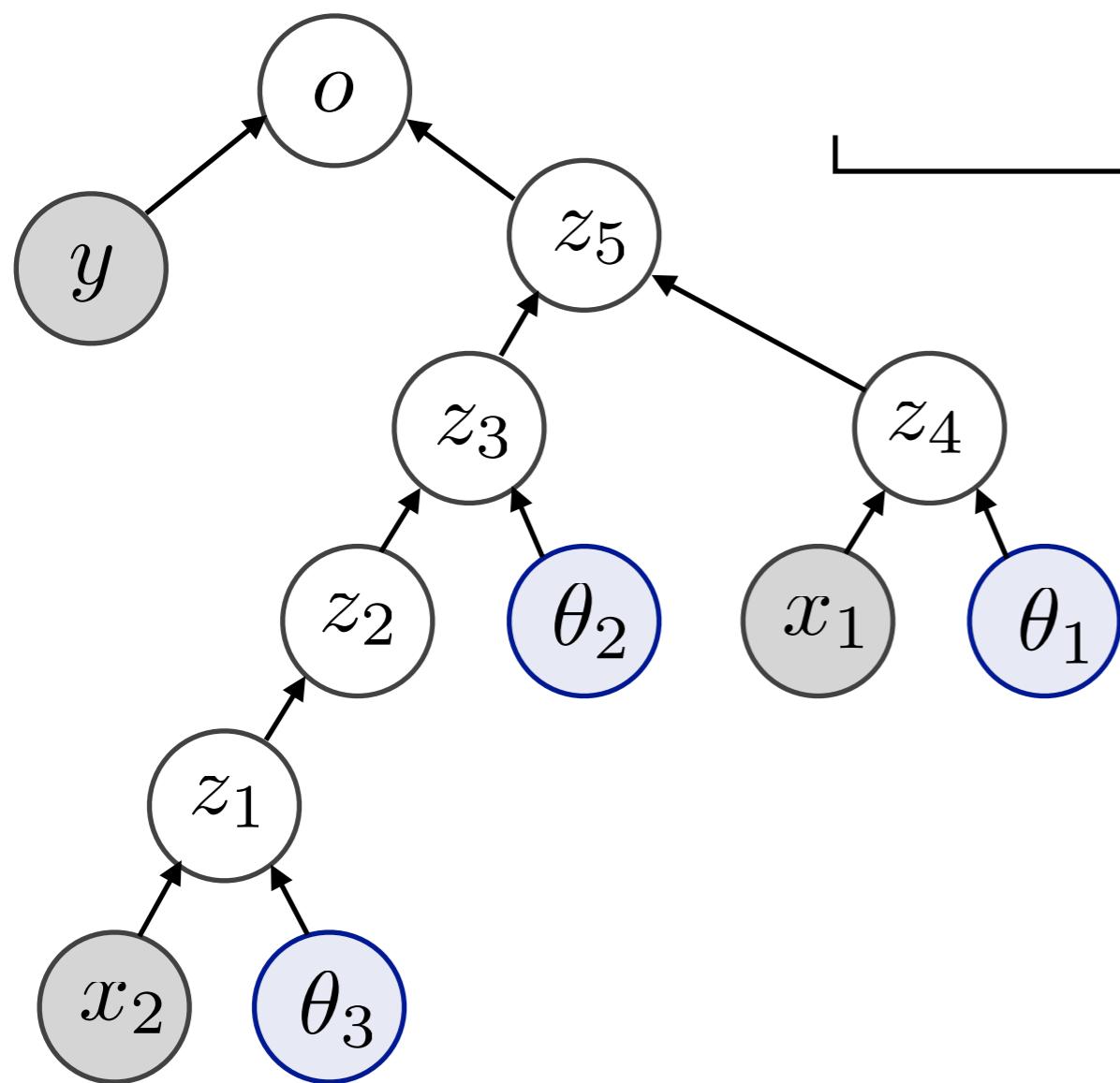
勾配ベクトル

$$\begin{bmatrix} \partial \text{loss}(\theta) / \partial \theta_1 \\ \partial \text{loss}(\theta) / \partial \theta_2 \\ \vdots \\ \partial \text{loss}(\theta) / \partial \theta_p \end{bmatrix}$$

# 計算グラフと自動微分：複雑なモデルの勾配の計算

$$\text{例 } g(\theta_1, \theta_2) = \left( \underline{f(x_1, x_2, \theta_1, \theta_2, \theta_3)} - y \right)^2$$

$$= \underbrace{\theta_1 x_1 - \theta_2 \cos(\theta_3 + x_2)}_{z_4} \underbrace{z_1}_{z_2} \underbrace{z_3}_{z_5}$$



