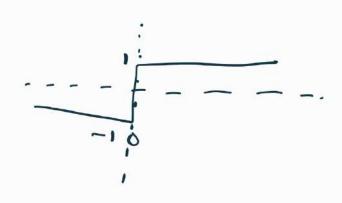


inhibitory inputs" refer to signals that decrease the likelihood of a neuron firing, while "excitatory inputs" are signals that increase the likelihood of a neuron firing

\* Perceptron.

Inputs con real, weights can be ditt too wiff.

$$f(x) = \sigma(\omega^T_X + b)$$



\* Dercettoon learning

\* Training data (x',y')Start with  $k \leftarrow 1 \notin W_k = 0$ While  $\exists : \in \mathcal{C}(1, 2 - \cdot \cdot N)$  Such that  $y: (w^T, x')_{\mathcal{K}}$ .  $W_{k+1} = W_k + y_i y_i$ k + t

HW Perceptoon wasning can we used for mp

A Porynomial orp.

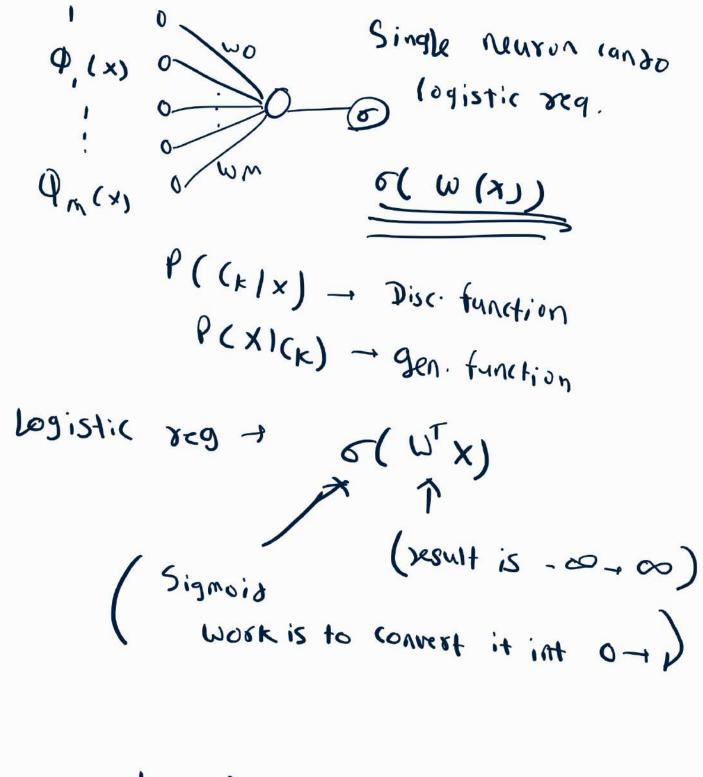
Bias-variance decomp.

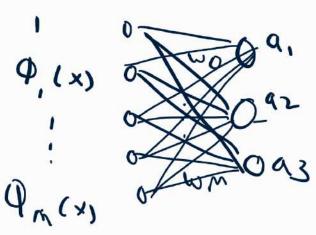
pre processing. (teature extraction)

Regularization

$$f = W^{T}(\phi(x))$$

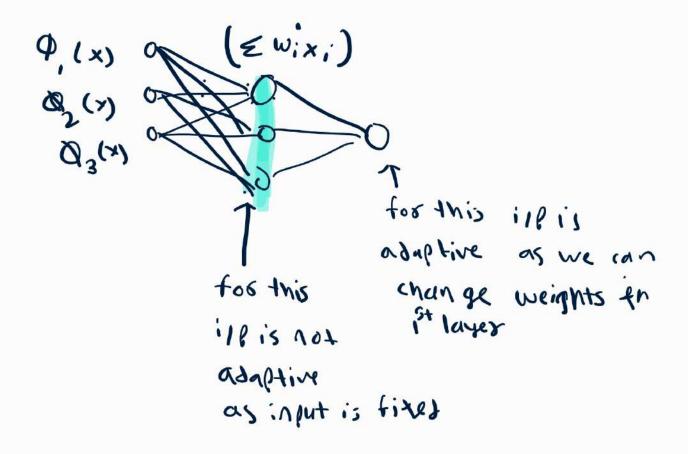
The degreesion.

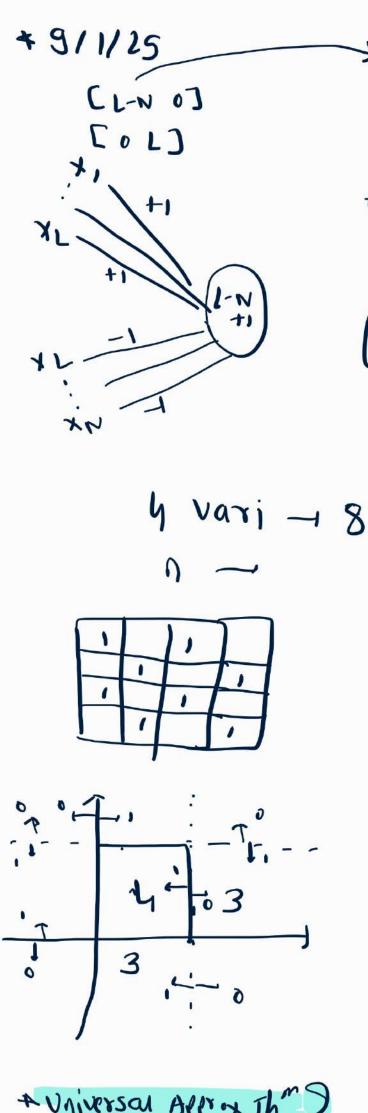




Theor comb of nonlinear bosis + n.

- With linear we can not do much
- We has to tix no. of the but make it
- where ANN comes in.





