

### **Chapter 2**

Algorithm
Discovery and
Design



### Learning Objectives (1 of 2)

- Explain the benefits of pseudocode over natural language or a programming language
- Represent algorithms using pseudocode
- Identify algorithm statements as sequential, conditional, or iterative
- Define abstraction and top-down design, and explain their use in breaking down complex problems

### Learning Objectives (2 of 2)

- Illustrate the operation of algorithms for:
  - Multiplication by repeated addition
  - Sequential search of a collection of values
  - Finding the maximum element in a collection
  - Finding a pattern string in a larger piece of text



#### Introduction

- Everyday algorithms, such as hair washing, may not be suitable for computers to perform (as in Chapter 1).
- Algorithmic problem solving focuses on algorithms suitable for computers such as searching lists and matching patterns.
- Pseudocode is a tool for designing algorithms but does not run on a computing device.
- This chapter will use a set of problems to illustrate algorithmic problem solving, including those with conditional statements and loops.



#### Representing Algorithms (1 of 5)

- Natural language is:
  - Expressive and easy to use
  - Verbose, unstructured, and ambiguous
- Programming languages are:
  - Structured and designed for computers
  - Grammatically fussy and cryptic
- Pseudocode lies somewhere between these two and is used to design algorithms prior to coding them



### Representing Algorithms Natural Language (1 of 2)

#### FIGURE 2.1

Initially, set the value of the variable carry to 0 and the value of the variable i to 0. When these initializations have been completed, begin looping as long as the value of the variable i is less than or equal to (m - 1). First, add together the values of the two digits  $a_i$  and  $b_i$  and the current value of the carry digit to get the result called ci Now check the value of  $c_i$  to see whether it is greater than or equal to 10. If  $c_i$  is greater than or equal to 10, then reset the value of carry to 1 and reduce the value of  $c_i$  by 10; otherwise, set the value of carry to 0. When you are

### Representing Algorithms Natural Language (2 of 2)

finished with that operation, add 1 to i and begin the loop all over again. When the loop has completed execution, set the leftmost digit of the result  $c_m$  to the value of carry and print out the final result, which consists of the digits  $c_m c_{m-1...} c_0$ . After printing the result, the algorithm is finished, and it terminates.

The addition algorithm of Figure 1.2 expressed in natural language

### Representing Algorithms Programming Language

```
FIGURE 2.2
  Scanner inp = new Scanner(System.in);
  int i, m, carry;
  int[] a = new int[100];
  int[] b = new int[100];
  int[] c = new int[100];
  m = inp.nextInt();
  for (int j = 0; j \le m-1; j++) {
         a[j] = inp.nextInt();
         b[j] = inp.nextInt();
  carry = 0;
  i = 0;
  while (i < m) {
      c[i] = a[i] + b[i] + carry;
      if (c[i] >= 10)
```

The beginning of the addition algorithm of Figure 1.2 expressed in a high-level programming language



#### Representing Algorithms (2 of 5)

- Sequential operations perform a single task
- The three basic sequential operations:
  - Computation: a single numeric calculation
  - Input: gets data values from outside the algorithm
  - Output: sends data values to the outside world
- A sequential algorithm is made up only of sequential operations
- A variable is a named storage location to hold a data value
- Example: computing average miles per gallon



# Representing Algorithms Sequential Algorithm

#### FIGURE 2.3

Step	Operation
1	Get values for <i>gallons used, starting mileage, ending mileage</i>
2	Set value of distance driven to (ending mileage - starting mileage)
3	Set value of average miles per gallon to (distance driven ÷ gallons used)
4	Print the value of average miles per gallon
5	Stop

Algorithm for computing average miles per gallon (version 1)

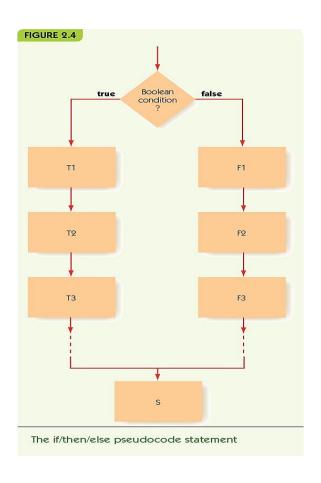


#### Representing Algorithms (3 of 5)

- Control operation: changes the normal flow of control
- Conditional statement: asks a question and selects among alternative options:
  - 1. Evaluate the true/false condition
  - 2. If the condition is true, then do the first set of operations and skip the second set
  - 3. If the condition is false, skip the first set of operations and do the second set
- Example: check for good or bad gas mileage



