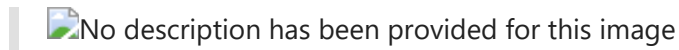


- Deep learning models that can process text (sequences of words or sequences of characters), time-series, etc.
- Two fundamental approaches for sequence processing: *recurrent neural networks* and *1D convnets*
- Applications
 - Document/time-series classification
 - Sequence-to-sequence learning such as machine translation
 - Sentiment analysis

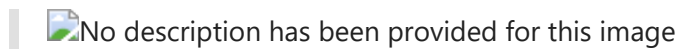
6.0 Sequential data and its representation

- Sequential data

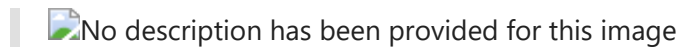


- Sequence representation

- Bag of words



- How can we deal with an order in sequence?
- Concatenate one-hot vectors



- To develop a model for sequence data, we need
 - to deal with variable length sequences
 - to maintain sequence order
 - to keep track of long-term dependencies
 - to share parameters across the sequence

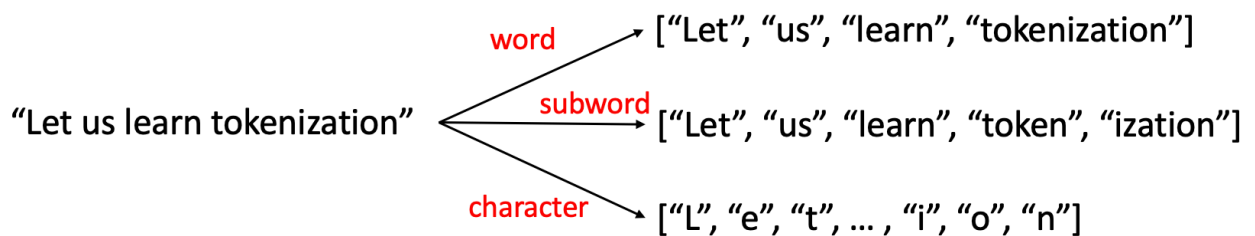
6.1 Working with text data

- Text is one of the most common forms of sequence data: a sequence of characters or a sequence of words.
- *Vectorizing* text is the process of transforming text into numeric tensors.
 - Segment text into words, and transform each word into a vector.
 - Segment text into characters, and transform each character into a vector.
 - Extract n-grams of words or characters, and transform each n-gram into a vector.
 - *N-grams* are overlapping groups of multiple consecutive words or characters.
 - Example. "The cat set on the mat."

- A bag-of-2-grams = {"The", "The cat", "cat", "cat sat", "sat", "sat on", "on", "on the", "the", "the mat", "mat"}
 - A bag-of-3-grams = {"The", "The cat", "cat", "cat sat", "The cat sat", "sat", "sat on", "on", "cat sat on", "on the", "the", "sat on the", "the mat", "mat", "on the mat"}
- The different units into which you can break down text (words, characters, or n-grams) are called *tokens*, and breaking text into such tokens is called *tokenization*.
- All text-vectorization processes consist of applying some tokenization scheme and then associating numeric vectors with the generated tokens.
 - These vectors, packed into sequence tensors, are fed into deep neural networks.

Tokenization

- One of the most important steps in text preprocessing
- The process of splitting a phrase, sentence, paragraph, one or multiple text documents into smaller units
 - Each of these smaller units is called a token.
 - Tokens can be anything: a word, a subword, or even a character.



- Word-based tokenization
 - The most commonly used delimiter is space.
 - "Is it weird I don't like coffee?" --> ["Is", "it", "weird", "I", "don't", "like", "coffee?"]
 - (if punctuation into account) --> ["Is", "it", "weird", "I", "don", "", "t", "like", "coffee", "?"]
 - Simple, but a big vocabulary (a huge embedding matrix)
 - What if we limit the number of words that can be added to the vocabulary?
- Character-based tokenization
 - Split the raw text into individual characters
 - This results in a very small vocabulary.
 - Drawbacks
 - A character usually don't carry any meaning or information.
 - Reducing the vocabulary size has a trade-off-with the sequence length.
- Subword-based tokenization
 - A solution between word and character-based tokenization

- Word-level: large vocab size, OOV tokens, misspelled words
 - Char-level: long sequences, less meaningful individual tokens
 - Principle
 - Do not split the frequently used words into smaller subwords.
 - Split the rare words into smaller meaningful subwords.
 - E.g., "boys" --> ["boy", "s"]
 - It is even possible for a model to process a word which it has never seen before as the decomposition can lead to known subwords.
-
- Byte-Pair Encoding (BPE)
 - BPE was originally a data compression algorithm proposed in 1994.
 - BPE is a powerful tool for subword tokenization.
 - The core idea
 - Iteratively find the most frequent pair of adjacent characters (or bytes) in the data and merge them into a single, new token.
 - Through this process, sequence of characters that frequently appear together are gradually grouped into meaningful subword units.
 - Process
 - Pre-tokenization --> measure frequency --> merge
 - Suppose that our corpus uses these five words.
 - ["hug", "pug", "pun", "bun", "hugs"]
 - The base vocab = ["b", "g", "h", "n", "p", "s", "u"]
 - Base vocab will contain all the ASCII characters or Unicode characters.
 - Some characters will be converted to the unknown token.
 - E.g., emojis
 - Byte-level BPE can solve this issue.
 - With base vocab, we add new tokens until the desired vocab size is reached by learning merges.
 - merge = rules to merge two elements of the existing vocab together into a new one
 - During the tokenizer training, the BPE algorithm searches for the most frequent pair of existing tokens.
 - That most frequent pair is the one that will be merged, and we rinse and repeat for the next step.
 - BPE example
 - 1. Assume that the words have the following frequencies.
 - ("hug", 10), ("pug", 5), ("pun", 12), ("bun", 4), ("hugs", 5)
 - 2. Split each word into characters (tokens in our base vocab)
 - ("h" "u" "g", 10), ("p" "u" "g", 5), ("p" "u" "n", 12), ("b" "u" "n", 4), ("h" "u" "g" "s", 5)
 - 3. Merge the most frequent pair: ("u", "g") -> "ug"
 - Vocab: ["b", "g", "h", "n", "p", "s", "u", "ug"]
 - Corpus: ("h" "ug", 10), ("p" "ug", 5), ("p" "u" "n", 12), ("b" "u" "n", 4), ("h" "ug" "s", 5)
 - 4. Merge the most frequent pair: ("u", "n") -> "un"
 - Vocab: ["b", "g", "h", "n", "p", "s", "u", "ug", "un"]
 - Corpus: ("h" "ug", 10), ("p" "ug", 5), ("p" "un", 12), ("b" "un", 4), ("h" "ug" "s", 5)
 - 5. Merge the most frequent pair: ("h", "ug") -> "hug"
 - Vocab: ["b", "g", "h", "n", "p", "s", "u", "ug", "un", "hug"]
 - Corpus: ("hug", 10), ("p" "ug", 5), ("p" "un", 12), ("b" "un", 4), ("hug" "s", 5)

- Continue until we reach the desired vocab size.
- Given the following vocab:
 - Vocab: ["b", "g", "h", "n", "p", "s", "u", "ug", "un", "hug"]
 - Corpus: ("hug", 10), ("p" "ug", 5), ("p" "un", 12), ("b" "un", 4), ("hug" "s", 5)
- New inputs are tokenized as follows:
 - "bug" -> ["b", "ug"]
 - "mug" -> ["[UNK]", "ug"]
 - "thug" -> ["[UNK]", "hug"]
 - "unhug" -> ?

In []:

```
# =====
# Exercise: BPE-based Tokenizer (OpenAI's Tiktoken)
# - The method used by models like GPT-4 and GPT-3.5-turbo.
# - Feature: Sophisticated Regex Pre-tokenization + Byte-Level BPE.
# =====
import tiktoken

print("="*25 + " Exercise 1: BPE-based Tokenizer (tiktoken) " + "="*25)

# 1. Load the tokenizer
# 'cl100k_base' is the encoding name used by OpenAI for models like GPT-4.
tokenizer_bpe = tiktoken.get_encoding("cl100k_base")

# 2. Define a sample text with English, numbers, and Korean
text = "Hello, world! 2024 is the year of AI. 안녕하세요!"

# 3. Encode (Text -> Token IDs)
encoded_ids_bpe = tokenizer_bpe.encode(text)

print(f"Original Text: {text}")
print(f"BPE Encoding Result (Token IDs): {encoded_ids_bpe}")
print(f"Total BPE Tokens: {len(encoded_ids_bpe)}\n")

# 4. Decode (Token IDs -> Text)
decoded_text_bpe = tokenizer_bpe.decode(encoded_ids_bpe)

print(f"BPE Decoding Result: {decoded_text_bpe}\n")

# 5. Inspect the individual tokens
print("Inspecting individual BPE tokens:")
tokens_bpe = [tokenizer_bpe.decode([token_id]) for token_id in encoded_ids_bpe]
print(tokens_bpe)
print("\n[Analysis Point 1] Note how the leading space is part of the token itself (e.g., ' world")
print("[Analysis Point 2] Note how '안녕하세요' (Korean) is broken down into multiple, less intuit
```

```
===== Exercise 1: BPE-based Tokenizer (tiktoken) =====  
Original Text: Hello, world! 2024 is the year of AI. 안녕하세요!  
BPE Encoding Result (Token IDs): [9906, 11, 1917, 0, 220, 2366, 19, 374, 279, 1060, 315, 15592, 1  
3, 96270, 75265, 243, 92245, 0]  
Total BPE Tokens: 18
```

BPE Decoding Result: Hello, world! 2024 is the year of AI. 안녕하세요!

Inspecting individual BPE tokens:


```
['Hello', ',', ' ', 'world', '!', ' ', '202', '4', ' ', 'is', ' ', 'the', ' ', 'year', ' ', 'of', ' ', 'AI', '.', ' ', '안',  
'녕', '하', '세', '요', '!', ' ']
```

[Analysis Point 1] Note how the leading space is part of the token itself (e.g., ' world').

[Analysis Point 2] Note how '안녕하세요' (Korean) is broken down into multiple, less intuitive byte-level tokens. This is inefficient but prevents 'unknown token' errors.

Vectorization

- There are multiple ways to associate a vector with a token.
 - *one-hot encoding* of tokens
 - *token embedding* (typically used exclusively for words, and called *word embedding*)

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One-hot encoding

- The most common, most basic way to turn a token into a vector
- It consists of associating a unique integer index with every token and then turning this integer index i into a binary vector of size N (the size of the vocabulary).
 - The vector is all zeros except for the i th entry, which is 1.

```
In [ ]: # Word-level one-hot encoding  
  
import numpy as np  
  
samples = ['The cat sat on the mat.', 'The dog ate my homework.']  
  
# build vocabulary dictionary  
token_index = {}  
for sample in samples:  
    for word in sample.split():  
        if word not in token_index:  
            token_index[word] = len(token_index)+1 # assign a unique index to each word  
  
max_length = 10 # only consider the first max_length words  
results = np.zeros(shape=(len(samples),  
                           max_length,  
                           max(token_index.values()+1)))  
  
for i, sample in enumerate(samples):  
    for j, word in list(enumerate(sample.split()))[:max_length]:
```

token_index

```
In [ ]: token_index
```

```
Out[ ]: {'0': 1,  
        '1': 2,  
        '2': 3,  
        '3': 4,  
        '4': 5,  
        '5': 6,  
        '6': 7,  
        '7': 8,  
        '8': 9,  
        '9': 10,  
        'a': 11,  
        'b': 12,  
        'c': 13,  
        'd': 14,  
        'e': 15,  
        'f': 16,  
        'g': 17,  
        'h': 18,  
        'i': 19,  
        'j': 20,  
        'k': 21,  
        'l': 22,  
        'm': 23,  
        'n': 24,  
        'o': 25,  
        'p': 26,  
        'q': 27,  
        'r': 28,  
        's': 29,  
        't': 30,  
        'u': 31,  
        'v': 32,  
        'w': 33,  
        'x': 34,  
        'y': 35,  
        'z': 36,  
        'A': 37,  
        'B': 38,  
        'C': 39,  
        'D': 40,  
        'E': 41,  
        'F': 42,  
        'G': 43,  
        'H': 44,  
        'I': 45,  
        'J': 46,  
        'K': 47,  
        'L': 48,  
        'M': 49,  
        'N': 50,  
        'O': 51,  
        'P': 52,  
        'Q': 53,  
        'R': 54,  
        'S': 55,  
        'T': 56,  
        'U': 57,  
        'V': 58,  
        'W': 59,  
        'X': 60,  
        'Y': 61,
```

```
'Z': 62,
'!': 63,
'"': 64,
'#': 65,
'$': 66,
'%': 67,
'&': 68,
"'": 69,
'(': 70,
')': 71,
'*': 72,
'+': 73,
',': 74,
'-': 75,
'.': 76,
'/': 77,
':': 78,
';': 79,
'<': 80,
'=': 81,
'>': 82,
'?: 83,
'@': 84,
 '[': 85,
 '\\': 86,
  ]': 87,
 '^': 88,
  _': 89,
  `': 90,
  {'': 91,
  '|': 92,
  }': 93,
  ~': 94,
  ' ': 95,
  \t': 96,
  \n': 97,
  \r': 98,
  \x0b': 99,
  \x0c': 100}
```

```
In [ ]: results.shape
```

```
Out[ ]: (2, 50, 101)
```

```
In [ ]: results[0,0,:]
```

```
Out[ ]: array([0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0.,
               0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0.,
               0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0.,
               0., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0., 0., 0., 0., 0.,
               0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0.,
               0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0.])
```


```
In [ ]: np.where(results[0,0,:]==1)
```

```
Out[ ]: (array([56]),)
```

Word embeddings

- The use of dense *word vectors*, also called *word embeddings*

- One-hot encoding = binary, sparse, high-dimensional


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- How to obtain word embeddings?

- Learn word embeddings jointly with the main task
- Load the precomputed word embeddings (*pretrained word embeddings*)

- **Learning word embeddings**

- In embedding space, the geometric relationship (distance, direction, etc.) between word vectors should reflect the semantic relationships between these words. \

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- Is there some ideal word-embedding space that would perfectly map human language and could be used for any natural-language-processing task?

