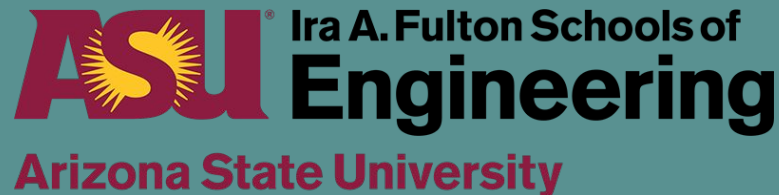


Topological Data Analysis for Parkinson's Disease Classification and Severity Assessment

Afra Nawar, Farhan Rahman, Narayanan Krishnamurthi, Anirudh Som, Pavan Turaga





Parkinson's Disease

Statistics

- 2nd most common neurodegenerative disease
- Incidence increasing
- 1 mil. affected in U.S., 10 mil. worldwide
- Elderly most commonly affected

Symptoms

- Muscle rigidity
- Lack of balance and postural control
- Tremors
- Lack of fine motor skills



Parkinson's Disease

UPDRS

- Unified Parkinson's Disease Rating Scale
- Includes sections based on clinical motor evaluation, self evaluation, and Mentation/Behavior/Mood

Proposed Method

- Signal Processing paired with Machine Learning (Automated Assessment Tool)

**Increased Accuracy
& Early Detection**

**Increased
Objectivity**

Dataset



Data Collection

Pressure
Plate
Platform



Figure 1: Patient Standing on Pressure Plate Platform

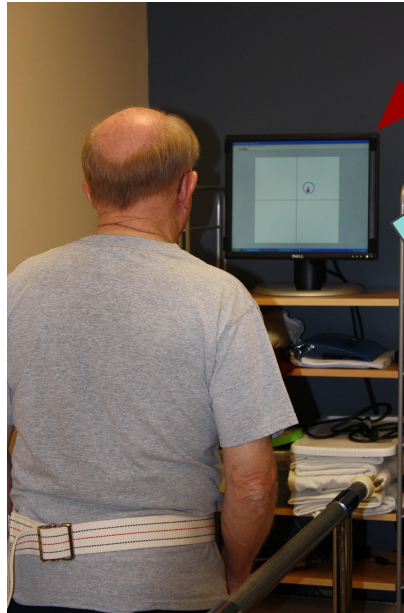


Figure 2: Patient View of screen marking targets and COP

Screen

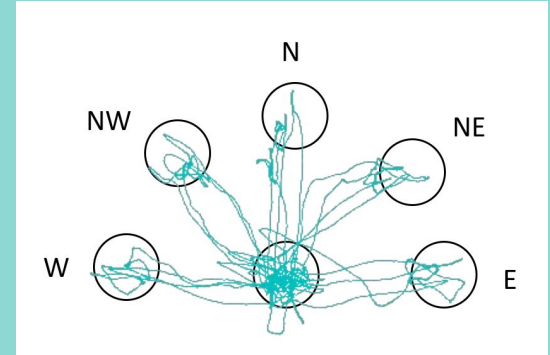


Figure 3: Visualization of COP movement during target reaches

[1] A. Som, N. Krishnamurthi, V. Venkataraman, and P. Turaga. Attractor-shape descriptors for balance impairment assessment in parkinson's disease. In 2016 38th Annual International Conference of the IEEE Engineering in Medicine and Biology Society (EMBC), pages 3096–3100. IEEE, 2016.

[2] N. Krishnamurthi, S. Mulligan, P. Mahant, J. Samanta, and J. J. Abbas. Deep brain stimulation amplitude alters posture shift velocity in parkinson's disease. Cognitive neurodynamics, 6(4):325–332, 2012.

Dataset Composition

Healthy Subjects

Elderly Subjects

- 22 Subjects
- 5 Trials Each

Young Subjects

- 21 subjects
- 5 Trials Each

Parkinson's Subjects

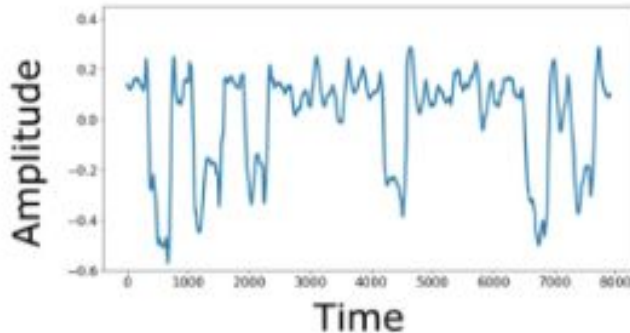
Parkinson's Disease Subjects

- 17 subjects
- 3 Trials Each

60 Subjects 266 Trials

Data Representation

- X : measurement in the medio-lateral direction
- Y: measurement in the antero-posterior direction
- F_x, F_y, F_z : Forces and in the X, Y, Z direction
- M_x, M_y, M_z : Moments in the X, Y, Z direction



Each signal consists of the value in the chosen direction with respect to time.

Methods



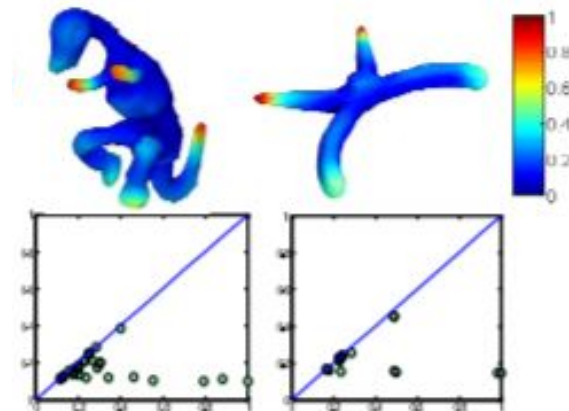


Topological Data Analysis

- Analyze Structure and Shape of Data
- Time Series, Point Clouds, Images

Why Topological Data Analysis?

- Invariant to order of target reaches
- Invariant to smooth deformations (stretching, bending, scaling, etc)



