

# CHAPTER NINE

## SET

### **The number system:**

Our number system can be divided into the following groups of set:

1. The set of integers, i.e  $\{\dots -3, -2, -1, 0, 1, 2, 3, 4 \dots\}$   
Integers are positive and negative whole numbers.
2. The set of whole numbers ie  $\{0, 1, 2, 3, 4 \dots\dots\dots\}$   
Whole numbers are numbers from zero upwards.
3. The set of natural or counting numbers i.e  
 $\{1, 2, 3, 4 \dots\}$   
These are numbers from 1 upwards
4. The set of odd numbers ie.  $\{1, 3, 5, 7, 9 \dots\dots\dots\}$   
These are numbers which when divide by 2, always give us a remainder, but 1 is an odd number.
5. The set of prime numbers ie  $\{2, 3, 5, 7, 11, 13, 17, \dots\}$   
Prime numbers are numbers which have only two factors, for example  $7 = 1 \times 7$  i.e has only two factors which are 1 and 7.  
Also  $3 = 1 \times 3$  ie has only two factors ie 1 and 3.  
But 9 is not a prime number since it has four factors which are 3 and 3, as well as 1 and 9. i.e  $9 = 1 \times 9$  and  $9 = 3 \times 3$ .
6. The set of composite numbers ie  $\{4, 6, 8, 9, 10 \dots\dots\}$   
These are numbers which have more than two factors. For example the factors of 4 are 1 and 4, as well as 2 and 2 i.e  $4 = 1 \times 4$  and  $4 = 2 \times 2$ .
7. The set of even numbers i.e  $\{2, 4, 6, 8, 10, 12 \dots\dots\}$   
These are numbers which can be divided by 2 without any a remainder.

### **Factors of a given number:**

These are whole numbers which can divide that given number without any remainder, with the given number being the highest factor. Examples are

1. The factors of  $6 = 1, 2, 3, 6$
2. The factors of  $8 = 1, 2, 4, 8$

3. The factors of  $30 = 1, 2, 3, 5, 6, 15, 30$ .

**Multiple of a given number:**

If  $y$  is our number, then the multiples of  $y = 1 \times y, 2 \times y, 3 \times y, 4 \times y, \dots$   
 $= y, 2y, 3y, 4y, \dots$

For example: The multiples of  $2 = 1 \times 2, 2 \times 2, 3 \times 2, 4 \times 2 = 2, 4, 6, 8, \dots$

Also the multiples of  $5 = 1 \times 5, 2 \times 5, 3 \times 5, 4 \times 5, \dots = 5, 10, 15, 20, \dots$

Q1. Find the set of natural numbers from 1 to 12.

Soln.

The set of natural numbers from 1 to 12  $= \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$  or  $\{1, 2, 3, \dots, 12\}$ .

Q2. Find the set of the even natural numbers from 1 to 12

Soln.

We first find the set of natural numbers from 1 to 12 ie.

$\{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$

We then select the even numbers among them. *Therefore* { natural even numbers from 1 to 12 }  $= \{2, 4, 6, 8, 10, \text{ and } 12\}$ .

Q3. Determine the set of the multiples of 3, which are less than 15.

Soln.

The multiples of 3 less than 15  $= \{3, 6, 9, 12\}$ .

Q4. Find the set of the odd multiples of 3 up to 18.

Soln.

The multiples of 3 up to 18  $= \{3, 6, 9, 12, 15, 18\}$ .

Selecting the odd ones among them  $\Rightarrow \{\text{Odd multiples of 3 up to 18}\} = \{3, 9, 15\}$ .

Q5. Find the set of the prime factors of 6.

Soln.

$\{\text{Factors of 6}\} = \{1, 2, 3, 6\}.$

Selecting only the prime numbers among them

$\Rightarrow \{\text{Prime factors of 6}\} = \{2, 3\}.$

Q6. Find the set of the even whole numbers from 10 to 15.

Soln.

$\{\text{whole numbers from 10 to 15}\} = \{10, 11, 12, 13, 14, 15\}$

Selecting the even numbers among them  $\Rightarrow \{\text{even whole numbers from 10 to 15}\}$   
 $= \{10, 12, 14\}.$

Q7. Find the set of the odd whole numbers from 5 to 10

Soln.

$\{\text{whole numbers from 5 to 10}\} = \{5, 6, 7, 8, 9, 10\}.$

Selecting the odd ones among them  $\Rightarrow \{\text{odd whole numbers from 5 to 10}\} = \{5, 7, 9\}.$

Q8. Find the set of all the composite numbers from 3 to 12.

Soln.

$\{\text{Composite numbers from 3 to 12}\} = \{4, 6, 8, 9, 10, 12\}.$

Q9. Find the set of the odd prime numbers from 1 to 6

Soln.

$\{\text{Prime numbers from 1 to 6}\} = \{2, 3, 5\}.$

Selecting the odd numbers among them  $\Rightarrow$  odd prime numbers from 1 to 6  $= \{3, 5\}$ .

Q10. Find the set of composite odd numbers from 5 to 12.

Soln.

$\{\text{Odd numbers from 5 to 12}\} = \{5, 7, 9, 11\}$ .

Selecting the composite ones among them  $\Rightarrow$  *the*  $\{\text{composite odd numbers from 5 to 12}\} = \{9\}$ .