# **CSCI 2110 Data Structures and Algorithms**

# **Module 7: Binary Search Trees**



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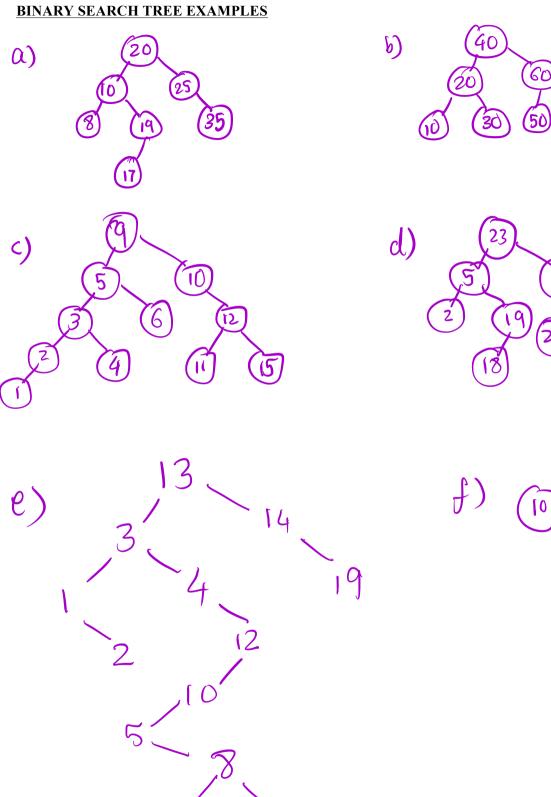
# **Binary Search Tree**

- A binary search tree (BST) is a binary tree that is **sorted or ordered** according to a rule.
- ■In general, the information contained in each node is a record one part of the record is called the **key**.
- ■BST Rule: A BST is a binary tree in which, for every node x
  - the keys in all nodes in the left subtree of x are smaller than the key in x.
  - the keys in all nodes in the right subtree of x are larger than the key in x.
- Duplicate keys are generally not allowed in a BST.



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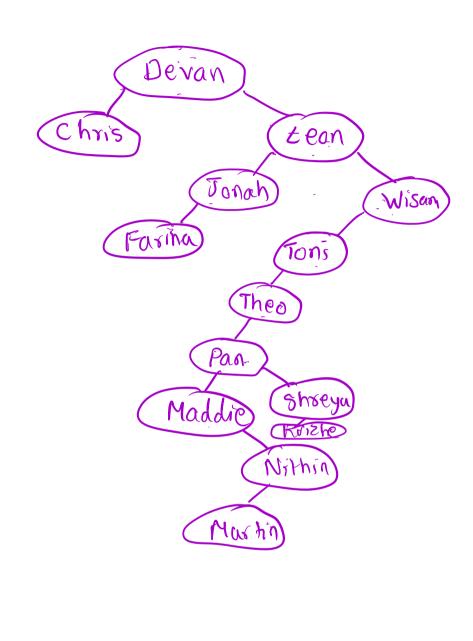
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## Example: Building a Binary Search Tree with names of students as keys

Devan Chris de m Wisam Toni Theo Pan Tonah Maddie Nithin Shreya MACHIA Rinzhe Fasiha



Inorder Tramersali Z - Root - R

Chris - Devan - Fariha - Jonah - LeonInorder traversal sorts the Keys in

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#### BINARY SEARCH TREE OPERATIONS

#### **SEARCH FOR A GIVEN KEY**

Compare target key with the value in the root.

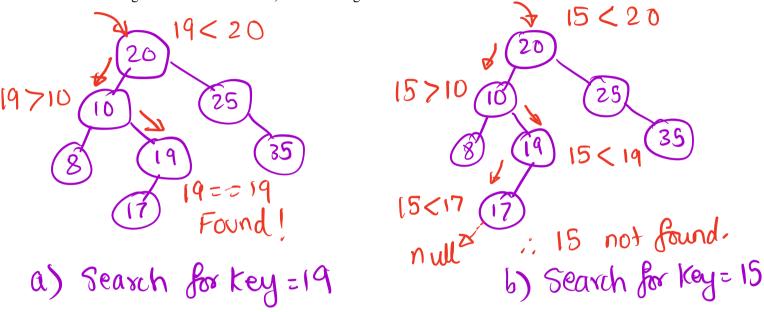
If it is equal, target found. Exit.

If an empty subtree is reached, target not found. Exit.