# Representing Algorithms Conditional Statement (1 of 2)



## Representing Algorithms Conditional Statement (2 of 2)

#### FIGURE 2.5

Step	Operation
1	Get values for gallons used, starting mileage, ending mileage
2	Set value of distance driven to (ending mileage – starting mileage)
3	Set value of average miles per gallon to (distance driven ÷ gallons used)
4	Print the value of average miles per gallon
5	If average miles per gallon is >25.0 then
6	Print the message 'You are getting good gas mileage'
	Else
7	Print the message 'You are NOT getting good gas mileage'
8	Stop

Second version of the average miles per gallon algorithm

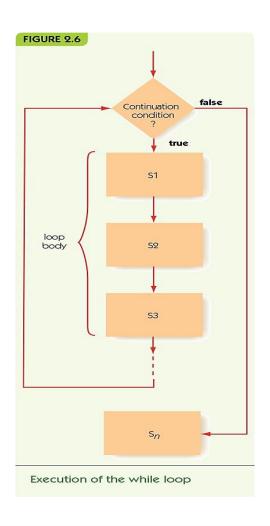


#### Representing Algorithms (4 of 5)

- Iteration: an operation that causes looping, repeating a block of instructions
- While statement repeats while a condition remains true
  - Continuation condition: a test to see if while loop should continue
  - Loop body: instructions to perform repeatedly
- Example: repeated mileage calculations



# Representing Algorithms Iteration and Loop Body (1 of 2)



## Representing Algorithms Iteration and Loop Body (2 of 2)

#### FIGURE 2.7

Step	Operation
1	response = Yes
2	While (response = Yes) do Steps 3 through 11
3	Get values for gallons used, starting mileage, ending mileage
4	Set value of distance driven to (ending mileage – starting mileage)
5	Set value of average miles per gallon to (distance driven ÷ gallons used)
6	Print the value of average miles per gallon
7	If average miles per gallon > 25.0 then
8	Print the message 'You are getting good gas mileage'
	Else
9	Print the message 'You are NOT getting good gas mileage'
10	Print the message 'Do you want to do this again? Enter Yes or No'
11	Get a new value for response from the user
12	Stop

Third version of the average miles per gallon algorithm

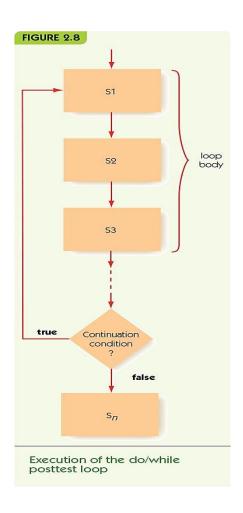


#### Representing Algorithms (5 of 5)

- Do/while, alternate iterative operation
  - Continuation condition appears at the end
  - Loop body always performed at least once
- Primitive operations: sequential, conditional, and iterative are all that is needed



## Representing Algorithms Do/While Posttest Loop (1 of 2)





```
Repre
```

```
Computation:
```

Set the value of "variable" to "arithmetic expression"

```
Input/Output:
```

```
Get a value for "variable", "variable"...
Print the value of "variable", "variable", ...
Print the message 'message'
```

#### Conditional:

```
If "a true/false condition" is true then
first set of algorithmic operations
Else
second set of algorithmic operations
```

#### Iterative:

```
While ("a true/false condition") do Step i through Step j
Step i: operation
Step j: operation
While ("a true/false condition") do
operation
```

```
operation
End of the loop
Do
operation
```

```
operation
.
.
operation
```

While ("a true/false condition")

## Examples of Algorithmic Problem Solving Example 1: Go Forth and Multiply (1 of 5)

Given two nonnegative integer values,  $a \ge 0$ ,  $b \ge 0$ , compute and output the product  $(a \times b)$  using the technique of repeated addition. That is, determine the value of the sum a + a + a + ... + a (b times).