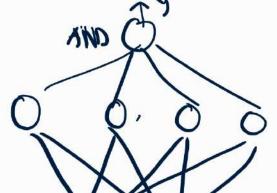
$$\begin{cases}
-1(N-L) \\
L-N
\end{cases}$$

$$+ (NB,C,D) = + NBCD + ...$$

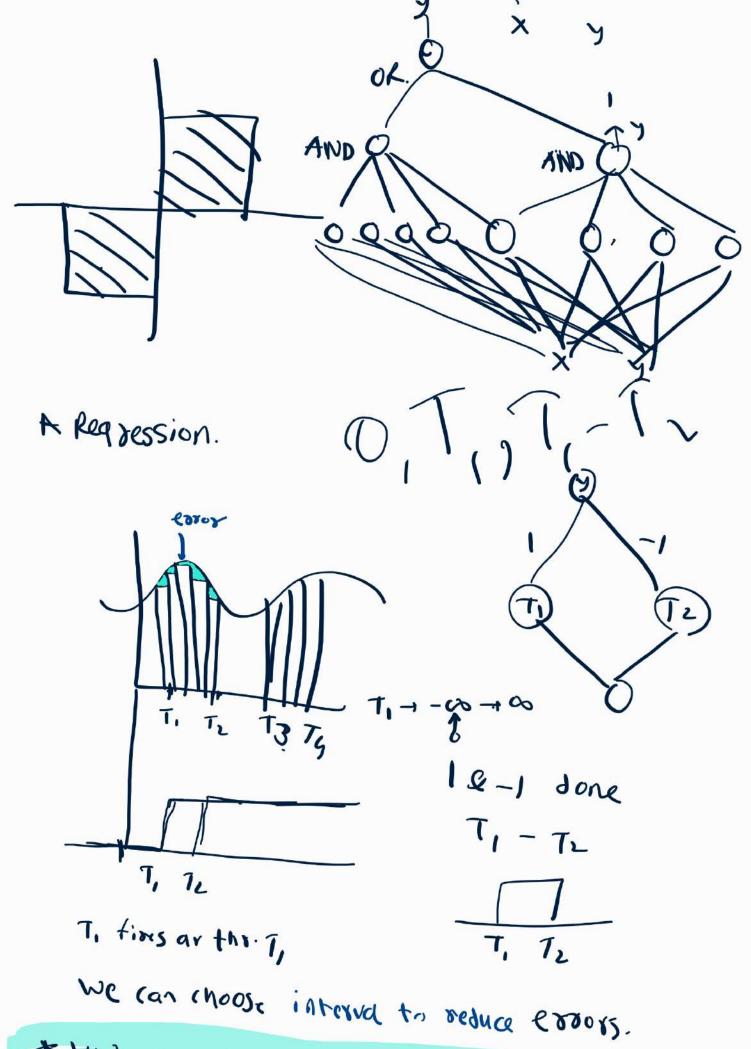
$$\begin{pmatrix}
V \\
i=1
\end{pmatrix}$$

$$V(V Xi)$$

make peoception which align with 4 lines & fix WWW It is 1

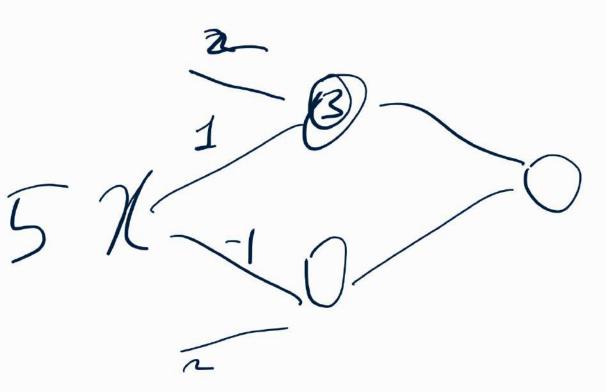


+ Universal Approx Thm)



\* HW no. of neurons too XOR

( b + wx) 0 TI Anything beyond 2 Layers in Deep NW. + Universal Approximation



\* 16/11/25

Graadient Descent.

9000 Fn + + toom F tind goodness of to f.

loss : Fx L = R.

I is increase with wrongness of f on 2.

possible loss for:-

Regression classification.

f with small risk R(f) = E2 (1(fiz))

to = argmin R(F) + EF

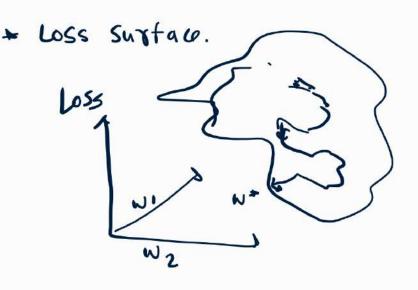
 $\hat{R}(f:0) = \hat{E}_{0}(f,z) = \frac{1}{N} \sum_{i=1}^{N} J(f,z_{i}).$ 

W\* = aregmin L(W) - optimize loss tunation.

W\* 6 = argmin ((+( w,6), D) w.b

How to getoptimal parameters.

linear regression. HOLOC (KNN)



Probe Jandon direction Progress it you tind useful direction Repeat.

Optimal looking:

Sense the slope around feet Identify steepest libr & make brief progress Repeat until convergence.
That is gradient descent.

Desivate of that point gives on the of change of tunition at that point.

$$\frac{d+}{dx} = \lim_{\delta \to 0} \frac{f(x+\delta) - f(x)}{\delta}$$

$$\Delta + = \frac{3}{4} \Delta \times .$$

$$\Delta t = K_D - K_D \qquad \times - \left( \frac{qx}{qt} - - \frac{qx^D}{qt} \right)$$

+ The vector gives dis 2 rate of tastes tinerease for f.

At = Jf. Dx. (dot Proluct)

= L(w) + Jw L(w).4.

