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Article

Local Crossover: A new genetic operator for Grammatical Evolution

Ioannis G. Tsoulos^{1,*}, Vasileios Charilogis² and Dimitrios Tsalikakis³

- Department of Informatics and Telecommunications, University of Ioannina, Greece; itsoulos@uoi.gr
- ² Department of Informatics and Telecommunications, University of Ioannina, Greece; v.charilog@uoi.gr
- Department of Engineering Informatics and Telecommunications, University of Western Macedonia, 50100 Kozani, Greece;tsalikakis@gmail.com
- * Correspondence: itsoulos@uoi.gr

Abstract: In this work, a new genetic crossover operator is proposed, which can be used to problems solved by the Grammatical Evolution technique. This new operator intensively applies the one point crossover procedure to randomly selected chromosomes with the aim of drastically reducing their fitness value. To apply the one point crossover method, a set of randomly selected chromosomes is selected from the current population. This new operator was applied to two techniques from the recent literature that exploit Grammatical Evolution: artificial neural network construction and rule construction. In both case studies, an extensive set of classification problems and data fitting problems were incorporated to estimate the effectiveness of the proposed genetic operator. The proposed operator significantly reduced both the classification error on the classification datasets and the feature learning error on the fitting datasets, compared to other machine learning techniques and also to the original models before applying the new operator.

Keywords: Genetic algorithms; Genetic Programming; Grammatical Evolution; Genetic operators

1. Introduction

Genetic algorithms are stochastic optimization algorithms originated in the work of Holland [1]. They belong to a wide area of optimization algorithms called evolutionary techniques [2]. Genetic algorithms initiate by formulating candidate solutions of the objective problem. These solutions are evolved through a series of processes that mimic natural evolution, such as selection, crossover and mutation [3–5]. The genetic algorithms were incorporated in a variety of problems, such as networking problems [6], problems arise in robotics [7,8], energy problems [9,10], medicine problems [11,12], agriculture problems [13] etc.

Grammatical Evolution [15] is an integer based genetic algorithm, where each chromosome represents a series of production rules derived from a Backus–Naur form (BNF) grammar [16]. Grammatical Evolution can be utilized to produce programs in any programming language. This method was used in a series of cases derived from real - world problems, such as data fitting [17,18], credit classification [19], detection of network attacks [20], solving differential equations [21], monitoring the quality of drinking water [22], construction of optimization methods [23], application in trigonometric problems [24], composition of music [25], constructing neural networks [26,27], production of numeric constants with a variable number of digits [28], video games [29,30], energy problems [31], combinatorial optimization [32], security topics [33], automatic construction of decision trees [34], circuit design [35], discovering taxonomies in Wikipedia [36], trading algorithms [37], bioinformatics [38], modeling glycemia in humans [39], etc.

Grammatical Evolution has been extended by many researches in recent bibliography. Among these extensions there are works, such as the Weighted Hierarchical Grammatical Evolution [40], which proposed a novel technique to map genotypes to phenotypes. Also,

Citation: Tsoulos, I.G.; Charilogis, V.; Tsalikakis, D. Local Crossover: A new genetic operator for Grammatical Evolution. *Journal Not Specified* **2024**, 1, 0. https://doi.org/

Received:

Revised:

Accepted:

Published:

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the method of Structured Grammatical Evolution [41,42], proposed a one-to-one mapping for chromosomes and the set of non - terminal symbols. Also, O'Neill et al. suggested the usage of shape grammars in the Grammatical Evolution for evolutionary design [43]. Also the π Grammatical Evolution method [44] was suggested as a modification of the Grammatical Evolution, where a position - independent mapping was proposed. Another interesting work was the incorporation of the Particle Swarm Optimization(PSO) [45] to create expressions in Grammatical Evolution. This method was named Grammatical Swarm [46,47] in the relevant literature. Moreover, the method of Probabilistic Grammatical Evolution [48] has been introduced recently, where a stochastic procedure was used as a mapping mechanism. Recently, the optimization method of Fireworks algorithm [49] was applied as a learning algorithm for the Grammatical Evolution procedure [50]. Contreras et al. suggested the combination of Grammatical Evolution and some ideas from interval analysis, to solve problems with uncertainty [51]. Grammatical evolution has also been extended using programming techniques [52,53] or Christiansen grammars [54].

Additionally, many researchers have developed and published open source software for Grammatical Evolution, such as the graphical user interface (GUI) application of Grammatical Evolution in Java (GEVA)[55], a Java implementation called jGE [56], an R implementation of Grammatical Evolution called gramEvol (Grammatical Evolution for R) [57], the GRAPE software that implemented Grammatical Evolution in Python [58], the GeLab [59] software that suggested a Matlab toolbox for Grammatical Evolution, a software which produced classification programs with Grammatical Evolution called GenClass [60], the QFc software [61] the used to create new features from the initial features with the assistance of Grammatical Evolution etc.