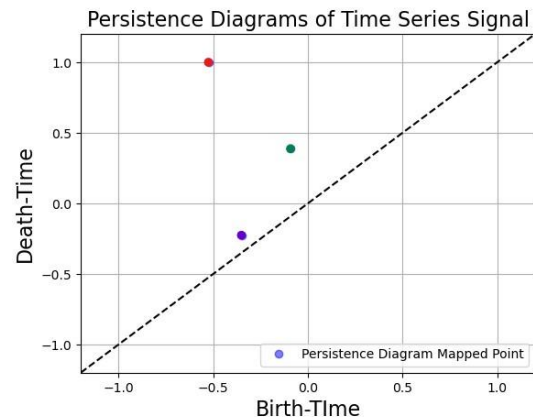
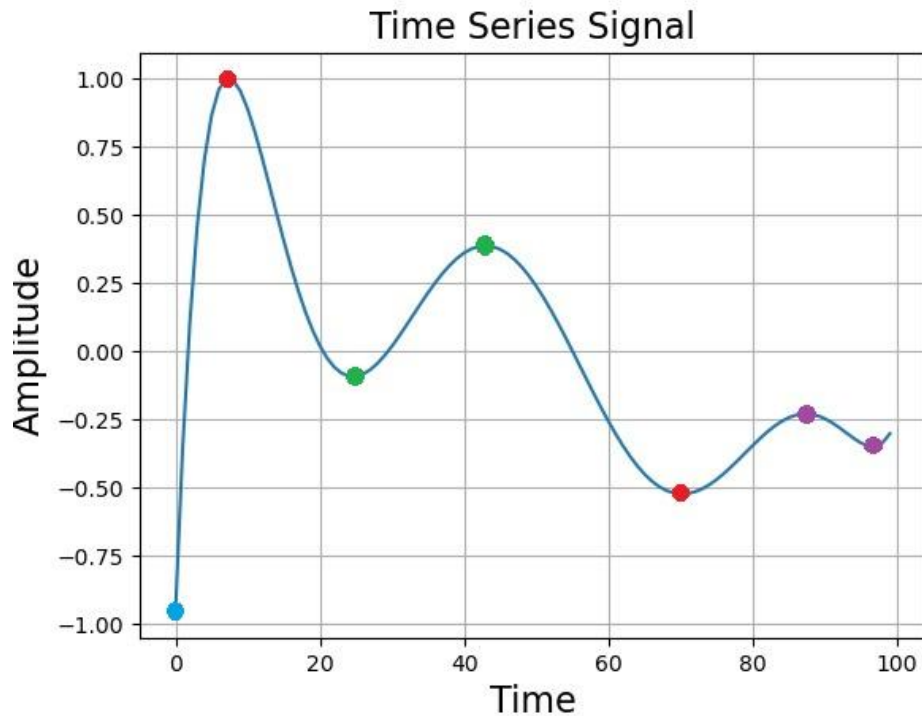
[3] C. Epstein, G. Carlsson, and H. Edelsbrunner. Topological data analysis. *Inverse Problems*, 27(12):120201, 2011

[4] G. Carlsson. Topology and data. *Bulletin of the American Mathematical Society*, 46(2):255–308, 2009.

[5] C. Li, M. Ovsjanikov, and F. Chazal. Persistence-based structural recognition. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pages 1995–2002, 2014



Topological Data Analysis

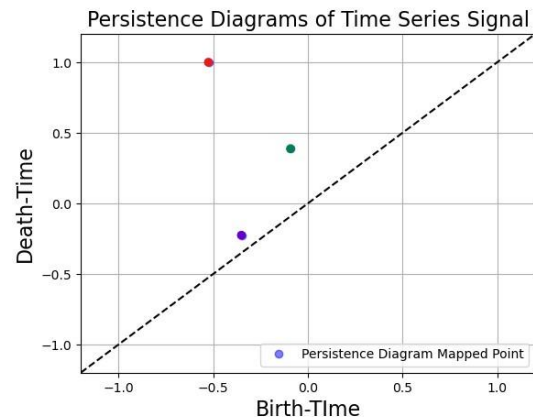
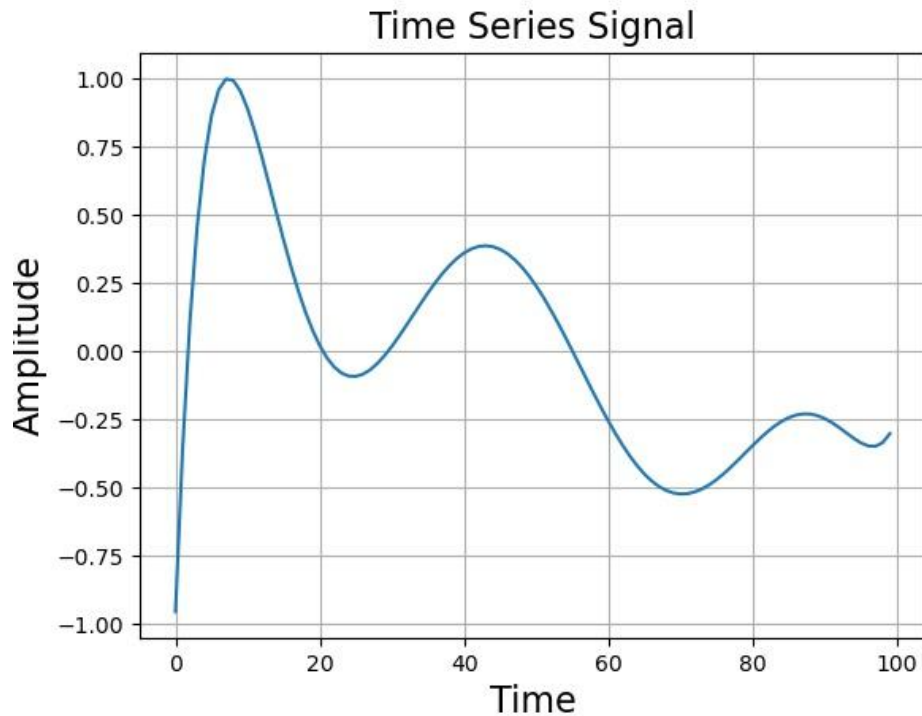


Mapping of time-series data as a pairing of its peaks with its troughs.

Represents information about the smoothness of the data, as well as its rises and falls



Topological Data Analysis

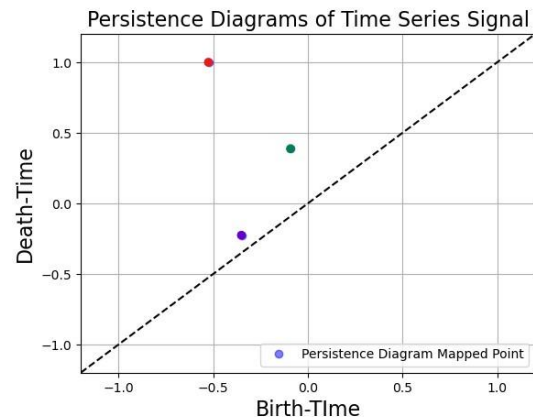
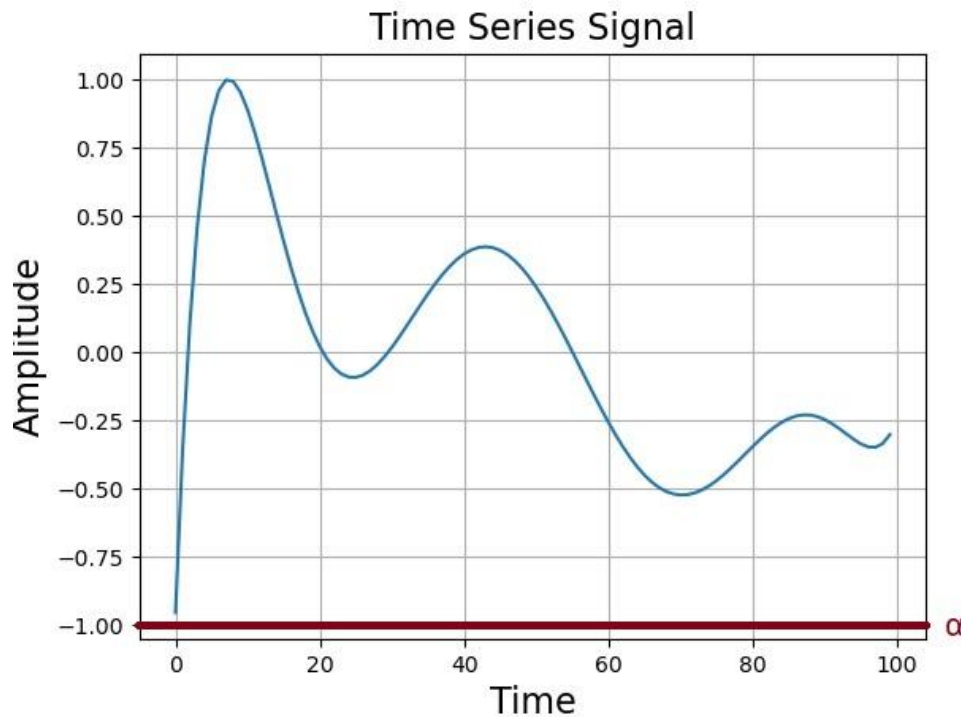