- The `Embedding` layer in PyTorch

```
import torch
import torch.nn as nn
```

```
embedding_layer = nn.Embedding(num_embeddings=1000, embedding_dim=64)
```

- The `Embedding` layer takes as input a 2D tensor of integers `(samples, sequence_length)`, and returns a 3D floating-point tensor of shape `(samples, sequence_length, embedding_dimensionality)`.
- Each integer in the input corresponds to an index in the embedding matrix, and the layer looks up the corresponding learned vector during the forward pass.

```
In [ ]: import torch
import torch.nn as nn

embedding_layer = nn.Embedding(num_embeddings=1000, embedding_dim=64)

# Example input: batch of 2 samples, each with 4 token indices
input_indices = torch.tensor([[1, 2, 3, 4],
                               [4, 3, 2, 1]])

output = embedding_layer(input_indices)
print("Output shape:", output.shape)
```

Output shape: torch.Size([2, 4, 64])

- An embedding layer is mathematically equivalent to a linear layer without bias applied to one-hot vectors.

```
In [ ]: import torch
import torch.nn as nn

# Vocabulary of size 5, embedding dim 3
embedding = nn.Embedding(5, 3)
linear = nn.Linear(5, 3, bias=False)
```

```

# Copy weights so they're identical
linear.weight.data = embedding.weight.data.clone()

# Input: index 2 -> one-hot equivalent is [0,0,1,0,0]
index = torch.tensor([2])
one_hot = torch.nn.functional.one_hot(index, num_classes=5).float()

# Compare outputs
print("Embedding:", embedding(index))
print("Linear (one-hot):", one_hot @ linear.weight)

```

```

Embedding: tensor([[ -0.5881, -0.8058,  0.9569]], grad_fn=<EmbeddingBackward0>)
Linear (one-hot): tensor([[ -0.5881, -0.8058,  0.9569]], grad_fn=<MmBackward0>)

```

- Then, why use **Embedding** instead of **Linear**
 - Efficiency: One-hot encoding would create extremely large, mostly zero vectors. **Embedding** performs direct row indexing, which is $O(1)$ and memory-efficient.
 - Interpretability: **Embedding** directly stores the token vectors and can be pretrained, visualized, or reused.
 - Simplicity: It's conceptually clear, "Each token has its own learnable vectors."

Revisited) Binary Classification with IMDB

In [108...

```

import re, random
import torch
from collections import Counter
from datasets import load_dataset

ds = load_dataset("imdb")

id2label = {0: "neg", 1: "pos"}
train_list = [(id2label[int(r["label"])], r["text"]) for r in ds["train"]]
test_list = [(id2label[int(r["label"])], r["text"]) for r in ds["test"]]

```

In []:

```

# Simple tokenizer (English)
def simple_tokenize(s: str):
    # alphanumeric word tokens, Lowercased
    return re.findall(r"\b\w+\b", s.lower())

# Build vocab from training set
# Keep top-N frequent tokens
MAX_VOCAB = 10000
specials = ["<unk>", "<pad>"]
counter = Counter()
for _, txt in train_list:
    counter.update(simple_tokenize(txt))

most_common = [w for w, _ in counter.most_common(MAX_VOCAB - len(specials))]
itos = specials + most_common
stoi = {w: i for i, w in enumerate(itos)}
UNK_IDX = stoi["<unk>"]
PAD_IDX = stoi["<pad>"]

```

In []:

```

label_to_int = {"neg": 0, "pos": 1}

# set MAX sequence length
MAX_LEN = 300

```

```
def text_pipeline(x: str):
    ids = [stoi.get(tok, UNK_IDX) for tok in simple_tokenize(x)]
    if len(ids) > MAX_LEN:
        ids = ids[:MAX_LEN]
    return torch.tensor(ids, dtype=torch.long)

def label_pipeline(y: str):
    return torch.tensor(label_to_int[y], dtype=torch.float32)
```

```
In [ ]: random.seed(42)
        random.shuffle(train_list)
        split_idx = int(len(train_list) * 0.9)
        train_data = train_list[:split_idx]
        valid_data = train_list[split_idx:]
        test_data = test_list
```

```
In [ ]: print(f"Vocab size: {len(stoi)}, Train/Valid/Test: {len(train_data)}/{len(valid_data)}/{len(test_data)}")

Vocab size: 10000, Train/Valid/Test: 22500/2500/25000
```

```
In [ ]: import os, random, math, time
        import torch
        from torch import nn
        from torch.utils.data import DataLoader
        from torch.nn.utils.rnn import pad_sequence
        import torch.optim as optim

        SEED = 42
        random.seed(SEED)
        os.environ["PYTHONHASHSEED"] = str(SEED)
        torch.manual_seed(SEED)
        torch.cuda.manual_seed_all(SEED)

        DEVICE = torch.device("cuda" if torch.cuda.is_available() else "cpu")
        DEVICE
```

```
Out[ ]: device(type='cuda')
```

```
In [ ]: from torch.utils.data import DataLoader
        from torch.nn.utils.rnn import pad_sequence

        def collate_batch(batch):
            text_list, label_list = [], []
            for (label, text) in batch:
                text_list.append(text_pipeline(text))
                label_list.append(label_pipeline(label))
            # pad to the same length
            text_padded = pad_sequence(text_list, batch_first=True, padding_value=PAD_IDX)
            labels = torch.stack(label_list)
            return text_padded.to(DEVICE), labels.to(DEVICE)

        BATCH_SIZE = 128
        train_loader = DataLoader(train_data, batch_size=BATCH_SIZE, shuffle=True, collate_fn=collate_batch)
        valid_loader = DataLoader(valid_data, batch_size=BATCH_SIZE, shuffle=False, collate_fn=collate_batch)
        test_loader = DataLoader(test_data, batch_size=BATCH_SIZE, shuffle=False, collate_fn=collate_batch)
        len(train_loader), len(valid_loader), len(test_loader)
```

```
Out[ ]: (176, 20, 196)
```

```
In [ ]: class SentimentMLP(nn.Module):
    def __init__(self, vocab_size, embed_dim=64, hidden_dims=(32, 32), pad_idx=None):
        super().__init__()
        self.embedding = nn.Embedding(vocab_size, embed_dim, padding_idx=pad_idx if pad_idx is not None else None)
        layers = []
        in_dim = embed_dim
        for h in hidden_dims:
            layers += [nn.Linear(in_dim, h), nn.ReLU()]
            in_dim = h
        layers += [nn.Linear(in_dim, 1)] # output logit
        self.mlp = nn.Sequential(*layers)

    def forward(self, x):
        # x: (B, T)
        emb = self.embedding(x) # (B, T, E)
        # Create mask for non-pad tokens
        if hasattr(self.embedding, "padding_idx") and self.embedding.padding_idx is not None:
            pad_idx = self.embedding.padding_idx
        else:
            pad_idx = 0
        mask = (x != pad_idx).unsqueeze(-1) # (B, T, 1)
        emb = emb * mask # zero out pad embeddings
        lengths = mask.sum(dim=1).clamp(min=1) # (B, 1)
        mean_pooled = emb.sum(dim=1) / lengths # (B, E)
        logits = self.mlp(mean_pooled).squeeze(1) # (B,)
        return logits

model = SentimentMLP(vocab_size=len(stoi), embed_dim=64, hidden_dims=(32, 32), pad_idx=PAD_IDX).
model
```

```
Out[ ]: SentimentMLP(
  (embedding): Embedding(10000, 64, padding_idx=1)
  (mlp): Sequential(
    (0): Linear(in_features=64, out_features=32, bias=True)
    (1): ReLU()
    (2): Linear(in_features=32, out_features=32, bias=True)
    (3): ReLU()
    (4): Linear(in_features=32, out_features=1, bias=True)
  )
)
```

```
In [ ]: def binary_accuracy_from_logits(logits, targets):
    probs = torch.sigmoid(logits)
    preds = (probs >= 0.5).float()
    correct = (preds == targets).sum().item()
    return correct / targets.numel()

def run_epoch(dataloader, model, criterion, optimizer=None):
    is_train = optimizer is not None
    model.train() if is_train else model.eval()
    total_loss, total_acc, total_count = 0.0, 0.0, 0
    for xb, yb in dataloader:
        if is_train:
            optimizer.zero_grad(set_to_none=True)
            logits = model(xb)
            loss = criterion(logits, yb)
            if is_train:
                loss.backward()
                optimizer.step()
            bs = yb.size(0)
            total_loss += loss.item() * bs
```

```

        total_acc += binary_accuracy_from_logits(logits.detach(), yb) * bs
        total_count += bs
    return total_loss / total_count, total_acc / total_count

criterion = nn.BCEWithLogitsLoss()
optimizer = optim.Adam(model.parameters(), lr=1e-3)

EPOCHS = 20
history = {"train_loss": [], "train_acc": [], "valid_loss": [], "valid_acc": []}
best_val_acc, best_state = 0.0, None

for epoch in range(1, EPOCHS + 1):
    tr_loss, tr_acc = run_epoch(train_loader, model, criterion, optimizer)
    va_loss, va_acc = run_epoch(valid_loader, model, criterion, optimizer=None)

    history["train_loss"].append(tr_loss)
    history["train_acc"].append(tr_acc)
    history["valid_loss"].append(va_loss)
    history["valid_acc"].append(va_acc)

    print(f"Epoch {epoch:02d} | train_loss={tr_loss:.4f} acc={tr_acc:.4f} | valid_loss={va_loss:.4f} va_acc={va_acc:.4f}")
    if va_acc > best_val_acc:
        best_val_acc = va_acc
        best_state = {k: v.detach().cpu().clone() for k, v in model.state_dict().items()}

if best_state is not None:
    model.load_state_dict(best_state)

```

```

Epoch 01 | train_loss=0.6262 acc=0.6577 | valid_loss=0.4695 acc=0.7880
Epoch 02 | train_loss=0.3948 acc=0.8227 | valid_loss=0.3757 acc=0.8400
Epoch 03 | train_loss=0.3111 acc=0.8693 | valid_loss=0.3277 acc=0.8636
Epoch 04 | train_loss=0.2654 acc=0.8932 | valid_loss=0.3172 acc=0.8676
Epoch 05 | train_loss=0.2344 acc=0.9088 | valid_loss=0.3293 acc=0.8672
Epoch 06 | train_loss=0.2094 acc=0.9199 | valid_loss=0.3058 acc=0.8816
Epoch 07 | train_loss=0.1877 acc=0.9288 | valid_loss=0.3125 acc=0.8844
Epoch 08 | train_loss=0.1696 acc=0.9385 | valid_loss=0.3205 acc=0.8824
Epoch 09 | train_loss=0.1520 acc=0.9449 | valid_loss=0.3273 acc=0.8828
Epoch 10 | train_loss=0.1382 acc=0.9524 | valid_loss=0.3384 acc=0.8824
Epoch 11 | train_loss=0.1224 acc=0.9593 | valid_loss=0.3579 acc=0.8820
Epoch 12 | train_loss=0.1081 acc=0.9662 | valid_loss=0.3786 acc=0.8784
Epoch 13 | train_loss=0.0968 acc=0.9705 | valid_loss=0.3995 acc=0.8752
Epoch 14 | train_loss=0.0855 acc=0.9766 | valid_loss=0.4289 acc=0.8752
Epoch 15 | train_loss=0.0742 acc=0.9814 | valid_loss=0.4495 acc=0.8728
Epoch 16 | train_loss=0.0640 acc=0.9864 | valid_loss=0.4805 acc=0.8716
Epoch 17 | train_loss=0.0554 acc=0.9896 | valid_loss=0.5222 acc=0.8692
Epoch 18 | train_loss=0.0483 acc=0.9917 | valid_loss=0.5369 acc=0.8684
Epoch 19 | train_loss=0.0416 acc=0.9940 | valid_loss=0.5820 acc=0.8672
Epoch 20 | train_loss=0.0356 acc=0.9949 | valid_loss=0.6148 acc=0.8644

```

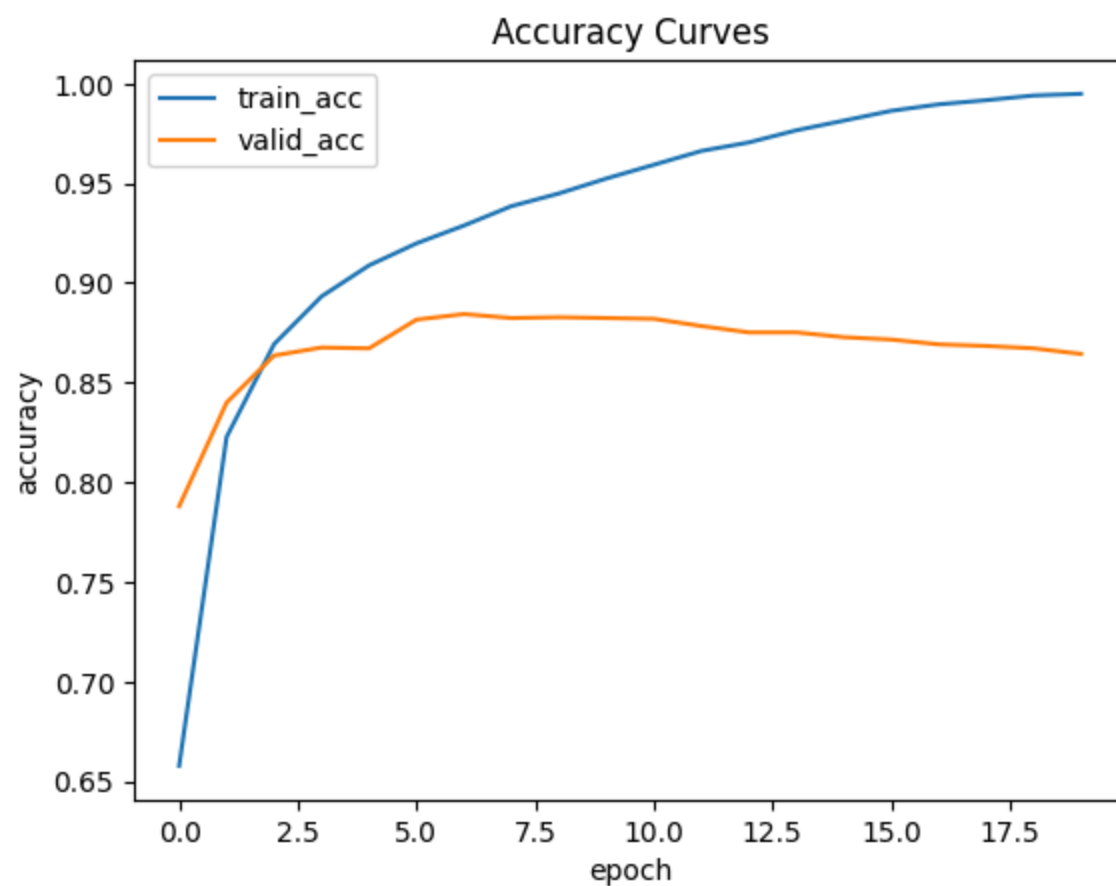
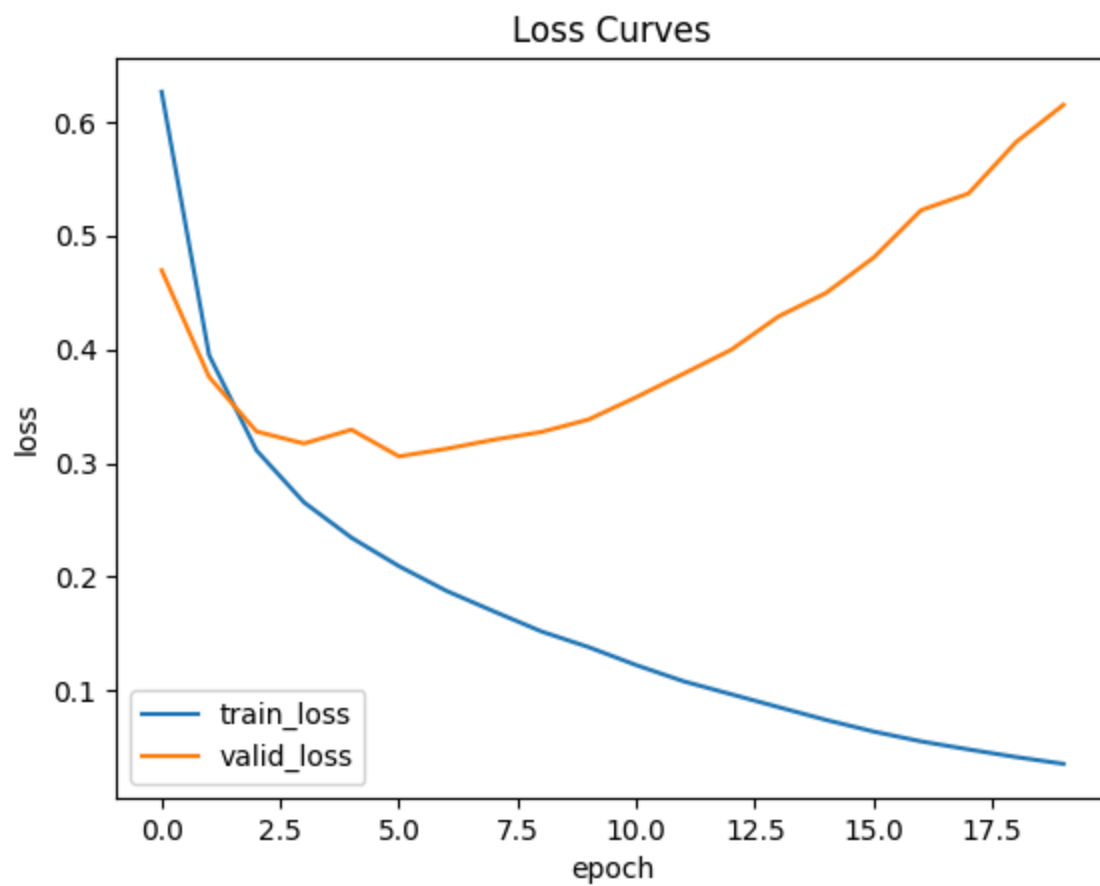
In []: `import matplotlib.pyplot as plt`

```

plt.figure()
plt.plot(history["train_loss"], label="train_loss")
plt.plot(history["valid_loss"], label="valid_loss")
plt.xlabel("epoch"); plt.ylabel("loss"); plt.legend(); plt.title("Loss Curves")
plt.show()

plt.figure()
plt.plot(history["train_acc"], label="train_acc")
plt.plot(history["valid_acc"], label="valid_acc")
plt.xlabel("epoch"); plt.ylabel("accuracy"); plt.legend(); plt.title("Accuracy Curves")
plt.show()