Otherwise.

if target is < value in the root, search the left subtree

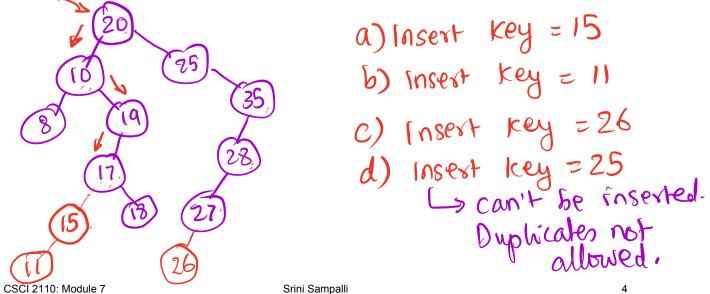
if target is > value in the root, search the right subtree



#### INSERT A VALUE INTO A BST

In order to insert a value, the search process is employed to force a failure, and the new value is inserted at the place where the search failed.

Note that the new node always becomes the leaf node in the BST.



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#### DELETE A NODE WITH A GIVEN VALUE FROM A BST

First locate the value in the BST. Let it be found in node X.

(x has no children) Case 1: X is a leaf node

Simply delete X, that is, detach X from its parent.

E.g. Delete 8.

Easy

#### Case 2: X has one child

Make the child of X the child of the parent of X.

Then delete X by delinking it from its parent.

E-g. Delete 19.

"Hand over the custody to the grandparent" Medium

#### Case 3: X has two children

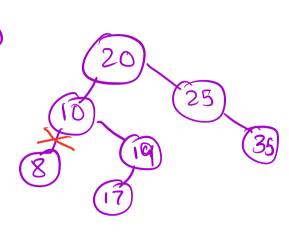
Replace the value in X by the largest value in the left subtree of X.

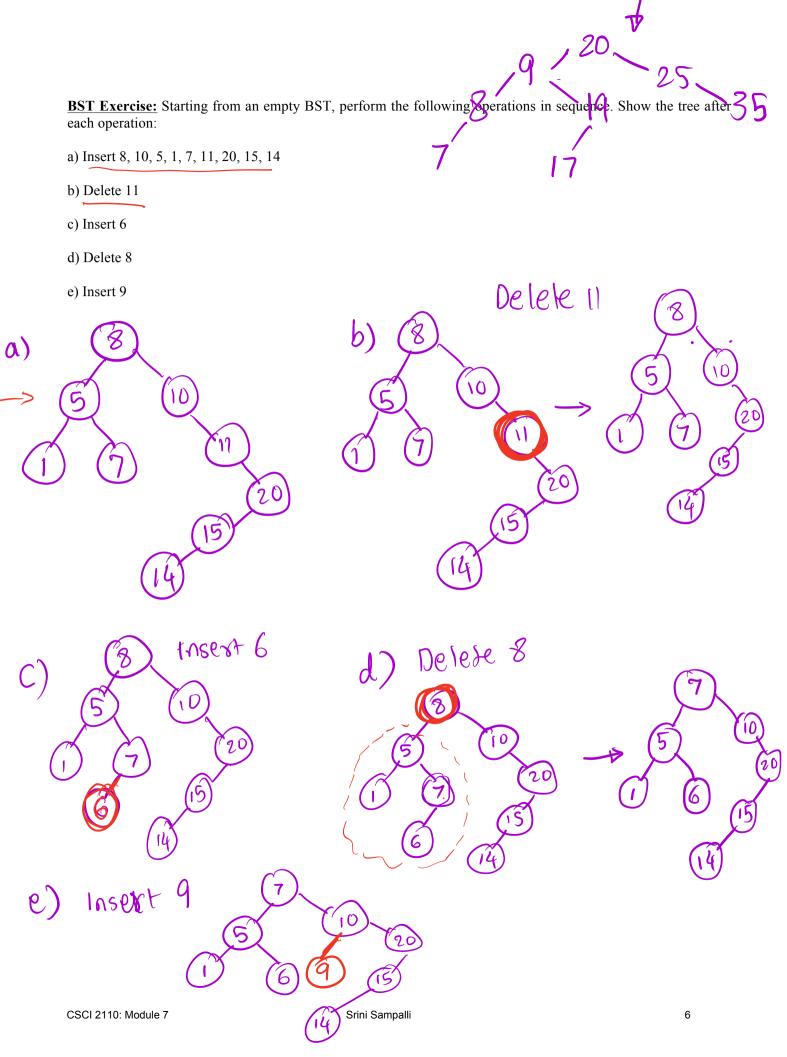
Let that value be found in node Y.

Delete Y. This step will be either Case 1 or Case 2.

Replace node 10 with node 9-Then go & delete node 9. This will be case 1 or Case 2
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because 9 cannot have a Might child





### **BINARY SEARCH TREE CLASS**

#### **Attributes**

int size;

BinaryTree<T> tree; int size:

#### Constructors

BinarySearchTree()	Creates an empty binary search tree

#### Methods

Name	What it does	Header	Price tag (complexity)	
getTree	Returns the BinaryTree	Binary Tree (T> get Tree ()	0(1)	
isEmpty	Checks if the tree is empty	boolean is Emply ()	0(1)	
size	Returns the size of the binary tree	int size ()	0(1)	
search	Searches for a given key and returns the node with the key	BinaryTree CT> Search (T Key)	) O(109.7) O(n)	)) (1 BF
insert	Inserts a given item into the binary search tree	void insert (T Key)	O(logen)	) (v Bt
delete	Delete the node with the given key	void delete (T key)	0 (h)	) bd BA

We will also add two more methods findPredecessor and deleteHere. These are helper methods for the delete

method.