## 合成関数

$$\begin{aligned} z_1 &= \theta_3 + x_2 \\ z_2 &= \cos(z_1) \end{aligned}$$

$$z_3 = \theta_2 z_2$$

$$z_4 = \theta_1 x_1$$

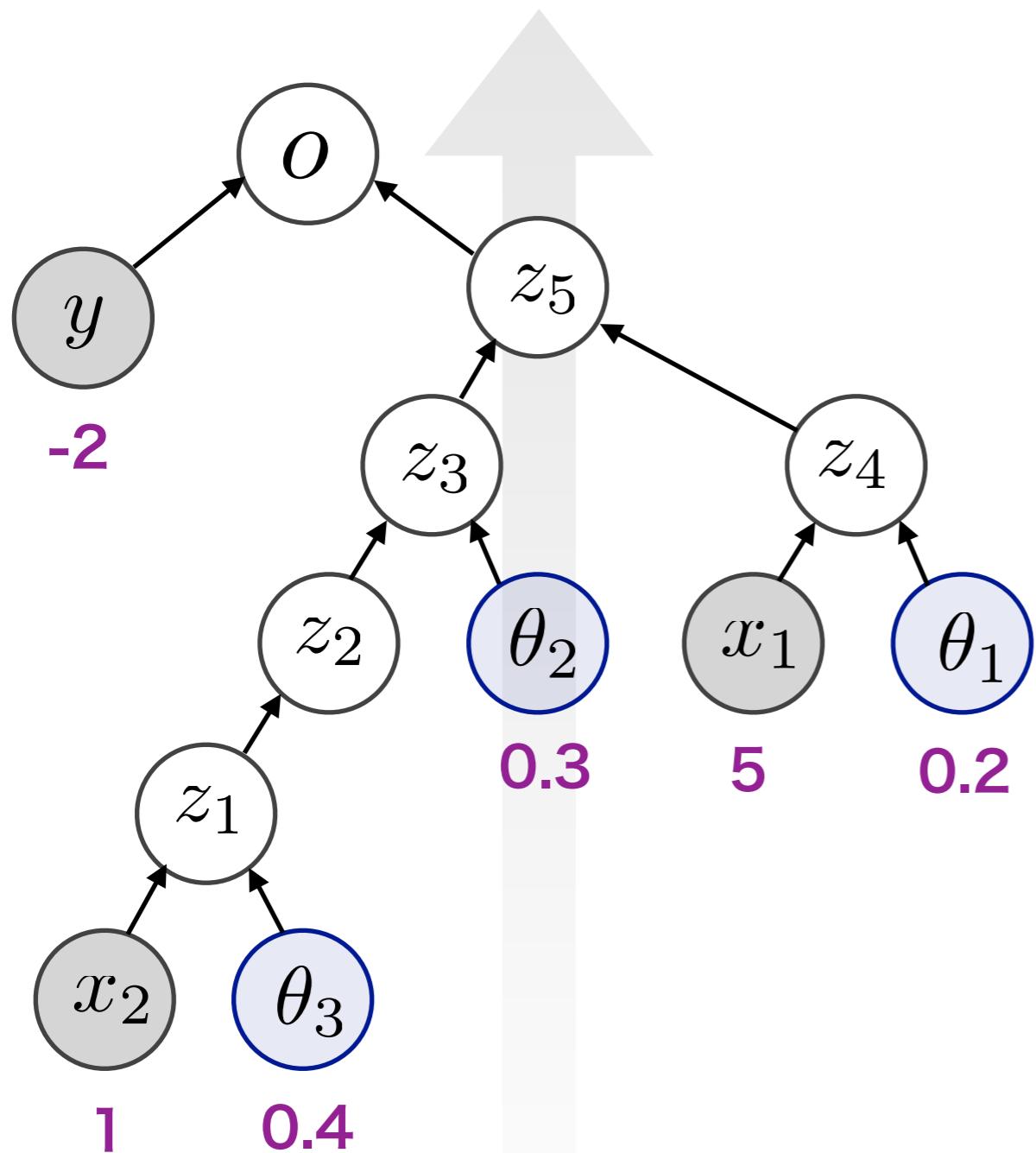
$$z_5 = z_4 - z_3$$

$$o = (z_5 - y)^2$$

# forward

---

このとき  $o$  は？



$$o = (z_5 - y)^2$$

$$z_5 = z_4 - z_3$$

$$z_4 = \theta_1 x_1$$

$$z_3 = \theta_2 z_2$$

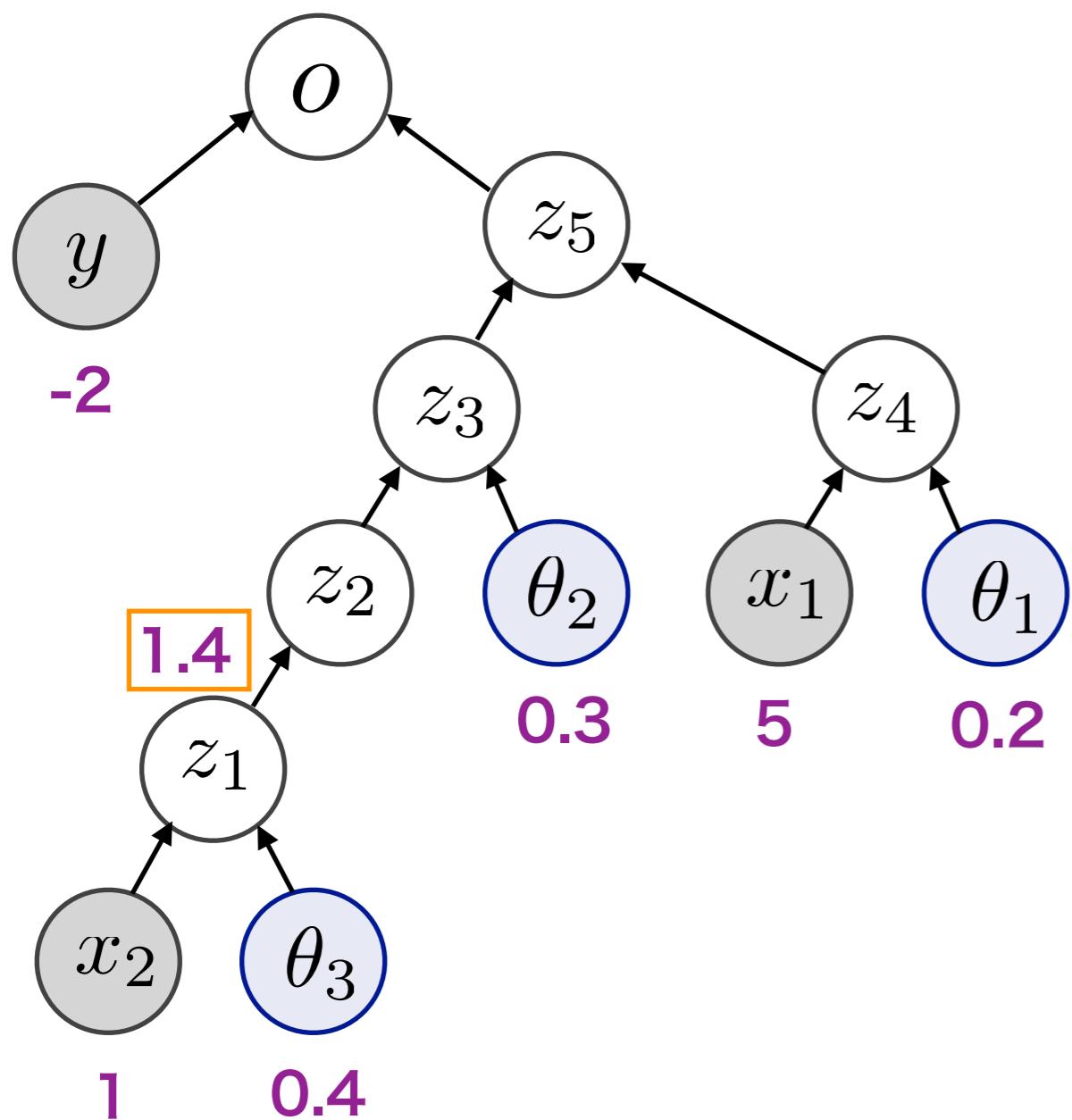
$$z_2 = \cos(z_1)$$

$$z_1 = \theta_3 + x_2$$

# forward

---

このとき  $o$  は？



$$o = (z_5 - y)^2$$

$$z_5 = z_4 - z_3$$

$$z_4 = \theta_1 x_1$$

$$z_3 = \theta_2 z_2$$

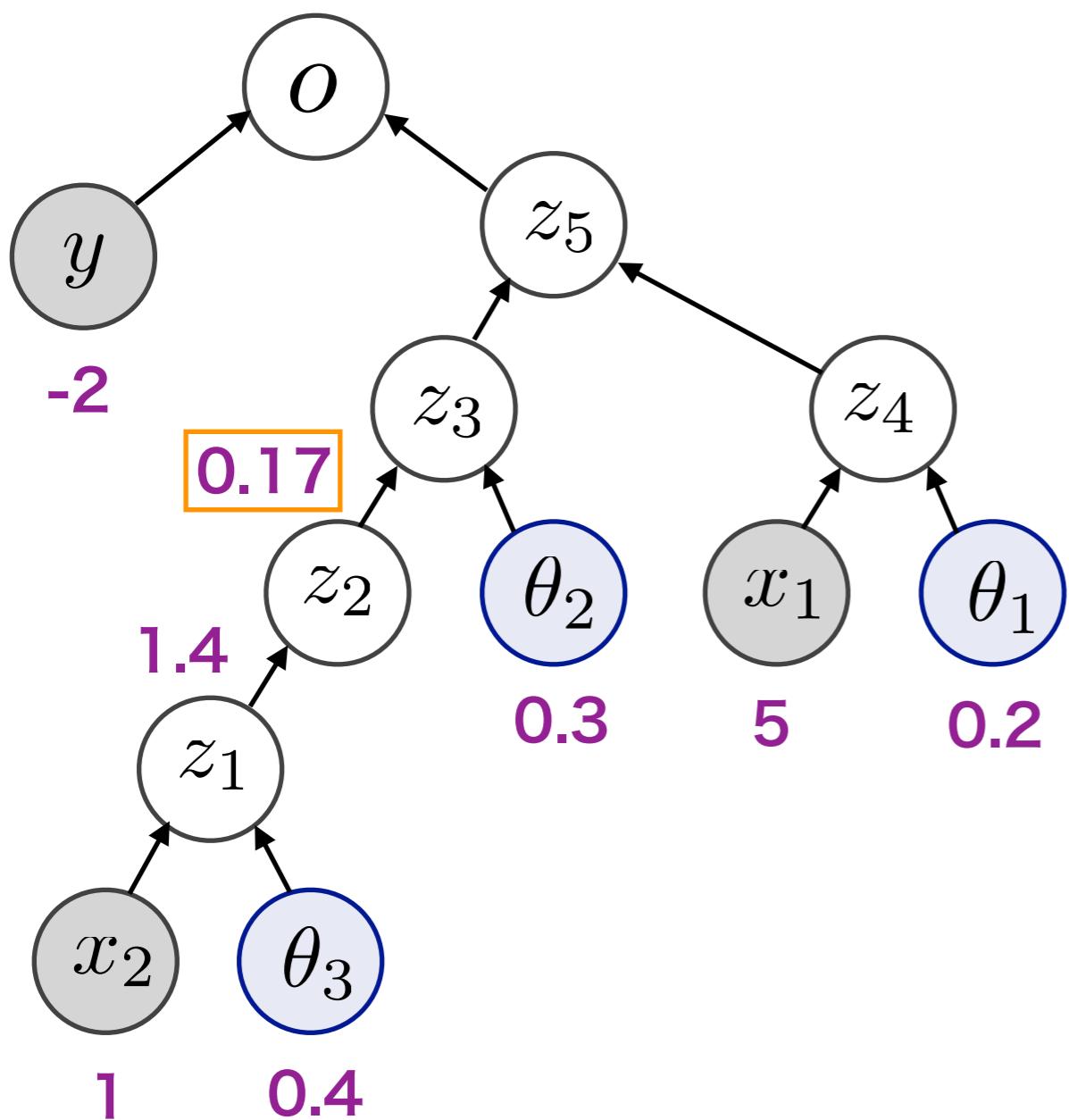
$$z_2 = \cos(z_1)$$

$$z_1 = \theta_3 + x_2$$

# forward

---

このとき  $o$  は？



$$o = (z_5 - y)^2$$

$$z_5 = z_4 - z_3$$

$$z_4 = \theta_1 x_1$$

$$z_3 = \theta_2 z_2$$

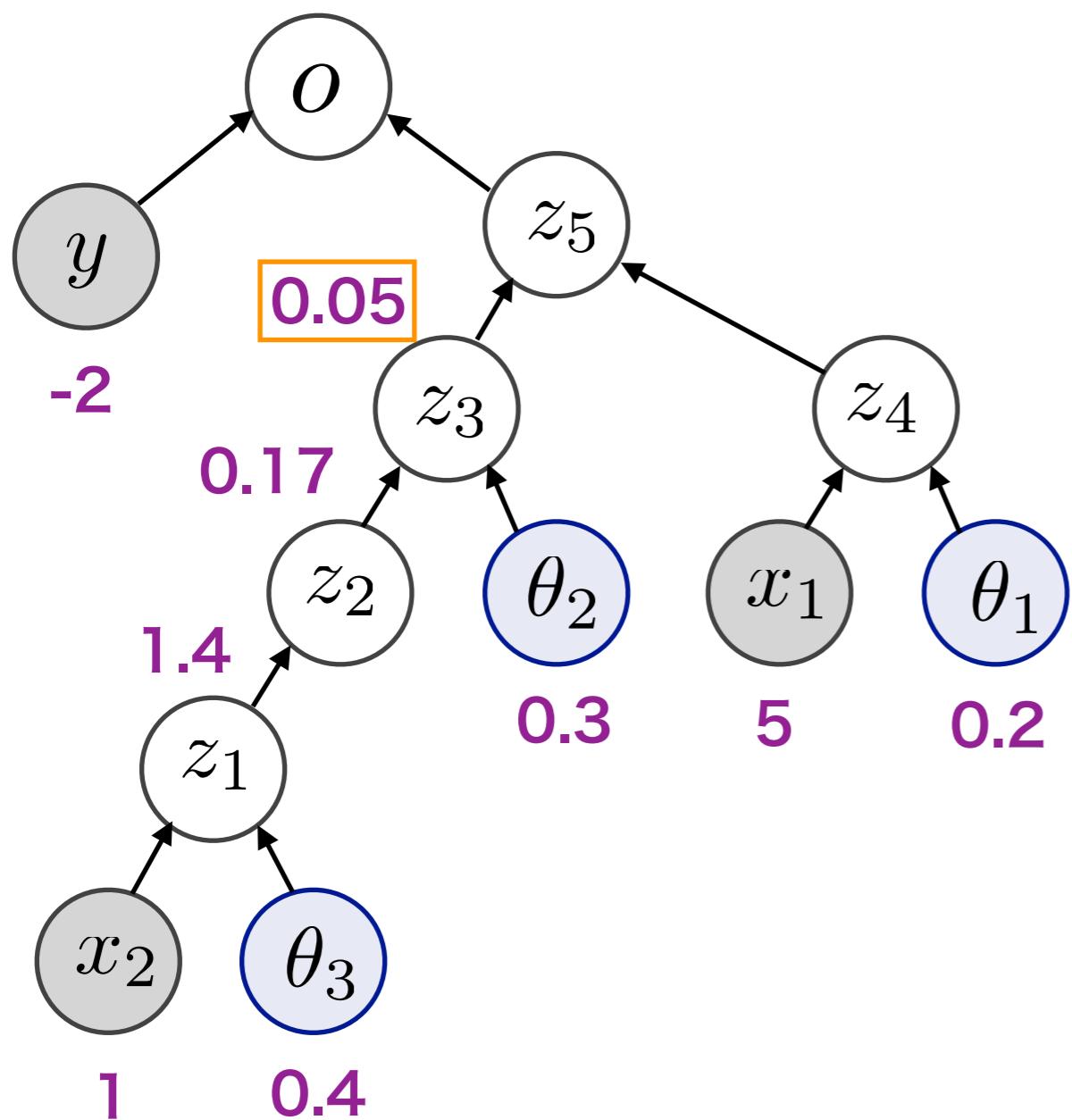
$$z_2 = \cos(z_1)$$

$$z_1 = \theta_3 + x_2$$

# forward

---

このとき  $o$  は？



$$o = (z_5 - y)^2$$

$$z_5 = z_4 - z_3$$

$$z_4 = \theta_1 x_1$$

$$z_3 = \theta_2 z_2$$

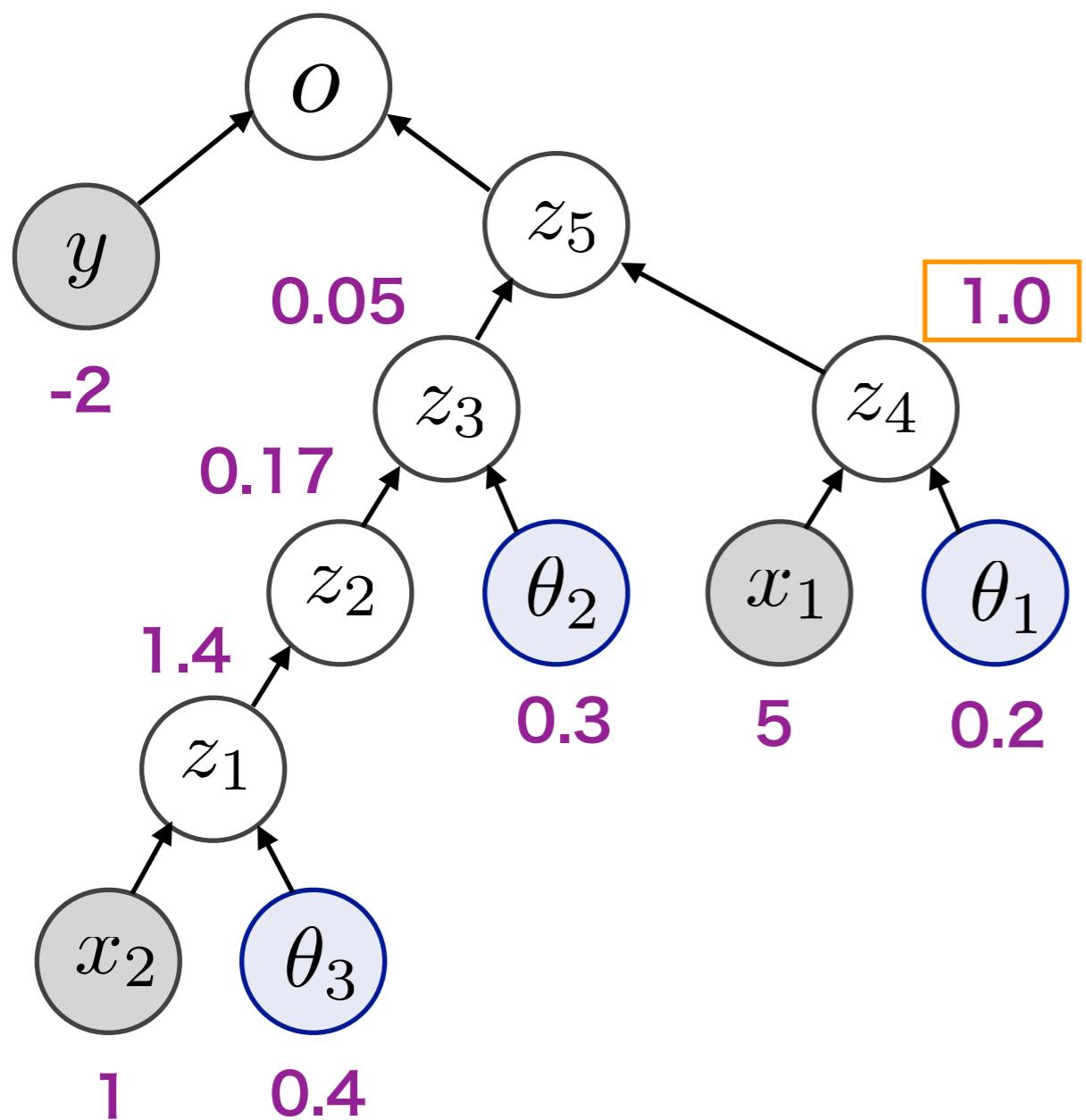
$$z_2 = \cos(z_1)$$

$$z_1 = \theta_3 + x_2$$

# forward

---

このとき  $o$  は？



$$o = (z_5 - y)^2$$

$$z_5 = z_4 - z_3$$

$$z_4 = \theta_1 x_1$$

$$z_3 = \theta_2 z_2$$

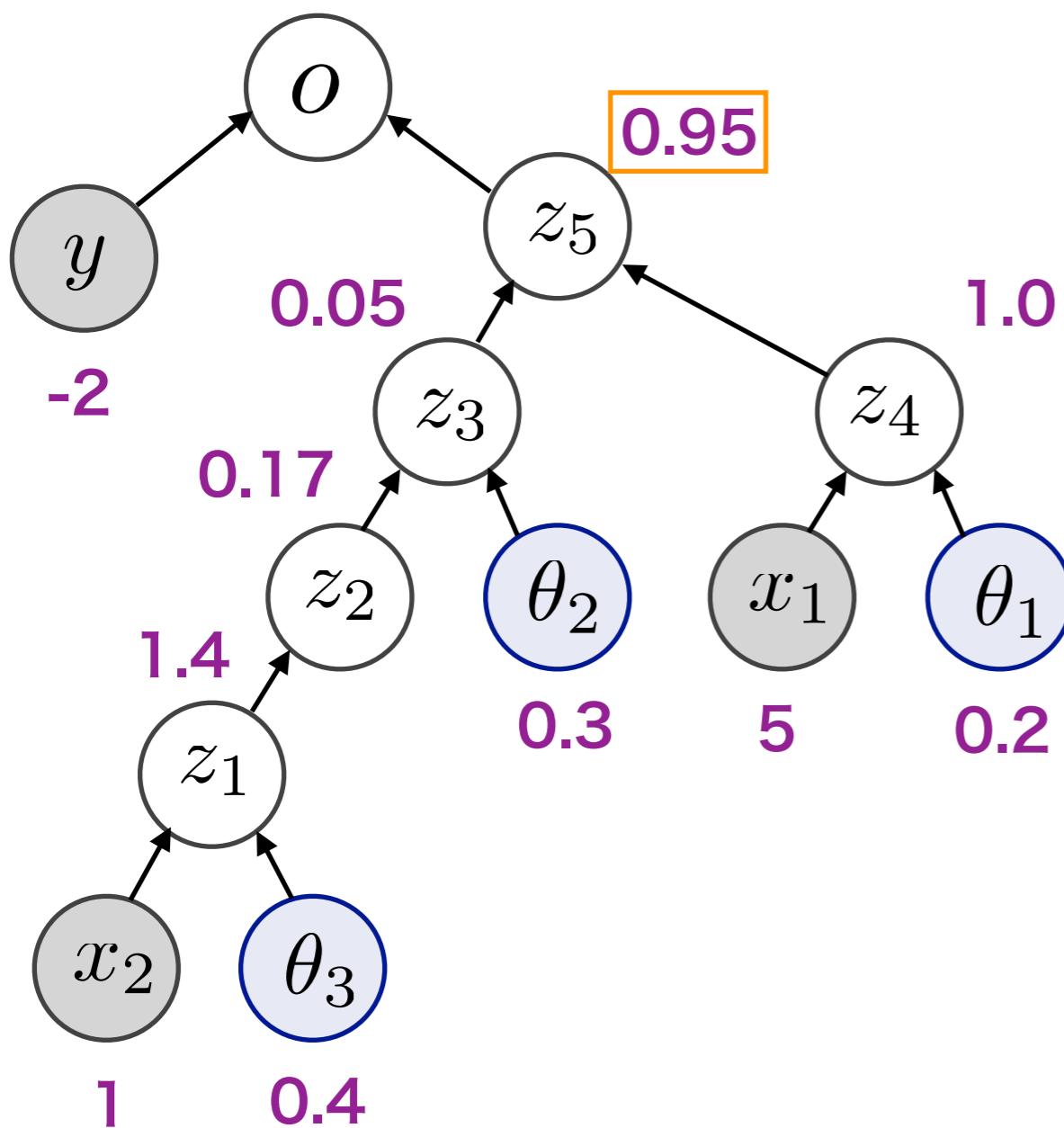
$$z_2 = \cos(z_1)$$

$$z_1 = \theta_3 + x_2$$

# forward

---

このとき  $o$  は？



$$o = (z_5 - y)^2$$

$$z_5 = z_4 - z_3$$