# Examples of Algorithmic Problem Solving Example 1: Go Forth and Multiply (2 of 5)

- Get input values
  - Get values for a and b
- Compute the answer
  - Loop b times, adding each time\*
- Output the result
  - Print the final value\*
- \* steps need elaboration



## Examples of Algorithmic Problem Solving Example 1: Go Forth and Multiply (3 of 5)

- Loop b times, adding each time
  - Get values for a and b
  - Set the value of count to 0
  - While (count < b) do</li>
    - ... the rest of the loop\*
    - Set the value of count to (count + 1)
  - End of the loop
- \* steps need elaboration

# Examples of Algorithmic Problem Solving Example 1: Go Forth and Multiply (4 of 5)

- Loop b times, adding each time
  - Get values for a and b
  - Set the value of count to 0
  - Set the value of product to 0
  - While (count < b) do</li>
    - Set the value of product to (product + a)
    - Set the value of count to (count + 1)
  - End of the loop
- Output the result
  - Print the value of product



# Examples of Algorithmic Problem Solving Example 1: Go Forth and Multiply (5 of 5)

#### FIGURE 2.10

```
Get values for a and b

If (either a = 0 or b = 0) then

Set the value of product to 0

Else

Set the value of count to 0

Set the value of product to 0

While (count < b) do

Set the value of product to (product + a)

Set the value of count to (count + 1)

End of loop

Print the value of product

Stop
```

Algorithm for multiplication of nonnegative values via repeated addition



### Examples of Algorithmic Problem Solving Example 2: Looking, Looking, Looking (1 of 5)

Assume that we have a list of 10,000 names that we define as  $N_1$ ,  $N_2$ ,  $N_3$ , ...,  $N_{10,000}$ , along with the 10,000 telephone numbers of those individuals, denoted as  $T_1$ ,  $T_2$ ,  $T_3$ , ...,  $T_{10,000}$ . To simplify the problem, we initially assume that all names in the book are unique and that the names need not be in alphabetical order.

### Examples of Algorithmic Problem Solving Example 2: Looking, Looking, Looking (2 of 5)

- Three versions here illustrate algorithm discovery, working toward a correct, efficient solution:
  - A sequential algorithm (no loops or conditionals)
  - An incomplete iterative algorithm
  - A correct algorithm



### Examples of Algorithmic Problem Solving Example 2: Looking, Looking, Looking (3 of 5)

#### FIGURE 2.11

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Get values for NUMBER, $T_1, \ldots, T_{10,000}$ , and $N_1, \ldots, N_{10,000}$
If $NUMBER = T_1$ then print the value of $N_1$
If $NUMBER = T_o$ then print the value of $N_o$
If $NUMBER = T_3$ then print the value of $N_3$
•
•
If $NUMBER = T_{9,999}$ then print the value of $N_{9,999}$
If $NUMBER = T_{10,000}$ then print the value of $N_{10,000}$
Stop

First attempt at designing a sequential search algorithm



### Examples of Algorithmic Problem Solving Example 2: Looking, Looking, Looking (4 of 5)

#### FIGURE 2.12

Step	Operation
1	Get values for NUMBER, $T_1, \ldots, T_{10,000}$ , and $N_1, \ldots, N_{10,000}$
2	Set the value of i to 1 and set the value of Found to NO
3	While (Found = NO) do Steps 4 through 7
4	If NUMBER is equal to the $i$ th number on the list, $T_i$ , then
5	Print the name of the corresponding person, N,
6	Set the value of Found to YES
	Else ( $NUMBER$ is not equal to $T_i$ )
7	Add 1 to the value of i
8	Stop

