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Article

Healing Intelligence: A Bio-Inspired Metaheuristic optimization method Using Recovery Dynamics

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Abstract

BioHealing Optimization (BHO) is a bio-inspired metaheuristic optimization algorithm that emulates the biological process of injury and recovery. Its operation follows a cyclical mechanism comprising three main stages: an optional recombination phase, an injury phase, and a healing phase. During recombination, elements from the best-known solution are combined with differences drawn from other population members, producing candidate solutions that inherit beneficial traits while maintaining diversity. The injury phase applies stochastic perturbations to selected dimensions of solutions, using either Gaussian-like distributions or heavy-tailed variations, thereby promoting exploration of new regions in the search space. In the healing phase, the altered dimensions are guided gradually toward the current best solution, mimicking the progressive restoration of function observed in biological tissues. These core mechanisms are enhanced through adaptive strategies, including dynamic adjustment of injury intensity and probability, a "scar mapping" system that stores directional trends, focus on dimensions of higher relevance, and the introduction of high-intensity disturbance phases to overcome stagnation. The combination of these elements results in a self-regulating search process that maintains a balance between exploration and exploitation, enabling effective performance on challenging continuous optimization problems.

Keywords: Bio-inspired Algorithms; Metaheuristics; Regenerative Computing; Wound Healing; Evolutionary Algorithms; Global Optimization; Mutation Strategies;

Received: Revised: Accepted: Published:

Citation: Charilogis, V.; Tsoulos, I.G. Healing Intelligence: A Bio-Inspired Metaheuristic optimization method Using Recovery Dynamicss. Journal Not Specified 2024, 1, 0.

https://doi.org/

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1. Introduction

Global optimization refers to the task of identifying the global minimum of a real-valued, continuous objective function f(x), where the variable x belongs to a predefined, bounded search space $S \subset \mathbb{R}^n$. The goal is to determine the point $x^* \in S$ such that the function f(x) achieves its lowest possible value over the entire domain:

$$x^* = \arg\min_{x \in S} f(x). \tag{1}$$

where:

- f(x): is the objective function to be minimized. This function can represent a variety of criteria depending on the problem context, such as cost, loss, error, potential energy, or any other performance metric.
- S: is the feasible search space, a compact subset of \mathbb{R}^n , meaning it is both closed and bounded. Typically, S is defined as an n-dimensional hyperrectangle (also called a box constraint), given by:

$$S = [a_1, b_1] \otimes [a_2, b_2] \otimes \dots [a_n, b_n]$$

This denotes that each variable x_i is constrained within a finite interval: $x_i \in [a_i, b_i]$, for i = 1, 2, ..., n = 1, 2, ..., n. The Cartesian product of these intervals defines the multidimensional region where the search for the global optimum takes place.

Optimization is one of the most fundamental and widely applied domains of computational intelligence, with a vast range of applications in scientific, technological, and industrial fields. Although classical optimization techniques can be effective for small-or medium-scale problems, they often fail to deliver satisfactory results when applied to complex, nonlinear, and high-dimensional environments, where issues such as nonconvexity, high dimensionality, and the presence of multiple local optima dominate the search landscape. In this context, recent years have seen a continuous rise in interest toward metaheuristic methods, which offer flexible and stochastic search tools capable of addressing complex optimization problems without requiring derivative information or assumptions of continuity in the solution space.

Metaheuristic techniques are typically inspired by natural, biological, social, or physical processes, aiming to simulate powerful mechanisms for balancing exploration and exploitation within complex search spaces. Classic examples include Genetic Algorithms (GA) [1], Particle Swarm Optimization (PSO) [2], and Ant Colony Optimization (ACO) [3], which have been widely used for decades. In recent years, however, a multitude of novel metaheuristics have emerged, motivated by the desire to overcome common limitations such as premature convergence and weak performance on rugged, multimodal landscapes [4]. These methods draw inspiration from a broad range of biological and ecological systems. From the animal kingdom, algorithms like Artificial Bee Colony (ABC) [6], Grey Wolf Optimizer (GWO) [7], Whale Optimization Algorithm (WOA) [8], Dragonfly Algorithm (DA) [9], Cuckoo Search (CS) [10], and Bat Algorithm [11] emulate foraging, social, or navigation behaviors. Predator-prey-based algorithms such as Harris Hawks Optimization (HHO) [12] and Snake Optimizer [13] capture hunting dynamics. Others derive from insect colonies or swarm intelligence, including Firefly Algorithm [14], Glowworm Swarm Optimization (GSO) [15], and Butterfly Optimization [16]. Likewise, bacterial or microbial behaviors inspire algorithms such as Bacterial Foraging Optimization (BFO) [17], Virus Colony Search [18], and COVIDOA [19]. Some algorithms are motivated by botanical and plant behavior, such as the Plant Propagation Algorithm (PPA) [20], Invasive Weed Optimization (IWO) [21], and Root Growth Optimizer [22]. Other methods

emerge from natural physical phenomena, including Gravitational Search Algorithm (GSA) [23], Simulated Annealing [24], and the Harmony Search algorithm [25]. More recently, complex hybrid and bio-inspired models such as Gorilla Troops Optimization (GTO) [26], Reptile Search Algorithm (RSA) [27], Sine Cosine Algorithm (SCA) [28], and Slime Mould Algorithm (SMA) [29] have been introduced. Despite the thematic diversity and creativity of modern bio-inspired metaheuristic techniques, many of them continue to face common shortcomings, such as the lack of truly adaptive dynamics, a static and rigid balance between exploration and exploitation, and the absence of documented convergence guarantees [30]. These limitations underline the need for next-generation algorithms capable of self-regulating their behavior according to the state of the search, maintaining stability in convergence, and faithfully reflecting the principles and rhythms of complex biological processes.