$$z_4 = \theta_1 x_1$$

$$z_3 = \theta_2 z_2$$

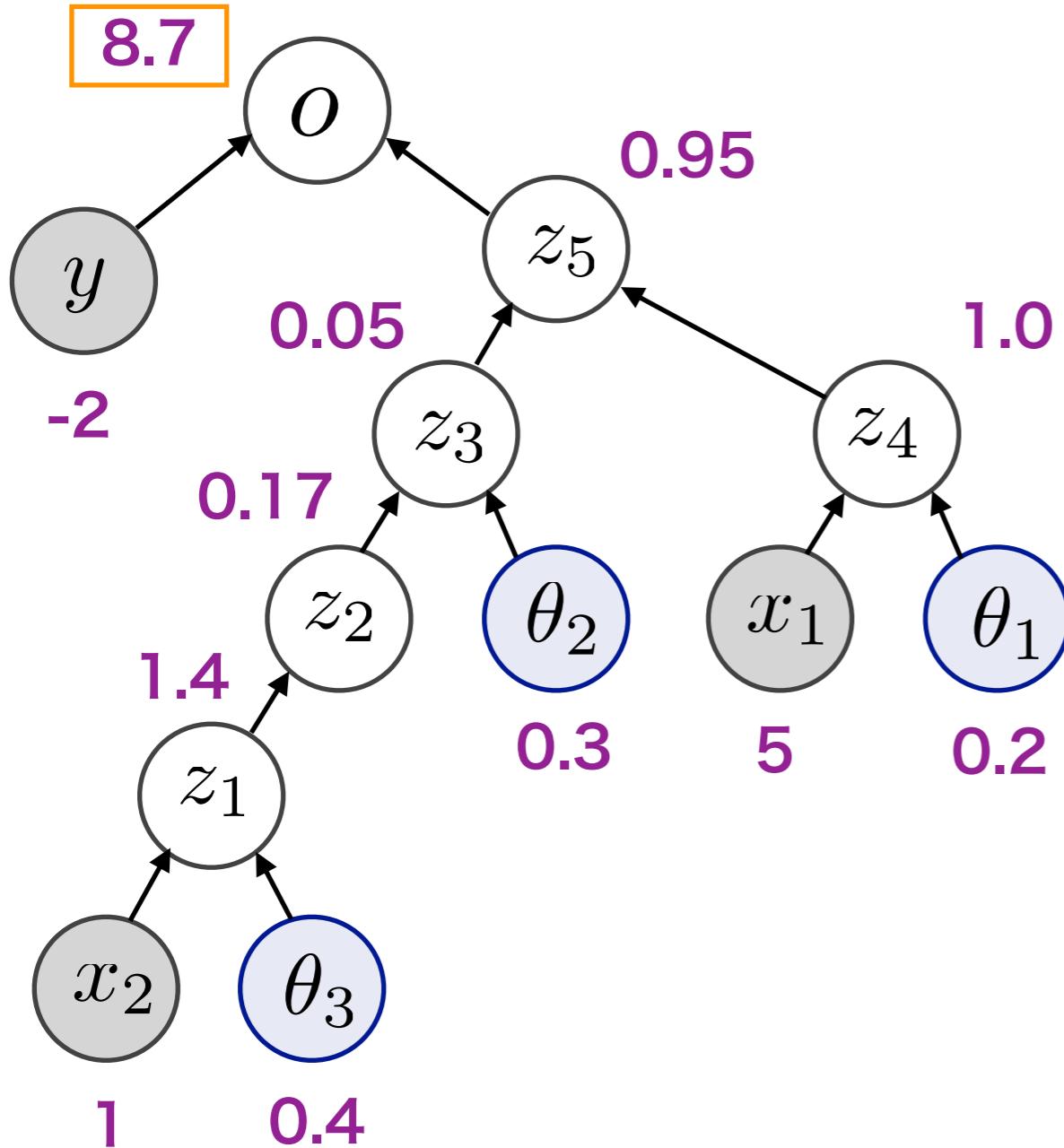
$$z_2 = \cos(z_1)$$

$$z_1 = \theta_3 + x_2$$

# forward

---

このとき  $o$  は？



$$o = (z_5 - y)^2$$

$$z_5 = z_4 - z_3$$

$$z_4 = \theta_1 x_1$$

$$z_3 = \theta_2 z_2$$

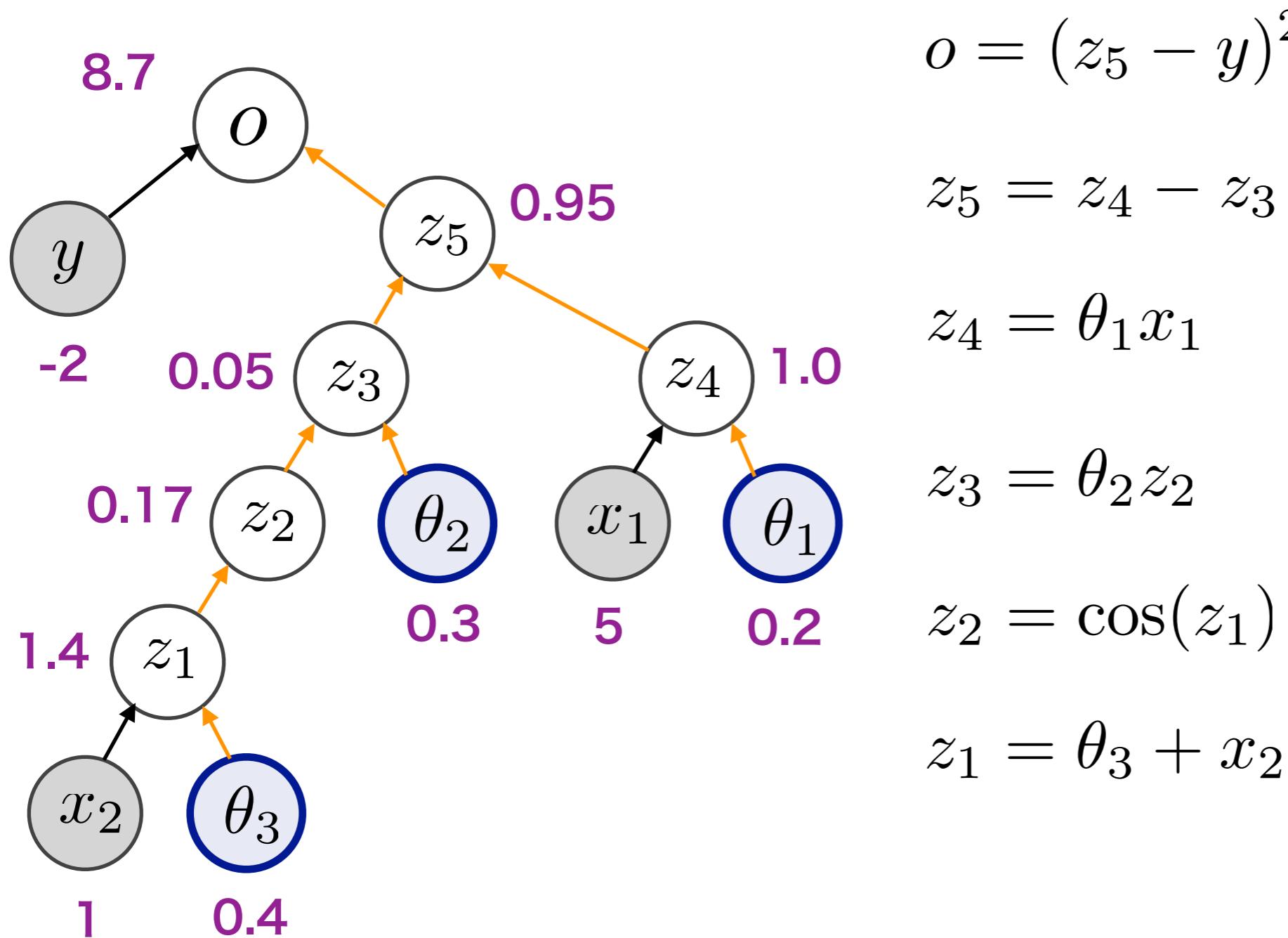
$$z_2 = \cos(z_1)$$

$$z_1 = \theta_3 + x_2$$

# forward

---

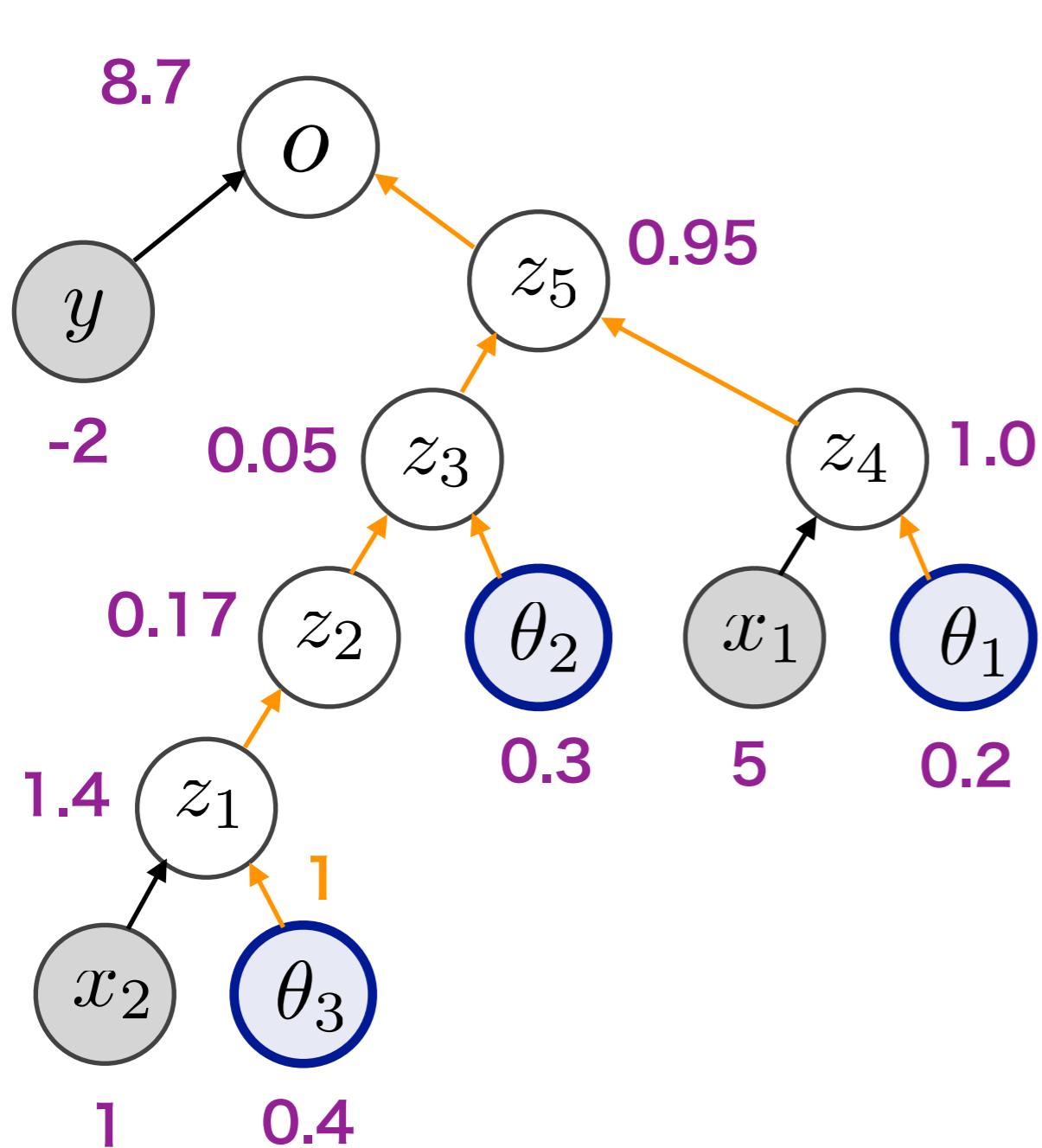
勾配を計算する変数はついでに各ステップの偏微分値も計算しておく



# forward

---

勾配を計算する変数はついでに各ステップの偏微分値も計算しておく



$$o = (z_5 - y)^2$$

$$z_5 = z_4 - z_3$$

$$z_4 = \theta_1 x_1$$

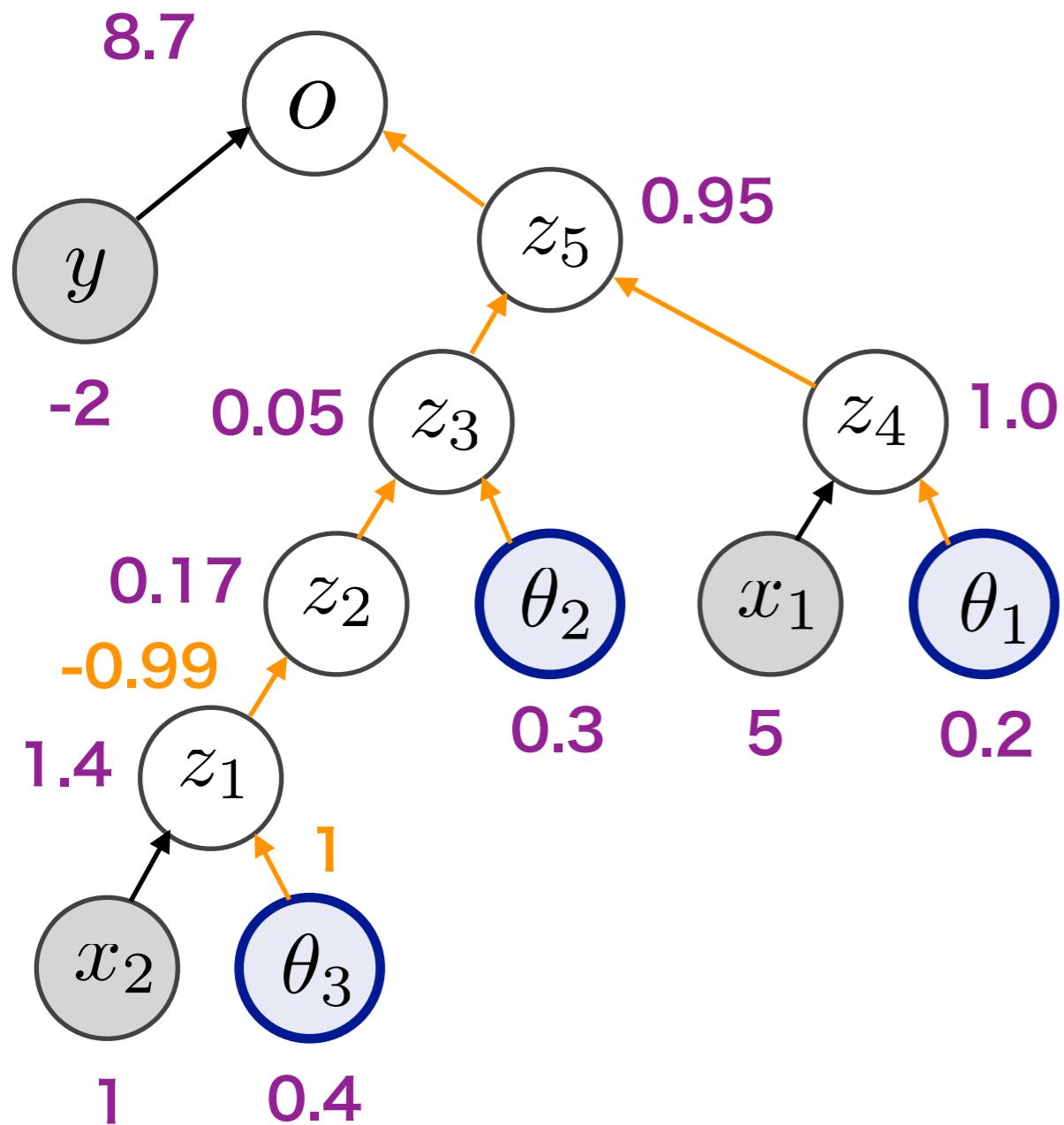
$$z_3 = \theta_2 z_2$$

$$z_2 = \cos(z_1)$$

$$z_1 = \theta_3 + x_2 \quad \partial z_1 / \partial \theta_3 = 1$$

# forward

勾配を計算する変数はついでに各ステップの偏微分値も計算しておく



$$o = (z_5 - y)^2$$

$$z_5 = z_4 - z_3$$

$$z_4 = \theta_1 x_1$$

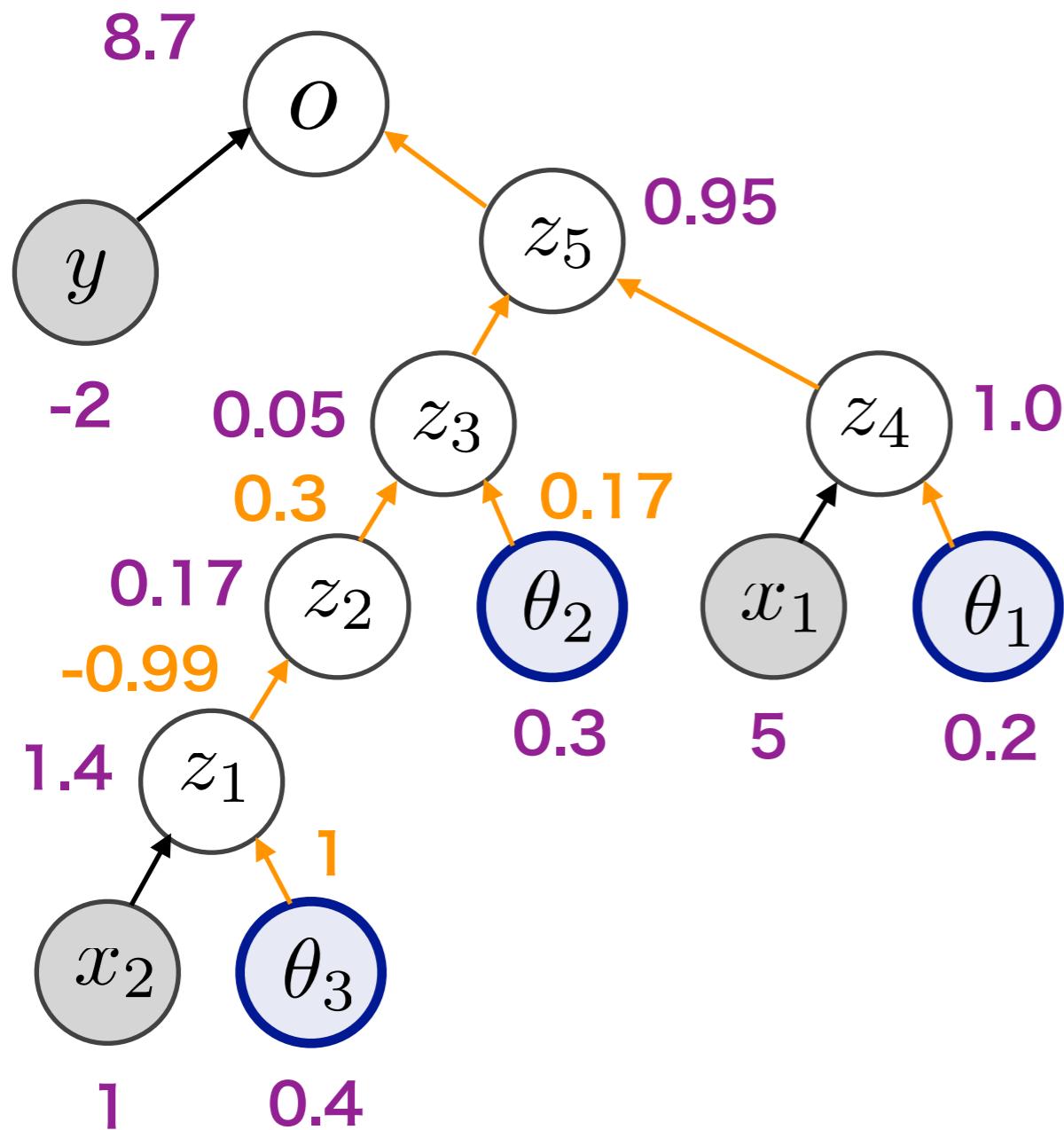
$$z_3 = \theta_2 z_2$$

$$z_2 = \cos(z_1) \quad \partial z_2 / \partial z_1 = -\sin(z_1)$$

$$z_1 = \theta_3 + x_2 \quad \partial z_1 / \partial \theta_3 = 1$$

# forward

勾配を計算する変数はついでに各ステップの偏微分値も計算しておく



$$o = (z_5 - y)^2$$

$$z_5 = z_4 - z_3$$

$$z_4 = \theta_1 x_1$$

$$z_3 = \theta_2 z_2$$

$$z_2 = \cos(z_1)$$

$$z_1 = \theta_3 + x_2$$

$$\partial z_3 / \partial z_2 = \theta_2$$

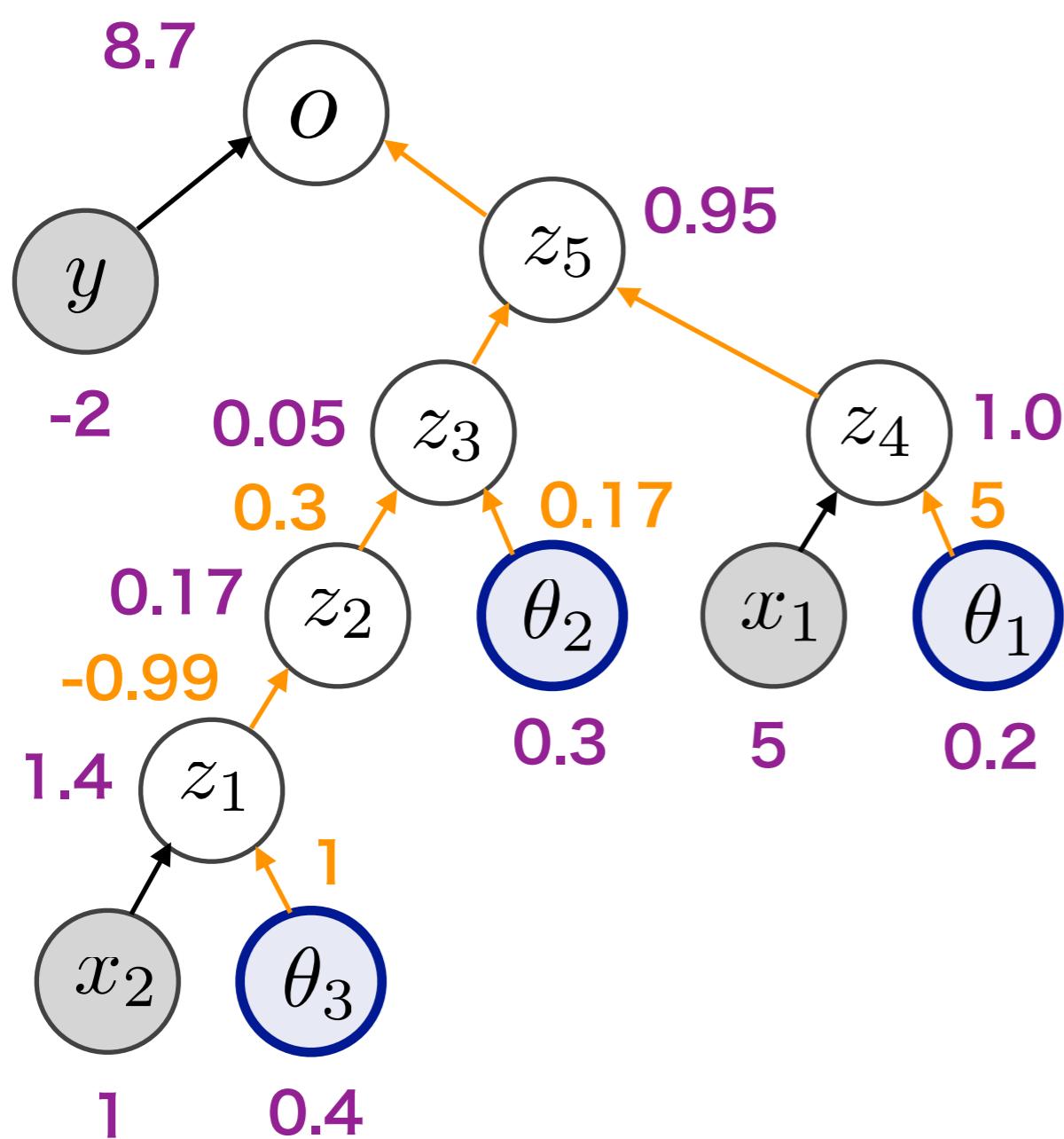
$$\partial z_3 / \partial \theta_2 = z_2$$

