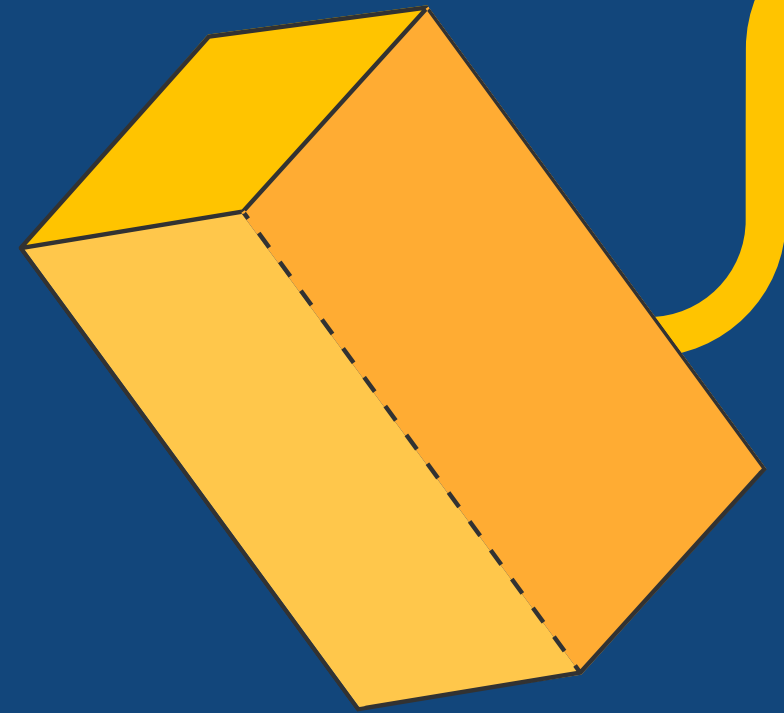


Surface Area

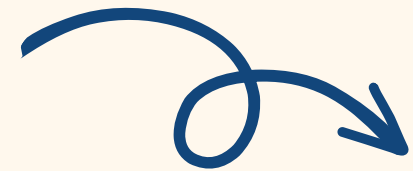
The sum of the areas of the base and the lateral faces of space figures.

Lesson Outline

- Surface area of a triangular prism
- Surface area of a cylinder
- Surface area of a pyramid
- Surface area of a cone
- Surface area of a sphere

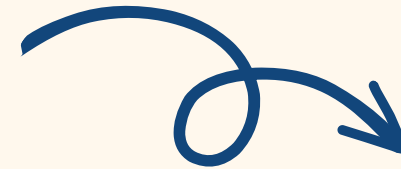


Surface Area of a Triangular Prism



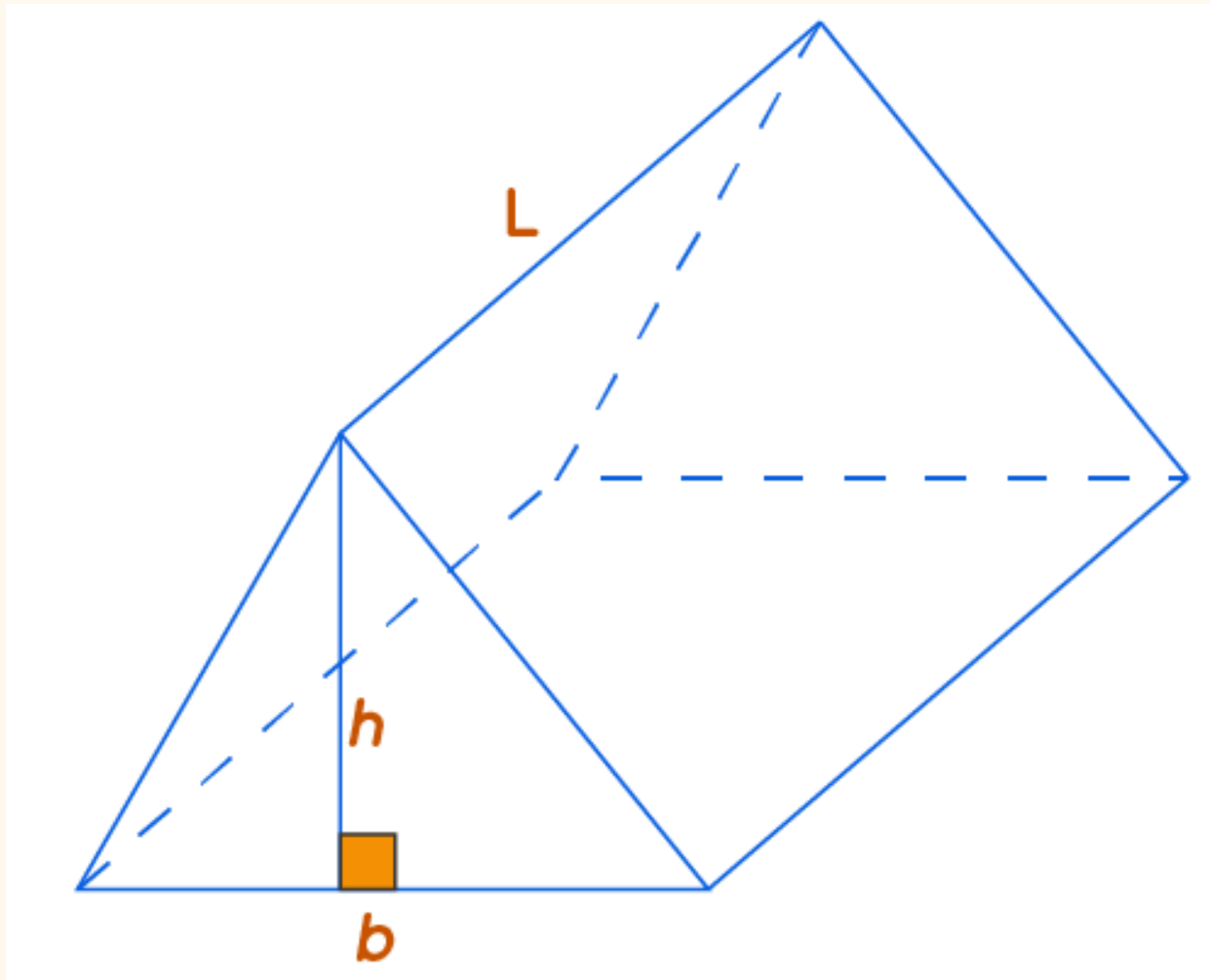
Surface Area of a Triangular Prism

To find the surface area of a triangular prism, $bh + (a + b + c)H = (2A + PH)$

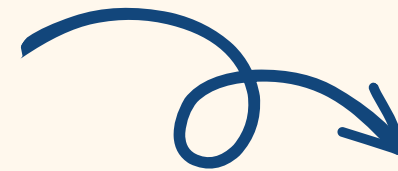


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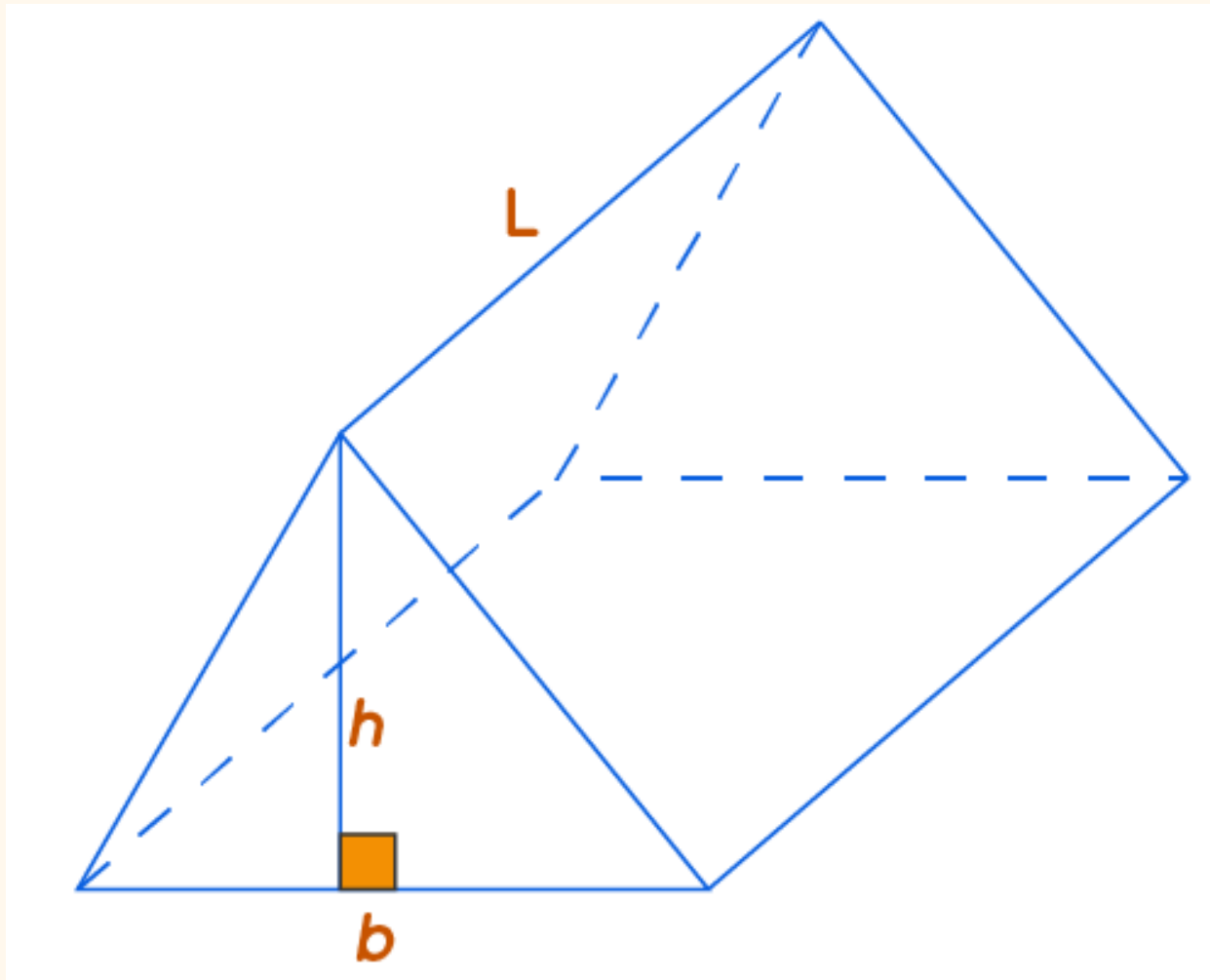