BioHealing Optimization (BHO) is positioned within this scientific and technological context, drawing inspiration from the regenerative process of wound healing in living organisms. Wound healing is a natural function characterized by a delicate balance between disruption and restoration, aimed at re-establishing homeostasis. BHO translates this biological principle into the optimization domain, creating a multi-phase methodology in which each phase has a distinct yet interdependent role.

- Injury phase: Rather than relying on static or simplistic modifications, BHO applies stochastic disturbances to selected dimensions of candidate solutions, emulating the initial, uncontrolled nature of biological injury. These disturbances may follow distributions that favor either gentler changes or rare, high-impact shifts, with their intensity dynamically adapted as the search progresses encouraging broad exploration in the early stages and gradually reducing disruption near convergence.
- 2. Healing phase: Subsequently, BHO selectively guides the modified dimensions toward the best-known solution, in a process that mirrors the progressive restoration of biological tissues. This movement is neither mechanical nor fixed; the proportion and direction of adjustments are adapted to the search conditions, maintaining diversity while also enhancing the exploitation of high-quality solutions.
- 3. **Recombination phase**: Optionally, this process is preceded by an information exchange mechanism inspired by Differential Evolution, where components of the best solution are combined with differences from other members of the population. This allows the inheritance of strong traits while simultaneously introducing variations that keep the search active.

Previous approaches inspired by healing processes, such as Wound Healing Based Optimization (WHO) [31] and the Synergistic Fibroblast Optimization (SFO) [32], , while interesting, implement more macroscopic models or focus primarily on biological analogies without a clear separation between exploration and exploitation. They also do not employ adaptive stochastic perturbations or integrate evolutionary recombination mechanisms.

In contrast, BHO combines stochastic disruption, guided restoration, and evolutionary recombination into a single, flexible architecture that transitions smoothly and self-regulates from exploration to exploitation. It further incorporates innovations such as dynamic adjustment of injury and healing probabilities and intensities, a "scar mapping" system that retains memory of improvement directions, focus on critical dimensions, and the introduction of high-intensity disturbance phases to overcome stagnation. Together, these elements form a methodological proposal that is fundamentally distinct from existing approaches and offers enhanced robustness and performance in demanding, high-dimensional optimization problems.

The rest of the paper is organized as follows:

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Section 2.4 presents the biological inspiration and motivation behind the proposed method. Section 2 details the mathematical formulation and step-by-step pseudocode of the BioHealingOptimizer. Section 3 describes the experimental setup, benchmark functions, and implementation details. Section 3.2 reports and analyzes the experimental results, including comparative performance and statistical evaluations. Section 4 provides the conclusions of the study, and Section 5 outlines directions for future research and potential extensions of the method.

2. The BioHealing Optimizer algorithm

2.1. The basic body of the BioHealing Optimizer

The overall algorithm of the method follows:

Algorithm 1 The basic body of the BioHealing Optimizer pseudocode

```
f: objective function to minimize
   dim: problem dimensionality
   NP: population size
   iter<sub>max</sub>: maximum number of iterations
   FE_{max}: maximum number of iterations
  lower, upper: bounds for each variable
Params:
   ws_0: initial wound intensity
   wp: probability of wounding per dimension
  hr: probability of healing per dimension
   rp: probability of recombination with the best solution
   \vec{F}: differential weight scaling factor in recombination
   CR: crossover probability in recombination
   LSR: local search rate
Output:
   x_{best}: the best solution found
   f_{best}: the value of f at best solution
Initialization:
01 for i=1..NP:
02
        for i=1..dim:
03
             x_{i,j} U(lower_j, upper_j)
        fit_i = f(x_i)
05 x_{best}, f_{best} = \operatorname{argmin}(fit_i)
06 iter = 0
Main loop:
07 while iter < iter_{max} or FE < FE_{max}:
08
        iter = iter + 1
09
        elite = argmin(fit_i)
10
        x_{best} = x_{elite}, fbest = fit_{elite}
        ws = \max(0.05 \cdot ws_0, ws_0 \cdot (1 - \frac{iter}{iter_{max}}))
11
12
        for i=1..NP:
             if i == elite: continue
13
14
             x_{old} = x_i, f_{old} = fit_i
15
             if U(0,1) < rp:
                  choose r_1 \neq i, r_2 \neq i, r_2 \neq r_1
16
17
                  j_r = \text{randInt}(1,dim)
18
                  for j=1..dim:
                       if U(0,1) < CR or j = j_r:
19
20
                            v = x_{best,i} + F \cdot (x_{r1,i} - x_{r2,i})
                            x_{i,j} = \text{clamp}(v, lower_i, upper_i)
21
22
             for j=1..dim:
23
                  if U(0,1) < wp:
                       \xi = stochasticStep() // N(0,1) or Lévy
24
25
                       d = ws \cdot \xi \cdot (upper_i - lower_i)
26
                       x_{i,j} = \text{clamp}(x_{i,j} + d, lower_j, upper_j)
             a = \text{healStep}(hr)
27
28
             for j=1..dim:
29
                  if U(0,1) < hr:
30
                        x_{i,j} = \text{clamp}(x_{i,j} + a(x_{best_i} - x_{i,j}), lower_j, upper_j)
31
             f_{new} = \mathbf{f}(x_i)
32
             if f_{new} < f_{old}:
                  fit_i = f_{new}
33
                 if f_{new} < f_{best}:
34
35
                      f_{best} = f_{new} , x_{best} = x_i
36
37
                       x_i = x_{old}; fit_i = f_{old}
38
        if LSR > 0:
             for i=1..NP:
39
40
                  if i = elite: continue
41
                  if U(0,1) < LSR:
42
                       x_{old} = x_i, \, f_{old} = fit_i
43
                       x_i = localSearch(x_i)
44
                       f_{new} = f(x_i)
45
                       if f_{new} < f_{old}:
                            fit_i = f_{new}
46
47
                            if f_{new} < f_{best}:
48
                                 f_{best} = f_{new}; x_{best} = x_i
49
                       else:
50
                            x_i = x_{old}, fit_i = f_{old}
51 return x_{best}, f_{best}
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Algorithm 2 zzz

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Input: changed_{dims}: Which dimensions changed, towardBest_j \in (0,1), signDir_j \in (-1,+1) Params: scarLR, scar_{pmin}, scar_{pmax}, scar_{pmin}, scar_{pmax}, mom_{decay}, bandage_{len} State: woundPdim_j, woundSdim_j, scarMomentum_j, bandage_i, j, dimScore_j 01 for each j in changed_{dims}: 02 gP = scarLR \cdot (0.5 + 0.5 \cdot towardBest_j) 03 gS = scarLR \cdot (0.25 + 0.75 \cdot towardBest_j) 04 woundPdim_j = clamp(woundPdim_j + gP, scar_{pmin}, scar_{pmax}) 05 woundSdim_j = clamp(woundSdim_j + gS, scar_{smin}, scar_{smax}) 06 scarMomentum_j = (1 - mom_{decay}) \cdot scarMomentum_j + mom_{decay} \cdot signDir_j 07 dimScore_j = dimScore_j + improvement_signal() // e.g. | f_old - f_new | 08 if bandage_{len} > 0: bandage_{len} = bandage
```

The core loop of the BHO maintains a population of candidate solutions within box constraints and repeatedly balances broad exploration with guided exploitation. It begins by sampling each vector uniformly within the per-dimension bounds, evaluating all candidates, and designating the incumbent best. At every iteration, the current elite is identified and the wound intensity follows a monotone decay schedule so that early updates encourage wide exploration while later ones stabilize around promising regions. For each non-elite individual, an optional Differential Evolution recombination (best/1, bin) may combine the incumbent best with a scaled difference of two distinct peers; all values are kept feasible through clamping to the bounds. The injury phase then applies a per-dimension stochastic disturbance with a specified probability, using either Gaussian noise or a Lévy-tailed step produced by a generic stochasticStep() procedure and scaled by the current wound intensity and the variable range, feasibility is again enforced by clamping. The healing phase gently attracts modified components toward the incumbent best with a specified probability, using a step a = healStep(hr) that increases with the healing rate and preserves bounds. The resulting trial is evaluated and accepted greedily only if it improves the previous fitness; whenever an improvement is accepted, the global best is also updated. Optionally, a lightweight local search may refine non-elite individuals with some probability, under the same greedy acceptance rule. The procedure terminates upon exhausting either the iteration budget or the cap on function evaluations, and returns the pair (x_{best} , f_{best}). This description captures the clean, modular backbone of BHO elite selection, optional recombination, injury, healing, and greedy replacement—while allowing optional extensions to be integrated without altering the fundamental methodology.

2.2. Mechanism A: Scar Map, Momentum & Bandag

After each successful acceptance (when the new solution improves the previous one), Mechanism A updates, per dimension, a "scar map" that stores two quantities: the future probability of wounding and its intensity. The update follows the learning rate (scarLR) and is clamped within $scar_{pmin}/scar_{pmax}$ and $scar_{smin}/scar_{smax}$. When the accepted change moved toward the current best (towardBest_j), the adjustment is strengthened so that dimensions that contributed to progress are wounded more often and more purposefully later. In parallel, the momentum term ($scarMomentum_j$) keeps a decayed running sign of recent accepted moves ($signDir_j$) using mom_decay, allowing the next stochastic step to lean slightly toward the beneficial direction. The dimension score ($dimScore_j$) rises proportionally to the achieved improvement and later feeds the selection of "hot" dimensions. Finally, $bandage_{len}$ freezes just-improved dimensions for a few iterations, protecting the gain from immediate over-disturbance.

