| ${\mathcal F}$ | ${\cal L}$ | ${\cal Z}$ |
|--|--|--|
| $F(\omega) = \int_{-\infty}^{\infty} f(t) e^{-i\omega t} dt$ | $F(s) = \int_0^\infty f(t) e^{-st} dt$ | $X(z) = \sum_{n=0}^{\infty} x[n]z^{-n}$ |
| $f(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} F(\omega) e^{i\omega t} d\omega$ | $f(t) = \frac{1}{2\pi i} \int_{Br} F(s) e^{st} ds$ | $x[n] = \frac{1}{2\pi i} \oint_C X(z) z^{n-1} dz$ |
| | $f(t) = 0 \ (t < 0)$ | $x[n] = 0 \ (n < 0)$ |
| $\mathcal{F}\left[f(t)\right] = F(\omega)$ | $\mathcal{L}\left[f(t) ight]=F(s)$ | $\mathcal{Z}\left[x[n]\right] = X(z)$ |
| $\mathcal{F}\left[af(t) + bg(t)\right] = aF(\omega) + bG(\omega)$ | $\mathcal{L}\left[af(t) + bg(t)\right] = aF(s) + bG(s)$ | $\mathcal{Z}\left[ax[n]+by[n]\right]=aX(z)+bY(z)$ |
| $\mathcal{F}\left[f(t-t_0)\right] = F(\omega)e^{-i\omega t_0}$ | $\mathcal{L}\left[f(t-t_0)\right] = F(s)e^{-t_0s}$ | $\mathcal{Z}\left[x[n-n_0]\right] = X(z)z^{-n_0}$ |
| $\mathcal{F}\left[f(t)e^{i\omega_0t}\right] = F\left(\omega - \omega_0\right)$ | $\mathcal{L}\left[f(t)e^{s_0t}\right] = F\left(s - s_0\right)$ | $\mathcal{Z}\left[x[n]z_0{}^n\right] = X\left(z/z_0\right)$ |
| $\mathcal{F}\left[f(at)\right] = \frac{1}{ a } F\left(\frac{\omega}{a}\right)$ | $\mathcal{L}\left[f(at)\right] = \frac{1}{ a } F\left(\frac{s}{a}\right)$ | |
| $\mathcal{F}\left[F(t)\right] = 2\pi f(-\omega)$ | | |
| $\mathcal{F}\left[\frac{\mathrm{d}^n f(t)}{\mathrm{d}t^n}\right] = (i\omega)^n F(\omega)$ | $\mathcal{L}\left[\frac{d^{n} f(t)}{dt^{n}}\right] = s^{n} s - \sum_{k=0}^{n-1} s^{n-k-1} f^{(k)}(+0)$ | $\mathcal{Z}[x[n] - x[n-1]] = \frac{X(z)}{1 - z^{-1}}$ |
| $\mathcal{F}\left[t^n f(t)\right] = i^n \frac{\mathrm{d}^n F(\omega)}{\mathrm{d}\omega^n}$ | $\mathcal{L}\left[t^n f(t)\right] = (-1)^n \frac{\mathrm{d}^n F(s)}{\mathrm{d}s^n}$ | $\mathcal{Z}\left[nx[n]\right] = -z\frac{\mathrm{d}X(z)}{\mathrm{d}z}$ |
| $\mathcal{F}\left[f(t)*g(t)\right] = F(\omega)G(\omega)$ | $\mathcal{L}\left[f(t)*g(t)\right] = F(s)G(s)$ | $\mathcal{Z}\left[x[n]*y[n]\right] = X(z)Y(z)$ |
| $\mathcal{F}\left[f(t)g(t)\right] = \frac{1}{2\pi}F(\omega)*G(\omega)$ | $\mathcal{L}\left[f(t)g(t)\right] = \frac{1}{2\pi i} \lim_{T \to \infty} \int_{c-iT}^{c+iT} F(\sigma)G(s-\sigma)d\sigma$ | $\mathcal{Z}[x[n]y[n]] = \frac{1}{2\pi i} \oint_C X(\sigma)Y(z/\sigma)\sigma^{-1}d\sigma$ |
| $f(t) * g(t) = \int_{-\infty}^{\infty} f(\tau)g(t-\tau)d\tau$ | $f(t) * g(t) = \int_0^t f(\tau)g(t-\tau)d\tau$ | $x[n] * y[n] = \sum_{m = -\infty}^{\infty} x[m]y[n - m]$ |
| $\mathcal{F}\left[\delta(t) ight]=1$ | $\mathcal{L}\left[\delta(t) ight]=1$ | $\mathcal{Z}\left[\delta[n] ight]=1$ |
| $\mathcal{F}[1] = 2\pi\delta(\omega)$ | $\mathcal{L}\left[1 ight]=rac{1}{s}$ | $\mathcal{Z}\left[1\right] = \frac{1}{1 - z^{-1}}$ |
| $\mathcal{F}\left[t ight] = -2\pi i rac{\delta(\omega)}{\omega}$ | $\mathcal{L}\left[t ight]=rac{1}{s^2}$ | $\mathcal{Z}\left[nT\right] = \frac{Tz^{-1}}{\left(1 - z^{-1}\right)^2}$ |
| $\mathcal{F}\left[t^{k}\right] = 2\pi i^{k} \delta^{(k)}(\omega)$ | $\mathcal{L}\left[t^{k} ight]=rac{k!}{s^{k+1}}$ | $\mathcal{Z}\left[\left(nT\right)^{k}\right] = \left[\frac{\mathrm{d}^{k}}{\mathrm{d}s^{k}} \frac{1}{\left(1 - z^{-1}\mathrm{e}^{sT}\right)}\right]\bigg _{s=0}$ |
| $\mathcal{F}\left[e^{i\omega_0 t}\right] = 2\pi\delta(\omega - \omega_0)$ | $\mathcal{L}\left[\mathbf{e}^{s_0 t}\right] = \frac{1}{s - s_0}$ | $\mathcal{Z}\left[\mathbf{e}^{\alpha nT}\right] = \frac{1}{1 - z^{-1}\mathbf{e}^{\alpha T}}$ |
| $\mathcal{F}\left[\sin\beta t\right] = -i\pi \left(\delta \left(\omega - \beta\right) - \delta \left(\omega + \beta\right)\right)$ | $\mathcal{L}\left[\sin\beta t\right] = \frac{\beta}{s^2 + \beta^2}$ | $\mathcal{Z}\left[\sin\beta nT\right] = \frac{z^{-1}\sin\beta T}{1 - 2z^{-1}\cos\beta T + z^{-2}}$ |
| $\mathcal{F}\left[\cos\beta t\right] = \pi\left(\delta\left(\omega - \beta\right) + \delta\left(\omega + \beta\right)\right)$ | $\mathcal{L}\left[\cos\beta t\right] = \frac{s}{s^2 + \beta^2}$ | $\mathcal{Z}[\cos \beta nT] = \frac{1 - z^{-1}\cos \beta T}{1 - 2z^{-1}\cos \beta T + z^{-2}}$ |
| $\mathcal{F}\left[\Pi(t/T)\right] = T\sin\frac{\omega T}{2} / \frac{\omega T}{2}$ | $\mathcal{L}\left[\Pi_{T_1}^{T_2}(t)\right] = \frac{1}{s}\left(e^{-sT_1} - e^{-sT_2}\right)$ | |