God is minimize 1055.

$$\frac{2x}{2t} = \lim_{x \to 0} \frac{2}{t} + (x+2) - f(x)$$

A Baten Gr. descent

too i in dange (no-epoch)

VLW = evaluate (9000.(L.D.V) W=W-1 \* VLV.

Grussatel to converge global minima in case of convex for & local minima in case of non convex function.

+ Scahastic gogsicht descent.

\* Backpropagation

$$\frac{\partial x}{\partial x} = \frac{dg_{1}(x)}{dg_{1}(x)} \frac{dx}{dg_{2}(x)} - \cdots \frac{df}{df} \frac{dg_{N}(x)}{dg_{N}(x)}$$

$$f(x) = e^{\sin(x^2)}$$
  
=  $e^{\sin(x^2)}$   
 $\frac{2x}{2}$ .  $\cos(x^2) \cdot 2x$ .

$$\frac{S_{S_{1}}}{S_{1}} = \frac{S_{X_{1}}}{S_{X_{1}}} \cdot \frac{S_{X_{1}}}{S_{X_{1}}}$$

$$= \frac{S_{X_{1}}}{S_{X_{1}}} \cdot \frac{S_{X_{$$

$$P(Y_i|X) = \frac{e^{X_i}}{\sum_{i=1}^{N} e^{X_i}}$$

$$Softmax$$
 Non linearly.

$$X_i = e^{S_i}$$

$$\frac{\delta x_i}{\delta s_j} = 0$$
 for hildenlayer

i ≠ j

FOO SOHMAX OIP layer this not valid.

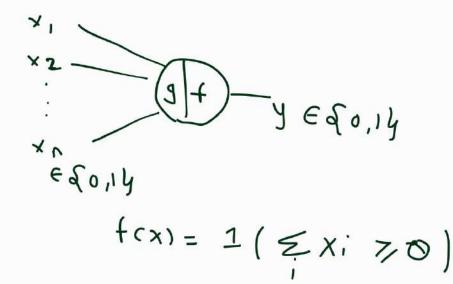
### \* NOTES FOR EXAM (24/11/25)

The Neuron.

Threshold Logic unit - 1st math model for neuron.

MP neuron.

Boolean ijp.

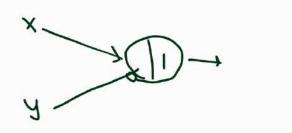


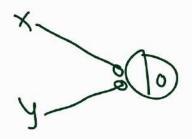
TIP can be excitatory & Inhibitory

To more likely Reduce
tire Likelihood.

- When Inhibitory i/p set (1) then opp to

Court no. of ON signals on exit. i/p vs





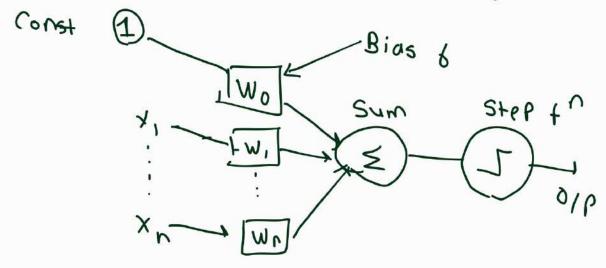
\* Leasn linear separation.

- No learning.

+ Perception.

- Same like MP.
- I nput can be real,
- weight can be diff. for diff. IIP.

- $f(x) = G(w^Tx + b)$  - Activation function.
- mechanism for learning weights.



- Training Data. (x', y') { -(-1, 14. Start k = 1 & WK = 0

while = : E & 1 -- 1) 5+ y i (wx, xi) Ko. upache m \* + 1 = m \* + 2 x ;

KF K+1.

- Bias can be appended with I suitably.

- \* Convergence Result.
  - For linear sep. dataset algo converges at Her finite iterations.
  - Stop as soon as find boundary.
- \* Perception learning code.

imboot torch.

D1 = tooch. normal (0.0, 1.0, Size [100,2])

D2 = torch. Normay 1 3.0, 1.0, Size=[100,2])

# Generale 100 data point from 2 Dwith mean

(0 & 3) & S.D of 1 & store in D, .D1.

PIt. scatter (D,[:,0], D,[:,1]) PIt . SCatter (D) [:,0], D) [:,17)

X = touch - empty (200, DI(5: ze (1)+1), fill\_(1))

X[1::2:2] = DZ

Print (X. Shafe)

7= tooch . culti(200,1)

4[::1,:2] = 1.0

9[1::2,:2] =-1.0

Bilt( Y. Shape)

# [200,3] [200 I]

(reate x with (200,3) fill with)

Store 1/P tox perception.

extra Dim for Bias.

```
C WOX MAND
                    4 Assign.
      099 ROM DS
      y emply - labelt.
       PVIN - 1.
    # 099 -1.
 W = torch. zeros (X. Size (1)). -- initialize W by U.
get trainperception (x, y, w, ebock)
    tor e in range (eporh)
        change = 0
        fox ( i = 0 - X. Size (0))
            o19+xm.. ?=> [:] h * (m) +0 fo
                w= w+ 4[i] *x[i]
               change = change +1
                                       W= W + xy.
         it change = = 0
             boeak # early stop.
    Print ( no. of changes., change).
  return w.
 W = tooin-perception (x, y, w, 5)
```

brivt (M)

\* DL-2.

#### Linear classifiers.

Sometime data is linearly seperable Sometime not Sometime specific preprocessing can make it seperable.

In XOR.

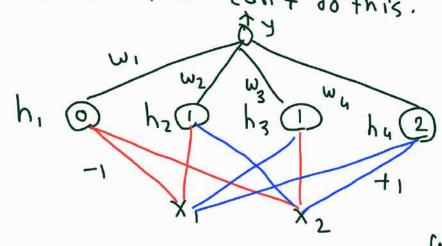
$$\phi(x) = \phi(x_u, x_v) = (x_u, x_v, x_u x_v)$$
Make new dimension than the

- make new dimension then you found the seperable
- Increasing dimension (degree) increase rapacity.
- Reduce Bias increase capacity.
- preprocessing is also may way to reduce capacity.

