

// Print out the prime numbers that are less than the given number.

According to Vedic mathematics (<http://vedicriver.blogspot.ca/>), it says if a number n is prime then it must satisfy this formula:

$$((2^{n-1}) \bmod n) - 1 = 0$$

Testing of the formula:

For $n = 5$, $2^4 \bmod 5 = 16 \bmod 5 = 1$. The formula is satisfied.

For $n = 13$, $2^{12} \bmod 13 = 4096 \bmod 13 = 1$. The formula is also satisfied.

For $n = 6$, $2^5 \bmod 6 = 32 \bmod 6 = 2 \neq 1$. The formula is not satisfied.

Similarly we can check for all other prime numbers.

Formula Time Complexity:

Since power and modulo operator takes constant time, the formula takes constant time to testify whether the number is prime or not. Therefore, its time complexity: $O(1)$.

Algorithm Time Complexity:

$O(N)$

Java version

```
/*
 * Check if a given number is a prime number. According to Vedic mathematics,
 * it says if a number n is prime then it must satisfy this formula:
 *  $((2^{n-1}) \bmod n) - 1 = 0$ 
 * Time complexity:  $O(1)$ 
 */
public boolean isPrime(int n) {
    return n == 2 ? true : ((int)Math.pow(2, n-1) % n) - 1 == 0;
}

/*
 * Find prime numbers that are less than the given number.
 * eg. Given number 14, yielding a prime sequence 2,3,5,7,11,13
 * Time complexity:  $O(N)$ , here  $N$  - the given number
 */
public String findPrimes(int m) {
    String result = "";
    for (int i = 2; i < m; i++) {
        if (isPrime(i)) {
```

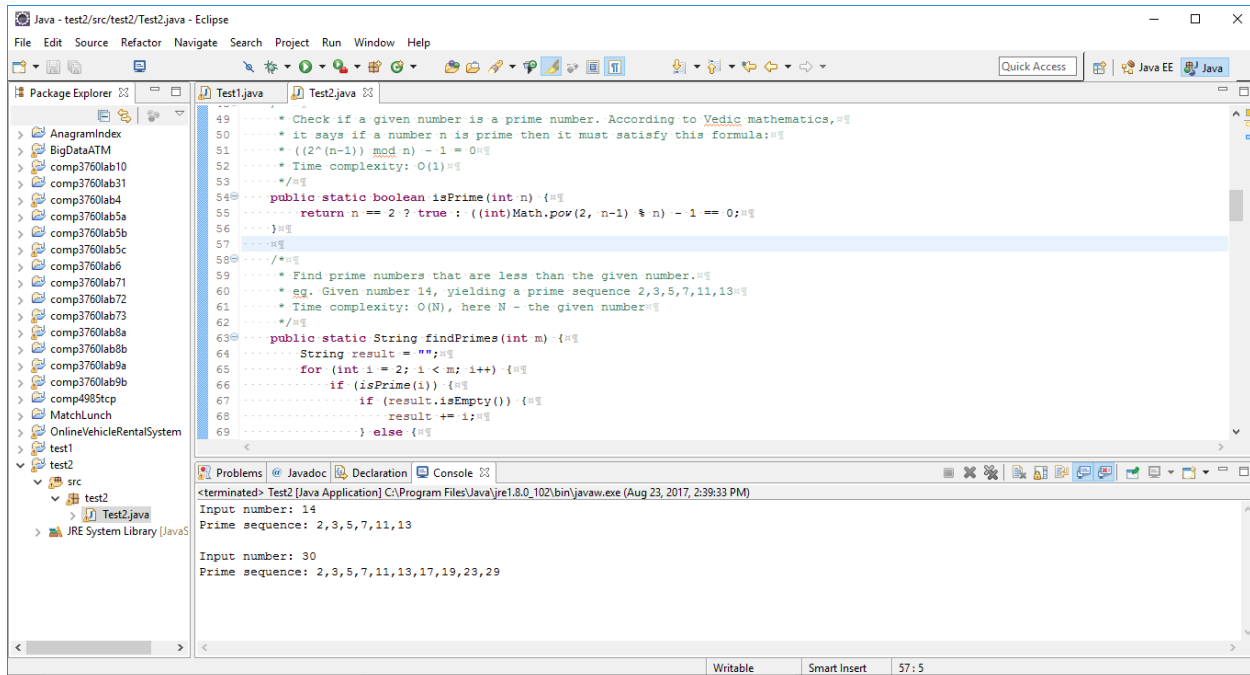
```

        if (result.isEmpty()) {
            result += i;
        } else {
            result += "," + i;
        }
    }

    return result;
}

```

Output screenshot:



C# version

```

/*
 * Check if a given number is a prime number. According to Vedic mathematics,
 * it says if a number n is prime then it must satisfy this formula:
 * ((2^(n-1)) mod n) - 1 = 0
 * Time complexity: O(1)
 */
public bool isPrime(int n)
{
    return n == 2 ? true : ((int)Math.Pow(2, n - 1) % n) - 1 == 0;
}

/*
 * Find prime numbers that are less than the given number.
 * eg. Given number 14, yielding a prime sequence 2,3,5,7,11,13
 * Time complexity: O(N), here N - the given number
 */

```

```

*/
public String findPrimes(int m)
{
    String result = String.Empty;
    for (int i = 2; i < m; i++)
    {
        if (isPrime(i))
        {
            if (String.IsNullOrEmpty(result))
            {
                result += i;
            }
            else {
                result += "," + i;
            }
        }
    }

    return result;
}

```

Output screenshot:

