CHAPTER SIX

GRAPHS:

Some basic graphs:

Before a graph can be plotted, we must first construct a table with reference to the equation of the given graph.

- A few values of x are selected and for each, the corresponding y value is computed.
- These two corresponding values i.e. the x and the y values are then plotted on a graph paper.
- There are certain basic graphs which students must be familiar with and be capable of plotting.
- The way or manner of plotting some of these graphs will be illustrated in the following questions:
- Q1). Using values of x from -2 to 2, plot the following graphs:

1)
$$y = 2x$$
.

2).
$$y + 4x = 0$$
.

3).
$$y = \frac{1x}{2}$$
.

4)
$$y = -x/2$$
.

5)
$$y = 2x + 1$$
.

6)
$$y + 4x + 2 = 0$$
.

Soln.

(1)

$$y = 2x$$

X	- 2	- 1	0	1	2
Y	- 4	- 2	0	2	4

(a) If
$$x = -2$$

$$y = 2x$$

$$=>y=2(-2)=-4$$

$$=>y = -4$$

(b) If
$$x = -1$$

$$y = 2x$$

$$=> y = 2 (-1)$$

$$=> y = -2$$

$$\bigcirc$$
 If $x = 0$

(d) If
$$x = 1$$

$$y = 2x$$

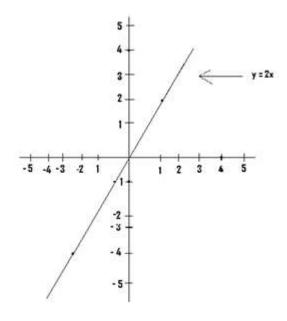
=> $y = 2(0) = 0$
=> $y = 0$

$$y = 2x$$

=> $y = 2(1) = 2$
=> $y = 2$

(e) If
$$x = 2$$

 $y = 2x$
=> $y = 2(2)$
=> $y = 4$



N/B: Before plotting any graph you, must first make sure y is the subject of the given equation. If not, then make y the subject.

(2) From
$$y + 4x = 0$$
, => $y = 0-4x$ => $y = -4x$

$$y = -4x$$

X	-2	-1	0	1	2
Y	8	4	0	s- 4	-8

(a) If
$$x = -2$$

 $y = -4x$
 $=> y = -4 (-2)$
 $=> y = 8$

(b) If
$$x = -1$$

=> $y = -4(-1)$
=> $y = 4$

(c) If
$$x = 0$$

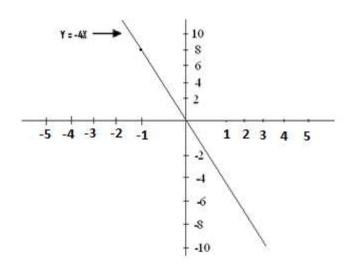
 $y = -4x$
 $\Rightarrow y = -4(0)$
 $\Rightarrow y = 0$

(d) If
$$x = 1$$

 $y = -4x$
 $\Rightarrow y = -4(1) = -4$
 $\Rightarrow y = -4$

(e) If
$$x = 2$$

 $y = -4x$
 $\Rightarrow y = -4(2) = -8$
 $\Rightarrow y = -8$



1.
$$y = \frac{1x}{2} \{ \text{ or } y = x/2 \}$$

3) $y = \frac{x}{2} \text{ or } y = \frac{1x}{2}$ $y = -1 \qquad 0 \qquad 1 \qquad 2$ $y = -1 \qquad -0.5 \qquad 0 \qquad 0.5 \qquad 1$

(a) If
$$x = -2$$

 $y = \frac{1x}{2} = \frac{1}{2}(-2)$

(b) If
$$x = -1$$

 $y = \frac{1x}{2} = \frac{1}{2}(-1)$

$$=> y = -2/2$$

. $=> y = -1$

$$=> y = -1/2 = -0.5$$

 $=> y = -0.5$

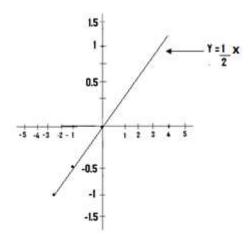
(c) If
$$x = 0$$

 $y = \frac{1x}{2} = \frac{1}{2}(0)$
=> $y = 0/2$
=> $y = 0$

(d) If
$$x = 1$$

 $y = \frac{1x}{2} = \frac{1}{2}(1)$
=> $y = \frac{1}{2}$
=> $y = 0.5$

X	-2	-1	0	1	2
Y	1	0.5	0	- 0.5	-1



N/B: In the plotting of a graph, the interval used on one particular axis (i.e. the difference between one number and the next) must be the same.

- For a particular graph, the interval used on the x-axis must be the same.
- But the scale used on the x-axis can be different from that used on the y-axis.

4)
$$y = -x/2$$
. or $y = \frac{-x}{2}$

1) If
$$x = -2$$

2) If
$$x = -1$$

$$y = -x/2 = -(-2)/2$$

$$y = -x/2 = -(-1)/2$$

$$\rightarrow$$
 y = $2/2 = 1$

$$=> y = \frac{1}{2} = 0.5$$

3) If
$$x = 0$$

$$y = -x/2 = -(0)/2 = 0$$

$$=> y = 0.$$

4) If
$$x = 1$$

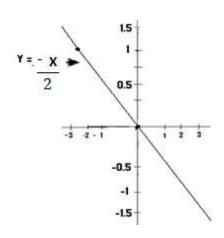
$$y = -x/2 = -(1)/2$$

$$=> y = -1/2 = -0.5$$

5) If
$$x = 2$$

$$y = -x/2 = -(2)/2$$

$$=> y = -1$$



5)

$$y = 2x + 1$$

X	-2	-1	0	1	2
Y	-3	-1	1	3	5

1) If
$$x = -2$$

$$y = 2x + 1$$

$$=> y = 2(-2) + 1$$

$$\Rightarrow$$
 y = -4 + 1 = -3.

2) If
$$x = -1$$

$$y = 2x + 1$$

$$=> y = 2(-1) + 1 = -2 + 1$$

$$=> y = -1.$$

3) If
$$x = 0$$

4) If
$$x = 1$$

$$y = 2x + 1$$

$$=> y = 2(0) + 1$$

$$=> y = 0+1 = 1.$$

$$y = 2x + 1$$

$$\Rightarrow$$
 y = 2(1) + 1 = 2 + 1 = 3

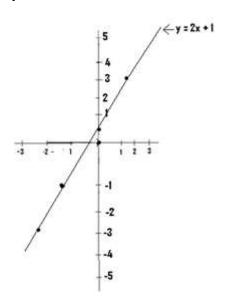
$$=> y = 3.$$

5) If
$$x = 2$$

$$y = 2x + 1$$

$$=> y = 2(2) + 1$$

$$=> y = 5.$$



6) From
$$y + 4x + 2 = 0$$

$$=> y + 2 = 0 - 4x$$

$$=> y + 2 = -4x$$

$$=> y = -4x - 2$$

$$y = -4x - 2$$

X	-2	-1	0	1	2
Y	6	2	-2	- 6	-10

a) If
$$x = -2$$

b) If
$$x = -1$$

$$y = -4x-2$$

$$y = -4x - 2$$

$$=> y = -4(-2)-2$$

$$=> y = -4(-1) -2$$

$$=> y = 8 - 2$$

$$=> y = 4 - 2$$

$$=> y = 6$$

$$=> y = 2$$

c) If
$$x = 0$$

d) If
$$x = 1$$

If
$$x = 2$$

$$y = -4x - 2$$

$$v = -4x - 2$$

$$y = -4x - 2$$
 $y = -4x - 2$

$$=> y = -4(0) -2$$

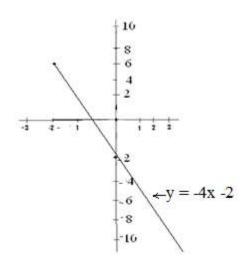
$$=> v = -4(1) - 2$$

$$=> y = -4(0) -2$$
 $=> y = -4(1) -2$ $=> y = -4(2) -2 = .$

$$==> y = 0 - 2 = -2.$$
 $=> y = -4 - 2 = -6.$ $-8 - 2 = -10.$

$$=> v = -4 - 2 = -6$$

$$-8-2=-10$$
.



Q2) Using values of x from -3 to 3, plot the graphs of the relations: a) $y = x^2$.

b)
$$y = -x^2$$

c)
$$y = 2x^2$$

d)
$$y + 2x^2 = 0$$

e)
$$y = \frac{1}{2}x^2$$

Soln

a)
$$y = x^2$$

$$y = x^2$$

X	-3	-2	-1	0	1	2	3
Y	9	4	1	0	1	4	9

(1) If
$$x = -3$$

2) If
$$x = -2$$

$$y = x^2$$

$$=> y = (-3)^2 = 9.$$

$$=> y = 9.$$

$$y = x^2$$

$$=> y = (-2)^2 = 4.$$

$$=>y=4.$$

3) If
$$x = -1$$

$$y = x^2$$

$$=> y = (-1)^2 = 1$$

$$=> y = 1.$$

4) If
$$x = 0$$

$$y = x^2$$

$$=> y = (0)^2 = 0$$

$$=> y = 0$$

5) If
$$x = 1$$

$$y = x^2$$

$$=> y = (1)^2$$

6) If
$$x = 2$$

 $y = x^2$

$$=> y = (2)^2$$

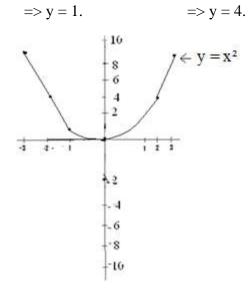
$$=> y = 4.$$

7) If
$$x = 3$$

$$y = x^2$$

$$=> y = (3)^2 = 9$$

$$=> y = 9.$$



b)

$$y = -x^2$$

X	-3	-2	-1	0	1	2	3
Y	-9	-4	-1	0	-1	- 4	-9

1) If
$$x = -3$$

$$y = -x^2$$

$$=> y = - (-3)^2$$

$$=> y = - (9)$$

$$=> y = -9$$

3) If
$$x = -1$$

$$y = -x^2$$

$$=> y = - (-1)^2$$

$$=> y = -(1)$$

$$=> y = -1.$$

5) If
$$x = 1$$

$$y = -x^2$$

$$=> y = -(1)^2$$

$$=> y = - (1)$$

$$=> y = -1.$$

7) If
$$x = 3s$$

$$y = -x^2$$

$$=> y = - (3)^2$$

$$=> y = - (9)$$

$$=> y = -9$$
.

2) If
$$x = -2$$

$$y = -x^2 = -(-2)^2$$

$$=> y = - (4) = - 4$$

$$=> y = -4.$$

4) If
$$x = 0$$

$$y = -x^2$$

$$=> y = -(0)^2$$

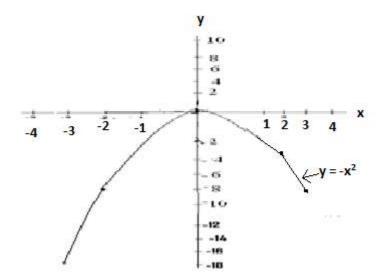
$$=> y = -(0) = 0.$$

6) If
$$x = 2$$

$$y = -x^2$$

$$\Rightarrow$$
 y = - (2)² = - (4)

$$=> y = -4.$$



c)

$$y = \frac{1}{2}x^2$$

X	-3	-2	-1	0	1	2	3
Y	4.5	2	0.5	0	0.5	2	4.5

1) If
$$x = -3$$

$$y = \frac{1}{2} x^2$$

$$=> y = \frac{1}{2}(-3)^2$$

$$=> y = \frac{1}{2} (9)$$

$$=> y = 9/2 = 4.5$$

2) If
$$x = -2$$

$$y = \frac{1}{2} x^2$$

$$=> y = \frac{1}{2} (-2)^2$$

$$=> y = \frac{1}{2}(4) = \frac{4}{2} = 2$$

3) If
$$x = -1$$

$$y = \frac{1}{2}x^2$$

$$=> y = \frac{1}{2}(-1)^2$$

$$=> y = \frac{1}{2}(1) = \frac{1}{2}$$

4) If
$$x = 0$$

$$y = \frac{1}{2}x^2$$

$$=> y = \frac{1}{2}(0)^2 = \frac{1}{2}(0)$$

$$=> y = 0$$

$$=> y = 0.5$$

5) If
$$x = 1$$

6) If x = 2

$$y = \frac{1}{2}(1)^2$$

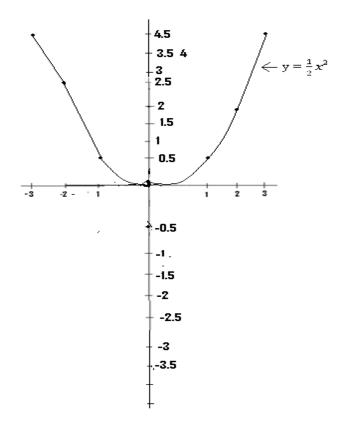
 $y = \frac{1}{2}(2)^2$

$$=> y = \frac{1}{2}(1) = \frac{1}{2}$$

 $=> y = \frac{1}{2}(4)$

$$=> y = 0.5$$

$$=> y = 4/2 = 2$$



(d) From
$$y + 2x^2 = 0 \Rightarrow y = 0-2x^2$$
,

$$=>y=-2x^2$$
.

$$y = -2x^2$$

X	-3	-2	-1	0	1	2	3
Y	-18	-8	-2	0	-2	-8	-18

1) If x = -3

2) If x = -

$$y = -2x^2$$

$$y = -2x^2$$

$$=> y = -2(-3)^2$$

$$\Rightarrow$$
 y = -2(-2)² = -2(4)

$$=> y = -2(9)$$

$$=> y = -8$$

$$=> y = -18.$$

3) If
$$x = -1$$

$$y = -2x^2$$

4) If
$$x = 0$$

$$=> y = -2(-1)^2$$

$$y = -2(0)^2 => y = -2(1)$$

$$\Rightarrow$$
 y = -2(1) = -2

$$=> y = -2$$

$$=> y = -2$$

5) If
$$x = 1$$

6) If
$$x = 2$$

$$y = -2(1)^2$$

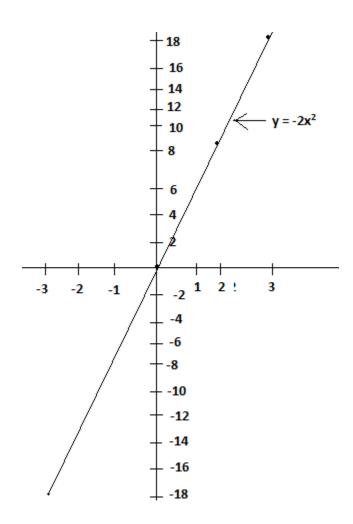
$$y = -2(2)^2$$

$$=> y = -2(1)$$

$$y = -2(4)$$

$$=> y = -2$$

$$y = -8$$



(Q3) Plot the graphs of the relations $y = \frac{2x}{3} - 1$ and $y = \frac{2x-1}{3}$ for $-3 \le x \le 3$.