#### XOR:

Χı	X <sub>2</sub>	XOR	
0	0	0	$\omega_{\delta} < 0$
0	1	Ī	
1	0	,	$W_2+W_0 7/0 = W_27/-W_0$
1	1	, ,	W
		O	$\omega_1 + \omega_0 > \sigma = \omega_1 - \omega_1$
			W, + W2 + W0 TO = W, + W2 (-14)
((0))			5, mo 10 = m, + m/-14

Single perception can't do this.



W, WZ W3 W4

$$(0,0) = (-1) 0 + (+1) \cdot 0$$
  
=  $(h_1 = 0) h_2 = 0 h_3 = 0 h_4 = 0$ 

$$(0,1) = -1, (1), -1, 1$$

this fire.

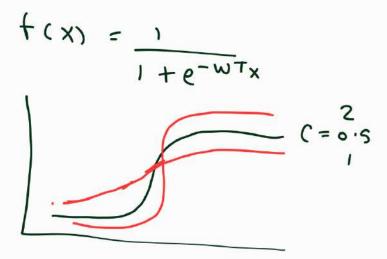
$$W, \zeta - W_0$$
  $W_2 7, -W_0$   $W_3 7, -W_0$ 
 $W_4 \leftarrow W_0$ 

Possible Find this weights

\* other 2 i/P boolean + .

- Can possible with 2 perceptson in hidden layer
- 2n+1 is sufficient but not necessary
- MLP (multi layer N/w of perceptson)

- + many real world problem have non-binary off.
  Peraphron only gives 2 off.
  - \* Sigmoid neuron.

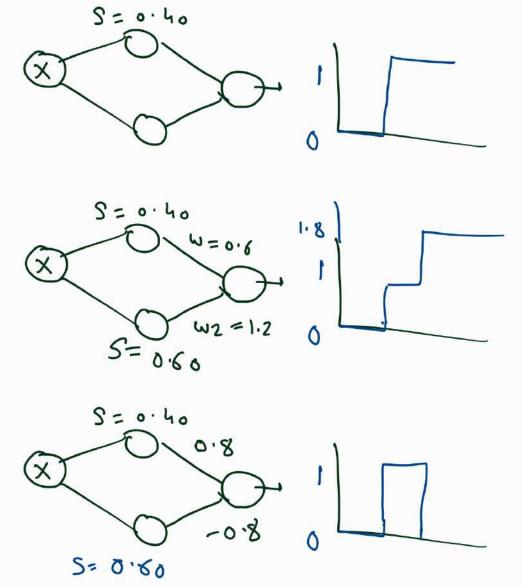


- Any Boolean function with n ill depresent with one hidden layer.
- approximation with linear comb. of sigmoid
- Neural N/w with single hidden layer used to approx any cont. for to any desired precision
- Using Kmap we can have 2N-1 perc. in hilden
- 3(N-1) refuires in deep Nim. Linear in N.

\* Unitorn Approximation Thm.

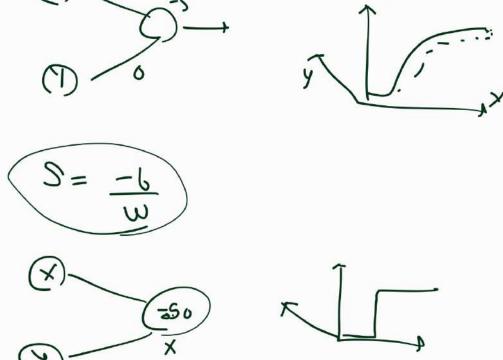
Using simple model (with I hidden layer) you can approximate any continuous function as closely

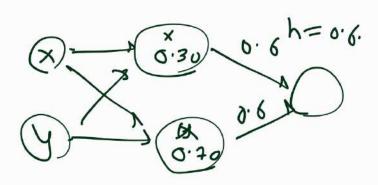
- Sigmoid neuron is taken ill & Mocoss & Moduce of
- NN with one hidden layer can tit any continuous

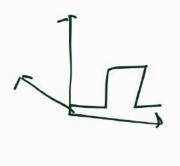


We only computed weighted sum of hidden outputs.

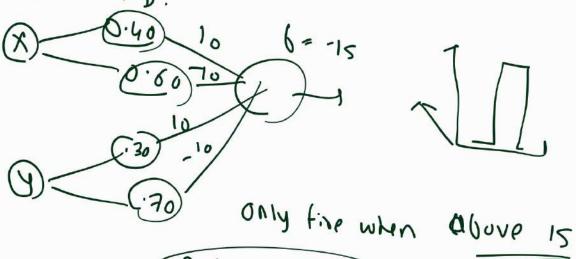
who 2:16 ms der 3 D blow.







\* Tower in 3D.



0.40 - 0.60

- \* Target to lie on space other than hypercube.
  - Discontinuord target can be approximately arbitrary well 6 is serveral as non poly for
- \* It one later is good than why we need deep N/W
  - May require inteaseble size for hidden layer.
  - May not generalize well.
  - Not enable hierarchical learning.

## \* DL-4

Learning - Finding + from F.

- Fox good function we use Loss.
- 1: F x / R.
- Such that value 1(t,z) increases with worning of + on Z. (diff. bet, expected & bregicted)
- Regression: 2 (f,(x,y)) = (f(x)-y)2 classification: Q(f,(x,y)) = 1(f(x) + y)
  - Density est: 1 (9,2) = log(2(z))
- We want + with expected bisk R(f) = EZ(I(f.71)
- f" = argmin R(f)
- Emperical Risk.

$$\hat{R}(f;D) = \hat{E}_{D}(l(f,z)) = \frac{1}{N} \sum_{i=1}^{N} l(f,z_{n})$$

- model Param, that minimize 1055 fn.