In this work, a new genetic operator for Grammatical Evolution is introduced, which is based on the one crossover technique. The new genetic operator is stochastically applied to the genetic population, randomly selecting a set of chromosomes on which to apply it. For each randomly selected chromosome, a group of chromosomes is stochastically formed from the current genetic population. Afterwards, a one - point crossover operation is performed between the selected chromosome and each of the generated group to search for a lower value of the fitness function. The new genetic operator was applied in two distinct cases of Grammatical Evolution methods: in the rule construction technique introduced recently [62] and in the neural network construction technique [63]. These machine learning tools were applied on a some classification and regression datasets proposed in the recent literature and the experimental results indicated a reduction in classification or regression error from the application of the new genetic operator.

The main components of the proposed technique are:

- 1. The method can be applied as a genetic operator to all problems solved by the Grammatical Evolution technique and the only information it exploits is the fitness function of the problem.
- 2. The method has no dependence on the grammar of the objective problem.
- 3. By using an application rate the user can require fewer or more applications of the new operator.
- 4. Although this operator requires significant computing time for its execution, its application between chromosomes can be done using parallel techniques, since there is no dependency between its successive applications.
- 5. Simple linear operations are required for its implementation, such as crossing a point between chromosomes.
- 6. The new genetic operator could theoretically be applied to other forms of genetic algorithms beyond Grammatical Evolution.

The following sections have this structure: in section 2 the basic principles of Grammatical Evolution are discussed as well as the current genetic operator. In section 3 the used datasets are described followed by the experimental results and in section 4 some conclusions are discussed in detail.

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2. Materials and Methods

2.1. Basics of the Grammatical Evolution method

The Grammatical Evolution considers chromosomes as set of production rules in the provided BNF grammar. BNF grammar is usually denoted as a set G = (N, T, S, P), with the following assumptions:

- *N* defines the set of non-terminal symbols.
- *T* is a set that contains the terminal symbols.
- *S* is a non terminal symbol that corresponds to the that start symbol of the grammar.
- P is the set of the rules used during production. These rules are in the form $A \to a$ or $A \to aB$, $A, B \in N$, $a \in T$. In Grammatical Evolution procedure a sequence number is assigned to every production rule.

The grammar used for the rule machine learning method is outlined in Figure 1 and the grammar used for the neural network construction technique is displayed in figure 2.