Soln:

$$y = 2x/3$$

X	-3	-2	-1	0	1	2	3
Y	-3	-2.3	-1.7	-1	-0.34	0.3	1
(1)If x = -3	3	(2)If $x = -2$	(.	3) If $x = -1$	(4) If	x = 0	
$y = \frac{2x}{3} - 1$		$y = \frac{2x}{3} - 1$	У	$=\frac{2x}{3}-1$	$y = \frac{2x}{3}$	- 1	
$=> y = \frac{2(-1)^{3}}{3}$	3) – 1	$=> y = \frac{2(-2)}{3}$	−1 => y	$=\frac{2(-1)}{3}-1$	=> y =	$\frac{2(0)}{3}$ – 1	
$=> y = \frac{-6}{3}$	- 1	$=> y = \frac{-4}{3}$	- 1 =>	$y = \frac{-2}{3} - 1$	=> y =	$=\frac{0}{3}-1$	
=> y = -2 -	-1 = -3	=> y = -1.3	3 – 1 =>	y = -0.66	- 1 => y	= 0 - 1	
=>=-3		=> y = -2.3	=>	y = -1.7	=> y	= -1	
(5) If $x = 1$		(6)If $x = 2$	(7)	If $x = 3$			

$$y = \frac{2x}{3} - 1$$

$$y = \frac{2x}{3} - \frac{1}{3}$$

$$y = \frac{2x}{3} - 1$$
 $y = \frac{2x}{3} - 1$ $y = \frac{2x}{3} - 1$

$$=> y = \frac{2(1)}{3} - 1$$

$$=> y = \frac{2(2)}{3}$$

$$=> y = \frac{2(1)}{3} - 1$$
 $=> y = \frac{2(2)}{3} - 1$ $=> y = \frac{2(3)}{3} - 1$

$$=> y = \frac{2}{3} - 1$$

$$=> y = \frac{4}{3} - 1$$

$$=> y = \frac{2}{3} - 1$$
 $=> y = \frac{4}{3} - 1$ $=> y = \frac{6}{3} - 1$

$$=> y = 0.66 - 1$$
 $=> y = 1.3 - 1$ $=> y = 2 - 1$

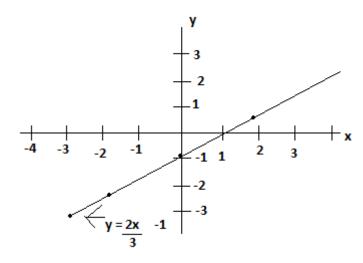
$$=> v = 1.3 - 1$$

$$=> y = 2 - 1$$

$$=> y = -0.34$$

$$=> y = 0.3$$
 $=> y = 1$

$$=> y = 1$$



$$y = \frac{2x-1}{3}$$

X	-3	-2	-1	0	1	2	3
Y	-2.3	-1.7	-1	-0.3	0.3	1	1.7

(1) If
$$x = -3$$

(2) If
$$x = -2$$
 (3) If $x = 0$

$$(3)$$
If $x = 0$

$$=> y = \frac{2(-3)-1}{3}$$

$$=> y = \frac{2(-2)-1}{2}$$

$$=> y = \frac{2(-2)-1}{3}$$
 $=> y = \frac{2(0)-1}{3}$

$$=> y = \frac{-6-1}{3}$$

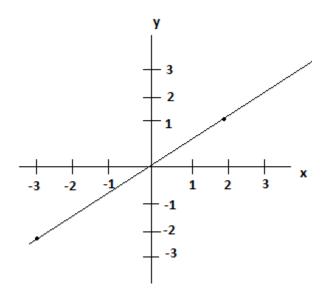
$$=> y = \frac{-4-1}{3}$$
 $=> y = \frac{0-1}{3}$

$$=> y = \frac{0-1}{2}$$

$$=> y = \frac{-7}{3} = -2.3$$

$$=> y = \frac{-5}{3} = -1.7$$

$$=> y = \frac{-7}{3} = -2.3$$
 $=> y = \frac{-5}{3} = -1.7$ $=> y = \frac{-1}{3} = -0.33$.



Q4. Using values of x from -2 to 1, plot the graphs of the following relations:

a)
$$y = x$$

b)
$$y = -x$$

NB: The graph of y = x is the same as the graph of -y = -x..

• Also the graph of y = x is the same as the graph of y-x = 0..

Soln

y = x

X	-2	-1	0	1
Y	-2	-1	0	1

1) If
$$x = -2$$

2) If
$$x = -1$$

y = x

$$y = x$$

$$=> y = -2$$

$$=> y = -1$$

3) If
$$x = 0$$

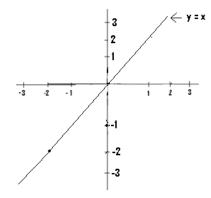
4) If
$$x = 1$$

$$y = x$$

$$y = x$$

$$=> y = 0$$

$$=> y = 1$$



NB: The graph of y = -x, is the same as the graph of -y = x.

• Also the graph of y = -x is the same as the graph of y + x = 0.

b)

$$y = -x$$

X	-2	-1	0	1	2
Y	2	1	0	-1	-2

1) If
$$x = -2$$

2) If
$$x = -1$$

$$y = -x$$

$$y = -x$$

$$=> y = - (-2)$$

$$=> y = - (-1)$$

$$=> y = 2$$

$$=> y = 1$$

4) If
$$x = 0$$

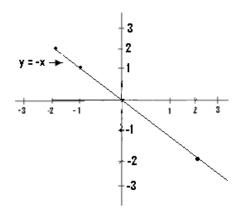
4) If
$$x = 1$$

$$y = -x$$

$$y = -x$$

$$=> y = 0$$

$$=> y = -1$$



NB: If for each graph, the range or the values of x which must be used is not given, we select a few values of x and compute the corresponding y values.

- Graphs of the form y = a, where a is a whole number, are graphs which are perpendicular to the y-axis, and passes through the whole number concerned.
- Such graphs are plotted straight away, without the construction of any table. These graphs are straight lines graphs.

Q5) Plot the graphs with the following equations:

a)
$$y = 3$$

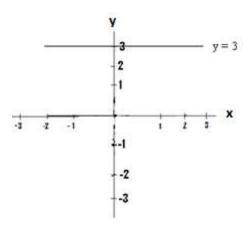
b)
$$y = 7$$

c)
$$y = -8$$

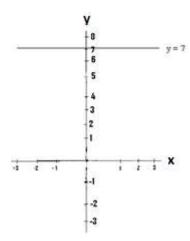
d)
$$y = -4$$

Soln:

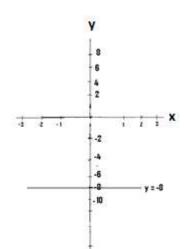
(a)



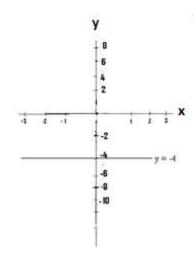
(b)



(c)



(d)



NB: The x-axis is the same as the graph of y = 0.

• Graphs of the form x = a, where a is a whole number are perpendicular to the x-axis, and passes through the whole number concerned.

Q6.) Plot the graphs with the following equations:

a)
$$x = 2$$

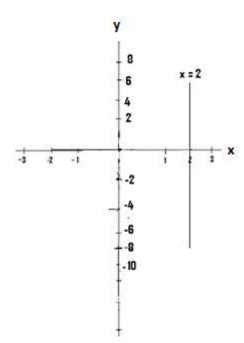
b)
$$x = 6$$

c) x = -4

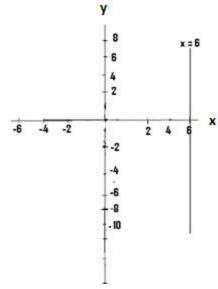
d) x = -8

Soln:

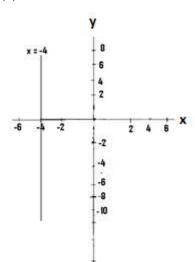
(a)



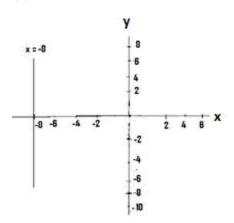
(b)



(c)



(d)



Quadratic Graphs:

These are graphs of quadratic expressions, which are expressions of the form $ax^2 + bx + c$, where a \neq 0 with b and c being of constants and where x and y are variables, i.e. they are not constants.

Examples are:

i.
$$Y = 2x^2 + 4x + 1$$

ii.
$$Y = 6x^2 - 7x - 8$$

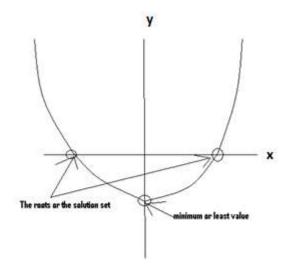
iii.
$$Y = -6x^2 + x - 1$$

iv.
$$Y = -x^2 - 4$$

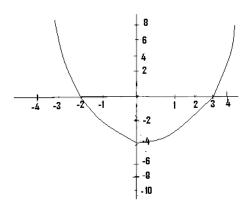
v.
$$Y = x^2 + 2$$

When graphs of quadratic expressions are plotted or drawn, we may arrive at any of these four cases:

Case 1:



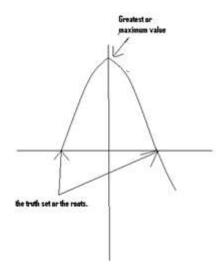
• For example assuming we had the next diagram after drawing our quadratic graph



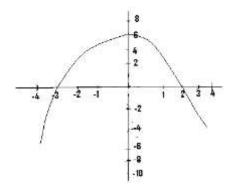
The minimum value is - 4 and the truth set or solution set = $\{x: x = -2 \text{ or } x = 3\}$..

The truth or solution set occurs at the point where the graph cuts the x- axis.

Case 2:



Example:



This graph has a maximum or a greatest value of 6. The truth set = $\{x: x = -3 \text{ or } x = 2\}$.

NB:

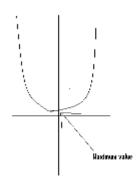
• When the shape of our graph is as shown next, then we shall have a minimum value.



• But when the shape is as shown next, then we shall have a maximum or greatest value.

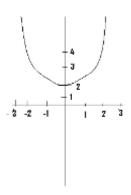


Case 3:



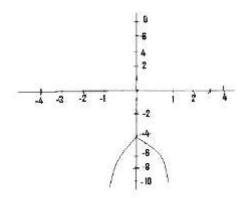
• Since the graph does not cut the x-axis, then the graph has no roots or truth set. But it has a minimum value.

Example:



This graph has no roots or truth set, but has a minimum value of 2.

Case 4.



• Such a graph has no truth set, since it also does not cut the x-axis, but it has a maximum value of -4.

- Q1. Using values of x from 6 to 6, plot the graph of the relation $y = -x^2 2$.
- b) Use your graph to determine the truth set of the following: 1) $-x^2 2 = 0$, 2) $-x^2 2 = -10$,

3)
$$-x^2 - 2 = -30$$

NB: In order to save space, only a few values of y will be computed as an illustration but during examinations, all the values of y must be computed.

Solution

X	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6
Y	-38	-27	-18	-11	-6	-3	-2	-3	-6	-11	-18	-27	-38

1. If
$$x = -6$$
, $y = -x^2 - 2$

$$=>Y = -(-6)^2 - 2$$

$$=>Y = -(36) - 2$$

$$=> Y = -36 - 2$$

$$=>Y = -38$$

i. If
$$x = -3$$
, $y = -x^2 - 2$

$$=>Y=-(-3)^2-2$$

$$=>Y = -(9) - 2$$

$$=>Y = -9 - 2 = -11.$$

ii. If
$$x = 0$$
, $y = -x^2 - 2$

$$=>Y = -(0)^2 - 2 = -0 - 2$$

$$=>Y = 0 - 2 = -2$$

iii. If
$$x = 2$$
, $y = -x^2 - 2$

$$=>Y = -(2)^2 - 2 = -(4) - 2$$

$$=.>Y = -4 - 2 = -6.$$

iv. If
$$x = 4$$
, $y = -x^2 - 2$

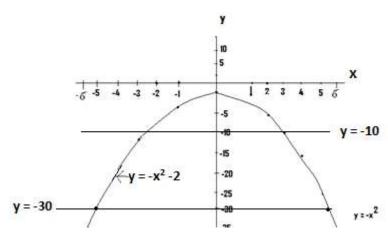
$$=>Y = -(4)^2 - 2 = -(16) - 2$$

$$=>Y = -16 - 2 = -18$$

v. If
$$x = 6$$
, $y = -x^2 - 2$

$$=>Y = -(6)^2 - 2 = -(36) - 2$$

$$=>Y = -36 - 2 = -38$$



b) The equation of the graph is $y = -x^2 - 2$.

i. From
$$-x^2 - 2 = 0$$

$$=>Y = -x^2 - 2 = 0$$

$$=>Y=0$$

We therefore draw the line graph y = 0, which is the x-axis. Since our graph does not cut the x-axis, then there is no truth set.

ii. From $-x^2 - 2 = -10$,

$$=>Y = -x^2 - 2 = -10$$

$$=>Y = -10.$$

We therefore draw the line y = -10 and at the points where it cuts the graph , we determine the corresponding values of x, which form the truth set. From the graph the truth set = $\{x: x = -2.5 \text{ or } x = 3\}$ approx..

iii. From $-x^2 - 2 = -30$

$$=>Y = -x^2 - 2 = -30$$

$$=>Y = -30.$$

We therefore draw the line graph of y = -30. From the graph, at the points where the graph cuts this line, the corresponding values of x are approximately -5 and 5,

$$=>$$
 truth set = {x: x = -5 or x = 5'

Q2.

y = 4									x - 21					
	X	-2.0	-1.5	-1.0	-0.5	0.0	0.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0
	Y	11		-9		-21		-25		-21			0	

The given table is an incomplete table for the relation $y = 4x^2 - 8x - 21$, for $-2.0 \le x \le 4.0$.

- i. Copy and complete the table.
- ii. Plot the graph for the given relation.
- iii. From your graph, determine the truth set of:
 - a) $4x^2 8x 21 = 0$
 - b) $4x^2 8x 21 = 10$.

Soln:

$$y = 4x^2 - 8x - 21$$

X	-2.0	-1.5	-1.0	-0.5	0.0	0.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0
Y	11	0	-9	-16	-21	24	-25	-24	-21	-1.6	-9	0	11

1. If
$$x = -1.5$$

$$Y = 4x^2 - 8x - 21$$

$$=>$$
Y = 4(-1.5)² - 8(-1.5) -21

$$=>Y = 4(2.25) + 8(1.5) - 21$$

$$=>Y = 9 + 12 - 21$$

$$=>Y = 21 - 21 = 0$$

$$=>Y=0$$

2. If
$$x = -0.5$$

$$=> Y = 4x^2 - 8x - 21$$

$$=>$$
Y = 4(-0.5)² - 8(-0.5) -21

$$=>Y = 4(0.25) + 8(0.5) -21$$

$$=>Y = 1 + 4 - 21$$

$$=>Y = 5 - 21$$

$$=>Y = -16$$

3. If
$$x = 1.0$$

$$Y = 4x^2 - 8x - 21$$

$$=>Y = 4(1)^2 - 8(1) - 21$$

$$=>Y = 4 - 8 - 21$$

$$=>Y = -4 - 21$$

$$=>Y = -25$$

4. If
$$x = 2.5$$

$$Y = 4x^2 - 8x - 21$$

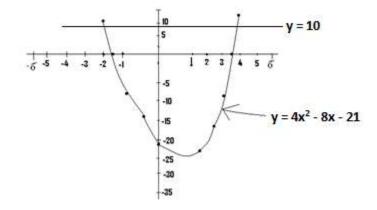
$$=>Y = 4(2.5)^2 - 8(2.5) - 21$$

$$=>$$
Y = 4(6.25) $-$ 20 $-$ 21

$$=>Y = 25 - 20 - 21$$

$$=>Y = 5 - 21$$

$$=>Y = -16$$



We are required to find the truth set of $4x^2 - 8x - 21 = 0$, using our graph. First you must check whether this equation is similar to that of the graph drawn or not. If these two equations are similar, then we proceed with the working. However, if they differ, then we have to make certain alterations before we continue with the work.

a) The equation of the graph is given by $y = 4x^2 - 8x - 21$ and the given equation is $4x^2 - 8x - 21 = 0$. These two equations are the same.

From
$$4x^2 - 8x - 21 = 0$$

$$=>Y = 4x^2 - 8x - 21 = 0$$

$$=>Y=0.$$

We therefore draw the line y = 0 (which is the x-axis) and determine the points where the graph cuts it. From the graph the required truth set = $\{x: x = -1.5 \text{ or } x = 3.5\}$.

b) We are required to find the truth set of $4x^2 - 8x - 21 = 10$. This equation is similar to that of the graph which is $y = 4x^2 - 8x - 21$.