$$\partial z_2 / \partial z_1 = -\sin(z_1)$$

$$\partial z_1 / \partial \theta_3 = 1$$

# forward

勾配を計算する変数はついでに各ステップの偏微分値も計算しておく



$$o = (z_5 - y)^2$$

$$z_5 = z_4 - z_3$$

$$z_4 = \theta_1 x_1$$

$$\partial z_4 / \partial \theta_1 = x_1$$

$$z_3 = \theta_2 z_2$$

$$\partial z_3 / \partial z_2 = \theta_2$$

$$\partial z_3 / \partial \theta_2 = z_2$$

$$z_2 = \cos(z_1)$$

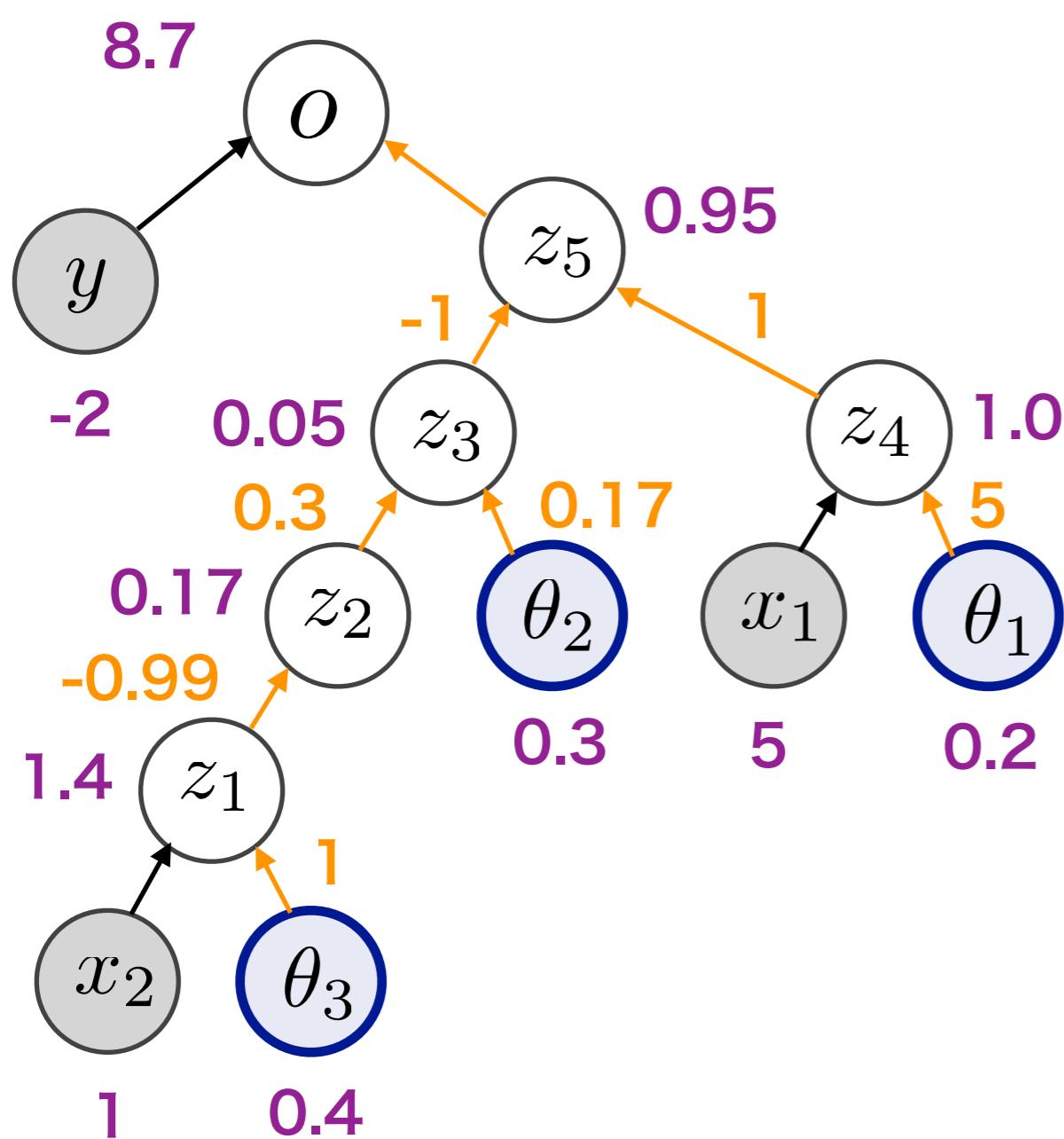
$$\partial z_2 / \partial z_1 = -\sin(z_1)$$

$$z_1 = \theta_3 + x_2$$

$$\partial z_1 / \partial \theta_3 = 1$$

# forward

勾配を計算する変数はついでに各ステップの偏微分値も計算しておく



$$o = (z_5 - y)^2$$

$$z_5 = z_4 - z_3$$

$$z_4 = \theta_1 x_1$$

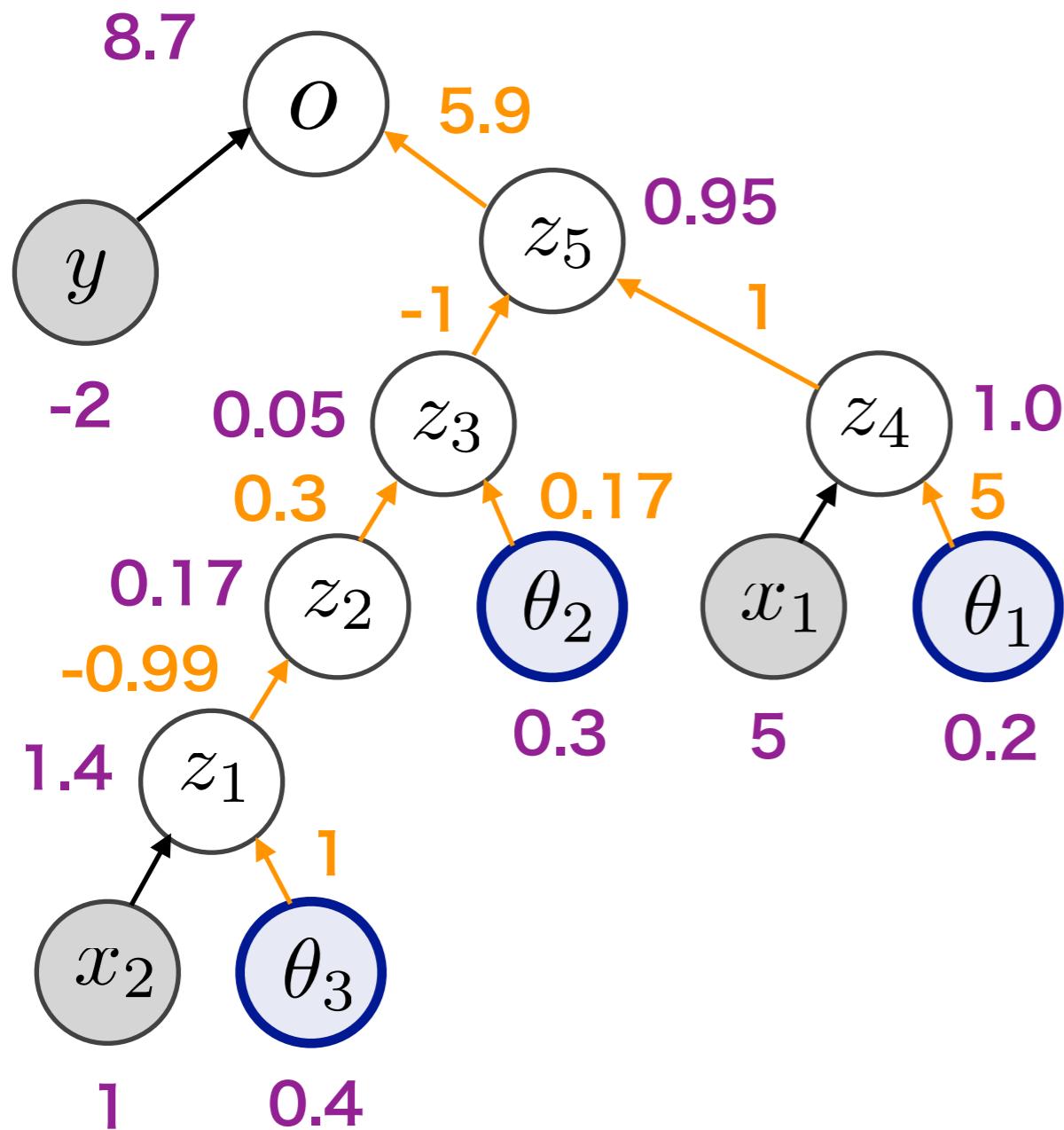
$$z_3 = \theta_2 z_2$$

$$z_2 = \cos(z_1)$$

$$z_1 = \theta_3 + x_2$$

# forward

勾配を計算する変数はついでに各ステップの偏微分値も計算しておく



$$o = (z_5 - y)^2 \quad \partial o / \partial z_5 = 2(z_5 - y)$$

$$z_5 = z_4 - z_3 \quad \partial z_5 / \partial z_4 = 1$$

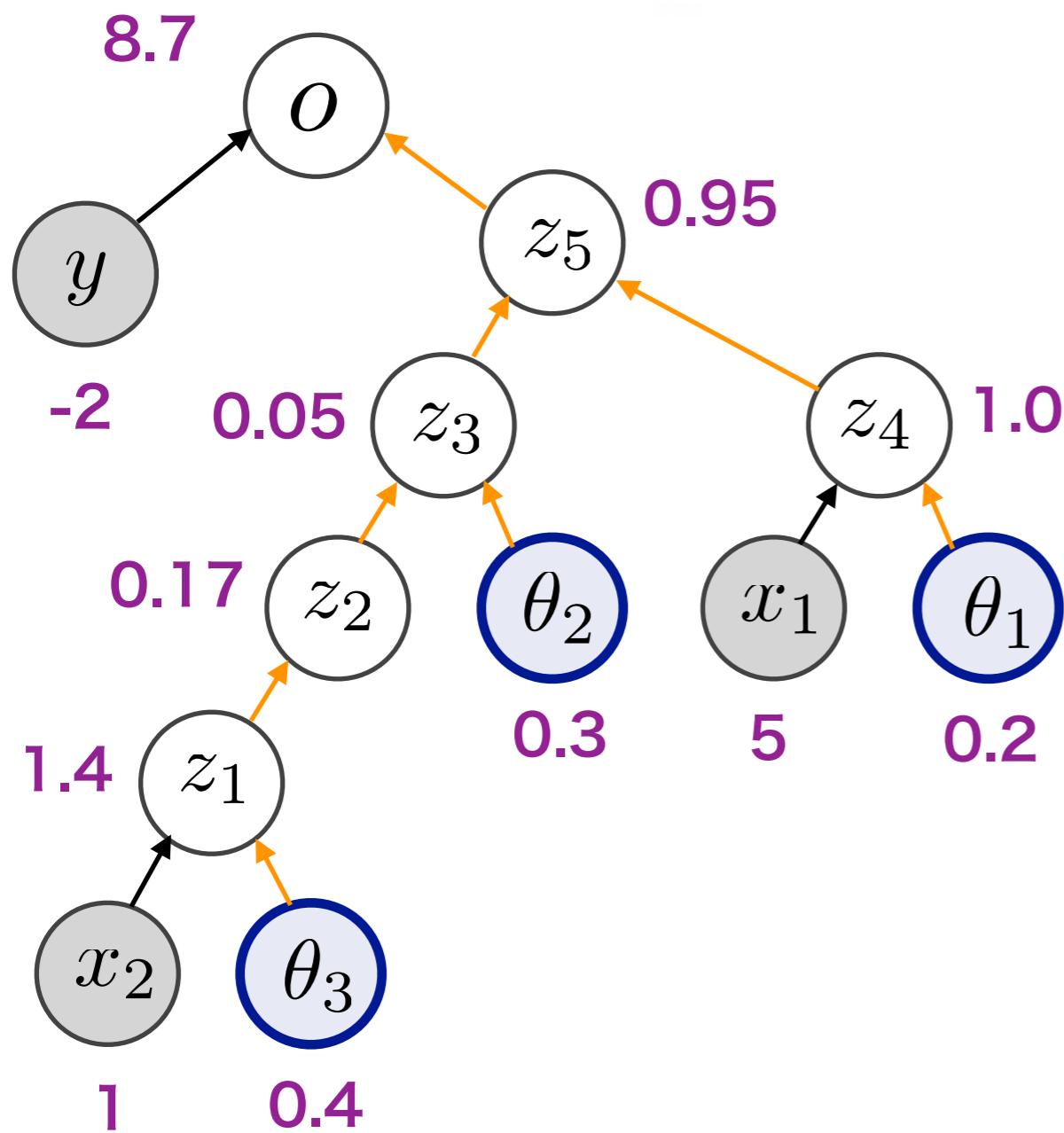
$$z_4 = \theta_1 x_1 \quad \partial z_4 / \partial \theta_1 = x_1$$

$$z_3 = \theta_2 z_2 \quad \partial z_3 / \partial z_2 = \theta_2$$

$$z_2 = \cos(z_1) \quad \partial z_2 / \partial z_1 = -\sin(z_1)$$

$$z_1 = \theta_3 + x_2 \quad \partial z_1 / \partial \theta_3 = 1$$

# forward



```
import torch
```

```
y = torch.tensor([-2])
x1 = torch.tensor([5])
x2 = torch.tensor([1])
theta1 = torch.tensor([0.2], requires_grad=True)
theta2 = torch.tensor([0.3], requires_grad=True)
theta3 = torch.tensor([0.4], requires_grad=True)
```

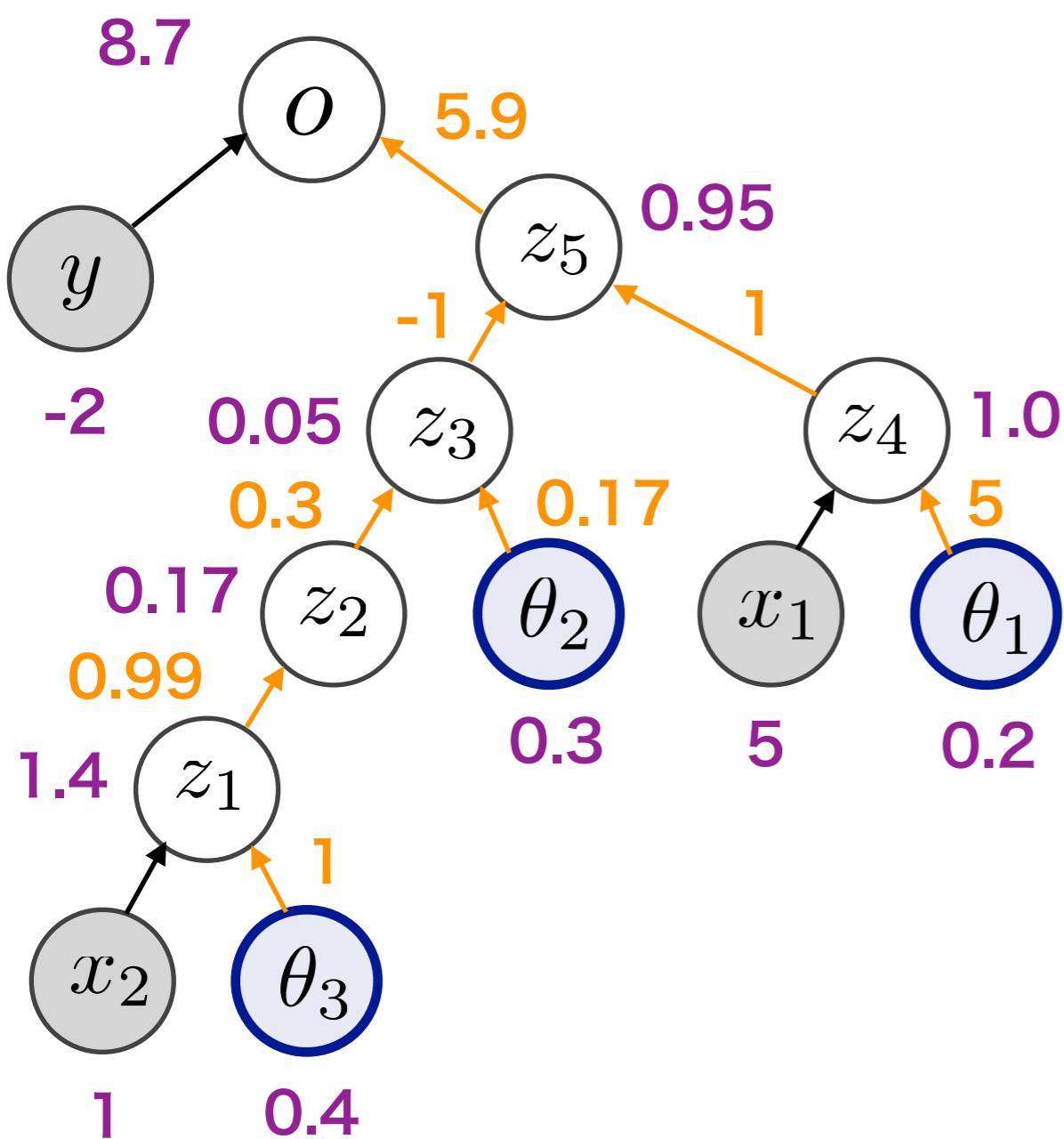
```
z1 = theta3 + x2
z2 = torch.cos(z1)
z3 = theta2 * z2
z4 = theta1 * x1
z5 = z4 - z3
o = (z5-y)**2
```

```
z1, z2, z3, z4, z5, o
```

```
(tensor([1.4000], grad_fn=<AddBackward0>),
 tensor([0.1700], grad_fn=<CosBackward>),
 tensor([0.0510], grad_fn=<MulBackward0>),
 tensor([1.], grad_fn=<MulBackward0>),
 tensor([0.9490], grad_fn=<SubBackward0>),
 tensor([8.6967], grad_fn=<PowBackward0>))
```