Figure 1. The BNF grammar used in the method that constructs rules using the Grammatical Evolution procedure.

```
<S>::= <ifexpr> value=<expr> else value=<expr>
<ifexpr>::= if(<bexpr>) value=<expr> (0)
             |<ifexpr> else if(<bexpr>) value=<expr> (1)
<bexpr>::=<expr> <rop> <expr> (0)
             |<bexpr> <bop> <bexpr> (1)
< rop > : : = > (0)
            |>= (1)
            < (2)
            |<=(3)
            | =
            |!=(5)|
<bop>::=
          & (0)
            | | (1)
<expr> ::=
            (<expr> <op> <expr>)
            | <func> ( <expr> )
                                     (1)
            <term>
<op> ::=
                      (0)
                      (1)
              *
                      (2)
                      (3)
<func> ::=
                   (0)
              sin
                   (1)
            cos
            exp
                    (2)
            log
                    (3)
                                   (0)
<term>::=<xlist>
            |<dlist>.<dlist> (1)
<xlist>::=x1
                 (0)
            | x2 (1)
            . . . . . . . . .
            | xD (D-1)
                                      (0)
<dlist>::=<digit>
             (1)
\langle \text{digit} \rangle ::= 0 (0) | 1 (1)
            | 2 (2) | 3 (3)
            | 4 (4) | 5 (5)
            | 6 (6) | 7 (7)
            | 8 (8) | 9 (9)
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Figure 2. The BNG grammar for the procedure of creating artificial neural networks with Grammatical Evolution.

The notation <> is used to enclose Non-terminal symbols. The numbers at the end of the production rules represent the sequence number of each rule. The parameter d is the dimension of the used dataset (number of features). Grammatical Evolution produces valid expressions by starting from the starting symbol S and by following the production rules. The method selects the following production rules according to the scheme:

- **Get** the next element *V* for the processed chromosome.
- **Select** the rule that will be applied as:

$$Rule = V \bmod NR \tag{1}$$

where the value NR represents the total number of production rules for the under processing non – terminal symbol.

For a dataset with three features (x_1, x_2, x_3) an example of rule construction method could be the following:

$$if(x_1 > 2 + sin(x_3))value = 1 + cos(x_2) else value = 1 + x_1$$

The terminal symbol value is used to denote the final outcome of the rule method. For the same dataset an example of neural network constructed by the Grammatical Evolution may be the following:

$$NNC(x) = 2.45sig(1.9x_1 + 3.11x_3 + 2.5) + 5.9sig(10.8x_2 + 6.25)$$

This grammar of Figure 2 is able to produce artificial neural networks using this form:

$$N(\overrightarrow{x}, \overrightarrow{p}) = \sum_{i=1}^{H} p_{(n+2)i-(n+1)} \sigma\left(\sum_{j=1}^{n} x_j p_{(n+2)i-(n+1)+j} + p_{(n+2)i}\right)$$
(2)

The vector \overrightarrow{x} represents the input vector, while the vector \overrightarrow{p} stands for the parameter set of the neural network. The parameter H represents the number of weights or processing units. These networks have one processing level, but the grammar could be easily extended

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to produce neural networks of additional levels. The function sig(x) used in the previous example denotes the sigmoid function given by:

$$\operatorname{sig}(x) = \frac{1}{1 + \exp(-x)} \tag{3}$$

used in the majority of cases of neural networks. Of course, the Grammatical Evolution procedure can construct neural networks with different activation functions or neural networks that use a mix of activation functions.

2.2. The genetic algorithm

The two machine learning techniques, in which the new genetic operator was applied, follow a series of similar execution steps, which are presented in detail below:

1. Initialization step.

- (a) **Set** k = 0 the generation counter.
- (b) **Set** N_g the maximum number of allowed generations.
- (c) **Set** as N_c the total number of chromosomes in the genetic population.
- (d) **Set** as p_s the selection rate, where $p_s \le 1$.
- (e) **Set** as p_m the mutation rate, where $p_m \le 1$
- (f) **Set** as p_{cr} the rate for the application of the new crossover operator, where $p_{cr} \le 1$
- (g) **Set** as N_{cr} the amount of chromosomes the will be selected for each chromosome where the new crossover operator will be applied.

2. Fitness step.

- (a) **For** $i = 1, ..., N_c$ **do**
 - i. **Set** as f_i the fitness of chromosome i. For the case of rule creation model the grammar of Figure 1 is applied while for the case of neural network construction the grammar of Figure 2 is utilized.