```



```
In [ ]: test_loss, test_acc = run_epoch(test_loader, model, criterion, optimizer=None)
print(f"TEST | loss={test_loss:.4f} acc={test_acc:.4f}")
```

TEST | loss=0.3433 acc=0.8610

Using pretrained word embeddings

- You don't have enough data available to learn truly powerful features on your own, but you expect the features that you need to be fairly generic.
- Word embedding models
 - Word2Vec (2013)
 - Global Vectors for Word Representation (GloVe) (2014)
 - fastText (2016)
 - BERT (2018)
- From raw text to word embeddings
 - Refer to the implementation above

```
In [ ]: # downloading the GloVe word embedding and preprocessing
# download url = https://drive.google.com/open?id=1NgMR-bnt02gYTr44BVTo2fRePastYypW

# mount Google Drive
from google.colab import drive
drive.mount('/content/gdrive')

EMBED_DIM = 100
glove_path = '/content/gdrive/My Drive/Lectures/deep-learning/datasets/glove.6B/glove.6B.100d.txt'
```

Drive already mounted at /content/gdrive; to attempt to forcibly remount, call drive.mount("/content/gdrive", force_remount=True).

```
In [ ]: import numpy as np

def load_glove_txt(glove_path, embedding_dim=100):
    """Read glove.6B.100d.txt into a dict: token -> np.array(embedding_dim)."""
    vectors = {}
    with open(glove_path, "r", encoding="utf-8") as f:
        for line in f:
            parts = line.rstrip().split(" ")
            token = parts[0]
            coefs = np.asarray(parts[1:], dtype=np.float32)
            if coefs.shape[0] != embedding_dim:
                continue # skip malformed rows
            vectors[token] = coefs
    return vectors

def build_embedding_matrix(stoi, glove_dict, embedding_dim=100, pad_idx=0, oov_init="normal"):
    """
    Build a (vocab_size x embedding_dim) embedding matrix aligned to 'stoi'.
    PAD row is zeros. OOV tokens use small random init.
    """
    vocab_size = len(stoi)
    emb = np.zeros((vocab_size, embedding_dim), dtype=np.float32)

    # OOV initialization
    if oov_init == "normal":
        def new_oov(): return np.random.normal(0, 0.05, size=(embedding_dim,)).astype(np.float32)
    elif oov_init == "uniform":
        def new_oov(): return np.random.uniform(-0.05, 0.05, size=(embedding_dim,)).astype(np.float32)
    else:
        def new_oov(): return np.zeros((embedding_dim,), dtype=np.float32)
```

```

    for token, idx in stoi.items():
        if idx == pad_idx:
            emb[idx] = np.zeros((embedding_dim,), dtype=np.float32)
            continue
        vec = glove_dict.get(token)
        if vec is None:
            vec = glove_dict.get(token.lower()) # just in case
        emb[idx] = vec if vec is not None else new_oov()

    return torch.tensor(emb) # (V, D)

```

```

In [ ]: # 1) Load GloVe dict
glove = load_glove_txt(glove_path, embedding_dim=EMBED_DIM)

# 2) Create embedding matrix aligned with 'stoi'
W = build_embedding_matrix(stoi, glove, embedding_dim=EMBED_DIM, pad_idx=PAD_IDX, oov_init="norm")

# 3) Build model with embed_dim=100 and Load GloVe weights
model = SentimentMLP(vocab_size=len(stoi), embed_dim=EMBED_DIM, hidden_dims=(32, 32), pad_idx=PAD_IDX)

# Copy weights to model's embedding. Match device.
with torch.no_grad():
    model.embedding.weight.data.copy_(W) # copy on CPU first
    model.embedding.weight.data[PAD_IDX].zero_() # safety: make sure PAD row is 0

# (Option A) Freeze embeddings initially (common practice), then later unfreeze for small-lr fine-tune
for p in model.embedding.parameters():
    p.requires_grad = False

# Move to device after weight init
model = model.to(DEVICE)
model

```

```

Out[ ]: SentimentMLP(
  (embedding): Embedding(10000, 100, padding_idx=1)
  (mlp): Sequential(
    (0): Linear(in_features=100, out_features=32, bias=True)
    (1): ReLU()
    (2): Linear(in_features=32, out_features=32, bias=True)
    (3): ReLU()
    (4): Linear(in_features=32, out_features=1, bias=True)
  )
)

```

```

In [ ]: criterion = nn.BCEWithLogitsLoss()
optimizer = optim.Adam(model.parameters(), lr=1e-3)

EPOCHS = 20
history = {"train_loss": [], "train_acc": [], "valid_loss": [], "valid_acc": []}
best_val_acc, best_state = 0.0, None

for epoch in range(1, EPOCHS + 1):
    tr_loss, tr_acc = run_epoch(train_loader, model, criterion, optimizer)
    va_loss, va_acc = run_epoch(valid_loader, model, criterion, optimizer=None)

    history["train_loss"].append(tr_loss)
    history["train_acc"].append(tr_acc)
    history["valid_loss"].append(va_loss)
    history["valid_acc"].append(va_acc)

    print(f"Epoch {epoch:02d} | train_loss={tr_loss:.4f} acc={tr_acc:.4f} | valid_loss={va_loss:.4f} acc={va_acc:.4f}")

```



```

    if va_acc > best_val_acc:
        best_val_acc = va_acc
        best_state = {k: v.detach().cpu().clone() for k, v in model.state_dict().items()}

if best_state is not None:
    model.load_state_dict(best_state)

```

Epoch 01		train_loss=0.6530	acc=0.6231		valid_loss=0.5802	acc=0.7100
Epoch 02		train_loss=0.5364	acc=0.7389		valid_loss=0.5005	acc=0.7552
Epoch 03		train_loss=0.4979	acc=0.7589		valid_loss=0.4893	acc=0.7628
Epoch 04		train_loss=0.4852	acc=0.7674		valid_loss=0.4969	acc=0.7588
Epoch 05		train_loss=0.4775	acc=0.7743		valid_loss=0.4688	acc=0.7800
Epoch 06		train_loss=0.4732	acc=0.7764		valid_loss=0.4759	acc=0.7720
Epoch 07		train_loss=0.4681	acc=0.7795		valid_loss=0.4628	acc=0.7844
Epoch 08		train_loss=0.4658	acc=0.7802		valid_loss=0.4725	acc=0.7752
Epoch 09		train_loss=0.4614	acc=0.7836		valid_loss=0.4578	acc=0.7840
Epoch 10		train_loss=0.4603	acc=0.7829		valid_loss=0.4576	acc=0.7860
Epoch 11		train_loss=0.4594	acc=0.7849		valid_loss=0.4553	acc=0.7836
Epoch 12		train_loss=0.4565	acc=0.7857		valid_loss=0.4570	acc=0.7860
Epoch 13		train_loss=0.4596	acc=0.7850		valid_loss=0.4532	acc=0.7860
Epoch 14		train_loss=0.4531	acc=0.7901		valid_loss=0.4533	acc=0.7872
Epoch 15		train_loss=0.4535	acc=0.7919		valid_loss=0.4510	acc=0.7880
Epoch 16		train_loss=0.4482	acc=0.7940		valid_loss=0.4496	acc=0.7876
Epoch 17		train_loss=0.4492	acc=0.7924		valid_loss=0.4483	acc=0.7908
Epoch 18		train_loss=0.4499	acc=0.7926		valid_loss=0.4514	acc=0.7888
Epoch 19		train_loss=0.4477	acc=0.7928		valid_loss=0.4468	acc=0.7912
Epoch 20		train_loss=0.4477	acc=0.7918		valid_loss=0.4492	acc=0.7884

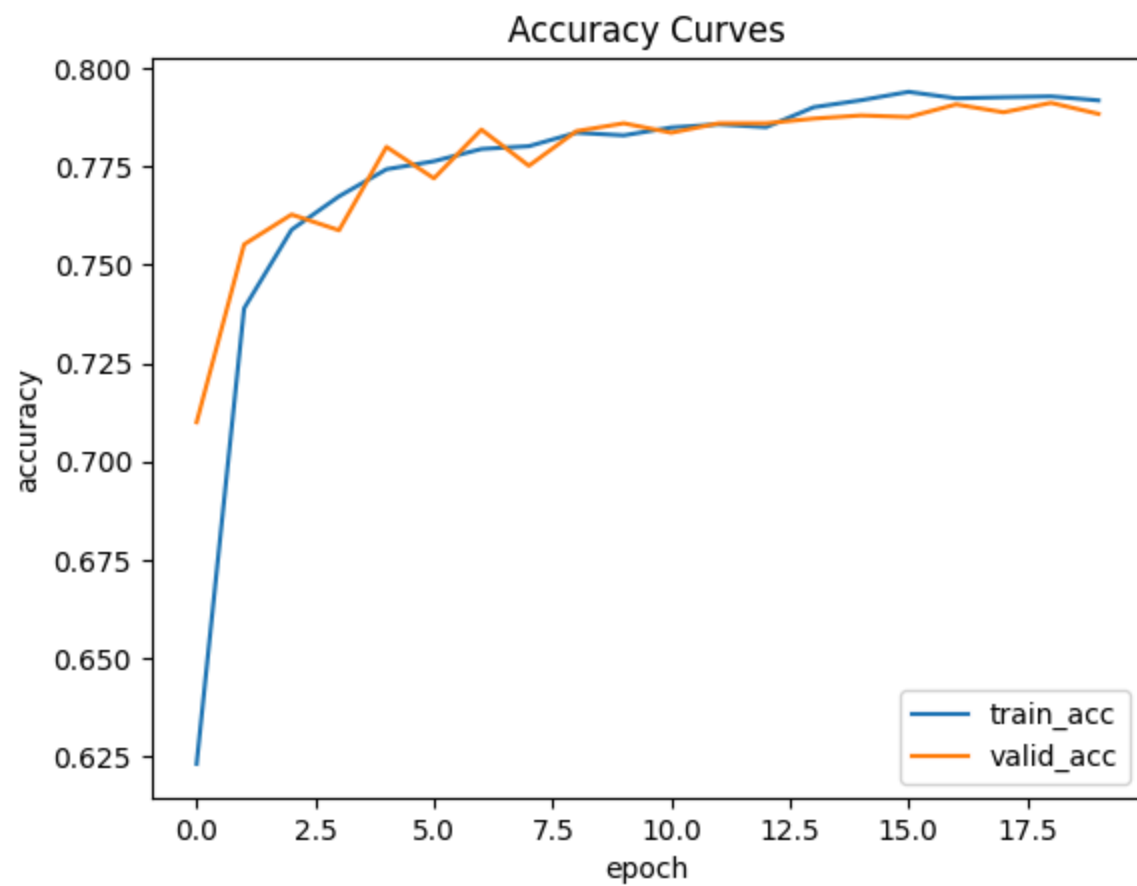
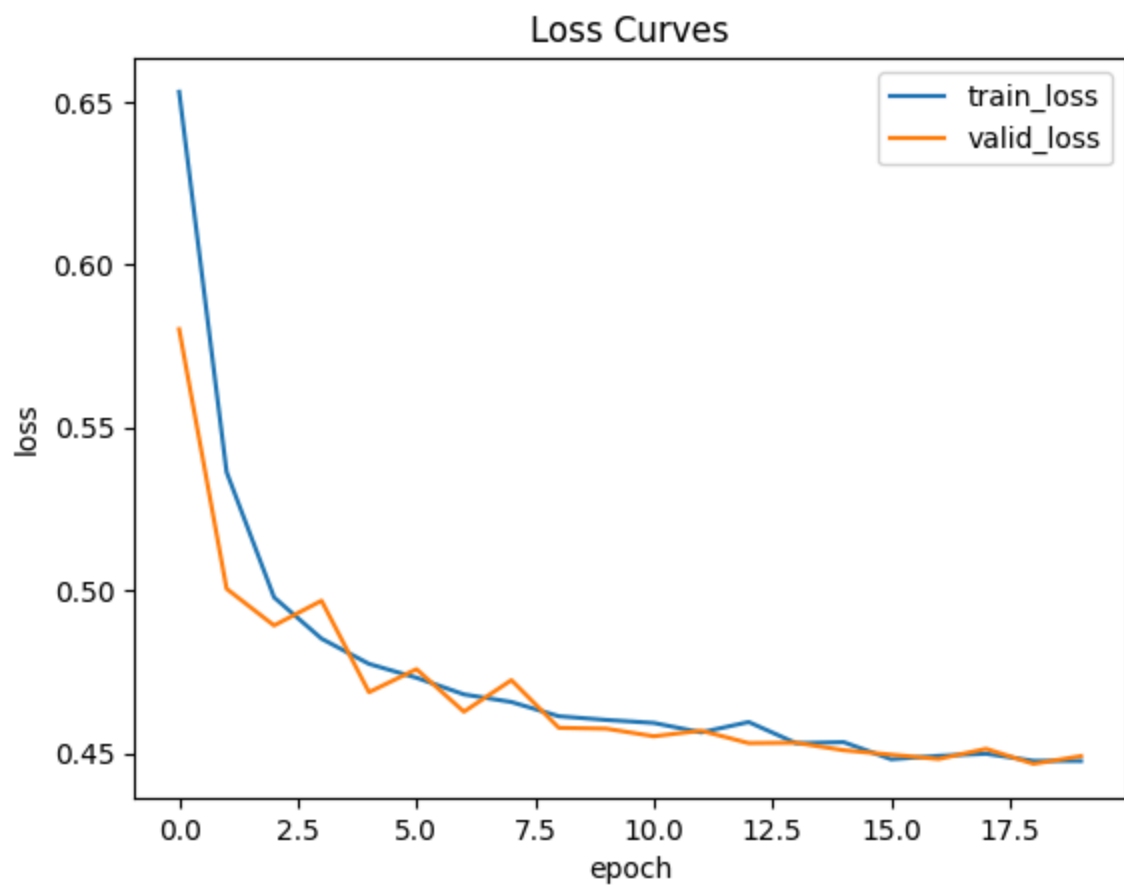
In []: `import matplotlib.pyplot as plt`

```

plt.figure()
plt.plot(history["train_loss"], label="train_loss")
plt.plot(history["valid_loss"], label="valid_loss")
plt.xlabel("epoch"); plt.ylabel("loss"); plt.legend(); plt.title("Loss Curves")
plt.show()

plt.figure()
plt.plot(history["train_acc"], label="train_acc")
plt.plot(history["valid_acc"], label="valid_acc")
plt.xlabel("epoch"); plt.ylabel("accuracy"); plt.legend(); plt.title("Accuracy Curves")
plt.show()