# 自動微分(リバースモード) "Back Propagation"

本当に計算したいのは勾配を計算する変数に関する偏微分

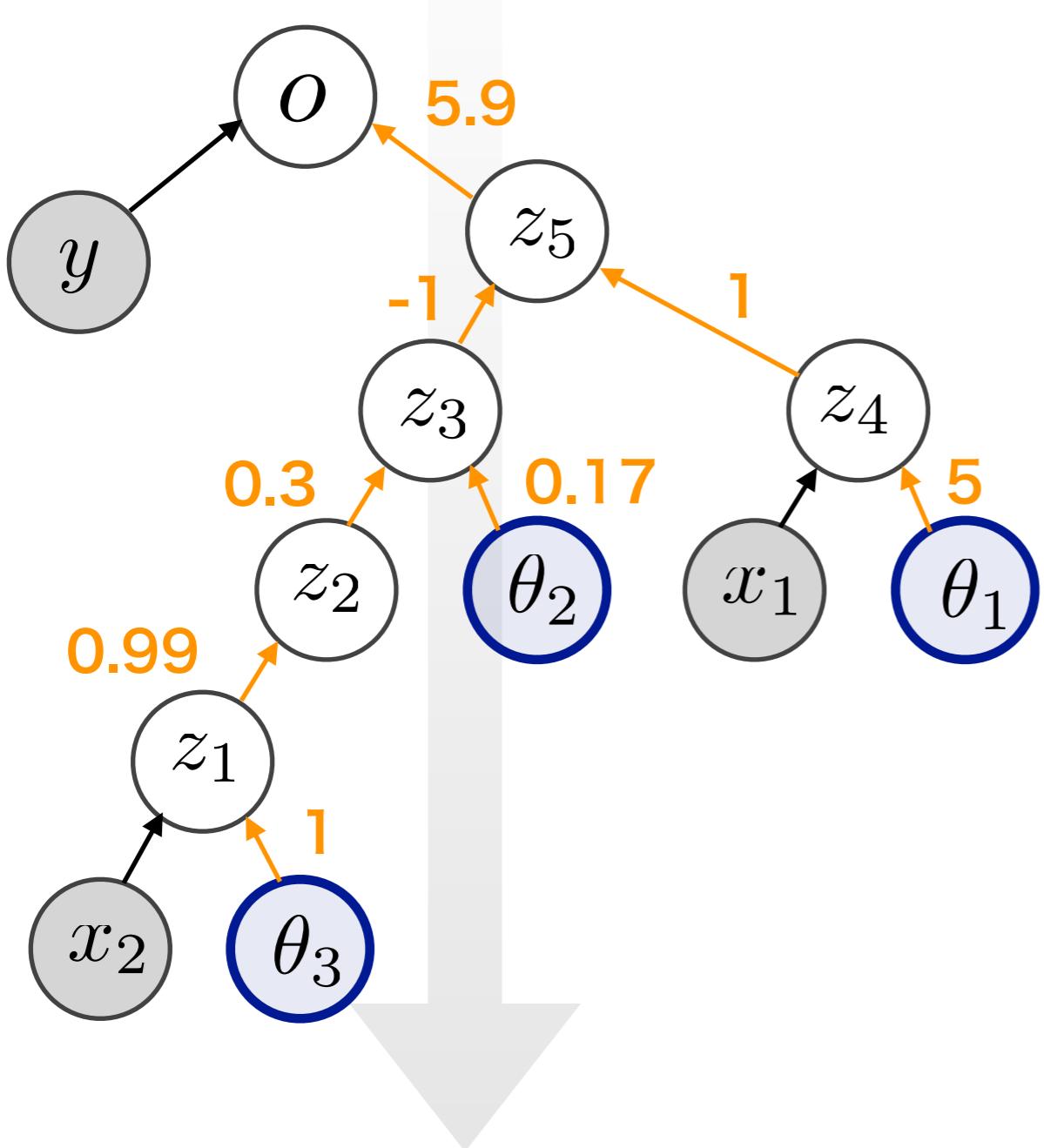


勾配  
ベクトル

$$= \begin{bmatrix} \frac{\partial o}{\partial \theta_1} \\ \frac{\partial o}{\partial \theta_2} \\ \frac{\partial o}{\partial \theta_3} \end{bmatrix}$$

# backward

本当に計算したいのは勾配を計算する変数に関する偏微分



左図を使って簡単に計算できる！

`o.backward()`

`theta1.grad, theta2.grad, theta3.grad`

`(tensor([29.4901]), tensor([-1.0025]), tensor([1.7437]))`

$$\frac{\partial o}{\partial \theta_1} = \frac{\partial o}{\partial z_5} \times \frac{\partial z_5}{\partial z_4} \times \frac{\partial z_4}{\partial \theta_1} = 29.5$$

**5.9      1      5**

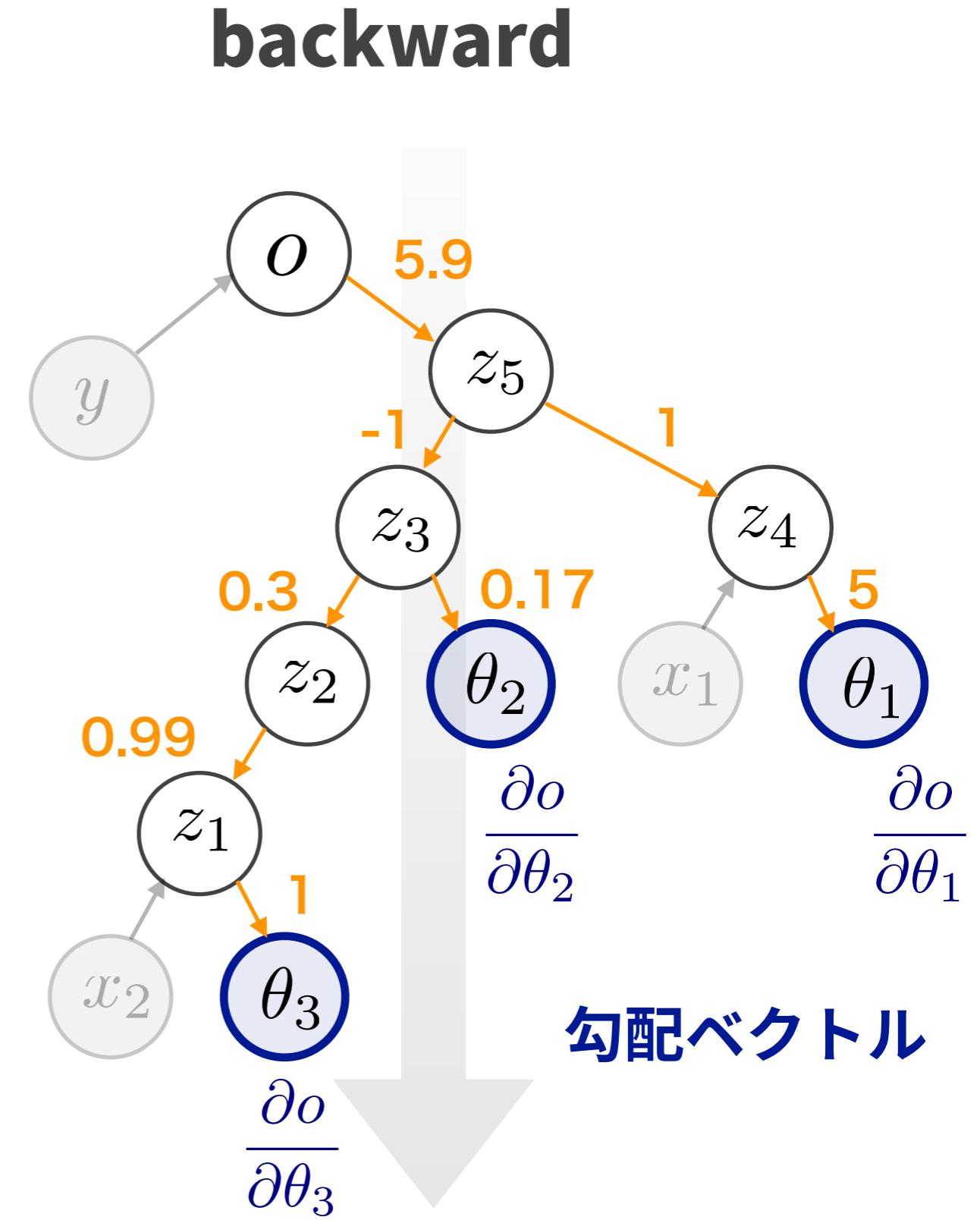
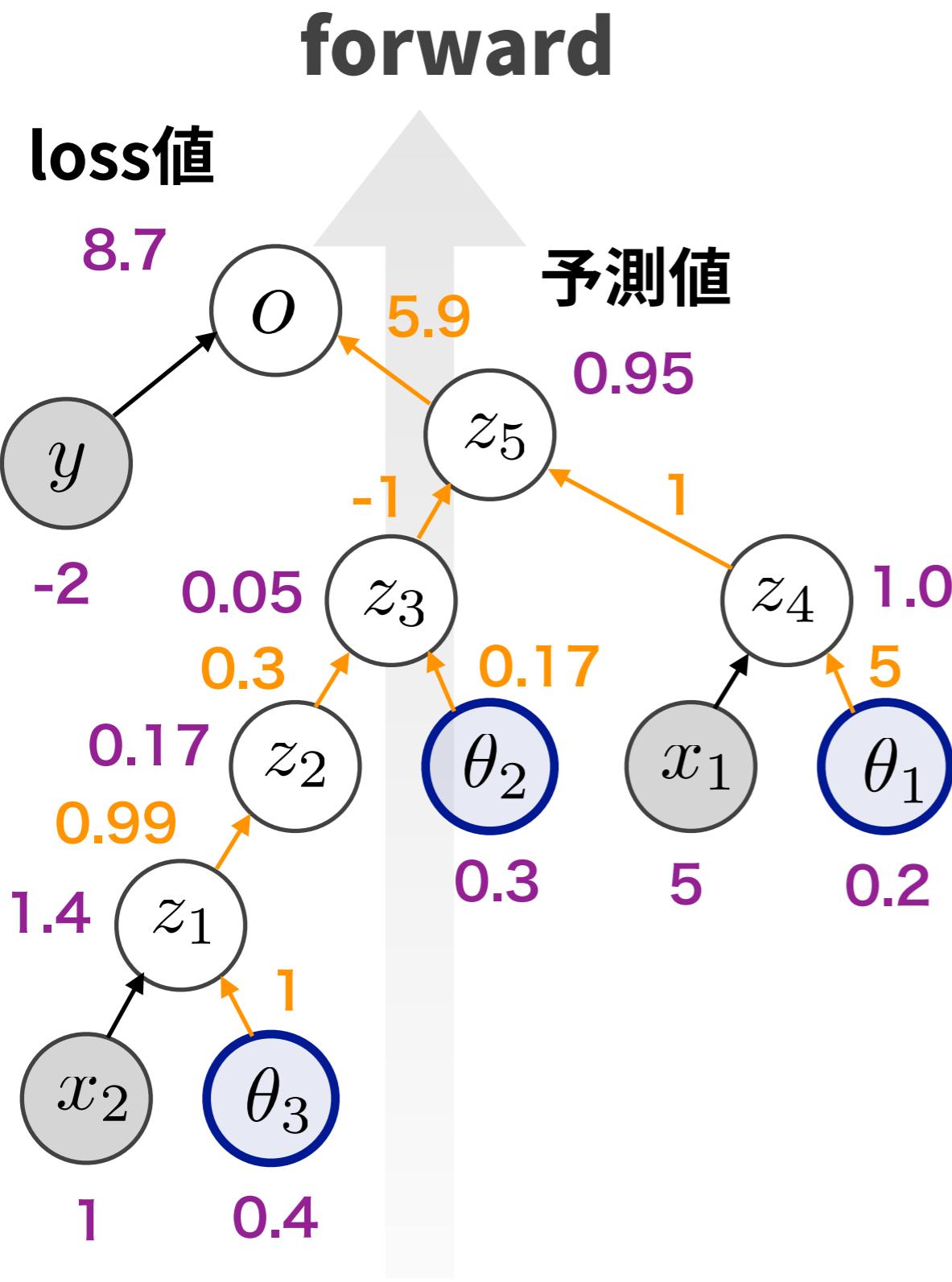
$$\frac{\partial o}{\partial \theta_2} = \frac{\partial o}{\partial z_5} \times \frac{\partial z_5}{\partial z_3} \times \frac{\partial z_3}{\partial \theta_2} = -1.00$$

**5.9      -1      0.17**

$$\frac{\partial o}{\partial \theta_3} = \frac{\partial o}{\partial z_5} \times \frac{\partial z_5}{\partial z_3} \times \frac{\partial z_3}{\partial z_2} \times \frac{\partial z_2}{\partial z_1} \times \frac{\partial z_1}{\partial \theta_3} = 1.75$$

**5.9      -1      0.3      -0.99      1**

# 合成関数の自動微分 (forward & backward)

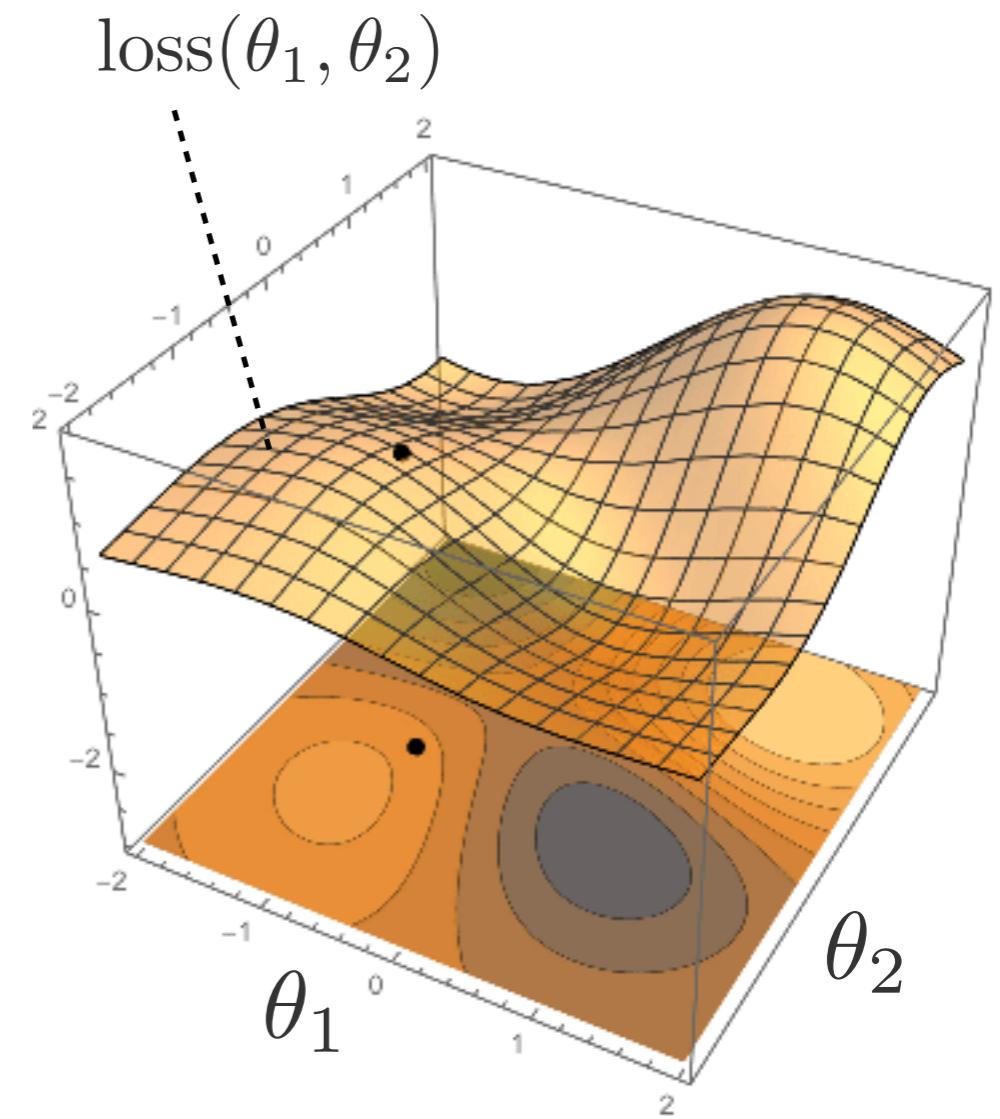


# 深層学習のココロ

機械学習モデルが合成関数(計算グラフ)になってさえいれば  
自動微分 + 勾配降下法でパラメタを最適にできる！

$$\begin{bmatrix} \theta_1 \\ \theta_2 \\ \vdots \\ \theta_p \end{bmatrix} \leftarrow \begin{bmatrix} \theta_1 \\ \theta_2 \\ \vdots \\ \theta_p \end{bmatrix} + \eta \times \begin{bmatrix} \partial \text{loss}(\theta) / \partial \theta_1 \\ \partial \text{loss}(\theta) / \partial \theta_2 \\ \vdots \\ \partial \text{loss}(\theta) / \partial \theta_p \end{bmatrix}$$

