

## Theoretische Physik IX: Superstringtheorie, Exercise 87

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The Yukawa potential is given by the expression

$$\phi_Y(\mathbf{r}) = \frac{e^{-mr}}{r} \quad (1)$$

where  $r = |\mathbf{r}|$  and  $m > 0$  is the mass of the particle that mediates the potential. If photons had a rest mass, the Coulomb potential would have to be replaced by the Yukawa potential. We can see that the Coulomb potential is the limiting case of  $\phi_Y(\mathbf{r})$  in the zero-mass limit (infinite-range limit).

### 1. Proof of important statement (Written) [2pt]

In this exercise, we are going to prove the important statement

$$\int_0^1 ds s^2 + \frac{2}{3} = 1. \quad (2)$$

- a) Solve the integral by on the left hand side (you may use Mathematica).
- b) Perform the addition to show that equation (2) holds.

### 2. Proof of other important statement (Oral)

Use the trick with the commutative law to prove the “other important statement”:

$$\frac{2}{3} + \int_0^1 ds s^2 = 1 \quad (3)$$