```



```
In [ ]: test_loss, test_acc = run_epoch(test_loader, model, criterion, optimizer=None)
        print(f"TEST | loss={test_loss:.4f} acc={test_acc:.4f}")
```

TEST | loss=0.4489 acc=0.7913

- Finetuning the pretrained embeddings

```

In [ ]: # 1) Load GloVe dict
glove = load_glove_txt(glove_path, embedding_dim=EMBED_DIM)

# 2) Create embedding matrix aligned with 'stoi'
W = build_embedding_matrix(stoi, glove, embedding_dim=EMBED_DIM, pad_idx=PAD_IDX, oov_init="norm")

# 3) Build model with embed_dim=100 and Load GloVe weights
model = SentimentMLP(vocab_size=len(stoi), embed_dim=EMBED_DIM, hidden_dims=(32, 32), pad_idx=PAD_IDX)

# Copy weights to model's embedding. Match device.
with torch.no_grad():
    model.embedding.weight.data.copy_(W) # copy on CPU first
    model.embedding.weight.data[PAD_IDX].zero_() # safety: make sure PAD row is 0

# (Option A) Freeze embeddings initially (common practice), then later unfreeze for small-lr fine-tune
# for p in model.embedding.parameters():
#     p.requires_grad = False

# Move to device after weight init
model = model.to(DEVICE)
model

```

```

Out[ ]: SentimentMLP(
  (embedding): Embedding(10000, 100, padding_idx=1)
  (mlp): Sequential(
    (0): Linear(in_features=100, out_features=32, bias=True)
    (1): ReLU()
    (2): Linear(in_features=32, out_features=32, bias=True)
    (3): ReLU()
    (4): Linear(in_features=32, out_features=1, bias=True)
  )
)

```

```

In [ ]: criterion = nn.BCEWithLogitsLoss()
optimizer = optim.Adam(model.parameters(), lr=1e-3)

EPOCHS = 20
history = {"train_loss": [], "train_acc": [], "valid_loss": [], "valid_acc": []}
best_val_acc, best_state = 0.0, None

for epoch in range(1, EPOCHS + 1):
    tr_loss, tr_acc = run_epoch(train_loader, model, criterion, optimizer)
    va_loss, va_acc = run_epoch(valid_loader, model, criterion, optimizer=None)

    history["train_loss"].append(tr_loss)
    history["train_acc"].append(tr_acc)
    history["valid_loss"].append(va_loss)
    history["valid_acc"].append(va_acc)

    print(f"Epoch {epoch:02d} | train_loss={tr_loss:.4f} acc={tr_acc:.4f} | valid_loss={va_loss:.4f} acc={va_acc:.4f}")
    if va_acc > best_val_acc:
        best_val_acc = va_acc
        best_state = {k: v.detach().cpu().clone() for k, v in model.state_dict().items()}

if best_state is not None:
    model.load_state_dict(best_state)

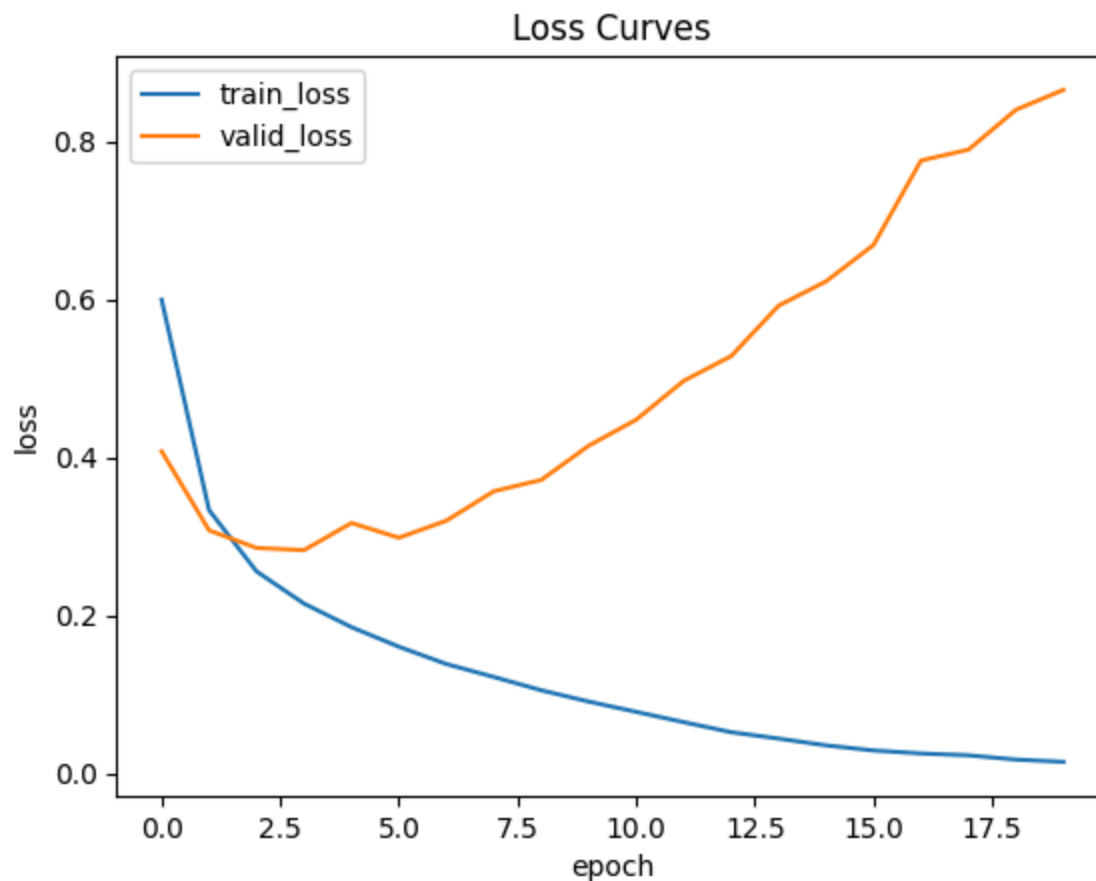
```

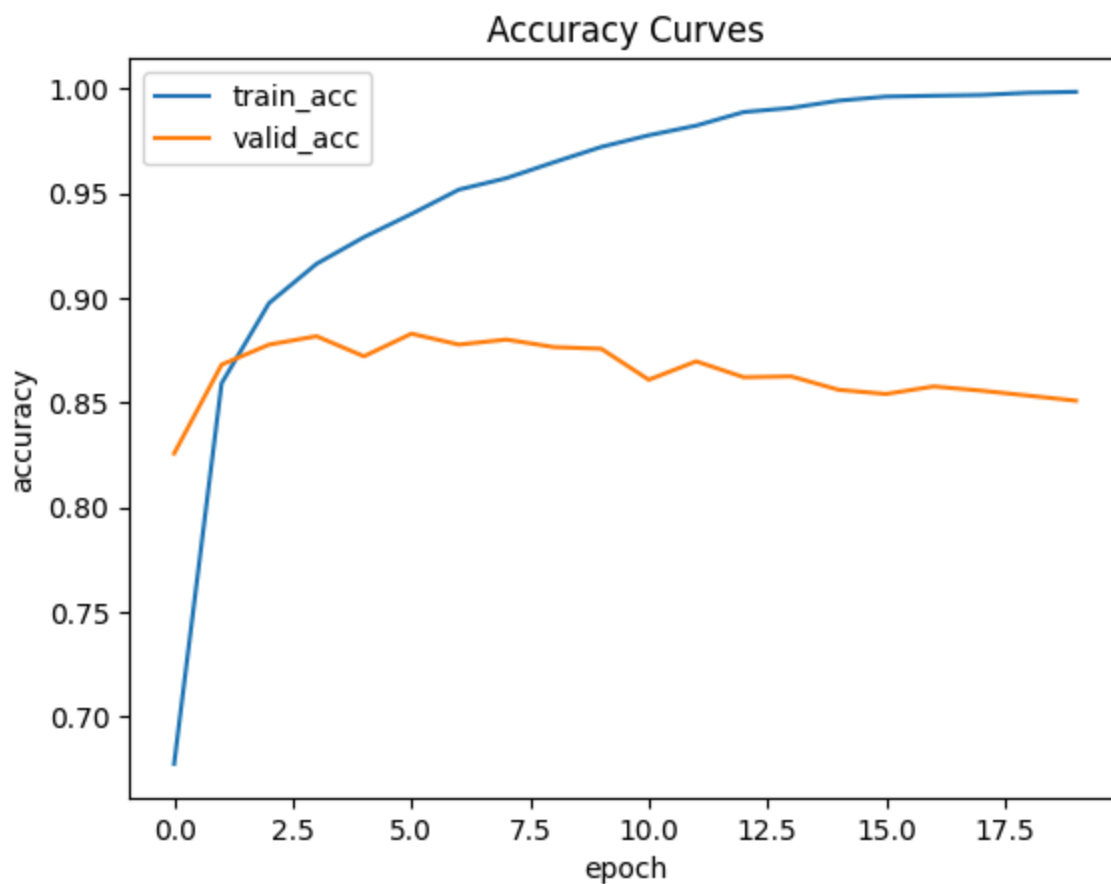
Epoch 01	train_loss=0.5995	acc=0.6773	valid_loss=0.4076	acc=0.8256
Epoch 02	train_loss=0.3332	acc=0.8591	valid_loss=0.3076	acc=0.8680
Epoch 03	train_loss=0.2557	acc=0.8974	valid_loss=0.2854	acc=0.8776
Epoch 04	train_loss=0.2150	acc=0.9162	valid_loss=0.2826	acc=0.8816
Epoch 05	train_loss=0.1851	acc=0.9289	valid_loss=0.3170	acc=0.8720
Epoch 06	train_loss=0.1604	acc=0.9400	valid_loss=0.2983	acc=0.8828
Epoch 07	train_loss=0.1385	acc=0.9516	valid_loss=0.3199	acc=0.8776
Epoch 08	train_loss=0.1221	acc=0.9571	valid_loss=0.3572	acc=0.8800
Epoch 09	train_loss=0.1053	acc=0.9647	valid_loss=0.3715	acc=0.8764
Epoch 10	train_loss=0.0909	acc=0.9720	valid_loss=0.4148	acc=0.8756
Epoch 11	train_loss=0.0779	acc=0.9776	valid_loss=0.4477	acc=0.8608
Epoch 12	train_loss=0.0649	acc=0.9822	valid_loss=0.4969	acc=0.8696
Epoch 13	train_loss=0.0522	acc=0.9887	valid_loss=0.5282	acc=0.8620
Epoch 14	train_loss=0.0441	acc=0.9907	valid_loss=0.5920	acc=0.8624
Epoch 15	train_loss=0.0356	acc=0.9941	valid_loss=0.6228	acc=0.8560
Epoch 16	train_loss=0.0291	acc=0.9961	valid_loss=0.6689	acc=0.8540
Epoch 17	train_loss=0.0253	acc=0.9965	valid_loss=0.7757	acc=0.8576
Epoch 18	train_loss=0.0229	acc=0.9968	valid_loss=0.7894	acc=0.8556
Epoch 19	train_loss=0.0176	acc=0.9979	valid_loss=0.8399	acc=0.8532
Epoch 20	train_loss=0.0147	acc=0.9984	valid_loss=0.8651	acc=0.8508

```
In [ ]: import matplotlib.pyplot as plt
```

```
plt.figure()
plt.plot(history["train_loss"], label="train_loss")
plt.plot(history["valid_loss"], label="valid_loss")
plt.xlabel("epoch"); plt.ylabel("loss"); plt.legend(); plt.title("Loss Curves")
plt.show()

plt.figure()
plt.plot(history["train_acc"], label="train_acc")
plt.plot(history["valid_acc"], label="valid_acc")
plt.xlabel("epoch"); plt.ylabel("accuracy"); plt.legend(); plt.title("Accuracy Curves")
plt.show()
```






```
In [ ]: test_loss, test_acc = run_epoch(test_loader, model, criterion, optimizer=None)
        print(f"TEST | loss={test_loss:.4f} acc={test_acc:.4f}")
```

TEST | loss=0.3290 acc=0.8700

6.2 Recurrent neural networks

- What we did in the IMDB example: an entire movie review was transformed into a single vector and processed in one go. --> *feedforward networks*
- As you are reading the present sentence, you are processing it word by word while keeping memories of what came before.
- A *recurrent neural network* (RNN) processes sequences by iterating through the sequence elements and maintaining a *state* containing information relative to what it has seen so far.
 - The network internally loops over sequence elements.

