AIM: Simplex technique to solve LPP and reading dual solution from the optimal table.

```
clc;
//----INPUT PARAMETERS
Noofvariables=3:
c = [-1 \ 3 \ -2]
info = [3 -1 2; -2 4 0; -4 3 8];
b = [7; 12; 10];
n= size(info,"r");
s = eye(n,n);
A = [info s b];
//disp(A);
cost= zeros(1,size(A,"c"));
cost(1:Noofvariables)= c;
//----Constrain BV
BV = Noofvariables+1:size(A,2)-1;
// -----Calculate ZjCj
Z_iC_i = cost(BV)*A - cost;
//disp(ZjCj);
ZCi = [ZiCi;A];
mprintf('\n =======\\n')
disp(['x1' 'x2' 'x3' 's1' 's2' 's3' "Sol"], [ ZCj(1:4,1),
ZCi(1:4,2),ZCi(1:4,3),ZCi(1:4,4),ZCi(1:4,5),ZCi(1:4,6),ZCi(1:4,
7)]);
//simplex table start
// check any negative value
for i = 1:size(ZiCi,"c")
if (ZiCi(i) < 0) then
  mprintf('\n The current BFS is NOT Optimal \n')
```

```
mprintf('\n ==== The NEXT ITERATION
RESULTS=====
  end
end
disp("Old Basic Variable = ");
disp(BV);
// Finding the Entering Variable
ZC = Z_iC_i(1:size(Z_iC_i, "c")-1);
[EnterCol,pvt col] = min(ZC);
    mprintf('\n The Minimum element in Zj-Cj is %d
Corresponding to Column %d \n',EnterCol,pvt col);
//Finding the Leaving Variable
sol = A(:,\$);
Column = A(:,pvt col);
z = size(Column, "r");
i=0
for i=1:size(Column,"r")
  if Column(i)<0
  j=j+1;
  end
end
// To check UNBOUNDED
disp(j);
if j == z;
  mprintf('LPP is UNBOUNDED. All entries <= 0 in
column %d \n',pvt col);
end
for i=1:size(Column,"r")
  if Column(i)>0
   ratio(i) =sol(i)./Column(i);
  else
   ratio(i)=%inf;
  end
end
```

```
[MinRatio,pvt row] = min(ratio);
mprintf('\n The Minimum Ratio Corresponding to
PIVOT Row %d \n',pvt row);
//n=pvt row
disp(['LEAVING variable is'],[BV(pvt row)]);
BV(pvt row)=pvt col;
disp(" New Basic Variable (BV)= ");
disp(BV);
//KEY ELEMENT
pvt key = A(pvt row,pvt col);
//disp(pvt key);
//UPDATE THE table for NEXT ITERATION
A(pvt row,:)=A(pvt row,:)./pvt key;
for i=1:size(A,1)
  if i~=pvt row
    A(i,:)=A(i,:)-A(i,pvt col).*A(pvt row,:);
  end
ZjCj = ZjCj-ZjCj(pvt col).*A(pvt row,:);
ZCj = [ZjCj;A];
mprintf('\n ====== Next Iteration
=====\n')
disp(['x1' 'x2' 'x3' 's1' 's2' 's3' "Sol"], [ ZCj(1:4,1),
ZCj(1:4,2),ZCj(1:4,3),ZCj(1:4,4),ZCj(1:4,5),ZCj(1:4,6),
ZCj(1:4,7)]);
end
BFS = zeros(1,size(A,2));
BFS(BV) = A(:,\$);
BFS(\$) = sum(BFS.*cost);
mprintf('\n =====The BFS is
=======\\n')
```

disp(['x1' 'x2' 'x3' 's1' 's2' 's3' "Sol"], [BFS(1,1), BFS(1,2),BFS(1,3),BFS(1,4),BFS(1,5),BFS(1,6),BFS(1,7)]);

```
Scilab 6.1.1 Console
======= Simplex Table =======
"x1" "x2" "x3" "s1" "s2" "s3" "So1"
 1. -3. 2. 0. 0. 0. 0.
 3. -1. 2. 1. 0. 0. 7.
-2. 4. 0. 0. 1. 0. 12.
    3.
        8. 0.
                 0.
                     1. 10.
 The current BFS is NOT Optimal
==== The NEXT ITERATION RESULTS=======
"Old Basic Variable = "
4. 5. 6.
The Minimum element in Zj-Cj is -3 Corresponding to Column 2
 1.
The Minimum Ratio Corresponding to PIVOT Row 2
" LEAVING variable is"
" New Basic Variable (BV) = "
 4. 2. 6.
====== Next Iteration =======
"x1" "x2" "x3" "s1" "s2" "s3" "So1"
-0.5 0. 2. 0. 0.75 0. 9.
 2.5 0. 2. 1. 0.25 0. 10.
-0.5 1. 0. 0. 0.25 0. 3.
```

```
-4. 3. 8. 0. 0. 1. 10.
======= Next Iteration =======
"x1" "x2" "x3" "s1" "s2" "s3" "So1"
-0.5 0. 2. 0. 0.75 0. 9.
    0. 2. 1. 0.25
2.5
                    0. 10.
               0.25
-0.5 1. 0. 0.
                    0. 3.
-4. 3. 8. 0.
               0. 1. 10.
====== Next Iteration =======
"x1" "x2" "x3" "s1" "s2" "s3" "So1"
        2. 0. 0.75 0. 9.
-0.5 0.
        2. 1. 0.25 0. 10.
2.5 0.
-0.5 1.
        0. 0. 0.25
                    0. 3.
-2.5 0.
        8. 0. -0.75
                    1. 1.
======The BFS is ========
"x1" "x2" "x3" "s1" "s2" "s3" "So1"
0. 3. 0. 10. 0. 1. 9.
```

AIM: Dual Simplex technique to solve LPP.

```
clc;
Variables = ['x1', 'x2', 'x3', 's1', 's2', 'Sol'];
cost = [-2 \ 0 \ -1 \ 0 \ 0 \ 0];
info = [-1 -1 1; -1 2 -4];
b = [-5; -8];
n= size(info,"r");
s = eye(n,n);
A = [info s b];
//----Finding starting BFS
BV=[];
for j=1:size(s,2)
  for i=1:size(A,2)
     if A(:,i) == s(:,j)
     BV = [BV i];
     end
  end
end
mprintf('\n Basic Variables (BV) = \n');
disp([Variables(BV)]);
Z_iC_i = cost(BV)*A - cost;
mprintf('\nZjCj = ');
disp(ZjCj);
// for print table
ZCj = [ZjCj;A];
//mprintf('\n ====== DUAL Simplex Table
 ======\n')
```

```
disp(['x1' 'x2' 'x3' 's1' 's2' "Sol"], [ ZCj(1:3,1),
ZCi(1:3,2),ZCi(1:3,3),ZCi(1:3,4),ZCi(1:3,5),ZCi(1:3,6)]);
// DUAL SIMPLEX START
RUN = 1;
while RUN
Sol = A(:,\$);
for i=1:size(Sol,2)
  if (Sol(i) < 0) then
  mprintf('\n=== The current BFS is NOT FEASIBLE ===\n')
//Finding Leaving Variable
  [LeaVal,pvt row] = min(Sol);
  mprintf('\nLeaving Row = \%d \n',pvt row);
//Finding Entering Variable
  Row = A(pvt row, 1:\$-1);
  ZJ = ZjCj(:,1:\$-1)
  for i = 1 :size(Row,2)
     if Row(i) < 0
       ratio(i) = abs(ZJ(i)./Row(i));
     else
       ratio(i) = \%inf;
     end
end
[minVAL, pvt col] = min(ratio);
mprintf('\nEntering Variable = %d \n',pvt col);
//Updating the BV
BV(pvt row) = pvt col;
mprintf('\nBasic Variables (BV) = ')
disp([Variables(BV)]);
//Update the table for Next Iteration
pvt key=A(pvt row,pvt col);
//disp(pvt key);
```

```
A(pvt row,:) = A(pvt row,:)./pvt key;
for i=1:size(A,1)
  if i~=pvt row
    A(i,:) = A(i,:)-A(i,pvt col).*A(pvt row,:);
  end
ZjCj = cost(BV)*A-cost
mprintf('\nZjCj = ');
disp(ZjCj);
//for print table
ZCj = [ZjCj;A];
mprintf('\n ====== Next Iteration =====\\n')
disp(['x1' 'x2' 'x3' 's1' 's2' "Sol"], [ ZCj(1:3,1),
ZCj(1:3,2),ZCj(1:3,3),ZCj(1:3,4),ZCj(1:3,5),ZCj(1:3,6)]);
//disp(A);
end
else
  RUN = 0;
  mprintf('\n=== The current BFS is FEASIBLE & OPTIMAL
===\n')
  end
end
end
```

```
======= Simplex Table =======
"x1" "x2" "x3" "s1" "s2" "s3" "So1"
 1. -3. 2. 0. 0. 0. 0.
 3. -1. 2. 1. 0. 0.
    4. 0. 0. 1. 0. 12.
    3. 8. 0. 0. 1. 10.
  The current BFS is NOT Optimal
==== The NEXT ITERATION RESULTS=======
"Old Basic Variable = "
 4. 5. 6.
The Minimum element in Zj-Cj is -3 Corresponding to Column 2
1.
The Minimum Ratio Corresponding to PIVOT Row 2
" LEAVING variable is"
" New Basic Variable (BV) = "
 4. 2. 6.
====== Next Iteration =======
"x1" "x2" "x3" "s1" "s2" "s3" "So1"
-0.5 0. 2. 0. 0.75 0. 9.
             1. 0.25 0. 10.
 2.5
     0. 2.
 -0.5 1. 0. 0. 0.25 0. 3.
```

```
----- Next Iteration -----
 "x1" "x2" "x3" "s1" "s2" "So1"
 1.75 0.5 0. 0. 0.25 -2.
 -1.25 -0.5 0. 1. 0.25 -7.
 0.25 -0.5
           1. 0. -0.25 2.
== The current BFS is NOT FEASIBLE ===
eaving Row = 1
ntering Variable = 2
asic Variables (BV) =
 "x2" "x3"
jCj =
 1.75 0.5 0. 0. 0.25 -2.
======= Next Iteration =======
 "x1" "x2" "x3" "s1" "s2" "So1"
 1.75 0.5 0. 0. 0.25 -2.
      1. 0. -2. -0.5 14.
 2.5
 0.25 -0.5 1. 0. -0.25 2.
jCj =
 0.5 0. 0. 1. 0.5 -9.
======= Next Iteration ========
 "x1" "x2" "x3" "s1" "s2" "So1"
 0.5 0. 0. 1. 0.5 -9.
 2.5 1. 0. -2. -0.5 14.
  1.5 0. 1. -1. -0.5 9.
```

AIM: Illustration of following special cases in LPP using Simplex Method.

UNRESTRICTED VARIABLE:

```
SOLVE LPP

Max z = x(0)1 + 3x(2)

St = x(0) + x(2) \le 2

x(0) is unrestricted

-x(0) + x(2) \le 4

x(2) >= 0

Here, x(0) = x - x(1) as
```

```
clc;
//----INPUT PARAMETERS
Noofvariables=3;
c = [1 - 1 3]
info = [1 -1 1; -1 1 1];
b = [2; 4];
n= size(info,"r");
s = eye(n,n);
A = [info s b];
//disp(A);
cost= zeros(1,size(A,"c"));
cost(1:Noofvariables)= c;
//----Constrain BV
BV = Noofvariables + 1:size(A,2) - 1;
// -----Calculate ZjCj
ZjCj = cost(BV)*A - cost;
//disp(ZjCj);
```

```
ZCj = [ZjCj;A];
//disp(ZCj);
mprintf('\n =======\n')
disp(['x' 'x1' 'x2' 's1' 's2' "Sol"], [ ZCj(1:3,1),
ZCj(1:3,2),ZCj(1:3,3),ZCj(1:3,4),ZCj(1:3,5),ZCj(1:3,6)]);
//simplex table start
// check any negative value
k=0
for i = 1:size(Z_iC_i,2)
if (ZiCi(i) < 0) then
   k=k+1
end
end
if k > 0
  mprintf('\n
              The current BFS is NOT Optimal \n')
end
disp("Old Basic Variable = ");
disp(BV);
// Finding the Entering Variable
ZC = Z_iC_i(1:size(Z_iC_i, "c")-1);
[EnterCol,pvt col] = min(ZC);
    mprintf('\n The Minimum element in Zj-Cj is %d
Corresponding to Column %d \n',EnterCol,pvt col);
//Finding the Leaving Variable
sol = A(:,\$);
Column = A(:,pvt col);
z = size(Column, "r");
i=0
for i=1:size(Column,"r")
  if Column(i)<0
  j=j+1;
  end
end
// To check UNBOUNDED
```

```
//disp(i);
if j == z;
  mprintf(' LPP is UNBOUNDED. All entries <= 0 in
column %d \n',pvt col);
end
for i=1:size(Column,"r")
  if Column(i)>0
   ratio(i) =sol(i)./Column(i);
 else
   ratio(i)=%inf;
  end
end
[MinRatio,pvt row] = min(ratio);
mprintf('\n The Minimum Ratio Corresponding to PIVOT
Row %d \n',pvt_row);
//n=pvt row
disp(['LEAVING variable is'],[BV(pvt row)]);
BV(pvt row)=pvt col;
disp(" New Basic Variable (BV)= ");
disp(BV);
//KEY ELEMENT
pvt key = A(pvt row, pvt col);
//disp(pvt key);
//UPDATE THE table for NEXT ITERATION
A(pvt row,:)=A(pvt row,:)./pvt key;
for i = 1:size(A,1)
  if i~=pvt row
    A(i,:)=A(i,:)-A(i,pvt col).*A(pvt row,:);
  end
Z_iC_i = Z_iC_i-Z_iC_i(pvt col).*A(pvt row,:);
ZCi = [ZiCi;A];
mprintf('\n ====== Next Iteration ===
```

```
======= Simplex Table =======
"x" "x1" "x2" "s1" "s2" "So1"
     1. -3. 0. 0. 0.
 1. -1.
        1. 1. 0.
-1.
     1.
          1. 0. 1.
  The current BFS is NOT Optimal
"Old Basic Variable = "
 4. 5.
The Minimum element in Zj-Cj is -3 Corresponding to Column 3
The Minimum Ratio Corresponding to PIVOT Row 1
" LEAVING variable is"
 4.
" New Basic Variable (BV) = "
 3. 5.
  ====== Next Iteration =======
"x" "x1" "x2" "s1" "s2" "So1"
```

```
2. -2. 0. 3. 0. 6.
```

====== Next Iteration =======

=======The BFS is =========

-->

UNBOUNDED SOLUTIONS

Consider the linear program:

Maximize
$$2x_1 + x_2$$

Subject to: $x_1 - x_2 \le 10$ (1) $2x_1 - x_2 \le 40$ (2) $x_1, x_2 \ge 0$.

```
clc;
//----INPUT PARAMETERS
Noofvariables=2;
c = [2 \ 1]
info = [1 -1; 2 -1];
b = [10; 40];
n= size(info,"r");
s = eye(n,n);
A = [info s b];
//disp(A);
cost= zeros(1,size(A,"c"));
cost(1:Noofvariables)= c;
//----Constrain BV
BV = Noofvariables+1:size(A,2)-1;
// -----Calculate ZjCj
Z_iC_i = cost(BV)*A - cost;
//disp(ZiCi);
ZCj = [ZjCj;A];
//disp(ZCj);
mprintf('\n =======\n')
```

```
disp(['x1' 'x2' 's1' 's2' "Sol"], [ ZCj(1:3,1),
ZCj(1:3,2),ZCj(1:3,3),ZCj(1:3,4),ZCj(1:3,5)]);
//simplex table start
k=0
// check any negative value
for i = 1:size(Z_iC_{i,2})
if (Z_iC_i(i) < 0) then
   k=k+1
end
if k > 0
  mprintf('\n
               The current BFS is NOT Optimal \n')
disp("Old Basic Variable = ");
disp(BV);
// Finding the Entering Variable
ZC = Z_iC_i(1:size(Z_iC_i, "c")-1);
[EnterCol,pvt col] = min(ZC);
    mprintf('\n The Minimum element in Zj-Cj is %d
Corresponding to Column %d \n',EnterCol,pvt col);
//Finding the Leaving Variable
sol = A(:,\$);
Column = A(:,pvt col);
z = size(Column,"r");
i=0
for i=1:size(Column,"r")
  if Column(i)<0
  j=j+1;
  end
end
// To check UNBOUNDED
 if j == z;
  mprintf('LPP is UNBOUNDED. All entries <= 0 in
column %d \n',pvt col);
  break
```

```
end:
for i=1:size(Column,"r")
  if Column(i)>0
  ratio(i) =sol(i)./Column(i);
 else
  ratio(i)=%inf;
  end
end
[MinRatio,pvt row] = min(ratio);
mprintf('\n The Minimum Ratio Corresponding to PIVOT
Row %d \n',pvt row);
//n=pvt row
disp(['LEAVING variable is'],[BV(pvt row)]);
BV(pvt row)=pvt col;
disp(" New Basic Variable (BV)= ");
disp(BV);
//KEY ELEMENT
pvt key = A(pvt row, pvt col);
//disp(pvt key);
//UPDATE THE table for NEXT ITERATION
A(pvt row,:)=A(pvt row,:)./pvt key;
for i = 1:size(A,1)
  if i~=pvt row
    A(i,:)=A(i,:)-A(i,pvt col).*A(pvt row,:);
  end
ZjCj = ZjCj-ZjCj(pvt_col).*A(pvt_row,:);
ZCj = [ZjCj;A];
mprintf('\n ====== Next Iteration =====\n')
disp(['x1' 'x2' 's1' 's2' "Sol"], [ ZCj(1:3,1),
ZCj(1:3,2),ZCj(1:3,3),ZCj(1:3,4),ZCj(1:3,5)]);
end
BFS = zeros(1,size(A,2));
BFS(BV) = A(:,\$);
```

```
======= Simplex Table =======
"x1" "x2" "s1" "s2" "So1"
-2. -1. 0. 0. 0.
1. -1. 1. 0. 10.
2. -1. 0. 1. 40.
 The current BFS is NOT Optimal
"Old Basic Variable = "
3. 4.
The Minimum element in Zj-Cj is -2 Corresponding to Column 1
The Minimum Ratio Corresponding to PIVOT Row 1
" LEAVING variable is"
3.
" New Basic Variable (BV)= "
====== Next Iteration ======
"x1" "x2" "s1" "s2" "So1"
 0. -3. 2. 0. 20.
 1. -1.
        1. 0. 10.
            1.
 ----- Next Iteration ----
"x1" "x2" "s1" "s2" "So1"
```

```
Scilab 6.1.1 Console
======= Next Iteration =======
"x1" "x2" "s1" "s2" "So1"
 0. -3. 2. 0. 20.
 1. -1. 1. 0. 10.
 2. -1. 0. 1. 40.
======= Next Iteration =======
"x1" "x2" "s1" "s2" "So1"
0. -3. 2. 0. 20.
 1. -1. 1. 0. 10.
 0. 1. -2. 1. 20.
=======The BFS is =========
"x1" "x2" "s1" "s2" "So1"
10. 0. 0. 20. 20.
 The current BFS is NOT Optimal
"Old Basic Variable = "
1. 4.
The Minimum element in Zj-Cj is -3 Corresponding to Column 2
The Minimum Ratio Corresponding to PIVOT Row 2
" LEAVING variable is"
" New Basic Variable (BV)= "
 1. 2.
```

```
----- Next Iteration -----
"x1" "x2" "s1" "s2" "So1"
 0. 0. -4. 3. 80.
 1. 0. -1. 1. 30.
    1. -2. 1.
 ====== Next Iteration =======
"x1" "x2" "s1" "s2" "So1"
    0. -4. 3. 80.
            1.
    0. -1.
                 30.
=======The BFS is ========
"x1" "x2" "s1" "s2" "So1"
 30. 20. 0. 0. 80.
 The current BFS is NOT Optimal
"Old Basic Variable = "
The Minimum element in Zj-Cj is -4 Corresponding to Column 3
LPP is UNBOUNDED. All entries <= 0 in column 3
```

MULTIPLE SOLUTIONS

Maximize 2000x1 + 3000x2

subject to

 $6X_1 + 9X_2 \le 100$ $2X_1 + X_2 \le 20$

 $X_1, X_2 \ge 0$

SOURCE CODE:

clc;
//----INPUT PARAMETERS
Noofvariables=2;

```
c = [4 14]
info = [2 7; 72];
b = [21; 21];
n= size(info,"r");
s = eye(n,n);
A = [info s b];
//disp(A);
cost= zeros(1,size(A,"c"));
cost(1:Noofvariables)= c;
//----Constrain BV
BV = Noofvariables + 1:size(A,2) - 1;
// -----Calculate ZjCj
Z_iC_i = cost(BV)*A - cost;
//disp(ZjCj);
ZCi = [ZiCi;A];
//disp(ZCj)
mprintf('\n =======\n')
disp(['x1' 'x2' 's1' 's2' "Sol"], [ ZCi(1:3,1),
ZCj(1:3,2),ZCj(1:3,3),ZCj(1:3,4),ZCj(1:3,5)]);
//simplex table start
// check any negative value
k=0
for i = 1:size(ZiCi,2)
if (ZjCj(i) < 0) then
   k=k+1
end
end
if k > 0
  mprintf('\n The current BFS is NOT Optimal \n')
end
disp("Old Basic Variable = ");
disp(BV);
// Finding the Entering Variable
ZC = Z_iC_i(1:size(Z_iC_i, "c")-1);
```

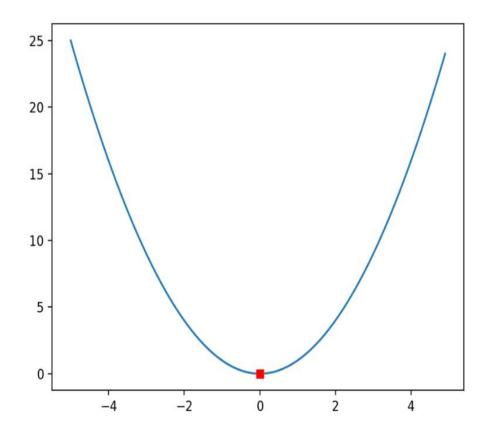
```
[EnterCol,pvt col] = min(ZC);
    mprintf('\n The Minimum element in Zj-Cj is %d
Corresponding to Column %d \n',EnterCol,pvt_col);
//Finding the Leaving Variable
sol = A(:,\$);
Column = A(:,pvt col);
z = size(Column, "r");
j=0
for i=1:size(Column,"r")
  if Column(i)<0
  j=j+1;
  end
end
// To check UNBOUNDED
//disp(j);
if i == z;
  mprintf('LPP is UNBOUNDED. All entries <= 0 in
column %d \n',pvt col);
end
for i=1:size(Column,"r")
  if Column(i)>0
   ratio(i) =sol(i)./Column(i);
 else
  ratio(i)=\%inf;
  end
end
[MinRatio,pvt row] = min(ratio);
mprintf('\n The Minimum Ratio Corresponding to PIVOT
Row %d \n',pvt row);
//n=pvt row
disp(['LEAVING variable is'],[BV(pvt row)]);
BV(pvt row)=pvt col;
disp(" New Basic Variable (BV)= ");
disp(BV);
```

```
//KEY ELEMENT
pvt key = A(pvt row, pvt col);
//disp(pvt key);
//UPDATE THE table for NEXT ITERATION
A(pvt_row,:)=A(pvt_row,:)./pvt_key;
for i = 1:size(A,1)
  if i~=pvt row
    A(i,:)=A(i,:)-A(i,pvt col).*A(pvt row,:);
  end
Z_iC_i = Z_iC_i-Z_iC_i(pvt col).*A(pvt row,:);
ZCj = [ZjCj;A];
mprintf('\n ======\n')
disp(['x1' 'x2' 's1' 's2' "Sol"], [ ZCj(1:3,1),
ZCj(1:3,2),ZCj(1:3,3),ZCj(1:3,4),ZCj(1:3,5)]);
end
BFS = zeros(1,size(A,2));
BFS(BV) = A(:,\$);
BFS(\$) = sum(BFS.*cost);
//disp(BFS);
mprintf('\n ======The BFS is ========
n'
disp(['x1' 'x2' 's1' 's2' ], [ BFS(1,1),
BFS(1,2),BFS(1,3),BFS(1,4)]);
for i = 1:2
if BFS(1,i)==0 then
  disp("Multiple Solutions as Zj-Cj value corresponding to non
basic variable is zero")
  else
end
end
```

```
======== Simplex Table ========
"x1" "x2" "s1" "s2" "So1"
-4. -14. 0. 0. 0.
2. 7. 1. 0. 21.
7. 2. 0. 1. 21.
 The current BFS is NOT Optimal
"Old Basic Variable = "
3. 4.
The Minimum element in Zj-Cj is -14 Corresponding to Column 2
The Minimum Ratio Corresponding to PIVOT Row 1
" LEAVING variable is"
" New Basic Variable (BV) = "
======= Next Iteration =======
"x1" "x2" "s1" "s2" "So1"
          0. 2.
                          0. 42.
 0.2857143 1. 0.1428571 0. 3.
           2.
               0.
                          1. 21.
====== Next Iteration =======
"x1" "x2" "s1" "s2" "So1"
```

AIM: To determine local/relative optima of a given unconstrained problem.

```
from numpy import arange
from matplotlib import pyplot
# objective function
def objective(x):
     return x**2.0
# define range for input
r min, r max = -5.0, 5.0
# sample input range uniformly at 0.1 increments
inputs = arange(r_min, r_max, 0.1)
# compute targets
results = objective(inputs)
# create a line plot of input vs result
pyplot.plot(inputs, results)
# define the known function optima
optima x = 0.0
optima_y = objective(optima_x)
# draw the function optima as a red square
pyplot.plot([optima_x], [optima_y], 's', color='r')
# show the plot
pyplot.show()
```



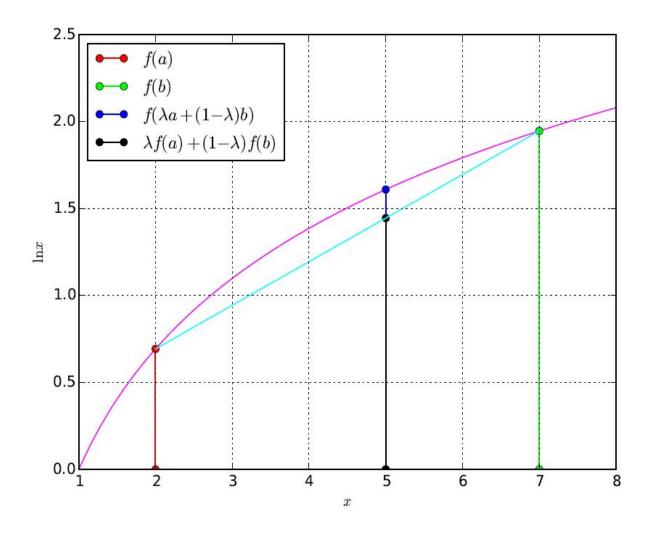
AIM: Test whether the given function is concave/convex.

Function - ln(x)

```
import numpy as np
import matplotlib.pyplot as plt
# Plotting log(x)
x = \text{np.linspace}(1, 8, 50)
#points on thexaxis
f=np.log(x)#Objectivefunction
plt.plot(x,f,color = (1,0,1))
plt.grid()
plt.xlabel('$x$")
plt.ylabel('$\lnx$')
# Convexity / Concavity
a = 2
b = 7
lamda = 0.4
c = lamda* a + (1-lamda)* b
f = np.log(a)
f b=np.log(b)
f = np.log(c)
f c hat=lamda* f a+(1-lamda)* f b
# Plot commands
plt.plot([a,a],[0,f a],color=(1,0,0),marker='o',label="$f(a)$")
plt.plot([b,b],[0,fb],color=(0,1,0),marker='o',label=
"$f(b)$")
plt.plot([c,c],[0,f],[c],color=(0,0,1),marker='o',label="
f(\lambda a+(1-\lambda b) )
plt.plot ([c,c], [0,f_c_hat], color=(1/2,2/3,3/4), marker=
'o', label=" \alpha(a)+(1-\lambda)f(b)")
plt.plot([a,b], [f a,f b], color=(0,1,1))
plt.legend(loc=2)
```

```
# plt. save fig ( '../figs/1.1.eps')
plt.show()
end
```

PLOT:



AIM: Solution of optimization problems using Karush-Kuhn-Tucker conditions.

Problem 2.17. Solve

$$\min_{\mathbf{x}} \quad x_1 + x_2 \tag{2.53}$$

with the constraints

$$x_1^2 - x_1 + x_2^2 \le 0 (2.54)$$

where
$$\mathbf{x} = \begin{pmatrix} x_1 \\ x_2 \end{pmatrix}$$

THEORY:

In general for solving a convex optimization problem like using Lagrange Multipliers. These are called Karush-Kuhn-Tucker(KKT) conditions.

Using the method of Lagrange multipliers,

$$\nabla \{f(\mathbf{x}) + \mu g(\mathbf{x})\} = 0, \, \mu \ge 0$$

resulting in the equations

$$2x_1 \mu - \mu + 1 = 0$$

$$2x^2\mu + 1 = 0$$

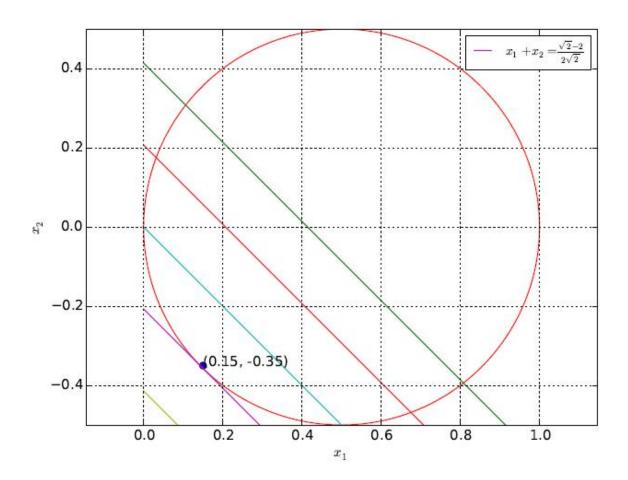
$$x^2_1 - x_1 + x_2 = 0$$

so,
$$\mu = \sqrt{2}$$
.

Graphical solution: The constraint can be expressed

$$x^21 - x_1 + x^2_1 \le 0$$

```
import numpy a s np
import matplotlib.pyplotasplt
sol = np.zeros((2,1))
# Printing minimum
sol[0] = (np.s qrt(2)-1) / (2 * np.sqrt(2))
sol[1] = -1/(2* np.sqr t(2))
# Plotting the circle
circle = plt.Circle((0.5,0), 0.5,
color='r',fill =False)
fig, ax = plt.sub plots()
ax .addartist(cir cle)
A = np.around (sol[0], decimals = 2)
B = np.around (sol [1], decimals = 2)
plt.plot (A,B, 'o')
for xy in zip (A,B):
ax . annotate ( '(%s , %s )' %xy , xy=xy , textcoords='data ')
print (sol)
# Plotting the line
p = (sol[0] + sol[1]) * np . arange(-2,3)
x = \text{np.linspace} (0, 1, 100)
na=np.newaxi s
x line = x [:,na]
y line = p [na, :] - x[:,na]
bx = plt. plot (x line, y line, '-')
plt.axis('equal')
plt . grid()
plt.xlabel('$x 1$')
plt .ylabel ( '$x 2$ ')
plt .ylim (-0.5, 0.5)
\{2 \setminus \text{sqr t} \{2\}\} \}  '],
loc=' best', prop = { 'size': 11 } )
plt.show()
```



AIM: Solution of Quadratic programming problem by Wolfe's method.

```
function [x, fval]=wolf(D, l, b, Mat, inq, minimize)
n = length(1);
m = length(b);
if \simisequal(size(Mat,1),m) \parallel \simisequal(length(inq),m) \parallel
\simisequal(size(D,1),size(D,2)) || \simisequal(size(D,1),n) ||
~isequal(size(Mat,2),n)
fprintf('\nError: Dimension mismatch!\n');
return
end
if nargin < 4 \parallel nargin > 6
  mprintf('\nError:Number of input arguments are
inappropriate!\n');
  return
end
if nargin < 5
  minimize = 0;
  inq = -ones(m,1);
elseif nargin < 6
  minimize = 0;
end
if minimize == 1
  1 = -1;
  D = -D;
end
if min(spec(-D)) < 0 % Checking convexity of Hessian
  mprintf('\nError: Wolf method may not converge to global
optimum!\n');
  return
elseif (min(spec(-D)) == 0) && \simisempty(find(1,1))
```

```
mprintf('\nError: Wolf method may not converge to global
optimum!\n');
  return
end
count = n;
for i = 1 : m
  if (inq(i) > 0)
     Mat(i,:) = -Mat(i,:);
     b(i) = -b(i);
  elseif(inq(i) == 0)
     count = count + 1;
     Mat(i,count) = -1;
     l(count) = 0;
     D(count, count) = 0;
  end
end
a = [-2*D Mat' - eye(count, count) zeros(count, m); Mat zeros(m, m)]
+ count) eye(m,m)];
d = [1;b];
for i = 1: count + m
  if(d(i) < 0)
     d(i) = -d(i);
     a(i,:) = -a(i,:);
  end
end
cb = zeros(1,count + m);
bv = zeros(1,count + m);
nbv = (1 : 2 * (count + m));
c = zeros(1,2 * (count + m));
rem = zeros(1,count + m);
for i = 1: count + m
  if(a(i,count + m + i) == -1)
     bv(i) = 2 * (count + m) + i;
     cb(i) = -1;
  elseif(a(i,count + m + i) == 1)
     rem(i)=count + m + i;
     bv(i) = count + m + i;
```

```
cb(i) = 0;
  end
end
[h,j,k] = find(rem);
a(:,k) = [];
c(k) = [];
nbv(k) = [];
r = cb * a - c;
exitflg = 0;
iter = 0;
z = cb * d;
[w,y] = size(a);
opt = 0;
while(exitflg == 0)
  iter = iter + 1;
  mprintf('\n\n %d th tableau:\n',iter);
  mprintf('\n\t\tBV\t');disp(nbv);
  disp([bv' d a ; 0 z r]);
  r new = r;
  found = 0;
  while found == 0
     [u,v] = min(r_new);
     leave = 0;
     if \sim (u < 0)
       if abs(z) > 10^{-6}
          mprintf('\nError: Wolf method fails to find
optimum!\n');
          exitflg = 1;
          found = 1;
       else
          mprintf('\nThe optimum has achieved!\n');
          exitflg = 1; opt = 1;
          found = 1;
       end
     else
```

```
ratio = 15;
        check = 0;
        for i = 1 : w
          if bv(i) \le 2 * (count + m) && abs(bv(i) - nbv(v)) ==
count + m
             check = 1;
          end
        end
        if check == 0
          for i = 1 : w
             if a(i,v) > 0 && (d(i) / a(i,v)) < ratio
                ratio = d(i) / a(i,v);
                leave = i;
             end
          end
          mprintf('\nEntering Variable:'); disp(nbv(v));
          mprintf('\nLeaving Variable:'); disp(bv(leave));
          for i = 1 : w
             for j = 1 : y
                if i \sim = leave && i \sim = v
                   a(i,j) = a(i,j) - a(i,v) * a(leave,j) / a(leave,v);
                end
             end
          end
          z = z - d(leave) * r(v) / a(leave, v);
          for j = 1 : y
             if j \sim = v
                r(j) = r(j) - r(v) * a(leave,j) / a(leave,v);
                a(leave,j) = a(leave,j) / a(leave,v);
             end
          end
```

```
for i = 1 : w
             if i \sim = leave
               d(i) = d(i) - a(i,v) * d(leave) / a(leave,v);
               a(i,v) = -a(i,v) / a(leave,v);
             end
          end
          d(leave) = d(leave) / a(leave,v);
          a(leave,v) = 1 / a(leave,v);
          r(v) = -r(v) / a(leave, v);
          temp = nbv(v);
          nbv(v) = bv(leave);
          bv(leave) = temp;
          found = 1;
       elseif check == 1
          r \text{ new}(v) = 1;
       end
     end
  end
end
if opt == 1
  x = zeros(n,1);
  for i = 1 : w
     if bv(i) \le n
       x(bv(i)) = d(i);
     end
  end
  fval = x'*l+x'*D*x;
  if minimize == 1
     fval = -fval;
  end
end
end
OUTPUT:
```