↓  
**学習率  
(step size)**      **勾配ベクトル**  
↓  
**自動微分で計算**

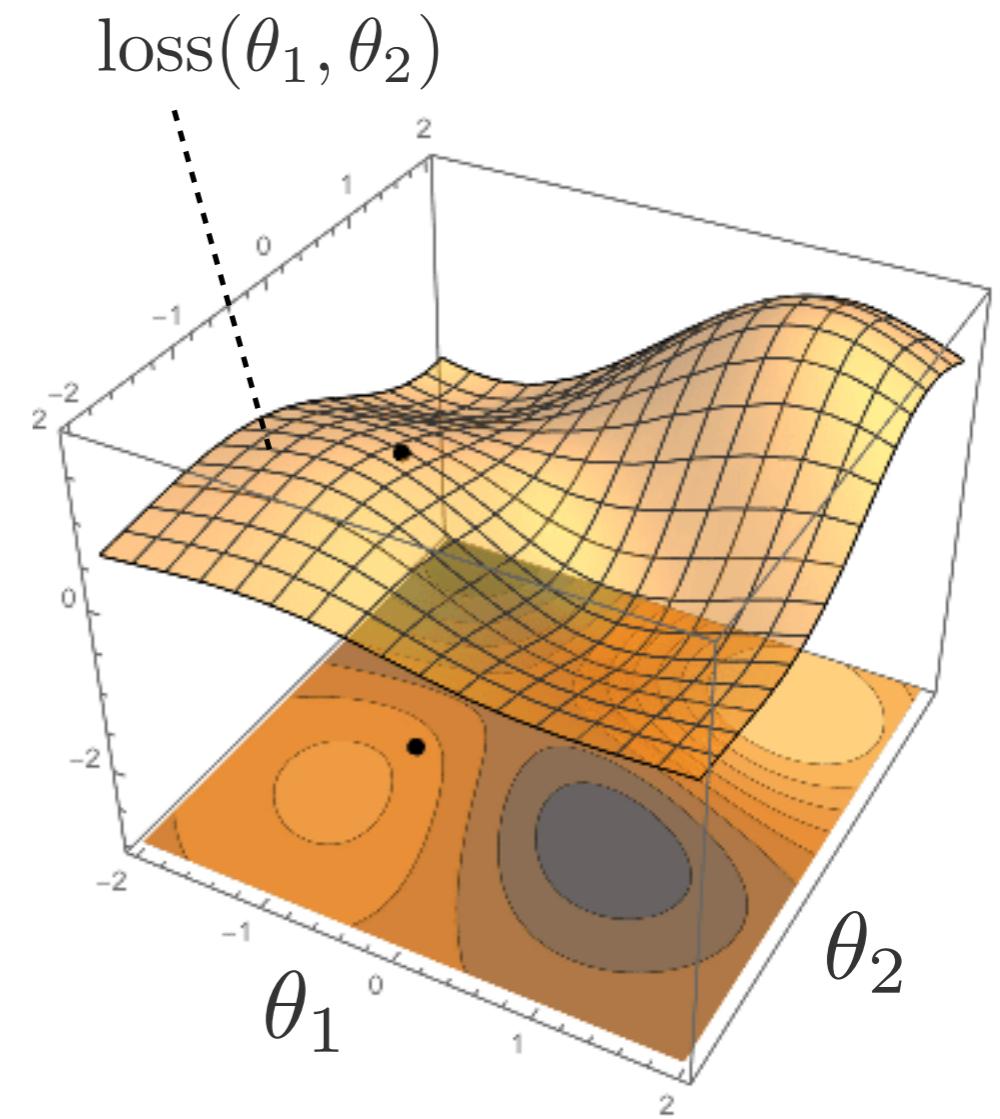


# 深層学習のココロ

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$$\begin{bmatrix} \theta_1 \\ \theta_2 \\ \vdots \\ \theta_p \end{bmatrix} \leftarrow \begin{bmatrix} \theta_1 \\ \theta_2 \\ \vdots \\ \theta_p \end{bmatrix} + \eta \times \begin{bmatrix} \partial \text{loss}(\theta) / \partial \theta_1 \\ \partial \text{loss}(\theta) / \partial \theta_2 \\ \vdots \\ \partial \text{loss}(\theta) / \partial \theta_p \end{bmatrix}$$

↓  
**学習率  
(step size)**      **勾配ベクトル**  
↓  
**自動微分で計算**



# 本日の内容

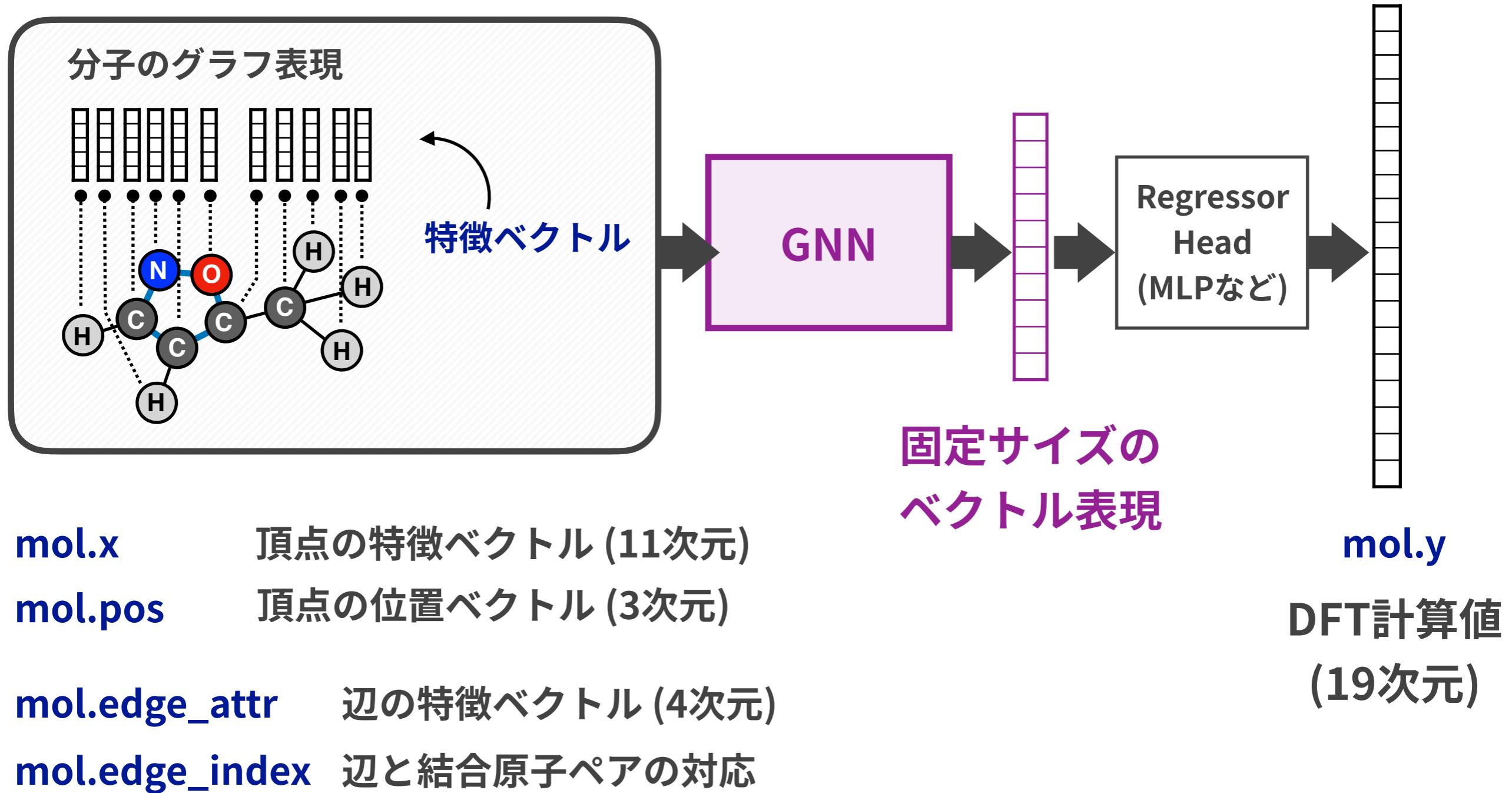
---

GNN(Graph Neural Networks)でグラフ表現された分子を  
入力にして機械学習するやり方をのぞいてみませんか？

- 機械学習とは？
- 分子のグラフ表現
- 準備：深層学習のココロ (forwardとbackward)
- Graph Neural Networksとは？
- 自分でやってみるための情報
- おまけ：  
最近の話 (計算限界、分子生成、事前学習、...)

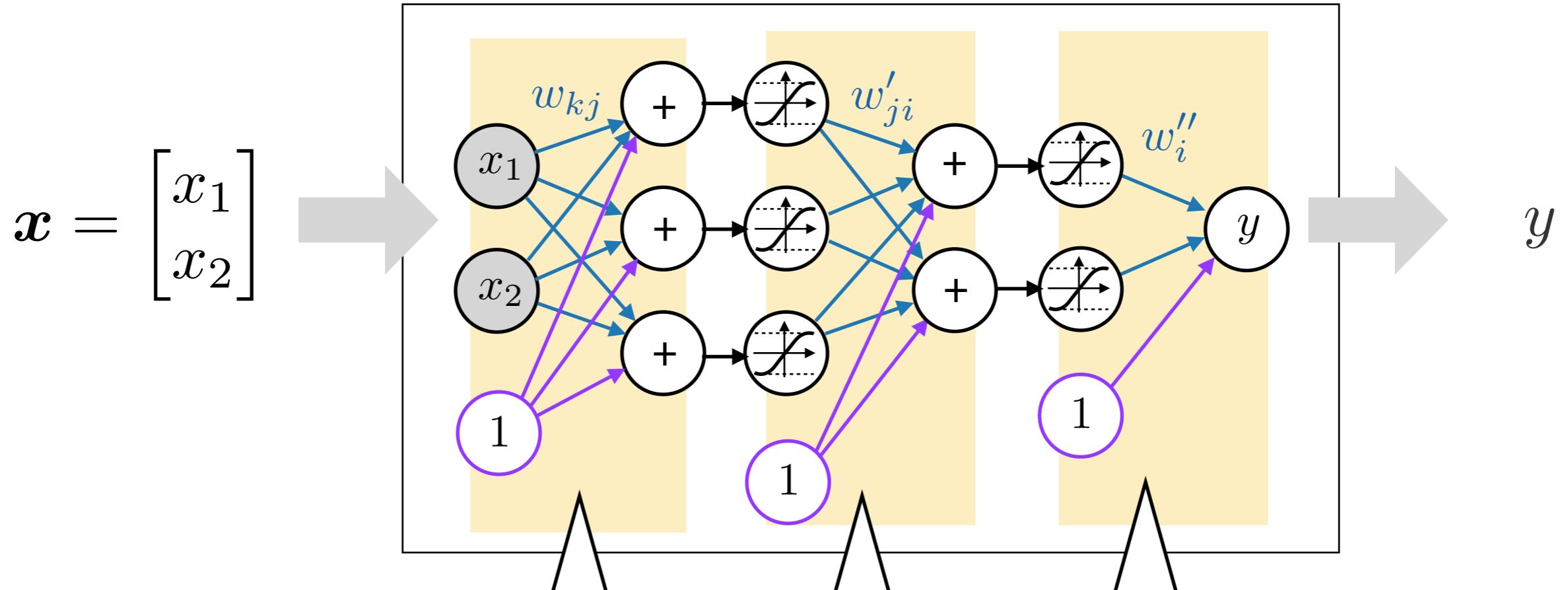
# GNN = 下記の変換を何らかの合成関数でデザインしたもの

可変サイズの分子グラフから「固定サイズのベクトル表現」への変換を学習



# 基本道具：MLP (多層パーセプトロン)

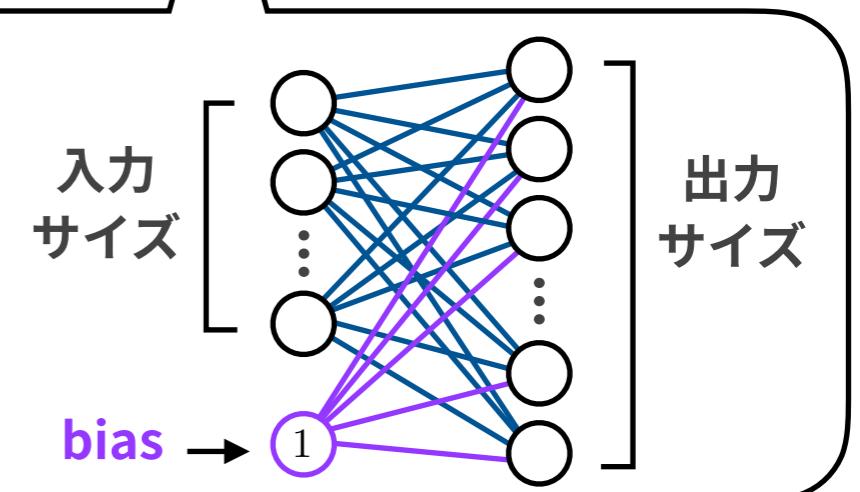
```
import torch.nn as nn  
nn.Sequential(nn.Linear(2, 3), nn.ReLU(), nn.Linear(3, 2), nn.ReLU(), nn.Linear(2, 1))
```



## torch.nn.Linear

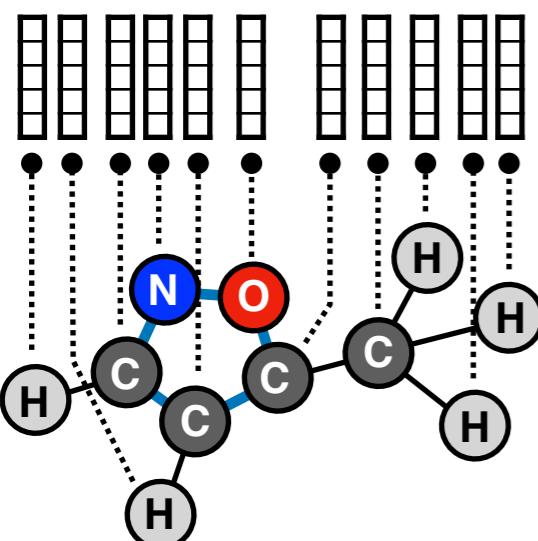
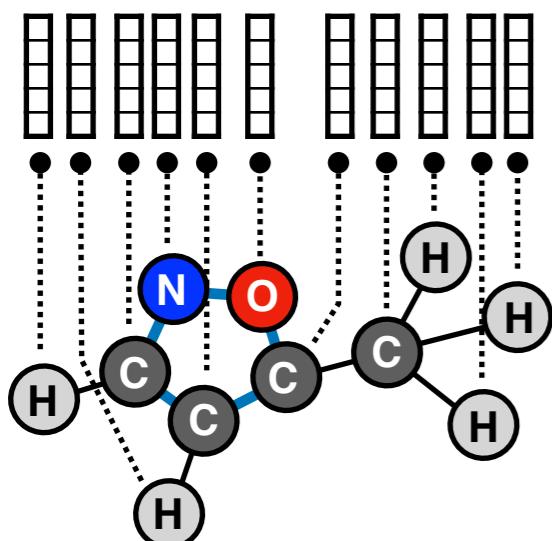
- **in\_features**
- **out\_features**
- **bias (True/False)**

入力サイズ  
出力サイズ  
**bias** の有無

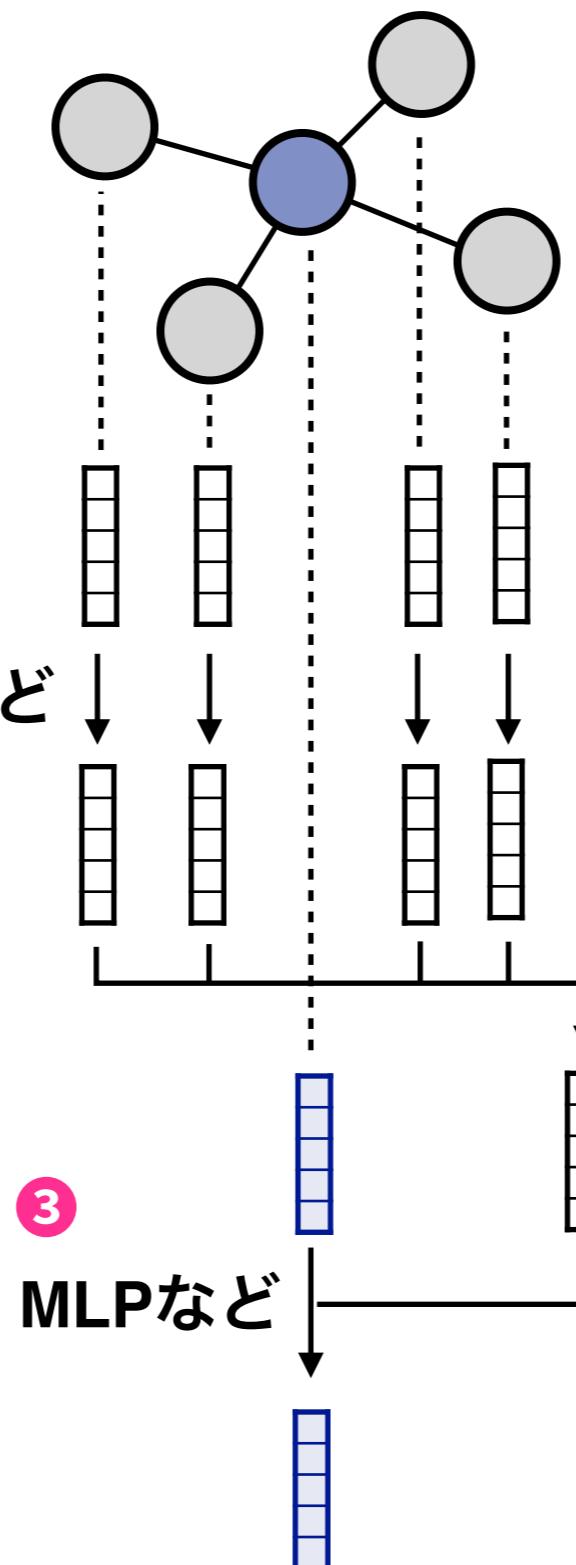


# Message Passing (or Neighborhood Aggregation)

各特徴ベクトルの更新



①  
MLPなど



torch\_geometric.nn.  
MessagePassing

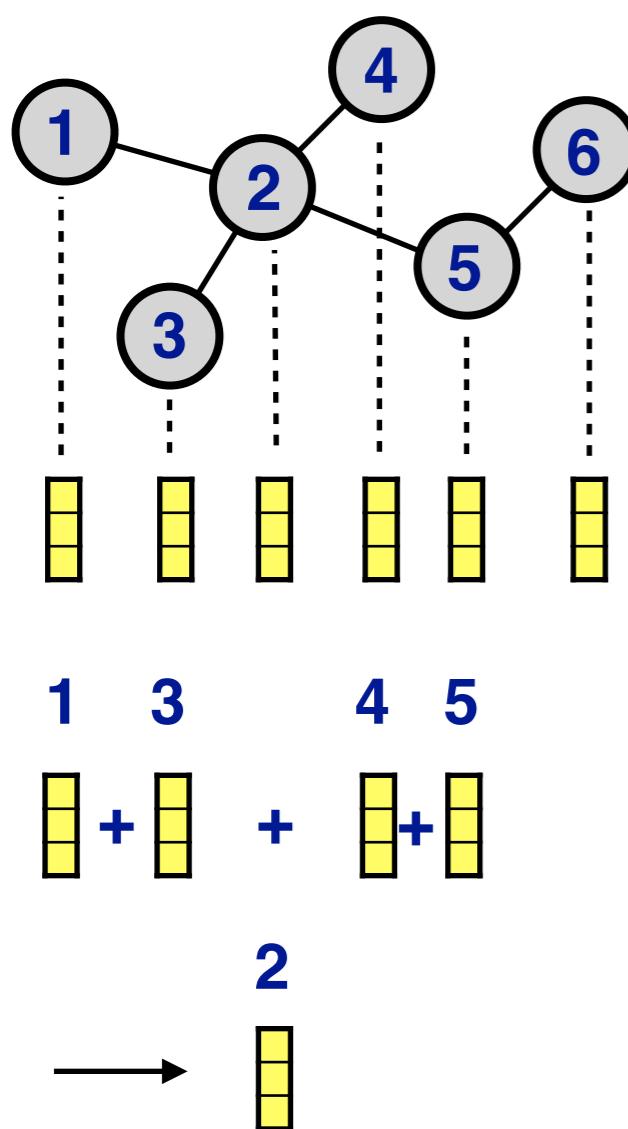
$$\mathbf{x}'_i = \gamma_{\Theta} (\mathbf{x}_i, \square_{j \in \mathcal{N}(i)} \phi_{\Theta} (\mathbf{x}_i, \mathbf{x}_j, \mathbf{e}_{j,i}))$$

③ ② ①

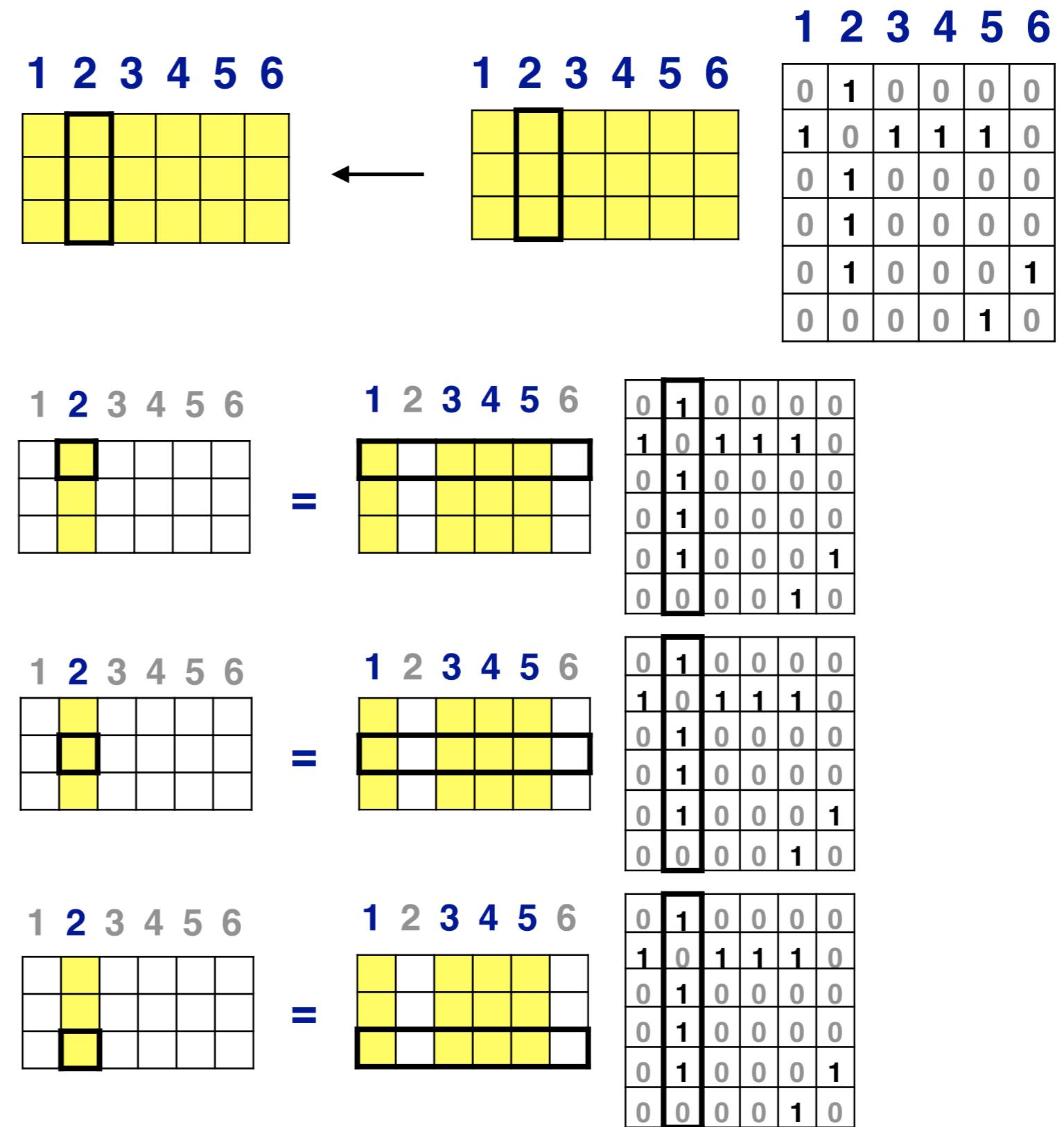
②  
順番に依存しない集約操作  
(sum, mean or max)

③  
MLPなど

# Message Passing (or Neighborhood Aggregation)



隣接行列などを使っても  
集約する操作は書ける



# Message Passing (or Neighborhood Aggregation)

---

- `torch_geometric.nn.GCNConv` (Kipf and Welling, ICML2017)

$$\mathbf{X}' = \hat{\mathbf{D}}^{-1/2} \hat{\mathbf{A}} \hat{\mathbf{D}}^{-1/2} \mathbf{X} \Theta$$

- `torch_geometric.nn.SAGEConv` (Hamilton et al, NIPS2017)

$$\mathbf{x}'_i = \mathbf{W}_1 \mathbf{x}_i + \mathbf{W}_2 \cdot \text{mean}_{j \in \mathcal{N}(i)} \mathbf{x}_j$$

- `torch_geometric.nn.GraphConv` (Morris et al, AAAI2019)

$$\mathbf{x}'_i = \Theta_1 \mathbf{x}_i + \sum_{j \in \mathcal{N}(i)} \Theta_2 \mathbf{x}_j$$

- `torch_geometric.nn.GINConv` (Xu et al, ICLR2019)

$$\mathbf{x}'_i = h_\Theta \left( (1 + \epsilon) \cdot \mathbf{x}_i + \sum_{j \in \mathcal{N}(i)} \mathbf{x}_j \right) \quad \text{or} \quad \mathbf{X}' = h_\Theta ((\mathbf{A} + (1 + \epsilon) \cdot \mathbf{I}) \cdot \mathbf{X})$$

# Message Passing (or Neighborhood Aggregation)

- `torch_geometric.nn.SchNet` (Schütt et al, NIPS2017)

$$\mathbf{x}'_i = \sum_{j \in \mathcal{N}(i)} \mathbf{x}_j \odot h_{\Theta}(\exp(-\gamma(\mathbf{e}_{j,i} - \mu)))$$

○ 要素積

→ xyzでの距離を辺重みにして集約時に活用する

- `torch_geometric.nn.GATConv` (Veličković et al., ICLR2018)

$$\mathbf{x}'_i = \alpha_{i,i} \Theta \mathbf{x}_i + \sum_{j \in \mathcal{N}(i)} \alpha_{i,j} \Theta \mathbf{x}_j$$

$$\alpha_{i,j} = \frac{\exp(\text{LeakyReLU}(\mathbf{a}^\top [\Theta \mathbf{x}_i \parallel \Theta \mathbf{x}_j]))}{\sum_{k \in \mathcal{N}(i) \cup \{i\}} \exp(\text{LeakyReLU}(\mathbf{a}^\top [\Theta \mathbf{x}_i \parallel \Theta \mathbf{x}_k]))}$$

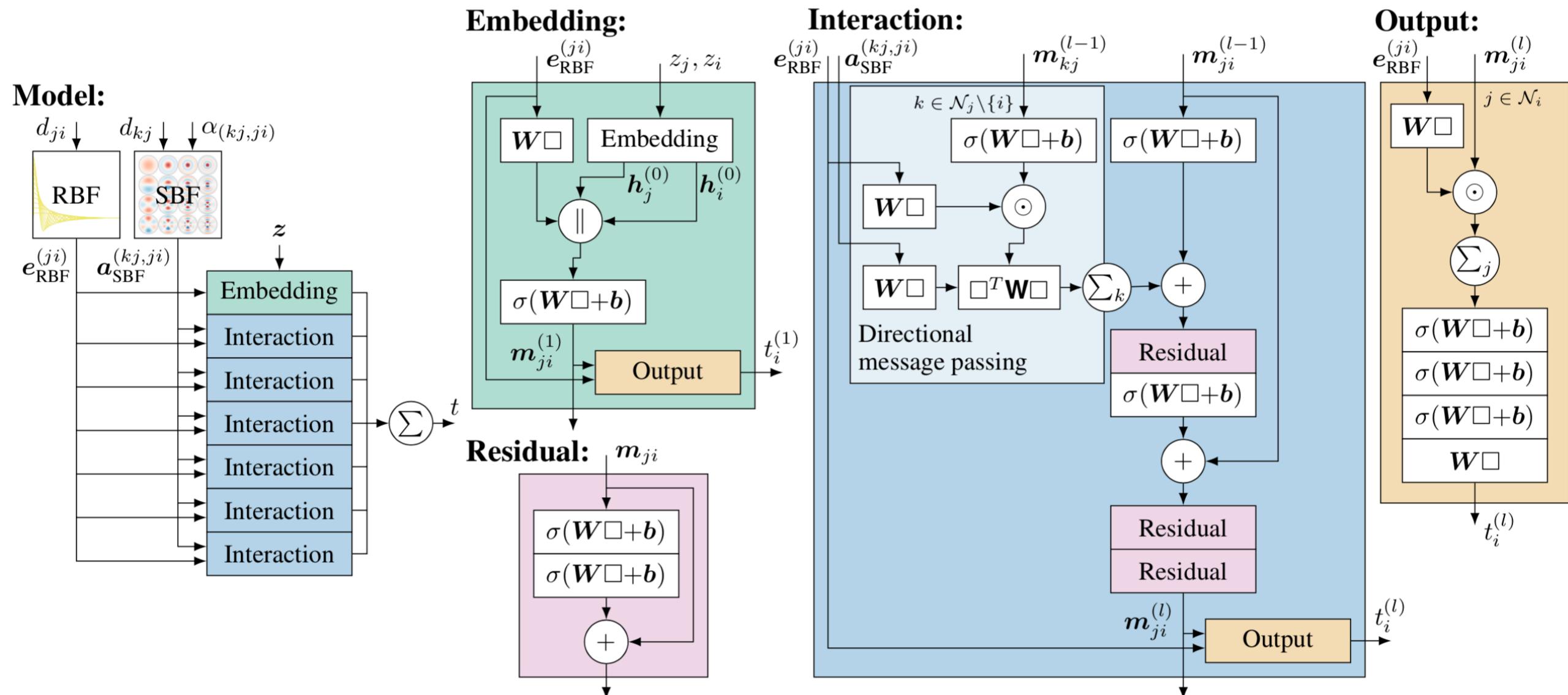
|| concat

→ 集約操作はシンプルだがアテンション機構で重みを適応的に

# Message Passing (or Neighborhood Aggregation)

- `torch_geometric.nn.DimeNet` (Klicpera et al, ICLR2020)

xyzに対して化学的なドメイン知識を活用して操作を作り込みまくった例



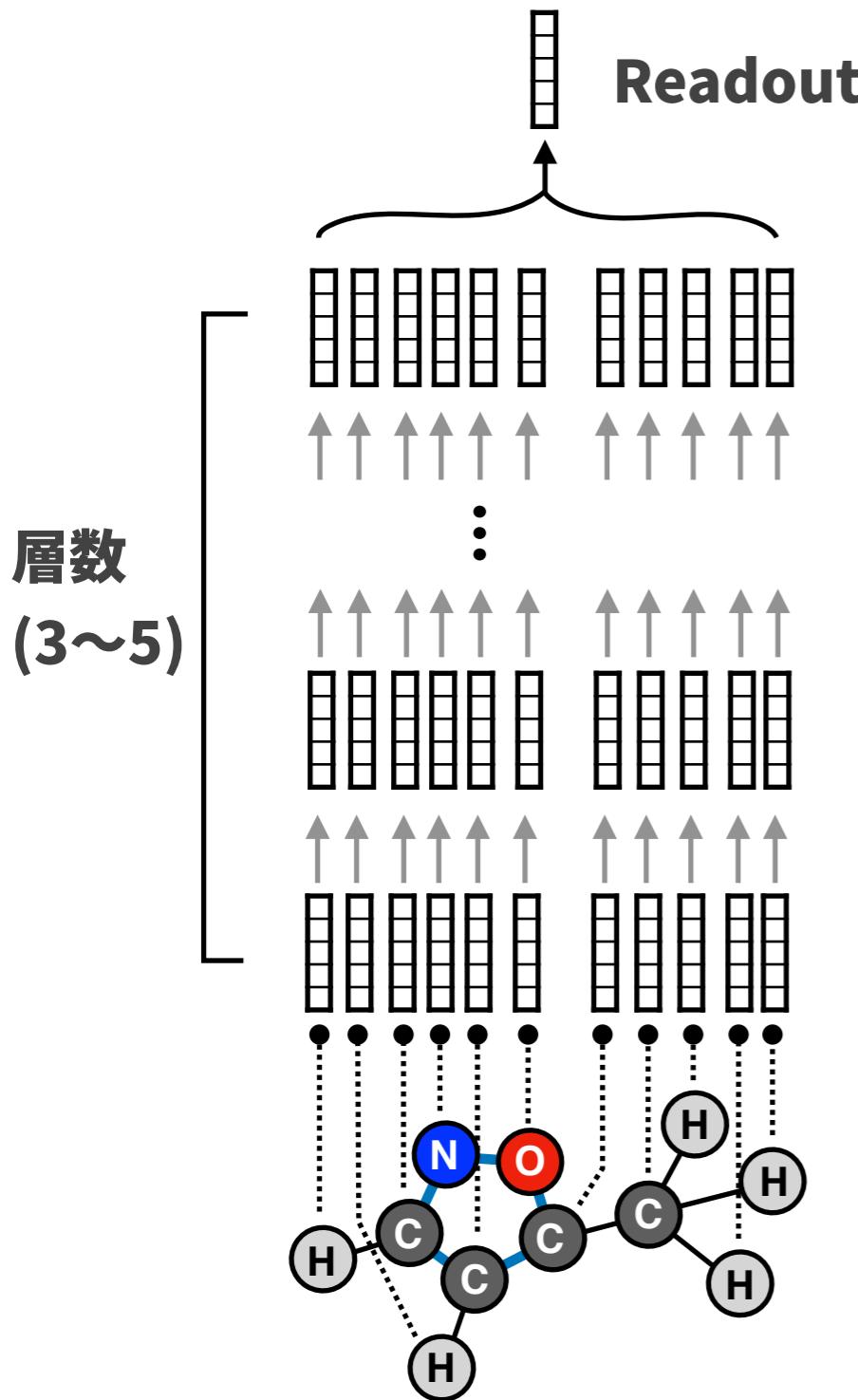
# Message Passing (or Neighborhood Aggregation)

最初に例に出したQM9データでは従来手法を優越する予測精度

Table 1: MAE on QM9. DimeNet sets the state of the art on 11 targets, outperforming the second-best model on average by 31 % (mean std. MAE).

| Target                   | Unit                              | PPGN  | SchNet       | PhysNet | MEGNet-s | Cormorant | DimeNet       |
|--------------------------|-----------------------------------|-------|--------------|---------|----------|-----------|---------------|
| $\mu$                    | D                                 | 0.047 | 0.033        | 0.0529  | 0.05     | 0.13      | <b>0.0286</b> |
| $\alpha$                 | $a_0^3$                           | 0.131 | 0.235        | 0.0615  | 0.081    | 0.092     | <b>0.0469</b> |
| $\epsilon_{\text{HOMO}}$ | meV                               | 40.3  | 41           | 32.9    | 43       | 36        | <b>27.8</b>   |
| $\epsilon_{\text{LUMO}}$ | meV                               | 32.7  | 34           | 24.7    | 44       | 36        | <b>19.7</b>   |
| $\Delta\epsilon$         | meV                               | 60.0  | 63           | 42.5    | 66       | 60        | <b>34.8</b>   |
| $\langle R^2 \rangle$    | $a_0^2$                           | 0.592 | <b>0.073</b> | 0.765   | 0.302    | 0.673     | 0.331         |
| ZPVE                     | meV                               | 3.12  | 1.7          | 1.39    | 1.43     | 1.98      | <b>1.29</b>   |
| $U_0$                    | meV                               | 36.8  | 14           | 8.15    | 12       | 28        | <b>8.02</b>   |
| $U$                      | meV                               | 36.8  | 19           | 8.34    | 13       | -         | <b>7.89</b>   |
| $H$                      | meV                               | 36.3  | 14           | 8.42    | 12       | -         | <b>8.11</b>   |
| $G$                      | meV                               | 36.4  | 14           | 9.40    | 12       | -         | <b>8.98</b>   |
| $c_v$                    | $\frac{\text{cal}}{\text{mol K}}$ | 0.055 | 0.033        | 0.0280  | 0.029    | 0.031     | <b>0.0249</b> |
| std. MAE                 | %                                 | 1.84  | 1.76         | 1.37    | 1.80     | 2.14      | <b>1.05</b>   |
| logMAE                   | -                                 | -4.64 | -5.17        | -5.35   | -5.17    | -4.75     | <b>-5.57</b>  |

