

I. Recursion

- A method of defining a function in terms of its own definition.
- Example:- The Fibonacci Series
 1. $f(n) = f(n-1) + f(n-2)$
 2. $f(0) = f(1) = 1$ ←----- base case
- In programming, recursion is a method call to the same method.

II. Why write a method that calls itself?

- Recursion is a good problem-solving approach.
- Recursion algorithms are elegant, simple to understand and prove correct, easy to implement. [BUT!!! ... Recursive calls can result in an infinite loop of calls. It needs a base-case in order to stop.]

III. Recursive algorithms

- To solve a problem recursively -
 1. Break into smaller problems
 2. Solve sub-problems recursively ←----- Problem solving technique:
 3. Assemble sub-solutions Divide-and-Conquer

```
recursive-algorithm( input ) {  
  // base-case  
  if (isSmallEnough( input ))  
    Compute the solution and return it  
  else  
    // recursive case  
    Break inout into simpler instances input 1, input 2, ...  
    solution1 = recursive-algorithm( input1 )  
    solution2 = recursive-algorithm( input2 )  
    .....  
    figure out solution to this problem from solution1, solution2, .....  
    return solution  
}
```

IV. Example

1. Write a function that computes the sum of numbers from 1 to n.

int sum (int n)

- Use a loop
- Recursively

//with a loop

```
int sum (int n) {  
    int s = 0;  
    for (int i=0; i<n; i++)  
        s+= i;  
    return s;  
}
```

//recursively

```
int sum (int n) {  
    int s;  
    if (n == 0) return 0;  
    //else  
    s = n + sum(n-1);  
    return s;  
}
```

HOW DOES THE RECURSION ONE WORK?