Integration with the core loop is straightforward: Mechanism A runs right after greedy acceptance, only when $f_{new} < f_{old}$. In subsequent cycles, the injury phase no longer uses a

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Algorithm 3 zzz

```
Params: hot_k, hot_boost_p, hot_boost_s, dim_decay  
State : dim_score[j]  
TopK:  
01 idx = argsort(dim_score, descending)  
02 hot = idx[1..min(hot_k, dim)]  
Decay (per-iter):  
03 for j=1..dim: dim_score[j] = (1 - \text{dim}_d\text{ecay}) * \text{dim}_s\text{core}[j]  
In Injury (per j):  
04 p_base = (scar_enabled ? clamp(wound_p_dim[j], scar_pmin, scar_pmax) : wp)  
05 scale = (scar_enabled ? clamp(wound_s_dim[j], scar_smin, scar_smax) : 1)  
06 if j \in \text{hot}: p_base = boostProb(p_base, hot_boost_p)  
07 if j \in \text{hot}: scale = scale * hot_boost_s
```

single wp but reads the per-dimension $woundPdim_j$ and $woundSdim_j$ and, where applicable, blends the random disturbance with momentum. The healing phase remains unchanged, while the bandage temporarily prevents new wounds on freshly improved dimensions. In this way, the core stays clean, and the auxiliary structures self-regulate the rate and targeting of exploration on a per-dimension basis.

```
2.3. Hot-Dims Focus (top-K & boosts for injury)
2.4. the bio
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3. Experimental setup and benchmark results

This section first introduces the benchmark functions selected for experimental evaluation, followed by a comprehensive analysis of the conducted experiments. The study systematically examines the various parameters of the proposed algorithm to assess its reliability and effectiveness in different optimization scenarios. The complete parameter configurations used throughout these experiments are documented in Table 1.

Table 1. Parameters and settings

PARAMETER	VALUE	DESCRIPTION	
NP	100	Population for all methods except CMA-ES	
NP_{CMA-ES}	$4 + \lfloor 3 \cdot \log(dim) \rfloor$	Population of CMA-ES	
iter _{max}	300	Maximum number of iterations for all methods	
FE_{max}	150,000	Maximum number of function evaluations for all methods	
SR	$\delta_{sim}^{(iter)} = \begin{vmatrix} f_{sim,min}^{(iter)} - f_{sim,min}^{(iter-1)} \end{vmatrix} [34-36]$ or $iter_{max}$ or FE_{max}	Stopping rule for all methods	
LSR	0	Local search rate for all methods	
ws_0	0.4	Initial wound strength (injury intensity) for BHO	
wp	0.3	Probability of wounding per dimension for BHO	
HR	0.2	Probability of healing per dimension for BHO	
rp	0.9	Probability of recombination with the best solution for BHO	
F	0.5	Differential weight scaling factor (recombination) for BHO	
CR	0.9	Crossover probability (recombination) for BHO	
T_s	Tourament size 8 [37]	Selection of GA	
C_{rate}	double, 0.1 (10%) (classic values)	Crossover for GA	
M_{rate}	double, 0.05 (5%) (classic values)	Mutation for GA	
c_1, c_2	1.494	Cognitive and Social coefficient for LCPSO	
w	0,729	Inertia for LCPSO	
F	0.5	Initial scaling factor for SaDE	
CR	0.5	Initial crossover rate for SaDE	

3.1. Test Functions

The performance assessment of the proposed method was carried out using a comprehensive and diverse collection of well-established benchmark functions [38–40], as listed in Table 2. These test functions represent a standard suite commonly utilized in the global optimization literature for validating and comparing metaheuristic algorithms. Each function exhibits distinct characteristics in terms of modality, separability, dimensionality, and landscape complexity, thus providing a robust basis for evaluating the generalization capability of the algorithm. Notably, the functions were employed in their original, unaltered form no additional transformations such as shifting, rotation, or scaling were applied allowing for a transparent and reproducible comparison with prior studies.