- How to find optimal parameters.
  - close From Solution. (linear Reg.)
  - Ad hoc secipes ( proceptson, KNN Clasifier)

\* How to tind minimum loss surface.

- Probe random directions
- progress it you find useful direction
- Repeat.
- Ineffective.

Better :- Follow the slope.

- Sense the slope around feet.
- Identify stiffest dig, make brief progress
- Repeat.
- GRADIENT DESCENT.

\* Derivative of that given point gives rate of change of that that point.

$$\frac{dx}{dx} = \lim_{\delta \to 0} \frac{f(x+\delta) - f(x)}{f(x+\delta)}$$

$$AA = \frac{\lambda}{\lambda} = \lambda$$

in higher dimensions

$$\nabla + : R^{\mathfrak{D}} \rightarrow R^{\mathfrak{D}}$$

$$x \rightarrow \left(\frac{\partial x}{\partial t}, - - \frac{\partial x}{\partial t}\right) - - gives dir de sate$$

((w+u) = ((w) + \nu ((w) . u , L(w) - loss atw To minimize loss ((w+u) > ((w)) 1 Dm<(m) + deagieur of 1055 9+ W. 7 w 2(w). u 7 o. 1 U + 5HP -diff. would be less if uis in opp. , Marix 72 ((w) -1 Hessian Matrix

# \* GRADIENT DESCENT

- Grow to minimize the error.
- Determine pareameter w that minimize ((w)
- Gradient points uphill - ve of good. Points downhill

\* Start with orbitrary initial parameter wo.

- Repeatedly modify it via updating in 5 may 5+pg
- At each step modify gis that broduce steepest descent along with expor

\* Numerically for each w.

$$\frac{8x}{8t} = \lim_{x \to 0} \frac{4(x+8) - f(x)}{8}$$

Slow & approximate.

\* Analytical methods.

- me rest this or unuescital winds is slow & allega - Analytical is exact & Micline (Calcular) use to raiculation in backpyp.

L; = \( Max (0,5j-Sy; +1) \rightarrow hirge loss

S = f(x,w)

TLiw = T Hingeloss + T Regularization.

J 85j - 85y: + 2 x W. L it 5; -5y; +170

Otherwise

& Batch Goadient Jescent.

tos i in soude (up-6 boin).

VLW = evaluate-goodient (1,D,w) W=W-1\*7LW

- It teems of convex travition for draseved get global minima.

\* Stochastic Gro. De.

weight update parameter for each training example  $w = w - N \nabla w L(w, xi, yi)$ 

- In cose of large Ds Batch GD compute & edunation gradients for similar example.
  - SGD does away with redundency & taster can be used to learn online.
  - Forquest updates with high variance lause objective
  - SGD fluctuation enable it to jump new & better local mining.
  - Complicate convergence.

for in range (e1-epo(n)

Np. sandom Shuffle (D)

too X; ED

VLW = evaluate gradient (L, X;, W)

W=W-N\* VLW.

\* Mini Botch Gro. De.

Best of both & update pasom every minibatch.

W= W-n Tw ((w, x 1:i+n, y1:i+n))

Reduce vasiance of pasom. updates

Used highly optimized matrix optimization.

Batch size 32 - 1471

too i in range ( NB epoch) np. random. shuffle (D) too latin in get lather (D. batchsiz = 128) Ow= evaluate 9 radient (L, 6atin, W) W= W- 1 + 7 lw.

\* Some challanges

- choose proper learning rate
- Make learning date applies to all param.

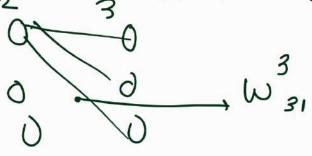
  Avoid numerous sub-optimal local minima.

Gradient of scaler of  $f(x) = \chi \rightarrow \left\{ \frac{\partial f}{\partial x}, -\frac{\partial f}{\partial y} \right\}^{7}$ .
Grandient of vector values of alles Tac.

$$J = \begin{bmatrix} \frac{\partial f}{\partial x_{1}} & -\frac{\partial f}{\partial x_{1}} \end{bmatrix} = \begin{bmatrix} \frac{\partial f}{\partial x_{1}} & -\frac{\partial f}{\partial x_{1}} \\ \frac{\partial f}{\partial x_{1}} & -\frac{\partial f}{\partial x_{1}} \end{bmatrix} = \begin{bmatrix} \frac{\partial f}{\partial x_{1}} & -\frac{\partial f}{\partial x_{1}} \\ \frac{\partial f}{\partial x_{1}} & -\frac{\partial f}{\partial x_{1}} \end{bmatrix}$$

ωjκ.

Connecting jth neuron in eth layer & kth neuron in (2-1)th layer.



bi bias of ith neuron in 1th layer.

x 1; op of jth neuron in Ith later.

$$x = 6 \left( \sum_{k} \omega_{jk} x_{k}^{d-1} + b_{j}^{d} \right)$$

\* vector of bios in layer 1 + 61.
What weight vector of layer 1.

$$S_{j}^{l} = \mathcal{E}_{k} \omega_{jk}^{l} \times_{k}^{l-1} + \delta_{j}^{l}$$

\* Loss 
$$\ell(w, b) = \sum_{n} J(f(x_n : w, b), y_n) = \sum_{n} \ell(x_n^{\perp}, y_n).$$

$$\chi = \chi \frac{1}{M(1)}, \frac{1}{M(1)}$$

$$x^{0} = x, f(x: W, b) = x^{(1)}$$

$$\forall \mathcal{I} = 1 - \dots \setminus \mathcal{I} = \mathcal{I} = \mathcal{I} = \mathcal{I} = \mathcal{I} + \mathcal{I}$$

\* Chain oute.