Time-series signal can be modeled as a graph with multiple nodes, each connected to two neighbors (except the ends)

Each node's value is its y-value on the plot



Topological Data Analysis

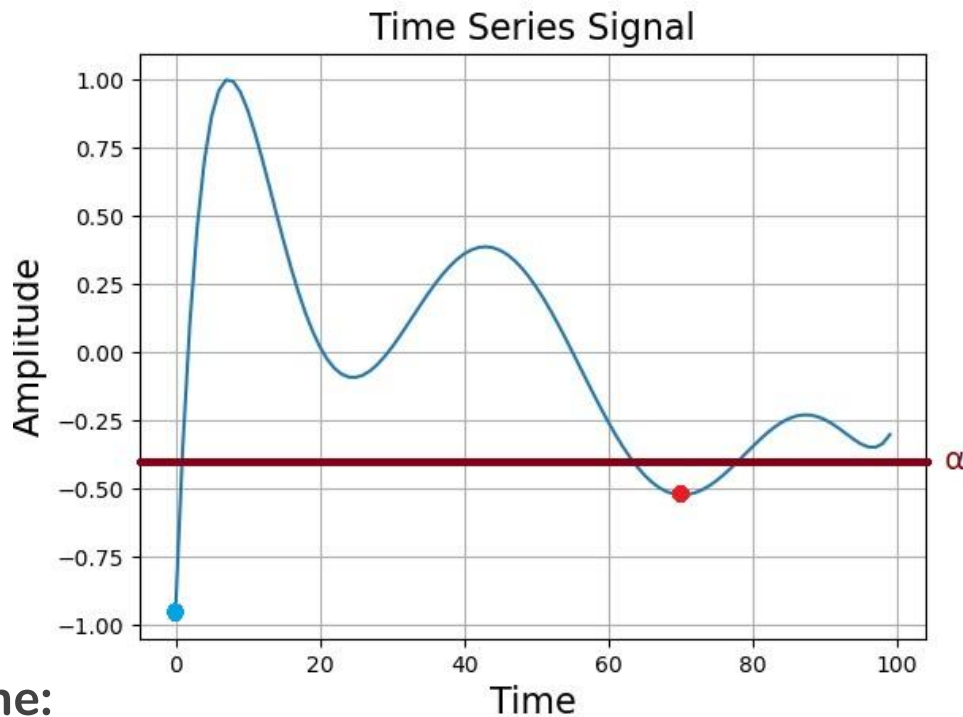


Alpha value is swept from $-\infty$ to ∞ , identifying troughs and matching them to peaks as it increases.

Local minimum (trough) is any node whose value is less than those of all of its neighbors.

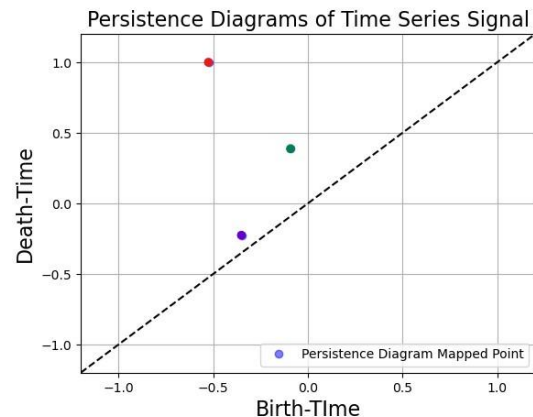


Topological Data Analysis



Birth-time:

Value (Y-axis) of local minimum.



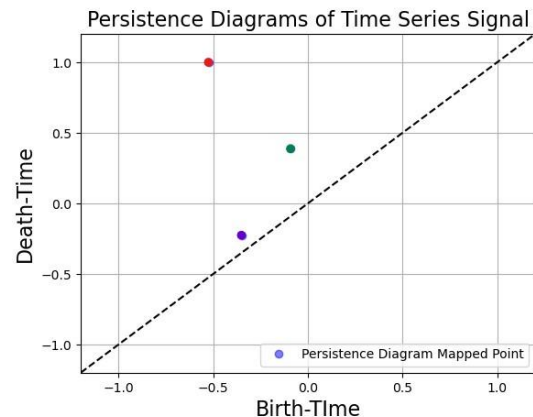
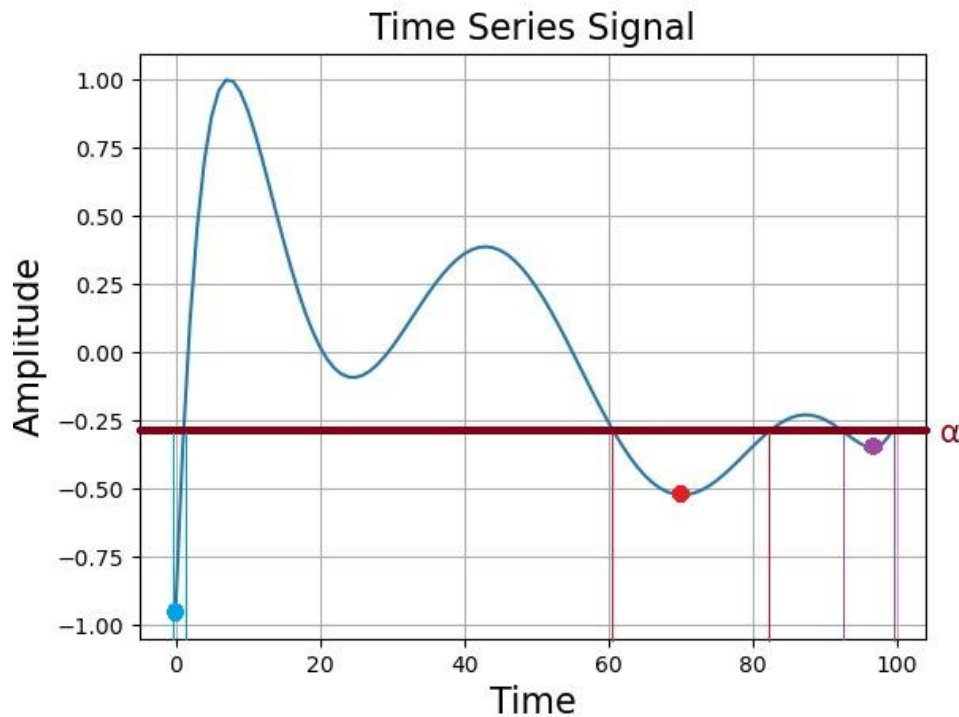
When alpha is swept passed a node that it identifies as a local minimum, it saves the value of that node as the birth of that trough

