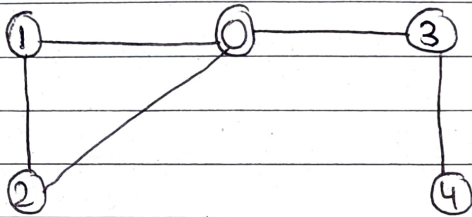


Day - 213Graph - 17* Euler Path:

⇒ It is a path in a graph that visits every edge exactly once.



⇒ So, for example, we use above example then — best path or euler path is

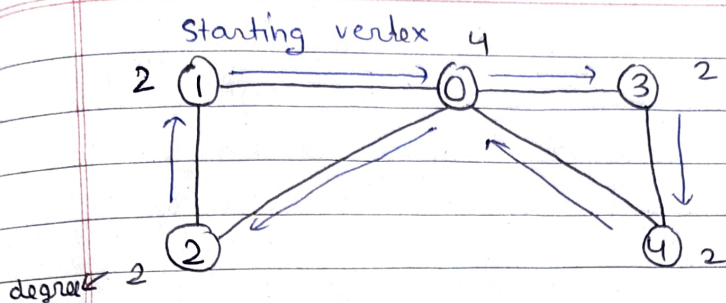
$0 \rightarrow 2 \rightarrow 1 \rightarrow 3 \rightarrow 4$

or $0 \rightarrow 1 \rightarrow 2 \rightarrow 0 \rightarrow 3 \rightarrow 4$

* Euler Circuit:

⇒ Euler circuit is like euler cycle.

⇒ In the euler circuit, we have find out the path that contain euler path and starting vertex is same as ending vertex.



⇒ There is a property of euler circuit that if we change the source vertex then also euler circuit will present.

⇒ But this is not valid for euler path.

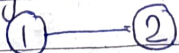
⇒ Now, how to know or find euler circuit by code.

⇒ For that, we have find a pattern that if a graph ~~has~~ is euler circuit then its degree will be even.

Degree: No. of incoming edges.

⇒ why?

⇒ Suppose if we have two nodes like

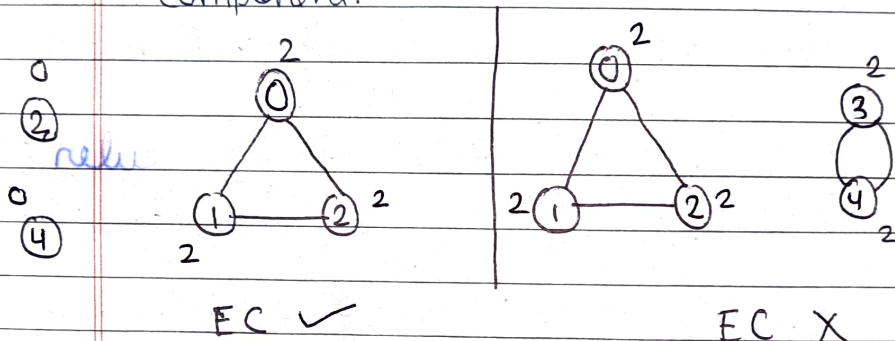


⇒ But we want to get back to the 1 then there should be a path —



⇒ So, if one edge is coming then there should be one edge ~~coming~~ going out from the vertex.

⇒ 2nd condition is that all the edges ~~are~~ should be part of single component.



⇒ In Euler path, there can be two nodes that have odd degree.

Steps:

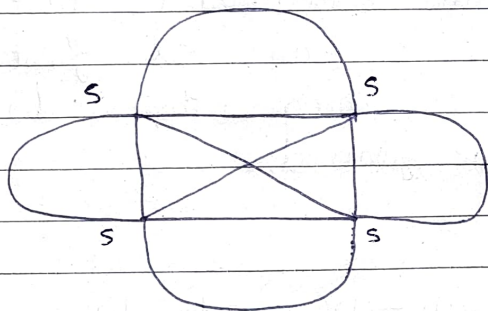
- ⇒ Find degree of each node.
- ⇒ If degree of any node is odd, not a EC.
- ⇒ If all even then —
- Apply DFS, from any non-zero degree node.
- Then make a visited array.
- After that if any degree of node have visited value 0 that means the graph is not euler circuit.

⇒ If the node have degree 0 then we don't have to check.

⇒ So, we can say, euler ~~is~~ circuit can have euler path but vice versa is not true.

EC \rightarrow EP ✓
but EP \rightarrow EC ✗

⇒



⇒ So, we have make this figure without taking off the pen from the copy.

⇒ But this is not possible because this is not a eulerian path or circuit.