

| $\mathcal{F}$   | $\mathcal{L}$   | $\mathcal{Z}$   |
|---|---|---|
| $F(\omega) = \int_{-\infty}^{\infty} f(t) \mathrm{e}^{-i\omega t} \mathrm{d}t$                    | $L(s) = \int_0^{\infty} f(t) \mathrm{e}^{-st} \mathrm{d}t$  | $X(z) = \sum_{n=0}^{\infty} x[n] z^{-n}$  |
| $f(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} F(\omega) \mathrm{e}^{i\omega t} \mathrm{d}\omega$ | $f(t) = \frac{1}{2\pi i} \int_{\mathrm{Br}} L(s) \mathrm{e}^{st} \mathrm{d}s$   | $x[n] = \frac{1}{2\pi i} \oint_C X(z) z^{n-1} \mathrm{d}z$  |
|   | $f(t) = 0 \ (t < 0)$  | $x[n] = 0 \ (n < 0)$  |
| $\mathcal{F} [f(t)] = F(\omega)$  | $\mathcal{L} [f(t)] = L(s)$   | $\mathcal{Z} [x[n]] = X(z)$   |
| $\mathcal{F} [af(t) + bg(t)] = aF(\omega) + bG(\omega)$   | $\mathcal{L} [af(t) + bg(t)] = aL(s) + bG(s)$   | $\mathcal{Z} [ax[n] + by[n]] = aX(z) + bY(z)$   |
| $\mathcal{F} [f(t - t_0)] = F(\omega) \mathrm{e}^{-i\omega t_0}$                                  | $\mathcal{L} [f(t - t_0)] = L(s) \mathrm{e}^{-t_0 s}$   | $\mathcal{Z} [x[n - n_0]] = X(z) z^{-n_0}$  |
| $\mathcal{F} [f(t) \mathrm{e}^{i\omega_0 t}] = F(\omega - \omega_0)$                              | $\mathcal{L} [f(t) \mathrm{e}^{s_0 t}] = L(s - s_0)$  | $\mathcal{Z} [x[n] z_0^n] = X(z/z_0)$   |
| $\mathcal{F} [f(at)] = \frac{1}{ a } F\left(\frac{\omega}{a}\right)$                              | $\mathcal{L} [f(at)] = \frac{1}{ a } L\left(\frac{s}{a}\right)$   |   |
| $\mathcal{F} [F(t)] = 2\pi f(-\omega)$  |   |   |
| $\mathcal{F} \left[ \frac{\mathrm{d}^n f(t)}{\mathrm{d}t^n} \right] = (i\omega)^n F(\omega)$      | $\mathcal{L} \left[ \frac{\mathrm{d}^n f(t)}{\mathrm{d}t^n} \right] = s^n L(s) - \sum_{k=0}^{n-1} s^{n-k-1} f^{(k)}(+0)$            | $\mathcal{Z} [x[n] - x[n-1]] = \frac{X(z)}{1 - z^{-1}}$   |
| $\mathcal{F} [t^n f(t)] = i^n \frac{\mathrm{d}^n F(\omega)}{\mathrm{d}\omega^n}$                  | $\mathcal{L} [t^n f(t)] = (-1)^n \frac{\mathrm{d}^n L(s)}{\mathrm{d}s^n}$   | $\mathcal{Z} [nx[n]] = -z \frac{\mathrm{d}X(z)}{\mathrm{d}z}$   |
| $\mathcal{F} [f(t) * g(t)] = F(\omega) G(\omega)$   | $\mathcal{L} [f(t) * g(t)] = L(s) G(s)$   | $\mathcal{Z} [x[n] * y[n]] = X(z) Y(z)$   |
| $\mathcal{F} [f(t)g(t)] = \frac{1}{2\pi} F(\omega) * G(\omega)$                                   | $\mathcal{L} [f(t)g(t)] = \frac{1}{2\pi i} \lim_{T \rightarrow \infty} \int_{c-iT}^{c+iT} L(\sigma) G(s - \sigma) \mathrm{d}\sigma$ | $\mathcal{Z} [x[n]y[n]] = \frac{1}{2\pi i} \oint_C X(\sigma) Y(z/\sigma) \sigma^{-1} \mathrm{d}\sigma$                                      |
| $f(t) * g(t) = \int_{-\infty}^{\infty} f(\tau) g(t - \tau) \mathrm{d}\tau$                        | $f(t) * g(t) = \int_0^t f(\tau) g(t - \tau) \mathrm{d}\tau$   | $x[n] * y[n] = \sum_{m=-\infty}^{\infty} x[m] y[n - m]$   |
| $\mathcal{F} [\delta(t)] = 1$   | $\mathcal{L} [\delta(t)] = 1$   | $\mathcal{Z} [\delta[n]] = 1$   |
| $\mathcal{F} [1] = 2\pi \delta(\omega)$   | $\mathcal{L} [1] = \frac{1}{s}$   | $\mathcal{Z} [1] = \frac{1}{1 - z^{-1}}$  |
| $\mathcal{F} [t] = -2\pi i \frac{\delta(\omega)}{\omega}$   | $\mathcal{L} [t] = \frac{1}{s^2}$   | $\mathcal{Z} [nT] = \frac{T z^{-1}}{(1 - z^{-1})^2}$  |
| $\mathcal{F} [t^k] = 2\pi i^k \delta^{(k)}(\omega)$   | $\mathcal{L} [t^k] = \frac{k!}{s^{k+1}}$  | $\mathcal{Z} \left[ (nT)^k \right] = \left[ \frac{\mathrm{d}^k}{\mathrm{d}s^k} \frac{1}{(1 - z^{-1} \mathrm{e}^{sT})} \right] \bigg _{s=0}$ |
| $\mathcal{F} [\mathrm{e}^{i\omega_0 t}] = 2\pi \delta(\omega - \omega_0)$                         | $\mathcal{L} [\mathrm{e}^{s_0 t}] = \frac{1}{s - s_0}$  | $\mathcal{Z} [\mathrm{e}^{\alpha n T}] = \frac{1}{1 - z^{-1} \mathrm{e}^{\alpha T}}$  |
| $\mathcal{F} [\sin \beta t] = -i\pi (\delta(\omega - \beta) - \delta(\omega + \beta))$            | $\mathcal{L} [\sin \beta t] = \frac{\beta}{s^2 + \beta^2}$  | $\mathcal{Z} [\sin \beta n T] = \frac{z^{-1} \sin \beta T}{1 - 2z^{-1} \cos \beta T + z^{-2}}$  |
| $\mathcal{F} [\cos \beta t] = \pi (\delta(\omega - \beta) + \delta(\omega + \beta))$              | $\mathcal{L} [\cos \beta t] = \frac{s}{s^2 + \beta^2}$  | $\mathcal{Z} [\cos \beta n T] = \frac{1 - z^{-1} \cos \beta T}{1 - 2z^{-1} \cos \beta T + z^{-2}}$  |
| $\mathcal{F} [\Pi(t/T)] = T \sin \frac{\omega T}{2} \bigg/ \frac{\omega T}{2}$                    | $\mathcal{L} [\Pi_{T_1}^{T_2}(t)] = \frac{1}{s} (\mathrm{e}^{-sT_1} - \mathrm{e}^{-sT_2})$  |   |