Second attempt at designing a sequential search algorithm



### Examples of Algorithmic Problem Solving Example 2: Looking, Looking, Looking (5 of 5)

#### FIGURE 2.13

Step	Operation
1	Get values for NUMBER, $T_1, \ldots, T_{10,000}$ , and $N_1, \ldots, N_{10,000}$
2	Set the value of i to 1 and set the value of Found to NO
3	While both (Found = NO) and ( $i \le 10,000$ ) do Steps 4 through 7
4	If NUMBER is equal to the ith number on the list $T_i$ then
5	Print the name of the corresponding person, N,
6	Set the value of Found to YES
	Else (NUMBER is not equal to $T_i$ )
7	Add 1 to the value of i
8	If $(Found = NO)$ then
9	Print the message 'Sorry, this number is not in the directory'
10	Stop

The sequential search algorithm



# Examples of Algorithmic Problem Solving Example 3: Big, Bigger, Biggest (1 of 2)

- Library: A collection of prewritten, useful algorithms
- A "building-block" algorithm used in many libraries: Given a value  $n \ge 1$  and a list containing exactly n unique numbers called  $A_1, A_2, \ldots, A_n$ , find and print out both the largest value in the list and the position in the list where that largest value occurred.

# Examples of Algorithmic Problem Solving Example 3: Big, Bigger, Biggest (2 of 2)

#### FIGURE 2.14

```
Get a value for n, the size of the list

Get values for A_1, A_2, \ldots, A_n, the list to be searched

Set the value of largest so far to A_1

Set the value of location to 1

Set the value of i to 2

While (i \le n) do

If A_i > largest so far then

Set largest so far to A_i

Set location to i

Add 1 to the value of i

End of the loop

Print out the values of largest so far and location

Stop
```

Algorithm to find the largest value in a list



# Examples of Algorithmic Problem Solving Example 4: Meeting Your Match (1 of 4)

- Pattern matching: common across many applications, such as:
  - Word processor search, web search, image analysis, and human genome project

Let's formally define the pattern-matching problem as follows:

You will be given some text composed of n characters that will be referred to as  $T_1 T_2 ... T_n$ . You will also be given a pattern of m characters,  $m \le n$ , that will be represented as  $P_1 P_2 ... P_m$ . The algorithm must locate every occurrence of the given pattern within the text. The output of the algorithm is the location in the text where each match occurred.



# Examples of Algorithmic Problem Solving Example 4: Meeting Your Match (2 of 4)

- Algorithm has two parts:
  - 1. Sliding the pattern along the text, aligning it with each position in turn
  - 2. Given a particular alignment, determine if there is a match at that location
- Solve parts separately and use
  - Abstraction: focus on high level, not details
  - Top-down design: start with big picture, gradually elaborate parts

# Examples of Algorithmic Problem Solving Example 4: Meeting Your Match (3 of 4)

#### FIGURE 2.15

```
Get values for n and m, the size of the text and the pattern, respectively Get values for both the text T_1 T_2 ... T_n and the pattern P_1 P_2 ... P_m Set k, the starting location for the attempted match, to 1 Keep going until we have fallen off the end of the text Attempt to match every character in the pattern beginning at position k of the text (this is Step 1 from the previous page) If there was a match then Print the value of k, the starting location of the match Add 1 to k, which slides the pattern forward one position (this is Step 2) End of the loop Stop
```

First draft of the pattern-matching algorithm



## Examples of Algorithmic Problem Solving Example 4: Meeting Your Match (4 of 4)

#### FIGURE 2.16

```
Get values for n and m, the size of the text and the pattern, respectively
Get values for both the text T_1, T_2, \dots, T_n and the pattern P_1, P_2, \dots, P_m
Set k, the starting location for the attempted match, to 1
While (k \le (n - m + 1)) do
     Set the value of i to 1
     Set the value of Mismatch to NO
     While both (i \le m) and (Mismatch = NO) do
          If P_i \neq T_{k+(i-1)} then
             Set Mismatch to YES
           Else
             Increment i by 1 (to move to the next character)
     End of the loop
     If Mismatch = NO then
          Print the message 'There is a match at position'
          Print the value of k
     Increment k by 1
End of the loop
Stop
```

Final draft of the pattern-matching algorithm



#### Summary

- Pseudocode is used for algorithm design: structured like code but allows English and mathematical phrasing and notation
- Pseudocode is made up of sequential, conditional, and iterative operations
- Algorithmic problem solving involves:
  - Step-by-step development of algorithm pieces
  - Use of abstraction and top-down design