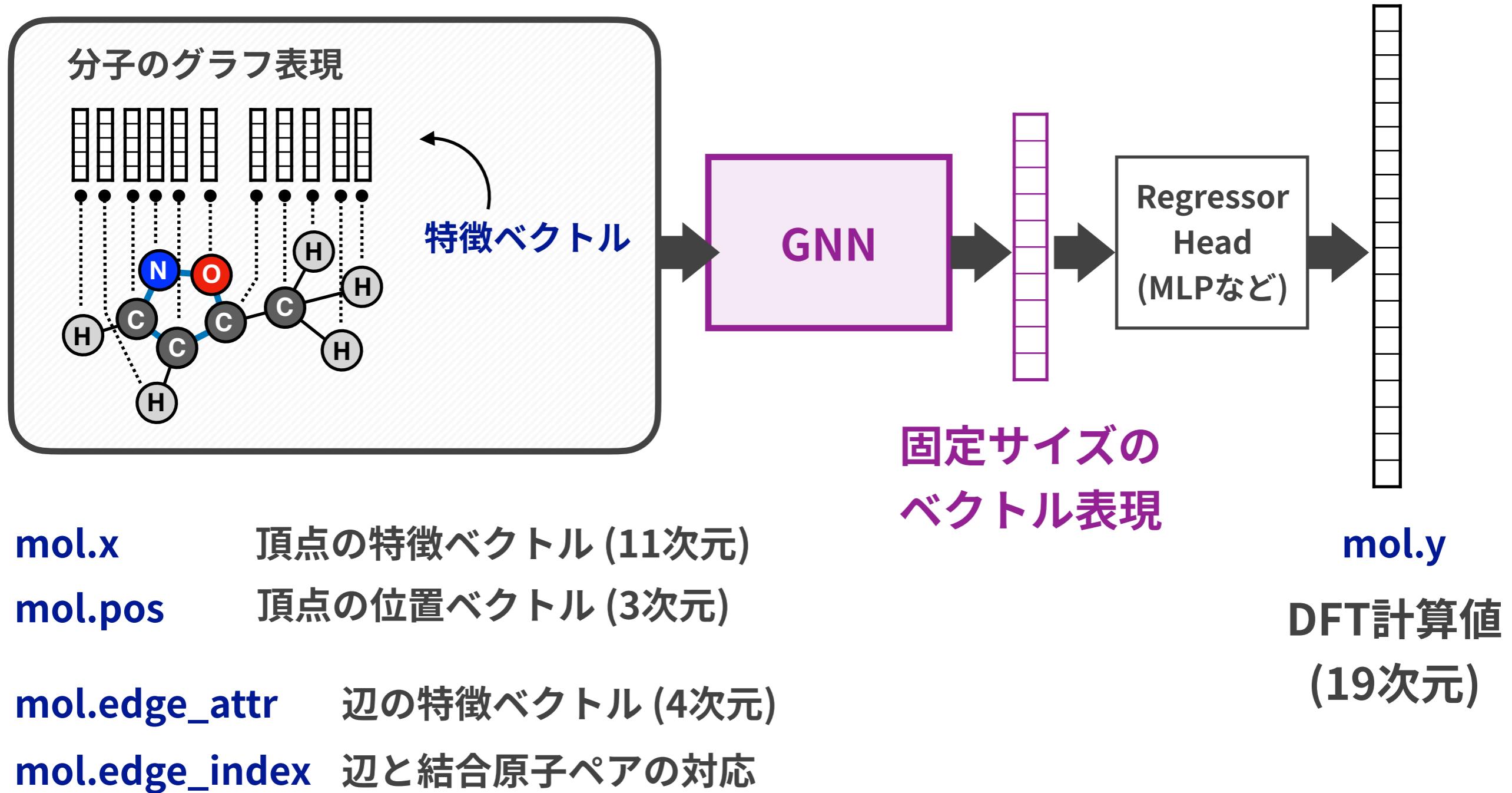
# Readout: グラフに対する固定サイズ表現を得る



- `torch_geometric.nn.global_add_pool`  
`torch_geometric.nn.global_max_pool`  
`torch_geometric.nn.global_mean_pool`  
順番に依存しない集約操作 (sum, mean or max)
- `torch_geometric.nn.global_sort_pool`  
最後の要素でsortしてトップkをconcat
- `torch_geometric.nn.GlobalAttention`
$$\mathbf{r}_i = \sum_{n=1}^{N_i} \text{softmax}\left(h_{\text{gate}}(\mathbf{x}_n)\right) \odot h_{\Theta}(\mathbf{x}_n),$$
- `torch_geometric.nn.Set2Set`
$$\mathbf{q}_t = \text{LSTM}(\mathbf{q}_{t-1}^*)$$
$$\alpha_{i,t} = \text{softmax}(\mathbf{x}_i \cdot \mathbf{q}_t)$$
$$\mathbf{r}_t = \sum_{i=1}^N \alpha_{i,t} \mathbf{x}_i$$
$$\mathbf{q}_t^* = \mathbf{q}_t \parallel \mathbf{r}_t,$$

# GNN = 下記の変換を何らかの合成関数でデザインしたもの

可変サイズの分子グラフから「固定サイズのベクトル表現」への変換を学習



# PyTorch Geometricの例 (Google Colab)

```
!pip install torch-scatter==latest+cu101 torch-sparse==latest+cu101 \
    torch-cluster==latest+cu101 -f https://pytorch-geometric.com/whl/torch-1.6.0.html
!pip install torch-geometric
```

```
import torch
import torch.nn as nn
import torch.nn.functional as F
import torch_geometric as pyg

from tqdm import tqdm

dataset = pyg.datasets.QM9(root='/tmp/QM9')
data_size = len(dataset)
loader = pyg.data.DataLoader(dataset[:int(data_size * 0.8)], batch_size=64, shuffle=True)
test_loader = pyg.data.DataLoader(dataset[int(data_size * 0.8):], batch_size=64, shuffle=True)
```

```
def mlp(input_dim, hidden_dim):
    return nn.Sequential(
        nn.Linear(input_dim, hidden_dim),
        nn.ReLU(),
        nn.Linear(hidden_dim, hidden_dim))
```

# モデルとforward定義

```
class MyGNN(nn.Module):
    def __init__(self, input_dim, hidden_dim, output_dim):
        super(MyGNN, self).__init__()
        self.convs = nn.ModuleList()
        self.convs.append(pyg.nn.GINConv(mlp(input_dim, hidden_dim)))
        for l in range(2):
            self.convs.append(pyg.nn.GINConv(mlp(hidden_dim, hidden_dim)))
        self.head = nn.Sequential(
            nn.Linear(hidden_dim, hidden_dim), nn.Dropout(0.25),
            nn.Linear(hidden_dim, output_dim))
```

Regresso  
Head (MLP)

```
def forward(self, data): ←———— 出力を計算するforward
    x, edge_index, batch = data.x, data.edge_index, data.batch
    for conv in self.convs:
        x = conv(x, edge_index)
        x = F.relu(x)
        x = F.dropout(x, p=0.25, training=self.training)
    x = pyg.nn.global_mean_pool(x, batch) ←———— Readout
    x = self.head(x)
    return x
```

Message  
Passing (x 3層)

# 学習：モデルのパラメタを最適にする

```
model = MyGNN(dataset.num_node_features, 32, dataset.num_classes)
```

```
opt = torch.optim.Adam(model.parameters(), lr=0.01)
error = torch.nn.MSELoss(reduction='sum')
```

```
for epoch in range(10):           ← とりあえず10 epoch (数百必要)
    total_loss = 0
    model.train()
    for batch in tqdm(loader):
        opt.zero_grad()
        pred = model(batch)
        loss = error(pred, batch.y)   ← モデルに入れて予測を得る
        loss.backward()              ← lossを計算しbackward
        opt.step()                  ← 勾配降下(パラメタ更新)
        total_loss += loss.item() * batch.num_graphs
    total_loss /= len(loader.dataset)
    print("loss", total_loss, epoch)
```

## 注意

---

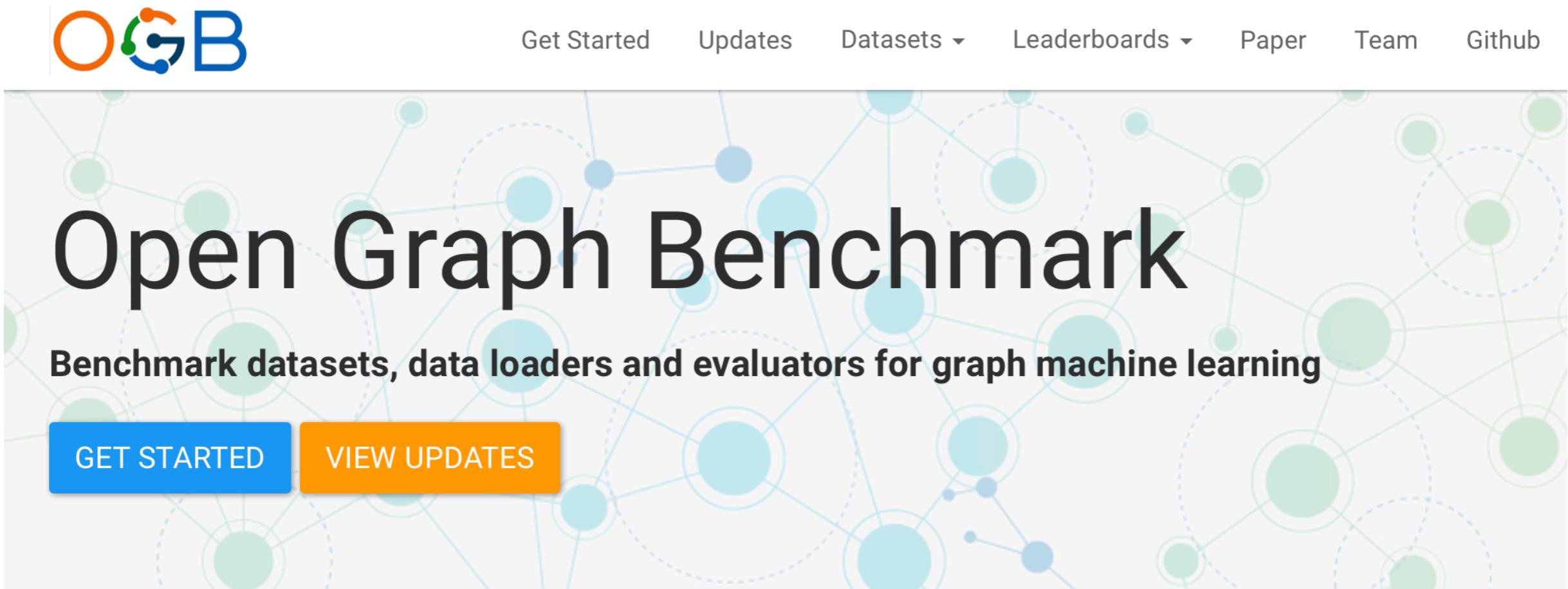
- QM9のタスクの場合はほぼxyz(x.pos)の情報が必要だが、単純なGNNはx.edge\_attrも使わないので適宜改変が必要
- 例えばx.edge\_attrに原子間距離を加えてConvで活用？

```
QM9_dist = []
for g in dataset:
    edge_attr = torch.empty(g.num_edges, g.num_edge_features + 1)
    for id, (s, t) in enumerate(zip(*g.edge_index)):
        d = torch.norm(g.pos[s]-g.pos[t])
        edge_attr[id] = torch.cat([g.edge_attr[id], d.reshape(1)])
    data = pyg.data.Data(x=g.x, z=g.z, pos=g.pos, edge_index=g.edge_index,
                          edge_attr=edge_attr, y=g.y, name=g.name, idx=id)
    QM9_dist.append(data)
```

- そのまま使う場合はSchNetやDimeNetが向いている
- 公式コードサンプルもチェック  
[https://github.com/rusty1s/pytorch\\_geometric/tree/master/examples](https://github.com/rusty1s/pytorch_geometric/tree/master/examples)

# Open Graph Benchmark <https://ogb.stanford.edu>

---



The Open Graph Benchmark (OGB) is a collection of realistic, large-scale, and diverse benchmark datasets for machine learning on graphs. OGB datasets are automatically downloaded, processed, and split using the [OGB Data Loader](#). The model performance can be evaluated using the [OGB Evaluator](#) in a unified manner.



# 本日の内容

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- 分子のグラフ表現
- 準備：深層学習のココロ (forwardとbackward)
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- 自分でやってみるための情報
- おまけ：  
最近の話 (計算限界、分子生成、事前学習、...)

# Graph Neural Networksを知るための3つのソース

---

- CS224W: Machine Learning with Graphs (Stanford)

<http://web.stanford.edu/class/cs224w/>



 YouTube <https://youtu.be/-UjytpbqX4A>

- KDD2020 Tutorial  
Deep Graph Learning: Foundations, Advances and Applications

<https://ai.tencent.com/ailab/ml/KDD-Deep-Graph-Learning.html>

- Book "Deep Learning on Graphs"

[http://cse.msu.edu/~mayao4/dlg\\_book/index.html](http://cse.msu.edu/~mayao4/dlg_book/index.html)

# Pytorch Geometricを使ったハンズオン (CS224W)

<https://colab.research.google.com/drive/1DIQm9rOx2mT1bZETEeVUThxcrP1RKqAn>

The screenshot shows a Google Colab notebook interface. The title bar says 'Graph Neural Networks'. The menu bar includes 'ファイル' (File), '編集' (Edit), '表示' (View), '挿入' (Insert), 'ランタイム' (Runtime), 'ツール' (Tools), 'ヘルプ' (Help), and '変更は保存されません' (Changes not saved). The toolbar has buttons for '+ コード' (Code), '+ テキスト' (Text), and 'ドライブにコピー' (Copy to Drive). The right sidebar has buttons for '共有' (Share), '接続' (Connect), '編集' (Edit), and a refresh icon. The main content area has a title 'Graph Neural Networks' and a text block: 'In this tutorial, we will explore the implementation of graph neural networks and investigate what representations these networks learn. Along the way, we'll see how PyTorch Geometric and TensorBoardX can help us with constructing and training graph models.' Below this, a section titled '▼ Preliminaries: PyTorch' is expanded, containing text about PyTorch and code imports.

In this tutorial, we will explore the implementation of graph neural networks and investigate what representations these networks learn. Along the way, we'll see how PyTorch Geometric and TensorBoardX can help us with constructing and training graph models.

▼ Preliminaries: PyTorch

We'll first demonstrate some essential features of PyTorch which we'll use throughout. PyTorch is a general machine learning library that allows us to dynamically define computation graphs which we'll use to describe our models and their training processes.

We'll start by importing everything we need:

```
[ ] Import torch
import torch.nn as nn
import torch.nn.functional as F
import torchvision
import torchvision.transforms as transforms
import sklearn.metrics as metrics
```

# Kaggle CHAMPS (xyzが要るタスク)

<https://www.kaggle.com/c/champs-scalar-coupling/discussion/93972>

Featured Prediction Competition

## Predicting Molecular Properties

Can you measure the magnetic interactions between a pair of atoms?

 CHAMPS (CHeMistry And Mathematics in Phase Space) · 2,749 teams · a year ago

\$30,000 Prize Money

Overview Data Notebooks Discussion Leaderboard Rules New Topic

255th place

 Which graph CNN is the best (with starter kit at LB -1.469)?  219

Posted in [champs-scalar-coupling](#) a year ago

This post is for information and results using graph CNN. For a start:

useful Graph CNN lib:

- [https://github.com/rusty1s/pytorch\\_geometric](https://github.com/rusty1s/pytorch_geometric)
- <https://github.com/pfnet-research/chainer-chemistry>
- <https://github.com/jparkhill/TensorMol>

# ICLR2020: A Fair Comparisons of GNNs

---

<https://github.com/diningphil/gnn-comparison>

## A FAIR COMPARISON OF GRAPH NEURAL NETWORKS FOR GRAPH CLASSIFICATION

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Table 3: Results on chemical datasets with mean accuracy and standard deviation are reported. Best performances are highlighted in bold.

|           | <b>D&amp;D</b>        | <b>NCI1</b>           | <b>PROTEINS</b>       | <b>ENZYMES</b>        |
|-----------|-----------------------|-----------------------|-----------------------|-----------------------|
| Baseline  | <b>78.4</b> $\pm$ 4.5 | 69.8 $\pm$ 2.2        | <b>75.8</b> $\pm$ 3.7 | <b>65.2</b> $\pm$ 6.4 |
| DGCNN     | 76.6 $\pm$ 4.3        | 76.4 $\pm$ 1.7        | 72.9 $\pm$ 3.5        | 38.9 $\pm$ 5.7        |
| DiffPool  | 75.0 $\pm$ 3.5        | 76.9 $\pm$ 1.9        | 73.7 $\pm$ 3.5        | 59.5 $\pm$ 5.6        |
| ECC       | 72.6 $\pm$ 4.1        | 76.2 $\pm$ 1.4        | 72.3 $\pm$ 3.4        | 29.5 $\pm$ 8.2        |
| GIN       | 75.3 $\pm$ 2.9        | <b>80.0</b> $\pm$ 1.4 | 73.3 $\pm$ 4.0        | 59.6 $\pm$ 4.5        |
| GraphSAGE | 72.9 $\pm$ 2.0        | 76.0 $\pm$ 1.8        | 73.0 $\pm$ 4.5        | 58.2 $\pm$ 6.0        |

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# GNNは発展途上の技術で現在進行形で研究されている

---

- 学習できる表現に限界がある？

**Generalization and Representational Limits of Graph Neural Networks**

Garg, Jegelka, Jaakkola (ICML2020)

- Deepにできない？

**DeepGCNs: Can GCNs Go as Deep as CNNs?**

Li, Müller, Thabet, Ghanem (ICCV2019)

**PairNorm: Tackling Oversmoothing in GNNs**

Zhao, Akoglu (ICLR2020)

**Towards Deeper Graph Neural Networks with Differentiable Group Normalization**

Zhou, Huang, Li, Zha, Chen, Hu (NeurIPS2020)

- 事前学習ができない？

**Strategies for Pre-training Graph Neural Networks**

Hu, Liu, Gomes, Zitnik, Liang, Pande, Leskovec (ICLR2020)

**GROVER: Self-Supervised Message Passing Transformer on Large-scale Molecular Graphs** Rong, Bian, Xu, Xie, Wei, Huang, Huang (NeurIPS2020)

# 今日の話の応用・発展

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## ● Graph Pooling

**Rethinking Pooling in Graph Neural Networks**

Mesquita, Souza, Kaski (NeurIPS2020)

**Path Integral Based Convolution and Pooling for Graph Neural Networks**

Ma, Xuan, Guang Wang, Li, Liò (NeurIPS2020)

## ● 分子の生成

**GraphAF: a Flow-based Autoregressive Model for Molecular Graph Generation**

Jin, Barzilay, Jaakkola (ICML2020)

**Generalization and Representational Limits of Graph Neural Networks**

Shi, Xu, Zhu, Zhang, Zhang, Tang (ICLR2020)

## ● 化学反応の予測・逆合成

**RetroXpert: Decompose Retrosynthesis Prediction like A Chemist**

Yan, Ding, Zhao, Zheng, Yang, Yu, Huang (NeurIPS2020)

**A Graph to Graphs Framework for Retrosynthesis Prediction**

Shi, Xu, Guo, Zhang, Tang (ICML2020)

# まとめ

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