- (b) EndFor

3. Genetic operations step.

- (a) **Apply** the selection procedure: In the first phase, the chromosomes are sorted according to their fitness. The $(1 p_s) \times N_c$ best of these are transmitted unchanged to the next generation, while the rest will be replaced by chromosomes produced through crossover and mutation.
- (b) **Perform** the crossover procedure: During this procedure $p_s \times N_c$ offsprings are produced from the population under processing. For every set (\tilde{z}, \tilde{w}) of produced children, two distinct chromosomes (z, w) are chosen from the current population with tournament selection. The offsprings (\tilde{z}, \tilde{w}) are formulated using the one point crossover procedure, graphically outlined in Figure 3.
- (c) **Perform** the mutation procedure. During this procedure a random number $r \in [0,1]$ is selected for each element of every chromosome and this element is changed randomly if $r \leq p_m$.
- (d) **Apply** the new crossover operator: For each chromosome g_i , $i = 1, ..., N_c$ a random number $r \in [0,1]$ is selected. If $r \leq p_{cr}$ then execute the procedure described in subsection 2.3 on g_i .

4. Termination step.

- (a) **Set** k = k + 1
- (b) If $k \le N_g$ goto Step 2, else terminate.

The previous algorithm is also graphically illustrated in the flowchart of Figure 4.

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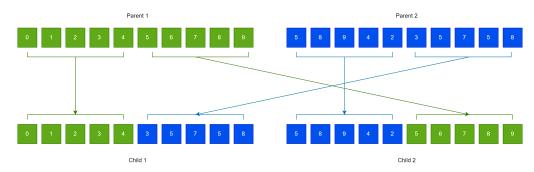


Figure 3. An example of the method of one - point crossover. This method is used as the crossover procedure in the Grammatical Evolution procedure.

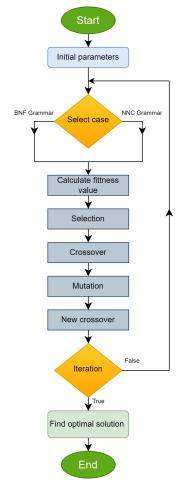


Figure 4. A flowchart indicating the main steps of the used genetic algorithm.

2.3. The new crossover operator

The new crossover operator executes the one - point crossover method on a selected chromosome using a set chromosomes that was selected randomly from the current population. The steps of this procedure are listed below:

- 1. **Set** as g the chromosome where the operator will be applied and as f_g the corresponding fitness value.
- 2. **Create** the set $C = \{x_1, x_2, \dots, x_{N_{cr}}\}$ of N_{cr} randomly selected chromosomes.
- 3. **For** $i = 1, ..., N_{cr}$ **do**
 - (a) **Perform** one point crossover between g and x_i . This procedure produces the offsprings g_1 and g_2 with associated fitness values f_{g_1} and f_{g_2} .

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(b) If $f_{g_1} \leq f_g$ then i. $g = g_1$ (c) also if $f_1 \leq f_2$ then

(c) else if $f_{g_2} \le f_g$ then i. $g = g_2$

(d) Endif

4. EndFor

3. Results

The suggested genetic operator was tested on a set of classification and regression datasets obtained from the recent bibliography and relevant websites. The internet sources for these datasets are the following websites:

- 1. The UCI dataset repository, https://archive.ics.uci.edu/ml/index.php(accessed on 10 October 2024)[64]
- 2. The Keel repository, https://sci2s.ugr.es/keel/datasets.php(accessed on 10 October 2024)[65].
- 3. The Statlib URL http://lib.stat.cmu.edu/datasets/(accessed on 10 October 2024).

3.1. The used classification datasets

A wide series of datasets presenting classification problems is used here:

- 1. **Appendictis** proposed in [66].
- 2. **Australian** dataset [67], suggested for credit card transactions.
- 3. **Balance** dataset [68], used in a series of psychological experiments.
- 4. **Circular** dataset, that is an artificial dataset.
- 5. **Cleveland** dataset [69,70].
- 6. **Dermatology** dataset [71], related to dermatological deceases.
- 7. **Ecoli** dataset, related to protein problems[72].
- 8. **Fert** dataset, for the detection of possible relations between fertility and sperm concentration.
- 9. **Haberman** dataset, used for breast cancer detection.
- 10. **Hayes roth** dataset [73].
- 11. **Heart** dataset [74], proposed for the detection of heart diseases.
- 12. **HeartAttack** dataset, a medical dataset related to heart diseases.
- 13. **House Votes** dataset [75], that contains the votes in the U.S. House of Representatives for various cases.
- 14. **Glass** dataset, which contains glass component analysis for glass pieces that belong to 6 classes.
- 15. **Liverdisorder** dataset [76], a medical dataset for the detection of liver disorders.
- 16. **Mammographic** dataset [78], used in breast cancer detection.
- 17. **Parkinsons** dataset, proposed in[77].
- 18. **Pima** dataset [79], used in the detection of diabetes.
- 19. **Popfailures** dataset [80], that to do with climate related measurements.
- 20. **Regions2** dataset, proposed in [81].