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Table 2. The benchmark functions used in the conducted experiments

PROBLEM	FORMULA	Dim	BOUNDS
Parameter Estimation for Frequency-Modulated Sound Waves	$\min_{x \in [-6.4, 6.35]^6} f(x) = \frac{1}{N} \sum_{n=1}^{N} y(n; x) - y_{\text{target}}(n) ^2$ $y(n; x) = x_0 \sin(x_1 n + x_2 \sin(x_3 n + x_4 \sin(x_5 n)))$	6	$x_i \in [-6.4, 6.35]$
Lennard-Jones Potential	$\min_{x \in \mathbb{R}^{3N-6}} f(x) = 4\sum_{i=1}^{N-1} \sum_{j=i+1}^{N} \left[\left(\frac{1}{r_{ij}} \right)^{12} - \left(\frac{1}{r_{ij}} \right)^{6} \right]$	30	$x_0 \in (0,0,0)$ $x_1, x_2 \in [0,4]$ $x_3 \in [0,\pi]$ x_{3k-3} x_{3k-2} $x_i \in [-b_k, +b_k]$
Bifunctional Catalyst	$\frac{dx_1}{dt} = -k_1 x_1, \frac{dx_2}{dt} = k_1 x_1 - k_2 x_2 + k_3 x_2 + k_4 x_3,$	1	$u \in [0.6, 0.9]$
Blend Optimal	$\frac{dx_3}{dt} = k_2 x_2, \frac{dx_4}{dt} = -k_4 x_4 + k_5 x_5,$		
Control	$\frac{dx_5}{dt} = -k_3x_2 + k_6x_4 - k_5x_5 + k_7x_6 + k_8x_7 + k_9x_5 + k_{10}x_7$		
	$\frac{dx_6}{dt} = k_8 x_5 - k_7 x_6, \frac{dx_7}{dt} = k_9 x_5 - k_{10} x_7$ $k_2(u) = c_{10} + c_{10} u + c_{10} u + c_{10} u^2 + c_{10} u^3$		
Optimal	$k_i(u) = c_{i1} + c_{i2}u + c_{i3}u^2 + c_{i4}u^3$ $J(u) = \int_0^{0.72} x_1(t)^2 + x_2(t)^2 + 0.1u^2 dt$	1	$u \in [0, 5]$
Control of a Non-Linear	$\frac{dx_1}{dt} = -2x_1 + x_2 + 1.25u + 0.5 \exp\left(\frac{x_1}{x_1 + 2}\right)$		
Stirred			
Tank Reactor	$\frac{dx_2}{dt} = -x_2 + 0.5 \exp\left(\frac{x_1}{x_1 + 2}\right)$		
Tersoff	$x_1(0) = 0.9, x_2(0) = 0.09, t \in [0, 0.72]$ $\min_{\mathbf{x} \in \Omega} f(\mathbf{x}) = \sum_{i=1}^{N} E(\mathbf{x}_i)$	30	$x_1 \in [0,4]$
Potential for model Si (B)	$E(\mathbf{x}_i) = \frac{1}{2} \sum_{j \neq i} f_C(r_{ij}) \left[V_R(r_{ij}) - B_{ij} V_A(r_{ij}) \right]$		$x_1 \in [0, 4]$ $x_2 \in [0, 4]$ $x_3 \in [0, \pi]$
Tot model St (b)	where $r_{ij} = \ \mathbf{x}_i - \mathbf{x}_j\ $, $V_R(r) = A \exp(-\lambda_1 r)$		$x_i \in \left[\frac{4(i-3)}{4}, 4\right]$
	$V_A(r) = B \exp(-\lambda_2 r)$ $f_C(r)$: cutoff function with $f_C(r)$: angle parameter		4,4
Tersoff	$\min_{\mathbf{x}} V(\mathbf{x}) = \sum_{i=1}^{N} \sum_{i>j}^{N} f_C(r_{ij}) \left[a_{ij} f_R(r_{ij}) + b_{ij} f_A(r_{ij}) \right]$	30	$x_1 \in [0, 4]$
Potential for model Si (C)	r < R - D		$x_1 \in [0,4] \\ x_2 \in [0,4] \\ x_3 \in [0,\pi] \\ x_i \in \left[\frac{4(i-3)}{4}, 4\right]$
	$f_{C}(r) = \begin{cases} \frac{1}{2} + \frac{1}{2}\cos\left(\frac{\pi(r-R+D)}{2D}\right), & r-R \le D \end{cases}$		$x_i \in \left[\frac{4(i-3)}{4}, 4\right]$
	$f_C(r) = \begin{cases} 1, & r < R - D \\ \frac{1}{2} + \frac{1}{2}\cos\left(\frac{\pi(r - R + D)}{2D}\right), & r - R \le D \\ 0, & r > R + D \end{cases}$ $f_R(r) = A\exp(-\lambda_1 r)$		
	$\begin{split} f_R(r) &= A \exp(-\lambda_1 r) \\ f_A(r) &= -B \exp(-\lambda_2 r) \\ b_{ij} &= \left[1 + (\beta^H) \xi_{ij}^H\right]^{-1/(2n)} \end{split}$		
	$h_{i:} = \left[1 + (\beta^n)^{n}\right]^{-1/(2n)}$		
Spread	$\frac{\sum_{k \neq i, j} f_{C}(r_{ik}) g(\theta_{ijk}) \exp \left[\lambda_{3}^{3} (r_{ij} - r_{ik})^{3} \right]}{\min_{x \in X} f(x) = \max \{ \varphi_{1}(x) , \varphi_{2}(x) , \dots, \varphi_{m}(x) \}}$	20	$x_i \in [0, 2\pi]$
Spectrum Radar Polly phase	$X = \{x \in \mathbb{R}^n \mid 0 \le x_j \le 2\pi, \ j = 1, \dots, n\} m = 2n - 1$,
Code Design	$\begin{cases} n-j \\ \sum_{i=1}^{n} \cos(x_k - x_{k+1}) & \text{for } j = 1, \dots, n-1 \end{cases}$		
	$\varphi_{j}(x) = \begin{cases} \sum_{k=1}^{n-j} \cos(x_{k} - x_{k+j}) & \text{for } j = 1, \dots, n-1 \\ n & \text{for } j = n \\ \rho & \text{for } j = n + 1, \dots, 2n-1 \end{cases}$		