$$(f_0g)'(x) = f'(g(x)) \cdot g'(x)$$

$$\frac{dx}{dy} = \frac{dy}{dy} \cdot \frac{dx}{dx}$$

$$\frac{dx}{dy} = \frac{d(a(x))}{dt} \cdot \frac{dx}{dt}$$

$$A = \frac{VB}{X} = VA$$

$$2 = g(x) \rightarrow \Delta z = \frac{Jg(x)}{Jx} \Delta x.$$

$$4 = f(z) \rightarrow \Delta x.$$

$$y = f(z) \rightarrow \Delta y = \frac{\partial f}{\partial z} \Delta z = \frac{\partial f}{\partial z} \cdot \frac{\partial g(x)}{\partial x} \Delta x$$

$$= \frac{\partial f}{\partial (g(x))} \frac{\partial g(x)}{\partial x} \Delta x$$

$$\frac{dy}{dx} = \frac{df}{dx} (x), q_2(x) = --q_M(x)$$

$$\frac{dx}{dx} = \frac{df}{df} \frac{dg_1(x)}{dg_1(x)} + \frac{df}{dg_1(x)} \frac{dx}{dg_1(x)}$$

$$\Delta A = Y \in A + (2' - - \cdot 2W)$$

$$\Delta y = \frac{\delta f}{\delta z_1} \Delta z_1 + \frac{\delta f}{\delta z_2} \Delta z_2 - - \cdot \frac{\delta f}{\delta z_m} \Delta z_m$$

$$\Delta y = \frac{\delta f}{\delta z_1} \Delta z_1 + \frac{\delta z_2}{\delta z_2} \Delta z_2 - - \cdot \frac{\delta f}{\delta z_m} \Delta z_m$$

$$\Delta y = \frac{\partial f}{\partial z_1} \frac{\partial z_1}{\partial x} \Delta x + \frac{\partial f}{\partial z} \frac{\partial z_2}{\partial x} \Delta x - \cdots$$

$$\Delta y = \frac{\partial f}{\partial z_1} \frac{\partial z_1}{\partial x} \Delta x + \frac{\partial f}{\partial z} \frac{\partial z_2}{\partial x} \Delta x - \cdots$$

$$\nabla \lambda = \left(\frac{9 d^{1(x)}}{9 t} \frac{9 d^{1(x)}}{9 d^{1(x)}} \cdots \right) \nabla x.$$

$$\frac{\partial L}{\partial g} = \frac{\partial L}{\partial f} \cdot \frac{\partial f}{\partial g} \cdot = (-2) \times \int_{1}^{1} f = g + 2.$$

$$\frac{\partial L}{\partial g} = \frac{\partial L}{\partial f} \cdot \frac{\partial f}{\partial g} \cdot = (-2) \times \int_{1}^{1} f = g + 2.$$

$$\frac{\partial L}{\partial g} = \frac{\partial L}{\partial f} \cdot \frac{\partial f}{\partial g} \cdot = (-2) \times \int_{1}^{1} f = g + 2.$$

$$\frac{\partial L}{\partial g} = \frac{\partial L}{\partial f} \cdot \frac{\partial f}{\partial g} \cdot = (-2) \times \int_{1}^{1} f = g + 2.$$

$$\frac{dd}{dt} = -2$$

$$\frac{dd}{dt} = -2$$

$$\frac{dL}{dt} = \frac{dL}{dt} \cdot \frac{df}{dt} = -2$$

$$\frac{dL}{dt} = \frac{dL}{dt} \cdot \frac{df}{dt} = -2$$

$$\frac{dL}{dt} = \frac{dL}{dt} \cdot \frac{df}{dt} = -2$$

$$\frac{x}{y} = -2$$

$$\frac{d}{dy} = -2$$

$$\frac{\partial L}{\partial x} = \frac{\partial L}{\partial g} \cdot \frac{\partial g}{\partial x}$$

$$= (-2) \times y$$

$$= (-6) - -(y = 3)$$

$$\frac{d2}{dy} = \frac{dL}{dg} \cdot \frac{dq}{dy}$$

$$= (-2) * x$$

$$= \frac{4}{4}$$

Town stream All = dl dg - Hocal we calcumpte beauty

 $T + N \circ f_{N-1} \circ \cdots f_{j}(x) = f_{N} (f_{N-1})(\cdots f_{j}(x)) \circ \cdots f_{j}(x)$   $(f_{N-2} \cdots f_{j}(x)) \cdots f_{j}(x)$  T + f(x) is Tacobian of F computed at x.

\* Backpropagation.

Take any layer.

$$x_{i}^{!} = e(s_{i}^{!})$$
 $x_{i}^{(s_{i}-1)} = e(s_{i}^{!})$ 
 $x_{i}^{(s_{i}-1)} = e(s_{i}^{!})$ 

s influence loss L through x(2) only.

$$\frac{Sx}{Ss_{(\delta)}} = \frac{Sx}{Sx_{(\delta)}} \cdot \frac{Sx_{(\delta)}}{Ss_{(\delta)}}$$

$$= \frac{Sx}{Sx_{(\delta)}} \cdot \frac{Sx_{(\delta)}}{Ss_{(\delta)}}$$

$$S_{i}^{(l)} = \sum_{j} W_{ij}^{(l)} \times_{j}^{(l-1)} + G_{i}^{(l)}$$

$$S_{i}^{(l)} = \sum_{j} W_{ij}^{(l)} \times_{j}^{(l)} + G_{i}^{(l)}$$

$$\frac{SL}{S_{x_{j}^{(k-1)}}} = \underbrace{\sum_{i} \frac{SL}{S_{x_{i}^{(k)}}}}_{i} \underbrace{\frac{SS_{i}(1)}{S_{x_{i}^{(k-1)}}}}_{S_{x_{i}^{(k-1)}}}$$

$$= \underbrace{\sum_{i} \frac{SL}{S_{x_{i}^{(k)}}}}_{S_{x_{i}^{(k)}}} \underbrace{\frac{SS_{i}(1)}{S_{x_{i}^{(k-1)}}}}_{S_{x_{i}^{(k)}}} \underbrace{--Sev.ot is w.}_{(wx+6)}$$

wheel influence loss via sh.