Trangular Prism

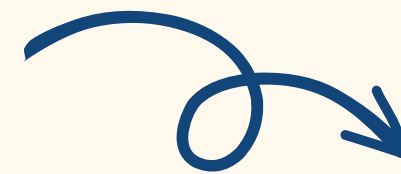


Surface Area of a Triangular Prism

To find the surface area of a triangular prism, $bh + (a + b + c)H = (2A + PH)$



Trangular Prism

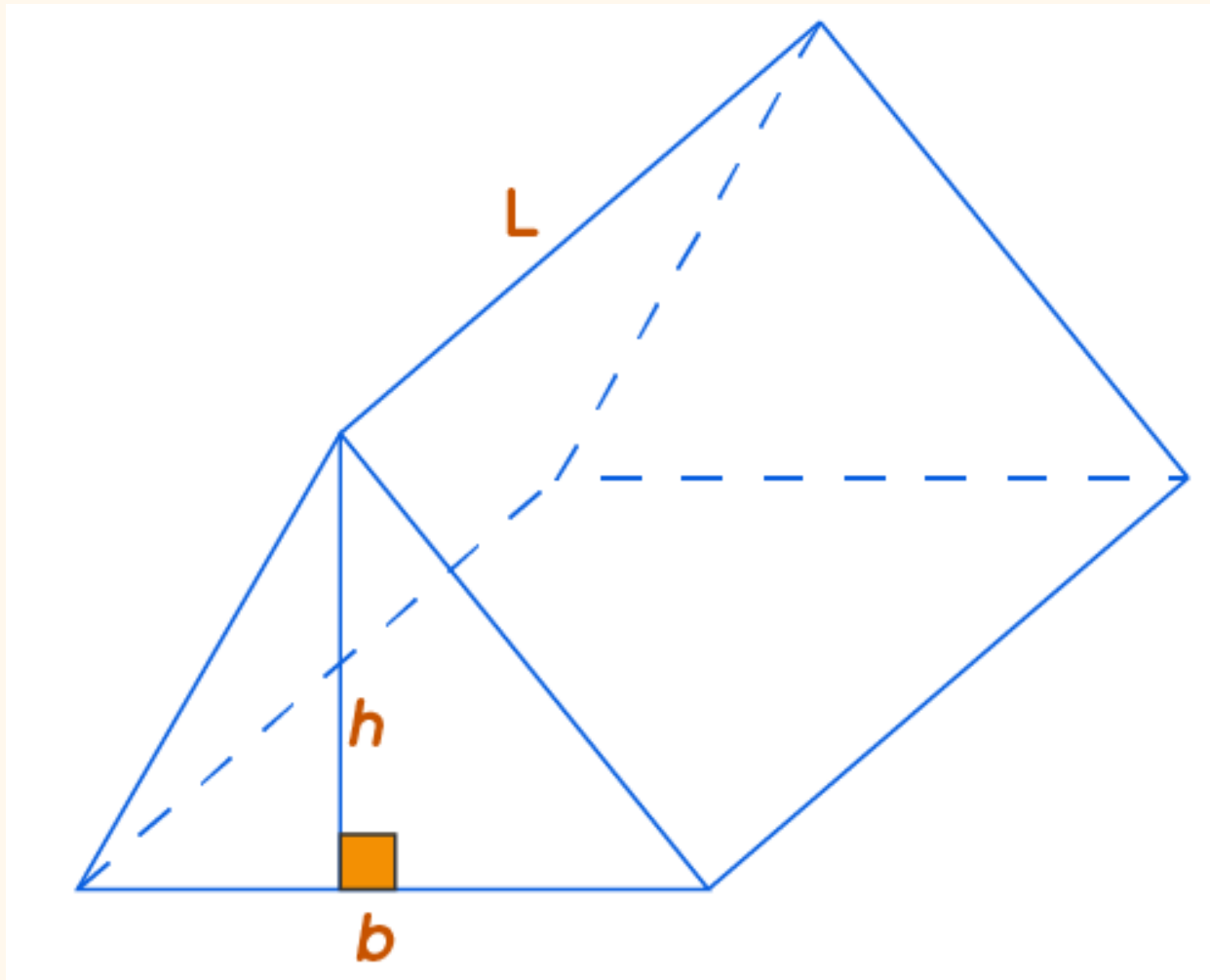


$$bh + (a + b + c)H = (2A + PH)$$

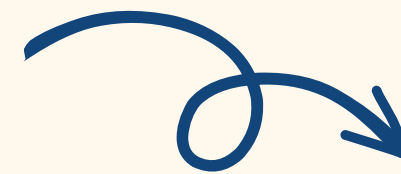


Surface Area of a Triangular Prism

To find the surface area of a triangular prism, $bh + (a + b + c)H = (2A + PH)$



Trangular Prism



$$bh + (a + b + c) H \quad (2A + PH)$$

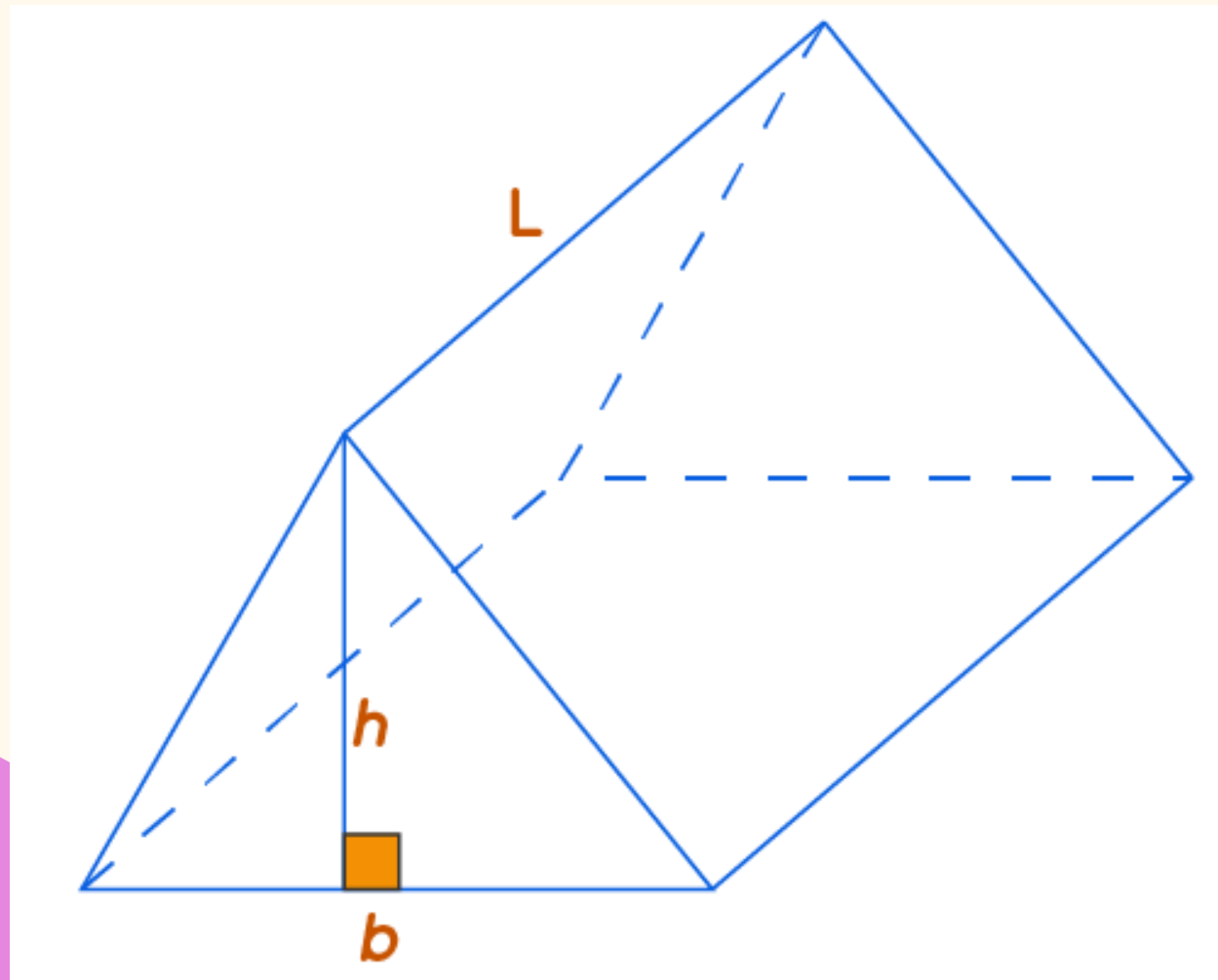


$$(2A + PH)$$

Surface Area of a Triangular Prism

Example:

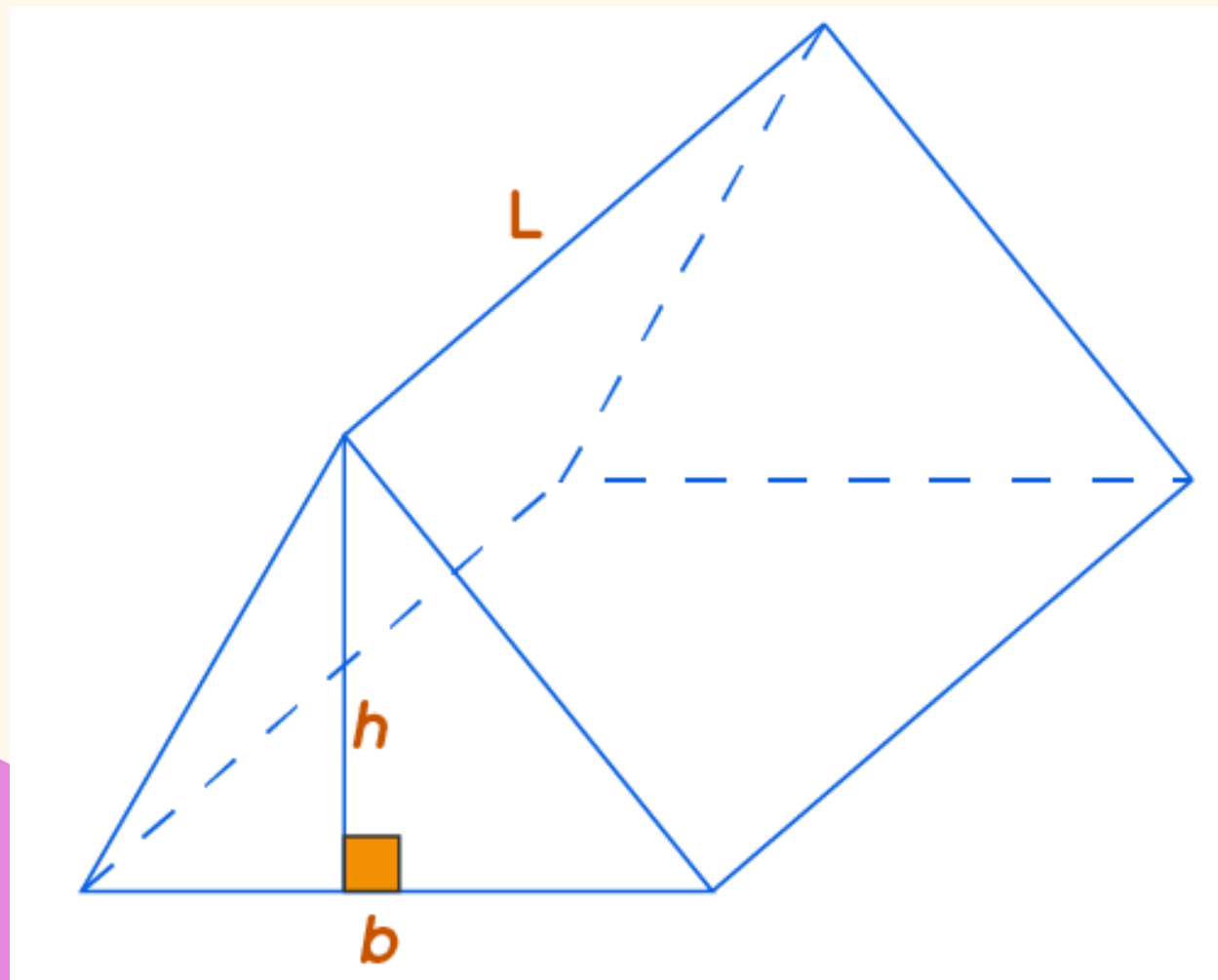
$$bh + (a + b + c)H = (2B + PH)$$



Find the surface area of a prism given above whose base area is 10 square units, the base perimeter is 20 units and the height of the prism is 6 units.