- 21. Saheart dataset [82], proposed to detect heart diseases.
- 22. **Segment** dataset [83], which contains information regarding image processing.
- 23. **Spiral** dataset, that is a dataset created artificially.
- 24. **Student** dataset [84], a dataset for measurements in schools.
- 25. Wdbc dataset [85], used in cancer detection.
- 26. Wine dataset, which contains information about wines. [86,87].
- 27. **Eeg** datasets, a medical dataset contains measurements from various experiments regarding EEG [88]. The following sub datasets were extracted from this dataset: Z_F_S, Z_O_N_F_S, ZO_NF_S and ZONF_S.
- 28. **Zoo** dataset [89], proposed to estimate the category of some animals.

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3.2. The used regression datasets

A series of datasets from this category was utilized in the experiments:

- 1. **Abalone** dataset [90], a dataset used to predict the age of abalones.
- 2. **Airfoil** dataset, provided by NASA [91].
- 3. **BK** dataset [92], related to the prediction of points in a basketball game.
- 4. **BL** dataset, that is related to calculations from electricity experiments.
- 5. **Baseball** dataset, used to estimate the income of baseball players.
- 6. **Concrete** dataset [93], is a dataset related to the durability of cements in public works.
- 7. **Dee** dataset, related to the prices of electricity.
- 8. **FY**, a dataset that contains measurements for the longevity of fruit flies.
- 9. **HO** dataset, provided from the the STALIB repository.
- 10. **Housing** dataset [94].
- 11. **Laser** dataset, that contains measurements from laser experiments.
- 12. LW dataset, that contains measurements regarding the weight of babies.
- 13. MORTGAGE, that contains economic measurements from USA.
- 14. MUNDIAL, used from the STALIB repository.
- 15. **PL** dataset, used from the STALIB repository.
- 16. **QUAKE** dataset, used in measurements from earthquakes.
- 17. **REALESTATE**, from the STALIB repository.
- 18. SN dataset, that is used in an experiment related to trellising and pruning.
- 19. **Treasury** dataset, that is a dataset regarding the economy of USA.
- 20. **TZ** dataset, founded in the STALIB repository.
- 21. VE dataset, from the STALIB repository.

3.3. Experimental results

ANSI C++ was used to code the software for the conducted experiments using also the Optimus optimization environment, available from https://github.com/itsoulos/GlobalOptimus/(accessed on 10 October 2024). The experiments were executed 30 times for each case and the random number generator was initialized using different seed in every execution. For the case of classification problems, the average classification error as measured on the test set was recorded and, for the case of regression datasets, the average regression error as measured on the test set was recorded. The validation of experiments was carried out using the method of ten - fold cross validation. Table 1 depicts the experimental settings for the performed experiments.

Table 1. This table presents the values used for the experimental parameters, used in the conducted experiments.

PARAMETER	MEANING	VALUE
N_c	Chromosomes used	500
N_g	Maximum number of generations	200
p_s	Crossover rate	0.10
p_m	Mutation rate	0.05
p_{cr}	New crossover rate	0.05
N_{cr}	New crossover items	100
Н	Weights for the neural network	10

Table 2 outlines the experimental results for the classification datasets while Table 3 hold the results for the mentioned regression datasets. The following notations are used in the experimental tables:

1. The column BFGS represents the incorporation of the BFGS method [95] to train an artificial neural network with *H* hidden nodes.

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- 2. The column GEN outlines the experimental results using a genetic algorithm [96] to train an artificial neural network with *H* hidden nodes. The values for the critical parameters of the genetic algorithm are included in Table 1.
- 3. The column RULE refers to the simple rule construction method [14], without the incorporation of the new crossover operator.
- 4. The column NNC refers to the method of neural network construction [63]. This method was applied without the new operator.
- 5. The column RULE_CROSS represents the application of the new crossover operator the rule construction machine learning model.
- 6. The column NNC_CROSS depicts the results for the neural construction method with the assistance of the new genetic operator.
- 7. The average error is depicted in row under the name AVERAGE.