 No description has been provided for this image

```
# Pseudocode RNN
state_t = 0 # the state at t
for input_t in input_sequence: # iterates over sequence elements
    output_t = f(input_t, state_t)
    state_t = output_t # the previous output becomes the state for the next iteration

# More detailed pseudocode for the RNN
state_t = 0
for input_t in input_sequence:
```

```
output_t = activation(dot(W, input_t) + dot(U, state_t) + b)
state_t = output_t
```

```
In [ ]: # Numpy implementation of a simple RNN
import numpy as np

timesteps = 100
input_features = 32
output_features = 64


inputs = np.random.random((timesteps, input_features)) # input data

state_t = np.zeros((output_features,))

W = np.random.random((output_features, input_features))
U = np.random.random((output_features, output_features))
b = np.random.random((output_features,))

successive_outputs = []
for input_t in inputs:
    output_t = np.tanh(np.dot(W, input_t) + np.dot(U, state_t) + b)
    successive_outputs.append(output_t)
    state_t = output_t

final_output_sequence = np.concatenate(successive_outputs, axis=0)
```

 No description has been provided for this image

A recurrent layer in PyTorch

```
import torch
import torch.nn as nn

rnn = nn.RNN(
    input_size=32,      # number of input features per timestep
    hidden_size=64,     # size of the hidden state (output features)
    batch_first=True    # input and output tensors have shape (batch, time, features)
)
```

- **RNN** processes batches of sequences.
 - Inputs (batch_size, timesteps, input_features)
 - The forward pass returns two tensors:
`output, hidden = rnn(x)`
 - **output** : contains the hidden state for each timestep
 - shape = (batch_size, timesteps, hidden_size)
 - **hidden** : contains the hidden state for the last timestep
 - shape = (num_layers, batch_size, hidden_size)

```
In [ ]: import torch
import torch.nn as nn

rnn = nn.RNN(
    input_size=32,      # number of input features per timestep
    hidden_size=64,     # size of the hidden state (output features)
    batch_first=True    # input and output tensors have shape (batch, time, features)
)
```

```

x = torch.randn(8, 10, 32) # (batch, timesteps, input_features)
output, hidden = rnn(x)

full_sequence = output          # all timesteps
last_output   = hidden[-1]      # last timestep only
print(full_sequence.shape)      # (8, 10, 64)
print(last_output.shape)        # (8, 64)

```

```

torch.Size([8, 10, 64])
torch.Size([8, 64])

```

```

In [ ]: import torch
import torch.nn as nn

class SentimentRNN(nn.Module):
    def __init__(self, vocab_size, embed_dim=64, hidden_size=64, num_layers=1, pad_idx=None):
        super().__init__()
        # Embedding Layer
        self.embedding = nn.Embedding(
            vocab_size,
            embed_dim,
            padding_idx=pad_idx if pad_idx is not None else 0
        )

        # Simple RNN Layer
        self.rnn = nn.RNN(
            input_size=embed_dim,
            hidden_size=hidden_size,
            num_layers=num_layers,
            batch_first=True
        )

        # Output Layer
        self.fc = nn.Linear(hidden_size, 1) # binary classification (logit output)

    def forward(self, x):
        # x: (B, T)
        emb = self.embedding(x) # (B, T, E)

        # Handle padding (mask and sequence lengths)
        if hasattr(self.embedding, "padding_idx") and self.embedding.padding_idx is not None:
            pad_idx = self.embedding.padding_idx
            lengths = (x != pad_idx).sum(dim=1).cpu() # (B,)
            packed = nn.utils.rnn.pack_padded_sequence(
                emb, lengths, batch_first=True, enforce_sorted=False
            )
            packed_out, hidden = self.rnn(packed)
            # hidden: (num_layers, B, hidden_size)
            last_hidden = hidden[-1] # Last layer's hidden state
        else:
            output, hidden = self.rnn(emb)
            last_hidden = hidden[-1] # (B, hidden_size)

        logits = self.fc(last_hidden).squeeze(1) # (B,)
        return logits

```

```

In [ ]: !pip install torchinfo -q
from torchinfo import summary

model = SentimentRNN(vocab_size=10000).cpu()

```

```
summary(model, input_data=torch.randint(0, 10000, (1, 20)).long())
```

```
Out[ ]: =====
Layer (type:depth-idx)          Output Shape          Param #
=====
SentimentRNN                    [1]                   --
├─Embedding: 1-1                [1, 20, 64]          640,000
├─RNN: 1-2                      [20, 64]             8,320
└─Linear: 1-3                  [1, 1]               65
=====
Total params: 648,385
Trainable params: 648,385
Non-trainable params: 0
Total mult-adds (Units.MEGABYTES): 11.29
=====
Input size (MB): 0.00
Forward/backward pass size (MB): 0.02
Params size (MB): 2.59
Estimated Total Size (MB): 2.61
=====
```

- Handling variable-length sequences with `nn.utils.rnn.pack_padded_sequence`
 - When working with text or sequential data, different samples often have different sequence lengths.
 - To form a batch, all sequences must be padded to the same length (e.g., using `<pad>` tokens).
 - However, RNNs will still process those padding tokens, which adds unnecessary computation and noise.
 - Ex.
 - "I love it" -> [12, 45, 88, 0]
 - "This movie is great" -> [13, 56, 44, 99]
 - "Bad" -> [77, 0, 0, 0]
 - The RNN will compute over all timesteps (including `<pad>`), even though most of those zeros carry no meaning.
 - `pack_padded_sequence`
 - PyTorch provides a utility that allows RNNs to ignore padded timesteps efficiently:
`from torch.nn.utils.rnn import pack_padded_sequence`
 - ```
packed = pack_padded_sequence(
 embedded_batch, lengths, batch_first=True, enforce_sorted=False
)
output, hidden = rnn(packed)
```

      - `embedded_batch` : (batch\_size, seq\_len, embed\_dim)
      - `lengths` : a tensor or list containing the true lengths of each sequence
      - `batch_first=True` : ensures batch dimension comes first ((B, T, E))
      - `enforce_sorted=False` : lets you use unsorted batches safely
    - Once packed, the RNN will automatically skip over padding positions, processing only the valid tokens in each sequence.



```
In []: import torch
from torch.nn.utils.rnn import pad_sequence, pack_padded_sequence, pad_packed_sequence

Example: three variable-length sequences (token IDs)
seqs = [
 torch.tensor([1, 2, 3, 4]), # length = 4
 torch.tensor([5, 6, 7]), # length = 3
 torch.tensor([8, 9]) # length = 2
]

Pad them to the same length (right-padding with 0)
padded = pad_sequence(seqs, batch_first=True, padding_value=0)
print("Padded batch (shape =", padded.shape, "):\n", padded)

Compute true lengths
lengths = torch.tensor([len(s) for s in seqs])
print("\nSequence lengths:", lengths.tolist())

Pack the padded batch
packed = pack_padded_sequence(padded, lengths, batch_first=True, enforce_sorted=False)
print("\nPacked data representation:\n", packed.data)
print("Packed batch_sizes:", packed.batch_sizes)

Unpack (restore to padded form)
unpacked, unpacked_lengths = pad_packed_sequence(packed, batch_first=True)
print("\nUnpacked (back to padded):\n", unpacked)
```

Padded batch (shape = torch.Size([3, 4]) ):

```
tensor([[1, 2, 3, 4],
 [5, 6, 7, 0],
 [8, 9, 0, 0]])
```

Sequence lengths: [4, 3, 2]

Packed data representation:

```
tensor([1, 5, 8, 2, 6, 9, 3, 7, 4])
```

Packed batch\_sizes: tensor([3, 3, 2, 1])

Unpacked (back to padded):

```
tensor([[1, 2, 3, 4],
 [5, 6, 7, 0],
 [8, 9, 0, 0]])
```

- Staking several recurrent layers

```
In []: !pip install torchinfo -q
from torchinfo import summary

model = SentimentRNN(vocab_size=10000, num_layers=2).cpu()

summary(model, input_data=torch.randint(0, 10000, (1, 20)).long())
```

```

Out[]: =====
Layer (type:depth-idx) Output Shape Param #
=====
SentimentRNN [1] --
├─Embedding: 1-1 [1, 20, 64] 640,000
├─RNN: 1-2 [20, 64] 16,640
└─Linear: 1-3 [1, 1] 65
=====

Total params: 656,705
Trainable params: 656,705
Non-trainable params: 0
Total mult-adds (Units.MEGABYTES): 21.94
=====

Input size (MB): 0.00
Forward/backward pass size (MB): 0.02
Params size (MB): 2.63
Estimated Total Size (MB): 2.65
=====

```

- Revisit the IMDB movie review classification problem

```

In []: model = SentimentRNN(
 vocab_size=len(stoi),
 embed_dim=64,
 hidden_size=32,
 num_layers=1,
 pad_idx=PAD_IDX
).to(DEVICE)

criterion = nn.BCEWithLogitsLoss()
optimizer = optim.Adam(model.parameters(), lr=1e-3)

EPOCHS = 20
history = {"train_loss": [], "train_acc": [], "valid_loss": [], "valid_acc": []}
best_val_acc, best_state = 0.0, None

for epoch in range(1, EPOCHS + 1):
 tr_loss, tr_acc = run_epoch(train_loader, model, criterion, optimizer)
 va_loss, va_acc = run_epoch(valid_loader, model, criterion, optimizer=None)

 history["train_loss"].append(tr_loss)
 history["train_acc"].append(tr_acc)
 history["valid_loss"].append(va_loss)
 history["valid_acc"].append(va_acc)

 print(f"Epoch {epoch:02d} | train_loss={tr_loss:.4f} acc={tr_acc:.4f} | valid_loss={va_loss:.4f} acc={va_acc:.4f}")
 if va_acc > best_val_acc:
 best_val_acc = va_acc
 best_state = {k: v.detach().cpu().clone() for k, v in model.state_dict().items()}

if best_state is not None:
 model.load_state_dict(best_state)

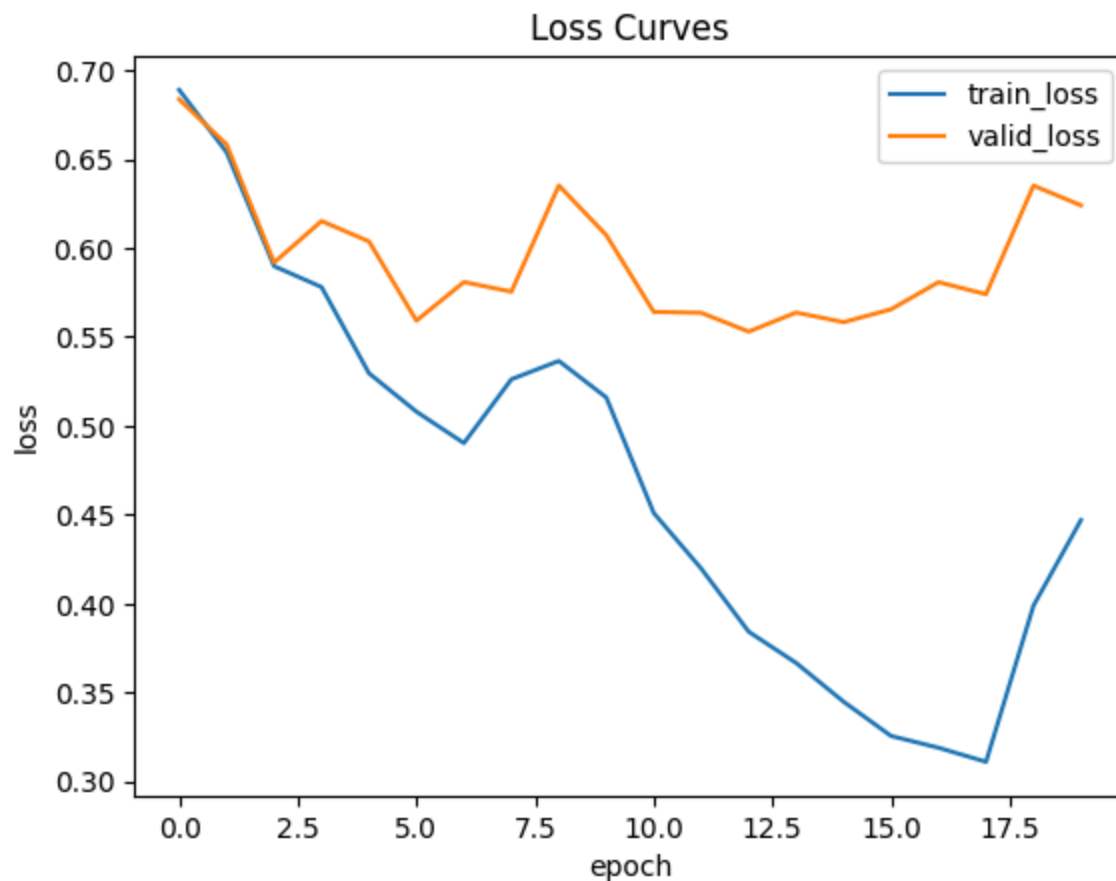
```