	$\varphi_{2n-j}(x) \qquad \text{for } j=n+1,\ldots,2n-1$		
	$\varphi_j(x) = \sum_{k=1}^{n-j} \cos(x_k - x_{k+j}), j = 1, \dots, n-1$		
Transmission	$\varphi_{n}(x) = n, \varphi_{n+\ell}(x) = \varphi_{n-\ell}(x), \ell = 1,, n-1$ $\min \sum_{l \in O} c_{l} n_{l} + W_{1} \sum_{l \in O} f_{l} - \tilde{f}_{l} + W_{2} \sum_{l \in O} \max(0, n_{l} - \tilde{n}_{l})$	7	$0 \le n_i \le \bar{n}_l$
Network Expansion	$Sf = g - d$ $f_l = \gamma_l \eta_l \Delta \theta_l, \forall l \in \Omega$		$n_i\in\mathbb{Z}$
Planning	$ f_l \le f_l n_l, \forall l \in \Omega$		
	$\begin{split} \varphi_{j}(x) &= \sum_{k=1}^{N} \cos(3k - \frac{x_{k+j}}{k}), j = 1, \dots, n-1 \\ \varphi_{n}(x) &= n, \varphi_{n+\ell}(x) = \varphi_{n-\ell}(x), \ell = 1, \dots, n-1 \\ \min \sum_{l \in \Omega} c_{l}n_{l} + W_{1} \sum_{l \in \Omega} [f_{l} - f_{l}] + W_{2} \sum_{l \in \Omega} \max(0, n_{l} - \bar{n}_{l}) \\ S_{j}^{f} &= g - d \\ f_{l} &= \gamma_{l}n_{l}\Delta\theta_{l}, \forall l \in \Omega \\ f_{l} &\leq f_{l}n_{l}, \forall l \in \Omega \\ 0 &\leq n_{l} \leq \bar{n}_{l}, n_{l} \in \mathbb{Z}, \forall l \in \Omega \\ \min_{x} &= f(x) = \sum_{l=1}^{N_{g}} \left(\frac{c_{l}^{gen}}{p_{k}^{gen}} - R_{l}^{gen}\right)^{2} + \sum_{j=1}^{N_{d}} \left(\frac{c_{l}^{joad}}{p_{j}^{joad}} - R_{l}^{joad}\right)^{2} \end{split}$		
Electricity Transmission	$\min_{x} f(x) = \sum_{i=1}^{Ng} \left(\frac{c_i}{p_i^{gen}} - R_i^{gen} \right) + \sum_{j=1}^{Nd} \left(\frac{c_j}{p_j^{load}} - R_j^{load} \right)$	126	$GD_{i,j} \in [0, GD_{i,j}^{max}]$
Pricing	$\sum_{i} GD_{i,i} + \sum_{i} BT_{i,i} = P_{i}^{gen}, \forall i$		
	$\sum_{i} GD_{i,j} + \sum_{i} BT_{i,j} = P_{j}^{load}, \forall j$		
	$GD_{i,j}^{max} = \min(P_i^{gen} - BT_{i,j}, P_j^{load} - BT_{i,j})$ $\min_{T_1, \dots, T_6, \varphi_1, \dots, \varphi_6} f(x) = \max_{\theta \in \Omega} AF(x, \theta)$		
Circular	$\min_{r_1,\dots,r_6,\varphi_1,\dots,\varphi_6} f(\mathbf{x}) = \max_{\theta \in \Omega} AF(\mathbf{x},\theta)$	12	$r_k \in [0.2, 1]$ $\varphi_k \in [-180, 180]$
Antenna Array	$AF(\mathbf{x}, \theta) = \left \sum_{k=1}^{6} \exp \left(j \left[2\pi r_k \cos(\theta - \theta_k) + \varphi_k \frac{\pi}{180} \right] \right) \right $		$\psi_k \in [-100, 180]$
Design Dynamic	$\min_{\mathbf{P}} f(\mathbf{P}) = \sum_{t=1}^{24} \sum_{i=1}^{5} (a_i P_{i,t}^2 + b_i P_{i,t} + c_i)$	120	$P_i^{\min} \leq P_{i,t} \leq P_i^{\min}$
Economic	$P_i^{\min} \le P_{i,t} \le P_i^{\max}, \forall i = 1,, 5, \ t = 1,, 24$		1 1,1 - 1
Disnatch 1	∇^{5} , $P_{t,t} = D_{t,t}$, $\forall t = 1, \dots, 24$		
Dispatch 1	1-1 1,7		
Dispatch 1	$P_{\text{min}} = [10, 20, 30, 40, 50]$ $P_{\text{max}} = [75, 125, 175, 250, 300]$		
Dynamic	$\begin{split} P_{\min} &= [10, 20, 30, 40, 50] \\ P_{\max} &= [75, 125, 175, 250, 300] \\ \min_{\mathbf{P}} & f(\mathbf{P}) &= \sum_{t=1}^{24} \sum_{i=1}^{9} a_i P_{i,t}^2 + b_i P_{i,t} + c_i \end{split}$	216	$P_i^{\min} \le P_{i,t} \le P_i^{\max}$
-	$\begin{split} P_{\min} &= [10, 20, 30, 40, 50] \\ P_{\max} &= [75, 125, 175, 250, 300] \\ \text{minp} & f(\mathbf{P}) = \sum_{t=1}^{24} \sum_{i=1}^{9} \left(a_i P_{i,t}^2 + b_i P_{i,t} + c_i\right) \\ P_i^{\min} &\leq P_{i,t} \leq P_i^{\max}, \forall i = 1, \dots, 5, \ t = 1, \dots, 24 \end{split}$	216	$P_i^{\min} \le P_{i,t} \le P_i^{\max}$
Dynamic Economic	$\begin{split} & \stackrel{\stackrel{\frown}{P}_{\min}}{P_{\max}} = [10, 20, 30, 40, 50] \\ & P_{\max} = [75, 125, 175, 250, 300] \\ & \min_{\mathbf{P}} f(\mathbf{P}) = \sum_{t=1}^{24} \sum_{t=1}^{9} \left(a_i P_{i,t}^2 + b_i P_{i,t} + c_i \right) \\ & P_i^{\min} \leq P_{i,t} \leq P_i^{\max}, \forall i = 1, \dots, 5, \ t = 1, \dots, 24 \\ & \sum_{t=1}^{5} P_{i,t} = D_{t}, \forall t = 1, \dots, 24 \end{split}$	216	$P_i^{\min} \le P_{i,t} \le P_i^{\min}$