Table 2. This table shows the average classification error as calculated on the corresponding test set for the classification datasets using all machine learning models.

DATASET	BFGS	GEN	RULE	NNC	RULE_CROSS	NNC_CROSS
APPENDICITIS	18.00%	24.40%	14.70%	13.70%	14.80%	14.40%
AUSTRALIAN	38.13%	36.64%	14.27%	14.51%	14.46%	14.71%
BALANCE	8.64%	8.36%	28.79%	22.11%	17.47%	14.32%
CIRCULAR	6.08%	5.13%	13.25%	13.64%	9.12%	7.49%
CLEVELAND	77.55%	57.21%	48.24%	50.10%	47.52%	49.21%
DERMATOLOGY	52.92%	16.60%	43.77%	25.06%	38.00%	12.92%
ECOLI	69.52%	54.67%	55.18%	47.82%	53.48%	49.15%
FERT	23.20%	28.50%	17.40%	19.00%	17.50%	19.20%
HABERMAN	33.10%	27.80%	27.03%	28.03%	26.53%	28.37%
HAYES-ROTH	56.54%	35.85%	39.39%	35.93%	38.08%	24.08%
HEART	39.44%	26.41%	20.30%	15.78%	19.41%	15.33%
HEARTATTACK	46.67%	29.03%	23.63%	19.33%	23.70%	18.73%
HOUSEVOTES	7.13%	7.00%	3.48%	3.65%	4.51%	3.22%
GLASS	69.95%	55.09%	58.10%	57.10%	54.81%	53.82%
IONOSPHERE	13.37%	18.03%	15.06%	11.12%	14.14%	9.25%
LIVERDISORDER	42.59%	37.09%	37.09%	33.71%	35.68%	31.24%
MAMMOGRAPHIC	29.54%	16.33%	19.00%	17.78%	18.10%	17.12%
PARKINSONS	27.58%	16.58%	13.47%	12.21%	13.37%	11.47%
PIMA	35.59%	34.21%	27.85%	27.99%	27.30%	25.95%
POPFAILURES	5.24%	4.17%	5.44%	6.74%	5.02%	6.41%
REGIONS2	36.28%	33.53%	29.13%	25.52%	29.26%	24.46%
SAHEART	37.48%	34.85%	30.20%	30.52%	31.00%	28.64%
SEGMENT	68.97%	46.30%	71.51%	54.99%	61.99%	35.82%
SPIRAL	47.99%	47.67%	50.06%	48.39%	49.08%	48.04%
STUDENT	4.90%	6.75%	11.08%	5.78%	7.23%	5.06%
TRANSFUSION	25.59%	24.01%	25.19%	25.34%	24.46%	24.44%
WDBC	29.91%	7.87%	7.66%	6.95%	6.43%	6.48%
WINE	59.71%	22.88%	15.35%	14.35%	12.47%	9.88%
Z_F_S	39.37%	24.60%	16.40%	14.17%	8.77%	10.23%
Z_O_N_F_S	79.04%	64.26%	53.64%	49.18%	44.60%	42.30%
ZO_NF_S	43.04%	21.54%	14.10%	14.14%	8.39%	9.12%
ZONF_S	15.62%	4.36%	2.76%	3.14%	2.06%	2.70%
ZOO	12.10%	10.20%	14.80%	9.20%	11.10%	5.70%
AVERAGE	36.39%	26.91%	26.28%	23.54%	23.93%	20.58%

Table 3. This table shows the experimental results when the regression datasets were used and the numbers stand for the average regression error as measured on the corresponding test set.

DATASET	BFGS	GEN	RULE	NNC	RULE_CROSS	NNC_CROSS
ABALONE	6.38	7.17	7.36	5.05	5.32	4.63
AIRFOIL	0.003	0.001	0.003	0.003	0.002	0.002
BK	0.36	0.26	0.02	2.32	0.037	0.15
BL	1.09	2.23	2.53	0.021	0.023	0.40
BASEBALL	119.63	64.60	65.64	59.85	61.35	58.75
CONCRETE	0.023	0.001	0.013	0.008	0.009	0.005
DEE	2.36	0.47	0.43	0.26	0.32	0.23
FY	0.19	0.65	0.041	0.058	0.046	0.049
НО	0.62	0.37	0.019	0.017	0.019	0.014
HOUSING	97.38	35.97	47.99	26.35	26.74	19.10
LASER	0.03	0.084	0.055	0.024	0.032	0.019
LW	0.26	0.54	0.012	0.011	0.013	0.017
MORTGAGE	8.23	0.40	0.20	0.30	0.13	0.21
MUNDIAL	0.05	1.22	0.038	4.47	0.049	0.76
PL	0.11	0.03	0.056	0.045	0.035	0.036
QUAKE	0.09	0.12	1.13	0.045	0.73	0.046
REALESTATE	128.94	81.19	104.74	76.78	92.49	69.77
SN	0.16	0.20	0.025	0.026	0.026	0.024
TREASURY	9.91	0.44	0.15	0.47	0.12	0.30
TZ	0.21	0.097	0.036	5.04	0.035	0.061
VE	1.92	2.43	0.028	6.61	0.043	0.084
AVERAGE	17.99	9.45	10.98	8.94	8.93	7.35

There is a clear indication from the experimental results that there is a significant reduction in the mean error using the new genetic operator in both machine learning models. In a wide range of data sets, the proposed technique drastically reduces the error of data classification or fitting, as it is also represented in the graphs 5 and 6. These graphs show the number of datasets in which the application of the new genetic operator resulted in a drastic reduction in the corresponding error.

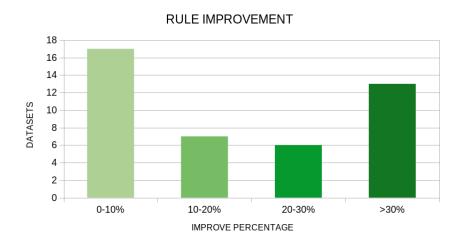


Figure 5. Number of datasets that improved in the RULE machine learning model using the proposed method. The vertical axis represents the number of data sets and the horizontal axis the percentage of reduction in error.

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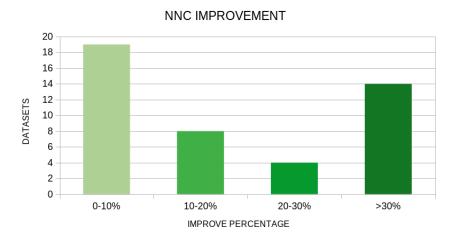


Figure 6. Number of datasets that improved in the NNC machine learning model using the proposed method. The vertical axis represents the number of data sets and the horizontal axis the percentage of reduction in error.

Furthermore, the box plots for the classification cases are shown in Figures 7 and 8 for the rule construction model and the network construction model respectively.

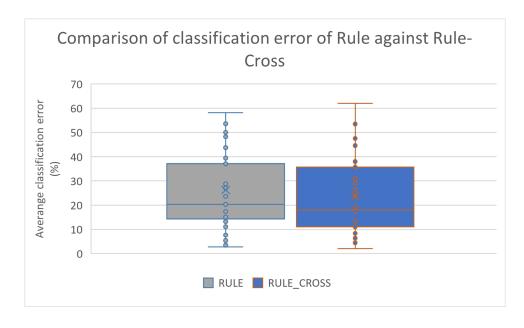


Figure 7. Box plot for the comparison between the original rule construction model and the improved one that utilizes the new crossover operator.

Figure 8. Box plot used to compare the original rule construction model and the improved one that utilizes the new crossover operator.

Box plots for the same comparisons as deduced from the results using the series of regression datasets are shown in Figures 9 and 10 respectively.

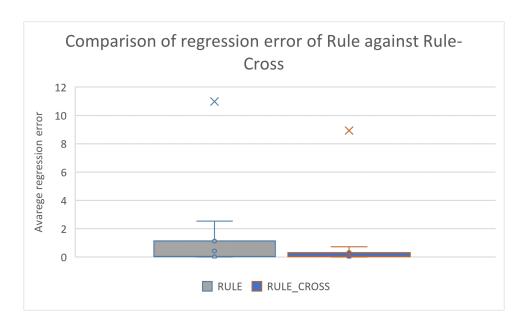