From
$$4x^2 - 8x - 21 = 10$$

$$=>Y = 4x^2 - 8x - 21 = 10$$

$$=>Y = 10$$

We therefore draw the line y = 10, and at the points where the graph cuts this line, the corresponding values of x are determined.

From the graph the truth set = $\{x: x = -2 \text{ or } x = 4\}$.

Q3.

- i. Using the same axes, draw the graphs of the equation $y + 3x^2 = x 8$ and y = 2x 12, for $-4 \le x \le 5$.
- ii. Using your graph, find the values of x which satisfy the simultaneous equation $-3x^2 + x 8 = 2x 12$.

NB:

The expression "Using the same axes" implies that these two graphs must be drawn on the same sheet of graph paper, after the construction of separate tables for each of the given equations.

Solution

The equation of the first graph is given as $y + 3x^2 = x - 8$

 $=>Y = x - 8 - 3x^2$, which can also be written as $y = -3x^2 + x - 8$.

_	$Y = -3x^2 + x - 8$												
	X	-4	-3	-2	-1	0	1	2	3	4	5		
	у	-60	-38	-22	-12	-8	-10	-18	-32	-52	-78		

i. If
$$x = -4$$

$$Y = -3x^2 + x - 8$$

$$=>Y=-3(-4)^2+(-4)-8$$

$$=>Y = -3(16) - 4 - 8$$

$$=>Y = -48 - 4 - 8$$

$$=>Y = -52 - 8$$

$$=>Y = -60$$

ii. If
$$x = -3$$

$$Y = -3x^2 + x - 8$$

$$=>Y = -3(-3)^2 + (-3) - 8$$

$$=>Y = -3(9) - 3 - 8$$

$$=>Y = -27 - 3 - 8$$

$$=>Y = -30 - 8$$

$$=>Y = -38$$

iii. If
$$x = 0$$

$$Y = -3x^{2} + x - 8$$

$$=>Y = -3(0)^{2} + (0) - 8$$

$$=>Y = -3(0) + 0 - 8$$

$$=>Y = 0 + 0 - 8$$

$$=>Y=0-8$$

$$=>Y = -8$$

iv. If
$$x = 2$$

$$Y = -3x^2 + x - 8$$

$$=>Y=-3(2)^2+2-8$$

$$=>$$
Y = -12 + 2 - 8

$$=>Y = -10 - 8$$

$$=>Y = -18$$

v. If
$$x = 5$$

$$Y = -3x^{2} + x - 8$$

$$=>Y = -3(5)^{2} + (5) - 8$$

$$=>Y = -3(25) + 5 - 8$$

$$=>Y = -75 + 5 - 8$$

$$=>Y = -70 - 8$$

$$=>Y = -78$$

We can now construct our second table.

$$Y = 2x - 12$$

X	-4	-3	-2	-1	0	1	2	3	4
Y	-20				-12		-8		

1b. The given equation i.e. y = 2x - 12 is that of a straight line or a straight line graph. In drawing a straight graph, we only need to compute only for two or three values of y.

i. If
$$x = -4$$

$$Y = 2x - 12$$

$$=>$$
Y = 2(-4) - 12

$$=>Y = -8 - 12$$

$$=>Y = -20$$

ii. If
$$x = 0$$

$$Y = 2x - 12$$

$$=> .Y = 2(0) - 12$$

$$=>Y = 0 - 12$$

$$=>Y = -12$$

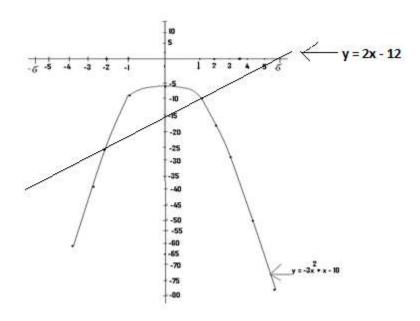
iii. If
$$x = 2$$

$$Y = 2x - 12$$

$$=>$$
Y = 2(2) - 12

$$=>Y = 4 - 12$$

$$=>Y = -8$$



NB: To use the graph to find the values of x which satisfy the equation $-3x^2 + x - 18 = 2x - 12$, we consider the points of intersections (i.e. where they meet) of the two graphs, and determine the corresponding x values.

To do this, straight lines are drawn from these points to meet the x-axis. The points where these drawn lines meet the x- axis represents the truth set.

From the graphs drawn, the truth set = $\{x: x = -1.5 \text{ or } x = 1\}$.

Q4.

- i. Using values of x from 4 to 8, plot on the same axis the graphs of the relations $y = x^2 6x + 2$ and $y = 3x^2 2x 1$.
- ii. Using your graphs, determine the truth set of the simultaneous equation x^2 $6x + 2 = 3x^2 2x 1$.

NB:

First construct separate tables for the two given equations.

Table 1

$$y = x^2 - 6x + 2$$

X	-4	-3	-2	-1	0	1	2	3	4	5	6	7	8
у	42	29	18	9	2	-3	-6	-7	-6	-3	2	9	18

i. If
$$x = -4$$

$$Y = x^2 - 6x + 2$$

$$=>Y = (-4)^2 - 6(-4) + 2$$

$$=>Y = 16 + 24 + 2$$

$$=>Y = 42$$

ii. If
$$x = -2$$

$$Y = x^2 - 6x + 2$$

$$=>Y=(-2)^2-6(-2)+2$$

$$=>Y=4+12+2$$

$$=>Y = 18$$

iii. If
$$x = 0$$

$$Y = x^2 - 6x + 2$$

$$=>Y=(0)^2+6(0)+2$$

$$=>Y = 0 + 0 + 2$$

$$=>Y = 0 + 2$$

$$=>Y=2$$

iv. If
$$x = 2$$

$$Y = x^2 - 6x + 2$$

$$=>Y=(2)^2-6(2)+2$$

$$=>Y = 4 - 12 + 2$$

$$=> Y = -8 + 2$$

$$=>Y = -6$$

v. If
$$x = 4$$

$$Y = x^2 - 6x + 2$$

$$=>Y=(4)^2-6(4)+2$$

$$=>Y = 16 - 24 + 2$$

$$=>Y = -8 + 2$$

$$=> Y = -6$$

vi. If
$$x = 6$$

$$Y = x^2 - 6x + 2$$

$$=>Y=(6)^2-6(6)+2$$

$$=>Y = 36 - 36 + 2$$

$$=>Y = 0 + 2$$

$$=>Y=2$$

Table 2

$$y = 3x^2 - 2x - 1$$

X	-4	-3	-2	-1	0	1	2	3	4	5	6	7	8
Y	55	32	15	4	-1	-1	7	20	39	64	95	132	175

i. If
$$x = -4$$

$$Y = 3x^2 - 2x - 1$$

$$=>Y = 3(-4)^2 - 2(-4) - 1$$

$$=>Y = 3(16) + 8 - 1$$

$$=>Y = 48 + 8 - 1$$

$$=>Y = 55$$

ii. If
$$x = -2$$

$$Y=3x^{\mathbf{2}}-2x-1$$

$$=>$$
Y = 3(-2)² - 2(-2) - 1

$$=>Y = 3(4) + 4 - 1$$

$$=>Y = 12 + 4 - 1$$

$$=>Y = 15$$

iii. If
$$x = -1$$

$$Y = 3x^2 - 2x - 1$$

$$=>$$
Y = 3(-1)² - 2(-1) - 1

$$=>Y = 3(1) + 2 - 1$$

$$=>$$
Y = 3 + 2 - 1

$$=>Y = 4$$

iv. If
$$x = 4$$

$$Y = 3x^2 - 2x - 1$$

$$=>Y = 3(4)^2 - 2(4) - 1$$

$$=>Y = 3(16) - 8 - 1$$

$$=>Y = 48 - 8 - 1$$

$$=> Y = 39$$

v. If
$$x = 6$$

$$Y = 3x^2 - 2x - 1$$

$$=>Y=3(6)^2-2(6)-1$$

$$=>Y = 3(36) - 12 - 1$$

$$=>Y = 108 - 12 - 1$$

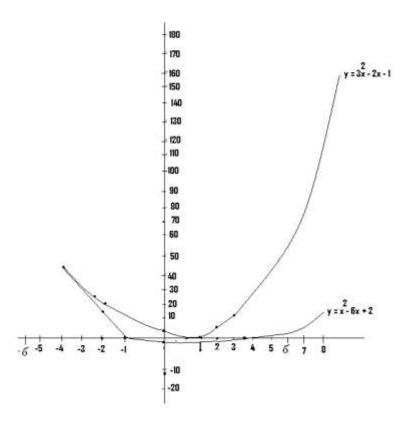
$$=>Y = 95$$

vi. If
$$x = 7$$

$$Y = 3x^2 - 2x - 1$$

$$=>Y=3(7)^2-2(7)-1$$

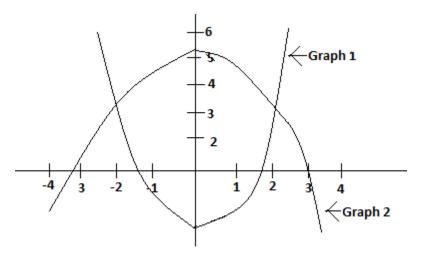
$$=>Y = 132$$



From the graph, the value of x which satisfies simultaneously the equation $3x^2 - 2x - 1 = x^2 - 6x + 2$ occurs at the points where the two graphs meet. The corresponding x values are then read after drawing straight lines from these point or points to meet the x-axis. From the graphs drawn the required value of x is = -2.5

NB: Before we can determine the value of x which satisfies the equations of two graphs simultaneously, then the two graphs must be drawn on the same axes.

N/B:



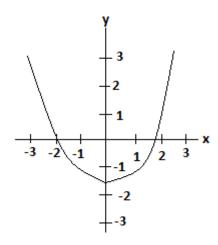
- It is possible to draw two quadratic graphs on the same axes and, get a diagram similar to the one just drawn.
- In such a case, the values of x which satisfy simultaneously the equations, of the two quadratic graphs is had by determining first the points of intersection or the point of intersection of the two graphs.

- From these points, straight lines are drawn to meet the x-axis and the values of x taken as the required ones.

The axis of symmetry or the line of symmetry of a quadratic graph:

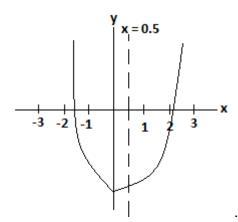
- The line of symmetry, the axis of symmetry or the symmetrical axis of a quadratic graph, is a line which is parallel to the y-axis, and which divides the graph into exactly or almost two equal parts.
- In certain cases, the line of symmetry may happen to be the y-axis.
- (Q1) Determine the lines of symmetry of these quadratic graphs drawn:

(a)



- The line of symmetry in this case is the axis or the line x = 0.

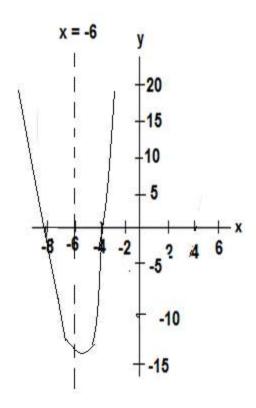
(b)



- For this, the line of symmetry is x = 0.5, since it divides the graph into almost two equal parts.

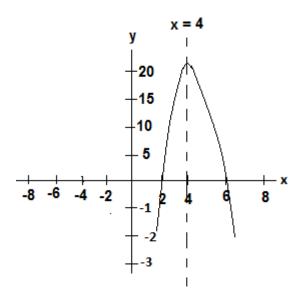
N/B:- The line of symmetry is represented usually by a broken line, and its position must be determined by the student.

(c)



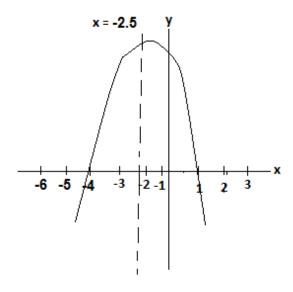
The axis of symmetry in this case is x = -6.

d)



The line of symmetry is x = 4.

e)



The line of symmetry is x = -2.5.

(Q1) (i) Construct a table for the relation $y = 2x^2 - 8x - 5$ for $-2 \le x \le 6$. (ii) Draw the graph for the given relation. (iii) Use your graph to find the truth set of

(a)
$$p = \{x: 2x^2 - 8x - 5 = 0\}.$$

(b)
$$Q = \{x: 2x^2 - 8x - 5 = 15\}.$$

(c)
$$R = \{x: 2x^2 - 9x - 5 = 0\}.$$

(d) Draw the line of symmetry and determine its equation.

Soln:

(i)

$$y = 2x^2 - 8x - 5$$

X	-2	-1	0	1	2	3	4	5	6
Y	19	5	-5	-11	-13	-11	-5	5	19

(1) If
$$x = -2$$

$$y = 2x^2 - 8x - 5$$

$$\Rightarrow$$
 y = 2(-2)² - 8(-2) - 5

$$=> y = 2(4) + 16 - 5$$

$$=> y = 8 + 16 - 5$$

$$=> y = 19.$$

(2) If
$$x = 1$$

$$y = 2x^2 - 8x - 5$$

$$\Rightarrow$$
 y = 2(1)² +8(1) - 5

$$=>y=2+8-5$$

$$=> y = 10 - 5$$

$$=> y = 5.$$

(3) If
$$x = 0$$

$$Y = 2x^2 - 8x - 5$$

$$=> Y = 2(0)^2 - 8(0) - 5$$

$$=> y = 0 - 0-5$$

$$=> y = 0 - 5$$

$$=> y = -5.$$

(4) If
$$x = 4$$

$$Y = 2x^2 - 8x - 5$$

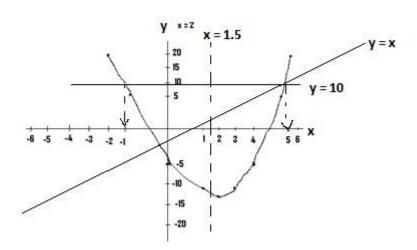
$$=> Y = 2(4)^2 - 8(4) - 5$$

$$=>Y=2(16)-32-5$$

$$=> y = 32 - 32 - 5$$

$$=> y = 0 - 5$$

$$=> y = -5.$$



(iii) (a) We are required to find the truth set of $P=\{x: 2x^2-8x-5=0.\}$.

But the equation of the graph is $y = 2x^2 - 8x - 5$. Since these two equations are similar, then from $2x^2 - 8x - 5 = 0 \Rightarrow y = 2x^2 - 8x - 5 = 0 \Rightarrow y = 0$.

We therefore consider the line y = 0, which is the x - axis and take the corresponding values of x, at the points where the graph cuts the x- axis.

Therefore the required truth set= $\{x: x = -0.5 \text{ or } x = 4.5\}.$

(b) We are required to find the truth set of $Q = \{x: 2x^2 - 8x = 15\}$. Since this equation i.e. $2x^2 - 8x$ = 15 is different from that of the graph, it must be altered using any possible means to make it become similar to that of the graph, which is $y = 2x^2 - 8x - 5$.

From $2x^2 - 8x = 15 \implies 2x^2 - 8x - 15 = 0$, Adding 10 to both sides of the equation $\implies 2x^2 - 8x = 15$ $+10=0+10 \Rightarrow 2x^2-8x-5=10$, which is similar to the equation of the graph, which is $y=2x^2-10$ 8x - 5.

Now from $2x^2 - 8x - 5 = 10$, \Rightarrow $y = 2x^2 - 8x - 5 = 10$,

=> y = 10. We therefore draw the line y = 10, and where it cuts the graph, the corresponding x values are determined from the graph, the required truth set is given by $\{x: x = -1 \text{ and } x = 5\}$.

(c) We are required to find the truth set of $R = \{x: 2x^2 - 9x - 5 = 0\}$. Since the relation $2x^2 - 9x - 5$ = 0 differs from $y = 2x^2 - 8x - 5$, it must be altered to become like that of the graph. The only way to do this is to add x to both sides of the equation.

i.e.
$$2x^2 - 9x - 5 + x = 0 + x$$
, $\Rightarrow 2x^2 - 8x - 5 = x$, but since $y = 2x^2 - 8x - 5$.