# searches = 3

n=7 # searcher=7

```
IMPLEMENTATION
public class BinarySearchTree<T extends Comparable<T>>
      //attributes
      private BinaryTree<T> tree;
      private int size;
      //constructor
      public BinarySearchTree()
            tree = new BinaryTree<T>();
            size = 0:
      //other methods
      public BinaryTree<T> getTree()
            return tree;
      public boolean isEmpty()
            return tree.isEmpty();
      public int size()
            return size;
      //Search for a given key and return the reference to that node; return null if key not found
                                                                         Search (16)
      public BinaryTree<T> search(T key)
        Binary Tree < T> t= tree;
        boolean found = false;
       conile (t'| = null & l' | found)
             int c= key.compareTo(t.getDahl))
             if (c<o) t=t.getZeft();
             if (c>0) t=t.getRight();
         3 if (cz=o) found z true;
         if (found) return t;
ebe return null;
```

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```
//insert an item into a binary search tree
                                                                                    25
       public void insert(T item)
           //first create a new single node Binary Tree with the item
           BinaryTree<T> newNode = new BinaryTree<T>();
           newNode.setData(item);
           //if this is the first node in the binary search tree
                                                               newNod
           if(size===0)
                  tree = newNode;
                  size++;
                  return;
           }
           //Otherwise, start at the root of the binary search tree and find the place to insert
           BinaryTree<T> t = tree;
           boolean done = false;
                int C = item. compare To (t-get Dala());
                   System. out. println("Duplicale key. Can't issest")
                Else if (C < 0) // need to go left

if (t.get/eft() = = null) // found the place to place to insert

t. Set/eft (newNode);
newNode. SetParent (t);
done = true;
7 8ize + t.
                  2 return;
                           7 8ize++;
                          ëne // keep going
                              t=t-get(eft();
                                       replace left with right
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                      z
```

```
node
                     //findPredecessor – helper method for the delete method
                     //returns the largest node in the left subtree of the given node
                     public BinaryTree<T> findPredecessor(BinaryTree<T> node)
                                                                                           Pred
                          if (node == null)
                                 return null;
                          BinaryTree<T> pred = node.getLeft();
                          if (pred < = null) rehun null;
                          while (pred.getRight()!=null)
                                 pred = pred.getRight();
                          return pred;
                     //deleteHere – helper method for the delete method
                     //deletes a given node and attaches its subtree(s) to its parent node
Case 1
                     public void deleteHere(BinaryTree<T> deleteNode, BinaryTree<T> attach)
                          if (deleteNode == null)
                                 return:
                          BinaryTree<T> parent = deleteNode.getParent();
                                                                                                             deleteNode
                                                                                     parent
                          if (parent == null)
                                 return;
                          if (attach == null)
                                 if (parent.getLeft()== deleteNode)
                                         parent.setLeft(null);
                                                                                                              - aHach
                                 else
                                        parent.setRight(null);
                                 return;
                          if (deleteNode==parent.getRight()){
                                 parent.detachRight();
                                 deleteNode.setParent(null);
     Case 2
                                 parent.attachRight(attach);
                                 attach.setParent(parent);
                          else
                                 parent.detachLeft();
                                 deleteNode.setParent(null);
                                 parent.attachLeft(attach);
                                 attach.setParent(parent);
                          deleteNode.clear();
```

```
//delete method: deletes a node with a given key
 public void delete (T key)
        if (size == 0) {
               System.out.println("Can't delete. Empty tree");
               return;
        }
                                                       -> Get to the mode to be
        BinaryTree<T> deleteNode = search(key);
        if (deleteNode == null) {
               System.out.println("Can't delete. Key not found");
               return;
        }
        BinaryTree < T > hold = null;
if (delete Node get Left() = = nell & delete Node get Right() = = nell)
                      deletettere (deletenode, nul).
        //Case 2: deleteNode has one child (left child)
ehe if (deleteNode get Right () = = null)

hold = deleteNode get Zeft();

delete Here (deleteNode, hold);
        //Case 2: deleteNode has one child (right child)

(de lete Node-get Left () = = null)

hold = deleteNode-get Right();
                  deletetere (deletenode, hold);
        //Case 3: deleteNode has two children
         ebe
                hold = find Predecessor (dele le Node);
dele le Node - set Daha (hold - get Daha ());
          deletetere (hold, hold-get/eft!)
```