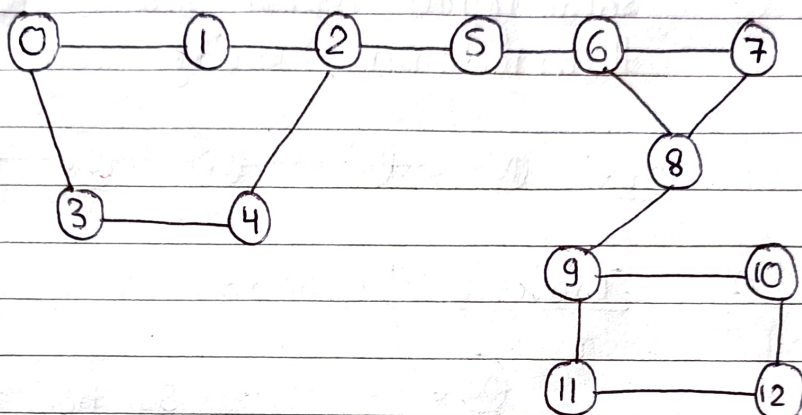


Day-218

Graph - 22

* Bridge in a graph:

=>



=> Bridge is that edge if we remove that edge then our graph divides into two component.

=> So, here edge b/w →

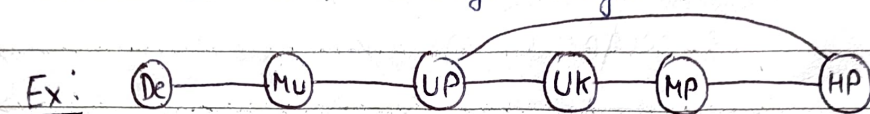
(2)-(5), (5)-(6), (8)-(9)

=> Brute force approach will be like we apply BFS & DFS and check we can reach that node or not after removing that edge.

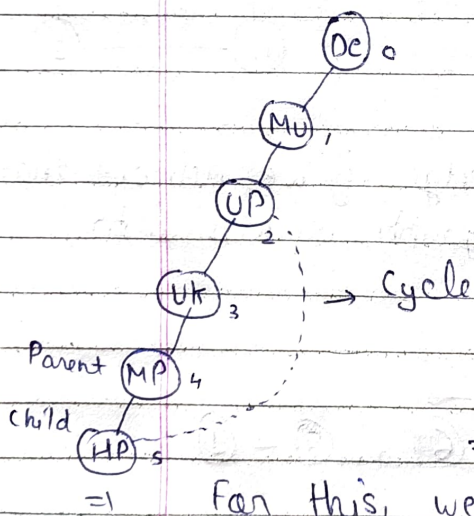
⇒ But this will increase our T.C.

=> So, if we observe that edges other than bridges edges all are the part of cycle.

=> If the node is not the part of same cycle then also edge b/w them is a bridge edge.



=> Traverse the Graph



=> So, how to identify bridge edges now.

=> Edge b/w UP - HP is not bridge is confirmed.

=> So, how about MP - HP.

For this, we will ask HP that it can visit any node that come before me (MP).

=> So, it will say yes because it can visit UP.

=> So, MP - HP also the part of cycle.

⇒ Data will be stored like this —

HP: HP, UP

MP: MP, HP, UP

4 5 2

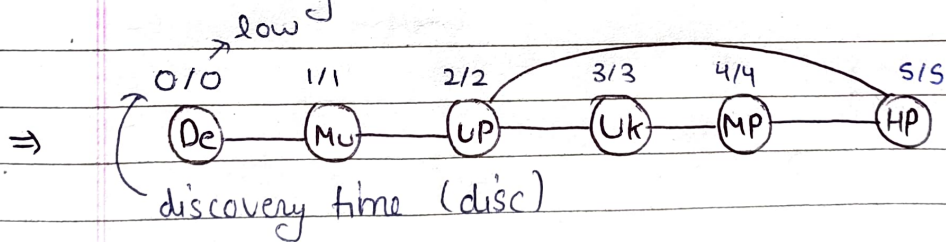
↑

⇒ If any value here, is less than or equal to parent value, then the edge is not a bridge.

⇒ ~~So~~ But, we have to traverse all the values of array for checking.

⇒ For that, we can just store the min. value.

⇒ This time or value, we called it as discovery time.



⇒ We will update the value of low with min of parent-child low value.

For bridge

$disc[\text{parent}] < low[\text{child}]$

=> Three conditions:

① $\text{if}(\text{neighbour} == \text{parent})$
 ignore

② $\text{else if}(\text{visited}[\text{neighbour}])$
 $\text{low}[\text{node}] = \min(\text{low}[\text{node}], \text{low}[\text{neighbour}])$

③ else {
 DFS ()
 $\text{if}(\text{dis}[\text{node}] < \text{low}[\text{neigh}])$
 bridge ++ ;