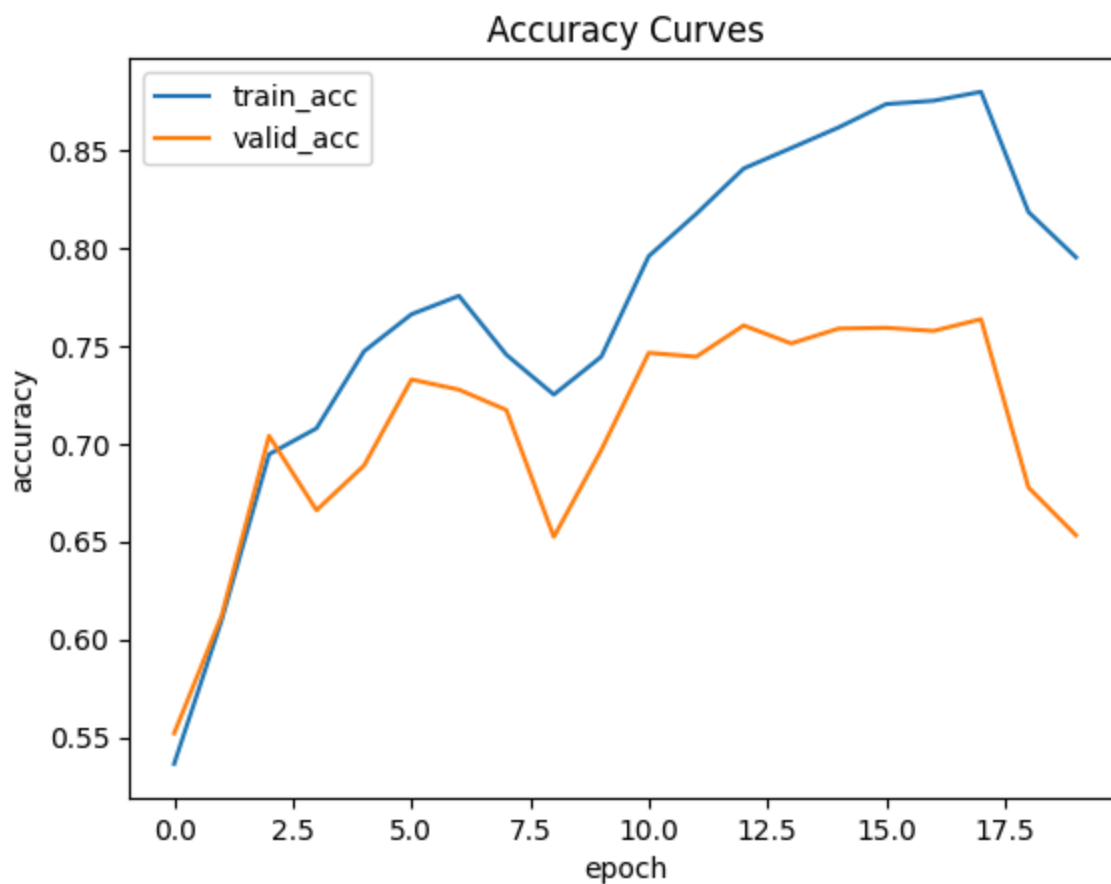
|          |                   |            |                   |            |
|----------|-------------------|------------|-------------------|------------|
| Epoch 01 | train_loss=0.6890 | acc=0.5364 | valid_loss=0.6836 | acc=0.5520 |
| Epoch 02 | train_loss=0.6539 | acc=0.6098 | valid_loss=0.6582 | acc=0.6120 |
| Epoch 03 | train_loss=0.5898 | acc=0.6946 | valid_loss=0.5918 | acc=0.7040 |
| Epoch 04 | train_loss=0.5781 | acc=0.7079 | valid_loss=0.6152 | acc=0.6660 |
| Epoch 05 | train_loss=0.5296 | acc=0.7472 | valid_loss=0.6037 | acc=0.6888 |
| Epoch 06 | train_loss=0.5080 | acc=0.7661 | valid_loss=0.5592 | acc=0.7328 |
| Epoch 07 | train_loss=0.4903 | acc=0.7755 | valid_loss=0.5809 | acc=0.7276 |
| Epoch 08 | train_loss=0.5262 | acc=0.7454 | valid_loss=0.5755 | acc=0.7172 |
| Epoch 09 | train_loss=0.5365 | acc=0.7251 | valid_loss=0.6352 | acc=0.6524 |
| Epoch 10 | train_loss=0.5160 | acc=0.7444 | valid_loss=0.6072 | acc=0.6968 |
| Epoch 11 | train_loss=0.4510 | acc=0.7958 | valid_loss=0.5641 | acc=0.7464 |
| Epoch 12 | train_loss=0.4197 | acc=0.8174 | valid_loss=0.5636 | acc=0.7444 |
| Epoch 13 | train_loss=0.3842 | acc=0.8406 | valid_loss=0.5530 | acc=0.7604 |
| Epoch 14 | train_loss=0.3667 | acc=0.8510 | valid_loss=0.5637 | acc=0.7512 |
| Epoch 15 | train_loss=0.3448 | acc=0.8616 | valid_loss=0.5583 | acc=0.7588 |
| Epoch 16 | train_loss=0.3256 | acc=0.8735 | valid_loss=0.5655 | acc=0.7592 |
| Epoch 17 | train_loss=0.3190 | acc=0.8752 | valid_loss=0.5808 | acc=0.7576 |
| Epoch 18 | train_loss=0.3111 | acc=0.8797 | valid_loss=0.5740 | acc=0.7636 |
| Epoch 19 | train_loss=0.3989 | acc=0.8183 | valid_loss=0.6351 | acc=0.6776 |
| Epoch 20 | train_loss=0.4470 | acc=0.7952 | valid_loss=0.6240 | acc=0.6532 |

```
In []: import matplotlib.pyplot as plt
```





```
plt.figure()
plt.plot(history["train_loss"], label="train_loss")
plt.plot(history["valid_loss"], label="valid_loss")
plt.xlabel("epoch"); plt.ylabel("loss"); plt.legend(); plt.title("Loss Curves")
plt.show()

plt.figure()
plt.plot(history["train_acc"], label="train_acc")
plt.plot(history["valid_acc"], label="valid_acc")
plt.xlabel("epoch"); plt.ylabel("accuracy"); plt.legend(); plt.title("Accuracy Curves")
plt.show()
```






## Applications of RNNs

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## Flexibility of RNNs

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## Understanding the LSTM and GRU layers


- There are two other popular recurrent layer: `LSTM` and `GRU`.
- `SimpleRNN` is difficult to learn long-term dependencies.
  - This is due to the *vanishing gradient problem*.
- Long Short-Term Memory (LSTM)
  - proposed by Hochreiter and Schmidhuber in 1997
  - It adds a way to carry information across many timesteps.

- SimpleRNN

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- SimpleRNN + additional data flow (carry)

- An additional data flow that carries information across timesteps
  - $C_t$  where  $C$  stands for *carry*
- It will be combined with the input connections and the recurrent connection via a dense transformation.
- Then, it will affect the state being sent to the next timestep.

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- LSTM

- How is the next value of the carry dataflow computed?
  - It involves three distinct transformations, which all have the form of the following:  
 $y = \text{activation}(\text{dot}(\text{state}_t, U) + \text{dot}(\text{input}_t, W) + b)$
  - All three transformations have their own weight matrices.  
 $\text{output}_t = \text{activation}(\text{dot}(\text{state}_t, U_o) + \text{dot}(\text{input}_t, W_o) + \text{dot}(C_t, V_o) + b_o)$

$i_t = \text{activation}(\text{dot}(\text{state}_t, U_i) + \text{dot}(\text{input}_t, W_i) + b_i)$   
 $f_t = \text{activation}(\text{dot}(\text{state}_t, U_f) + \text{dot}(\text{input}_t, W_f) + b_f)$   
 $k_t = \text{activation}(\text{dot}(\text{state}_t, U_k) + \text{dot}(\text{input}_t, W_k) + b_k)$

- We obtain the new carry state ( $c_t$ ).

$c_{(t+1)} = i_t * k_t + c_t * f_t$

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- Details of LSTM

- LSTM diagram


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- Computations involved in LSTM


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- GRU (Gated Recurrent Unit)

- GRU diagram

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- Computations involved in GRU

 No description has been provided for this image

# LSTM example in PyTorch

```
In []: import torch
import torch.nn as nn

class SentimentLSTM(nn.Module):
 def __init__(self, vocab_size, embed_dim=64, hidden_size=64, num_layers=1, pad_idx=None):
 super().__init__()
 # Embedding Layer
 self.embedding = nn.Embedding(
 vocab_size,
 embed_dim,
 padding_idx=pad_idx if pad_idx is not None else 0
)

 # LSTM Layer
 self.lstm = nn.LSTM(
 input_size=embed_dim,
 hidden_size=hidden_size,
 num_layers=num_layers,
 batch_first=True
)

 # Output Layer
 self.fc = nn.Linear(hidden_size, 1) # binary classification (logit output)

 def forward(self, x):
 # x: (B, T)
 emb = self.embedding(x) # (B, T, E)

 # Handle padding (mask and sequence lengths)
 if hasattr(self.embedding, "padding_idx") and self.embedding.padding_idx is not None:
 pad_idx = self.embedding.padding_idx
 lengths = (x != pad_idx).sum(dim=1).cpu() # (B,)
 packed = nn.utils.rnn.pack_padded_sequence(
 emb, lengths, batch_first=True, enforce_sorted=False
)
 packed_out, (hidden, cell) = self.lstm(packed)
 # hidden: (num_layers, B, hidden_size)
 last_hidden = hidden[-1] # Last layer's hidden state
 else:
 output, hidden = self.lstm(emb)
 last_hidden = hidden[-1] # (B, hidden_size)

 logits = self.fc(last_hidden).squeeze(1) # (B,)
 return logits
```

```
In []: model = SentimentLSTM(
 vocab_size=len(stoi),
 embed_dim=64,
 hidden_size=32,
 num_layers=1,
 pad_idx=PAD_IDX
).to(DEVICE)

criterion = nn.BCEWithLogitsLoss()
optimizer = optim.Adam(model.parameters(), lr=1e-3)

EPOCHS = 20
history = {"train_loss": [], "train_acc": [], "valid_loss": [], "valid_acc": []}
```

```

best_val_acc, best_state = 0.0, None

for epoch in range(1, EPOCHS + 1):
 tr_loss, tr_acc = run_epoch(train_loader, model, criterion, optimizer)
 va_loss, va_acc = run_epoch(valid_loader, model, criterion, optimizer=None)

 history["train_loss"].append(tr_loss)
 history["train_acc"].append(tr_acc)
 history["valid_loss"].append(va_loss)
 history["valid_acc"].append(va_acc)

 print(f"Epoch {epoch:02d} | train_loss={tr_loss:.4f} acc={tr_acc:.4f} | valid_loss={va_loss:.4f} acc={va_acc:.4f}")
 if va_acc > best_val_acc:
 best_val_acc = va_acc
 best_state = {k: v.detach().cpu().clone() for k, v in model.state_dict().items()}

if best_state is not None:
 model.load_state_dict(best_state)

```

```

Epoch 01 | train_loss=0.6766 acc=0.5595 | valid_loss=0.6332 acc=0.6412
Epoch 02 | train_loss=0.6217 acc=0.6840 | valid_loss=0.6209 acc=0.6672
Epoch 03 | train_loss=0.6479 acc=0.6232 | valid_loss=0.6429 acc=0.6380
Epoch 04 | train_loss=0.5682 acc=0.7108 | valid_loss=0.5201 acc=0.7396
Epoch 05 | train_loss=0.4917 acc=0.7706 | valid_loss=0.5129 acc=0.7552
Epoch 06 | train_loss=0.5017 acc=0.7592 | valid_loss=0.4681 acc=0.7964
Epoch 07 | train_loss=0.4641 acc=0.7834 | valid_loss=0.4919 acc=0.7828
Epoch 08 | train_loss=0.4540 acc=0.7896 | valid_loss=0.4468 acc=0.8052
Epoch 09 | train_loss=0.4283 acc=0.8141 | valid_loss=0.4423 acc=0.8060
Epoch 10 | train_loss=0.3534 acc=0.8544 | valid_loss=0.4261 acc=0.8096
Epoch 11 | train_loss=0.3267 acc=0.8695 | valid_loss=0.4059 acc=0.8320
Epoch 12 | train_loss=0.2984 acc=0.8837 | valid_loss=0.4137 acc=0.8268
Epoch 13 | train_loss=0.2879 acc=0.8904 | valid_loss=0.4037 acc=0.8296
Epoch 14 | train_loss=0.2768 acc=0.8947 | valid_loss=0.5504 acc=0.7836
Epoch 15 | train_loss=0.3201 acc=0.8686 | valid_loss=0.4482 acc=0.8112
Epoch 16 | train_loss=0.2597 acc=0.9013 | valid_loss=0.4590 acc=0.8104
Epoch 17 | train_loss=0.2457 acc=0.9081 | valid_loss=0.4090 acc=0.8428
Epoch 18 | train_loss=0.2438 acc=0.9069 | valid_loss=0.4154 acc=0.8420
Epoch 19 | train_loss=0.2056 acc=0.9264 | valid_loss=0.4127 acc=0.8388
Epoch 20 | train_loss=0.1937 acc=0.9315 | valid_loss=0.4244 acc=0.8440

```

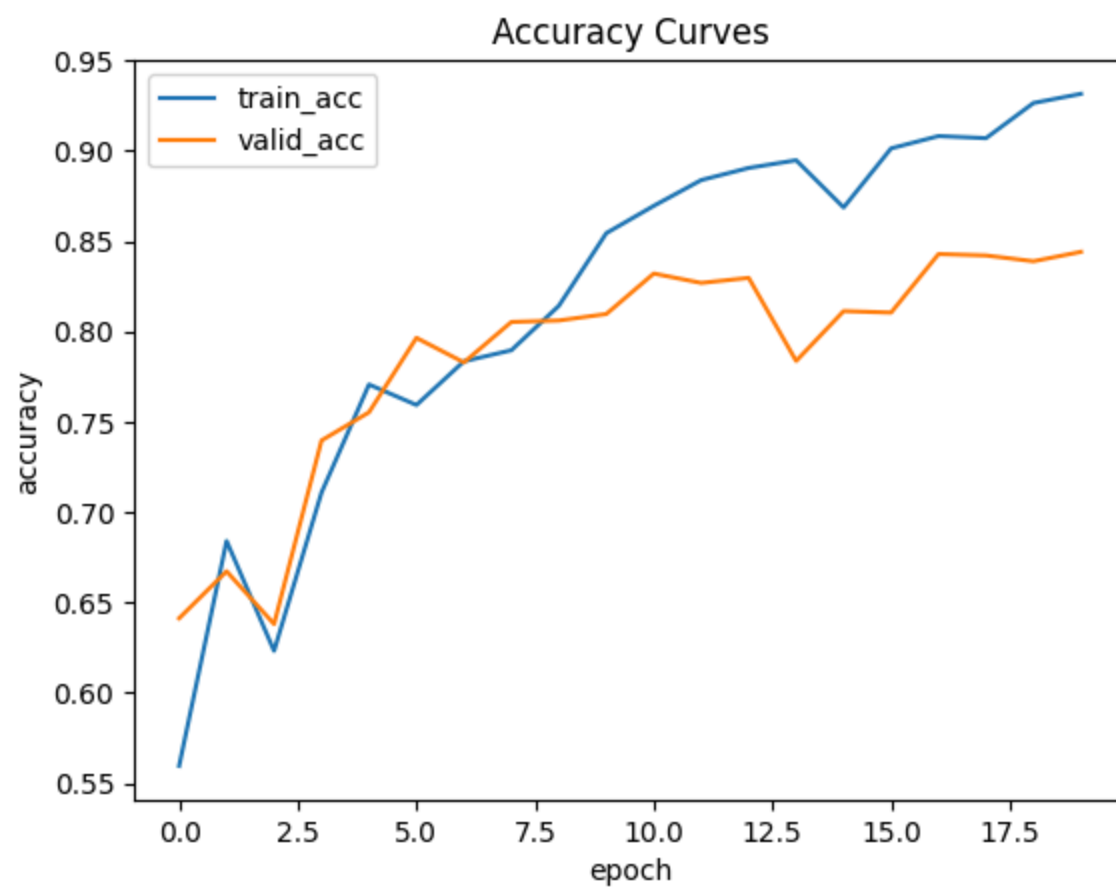
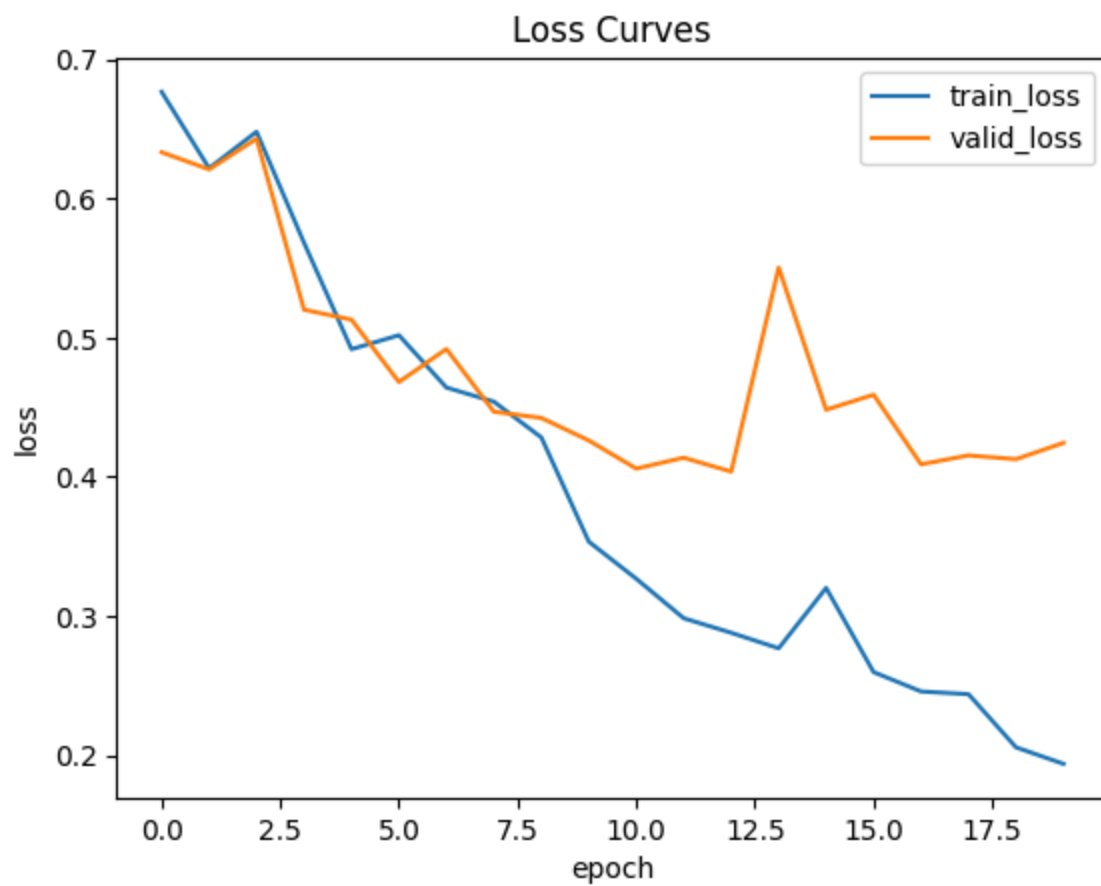
In [ ]: `import matplotlib.pyplot as plt`

```

plt.figure()
plt.plot(history["train_loss"], label="train_loss")
plt.plot(history["valid_loss"], label="valid_loss")
plt.xlabel("epoch"); plt.ylabel("loss"); plt.legend(); plt.title("Loss Curves")
plt.show()

plt.figure()
plt.plot(history["train_acc"], label="train_acc")
plt.plot(history["valid_acc"], label="valid_acc")
plt.xlabel("epoch"); plt.ylabel("accuracy"); plt.legend(); plt.title("Accuracy Curves")
plt.show()