Surface Area of a Triangular Prism

Example:



Surface Area of Prism = $(2 \times \text{Base Area}) + (\text{Base perimeter} \times \text{height})$

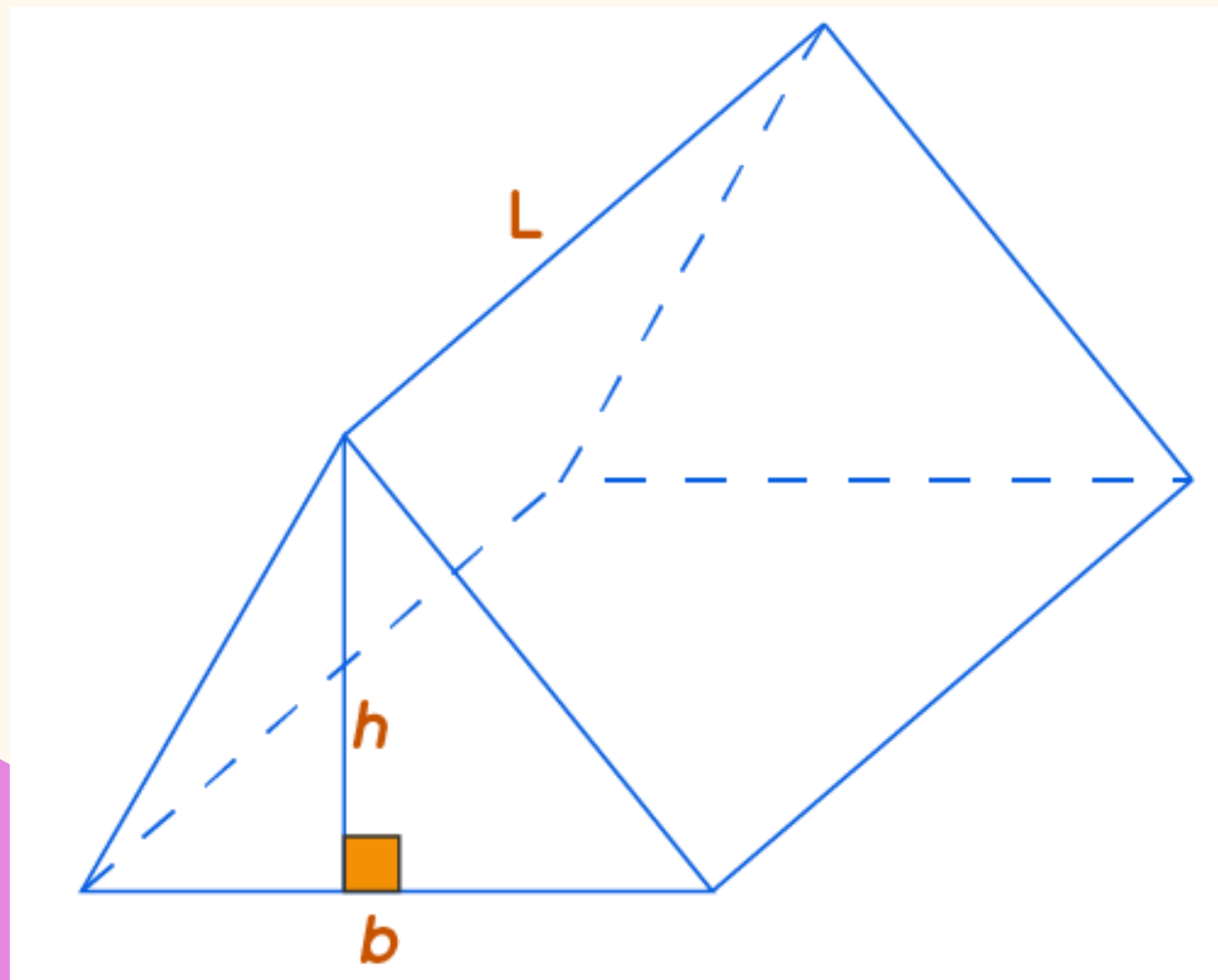
Base area = 10 square units

Base perimeter = 20 units

Height of the prism = 6 units

Surface Area of a Triangular Prism

Example:



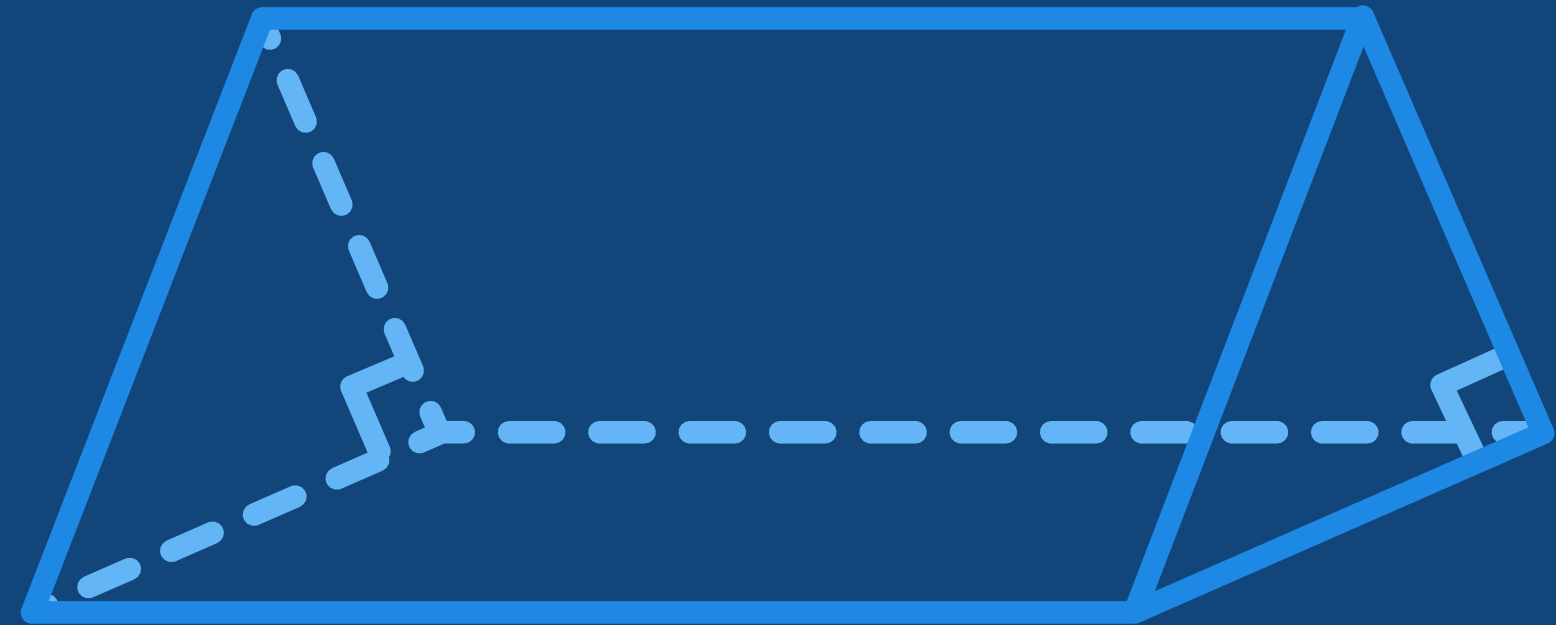
Surface Area of Prism = $(2 \times \text{Base Area}) + (\text{Base perimeter} \times \text{height})$

$$\text{Surface Area of Prism} = (2 \times 10) + (20 \times 6)$$

\therefore The surface area of prism is 140 square units.

Try This!

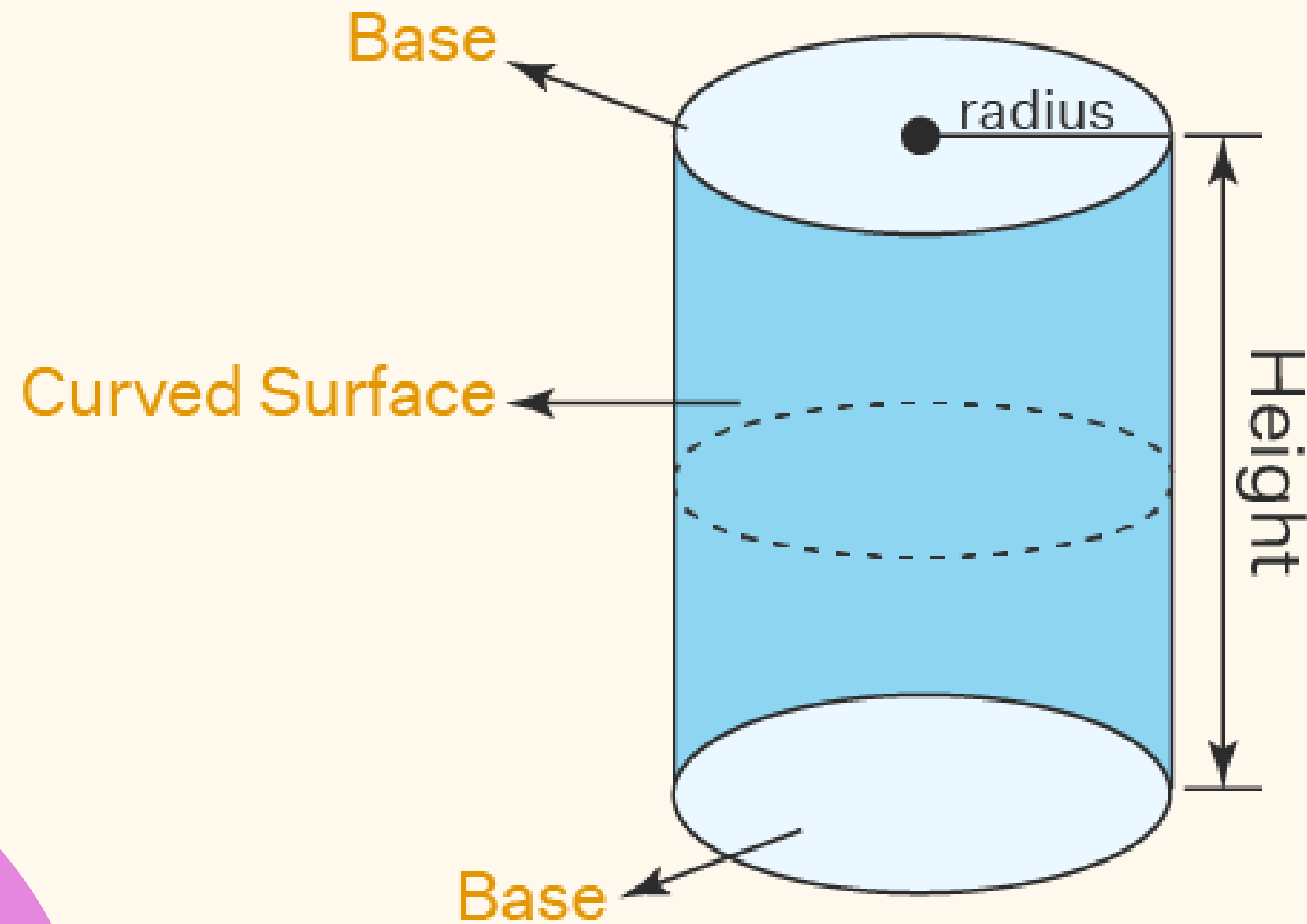
What will be the surface area of the triangular prism if the base and height of a triangular prism are 8 units and 14 units respectively along with the height of the equilateral triangular bases being 9 units?



Surface Area of a Cylinder

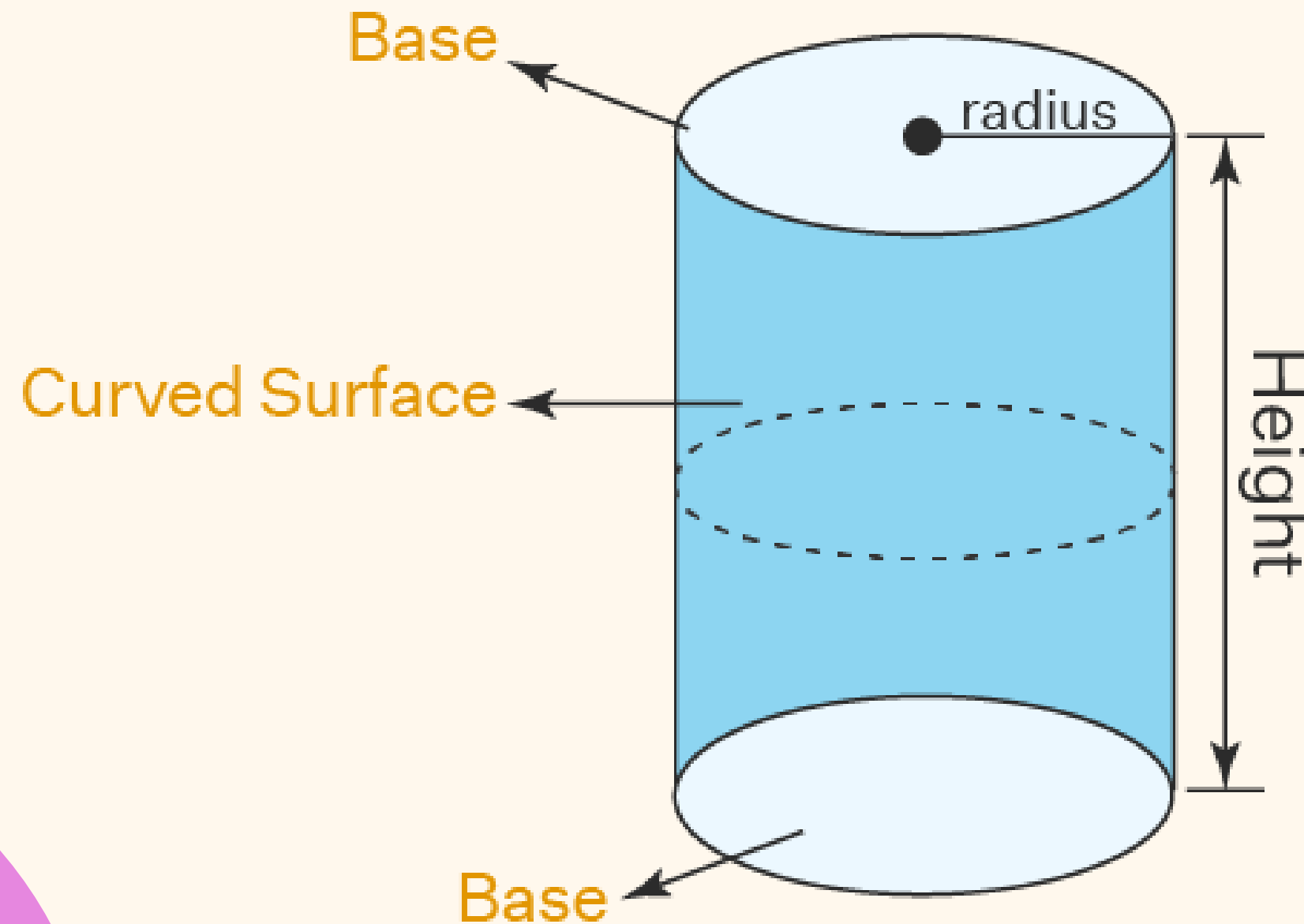
Surface Area of a Cylinder

To find the surface area of a cylinder, $2\pi rh$



Surface Area of a Cylinder

To find the surface area of a cylinder, $2\pi rh$



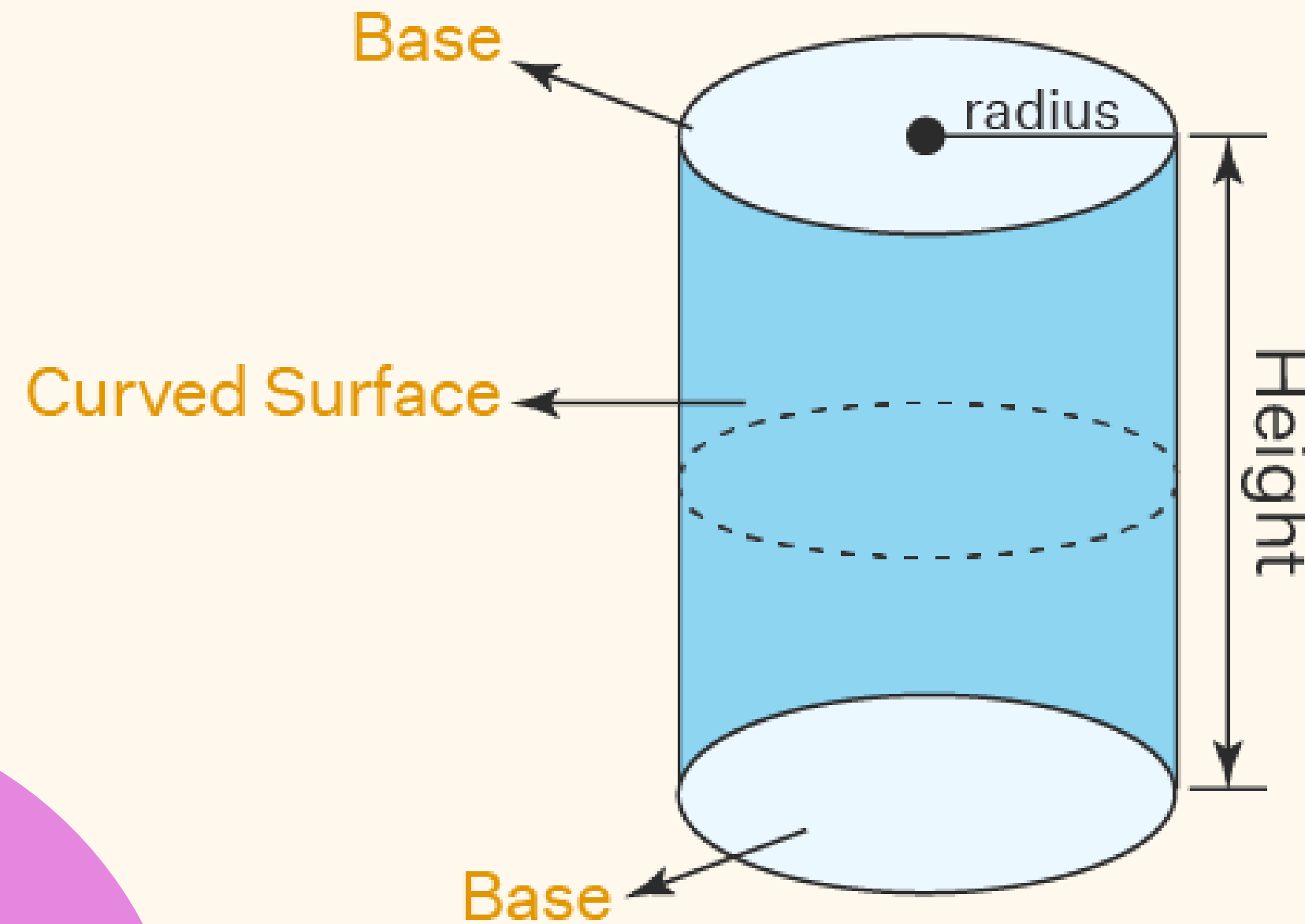
r = radius of the cylinder

h = height of cylinder

$\pi = 22/7$ or 3.14

Surface Area of a Cylinder

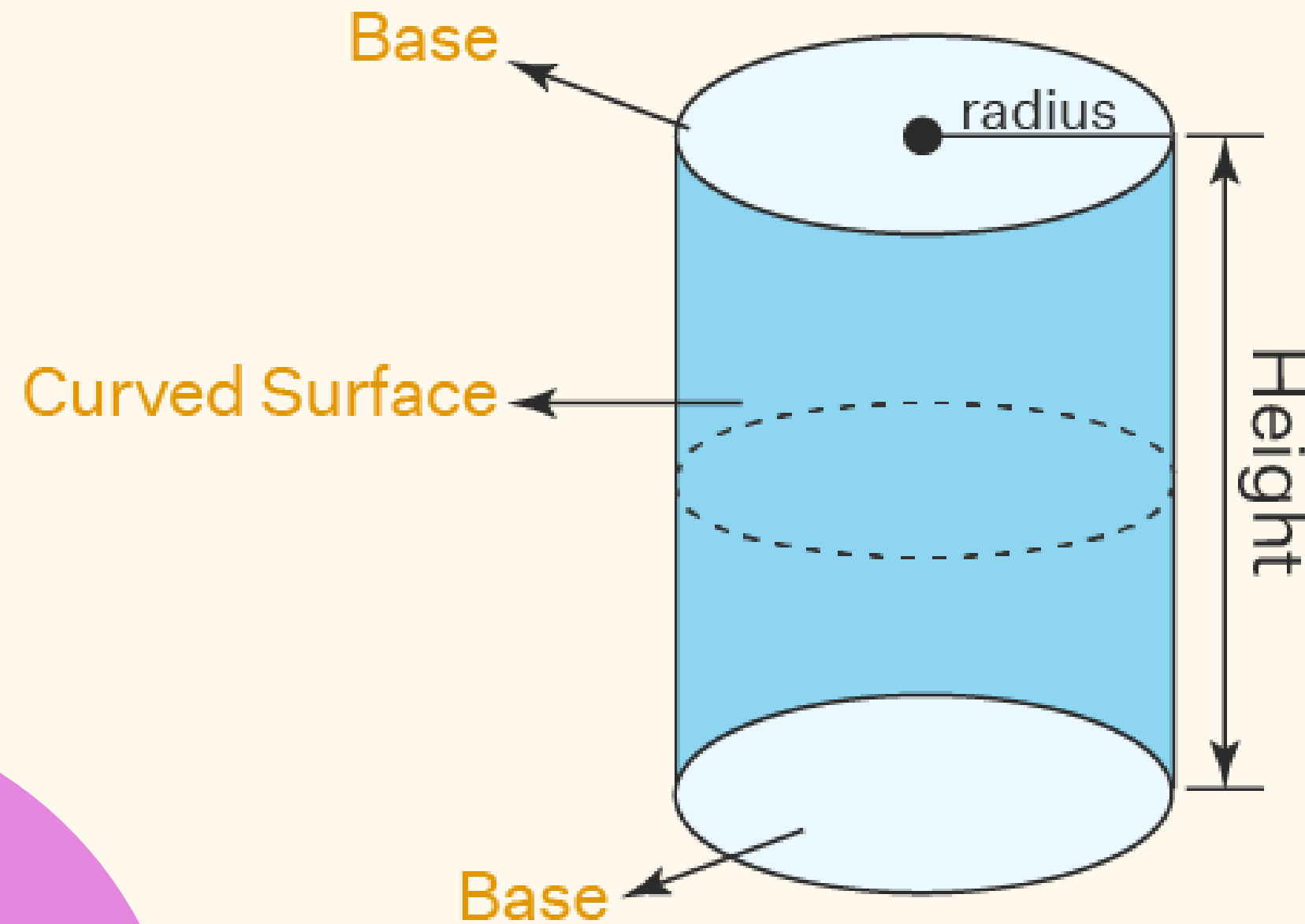
To find the surface area of a cylinder, $2\pi rh$



Find the curved surface area of a cylinder of radius 9 cm and height 17 cm.

Surface Area of a Cylinder

To find the surface area of a cylinder, $2\pi rh$

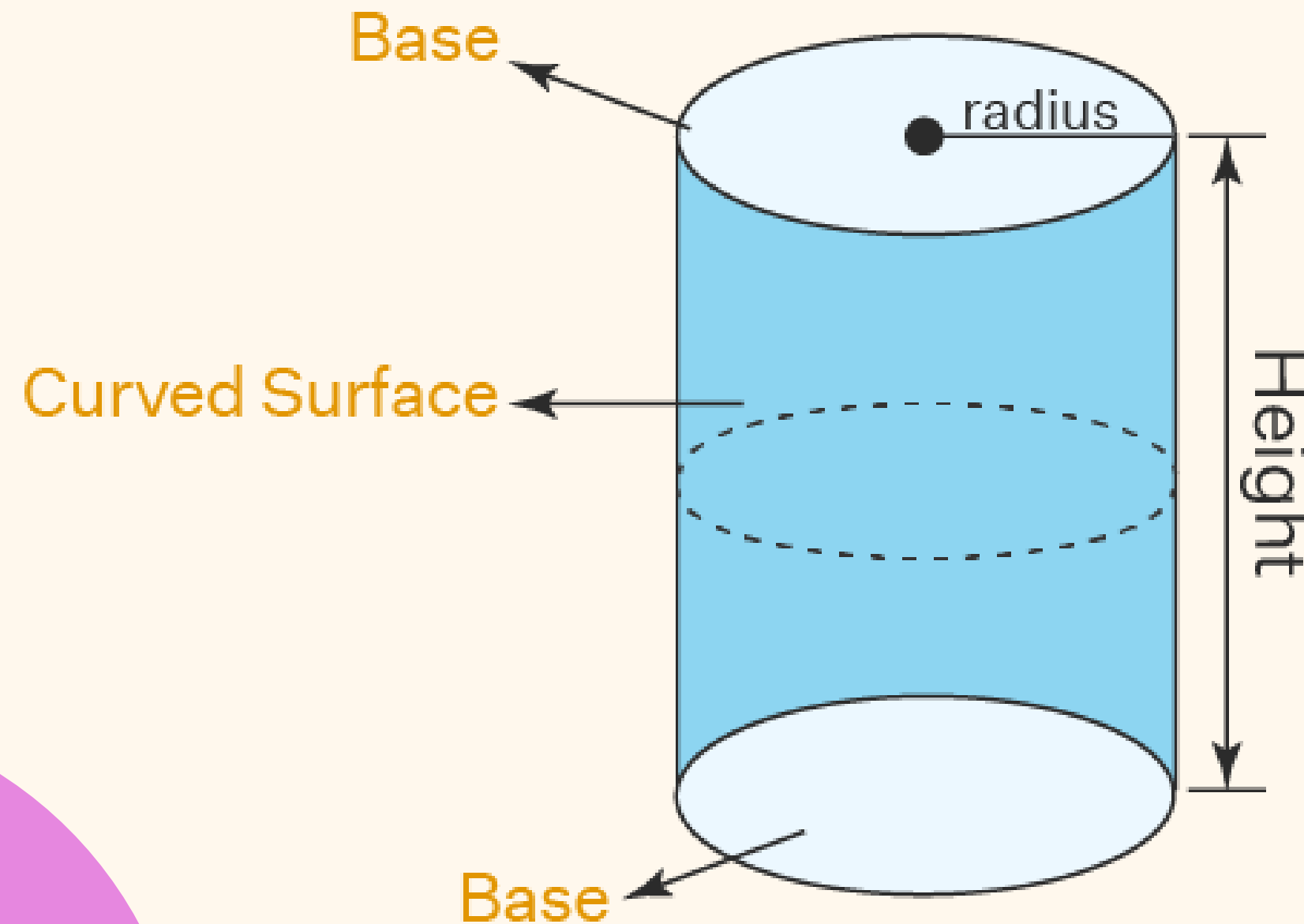


Find the curved surface area of a cylinder of radius 9 cm and height 17 cm.

Solution: The curved surface area of a cylinder can be calculated using the formula,
 $CSA = 2\pi rh$.

Surface Area of a Cylinder

To find the surface area of a cylinder, $2\pi rh$



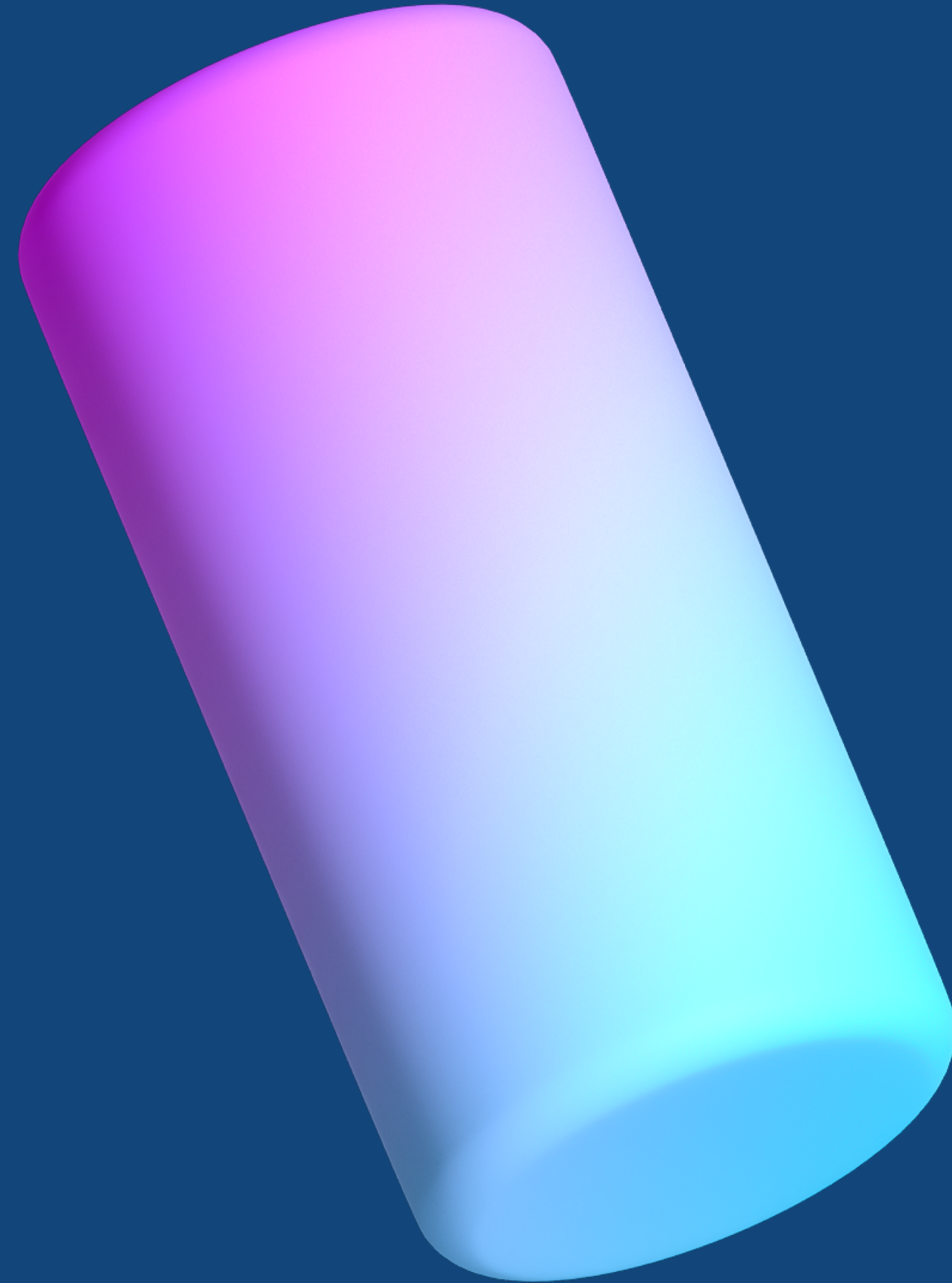
Find the curved surface area of a cylinder of radius 9 cm and height 17 cm.

Solution: The curved surface area of a cylinder can be calculated using the formula,
 $CSA = 2\pi rh$.

By substituting the values of $r = 9$, $h = 17$, we get:
 $CSA = 2\pi rh = 2 \times 3.14 \times 9 \times 17 = 960.8 \text{ cm}^2$.

Try This!

Find the curved surface area of a cylinder of radius 7 cm and height 14 cm.



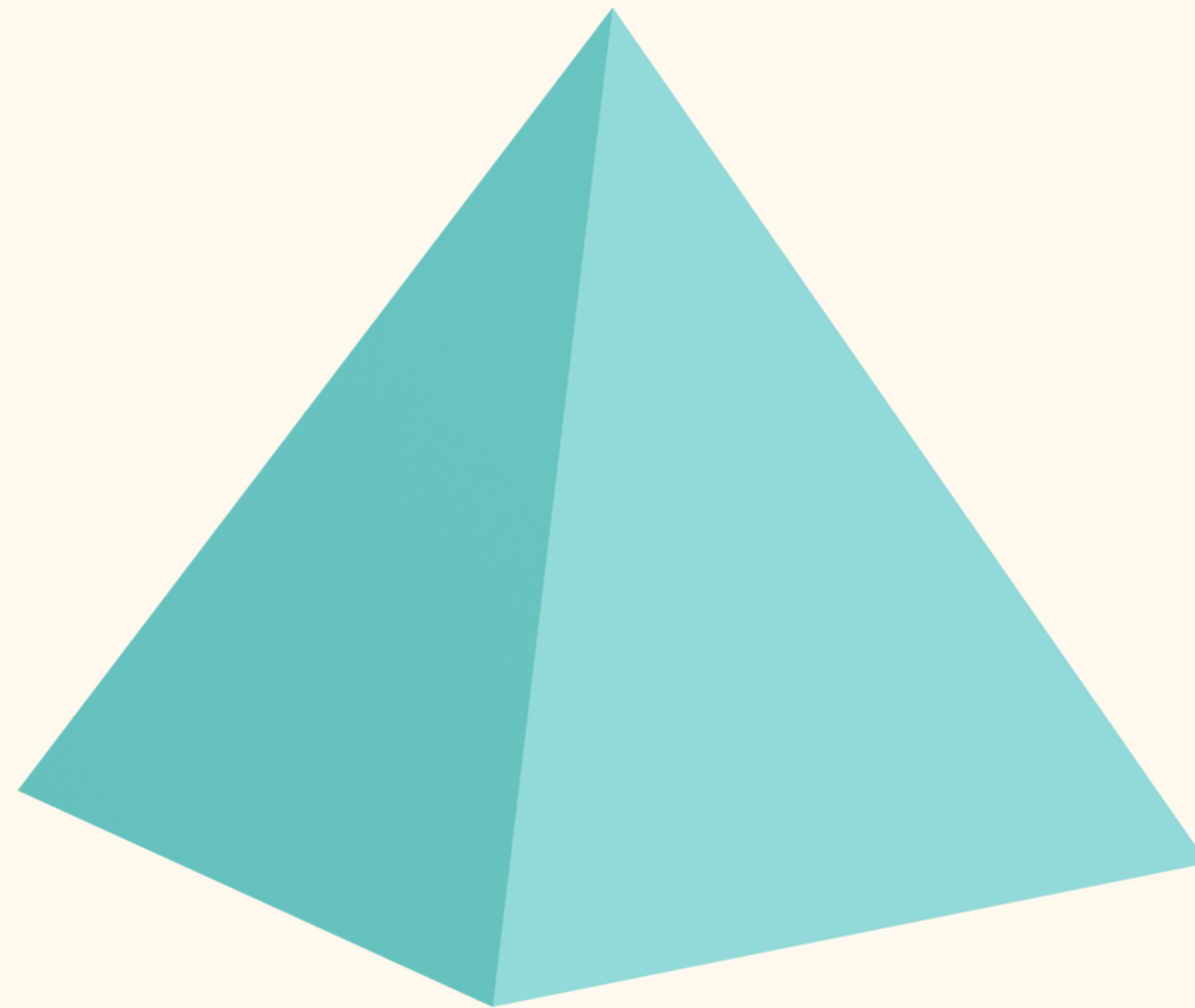
Surface Area of a Pyramid

Surface Area of a Pyramid

To find the surface area of a pyramid,
Lateral surface area (LSA) = $\frac{1}{2}p$ and Total Surface Area = $\frac{1}{2}p + B$

Surface Area of a Pyramid

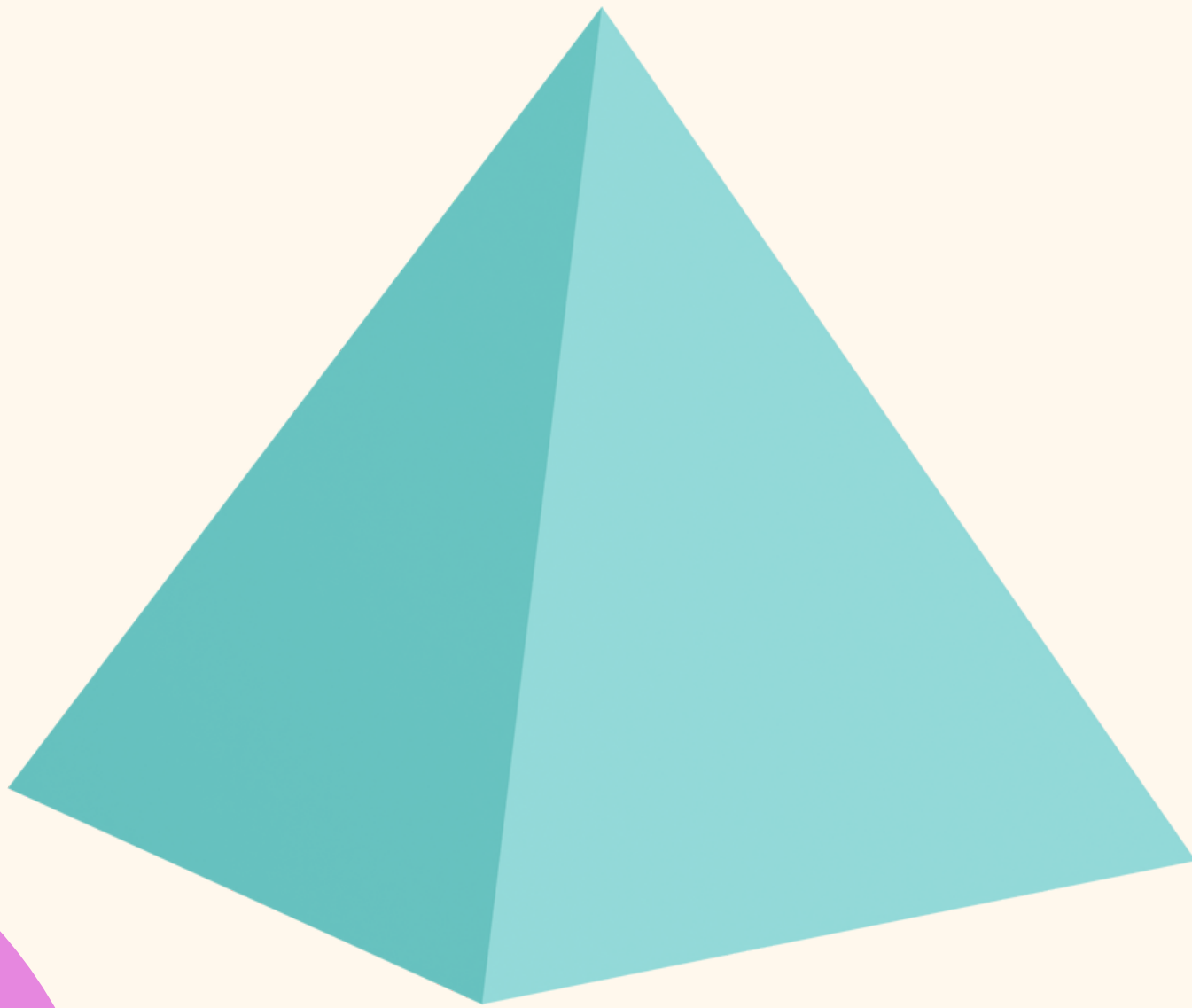
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Surface Area of a Pyramid

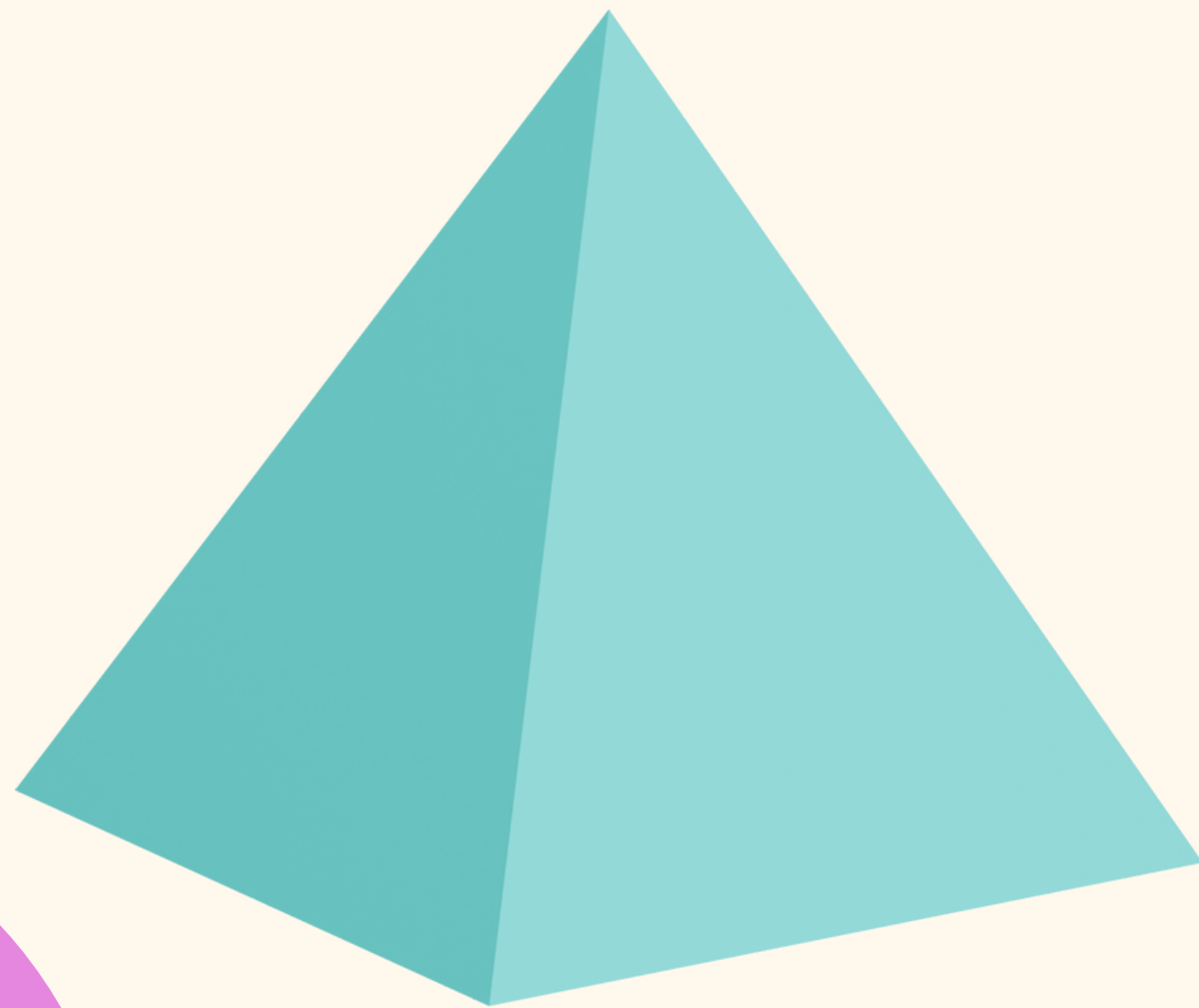
Example

Calculate the lateral surface area of a square pyramid if the side length of the base is 18 inches and the slant height of the pyramid is 22 inches.



Surface Area of a Pyramid

Example



Calculate the lateral surface area of a square pyramid if the side length of the base is 18 inches and the slant height of the pyramid is 22 inches.

The side length of the base, $a = 18$ inches
Then, the perimeter of the base (square) is, $P = 4a = 4(18) = 72$ inches.

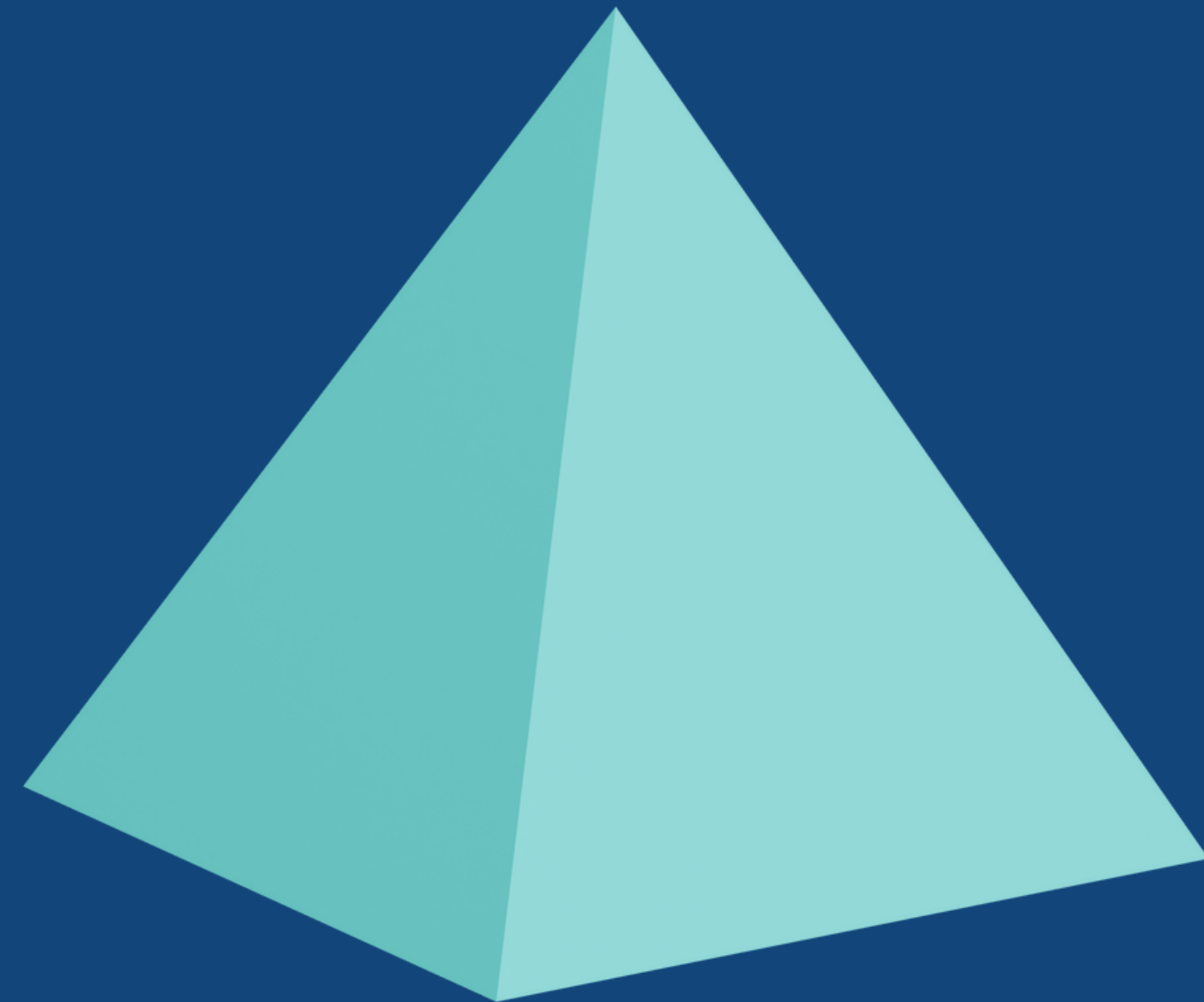
Slant height, $l = 22$ inches

The lateral surface area of a square pyramid is,

$$\begin{aligned} \text{Lateral surface area (LSA)} &= (1/2) Pl \\ (\text{LSA}) &= (1/2) \times (72) \times 22 = 792 \text{ inches squared} \end{aligned}$$

Try This!

Calculate the lateral surface area of a square pyramid if the side length of the base is 14 inches and the slant height of the pyramid is 20 inches.



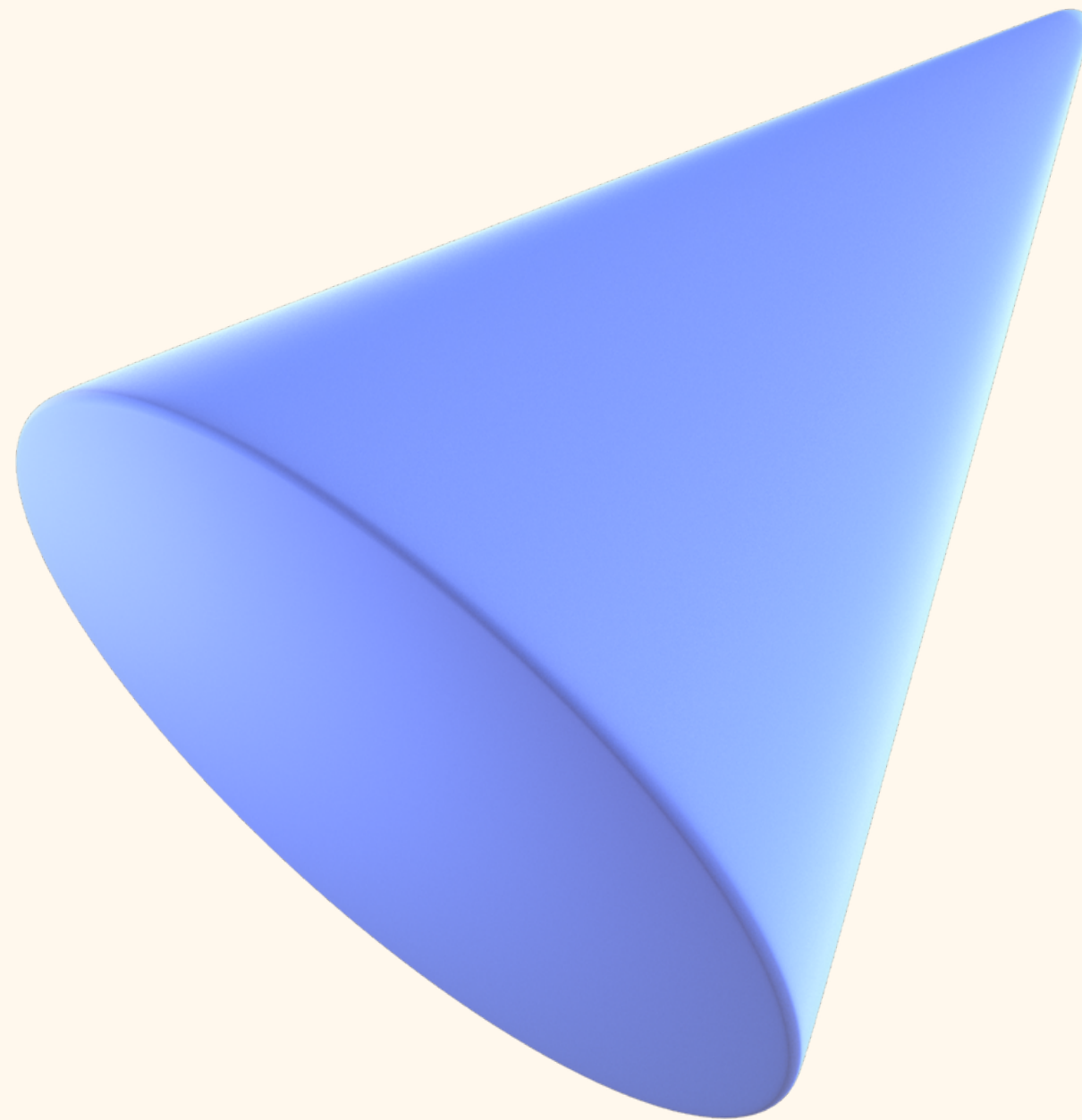
Surface Area of a Cone

Surface Area of a Cone

Total surface area of cone = $\pi r (r + l)$

Surface Area of a Cone

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Surface Area of a Cone

Total surface area of cone = $\pi r (r + l)$



What is the slant height of the cone if the total surface area of the cone is 616in^2 and the radius is 7 inches?

Surface Area of a Cone

$$\text{Total surface area of cone} = \pi r (r + l)$$



What is the slant height of the cone if the total surface area of the cone is 616in^2 and the radius is 7 inches?

$$\begin{aligned}\text{Total surface area of cone} &= \pi r (r + l) = \left(\frac{22}{7}\right) \times 7 \\ &\times (7 + x) = 616\end{aligned}$$

$$\Rightarrow 22 \times (7 + x) = 616$$

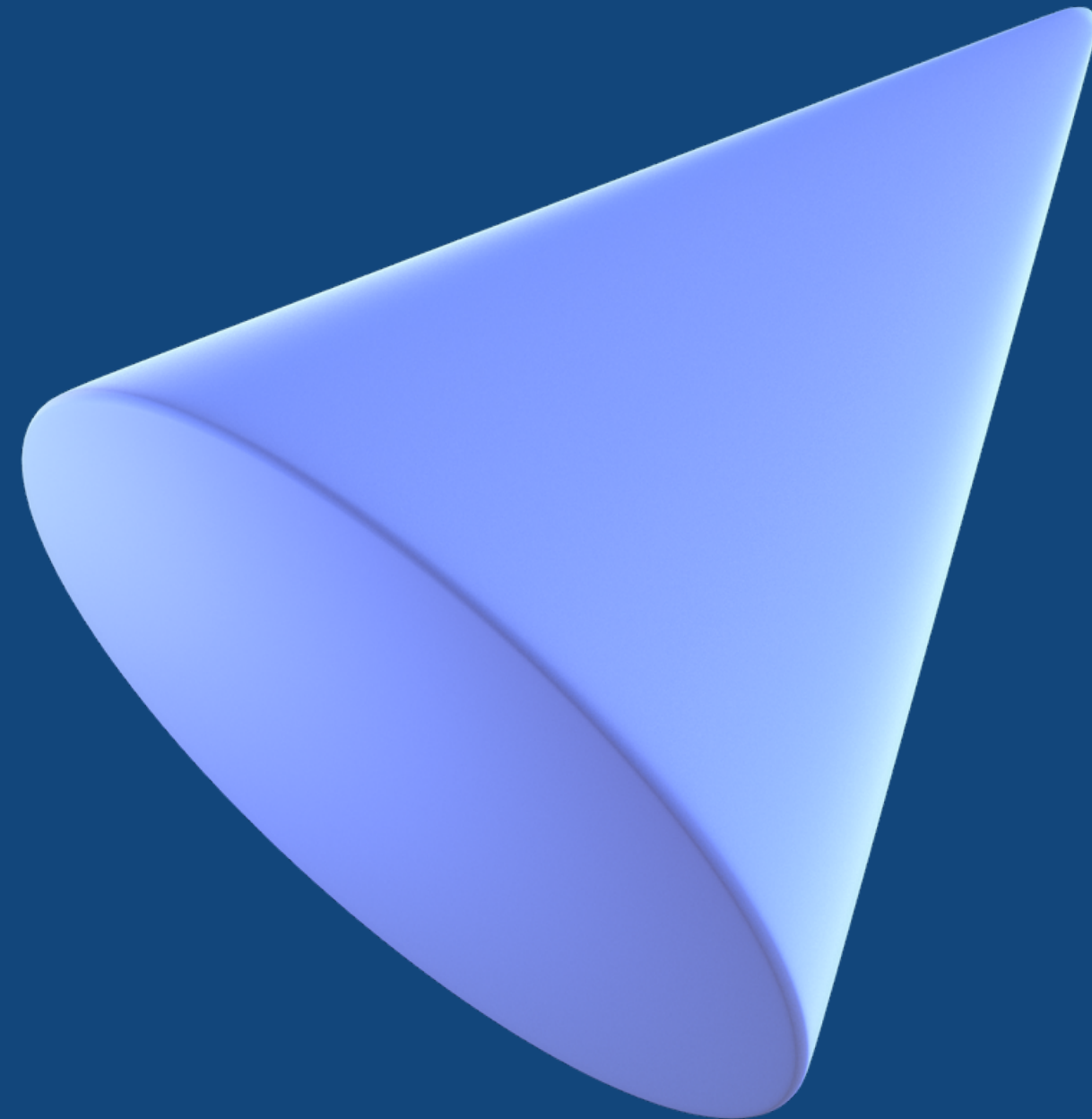
$$\Rightarrow 7 + x = 28$$

$$\Rightarrow x = 21 \text{ inches}$$

Answer: The slant height of the cone is 21 inches.

Try This!

What is the height of a cone whose radius is 7 inches and curved surface area is 550 in²? (Use $\pi = 22/7$)



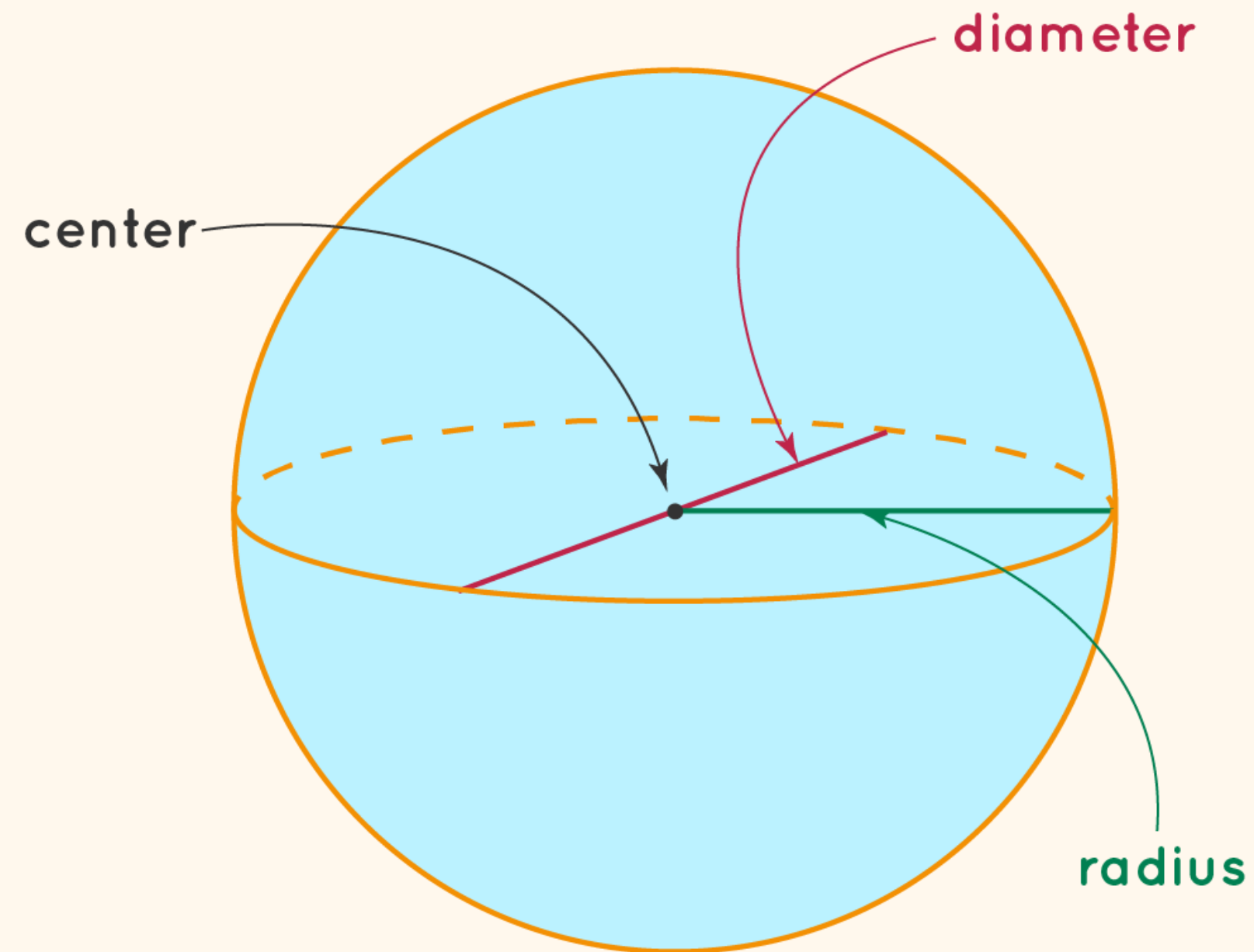
Surface Area of a Sphere

Surface Area of a Sphere

Total surface area of Sphere = $4\pi r^2$

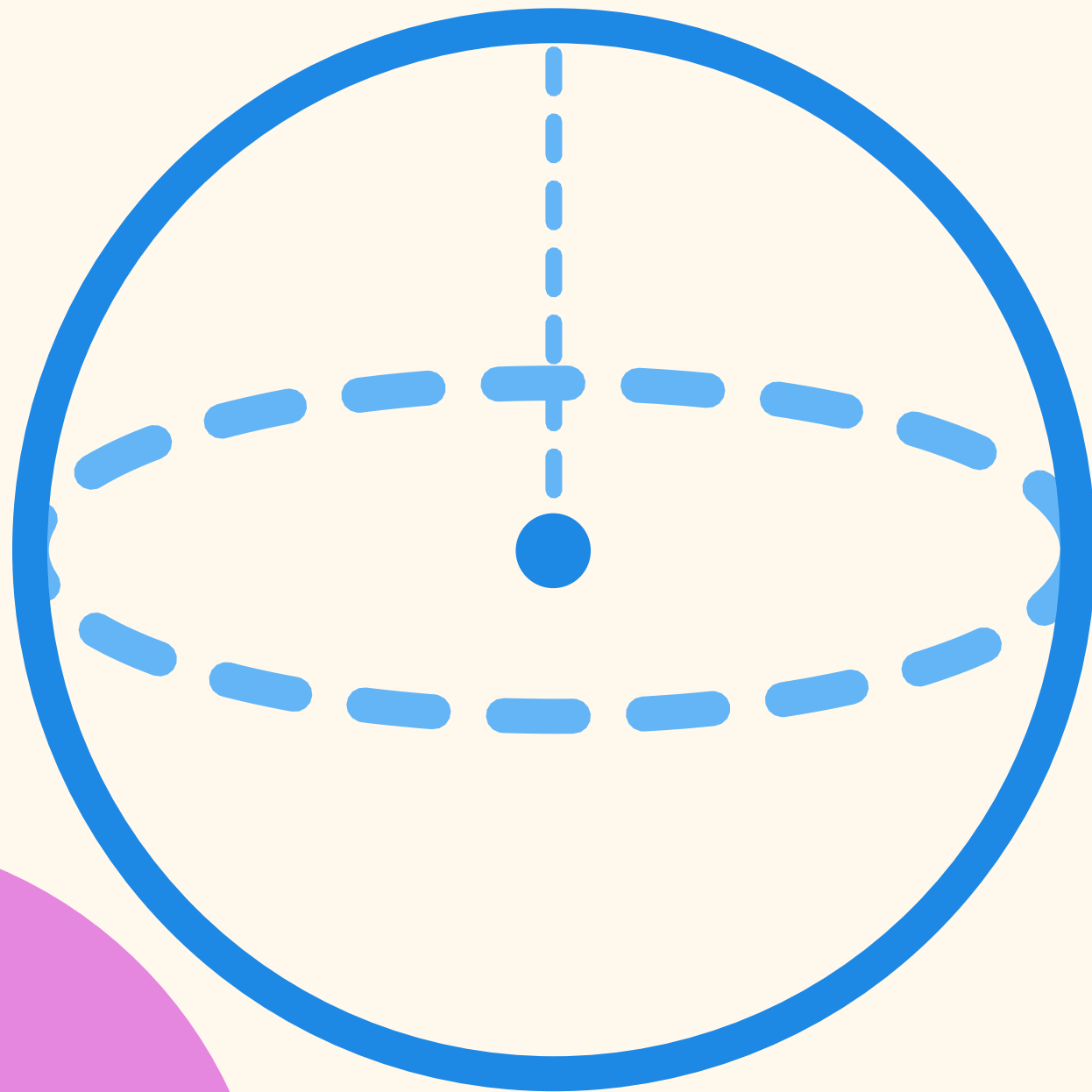
Surface Area of a Sphere

Total surface area of Sphere = $4\pi r^2$



Surface Area of a Sphere

$$\text{Total surface area of Sphere} = 4\pi r^2$$



If the radius of a sphere is 20 feet, find its surface area. (Use $\pi = 3.14$).

Surface Area of a Sphere

$$\text{Total surface area of Sphere} = 4\pi r^2$$



If the radius of a sphere is 20 feet, find its surface area. (Use $\pi = 3.14$).

The surface area of the sphere = $4\pi r^2 = 4 \times \pi \times 20^2 = 5024 \text{ feet}^2$
 \therefore The surface area of the sphere is 5024 feet^2

Try This!

Find the surface area of a sphere if its radius is given as 6 units.