Then from $y = 2x^2 - 8x - 5 = x \Rightarrow y = x$. We therefore draw the line y = x and at the points where it cuts the graph, the corresponding x - axis values are determined. Before we draw the graph of y = x, we must first construct a table.

X	1	2	3
Y	1	2	3
(1) If $x = 1$	(2) If $x = 2$	(3) If $x = 3$	<u> </u>

$$y = x$$

$$\mathbf{v} = \mathbf{x}$$

$$\mathbf{v} - \mathbf{v}$$

$$=> y = 1$$
 $=> y = 2$

$$=> y = 3$$

From the graph drawn, the required truth set is given by $\{x: x = -0.5 \text{ or } x = 5\}$ approx.

- (e) From the line of symmetry drawn, its equation is x = 1.5 approx.
- (Q2) (i) Using a scale of 2cm to 1 unit on the x-axis and 2 cm to 2units on the other axis, draw on the same axes the graphs of

(a)
$$x \to 6 + 2x - x^2$$

(b)
$$x \longrightarrow x + 2$$
, For $-3 \le x \le 5$.

Use your graph to determine the truth set of the simultaneous equation y - x = 2 and $x^2 + y = 6 + 2x$.

N/B: $x \rightarrow 6 + 2x - x^2 => y = 6 + 2x - x^2$, which we may choose to write as

$$y = -x^2 + 2x + 6$$
.

Also
$$x \to x + 2 => y = x + 2$$
.

We therefore construct separate tables for $y = -x^2 + 2x + 6$ and y = x + 2 and draw their graphs on the same sheet of graph paper.

$$y = -x^2 + 2x + 6$$

X	-3	-2	-1	0	1	2	3	4	5
Y	-9	-2	3	6	7	6	3	-2	-9

1) If
$$x = -3$$

(2) If
$$x = -1$$

$$y = -x^2 + 2x + 6$$

$$y = -x^2 + 2x + 6$$

$$=> y = -(-3)^2 + 2(-3) + 6$$

$$\Rightarrow$$
 y = - (-1)² + 2(-1) + 6

$$=>y=-(9)-6+6$$

$$=> y = -(1) - 2 + 6$$

$$=> y = -9.$$

$$=> y = -3 + 6 = 3$$

3) If
$$x = 0$$

(4) If
$$x = 2$$

$$y = -x^2 + 2x + 6$$

$$y = -x^2 + 2x + 6$$

$$=> y = -(0)^2 + 2(0) + 6$$

$$=> y = -(2)^2 + 2(2) + 6$$

$$=> y = 0 + 0 + 6$$

$$=> y = -(4) + 4 + 6$$

$$=> y = 0 + 6 = 6$$

$$=> y = -4 + 4 + 6 => y = 6$$

(5) If
$$x = 4$$

(6) If
$$x = 5$$

$$y = -x^2 + 2x + 6$$

$$y = -x^2 + 2x + 6$$

$$=> y = -(4)^2 + 2(4) + 6 => y = -(5)^2 + 2(5) + 6$$

$$=> y = -(16) + 8 + 6$$
 $=> y = -(25) + 10 + 6$

$$=> v = -(25) + 10 + 6$$

$$=> y = -16 + 8 + 6$$

$$=> y = -25 + 10 + 6$$

$$=> y = -8 + 6 = -2$$

$$=> y = -9$$

$$=> y = -2$$

$$y = x + 2$$

X	-3	-2	-2	0	1	2	3	4	5
Y	-1			2	3				

Since this is a straight line graph, we shall only compute three values of y.

(1) If
$$x = -3$$

(2) If
$$x = 0$$

(3) If
$$x = 1$$

$$Y = x + 2$$

$$y = x + 2$$

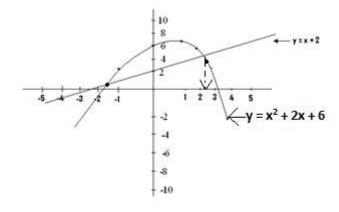
$$y = x + 2$$

$$=>Y=-3+2$$

$$=> y = 0 + 2 = 2$$

$$=> y = 1 + 2 = 3$$

$$=> y = -1$$



(iii) We are required to use our graphs to find the truth set of the simultaneous equation y - x = 2

$$x^2 + y = 6 + 2x$$

Soln:

From $y - x = 2 \Rightarrow y = 2 + x$, which is the equation for the second graph just drawn.

Also from $x^2 + y = 6 + 2x$, \Rightarrow $y = 6 + 2x - x^2 \Rightarrow$ $y = -x^2 + 2x + 6$, which is the equation for the first graph drawn.

We therefore determine the meeting point or the points of intersection of these two graphs and for each of these points, we determine the corresponding x – axis value or component. The required truth set ={x: x = -1.5 or x = 2.5} approx.

(Q3) Copy and complete the following table for the relation $y = \frac{1}{2}(2x - 1)(x + 2)$

X	-3.5	-3	-2	-1	-0.5	0	1	2
Y	6		0				1.5	

- (a) Using a scale of 2cm to 1 unit on each axis, draw the graph of the relation $y = \frac{1}{2}(2x-1)(x+2)$ for $-3.5 \le x \le 2$.
- (b) From your graph, determine the values of x for which y is least.
- (c) Find also from your graph the truth set of $\frac{1}{2}(2x-1)(x+2)=4$

Soln:

X	-3.5	-3	-2	-1	-0.5	0	1	2
Y	6	3.5	0	-1.5	-1.5	-1	1.5	6

$$y = \frac{1}{2}(2x-1)(x+2)$$

$$=> y = \frac{1}{2}(2(-3) - 1)(\{-3\} + 2)$$

$$=> y = \frac{1}{2}(-6-1)(-1)$$

$$=> y = \frac{1}{2}(-7)(-1)$$

$$=> y = \frac{1}{2}(7) = \frac{7}{2} = 3.5.$$

(2) If
$$x = -0.5$$

$$y = \frac{1}{2}(2x-1)(x+2)$$

$$=> y = \frac{1}{2}(2(-0.5) - 1)(\{-0.5\} + 2)$$

$$=> y = \frac{1}{2}(-1-1)(1.5)$$

$$=> y = \frac{1}{2}(-2)(1.5)$$

$$=> y = \frac{1}{2}(-3) => y = -1.5.$$

(3) If
$$x = 2$$

$$y = \frac{1}{2}(2x-1)(x+2)$$

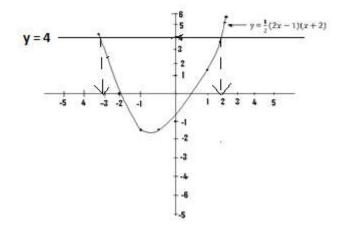
$$=> y = \frac{1}{2}(2\{2\} - 1)(2 + 2)$$

$$=> y = \frac{1}{2}(4-1)(4)$$

$$=> y = \frac{1}{2}(3)(4) = \frac{1}{2}(12)$$

$$=> y = 6.$$

(a)



(b) y is least at the point where the minimum value occurs and the corresponding x values are - 0.5 and -1.

(c) The equation of the graph is $y = \frac{1}{2}(2x - 1)(x + 2)$.

The given equation which is $\frac{1}{2}(2x-1)(x+2)=4$ is similar to that of the graph.

From
$$y = \frac{1}{2}(2x - 1)(x + 2) = 4 \Rightarrow y = \frac{1}{2}(2x - 1)(x + 2) = 4, \Rightarrow y = 4.$$

Draw the line y = 4 and at points that is meets the graph, find the corresponding x components or values.

Truth set= $\{x:x = -3 \text{ or } x = 2\}$ approx.

(Q4)

X	-3	-2	-1	0	1	2	3	4
Y		1.7		4	4.2	3.7		

Copy and complete the table for the relation $y = 4 + \frac{1}{2}x - \frac{1}{3}x^2$ for $-3 \le x \le 4$.

- (i) Draw the graph for the relation $y = 4 + \frac{1}{2}x \frac{1}{3}x^2$.
- (ii) From your graph, determine the line of symmetry.
- (iii) What is the truth set of $24 + 3x 2x^2 = 0$.

Soln

$$y = 4 + \frac{1}{2}x - \frac{1}{3}x^2$$

X	-3	-2	-1	0	1	2	3	4
Y	-0.5	1.7	3.2	4	4.2	3.7	2.5	0.7

$$(1)$$
 If $x = -3$

$$y = 4 + \frac{1}{2}x - \frac{1}{2}x^2$$

$$=> y = 4 + \frac{1}{2}(-3) - \frac{1}{3}(-3)^{2}$$

$$=> y = 4 + \frac{-3}{2} - \frac{1}{3}(-3)^{2}$$

$$=> y = 4 + \frac{-3}{2} - \frac{1}{3}(9)$$

$$=> y = 4 + (-1.5) - 3$$

$$=> y = 4 - 1.5 - 3$$

$$=> y = -0.5$$

(2) If
$$x = -1$$

 $y = 4 + \frac{1}{2}x - \frac{1}{3}x^2$
 $\Rightarrow y = 4 + \frac{1}{2}(-1) - \frac{1}{3}(-1)^2$
 $\Rightarrow y = 4 + \frac{-1}{2} - \frac{1}{3}(1)$
 $\Rightarrow y = 4 - 0.5 - 0.33$
 $\Rightarrow y = 3.2$

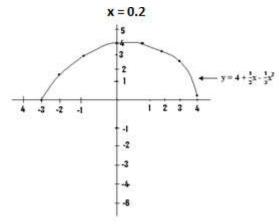
(3) If
$$x = 3$$

 $y = 4 + \frac{1}{2}x - \frac{1}{3}x^2$
 $\Rightarrow y = 4 + \frac{3}{2} - \frac{1}{3}$ (9)
 $\Rightarrow y = 4 + 1.5 - 3$
 $\Rightarrow y = 2.5$

(4) If
$$x = 4$$

 $y = 4 + \frac{1}{2}x - \frac{1}{3}x^2$
 $\Rightarrow y = 4 + \frac{1}{2}(4) - \frac{1}{3}(4)^2 \Rightarrow y = 4 + 2 - \frac{1}{3}(16)$
 $\Rightarrow y = 4 + 2 - 5.3$
 $\Rightarrow y = 0.7$

(i)



- (ii) From the graph, the line of symmetry is x = 0.2 (approximately).
- (iii) We are required to find the truth set of $24 + 3x 2x 2x^2 = 0$.

This must be altered to be similar to the equation of the graph which is

$$y = 4 + \frac{1}{2}x - \frac{1}{3}x^2$$
.

From $24 + 3x - 2x^2 = 0$, divide through using 6

$$=>\frac{24}{6} + \frac{3x}{6} - \frac{2x^2}{6} = \frac{0}{6} => 4 + \frac{1}{2}x - \frac{1}{3}x^2 = 0,$$

 \Rightarrow $y = 4 + \frac{1}{2}x - \frac{1}{3}x^2 = 0 \Rightarrow y = 0$ (which is the - x axis constitute the truth set.

The truth set = $\{x: x = -2.5\}$ approx, i.e. determine the points where the graph cuts the x-axis.

- (Q4) An object is thrown vertically upward from the top of a cliff and its height, y metres, above sea level after t seconds is given by $y = -16t^2 + 64t + 5$.
 - (a) Copy and complete the table of values for $y = -16t^2 + 64t + 5$, for $0 \le x \le 4.0$.

	t	0.0	0.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0
•	у	5			65		65	53		

- (b) Using scales of 2cm to 0.5 seconds on the t-axis, and 2cm to 10m on the y-axis, draw the graph of $y=-16t^2+64t+5$ for $0 \le x \le 4.0$.
- (c) Use the graph to find the
 - (i) height reached when t = 1.75 seconds.
 - (ii) time the object was at a height of 50m.
 - (iii) maximum height reached.

Hint:

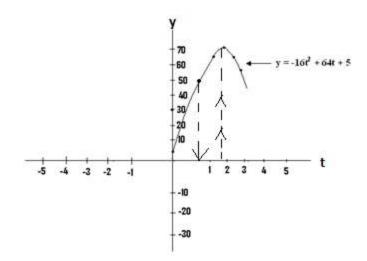
From $y = -16t^2 + 64t + 5 =>$ when t = 2, then $y = -16(2)^2 + 64(2) + 5$,

$$=> y = -16(4) + 128 + 5$$

$$=> y = -64 + 128 + 5 = 69.$$

A rough sketch of how the graph will look is shown next.

(c)



- (i) t = 1.75 can be approximated to t = 1.8: From t = 1.8, draw a straight line to meet the graph and from this point, draw another one to meet the y axis. The point where it meets the y axis is the required value.
- (ii) If the height is 50m, then y = 50m. From y = 50, draw a straight line and at the points where it meets the graph, straight lines are then drawn to meet the t or time axis. These meeting points are the required values.
- (iii) The maximum height reached refers to the highest value of y i.e. 69(69m).

(Q5)

X	- 6	- 4	-3	-1	0	1	2	3	5	6
$2x^2$	72			2	0	2	8	18		72
3x + 1	-17			-2	1	4		10		19
Y	55			0	1	6	15	28		91

- (a) Copy and complete the table for the relation $y = 2x^2 + 3x + 1$ for the given values of x.
- (b) Plot a graph of the given relation.

Soln:

$$y = 2x^2 + 3x + 1$$

X	-6	-4	-3	-1	0	1	2	3	5	6
$2x^2$	72	32	18	2	0	2	8	18	50	72
3x +1	-17	-11	-8	-2	1	4	7	10	16	19
Y	55	21	10	0	1	6	15	28	66	91

(1) If
$$x = -4$$

(2) If
$$x = -3$$

(3) If
$$x = 5$$

= 50

$$=> 2x^2 = 2(-4)^2$$

$$=>2x^2=2(-3)^2$$

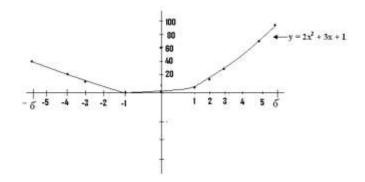
$$=>2x^2=2(5)^2=2(25)$$

$$= 2(16) = 32$$
$$3x + 1 = 3(-4) + 1$$

$$= 2(9) = 18$$

3x + 1 = 3(-3) + 1

$$3x + 1 = 3(5) + 1$$



(Q6)

X	-6	-4	-3	-2	-1	0	2	4	5	6	7	8
-x ²	-36		-9			0		-16		-36	-49	-64
3x-1	-19		-10			-1		11		17	20	23
у	-55		-19			-1		-5		-19	-29	-41

The given table which is incomplete is that for the relation $y = -x^2 + 3x - 1$, for values of x between - 6 and 8.

- (a) Copy and complete the given table.
- (b) Draw a graph for the given relation.

Soln:

(1) If
$$x = -4$$

$$= -x^{2} = -(-4)^{2}$$

$$= -(16) = -16$$

$$= 3x - 1 = 3(-4) - 1$$

$$= -12 - 1 = -13$$

$$y = -x^{2} + 3x - 1$$

$$= > y = -16 + (-13)$$

$$= > y = -16 - 13 = -29$$

(2) If
$$x = -2$$

 $= -x^2 = -(-2)^2$
 $= -(4) = -4$
 $3x - 1 = 3(-2) - 1$
 $= -6 - 1 = -7$
 $y = -x^2 + 3x - 1$

$$=> y = -4 + (-7) = -4 - 7$$

$$=> y = -11$$

(3) If
$$x = 2$$

$$=> -x^2 = -(2)^2$$

$$= - (4) = - 4$$

$$3x - 1 = 3(2) - 1$$

$$=6-1=5$$

$$y = -x^2 + 3x - 1$$

$$=> y = -4 + 5$$

$$=> y = 1$$

(4) If
$$x = 5$$

$$=> -x^2 = -(5)^2$$

$$=$$
 - (25) $=$ -25

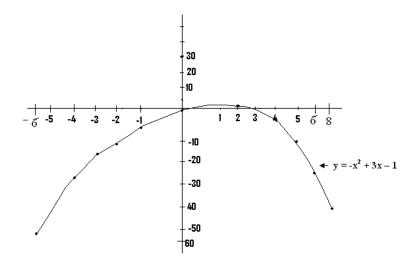
$$3x - 1 = 3(5) - 1$$

$$= 15 - 1 = 14$$

$$y = -x^2 + 3x - 1$$

$$=> y = -25 + 14$$

$$=> y = -11$$



(Q7)

X	-2.5	-2	-1	0	1	1.5	2	2.5	3
$2x^2$			2	0	2	4.5			
x+6			5	6	7	7.5			
Y			-3	-6	-5	-3			

- (i) Copy and complete the table for $y = 2x^2 x 6$ for $-2.5 \le x \le 3$.
- (ii) Using a scale of 2cm = 1unit on the x-axis and 2cm = 2 units on the y-axis, draw the graph of the given relation and use it to find the truth sets of:
 - (a) $2x^2 x 6 = 0$.
 - (b) $2x^2 x 12 = 0$.