$$S_{i}^{(l)} = S_{j} W_{ij}^{(l)} X_{j}^{(l-1)} + \delta_{i}^{(l)}$$

$$\frac{S_{N}}{S_{N,i,j}} = \frac{S_{N,i,j}}{S_{N,i,j}} = \frac{S_{N,i,j}}{S_{N,i,j}} = \frac{S_{N,i,j}}{S_{N,i,j}} = \frac{S_{N,i,j}}{S_{N,i,j}} \times (1-1)$$

$$\frac{g_{\beta}(g)}{g_{\beta}(g)} = \frac{g_{\beta}}{g_{\beta}} \frac{g_{\beta}(g)}{g_{\beta}(g)} = \frac{g_{\beta}(g)}{g_{\beta}(g)}$$

Recursively compute loss dev. wat activations.

$$\frac{g_{s'(g)}}{g_{1}} = \frac{g_{x'}}{g_{1}} e_{(s',g)}$$

$$\frac{g_{x_{j}}}{g_{x_{j}}} = \sum_{i} \frac{g_{s_{i}}}{g_{s_{i}}} \cdot w_{i}$$

$$\frac{g_{x_{i}}}{g_{x_{i}}} = \sum_{i} \frac{g_{s_{i}}}{g_{s_{i}}} \cdot w_{i}$$

$$Gaugiant-$$

then wit parameters.

$$\frac{gg}{gw_{ij}} = \frac{gg}{gs_{i}} \times \chi_{j}^{(1-1)} \qquad \frac{gg}{gs_{i}} = \frac{gg}{gs_{i}}$$
 Param.

$$\psi: k_{N} \rightarrow k_{w} \quad \text{then} \left[ \frac{\partial h}{\partial x} \right] = \left[ \frac{\partial h}{\partial x} \right] - \frac{\partial h}{\partial x}$$

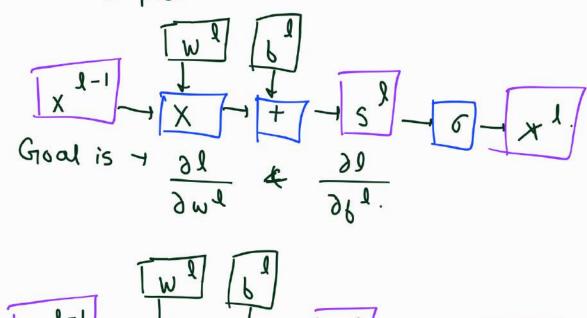
$$\frac{\partial h}{\partial x} - \frac{\partial h}{\partial x}$$

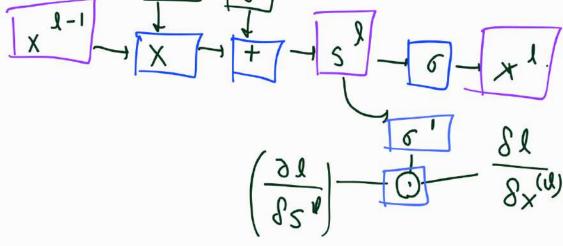
$$\frac{\partial h}{\partial x} - \frac{\partial h}{\partial x}$$

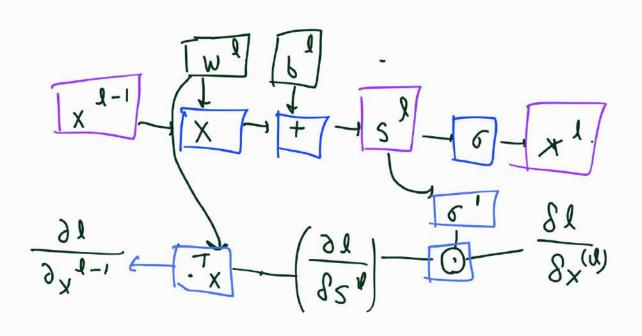
$$A = \sum_{N \times w} B + \mu \ln \left[ \left[ \frac{4x}{4h} \right] \right] = \left[ \frac{9m^{N}}{9h} \right] - \frac{9m^{N}}{9h}$$

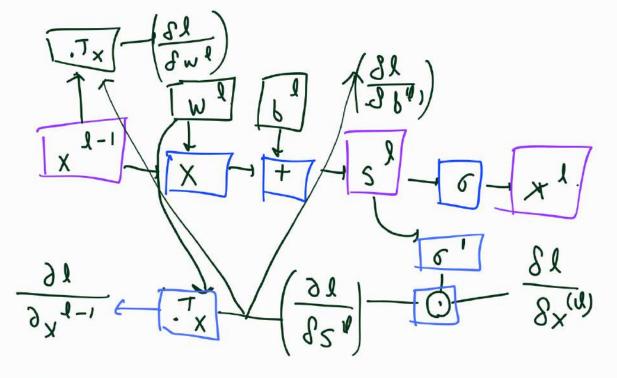
$$\frac{9m^{N}}{9h} - \frac{9m^{N}}{9h}$$

\* Forward pass









uplate pasams

$$w' = w' - \sqrt{\left[\frac{\partial w}{\partial x}\right]} \sqrt{\left[\frac{\partial w}{\partial y}\right]}$$
is applying a  $\delta = \delta - \sqrt{\left[\frac{\partial \delta}{\partial y}\right]}$ 

BP is applying chain ouce iteratively.

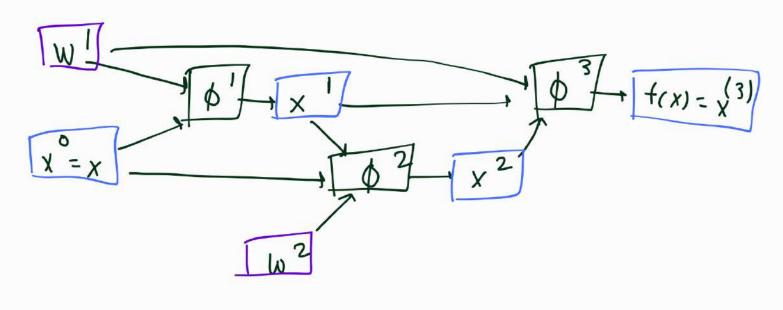
expressed in tensorial from

Heavy computation with linear ops.