Blue trough is born at about -0.95

Red trough is born at about -0.5



Topological Data Analysis



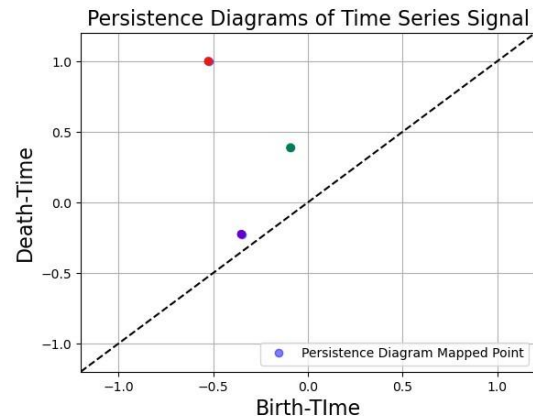
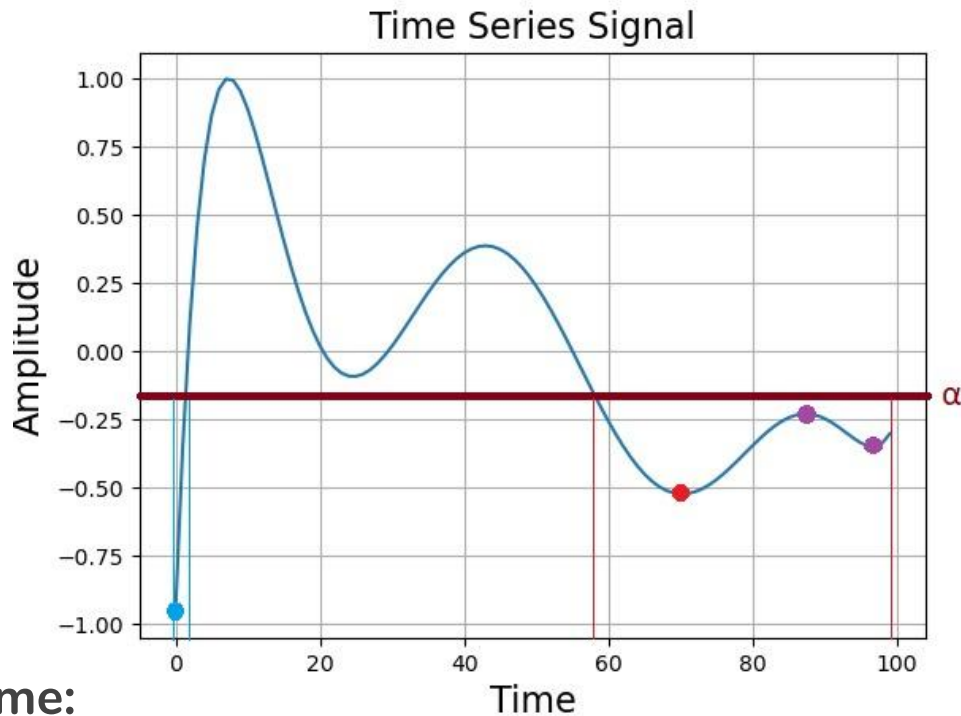
Purple trough born at about -0.3

Algorithm keeps track of the subgraphs of the overall graph for values below alpha

Alpha value splits graph into several explored subgraphs, boundaries show the minimum for each subgraph



Topological Data Analysis



The death of a trough is given by the lowest alpha value such that the trough is no longer the minimum of its subgraph.

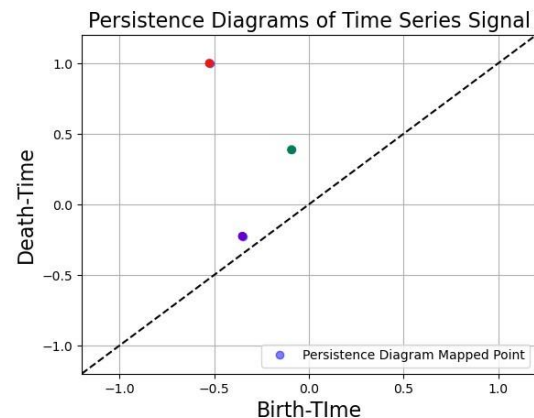
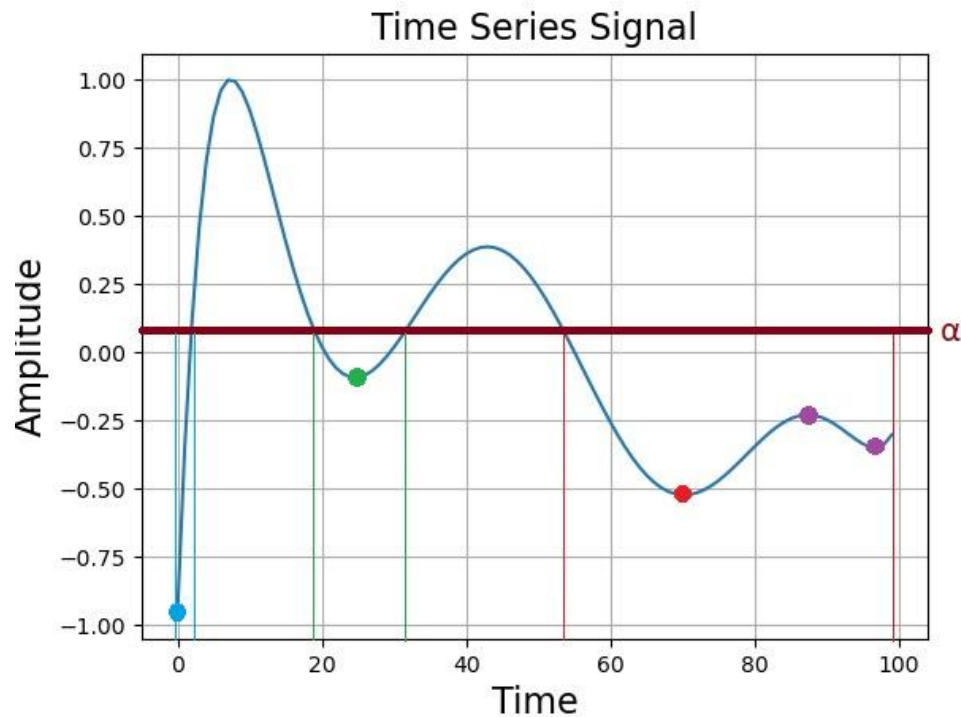
Red trough is now the minimum of the right subgraph.

Purple trough dies at about -0.25

Death-time:
Value (Y-axis) of matched peak.