N/B: $y = 2x^2 - x - 6$, consider the R.H.S i.e. $2x^2 - x - 6$.

There are two negative signs as shown. Such questions must be handled with care.

$$2x^{2}-x-6=2x^{2}-(x+6) \Rightarrow y=2x^{2}-(x+6)$$

= 3.5

=> y = 9

 $y = 2x^2 - (x + 6)$

=> y = 12.5 - (3.5)

Soln:

(1) If
$$x = -2.5$$
 (2) If $x = -2$ (3) If $x = 2$

$$=>2x^{2} = 2(-2.5)^{2} => 2x^{2} = 2(-2)^{2} => 2x^{2} = 2(2)^{2}$$

$$= 2(6.5) = 12.5 = 2(4) = 8 = 8$$

$$x + 6 = -2.5 + 6 = 4 = 4 = 8$$

$$= 3.5 = 4 = 4 = 2x^{2} = 2x$$

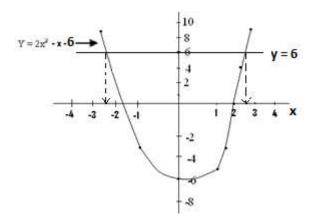
= 9

=> y = 9

 $y = 2x^2 - (x + 6)$

=> y = 18 - (9)

X	-2.5	-2	-1	0	1	1.5	2	2.5	3
$2x^2$	12.5	8	2	0	2	4.5	8	12.5	18
x+6	3.5	4	5	6	7	7.5	8	8.5	9
Y	9	4	-3	-6	-5	-3	0	4	9



(a)
$$2x^2 - x - 6 = 0$$

$$=> y = 2x^2 - x - 6 = 0 => y = 0$$

(which is the same as the x - axis).

$$\Rightarrow$$
 Required truth set $=$ {x : $x = -1.5$ or $x = 2$ }

(b)
$$2x^2 - x - 12 = 0$$

In order to do the necessary alteration, add 6 to both sides.

$$=> 2x^2 - x - 12 + 6 = 0 + 6$$

$$=> 2x^2 - x - 6 = 6$$

$$=> y = 2x^2 - x - 6 = 6$$

$$=> y = 6.$$

We then draw the line y = 6. Required truth set = $\{x : x = -2.3 - 2 \text{ or } x = 2.3\}$ approx.

(Q8)

X	-6	-5	-3	-2	0	2	3	4	6
$3x^2$	108			12			27		
4x+1	23			-7			13		
Y	13			19			14		

- (a) Copy and complete the table for the relation $y = 3x^2 4x 1$ for $-6 \le x \le 6$.
- (b) Plot the graph for the given relation.

Soln:

$$y = 3x^2 - 4x - 1 => y = 3x^2 - (4x + 1)$$

X	-6	-5	-3	-2	0	2	3	4	6
$3x^2$	108	75	27	12	0	12	27	48	108

4x+1	-23	-19	-11	-7	1	9	13	17	25
Y	13	94	38	19	-1	3	14	31	83

(1) If
$$x = -5$$

$$=>3x^2=3(-5)^2$$

$$=3(25) = 75$$

$$4x + 1 = 4(-5) + 1$$

$$= -20 + 1 = -19$$

$$y = 3x^2 - (4x + 1)$$

$$=> y = 75 - (-19)$$

$$=> y = 75 + 19$$

$$=> y = 94$$

(2) If
$$x = -3$$

$$=>3x^2=3(-3)^2$$

$$=3(9) = 27.$$

$$4x + 1 = 4(-3) + 1$$

$$= -12 + 1 = -11.$$

$$y = 3x^2 - (4x + 1)$$

$$=> y = 27 - (-11)$$

$$=> y = 27 + 11$$

$$y = 38$$
.

(3) If x = 2

$$3x^2 = 3(2)^2$$

$$= 3(4) = 12$$

$$4x + 1 = 4(2) + 1$$

$$= 8 + 1 = 9$$

$$y = 3x^2 - (4x + 1)$$

$$=> y = 12 - (9)$$

$$=> y = 12 - 9$$

$$=> y = 3$$

(4) If x = 6

$$=>3x^2=3(6)^2$$

$$=3(36) = 108.$$

$$4x + 1 = 4(6) + 1$$

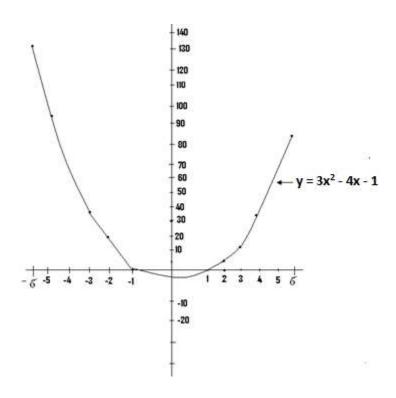
$$= 24 + 1 = 25$$

$$y = 3x^2 - (4x + 1)$$

$$=> y = 108 - (25)$$

$$=> y = 108 - 25$$

$$=> y = 83..$$



(Q9)

X	-7	-5	-3	0	2	4	5	6
$-3x^2$	-147	-75	-27	0	-12	-48	-75	-108
$-3x^2-4x$	-119	-55	-15	0	-20	-64	-95	-132
$-3x^2-4x+2$	-117	-53	-13	2	-18	-62	-93	-130
Y	-117	-53	-13	2	-18	-62	-93	-130

The given incomplete table is that for the relation $y = -3x^2 - 4x + 2$.

- (a) Copy and complete the given table.
- (b) Draw the graph for the given relation.

Soln:

(1) If
$$x = -5$$

 $= > -3x^2 = -3(-5)^2$
 $= -3(25) = -75$.
 $-3x^2 - 4x = -3(-5)^2 - 4(-5)$
 $= -75 - 4(-5) = -75 + 20 = -55$
 $-3x^2 - 4x + 2$
 $= -3(-5)^2 - 4(-5) + 2$

$$= -55 + 2 = -53.$$

(2) If
$$x = -3$$

$$-3x^2 = -3(-3)^2$$

$$= -3(9) = -27.$$

$$-3x^2 - 4x = -3(-3)^2 - 4(-3)$$

$$= -3(9) + 12 = -27 + 12 = -15.$$

$$-3x^2 - 4x + 2$$

$$=-3(-3)^2-4(-3)+2$$

$$= -15 + 2 = -13.$$

(3) If
$$x = 2$$

$$=>-3x^2=-3(2)^2$$

$$= -3(4) = -12.$$

$$-3x^2 - 4x = -3(2)^2 - 4(2)$$

$$= -3(4) - 8 = -12 - 8 = -20.$$

$$-3x^2 - 4x + 2$$

$$=-3(2)^2-4(2)+2$$

$$=-3(4)-8+2$$

$$= -20 + 2 = -18.$$

(4) If
$$x = 6$$

$$-3x^2 = -3(6)^2$$

$$= -3(36) = -108.$$

$$-3x^2 - 4x = -3(6)^2 - 4(6)$$

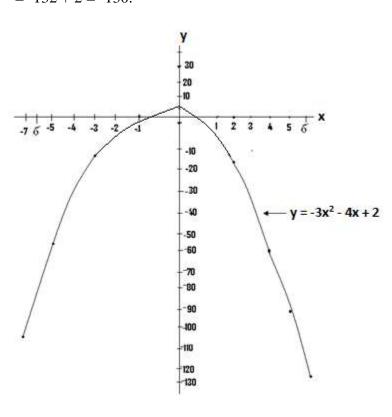
$$=-108-24=-132$$
.

$$-3x^2 - 4x + 2$$

$$=-3(6)^2-4(6)+2$$

$$= -108 - 24 + 2$$

$$= -132 + 2 = -130.$$



N/B: The question just solved could also have taken the form shown next, for the incomplete table is that for the relation $y = 3x^2 - 4x + 2$.

X	-7	-5	-3	0	2	4	5	6
$-3x^2$			-27					
- 4x			-5					
+2			-13					
Y			-13					

Assume x = -3, then $-3x^2 = -3(-3)^2 = -3(9) = -27$

We then find the value of - 4x. If $x = -3 \Rightarrow -4x = -4(-3) = 12$ or + 12. Add the 12 to the -27 to get - 15. Next, we find the + 2. Since it is + 2, we add it to the -15 to get -13. i.e. -15 + 2 = -13

(Q10)

X	- 6	-5	-2	0	1	2	4	5	6
$4x^2$	144			0	4				144
$4x^2+2x$	132			0	6				156
$4x^2+2x-12$	120			-12	- 6				144
$Y=4x^2+2x-12$	120			-12	- 6				144

- (a) Copy and complete the table for the relation $y = 4x^2 + 2x 12$ for $-6 \le x \le 6$..
- (b) Plot the graph of the relation within the given interval.
- (c) Determine the equation of the axis of symmetry.

Soln:

X	- 6	-5	-2	0	1	2	4	5	6
$4x^2$	144	100	16	0	4	16	64	100	144
$4x^2+2x$	132	90	12	0	6	20	72	110	156
$4x^2+2x-12$	120	78	0	-12	-6	8	60	98	144
$Y=4x^2+2x-12$	120	78	0	-12	-6	8	60	98	144

(1) If x = -5

$$=>4x^2=4(-5)^2=4(25)$$

$$4x^{2}+2x = 4(-5)^{2} + 2(-5)$$

$$= 4(25) - 10 = 100 - 10$$

$$= 90.$$

$$4x^{2} + 2x - 12$$

$$= 4(-5)^{2} + 2(-5) - 12$$

$$= 90 - 12 = 78$$
(2) If $x = -2$

$$=>4x^{2} = 4(-2)^{2} = 4(4) = 16.$$

$$4x^{2}+2x = 4(-2)^{2} + 2(-2)$$

$$= 16 - 4 = 12.$$

$$4x^{2} + 2x - 12$$

$$= 4(-2)^{2} + 2(-2) - 12$$

$$= 12 - 12 = 0.$$
(3) If $x = 4$

$$4x^{2} = 4(4)^{2} = 4(16)$$

$$= 64.$$

$$4x^{2}+2x = 4(4)^{2} + 2(4)$$

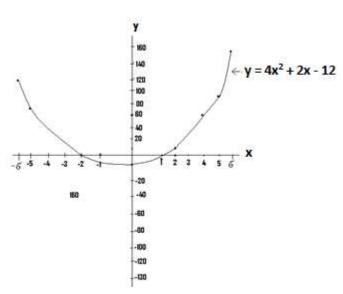
$$= 64 + 8 = 72.$$

$$4x^{2} + 2x - 12$$

$$= 4(4)^{2} + 2(4) - 12$$

$$= 64 + 8 - 12 = 72 - 12 = 60.$$

(b)



(c) From the graph, it is obvious that the y axis or the line x = 0, is the line of symmetry.

N/B: This question just solved could also have taken the form shown next, in which case the incomplete table is that for the relation $y = 4x^2 + 2x - 12$.

X	-6	-5	-2	0	1	2	4	5	6
$4x^2$			16			16			

+2x		12		20		
-12		0		8		
$Y=4x^2+2x-12$		0		8		

The completion of such a table is as following

- (1) Assuming $x = -2 \Rightarrow 4x^2 = 4(-2)^2 = 4(4) = 16$.
- (2) +2x = +2(-2) = +(-4) = -4. Since the answer is negative, we subtract 4 from the 16 i.e. 16 4 = 12.
- (3) The -12 is the subtracted from the 12 to get 0. Also, if x = 2, then $4x^2 = 4(2)^2 = 4(4) = 16$.
- The +2x = +2(2) = 4, and since the sign is positive, we add 4 to the 16 to get 20 i.e. 16 + 4 = 20..
- For the -12, since the sign is negative, we subtract 12 from the 20 to get 8.

Graphs of the form $y = \frac{Ax+C}{Bx+D}$

- There are certain graphs which are of the form $y = \frac{Ax + C}{Bx + D}$, and examples are
 - (i) $y = \frac{2x+5}{x^2+1}$
- (ii) $y = \frac{5x-1}{x-2}$
- Questions based on this type of graph are solved in the usual manner.
- (Q1) The following is an incomplete table of values for the relation $y = \frac{x+5}{x^2+1}$ for

 $-3 \le x \le 3$.

X	-3.0	-2.0	-1.0	0.0	0.2	1.0	2.0	3.0
Y	0.2			5				

- (a) Copy and complete the table.
- (b) Using a scale of 2cm to 1 unit on each axis, draw the graph of the given relation.
- (c) From your graph, find the greatest value of $\frac{x+5}{x^2+1}$.
- (d) Using the same axes and scale, draw the graph of the relation y = x.
- (e) From your graphs, find the truth set of $\frac{x+5}{x^2+1} = x$.

Soln:

(a)
$$y = \frac{x+5}{x^2+1}$$

X	-3.0	-2.0	-1.0	0.0	0.2	1.0	2.0	3.0
Y	0.2	0.6	2	5	5	3	1.4	0.8

(1) If x = -2

(2)If x = -1

$$y = \frac{x+5}{x^2+1} \qquad y = \frac{x+5}{x^2+1}$$

$$\Rightarrow y = \frac{-2+5}{-(-2)^2+1} \qquad \Rightarrow y = \frac{-1+5}{-(-1)^2+1}$$

$$\Rightarrow y = \frac{3}{4+1} = \frac{3}{5} \qquad \Rightarrow y = \frac{-1+5}{1+1} = \frac{4}{2}$$

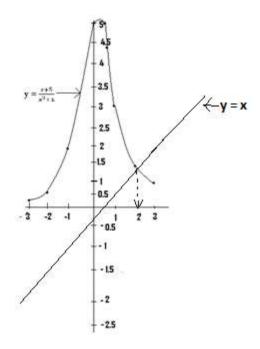
$$\Rightarrow y = 0.6 \qquad \Rightarrow y = 2$$
(3) If $x = 0.5$

$$y = \frac{x+5}{x^2+1} \qquad \Rightarrow y = \frac{x+5}{x^2+1}$$

$$\Rightarrow y = \frac{0.5+5}{(0.5)^2+1} \qquad \Rightarrow y = \frac{2+5}{(2)^2+1}$$

$$\Rightarrow y = \frac{5.5}{1.25} = \frac{3}{1.25} \qquad \Rightarrow y = 4.4 \qquad \Rightarrow y = 1.4$$

(b)



(c) From the graph, the greatest value of $\frac{x+5}{x^2+1}$ is around or about 5.

(d) To draw the graph of y = x, we first construct a table.

y = x

Y 0 1	2

(1) If x = 1

(2)If x = 0

(3) If x = 2

$$y = x$$
$$=> y = 1$$

$$y = x$$
$$=> y = 0$$

$$y = x$$
$$=> y = 2$$

From
$$\frac{x+5}{x^2+1} = x \implies y = \frac{x+5}{x^2+1} = x$$
,

$$\Rightarrow$$
 y = x.

We therefore draw the line y = x (which we've already drawn), and where it cuts the graph, the corresponding x value or values are taken.

the truth set = $\{x: x = 1.5\}$.