```

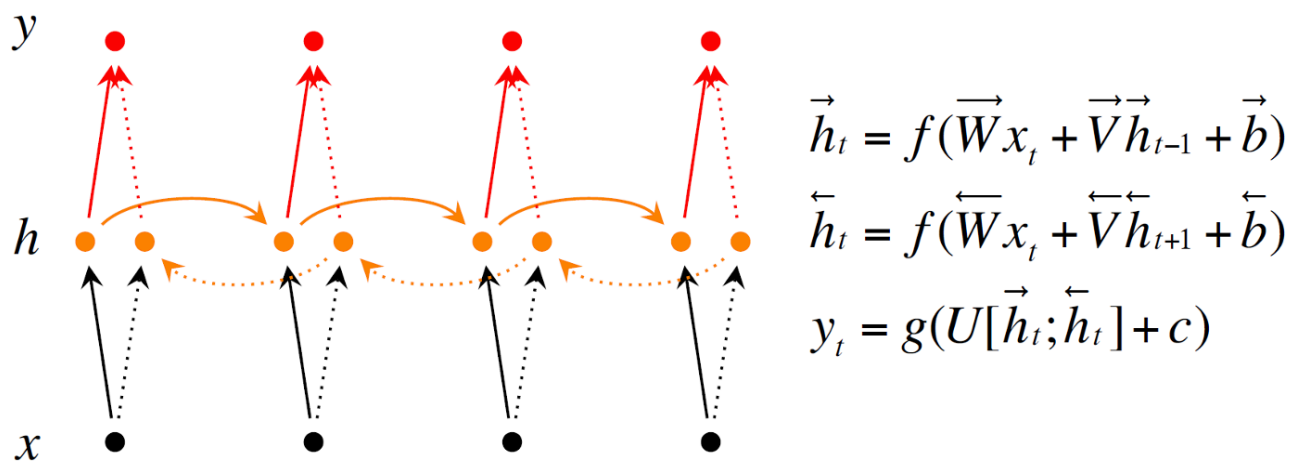


- **Exercise:** implement RNN or LSTM + mean pooling over timesteps + Linear

## Bidirectional RNNs



- A standard RNN (or an LSTM/GRU) processes a sequence chronologically, from the first token to the last. This is called a unidirectional model.
- The hidden state at any time step  $t(h_t)$  only contains information about the inputs from the past  $(x_1, \dots, x_t)$ . It has no knowledge of what is coming next in the sequence.
- Consider "The apple pie was delicious."
  - To correctly understand that "apple" refers to a food item (and not the company), it is helpful to know that the next word is "pie". A standard RNN making a decision at the word "apple" does not have this future context.
- A Bidirectional RNN solves this problem by processing the sequences in two directions at once:
  - A Forward RNN: from left to right
  - A Backward RNN: from right to left



In [109...

```
import torch
import torch.nn as nn

class BiLSTMSentiment(nn.Module):
 def __init__(self, vocab_size, embed_dim=100, hidden_size=128, num_layers=1, pad_idx=0, dropout=0.0):
 super().__init__()
 self.embedding = nn.Embedding(vocab_size, embed_dim, padding_idx=pad_idx)
 self.lstm = nn.LSTM(
 input_size=embed_dim,
 hidden_size=hidden_size,
 num_layers=num_layers,
 batch_first=True,
 bidirectional=True, # <- bidirectional LSTM
 dropout=0.0 if num_layers == 1 else dropout
)
 # Concatenate forward/backward last hidden → 2*hidden_size
 self.head = nn.Sequential(
 nn.Dropout(dropout),
 nn.Linear(2 * hidden_size, 1) # binary Logit
)

 def forward(self, x):
 # x: (B, T) with PAD indices
 emb = self.embedding(x) # (B, T, E)
```

```

Pack to ignore PAD steps in the LSTM
pad_idx = self.embedding.padding_idx if self.embedding.padding_idx is not None else 0
lengths = (x != pad_idx).sum(dim=1).cpu() # (B,)
packed = nn.utils.rnn.pack_padded_sequence(emb, lengths, batch_first=True, enforce_sorted=False)

packed_out, (h_n, c_n) = self.lstm(packed)
h_n: (num_layers*2, B, H). Take Last Layer's forward/backward: [-2], [-1]
last_fwd = h_n[-2] # (B, H)
last_bwd = h_n[-1] # (B, H)
feat = torch.cat([last_fwd, last_bwd], dim=1) # (B, 2H)

logits = self.head(feat).squeeze(1) # (B,)
return logits

```

In [111...

```

model = BiLSTMSentiment(
 vocab_size=len(stoi),
 embed_dim=64,
 hidden_size=32,
 num_layers=1,
 pad_idx=PAD_IDX,
 dropout=0.2
).to(DEVICE)

print(model)

criterion = nn.BCEWithLogitsLoss()
optimizer = optim.Adam(model.parameters(), lr=1e-3)

EPOCHS = 20
history = {"train_loss": [], "train_acc": [], "valid_loss": [], "valid_acc": []}
best_val_acc, best_state = 0.0, None

for epoch in range(1, EPOCHS + 1):
 tr_loss, tr_acc = run_epoch(train_loader, model, criterion, optimizer)
 va_loss, va_acc = run_epoch(valid_loader, model, criterion, optimizer=None)

 history["train_loss"].append(tr_loss)
 history["train_acc"].append(tr_acc)
 history["valid_loss"].append(va_loss)
 history["valid_acc"].append(va_acc)

 print(f"Epoch {epoch:02d} | train_loss={tr_loss:.4f} acc={tr_acc:.4f} | valid_loss={va_loss:.4f} acc={va_acc:.4f}")
 if va_acc > best_val_acc:
 best_val_acc = va_acc
 best_state = {k: v.detach().cpu().clone() for k, v in model.state_dict().items()}

if best_state is not None:
 model.load_state_dict(best_state)

```

```

BiLSTMSentiment(
 (embedding): Embedding(10000, 64, padding_idx=1)
 (lstm): LSTM(64, 32, batch_first=True, bidirectional=True)
 (head): Sequential(
 (0): Dropout(p=0.2, inplace=False)
 (1): Linear(in_features=64, out_features=1, bias=True)
)
)
Epoch 01 | train_loss=0.6784 acc=0.5624 | valid_loss=0.6283 acc=0.6516
Epoch 02 | train_loss=0.5455 acc=0.7248 | valid_loss=0.4817 acc=0.7752
Epoch 03 | train_loss=0.4203 acc=0.8113 | valid_loss=0.3994 acc=0.8224
Epoch 04 | train_loss=0.3604 acc=0.8466 | valid_loss=0.3934 acc=0.8324
Epoch 05 | train_loss=0.2980 acc=0.8791 | valid_loss=0.3613 acc=0.8468
Epoch 06 | train_loss=0.2554 acc=0.8995 | valid_loss=0.3454 acc=0.8576
Epoch 07 | train_loss=0.2254 acc=0.9129 | valid_loss=0.3518 acc=0.8608
Epoch 08 | train_loss=0.1910 acc=0.9275 | valid_loss=0.3612 acc=0.8632
Epoch 09 | train_loss=0.1662 acc=0.9377 | valid_loss=0.3526 acc=0.8508
Epoch 10 | train_loss=0.1444 acc=0.9472 | valid_loss=0.3575 acc=0.8560
Epoch 11 | train_loss=0.1189 acc=0.9580 | valid_loss=0.3841 acc=0.8584
Epoch 12 | train_loss=0.1060 acc=0.9623 | valid_loss=0.3926 acc=0.8584
Epoch 13 | train_loss=0.0850 acc=0.9714 | valid_loss=0.4128 acc=0.8664
Epoch 14 | train_loss=0.1269 acc=0.9538 | valid_loss=0.4401 acc=0.8472
Epoch 15 | train_loss=0.0778 acc=0.9752 | valid_loss=0.4826 acc=0.8644
Epoch 16 | train_loss=0.0540 acc=0.9844 | valid_loss=0.4786 acc=0.8596
Epoch 17 | train_loss=0.0497 acc=0.9853 | valid_loss=0.4757 acc=0.8556
Epoch 18 | train_loss=0.0401 acc=0.9891 | valid_loss=0.5452 acc=0.8624
Epoch 19 | train_loss=0.0282 acc=0.9938 | valid_loss=0.5906 acc=0.8616
Epoch 20 | train_loss=0.0490 acc=0.9838 | valid_loss=0.5361 acc=0.8568

```

In [112...

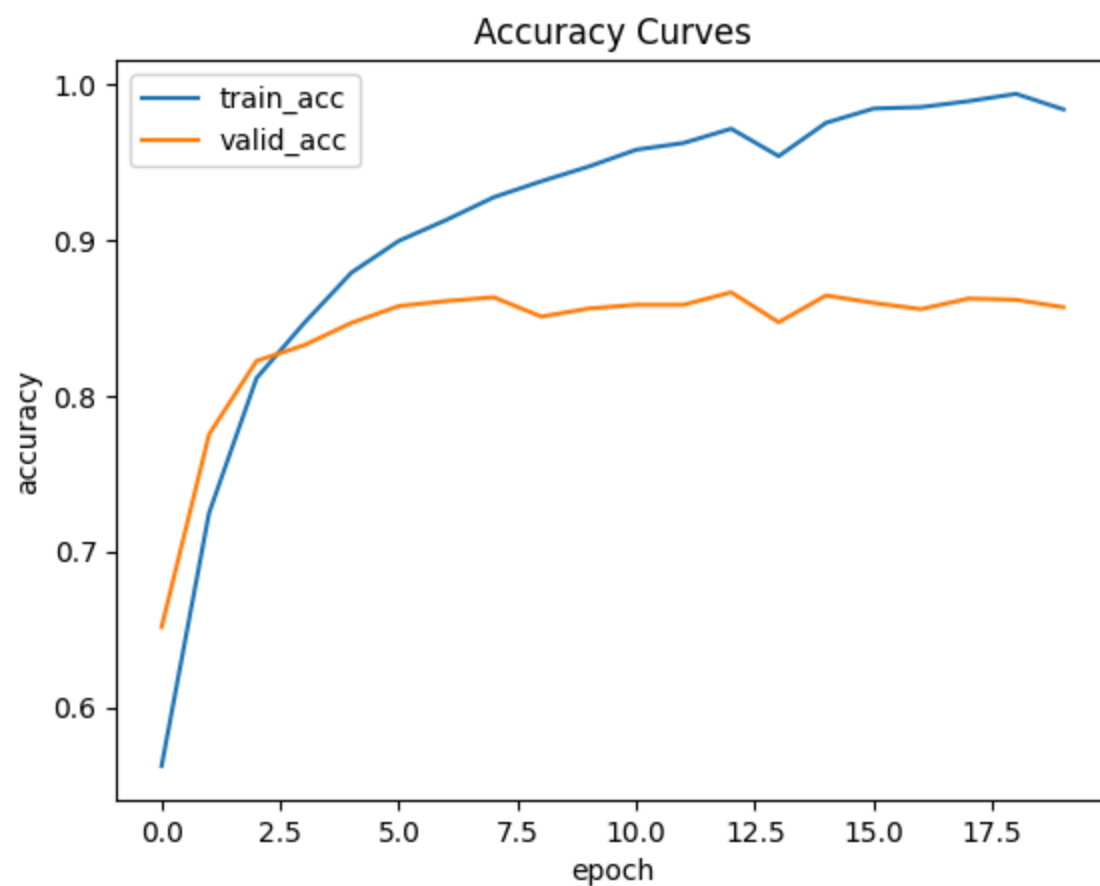
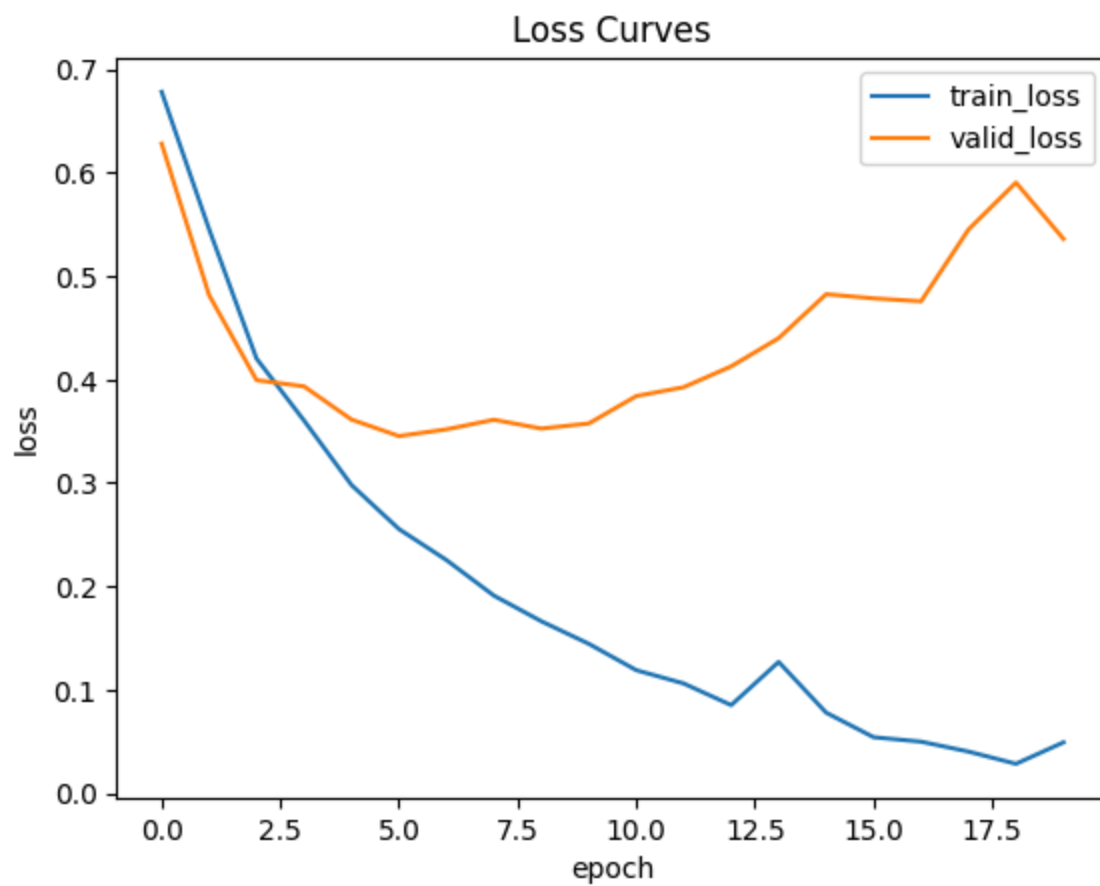
```

import matplotlib.pyplot as plt

plt.figure()
plt.plot(history["train_loss"], label="train_loss")
plt.plot(history["valid_loss"], label="valid_loss")
plt.xlabel("epoch"); plt.ylabel("loss"); plt.legend(); plt.title("Loss Curves")
plt.show()

plt.figure()
plt.plot(history["train_acc"], label="train_acc")
plt.plot(history["valid_acc"], label="valid_acc")
plt.xlabel("epoch"); plt.ylabel("accuracy"); plt.legend(); plt.title("Accuracy Curves")
plt.show()

