

# Homework 1

## Maths Introduction

### Some modular arithmetic

1. Working with the following set of Integers  $S = \{0,1,2,3,4,5,6\}$  **Meaning that the prime number is 7**

What is

a)  $4 + 4$   **$4+4 = 8 = 1 \bmod 7$**

b)  $3 \times 5$   **$3 \times 5 = 15 = 1 \bmod 7$**

c) what is the inverse of 3 ? **\*Applying Fermat little's theorem:  
Multiplicative inverse:  $3^{(7-2)} \bmod 7 = 5$ ,  
\*Additive inverse is  $4 : 3 + 4 \bmod 7 = 0$**

2. For  $S = \{0,1,2,3,4,5,6\}$

Can we consider 'S' and the operation '+' to be a group ?

3. What is

$-13 \bmod 5$  ?  **$-13 \bmod 5 = 2$**

4. Polynomials

For the polynomial  $x^3 - x^2 + 4x - 12$

Find a the positive root ? **Solve where eq = 0,  $x = 2$**

What is the degree of this polynomial ? **Degree = 3**

**2) (S,+s) is a group.**

#### i. Closure

**(S,+s) is close under the +s operation. Since it is  $Z_7$ , for all a, b in S,  $a +s b \bmod 7$  in the S.**

#### ii. Associativity

**From the closure,  $a +s b = (a + b) \bmod 7$  where + operation is ordinary addition in  $Z$ .**

**$a +s (b +s c) = (a + b) + c \bmod 7$  (from  $(Z, +)$  is associative )**

**$(a + b) + c \bmod 7 = (a +s b) +s c$  therefore (S,+s) is also associative.**

#### iii. Identity Element

**Is there any element a in S, so that for all b in S,  $a +s b$  is equal b.**

**$a = 0$**

**iv. Each element except the identity(zero), has the inverse under the addition operation.**

**Not elegantly :)**

**the inverse of 1 equals 6 since  $1 +s 6 = 0$**

**So each element has its inverse.**

**From i, ii, iii, and iv, (S,+s) is a group.**

## Use cases

In your teams discuss any systems you have used that involved zero knowledge proofs.

Have you seen any applications of zero knowledge proofs other than with a blockchain ?

What is to you, the most important feature of zkp technology ?

Think of some use cases of zero knowledge proofs that you would like to see developed.