N:B – Ordinate refers to the y – axis,

- Abscissa refers to the x axis.
- (Q2) (i) Plot the graphs of $y = \frac{-2x+2}{-x^2-1}$ and y = 2x for $-2 \le x \le 3$ on the same axes.
 - (ii) Determine the minimum or maximum value of the graph.
 - (iii) Find the values of x for which $\frac{-2x+2}{-x^2-1} = 2x$.

Soln:

(i)

X	-2	-1	0	1	2	3
Y	-1.2	-2	-2	0	0.4	0.4

(1) If
$$x = -2$$

$$y = \frac{-2x+2}{-x^2-1}$$

$$=> y = \frac{-2(-2)+2}{-(-2)^2-1}$$

$$=> y = \frac{4+2}{-(4)-1}$$

$$=> y = \frac{6}{-5} = -1.2$$

(2) If
$$x = -1$$

$$y = \frac{-2x+2}{-x^2-1}$$

$$\Rightarrow y = \frac{-2(-1)+2}{-(-1)^2-1}$$

$$\Rightarrow y = \frac{2+2}{-(1)-1}$$

$$\Rightarrow y = \frac{4}{-2} = -2$$

(3) If
$$x = 0$$
, $y = \frac{-2x+2}{-x^2-1}$
=> $y = \frac{-2(0)+2}{-(0)^2-1}$
=> $y = \frac{-2(0)+2}{-(0)^2-1}$

$$=> y = \frac{0+2}{-(0)-1}$$
$$=> y = \frac{2}{-1} = -2'$$

(4) If
$$x = 2$$

$$y = \frac{-2x+2}{-x^2-1}$$

$$\Rightarrow y = \frac{-2(2)+2}{-(2)^2-1}$$

$$\Rightarrow y = \frac{-4+2}{-(4)-1}$$

$$=> y = \frac{-2}{-5} = 0.4.$$

Next we construct a table for the relation y = 2x, which is a straight line graph.

$$y = 2x$$

X	0	1	2
Y	0	2	4

- (1) If x = 0

(3) If x = 2

y = 2x

(2) If x = 1y = 2x

y = 2x

y = 2(0)

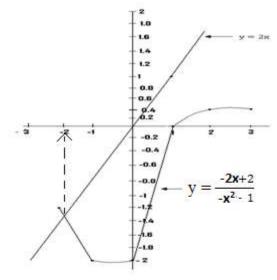
y = 2(1)

y = 2(2)

y = 0

y = 2

y = 4



- (ii) From the graph drawn, the minimum value is -2 (with reference to the y-axis).
- (iii) $y = \frac{-2x+2}{-x^2-1}$

From
$$\frac{-2x+2}{-x^2-1} = 2x$$

$$=> y = \frac{-2x+2}{-x^2-1} = 2x$$

$$=> y = 2x$$
.

We therefore draw the line y = 2x (which has already been drawn), and at the point where it cuts the graph, the corresponding x component or value is determined.

Truth set = $\{x: x = -2\}$ approx.

N/B: - The value of x for which $\frac{-2x+2}{-x^2-1} = 2x$ is the same as the value of x which satisfies simultaneously the equation $\frac{-2x+2}{-x^2-1} = 2x$.

- Before this value can be had, then the two graphs must be plotted on the same axes, or on the same graph sheet, even if we are not told to do so in the question.
- (Q3) (i) On the same axes, plot the graphs of $y = \frac{3x^2+1}{x+1}$ and $y = \frac{2x^2-6}{x^2-2} + 5$ for $-5 \le x \le 6$.
- (ii) Using your graphs, determine the value of x for which $\frac{2x^2-6}{x^2-2} = \frac{3x^2+1}{x+1}$.

Soln:

Table one:

$$y = \frac{3x^2 + 1}{x + 1}$$

X	-5	-4	-3	-2	-1	0	1	2	3	4	5	6
y	-19	-16.3	-14	-13	0	1	2	4.3	7	9.8	12.7	15.6

(1) If
$$x = -4$$

$$y = \frac{3x^2 + 1}{x + 1}$$

$$=> y = \frac{3(-4)^2+1}{-4+1}$$

$$=> y = \frac{3(16) + 1}{-3}$$

$$=> y = \frac{48 + 1}{-3}$$

$$=> y = \frac{49}{-3}$$

$$=> y = -16.$$

(2) If
$$x = -3$$

$$y = \frac{3x^2 + 1}{x + 1}$$

$$=> y = \frac{3(-3)^2+1}{-3+1}$$

$$=> y = \frac{3(9)+1}{-2}$$

$$=> y = \frac{27+1}{-2}$$

$$=> y = \frac{28}{-2}$$

$$=> y = -14.$$

(3) If
$$x = 2$$

$$y = \frac{3x^2 + 1}{x + 1}$$

$$=> y = \frac{3(2)^2 + 1}{2 + 1}$$

$$=> y = \frac{3(4)+1}{3}$$

$$=> y = \frac{12+1}{3}$$

$$=> y = \frac{13}{3}$$

=> y = 4.3
(4) If x = 6

$$y = \frac{3x^2 + 1}{x + 1}$$
=> y = $\frac{3(6)^2 + 1}{6 + 1}$
=> y = $\frac{3(36) + 1}{7}$
=> y = $\frac{108 + 1}{7}$
=> y = $\frac{109}{7}$

=> y = 15.6

Table two:

$$y = \frac{2x^2 - 6}{x^2 - 2} + 5$$

X		-5	- 4	-3	-2	-1	0	1	2	3	4	5	6
У	7	6.8	6.8	6.7	6	9	8	9	6	6.7	6.9	7	6.9

(1) If
$$x = -5$$

$$y = \frac{2x^2 - 6}{x^2 - 2} + 5$$

$$= y = \frac{2(-5)^2 - 6}{(-5)^2 - 2} + 5$$

$$= y = \frac{2(25) - 6}{25 - 2} + 5$$

$$= y = \frac{50 - 6}{23} + 5$$

$$= y = \frac{44}{23} + 5$$

$$= y = 1.8 + 5$$

$$= y = 6.8$$

(2) If
$$x = -2$$

$$y = \frac{2x^2 - 6}{x^2 - 2} + 5, \Rightarrow y = \frac{2(-2)^2 - 6}{(-2)^2 - 2} + 5$$

$$\Rightarrow y = \frac{2(4) - 6}{4 - 2} + 5$$

$$\Rightarrow y = \frac{8 - 6}{2} + 5$$

$$\Rightarrow y = \frac{2}{2} + 5$$

$$\Rightarrow y = 1 + 5$$

$$\Rightarrow y = 6.$$

(3) If
$$x = 3$$

$$y = \frac{2x^2 - 6}{x^2 - 2} + 5$$

$$= y = \frac{2(3)^2 - 6}{(3)^2 - 2} + 5$$

$$= y = \frac{2(9) - 6}{9 - 2} + 5$$

$$= y = \frac{18 - 6}{7} + 5$$

$$=> y = \frac{12}{7} + 5$$

 $=> y = 1.7 + 5$
 $=> y = 6.7$

(4) If
$$x = 6$$

$$y = \frac{2x^2 - 6}{x^2 - 2} + 5$$

$$= y = \frac{2(6)^2 - 6}{(6)^2 - 2} + 5$$

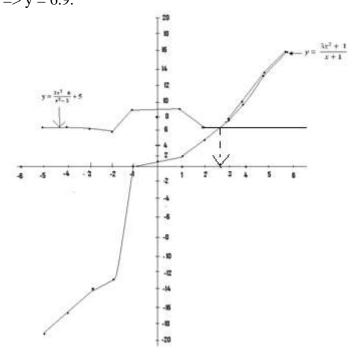
$$= y = \frac{2(36) - 6}{36 - 2} + 5$$

$$= y = \frac{72 - 6}{34} + 5$$

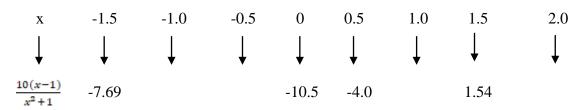
$$= y = \frac{66}{34} + 5$$

$$= y = 1.9 + 5$$

$$= y = 6.9.$$



- (ii) The two graphs are equal i.e. $\frac{2x^2-6}{x^2-2} = \frac{3x^2+1}{x+1}$ at their points of intersection and the corresponding x value is x = 2.5 approx.
- (Q4) (a) Copy and complete the table for the mapping $x \longrightarrow \frac{10(x-1)}{x^2+1}$



(b) Using a scale of 2cm to 0.5 units on the x – axis and 2cm to 2 units on the other axis, draw the graph of the mapping within the interval -1.5 \leq x \leq 2.0.

(c) From your graph, determine the minimum value of $\frac{10(x-1)}{x^2+1}$.

N/B: (1)
$$x \rightarrow \frac{10(x-1)}{x^2+1} = y = \frac{10(x-1)}{x^2+1}$$
.

(2) Decimals can be approximated to whole numbers. For example 2.71 can be approximated to be equal to 3. Decimals such as 4.46 can be approximated to 4.5 and 7.69 can either be approximated to 8 or 7.7.

Soln:

(1) If
$$x = -1$$

$$y = \frac{10(x-1)}{x^2+1}$$

(2) If
$$x = -0.5$$

$$y = \frac{10(x-1)}{x^2+1}$$

(3) If
$$x = 1$$

$$y = \frac{10(x-1)}{x^2+1}$$

$$=> y = \frac{10(-1-1)}{(-1)^2+1}$$

$$=> y = \frac{10(-0.5 - 1)}{(-0.5)^2 + 1}$$

$$=> y = \frac{10(1-1)}{(1)^2+1}$$

$$=> y = \frac{10(-2)}{1+1}$$

$$=> y = \frac{10(-2)}{1+1}$$
 $=> y = \frac{10(-1.5)}{0.25+1}$ $=> y = \frac{10(0)}{2}$

$$=> y = \frac{10(0)}{2}$$

$$=> y = \frac{-20}{2} = -10$$

$$=> y = \frac{-20}{2} = -10$$
 $=> y = \frac{-15}{1.25} = -11.5$ $=> y = \frac{0}{2} = 0$

$$=> y = \frac{0}{2} = 0$$

(4) If
$$x = 2$$

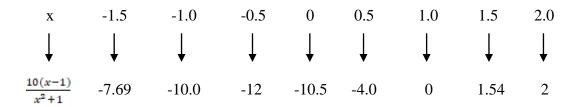
$$y = \frac{10(x-1)}{x^2 + 1}$$

$$=> y = \frac{10(2-1)}{(2)^2+1}$$

$$=> y = \frac{10(1)}{4+1}$$

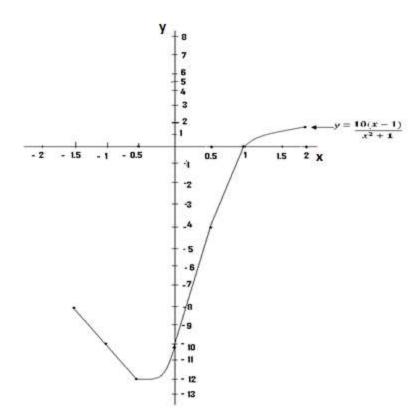
$$=> y = \frac{10}{5}$$

$$=> y = 2.$$



N/B: Since $y = \frac{10(x-1)}{x^2+1}$, the above table is the same as the next given table, in which the approximation of certain decimals have taken place.

X	-1.5	-1.0	-0.5	0	0.5	1.0	1.5	2.0
Y	-8	-10.0	-12	-11	-4.0	0	1.5	2



(c) From the graph, the minimum value of $\frac{10(x-1)}{x^2+1}$ = the lowest value of y = -12.

(Q5) Copy and complete the table for values for the relation $y = \frac{2x(x-1)}{x+3}$ for $-1 \le x \le 6$.

(i) Using a scale of 2cm = 1 unit on both axes, draw the graph of $y = \frac{2x(x-1)}{x+3}$

(ii) Use it to find the values of x for which y is negative.

(iii)

X	-1	0	0.5	1	2	3	4	5	6
2x(x-1)		0	-0.5				24	40	60
x + 3		3	3.5				7	8	9
$\frac{2x(x-1)}{x+3}$		0	-0.14				3.43	5	6.7

If
$$x = -1$$

(2) If
$$x = 2$$

(3) If
$$x = 3$$

$$2x(x-1) =$$

$$2x(x-1) = 2(2)\{2-1\}$$

$$2x(x-1)=2(3){3-1}$$

$$2(-1)\{-1-1\}=2(-1)\{-2\}$$
 = $2(2)\{1\}$

$$= 2(2)\{1\}$$

$$= 2(3)(2)$$

$$= -2(-2) = 4$$

$$= 4(1) = 4$$

$$= 6(2) = 12$$

$$x + 3 = -1 + 3 = 2$$

$$x + 3 = 2 + 3 = 5$$

$$x + 3 = 3 + 3 = 6$$

$$\frac{2x(x-1)}{x+2} = \frac{4}{2} = 2.$$

$$\frac{3x(x-1)}{x+3} = \frac{4}{5} = 0.8.$$

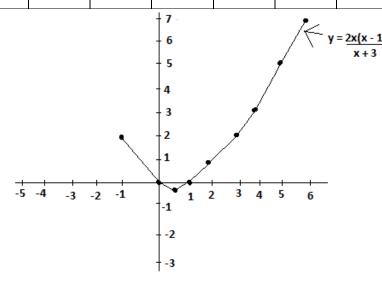
$$\frac{2x(x-1)}{x+3} = \frac{12}{6} = 2.$$

X	-1	0	0.5	1	2	3	4	5	6
2x(x-1)	4	0	-0.5	0	4	12	24	40	60
x + 3	2	3	3.5	4	5	6	7	8	9
$\frac{2x(x-1)}{x+3}$	2	0	-0.14	0	0.8	2	3.43	5	6.7

N/B: Since y = $\frac{2x(x-1)}{x^2}$,

then this table can be represented as shown next, and certain decimals have been approximated.

X	-1	0	0.5	1	2	3	4	5	6
Y	2	0	-0.1	0	0.8	2	3	5	7



(II) y is negative when the graph falls below the x-axis, and this occurs when x is from 0 to 1.

Cubic Curves (graphs):

- A cube curve or graph is the type of graph we get, when the x value is cubed or raised to the third power within the equation of a graph.
- Apart from the raising the x value to the third power, the way and manner of handling cubic curves is similar to that of the quadratic graph.

(Q1)

X	-2.5	-2.0	-1.5	-1	-0.5	0.0	0.5	1.0	1.5	2.0	2.5

Y	-3.1		4	2.4	-2.4	-4.1	3.1

- (a) Copy and complete the given table for the relation $y = x^3 5x$.
- (b) Using a scale of 2cm to 1 unit on the x-axis, and 2cm to 2 units on the y axis, draw the graph of $y = x^3 - 5x$ for $-2.5 \le x \le 2.5$, and determine its least value.
- (c) From your graph, find the truth set of $(x^3 5x) = -1$.
- (d) On the same axes, draw the line y = x and determine the truth set of $x^3 6x = 0$. Soln:

X	-2.5	-2.0	-1.5	-1	-0.5	0.0	0.5	1.0	1.5	2.0	2.5
Y	-3.1	2	4.1	4	2.4	0	-2.4	-4	-4.1	-2	3.1
If $\mathbf{x} = -$	If $x = -2$ (2) If $x = -1.5$				(3) If $x = 0$ (4) If $x = 2$)		

$$(2)$$
 If $x = -1.5$

(3) If
$$x = 0$$

(4) If
$$x = 2$$

$$v = x^3 - 5x$$

$$y = x^3 - 5x$$
 $y = x^3 - 5x$ $y = x^3 - 5x$ $y = x^3 - 5x$

$$y = x^3 - 5x$$

$$y - y^3 - 5y$$

$$=> y = (-2)^3 - 5(-2)$$
 $=> y = (-1.5)^3 - 5(-1.5)$ $=> y = (0)^3 - 5(0)$ $=> y = (2)^3 - 5(2)$

$$\Rightarrow$$
 $y = (0)^3 - 5(0) \Rightarrow y = (2)^3 - 5(2)$

$$=> y = (-8) + 10$$

$$=> y = -3.4 + 7.5$$

$$=> y = (-8) + 10$$
 $=> y = -3.4 + 7.5$ $=> y = 0 - 0$ $=> y = 8 - 10$

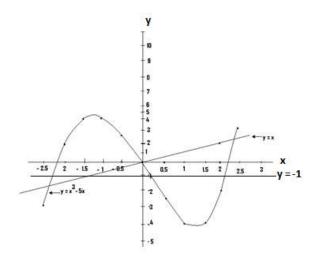
$$=> y = -8 + 10$$
 $=> y = 4.1$

$$=> y = 4.1$$

$$=> y = 0$$

$$=> y = 0$$
 $=> y = -2$

$$=> y = 2$$



From the graph, the least value is -4.

(c)
$$(x^3 - 5x) = -1$$
. Since $y = (x^3 - 5x)$. $\Rightarrow y = x^3 - 5x = -1$,

=> y = -1, we therefore draw the line y = -1, and at the points that is cuts the graph or curve, we determine the corresponding x values.

Truth set = $\{ x : x = -2.3, x = 0.2 \text{ or } x = 2.2 \}$ approx.

$$y = x$$

X	-1	0	2
Y	-1	0	2

(1) If
$$x = -1$$
, $y = -1$

(2) If
$$x = 0$$
, $y = 0$

(3) If
$$x = 2$$
, $y = 2$

(e) The given equation is $x^3 - 6x = 0$, but that of the graph is $y = x^3 - 5x$.

Consider $x^3 - 6x = 0$. Add x to both sides => $x^3 - 6x + x = 0 + x => x^3 - 5x = x$

=> $y = x^3 - 5x = x$, => y = x. We therefore draw the line y = x (which has been already drawn) and where it cuts the graph, the corresponding x values are determined. Required truth set = { x: x = -2.4, x = 0 or x = 2.3 }.

(Q2) (a) Copy and complete the table for the relation $y = x^3 - 12x + 3$, for $-2.5 \le x \le 2.5$.

X	-2.5	-2	-1.5	-1	-0.5	0	0.5	1.0	1.5	2	2.5
Y	17.4			14		3		-8.9	-11		-11.3

- (c) Draw the graph or the curve for the given relation.
- (d) Determine the greatest or the minimum value of y.
- (e) Find the truth set of $x^3 12x + 3 = 0$.

Soln:

X	-2.5	-2	-1.5	-1	-0.5	0	0.5	1.0	1.5	2	2.5
Y	17.4	19	17.6	14	8.9	3	-2.8	-8.9	-11	-13	-11.3

(1) If
$$x = -2$$

(2) If
$$x = -1.5$$

$$y = x^3 - 12x + 3$$

$$y = x^3 - 12x + 3$$

$$=> y = (-2)^3 - 12(-2) + 3$$

$$=> y = (-1.5)^3 - 12(-1.5) + 3$$

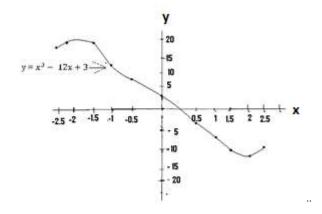
$$=> y = -8 + 24 + 3$$

$$=> y = -3.4 + 18 + 3$$

$$=> y = 19$$

$$=> y = 17.6.$$

(b)



(c) From the graph, the minimum value of y is y = -13 and the greatest value of y is 19.

(d) The equation of the curve is $y = x^3 - 12x + 3$. From the given equation, $x^3 - 12x + 3 = 0$, $\Rightarrow y = x^3 - 12x + 3 = 0$, $\Rightarrow y = 0$ (which is the same as the x-axis). We therefore determine the x value or values at the points or point where the graph cuts the x-axis.

The required truth set = $\{x : x = 0.3\}$.

Other forms of graphs:

(Q1) The following is an incomplete table for the relation $\frac{y}{x+1} = 3 - x$ for $-2 \le x \le 3.5$.

X	-2	-1	0	1	1.5	2	2.5	3	3.5
Y		0	3	4			1.75		-2.25

- (i) Copy and complete the given table.
- (ii) Using 2cm as 1 unit on both axes draw the graph of the relation for the given interval.
- (iii)Use your graph to find:
 - (a) the truth set of (x+1)(x-3) = -1.
 - (b) the greatest value of y and the value of x for which is occurs.

N/B: - As already mentioned, before any graph is plotted, we must first make y the subject of the given equation.

- From $\frac{y}{x+1} = 3 x => y = (3-x)(x+1)$.
- We therefore plot the graph of y = (3-x)(x+1).
- In multiplication, when there is a negative or a positive sign between a number and a letter, we must introduce the bracket sign as we have just done.

Example(1):
$$\frac{y}{x-1} = 2 \Rightarrow y = 2(x-1) \Rightarrow y = 2x - 2$$
.

Example (2):
$$\frac{y}{2+x} = x - 1 => y = (2 + x) (x - 1).$$

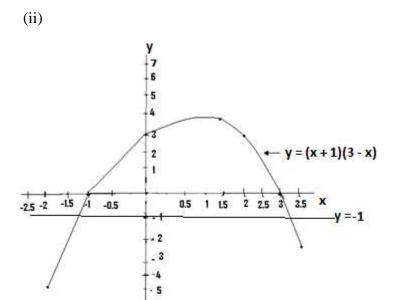
Soln:

(i)

$$y = (x+1)(3-x)$$

X	-2	-1	0	1	1.5	2	2.5	3	3.5
Y	-5	0	3	4	3.8	3	1.75	0	-2.25

(1) If
$$x = -2$$
 (2) If $x = 1.5$ $y = (x+1)(3-x)$ $=> y = \{(-2) + 1\} \{3-(-2)\}$ $=> y = (-2+1)(3+2)$ $=> y = (-1)(5)$ $=> y = -5$.



(iii)

(a) y = (x+1)(3-x) is the equation of the graph.

From (x+1)(3-x) = -1 => y = (x+1)(3-x) = -1, => y = -1.

Draw the line y = -1 and at the points where it cuts the graph, determine the corresponding x components.

Truth set = $\{x : x = -1.2 \text{ or } x = 3.2\}$ approx.

(b) From the graph, the greatest value of y is 4, and occurs when x = 1.

(Q2)(a) Copy and complete the table for the relation (x-1)(y-1) = 6 for $2 \le x \le 7$.

X	2	2.5	3	4	5	6	7
Y	7			3			2

(b) Using a scale of 2cm to 1 unit on both axes, draw the graphs of (x-1)(y-1) = 6 and x + y = 8 within the given interval.

(c) Using your graph, find the truth set of the simultaneous equations (x - 1)(y - 1) = 6 and x + y = 08.

Soln:

(a)

N/B:: Considering (x-1)(y-1) = 6, first make y the subject by dividing through using (x-1), and (y-1) will be left on the left hand side of the equation/. The -1 found on the left hand side is then made to cross the equal to sign and this changes to +1. The y is then left alone on the left hand side of the equation.. This is illustrated below:

Table one:

$$y = \frac{6}{(x-1)} + 1$$

X	2	2.5	3	4	5	6	7
Y	7	5	4	3	2.5	2.2	2

From (x - 1)(y - 1) = 6, divide through using (x-1)

$$=>\frac{(x-1)(y-1)}{(x-1)} = \frac{6}{(x-1)} => y-1 = \frac{6}{(x-1)}$$

$$=> y = \frac{6}{(x-1)} + 1.$$

(1) If
$$x = 2.5$$

(2) If
$$x = 3$$

(3) If
$$x = 6$$

$$y = \frac{6}{(x-1)} + 1$$
 $y = \frac{6}{(x-1)} + 1$

$$y = \frac{6}{(r-1)} + 1$$

$$y = \frac{6}{(x-1)} + 1$$

$$=> y = \frac{6}{(2.5-1)} + 1$$
 $=> y = \frac{6}{(3-1)} + 1$ $=> y = \frac{6}{(6-1)} + 1$

$$=> y = \frac{6}{(3-1)} + 1$$

$$=> y = \frac{6}{(6-1)} + 1$$

$$=> y = \frac{6}{1.5} + 1 = 4 + 1 \qquad => y = \frac{6}{2} + 1 = 3 + 1 \qquad => y = \frac{6}{5} + 1 = 1.2 + 1$$

$$=> y = \frac{5}{2} + 1 = 3 + 1$$

$$=> y = \frac{6}{5} + 1 = 1.2 + 1$$

$$=> y = 5.$$

$$=> y = 4$$

$$=> y = 2.2.$$

Table (2)

$$y = 8 - x$$

X	2	2.5	3	4	5	6	7
Y	6			4			1

From $x + y = 8 \Rightarrow y = 8 - x$. Since this is a straight line graph, we compute only three values of y.

(1) If
$$x = 2$$

(2) If
$$y = 4$$

(3) If
$$x = 7$$

$$y = 8 - x \qquad \qquad y = 8 - x$$

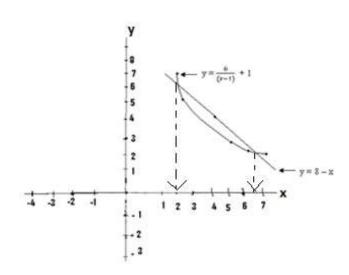
$$v = 8 - x$$

$$y = 8 - x$$

$$=> y = 8 - 2$$
 $=> y = 8 - 4$

$$=> y = 8 - 4$$

$$=> y = 8 - 7$$



(c)For the required truth set, we fist locate the points of intersection of the graphs, and determine their corresponding x components. Truth set= $\{x : x = 2 \text{ or } x = 6.2\}$ approx.

(Q3) Copy and complete the table for the relation $y = 4 + \frac{1}{2}x - \frac{1}{3}x^2$ for $-3 \le x \le 4$.

X	-3	-2	-1	0	1	2	3	4
X		1.7	3.2		4.2	3.7		0.7

(i) Draw the graph for the relation $y = 4 + \frac{1}{2}x - \frac{1}{3}x^2$.

What is the

- (ii) the equation of the line of symmetry of your graph.
- (iii) truth set of $24 + 3x 2x^2 = 0$.

(i)
$$y = 4 + \frac{1}{2}x - \frac{1}{3}x^2$$

X	-3	-2	-1	0	1	2	3	4
X	-0.5	1.7	3.2	4	4.2	3.7	2.5	0.7

N/B: $y = 4 + \frac{1}{2}x - \frac{1}{3}x^2$ is the same as $y = -\frac{1}{3}x^2 + \frac{1}{2}x + 4$.

(1) If
$$x = -3$$

(2) If
$$x = 0$$

(3) If
$$x = 3$$

$$y = 4 + \frac{1x}{2} - \frac{1}{3}x^2$$

$$y = 4 + \frac{1}{2}x - \frac{1}{2}x^2$$

$$y = 4 + \frac{1}{2}x - \frac{1}{3}x^2$$
 $y = 4 + \frac{1}{2}x - \frac{1}{3}x^2$

$$=> y = 4 + \frac{1}{2}(-3) - \frac{1}{3}(-3)^2$$

$$=> y = 4 + \frac{1}{2}(-3) - \frac{1}{3}(-3)^2 \qquad \qquad => y = 4 + \frac{1}{2}(0) - \frac{1}{3}(0)^2 \quad => y = 4 + \frac{1}{2}(3) - \frac{1}{3}(3)^2$$

$$=> y = 4 - \frac{3}{2} - \frac{1}{3}(9)$$

$$=> y = 4 + 0 - 0$$

$$=> y = 4 + 0 - 0$$
 $=> y = 4 + 1.5 - \frac{1}{3}(9)$

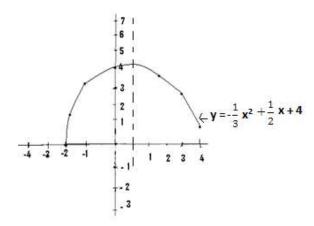
$$=> y = 4 - 1.5 - 3$$

$$=> y = 4$$

$$=> y = 5.5 - 3$$

$$=> y = -0.5$$

$$=> y = 2.5$$



- (ii) From the graph, the line of symmetry is x = 0.5 approx.
- (iii) The equation of the graph is $y = 4 + \frac{1}{2}x \frac{1}{3}x^2$

The given equation is $24 + 3x - 2x^2 = 0$.

In order to convert this equation to be in line with that of the graph, we use 6 to divide.

$$=>\frac{24}{6}+\frac{3x}{6}-\frac{2x^2}{6}=\frac{0}{6}=>y=4+\frac{1}{2}x-\frac{1}{3}x^2=0,$$

 $=> y = 4 + \frac{1}{2}x - \frac{1}{3}x^2 = 0$, => y = 0 (which is the x - axis). The truth set occurs at the point or points where the graph cuts the x - axis.

Truth set = $\{ x : x = -2.5 \}$.

- (Q4) (a) Copy and complete the table for the relation y = x (12 x) (8-x) for $0 \le x \le 8$.
- (b) Plot the graph for the given relation.
- (c)Determine the equation of the line of symmetry.

X	0	1	2	3	4	5	6	7	8
12 – x	12	11			8			5	
8 – x	8	7			4			1	
x(12-x)(8-x)	0	77			128			35	

(1) If
$$x = 2$$

(2) If
$$x = 3$$

(3) If
$$x = 6$$

$$12 - x = 12 - 2 = 10$$
 $12 - x = 12 - 3 = 9$

$$12 - x = 12 - 3 = 9$$

$$12 - x = 12 - 6 = 6$$

$$8 - x = 8 - 2 = 6$$

$$8 - x = 8 - 2 = 6$$
 $8 - x = 8 - 3 = 5$

$$8 - x = 8 - 6 = 2$$

$$=> x(12-x)(8-x)$$

$$=> x(12-x)(8-x)$$

$$=> x(12-x)(8-x)$$
 $=> x(12-x)(8-x)$

$$= 2(10)(6)$$

$$=3(9)(5)$$

$$=6(6)(2)$$

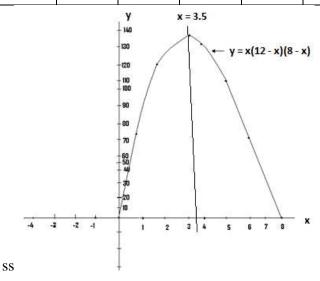
$$=120$$

$$= 72$$

X	0	1	2	3	4	5	6	7	8
12 – x	12	11	10	9	8	7	6	5	4
8 – x	8	7	6	5	4	3	2	1	0
x(12-x)(8-x)	0	77	120	135	128	105	72	35	0

N/B: Since y = x(12 - x)(8-x), this table can be represented or is the same as the next one given.

X	0	1	2	3	4	5	6	7	8
Y	0	77	120	135	128	105	72	35	0



(d) The equation of the line of symmetry is x = 3.5.

(Q5)(a) Copy and complete the following table for the relation $y = 5 - (x - 2)^2$ for the interval $-2 \le x \le 6$.

X	-2	-1	0	1	2	3	4	5	6
Y	-11		1		5		1		-11

(b) Using a scale of 2cm to 1 unit on the x- axis and 2cm to 2 units on the y- axis, draw the graph of the given relation.

(c)Draw on the same axes the line 2x - y - 3 = 0.

(d) Use your graphs to find

(i) the co-ordinates of the turning point of $y = 5 - (x-2)^2$

(ii) the equation of the axis of symmetry of 5 - (x-2).

(iii) the truth set of

(a)
$$7 - (x-2)^2 = 0$$
.

(b)
$$5 - (x - 2)^2 = 2x - 3$$
.