```




## 6.4 Sequence processing with convnets

- For sequence processing, time can be treated as a spatial dimension like the height or width of a 2D image.

- 1D convnets can be competitive with RNNs on certain sequence processing tasks.
  - It has cheaper computational cost.

## Understanding 1D convolution for sequence data

- We can use 1D convolutions, extracting local 1D patches (subsequences) from sequences.

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- Such 1D convolution layers can recognize local patterns in a sequence.

## 1D pooling for sequence data

- Similar to 2D pooling operations: 2D average/max pooling
- It extracts 1D patches (subsequences) from an input and outputting the maximum value (max pooling) or average value (average pooling).
- It is used for reducing the length of 1D inputs (subsampling).

## Implementing a 1D convnet

```
In []: import torch
import torch.nn as nn
import torch.optim as optim

--- Conv1D Sentiment Model ---
class SentimentCNN(nn.Module):
 def __init__(self, vocab_size, embed_dim=128, pad_idx=0):
 super().__init__()
 self.embedding = nn.Embedding(vocab_size, embed_dim, padding_idx=pad_idx)

 self.conv_block = nn.Sequential(
 nn.Conv1d(in_channels=embed_dim, out_channels=32, kernel_size=7),
 nn.ReLU(),
 nn.MaxPool1d(kernel_size=5),
 nn.Conv1d(in_channels=32, out_channels=32, kernel_size=7),
 nn.ReLU()
)

 # Global max pooling over time
 self.global_max_pool = nn.AdaptiveMaxPool1d(1)

 # Fully connected output layer
 self.fc = nn.Linear(32, 1)

 def forward(self, x):
 # x: (B, T)
 emb = self.embedding(x) # (B, T, E)
 emb = emb.transpose(1, 2) # (B, E, T) → required by Conv1d

 features = self.conv_block(emb) # (B, 32, L)
```

```

 pooled = self.global_max_pool(features).squeeze(-1) # (B, 32)
 logits = self.fc(pooled).squeeze(1) # (B,)
 return logits

--- Model initialization ---
model = SentimentCNN(vocab_size=len(stoi), embed_dim=128, pad_idx=PAD_IDX).to(DEVICE)
print(model)

```

```

SentimentCNN(
 (embedding): Embedding(10000, 128, padding_idx=1)
 (conv_block): Sequential(
 (0): Conv1d(128, 32, kernel_size=(7,), stride=(1,))
 (1): ReLU()
 (2): MaxPool1d(kernel_size=5, stride=5, padding=0, dilation=1, ceil_mode=False)
 (3): Conv1d(32, 32, kernel_size=(7,), stride=(1,))
 (4): ReLU()
)
 (global_max_pool): AdaptiveMaxPool1d(output_size=1)
 (fc): Linear(in_features=32, out_features=1, bias=True)
)

```

```

In []: # criterion = nn.BCEWithLogitsLoss()
optimizer = optim.RMSprop(model.parameters(), lr=1e-4)

criterion = nn.BCEWithLogitsLoss()
optimizer = optim.Adam(model.parameters(), lr=1e-3)

EPOCHS = 10
history = {"train_loss": [], "train_acc": [], "valid_loss": [], "valid_acc": []}
best_val_acc, best_state = 0.0, None

for epoch in range(1, EPOCHS + 1):
 tr_loss, tr_acc = run_epoch(train_loader, model, criterion, optimizer)
 va_loss, va_acc = run_epoch(valid_loader, model, criterion, optimizer=None)

 history["train_loss"].append(tr_loss)
 history["train_acc"].append(tr_acc)
 history["valid_loss"].append(va_loss)
 history["valid_acc"].append(va_acc)

 print(f"[CNN] Epoch {epoch:02d} | "
 f"train_loss={tr_loss:.4f} acc={tr_acc:.4f} | "
 f"valid_loss={va_loss:.4f} acc={va_acc:.4f}")

 if va_acc > best_val_acc:
 best_val_acc = va_acc
 best_state = {k: v.detach().cpu().clone() for k, v in model.state_dict().items()}

Load best weights
if best_state is not None:
 model.load_state_dict(best_state)
 print(f"Loaded best CNN model (val_acc={best_val_acc:.4f}).")

Evaluate on test set
test_loss, test_acc = run_epoch(test_loader, model, criterion, optimizer=None)
print("=" * 60)
print(f"[CNN] Test Loss: {test_loss:.4f} | Test Accuracy: {test_acc:.4f}")
print("=" * 60)

```

```

[CNN] Epoch 01 | train_loss=0.6301 acc=0.6212 | valid_loss=0.4997 acc=0.7588
[CNN] Epoch 02 | train_loss=0.4041 acc=0.8181 | valid_loss=0.3944 acc=0.8244
[CNN] Epoch 03 | train_loss=0.2785 acc=0.8861 | valid_loss=0.3615 acc=0.8372
[CNN] Epoch 04 | train_loss=0.1908 acc=0.9282 | valid_loss=0.3740 acc=0.8476
[CNN] Epoch 05 | train_loss=0.1231 acc=0.9605 | valid_loss=0.4028 acc=0.8556
[CNN] Epoch 06 | train_loss=0.0700 acc=0.9822 | valid_loss=0.4521 acc=0.8516
[CNN] Epoch 07 | train_loss=0.0340 acc=0.9945 | valid_loss=0.5002 acc=0.8548
[CNN] Epoch 08 | train_loss=0.0148 acc=0.9992 | valid_loss=0.5521 acc=0.8580
[CNN] Epoch 09 | train_loss=0.0063 acc=0.9999 | valid_loss=0.6019 acc=0.8572
[CNN] Epoch 10 | train_loss=0.0031 acc=1.0000 | valid_loss=0.6410 acc=0.8556
Loaded best CNN model (val_acc=0.8580).
=====
[CNN] Test Loss: 0.5811 | Test Accuracy: 0.8463
=====

```

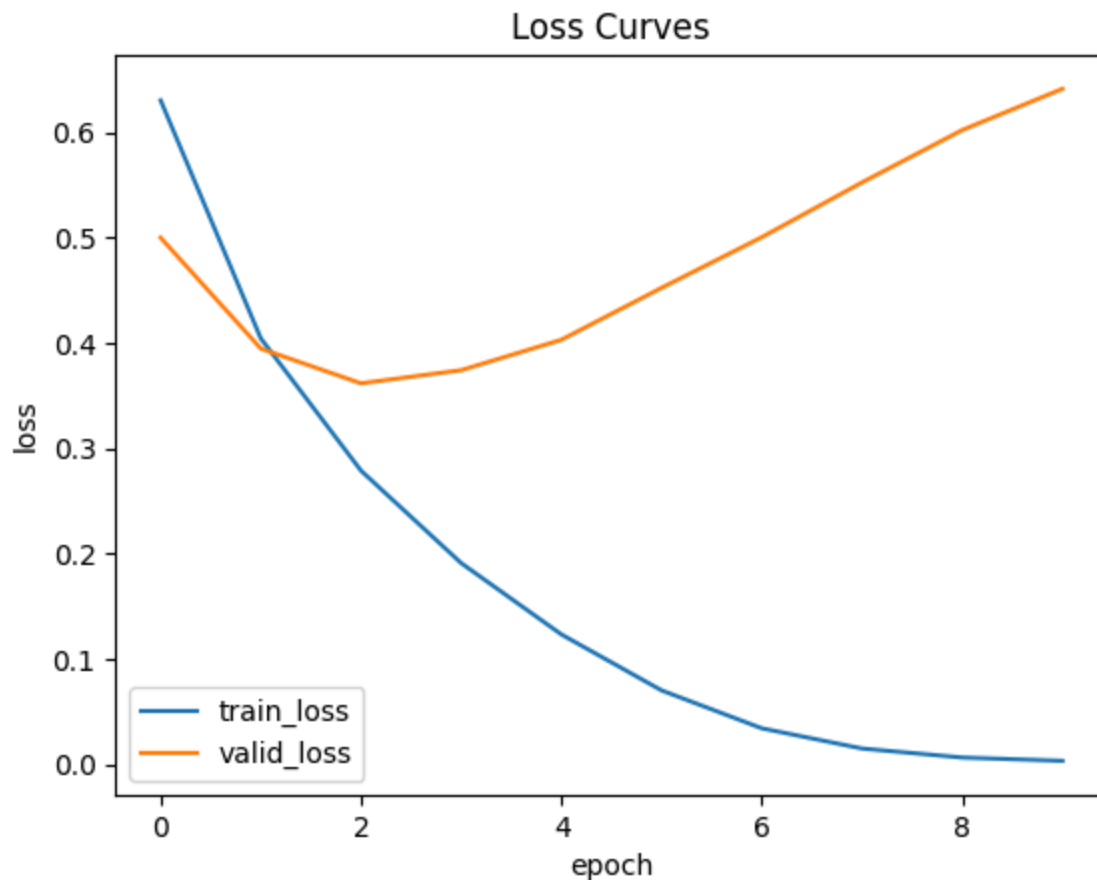
```
In []: import matplotlib.pyplot as plt
```

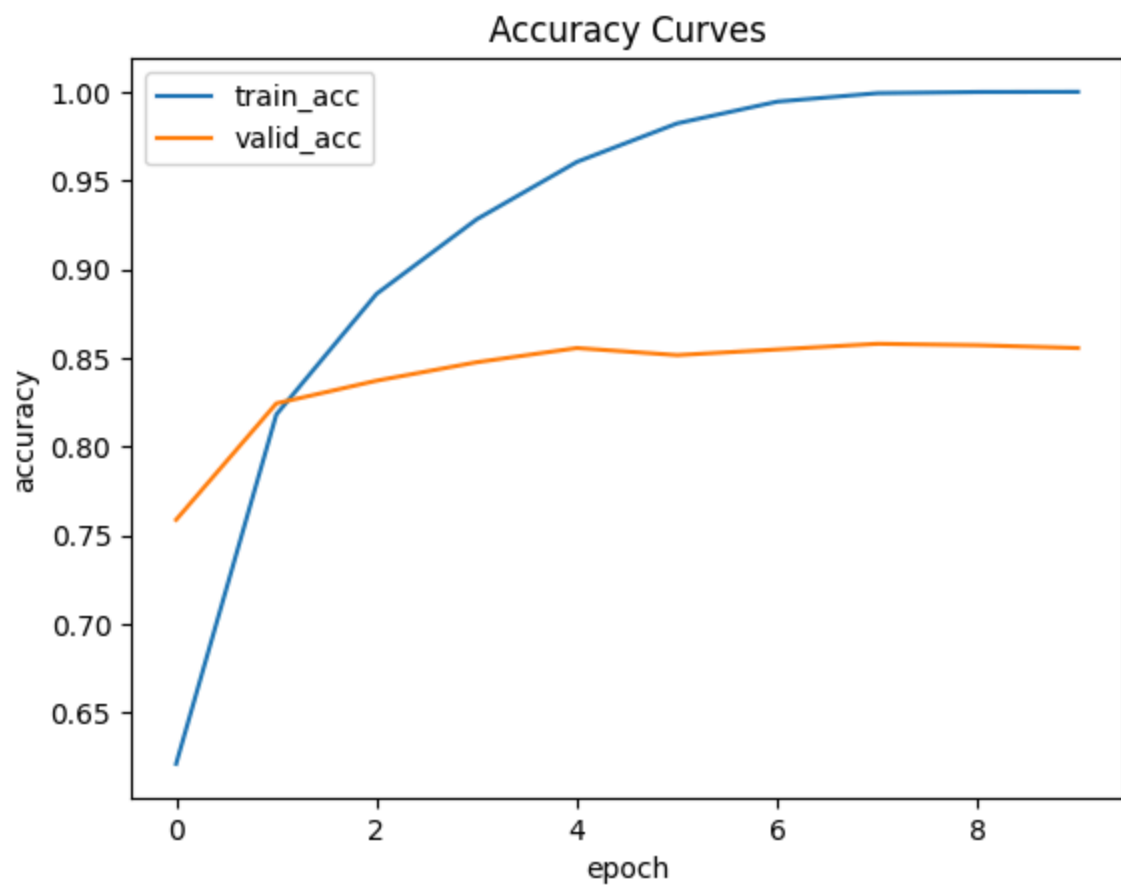
```

plt.figure()
plt.plot(history["train_loss"], label="train_loss")
plt.plot(history["valid_loss"], label="valid_loss")
plt.xlabel("epoch"); plt.ylabel("loss"); plt.legend(); plt.title("Loss Curves")
plt.show()

plt.figure()
plt.plot(history["train_acc"], label="train_acc")
plt.plot(history["valid_acc"], label="valid_acc")
plt.xlabel("epoch"); plt.ylabel("accuracy"); plt.legend(); plt.title("Accuracy Curves")
plt.show()

```





In [ ]: