

## Lab 7 – Quantization

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**Objectives:** In this lab, we will

- use Matlab to quantize *continuous-valued* signals, compute SQNR •
  - study effect of quantization on the quality of reconstructed signal.
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### 7.1 Quantization

Quantization involves discretization and encoding of samples of a signal. In this task we will take a closer look at discretization and how it effects the signal values. The encoding part which maps these levels to appropriately chosen binary code words is not considered here. For a discrete-time signal  $x[n]$ , quantization and quantization error are given by

$$x_q[n] = Q(x[n])$$

$$e_q[n] = x[n] - x_q[n].$$

The quantization function  $Q(\cdot)$  maps any real input to a point from discrete set of values. There are numerous quantization functions used in practice. We implement a non-uniform quantizer in the function below.

>> Write a Matlab function `y = quadratic_quant(x,B,a)` with inputs

- $x$  – input signal as a vector
- $B$  – number of bits used to decide quantization levels (positive integer)
- $a$  – positive real number such that  $[-a,a]$  forms the range for quantization.

The function should produce an output  $y$ , which is the quantized version of the input signal. For purpose of this function, assume that the input signal  $x$  itself is not quantized (though this is not true). We wish to implement a *quadratic non-uniform quantizer* as discussed below.

>> For the range  $[0, a)$  : To implement the above function, divide the interval  $[0,1]$  into  $L = 2^{B-1}$  equal sized intervals. Let  $0 = r_0 < r_1 \dots < r_{L-1} < r_L = 1$  be edge points of these intervals. Then the quantizer should map values in the interval  $[r_i, r_{i+1})$  to its mid-point. Repeat the process symmetrically for the range  $[-a, 0)$ . Make sure your quantizer has a total of  $2^B$  levels in the interval  $[-a, a)$ .

As an example, if  $a = 1$  and  $B = 2$ , then the  $2^B = 4$  quantizer intervals are  $[-1, -0.25)$ ;  $[-0.25, 0)$ ;  $[0, 0.25)$ ;  $[0.25, 1)$  and the quantization follows

if  $x[i] \in [-1, -0.25)$ ,  $y[i] = -0.625$ , if  $x[i] \in [0, 0.25)$ ,  $y[i] = 0.125$

and so on. This is only an example; the code should consider general inputs 'a' and B. For inputs outside the interval  $[-a, a)$  you should quantize them to the end points of your quantized set of values.

>> Write a matlab script which does the following tasks:

- Consider the analog signal  $x(t) = \sin(2\pi f_0 t)$  with  $f_0 = 10 \text{ Hz}$ . Sample a 1 second portion of this signal (in the time interval  $t \in [0, 1]$ ) at a sampling frequency of  $F_s = 5 \text{ KHz}$  to obtain the discrete-time signal  $x[n]$ . Use the function above to obtain the quantised signal  $x_q[n]$ .
- Create a figure with 3x1 subplot grid and plot the sampled signal and quantised signal in the first two subplots (use proper labelling). Use  $a = 1$  and  $B = 4$ .
- Compute and plot the quantization error in the remaining panel of the figure.
- In a different figure, plot histogram of the quantization error using the matlab function `histogram()` with 15 bins (see documentation). Repeat for  $B = 3$  and compare the histograms.
- Repeat above processing for  $B = 1:8$  (do not repeat the figures). In another figure, plot a graph with B on X-axis and maximum absolute quantization error (over the complete signal duration) on Y-axis and comment on your observations.
- Experimentally measured SQNR is defined as the ratio of signal power to quantization noise power:

$$SQNR = \frac{\sum_n |x[n]|^2}{\sum_n |e_q[n]|^2}$$

In another figure, plot a graph with B on X-axis and Signal to Quantization Noise Ratio (SQNR) on Y-axis and comment on your observations.

- What can you say about accuracy of the above non-uniform quantizer in various regions of the interval  $[-a, a)$ ? How would this compare with say a uniform quantizer which instead considers intervals of the form  $[ar_i, ar_{i+1})$ ?

## 7.2 Quantization of Audio signals

For this section, use one of the audio file from part 6.5 (previous lab) and write a matlab script.

>> Load .wav file in Matlab. Quantize this signal using your quantization function with  $B = 3$  and  $a = 1$ . Listen to the original signal and the quantized signal using the `sound()` command. How does the sound quality of these two signals compare?

>> Perform quantization for different levels ( $B = 1:8$ ) in a for-loop. Play the quantized signal in the for-loop with a pause of 2 seconds added after every call to the `sound()` command. Note your observations as levels increases and comment on quality of sound by hearing them.

>> How does quantization affect the frequency content of the quantized signal compared to that of the input signal? How does  $B$  play a role in this?