Soln:

(a)

X	-2	-1	0	1	2	3	4	5	6
Y	-11	-4	1	6	5	4	1	-4	-11

(1) If
$$x = -1$$

$$y = 5 - (x - 2)^2$$

$$=> y = 5 - (-1 - 2)^2$$

$$=> y = 5 - (-3)^2$$

 $=> y = 5 - 9$

$$=> y = -4.$$

(2) If
$$x = 3$$

$$y = 5 - (x - 2)^2$$

$$=> y = 5 - (3 - 2)^2$$

 $=> y = 5 - (1)^2$

$$\Rightarrow$$
 y = 5 - 1

$$=> y = 4.$$

(3) If
$$x = 5$$

$$y = 5 - (x - 2)^2$$

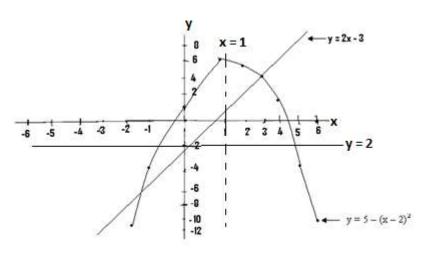
$$\Rightarrow$$
 y = 5 - (5 - 2)²

$$=> y = 5 - (3)^2$$

$$=> y = 5 - 9$$

 $=> y = -4$

(b)



N/B:

(c) To draw the line or graph of 2x - y - 3 = 0, we must first make y the subject and construct our table.

$$2x - y - 3 = 0$$

$$=> 2x - 3 = 0 + y$$

$$=> 2x - 3 = y => y = 2x - 3.$$

$$y = 2x - 3$$

X	-2	-1	0	1	2	3	4	5	6
Y	-7		-3			3			

(1) If
$$x = -2$$

(2) If
$$x = 0$$

(3) If
$$x = 3$$

$$y = 2x - 3$$

$$y = 2x - 3$$

$$y = 2x - 3$$

$$=> y = 2(-2) - 3$$

$$=> y = 2(0) - 3$$

$$=> y = 2(3) - 3$$

$$=> y = -4 - 3$$
 $=> y = 0 - 3$ $=> y = 6 - 3$ $=> y = -7$ $=> y = -3$ $=> y = 3$

- (d)(i) The co-ordinates of the turning point of $y = 5 (x 2)^2$ are (1, 6) i.e. x = 1 and y = 6.
- (ii) Equation of axis of symmetry is x = 1.
 - (iv) To find the truth set of $7 (x 2)^2 = 0$, we must first transform this equation into that of the graph i.e. $y = 5 (x 2)^2$

Consider
$$7 - (x - 2)^2 = 0$$

Subtract 2 from both sides

i.e.
$$7 - (x - 2)^2 - 2 = 0 - 2$$

$$=>7-2-(x-2)^2=-2$$

$$=> 5 - (x - 2)^2 = -2$$
, but since $y = 5 - (x - 2)^2$

$$=> y = 5 - (x - 2)^2 = -2$$

$$=> y = -2.$$

We therefore draw the line y = -2, and determine the corresponding x values at the points or point where it cuts the graph.

Required truth set = $\{x: x = -0.5 \text{ or } x = 5\}$ approx.

(b) We are required to find the truth set of $5 - (x - 2)^2 = 2x - 3$.

Since
$$y = 5 - (x - 2)^2$$

$$=> y = 5 - (x - 2)^2 = 2x - 3$$

$$=> y = 2x - 3$$

We draw the line y = 2x - 3, which we have already drawn and determine the corresponding x components at the points where it cuts the graph.

Therefore truth set = $\{x: x = -1.5 \text{ or } x = 3\}$ approx.

(Q6)

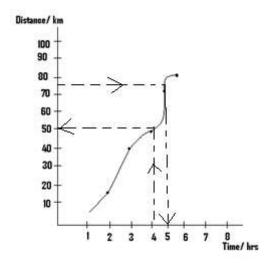
Dist/ km	10	15	40	45	70	80	85
Time/ hrs	1	2	3	4	5	6	7

The given table shows the distance travelled by a car, with respect to time.

- (i) Represent this on a graph.
- (ii) Using your graph, determine the distance travelled when the time is $4\frac{1}{2}$ hours.
- (iii)If the distance travelled is 75km, find the time.

Soln:

(i)



- (ii) Form the graph, the distance travelled in $4\frac{1}{2}$ hrs is 50km.
 - (iv)From the graph, when the distance travelled is 75km, the time is 5hrs.

N/B: The variable with the constant interval is plotted usually on the x - axis unless otherwise stated.

Q7)

Temp/ ⁰ C	5	10	15	20	25	30
Mass/ kg	10	15	60	65	100	110

The given table shows the manner in which the temperature of a body varies with its mass.

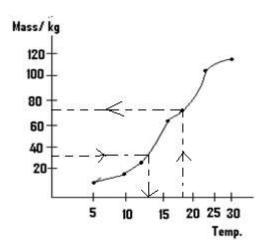
- (i) Represent this graphically.
- (ii) From the graph, determine the temperature when the mass of the body is 30kg.
- (iii)At what mass will the temperature be 17°C.

N/B: Since temperature has a constant or the same interval, it is plotted on the x-axis.

- If the interval is time, then we must plot it on the x - axis.

Soln:

(i)



- (ii) From the graph, when the mass is 30kg, the temperature is 12°C.
- (iii) When the temperature is 17^{0} C, then the mass is 70kg.

(Q8)

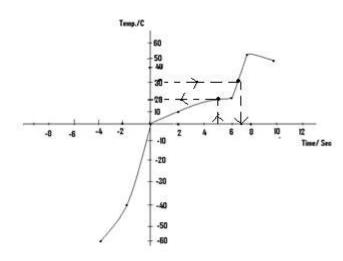
Temp/ ⁰ C	-60	-40	0	10	15	20	50	40
Time/ sec	-4	-2	0	2	4	6	8	10

The variation of temperature with time of a substance is shown in the given table.

- (a) Represent this on a graph.
- (b) At what temperature will the time be 5 seconds?
- (c) At what time will the temperature be 30° C.

Soln:

(a)



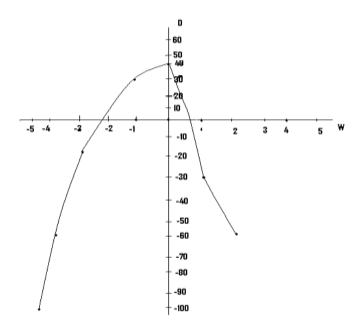
- (b) When the time is 5 seconds, the temperature is $20^{\circ}c$.
- (c) When the temperature is 30° C, the time is 61sec.

(Q9)

W	D
-5	-100
-4	-60
-3	-20
-2	0
-1	30
-0	40
1	-30
2	-60

The given table shows the way and manner the variable W, varies another one, D represents this on a graph.

Soln:



Questions:

(Q1) (a) Construct a table for the relation $y = 3x^2 + 4x - 3$ for $-6 \le x \le 5$.

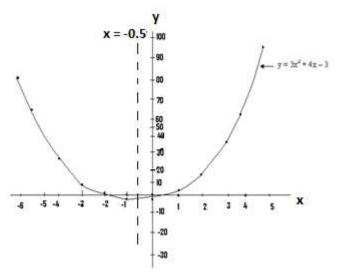
(b) Plot the graph of the given relation.

(c) Determine the maximum or the minimum value of your graph.

(d) Determine the equation of the line of symmetry.

Ans:

(a)

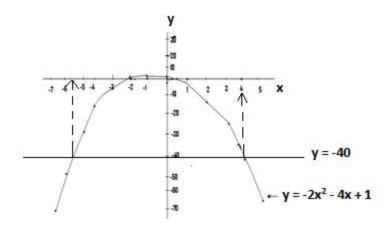


- (b) The minimum value of the graph is -4.
- (c) The equation of the line of symmetry is x = -0.5
- (d) (Q2) (a) Construct a table for the relation $y = -2x^2 4x + 1$ for $-7 \le x \le 5$.
- (b) Plot the graph of the given relation.
- (c) Determine the maximum or minimum value of your graph.
- (d) Using your graph, find the truth set of $-2x^2 4x + 1 = -40$

Ans:

 $Y = -2x^2 - 4x + 1$ (a)

X	-7	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5
Y	-69	-47	-29	-15	-5	1	3	1	-5	-15	-29	-47	-69



- (b) From the graph, the maximum value is 3.
- (c) Truth set = $\{x \mid x = -5.5 \text{ or } x = 4\}$ approx.
- (Q3)(a) Using the same axes, plot the graphs of $y = x^2 5$ and y 5x = 0 for $-7 \le x \le 7$.
- (b) Use your graph to find the truth set of $5x = -x^2 5$

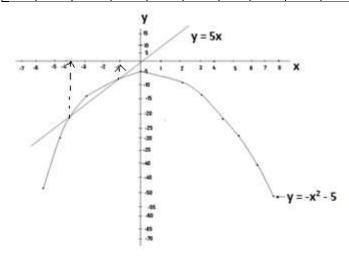
Ans:

(a) $y = -x^2 - 5$

ω,	J	71														
	X	-7	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6	7
•	у	-54	-41	-30	-21	-14	-9	-6	-5	-6	-9	-14	-21	-30	-41	-54

y = 5x

X	-7	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6	7
У								0	5		15				



- (b) From the graph, the required truth set = $\{x: x = -3.5 \text{ or } x = -1\}$ approx.
- (Q4)(a) On the same axes, plot the graphs of the relation $y = \frac{2x+1}{x^2-2}$, and $y = -\frac{1}{2}x + 3$ for

 $-6 \le x \le 6$.

(b) Determine the truth set of $\frac{2x+1}{x^2-2} = -\frac{1}{2}x + 3$.

Ans:

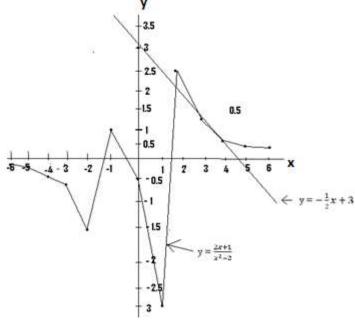
$$y = \frac{2x+1}{x^2-2}$$

(a)

X	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6
У	-0.3	-0.4	-0.5	-0.7	-1.5	1	-0.5	-3	2.5	1	0.6	0.5	0.4

$$y = -\frac{1}{2}x + 3$$

X	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6
Y							3	2.5	2				



(b) Truth set = $\{x : x = 2 \text{ or } x = 4\}$ approx.

(5)

X	-4	-3	-2.5	-2	0	0.5	2	3	4
Y	12.5				-0.5	0.4			10.5

(a) Copy and complete the given table for the relation $y = \frac{1}{4}(3x + 2)(x - 1)$ for $-4 \le x \le 4$.

(b) Plot the graph of the given relation.

(c) Draw on the same axes the graph of y + x = 0.

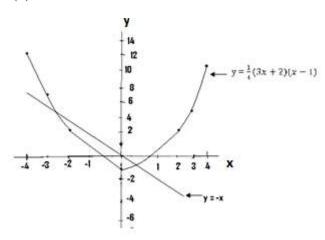
Ans:

(a)

$$y = \frac{1}{4}(3x+2)(x-1)$$

X	-4	-3	-2.5	-2	0	0.5	2	3	4
Y	12.5	7	6.6	3	-0.5	0.4	2	5.5	10.5

(b)



(Q6)(a) Copy and complete the given table for the relation $y - (3x - 1)^2 = 7$ for

 $-3 \le x \le 4$.

(b) Plot the graph of the given relation.

(c) Using your graph, determine the truth set of -73 + (3x - 1) = 0.

X	-3	-2	-1	0	1	2	3	4
Y	107				11			128

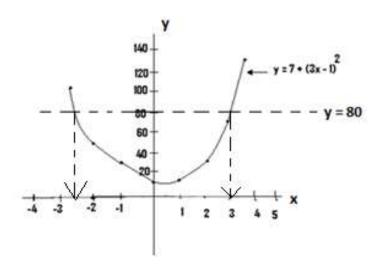
Ans:

(a)

$$y = 7 + (3x - 1)^2$$

X	-3	-2	-1	0	1	2	3	4
Y	107	56	23	8	11	32	71	128

(b)



(c) The required truth set= $\{x: x = -2.5 \text{ or } x = 3\}$ approx.

(Q7)(a) Using values of x from -2 to 4, plot on the same axes the graphs of $y = \frac{1}{2}x^2 - \frac{1}{3}x + 2$ and (2x + 1)(y - 2) = 8.

(b) Find the coordinates of the turning points of $y = \frac{1}{2}x^2 - \frac{1}{3}x + 2$

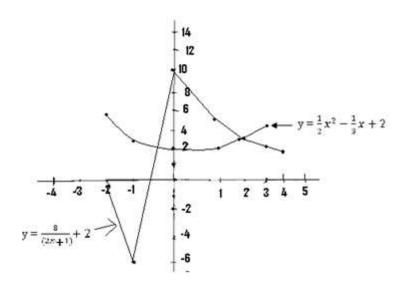
Ans:

Table (1):
$$y = \frac{1}{2}x^2 - \frac{1}{3}x + 2$$

X	-2	-1	0	1	2	3	4
Y	5.5	2.8	2	2.2	3.3	5.5	8.9

Table (2):
$$y = \frac{8}{(2x+1)} + 2$$

X	-2	-1	0	1	2	3	4
Y	-0.7	-6	10	4.7	3.6	3.1	2.9



(b) The coordinates of the turning point = (0, 2).

(Q8)

X	-6	-4	-2	0	2	4	6	7
$2x^2$	72						72	
$2x^2-4x$	96		16					
$2x^2 - 4x - 3$	93			-3	-3			67
Y	93							

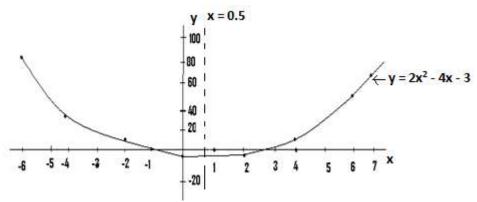
- (a) Copy and complete the given table for the relation $y = 2x^2 4x 3$.
- (b) Plot the graph of the given relation.
- (c) From your graph, determine the roots.
- (d) Write down the equation of the axis of symmetry.

Ans:

(a)

$$y = 2x^2 - 4x - 3$$

X	-6	-4	-2	0	2	4	6	7
$2x^2$	72	32	8	0	8	32	72	98
$2x^2-4x$	95	48	16	0	0	16	48	70
$2x^2 - 4x - 3$	93	45	13	0	-3	13	45	67
Y	93	45	13	-3	-3	13	45	67



- (b) The roots from the graph = $\{x : x = 2.6 \text{ or } x = -0.6\}$ approx.
- (c) The axis of symmetry is x = 0.5 approx.

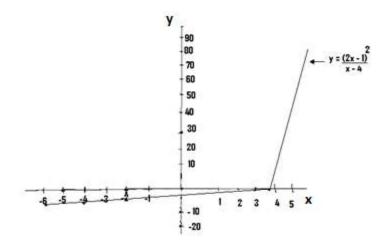
(Q9)

X	-6	-4	-2	0	1	2	4	5
2x-1	-13				1		7	9
$(2x-1)^2$	169				1		49	81
x – 4	-10				-3		0	1
$\frac{(2x-1)^2}{x-4}$	-16.9				-3		0	81

- (a) Copy and complete the given table for the relation $y = \frac{(2x-1)^2}{x-4}$ for $-6 \le x \le 6$.
- (b) Plot the graph of the given relation.

Ans:

X	-6	-4	-2	0	1	2	4	5
2x-1	-13	-9	-5	-1	1	3	7	9
$(2x-1)^2$	169	81	25	1	1	9	49	81
x – 4	-10	-8	-6	-4	-3	-2	0	1
$\frac{(2x-1)^2}{x-4}$	-16.9	-10.1	-4.2	-0.25	-0.3	-4.5	0	81



(Q10)

X	-3	-2	-1	0	1	2	3
Y	-74			-5			

- (a) Copy and complete the given table for the relation $y = 3x^3 4x 5$ for $-3 \le x \le 3$.
- (b) Plot the graph of the given relation.

Ans

a)

X	-3	-2	-1	0	1	2	3
Y	-74	-21	-4	-5	-6	11	64