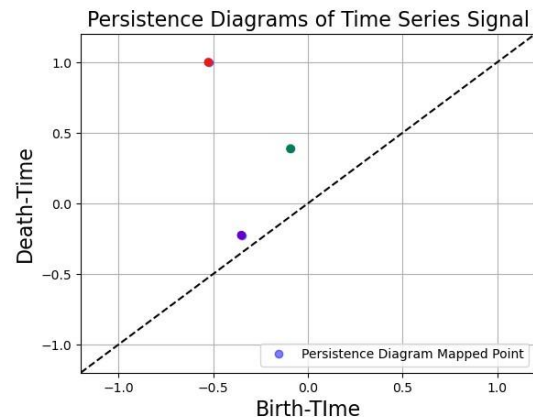
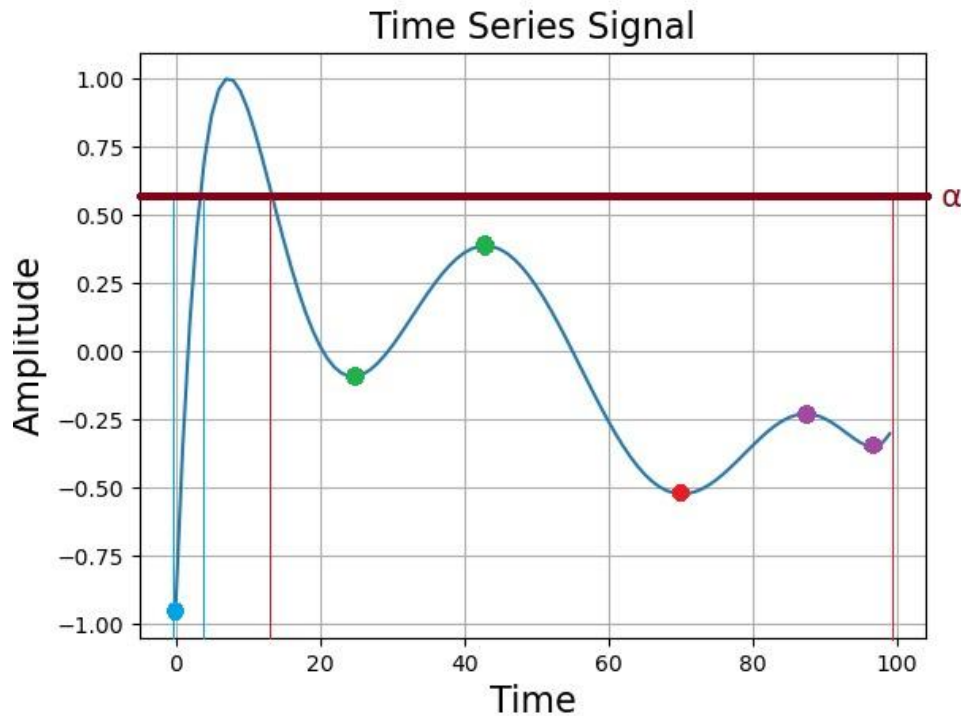
Topological Data Analysis



Green trough is born at about -0.1



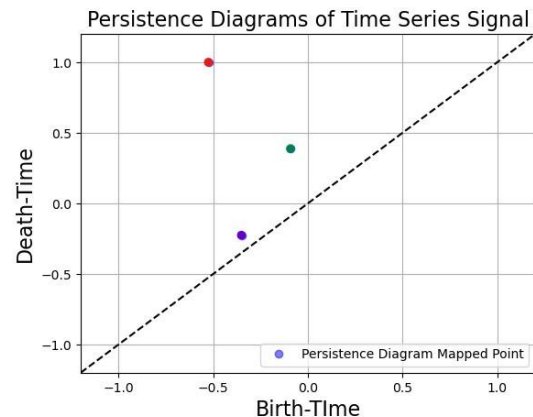
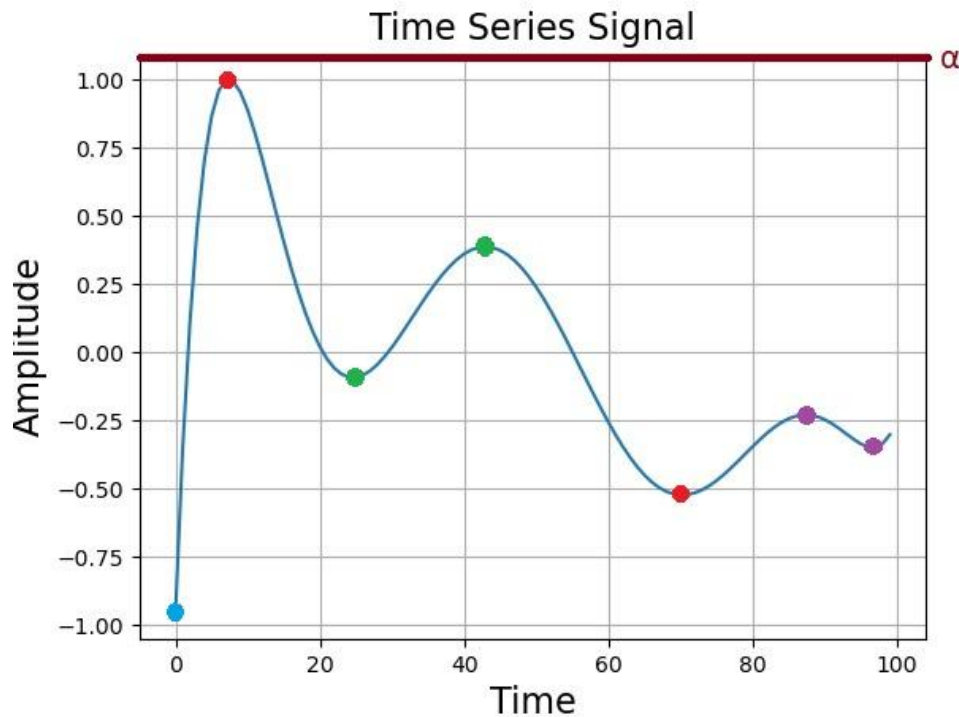
Topological Data Analysis



Green trough dies at about 0.35

Red trough is now the minimum of right-most subgraph.

Topological Data Analysis

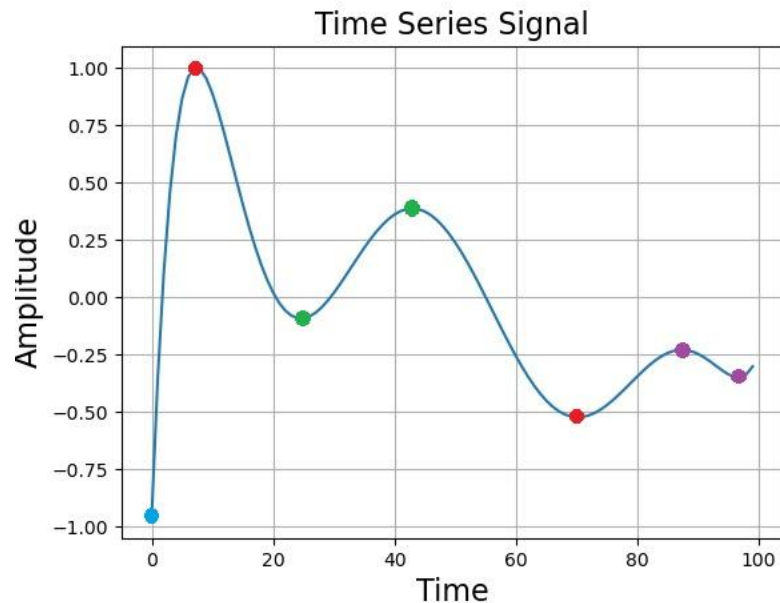
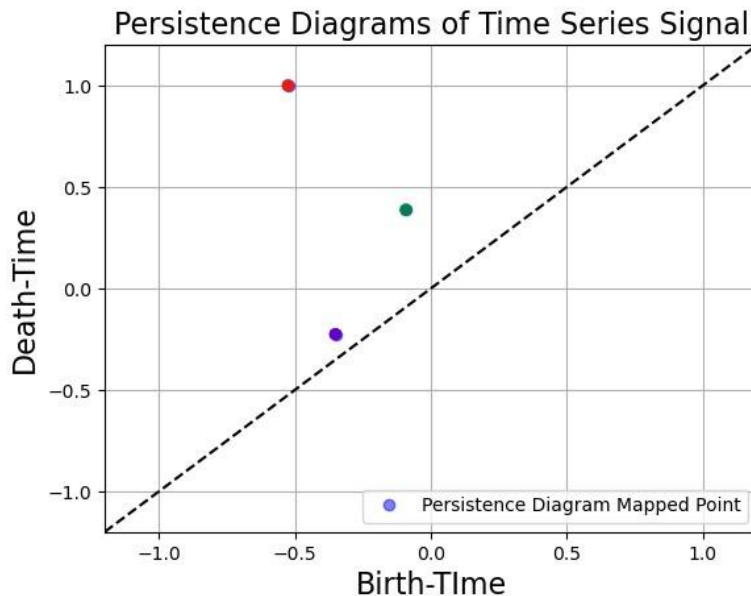


Red trough dies at about 1.

The algorithm terminates when all node values are smaller than alpha.

As the global minimum (blue trough) does not die, it is given a death time of infinity.

Persistence Diagrams



$$\text{Lifetime} = \text{Death-time} - \text{Birth-time}$$



Persistence Diagrams

Pros:

Good way to uniformly represent variable length time-series data.

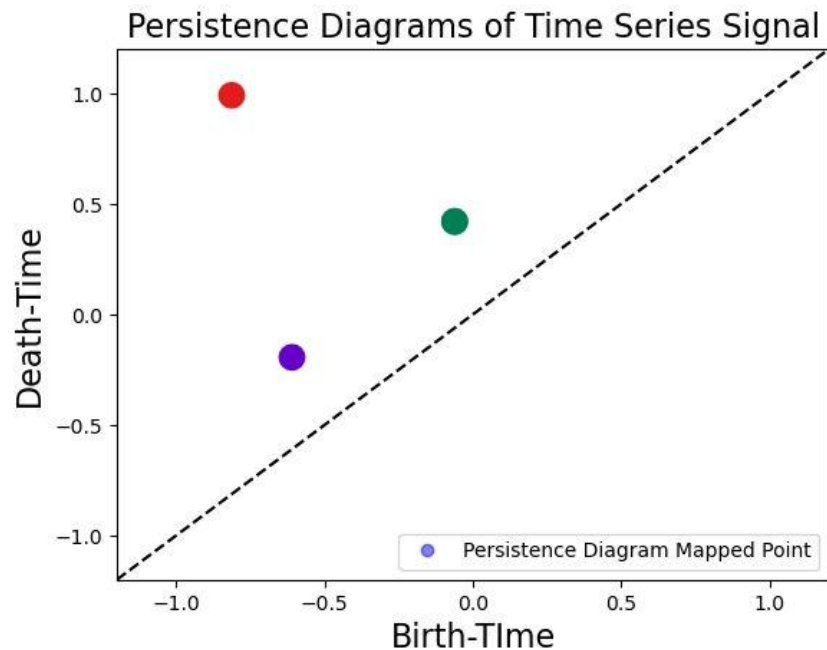
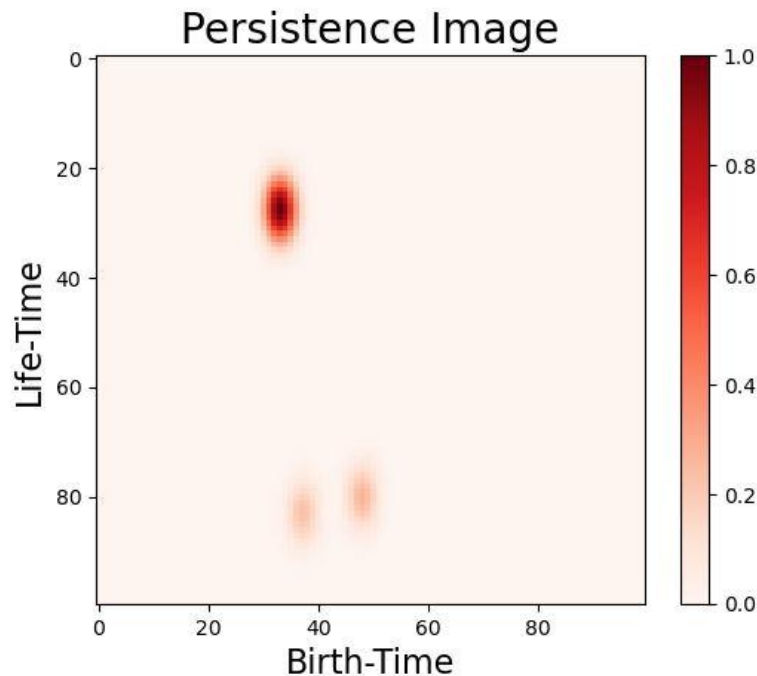
One of the most commonly used topological descriptors

Cons:

Not easily used in standard machine learning algorithms, as the number of points that we observe on a persistence diagram varies from sample to sample