Non-lin. goes with simple element wise ops.

BP needs au int layer result to be in memory Take twice the computations of Fw pass.

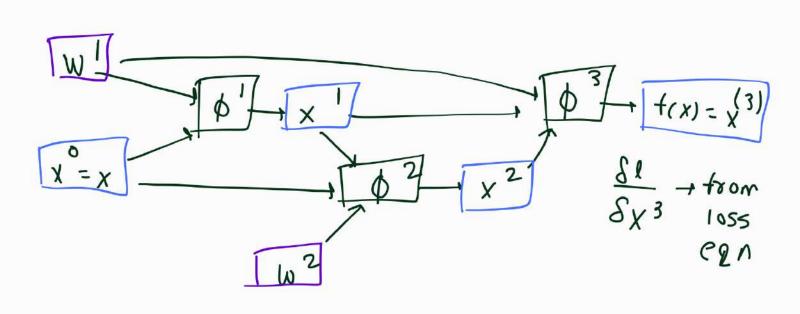
\* For an Example.

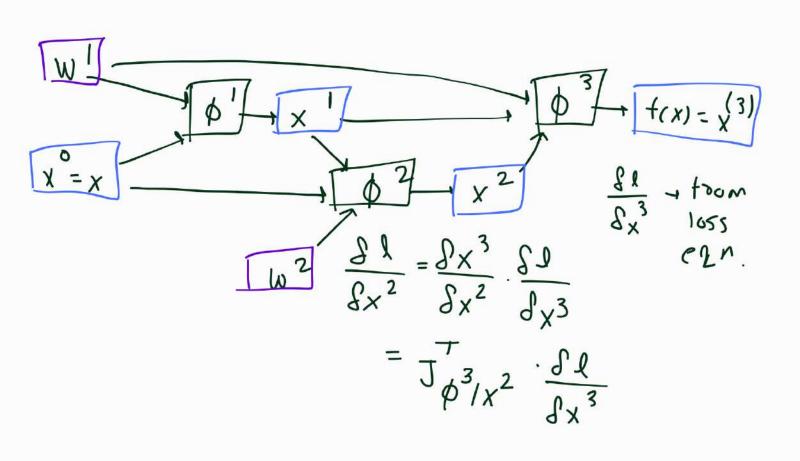


Forward pass

$$x^{\circ} = x$$
 $x' = \phi'(x^{\circ}.\omega')$ 
 $x^{2} = \phi^{2}(x^{\circ}, x', \omega^{2})$ 
 $x^{3} = \phi^{3}(x', x^{2}, \omega')$ 

\* Back propagation.





$$\frac{SI}{Sx'} = \frac{g_{x'}^{3}}{g_{x'}} \cdot \frac{fl}{f_{x'}^{3}} + \frac{f_{x'}^{2}}{f_{x'}^{3}} \cdot \frac{fl}{f_{x'}^{2}}$$

$$= \int_{\phi^{3}/y}^{7} \frac{dl}{dx^{3}} + \int_{\phi^{2}/x}^{7} \cdot \frac{sl}{f_{x'}^{2}}$$

$$= \int_{\phi^{3}/x^{2}}^{7} \cdot \frac{g_{x'}^{2}}{g_{x'}^{3}} \cdot \frac{g_{x'}^{2}}{g_{x'}^{3}} \cdot \frac{g_{x'}^{2}}{g_{x'}^{3}}$$

$$= \int_{\phi^{3}/x^{2}}^{7} \cdot \frac{sl}{f_{x'}^{3}} \cdot \frac{sl}{f_{x'}^{3}}$$

$$= \int_{\phi^{3}/x^{2}}^{7} \cdot \frac{sl}{f_{x'}^{3}} \cdot \frac{sl}{f_{x'}^{3}}$$

$$\frac{Sl}{Sx'} = \frac{gx^3}{gx'} \frac{\int l}{\int x^3} + \frac{fx^2}{fx'} \frac{\int l}{\int x^2}$$

$$= \int_{\phi^3/y}^{3} \frac{dl}{dx^3} + \int_{\phi^2/x}^{7} \frac{dl}{dx^2}$$

$$= \int_{\phi^3/x}^{7} \frac{dl}{dx^3} + \int_{\phi^2/x}^{7} \frac{dl}{dx^2}$$

$$= \int_{\phi^3/x^2}^{7} \frac{\int l}{dx^3} \frac{dl}{dx^3} + \int_{\phi^2/x}^{7} \frac{dl}{dx^3}$$

$$= \int_{\phi^3/x^2}^{7} \frac{\int l}{dx^3} \frac{dl}{dx^3}$$

$$= \int_{\phi^3/x^2}^{7} \frac{\int l}{dx^3} \frac{dl}{dx^3}$$

$$= \int_{\phi^3/x^2}^{7} \frac{dl}{dx^3} + \int_{\phi^2/x^3}^{7} \frac{dl}{dx^3}$$

$$= \int_{\phi^3/x^3}^{7} \frac{dl}{dx^3} + \int_{\phi^3/x^3}^{7} \frac{dl}{dx^3} + \int_{\phi^3/x^3}^{7} \frac{dl}{dx^3}$$

$$= \int_{\phi^3/x^3}^{7} \frac{dl}{dx^3} + \int_{\phi^3$$

New todining samples may change BP minimally Prefers consistency (low variance) over perfection (low. minimizing pooxy may not minimize actual.

- Saddle points are more trequent than local minima.
- most local minima are equivalent & close to global