Dynamic Economic	$\begin{split} & \stackrel{\cdot P_{\min}}{P_{\max}} = [10, 20, 30, 40, 50] \\ & P_{\max} = [75, 125, 175, 250, 300] \\ & \min_{t} p f(\mathbf{P}) = \sum_{t=1}^{24} \sum_{t=1}^{9} \left(a_{t} P_{t,t}^{2} + b_{t} P_{t,t} + c_{t} \right) \\ & P_{t}^{\min} \leq P_{t,t} \leq P_{\max}^{\max}, \forall t = 1, \dots, 5, \ t = 1, \dots, 24 \\ & \sum_{t=1}^{5} P_{t,t} = D_{t}, \forall t = 1, \dots, 24 \\ & P_{\min} = [150, 135, 73, 60, 73, 57, 20, 47, 20] \\ & P_{\max} = [470, 40, 344, 300, 234, 160, 120, 90] \end{split}$	216	$P_i^{\min} \le P_{i,t} \le P_i^{\max}$
Dynamic Economic Dispatch 2	$\begin{split} & \stackrel{\stackrel{\frown}{P}_{\min}}{P_{\max}} = [10, 20, 30, 40, 50] \\ & P_{\max} = [75, 125, 175, 250, 300] \\ & \min_{\mathbf{P}} f(\mathbf{P}) = \sum_{t=1}^{24} \sum_{t=1}^{9} \left(a_i P_{i,t}^2 + b_i P_{i,t} + c_i \right) \\ & P_i^{\min} \leq P_{i,t} \leq P_i^{\max}, \forall i = 1, \dots, 5, \ t = 1, \dots, 24 \\ & \sum_{t=1}^{5} P_{i,t} = D_{t}, \forall t = 1, \dots, 24 \end{split}$	6	See
Dynamic Economic Dispatch 2 Static Economic Load	$\begin{split} & \stackrel{\stackrel{\frown}{P_{\min}}}{P_{\max}} = [10, 20, 30, 40, 50] \\ & P_{\max} = [75, 125, 175, 250, 300] \\ & \min_{P} f(P) = \sum_{t=1}^{24} \sum_{i=1}^{9} \left(a_i P_{i,t}^2 + b_i P_{i,t} + c_i\right) \\ & P_i^{\min} \leq P_{i,t} \leq P_i^{\max}, \forall i = 1, \dots, 5, \ t = 1, \dots, 24 \\ & \sum_{i=1}^{5} P_{i,t} = D_t, \forall t = 1, \dots, 24 \\ & P_{\min} = [150, 135, 73, 60, 73, 57, 20, 47, 20] \\ & P_{\max} = [470, 460, 340, 300, 243, 160, 130, 120, 80] \\ & \min_{P_1, \dots, P_{N_G}} F = \sum_{i=1}^{N_G} f_i(P_i) \\ & f_i(P_i) = a_i P_i^2 + b_i P_i + c_i, i = 1, 2, \dots, N_G \end{split}$	6 13 15	Technical Report
Dynamic Economic Dispatch 2 Static Economic	$\begin{split} & \stackrel{\cdot P_{\min}}{P_{\max}} = [1, 20, 30, 40, 50] \\ & P_{\max} = [75, 125, 175, 250, 300] \\ & \min_{P} f(P) = \sum_{t=1}^{2d} \sum_{t=1}^{q} \left(a_{t} P_{t,t}^{2} + b_{t} P_{t,t} + c_{t} \right) \\ & P_{t}^{\min} \leq P_{t,t} \leq P_{t}^{\max} \times \forall t = 1, \dots, 5, \ t = 1, \dots, 24 \\ & \sum_{i=1}^{5} P_{t,t} = D_{t}, \forall t = 1, \dots, 24 \\ & P_{\min} = [150, 135, 73, 60, 73, 57, 20, 47, 20] \\ & P_{\max} = [470, 460, 340, 300, 243, 160, 130, 120, 80] \\ & \min_{P_{1}, \dots, P_{N_{G}}} F = \sum_{t=1}^{N_{G}} f_{t}(P_{t}) \\ & f_{t}(P_{t}) = a_{t} P_{t}^{2} + b_{t} P_{t} + c_{t}, i = 1, 2, \dots, N_{G} \\ & f_{t}(P_{t}) = a_{t} P_{t}^{2} + b_{t} P_{t} + c_{t} + le_{t} \sin(f_{t}(P_{t}^{\min} - P_{t}))] \end{split}$	6 13	See Technical
Dynamic Economic Dispatch 2 Static Economic Load Dispatch	$\begin{split} & \stackrel{\cdot P_{\min}}{P_{\min}} = [1, 20, 30, 40, 50] \\ & P_{\max} = [75, 125, 175, 250, 300] \\ & \min_{P} f(P) = \sum_{t=1}^{2d} \sum_{t=1}^{q} \left[a_{t} P_{t,t}^{2} + b_{t} P_{t,t} + c_{t} \right] \\ & P_{t}^{\min} \leq P_{t,t} \leq P_{\max}^{\max}, \forall t = 1, \dots, 5, \ t = 1, \dots, 24 \\ & \sum_{i=1}^{5} P_{t,t} = D_{t}, \forall t = 1, \dots, 24 \\ & P_{\min} = [150, 135, 73, 60, 73, 57, 20, 47, 20] \\ & P_{\max} = [470, 460, 340, 300, 243, 160, 130, 120, 80] \\ & \min_{P_{1}, \dots, P_{N_{G}}} F = \sum_{t=1}^{N_{G}} f_{t}(P_{t}) \\ & f_{t}(P_{t}) = a_{t} P_{t}^{2} + b_{t} P_{t} + c_{t}, i = 1, 2, \dots, N_{G} \\ & f_{t}(P_{t}) = a_{t} P_{t}^{2} + b_{t} P_{t} + c_{t} + c_{t} \sin f_{t}(P_{t}^{\min} - P_{t})) \\ & P_{t}^{\min} \leq P_{t} \leq P_{t}^{\max}, i = 1, 2, \dots, N_{G} \end{split}$	6 13 15 40	See Technical Report of
Dynamic Economic Dispatch 2 Static Economic Load Dispatch	$\begin{split} & \stackrel{\cdot P_{\min}}{P_{\max}} = [1, 20, 30, 40, 50] \\ & P_{\max} = [75, 125, 175, 250, 300] \\ & \min_{P} f(P) = \sum_{t=1}^{2d} \sum_{t=1}^{q} \left(a_{t} P_{t,t}^{2} + b_{t} P_{t,t} + c_{t} \right) \\ & P_{t}^{\min} \leq P_{t,t} \leq P_{t}^{\max} \times \forall t = 1, \dots, 5, \ t = 1, \dots, 24 \\ & \sum_{i=1}^{5} P_{t,t} = D_{t}, \forall t = 1, \dots, 24 \\ & P_{\min} = [150, 135, 73, 60, 73, 57, 20, 47, 20] \\ & P_{\max} = [470, 460, 340, 300, 243, 160, 130, 120, 80] \\ & \min_{P_{1}, \dots, P_{N_{G}}} F = \sum_{t=1}^{N_{G}} f_{t}(P_{t}) \\ & f_{t}(P_{t}) = a_{t} P_{t}^{2} + b_{t} P_{t} + c_{t}, i = 1, 2, \dots, N_{G} \\ & f_{t}(P_{t}) = a_{t} P_{t}^{2} + b_{t} P_{t} + c_{t} + le_{t} \sin(f_{t}(P_{t}^{\min} - P_{t}))] \end{split}$	6 13 15 40	See Technical Report of

3.2. Experimental results

All experimental procedures were executed on a high-performance computational infrastructure equipped with an AMD Ryzen 9 5950X CPU (16 cores, 32 threads) and 128 GB of DDR4 RAM, running under a Debian Linux environment. The evaluation protocol

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was designed to ensure statistical rigor and reproducibility. Specifically, each benchmark function was subjected to 30 independent runs, with each trial initialized using distinct random seeds to account for stochastic variability in the algorithm's behavior.

The BioHealingOptimizer and all comparative methods were implemented in highly optimized ANSI C++ code, integrated into the GLOBALOPTIMUS optimization framework [44], which is an open-source software environment for metaheuristic experimentation. The source code is publicly available at https://github.com/itsoulos/GLOBALOPTIMUS (accessed August 1, 2025), promoting transparency and reproducibility in research.

All algorithmic parameters, including those of competing methods, are comprehensively outlined in Table 1. The primary performance metric reported is the average number of objective function evaluations (NFEs) computed over the 30 runs for each test function. Additionally, success rates defined as the percentage of runs in which the global optimum was successfully located are included in parentheses next to the corresponding mean values. In cases where all runs achieved optimal convergence, the success rate indicator is omitted for clarity. Within the result tables, best-performing entries (i.e., those requiring the fewest function evaluations) are visually highlighted in green to facilitate comparison.

4. Conclusions

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5. Future Research Directions

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Author Contributions: V.C. implemented the methodology, I.G.T. and V.C conducted the experiments, employing all optimization methods and problems and provided the comparative experiments. I.G.T. and V.C performed the statistical analysis and prepared the manuscript. All authors have read and agreed to the published version of the manuscript.

Funding: This research received no external funding.

Institutional Review Board Statement: Not Applicable.

Informed Consent Statement: Not applicable.

Acknowledgments: This research has been financed by the European Union: Next Generation EU through the Program Greece 2.0 National Recovery and Resilience Plan, under the call RESEARCH–CREATE–INNOVATE, project name "iCREW: Intelligent small craft simulator for advanced crew training using Virtual Reality techniques" (project code: TAEDK-06195).

Conflicts of Interest: The authors declare no conflicts of interest.

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