Figure 9. Box plot used to compare the original rule construction model and the improved one that utilizes the new crossover operator for the regression datasets.

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Figure 10. Box plot used to compare the original rule construction model and the improved one that utilizes the new crossover operator for the regression datasets.

These figures confirm the significant improvement brought about by the use of the new operator in the effectiveness of the two techniques that utilize Grammatical Evolution. This improvement appears to be greater in the datasets used in data fitting.

Also, a statistical comparison was performed between the two machine learning methods and the enhanced ones that use the new crossover operator. This comparison was performed using the classification datasets, and it is shown in Figure 11.

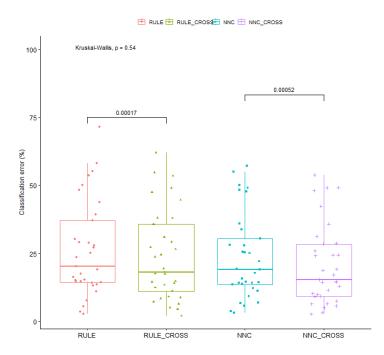


Figure 11. Statistical test for all the improved machine learning methods and the original methods. The methods were tested on the classification datasets.

Moreover, an additional test was executed in order to estimate the effectiveness of the new crossover rate parameter denoted as p_{cr} . In this experiment the rule construction

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machine learning model was applied on the classification datasets using a series of values for p_{cr} and the results are shown in Table 4.

Table 4. The effect of a series of values of p_{cr} to the RULE model with application on the classification datasets.

DATASET	RULE	$p_{cr} = 0.025$	$p_{cr} = 0.05$	$p_{cr} = 0.075$
APPENDICITIS	14.70%	15.80%	14.80%	15.10%
AUSTRALIAN	14.27%	13.96%	14.46%	14.03%
BALANCE	28.79%	20.18%	17.47%	18.07%
CIRCULAR	13.25%	11.00%	9.12%	9.78%
CLEVELAND	48.24%	48.24%	47.52%	46.07%
DERMATOLOGY	43.77%	38.60%	38.00%	36.00%
ECOLI	55.18%	52.49%	53.48%	48.83%
FERT	17.40%	16.70%	17.50%	18.50%
HABERMAN	27.03%	27.57%	26.53%	26.87%
HAYES-ROTH	39.39%	35.69%	38.08%	36.77%
HEART	20.30%	20.48%	19.41%	20.37%
HEARTATTACK	23.63%	22.83%	23.70%	22.53%
HOUSEVOTES	3.48%	3.48%	4.51%	3.13%
GLASS	58.10%	55.62%	54.81%	52.76%
IONOSPHERE	15.06%	15.14%	14.14%	14.14%
LIVERDISORDER	37.09%	34.79%	35.68%	33.50%
MAMMOGRAPHIC	19.00%	18.34%	18.10%	17.90%
PARKINSONS	13.47%	13.95%	13.37%	13.21%
PIMA	27.85%	27.80%	27.30%	27.84%
POPFAILURES	5.44%	5.33%	5.02%	5.32%
REGIONS2	29.13%	28.82%	29.26%	28.00%
SAHEART	30.20%	30.00%	31.00%	30.18%
SEGMENT	71.51%	67.36%	61.99%	63.91%
SPIRAL	50.06%	50.42%	49.08%	49.60%
STUDENT	11.08%	7.50%	7.23%	6.07%
TRANSFUSION	25.19%	24.20%	24.46%	24.68%
WDBC	7.66%	5.79%	6.43%	6.41%
WINE	15.35%	15.47%	12.47%	13.59%
Z_F_S	16.40%	11.63%	8.77%	9.10%
Z_O_N_F_S	53.64%	47.14%	44.60%	44.04%
ZO_NF_S	14.10%	10.50%	8.39%	8.42%
ZONF_S	2.76%	2.64%	2.06%	2.14%
ZOO	14.80%	11.30%	11.10%	8.70%
AVERAGE	26.28%	24.57%	23.93%	23.50%

Looking at the table of results, one can see a significant decrease in the average classification error when the application rate of the genetic operator increases from 2.5% to 5%. However, the rate of reduction of the average error decreases significantly when the application rate increases to 7.5%. This finding reinforces the idea of implementing the new genetic operator at a rate of 5%.

Another experiment was performed in order to estimate the importance of the parameter N_{cr} , which controls the number of chromosomes participating in the new crossover operator. In this experiment the neural network construction method was tested on the classification datasets using a series of values for the parameter N_{cr} while the parameter p_{cr} was fixed to 2.5%. The outcomes obtained from this experiment are depicted in Table 5.

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Table 5. The effects of the parameter N_{cr} to the NNC machine learning model. The classification datasets were used in this experiment. In all experiments the value p_{cr} was set to 0.025.

DATASET	NNC	$N_{cr}=25$	$N_{cr}=50$	$N_{cr} = 100$
APPENDICITIS	13.70%	14.00%	14.50%	14.70%
AUSTRALIAN	14.51%	14.46%	14.13%	13.97%
BALANCE	22.11%	22.29%	17.76%	18.05%
CIRCULAR	13.64%	11.90%	9.38%	8.46%
CLEVELAND	50.10%	49.69%	48.90%	49.17%
DERMATOLOGY	25.06%	20.51%	18.20%	16.29%
ECOLI	47.82%	47.79%	47.39%	47.52%
FERT	19.00%	18.70%	19.20%	18.70%
HABERMAN	28.03%	28.27%	28.43%	26.70%
HAYES-ROTH	35.93%	31.54%	27.77%	27.69%
HEART	15.78%	15.07%	16.00%	14.67%
HEARTATTACK	19.33%	20.13%	19.73%	18.50%
HOUSEVOTES	3.65%	3.30%	3.26%	3.13%
GLASS	57.10%	55.38%	54.62%	54.29%
IONOSPHERE	11.12%	10.63%	10.71%	9.89%
LIVERDISORDER	33.71%	32.03%	32.53%	31.12%
MAMMOGRAPHIC	17.78%	17.72%	17.64%	17.12%
PARKINSONS	12.21%	12.53%	12.79%	11.58%