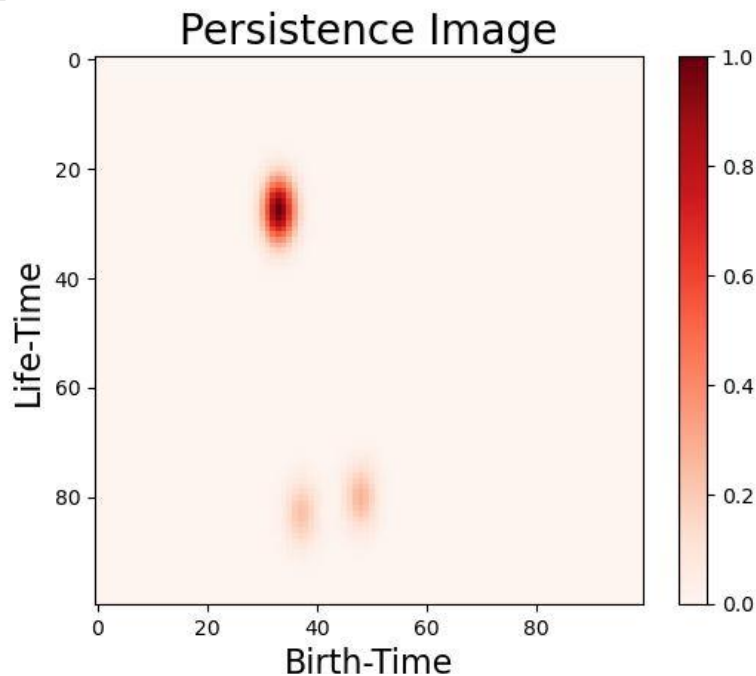


Persistence Images

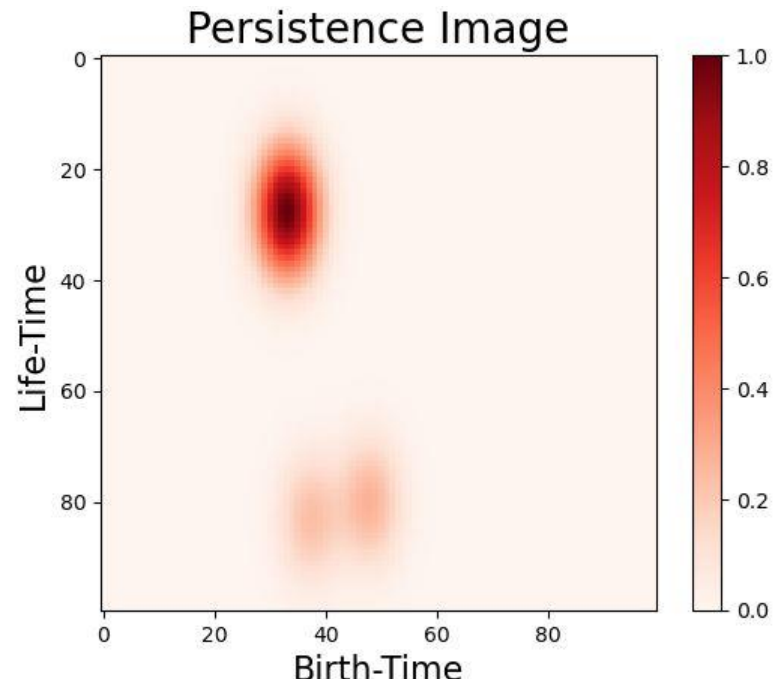




Effect of Spread

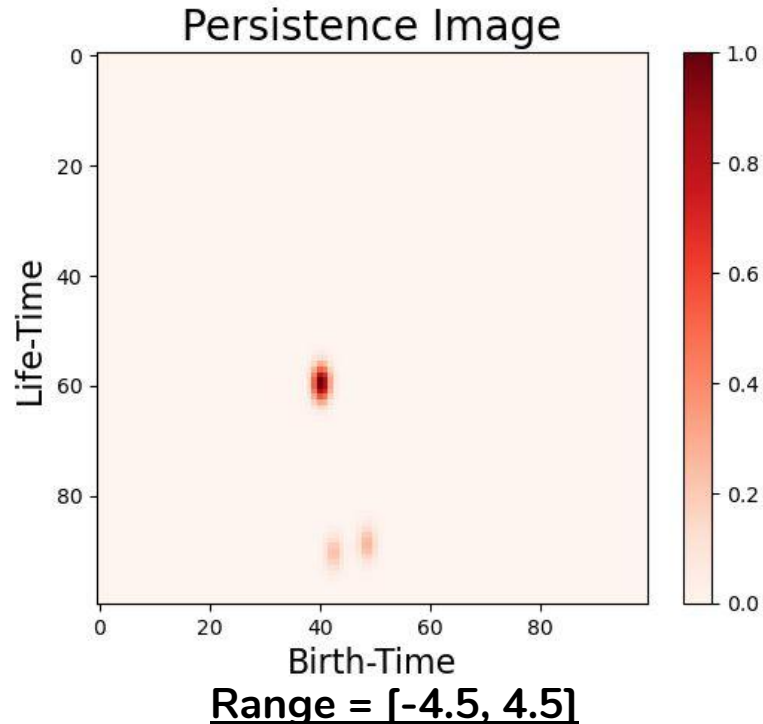
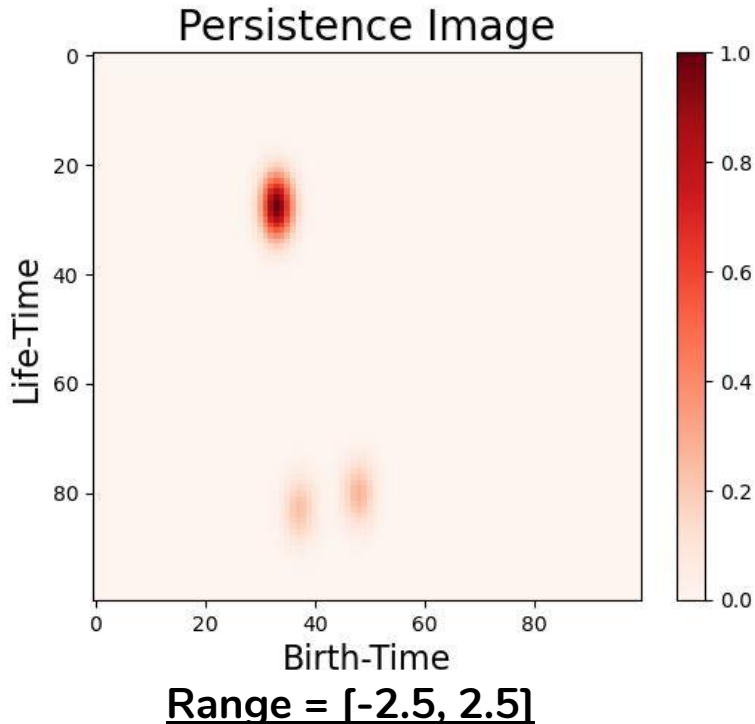