PIMA	27.99%	27.26%	27.68%	26.09%
POPFAILURES	6.74%	6.33%	6.91%	6.35%
REGIONS2	25.52%	26.20%	25.47%	24.82%
SAHEART	30.52%	30.61%	29.81%	29.58%
SEGMENT	54.99%	53.07%	49.24%	42.90%
SPIRAL	48.39%	48.08%	48.20%	48.34%
STUDENT	5.78%	5.40%	5.20%	4.10%
TRANSFUSION	25.34%	25.26%	24.80%	24.47%
WDBC	6.95%	6.82%	7.39%	6.59%
WINE	14.35%	11.82%	11.77%	9.88%
Z_F_S	14.17%	12.60%	13.50%	9.98%
Z_O_N_F_S	49.18%	48.20%	46.24%	44.73%
ZO_NF_S	14.14%	12.72%	12.18%	10.42%
ZONF_S	3.14%	3.18%	2.82%	2.58%
ZOO	9.20%	8.20%	8.10%	7.50%
AVERAGE	23.54%	22.78%	22.19%	21.21%

The lowest average classification error is observed for $N_{cr}=100$, however, no major changes are observed in the classification errors as the parameter increases. Furthermore, is expected the average execution time to increase as the value N_{cr} increases and this is demonstrated in Figure 12, where the computation time for the neural network construction method is plotted with respect to the N_{cr} .

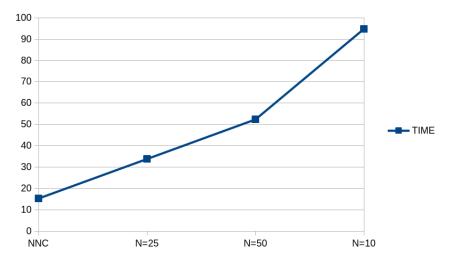


Figure 12. Average execution time for the NNC machine learning model using different values of the N_{cr} value.

The average computation time increases dramatically as the critical parameter N_{cr} increases, something that is expected since the crossings increase significantly with the increase of this parameter. This dramatic increase in required execution time can be reduced by incorporating modern parallel libraries. These programming techniques may include the application of the Message Passing Interface (MPI) library [97] or the incorporation of the OpenMP library [98].

4. Conclusions

A new genetic operator for tasks based on Grammatical Evolution is introduced in this article. This operator is applied to randomly selected chromosomes of the genetic population. On each application, a group of randomly selected chromosomes is formulated for every chromosome and one - point crossover is executed between each member of the group and the selected chromosome, aiming to reduce the associated fitness value. In order to measure the effectiveness of the new operator, it was applied with success in two machine learning models from the recent bibliography that utilize the Grammatical Evolution method:

- A rule construction method, that constructs rules in language similar to the C programming language for data classification or regression problems.
- A method that constructs artificial neural networks.

Several datasets from the literature were used to test the proposed method. In the vast majority of cases, the application of the new genetic operator resulted in a drastic reduction of the corresponding classification or data fitting error. Furthermore, to measure to asses the sensitivity of the proposed method to some critical parameters, more experiments were conducted in which these parameters were changed inside a wide range of values. Boosting these values improves the performance of machine learning methods by applying the new genetic operator, but up to a point. In addition, an increase in the chromosomes involved in the genetic operator, has a significant increase in the required execution time, as was also seen in the performed experiments. However, with the use of recent techniques that can utilize modern parallel computing structures, this additional time can be significantly reduced.

Improvements of the proposed operator in future studies may include the application of the new crossover in other machine learning methods based on Grammatical Evolution, a parallel implementation of the operator or even the usage of this operator in other tasks involving Genetic Algorithms.

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Author Contributions: V.C. and I.G.T. conducted the experiments, employing several datasets and provided the comparative experiments. D.T. and V.C. performed the statistical analysis and prepared the manuscript. All authors have read and agreed to the published version of the manuscript.

Funding: This research received no external funding.

Institutional Review Board Statement: Not applicable.

Institutional Review Board Statement: Not applicable.

Institutional Review Board Statement: Not applicable.

Acknowledgments: This research has been financed by the European Union: Next Generation EU through the Program Greece 2.0 National Recovery and Resilience Plan, under the call RESEARCH – CREATE – INNOVATE, project name "iCREW: Intelligent small craft simulator for advanced crew training using Virtual Reality techniques" (project code:TAEDK-06195).

Conflicts of Interest: The authors declare no conflicts of interest.

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