Spread = 0.1

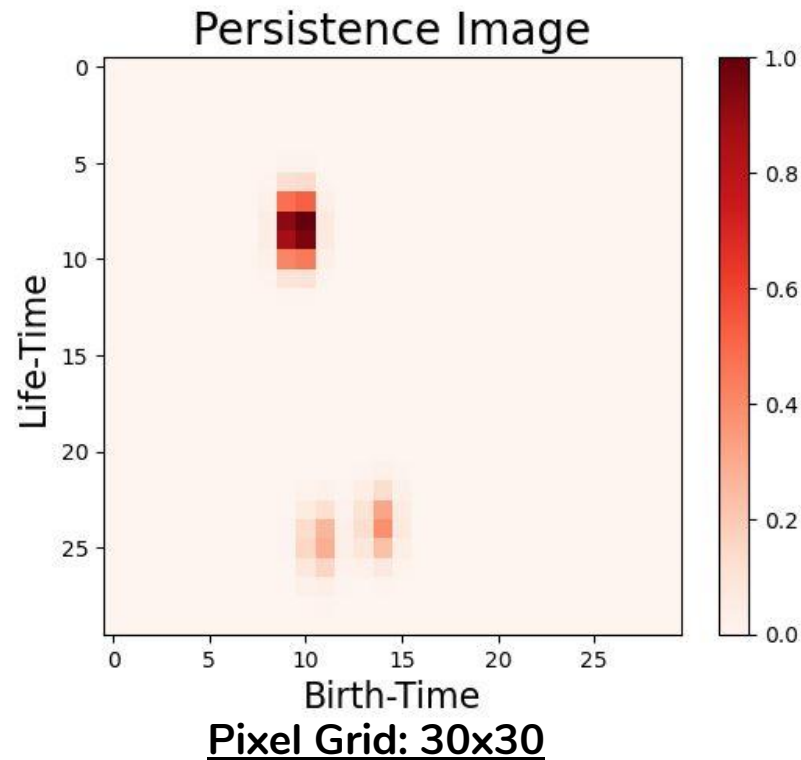
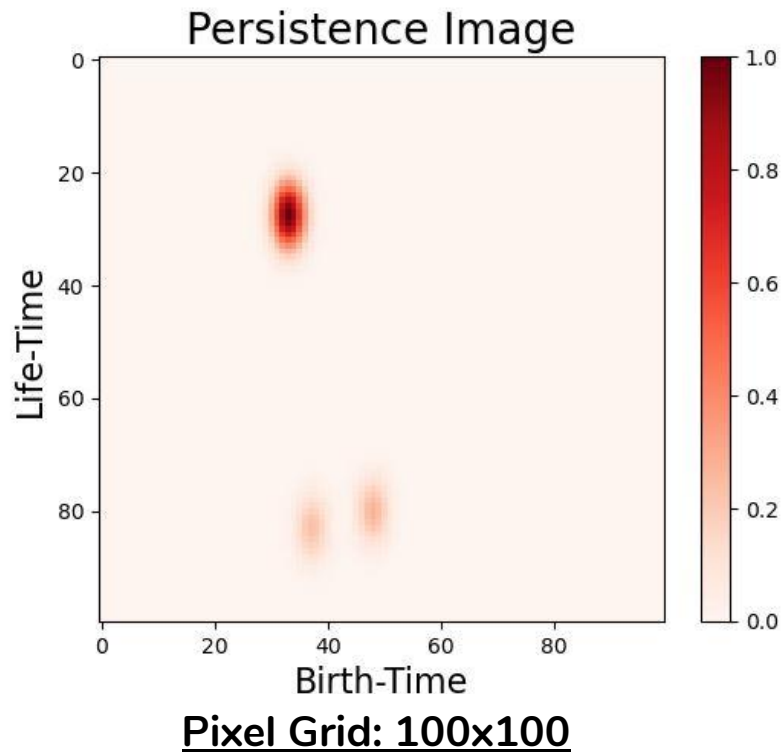


Spread = 0.2

Effect of Range



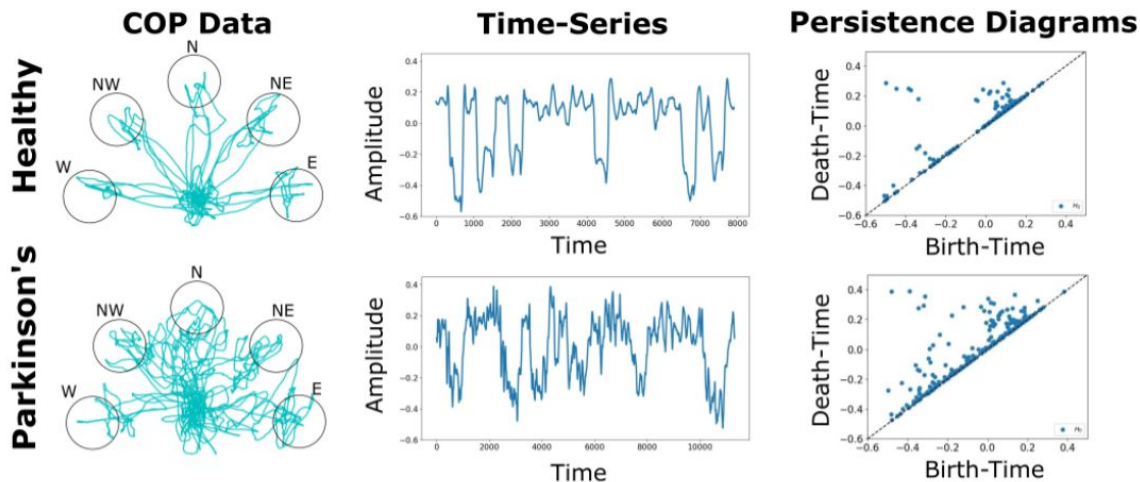
Effect of Pixel Value



Application



Processing Flow



Round-Robin
Leave-One-Subject-Out Cross
Validation Protocol with Support
Vector Machines

Binary Classification
- Parkinsons vs. Healthy

Three-Class Classification
- Parkinsons vs. Young vs.
Elderly

Regression
- Parkinsons Patients
Given Clinically Assigned
UPDRS Scores
- Healthy Patients Given
UPDRS Score of 0

Experimental Results

Method	3-Class Classification (%)	Regression	
		Correlation	P-Value
Peak Velocity Index	53.01	0.8153	$2.8227e^{-15}$
LLE	47.37	0.6449	$2.6707e^{-08}$
A3 [1]	60.53	0.7518	$4.4376e^{-12}$
D1 [1]	70.30	0.8479	$9.2763e^{-18}$
D2 [1]	71.43	0.9006	$1.1847e^{-22}$
D3 [1]	68.42	0.8479	$1.2715e^{-17}$
D4 [1]	65.79	0.8509	$7.2852e^{-18}$
A3M [7]	65.41	0.8528	$5.2806e^{-18}$
D1M [7]	73.31	0.8649	$5.1880e^{-19}$
D2M [7]	71.05	0.8639	$6.3778e^{-19}$
D3M [7]	71.80	0.8598	$1.4184e^{-18}$
D4M [7]	68.05	0.8680	$2.7529e^{-19}$
Persistence Images	73.68	0.8493	$9.85e^{-18}$

Binary
Classification:
98.87%

[1] A. Som, N. Krishnamurthi, V. Venkataraman, and P. Turaga. Attractor shape descriptors for balance impairment assessment in parkinson's disease. In 2016 38th Annual International Conference of the IEEE Engineering in Medicine and Biology Society (EMBC), pages 3096–3100. IEEE, 2016

[7] A. Som, N. Krishnamurthi, V. Venkataraman, K. N. Ramamurthy, and P. Turaga. Multiscale evolution of attractor-shape descriptors for assessing parkinson's disease severity. In 2017 IEEE Global Conference on Signal and Information Processing (GlobalSIP), pages 938–942. IEEE, 2017.



Thank You

For any questions, please do not hesitate to email us at:

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- Farhan Rahman: fnrahman@asu.edu
- Anirudh Som: asom2@asu.edu



Also refer to our GitHub repository with sample code here: <https://github.com/itsmeafra/Sublevel-Set-TDA>