

# Predicting the damage of urban fires with Grammatical Evolution.

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**Abstract:** Fire, whether wild or urban, depends on the triad of oxygen, fuel, and heat. Urban fires, though smaller in scale, have devastating impacts, as evidenced by the 2018 wildfire in Mati, Attica (Greece), which claimed 104 lives. The elderly and children are the most vulnerable due to mobility and cognitive limitations. This study applies Grammatical Evolution (GE), a machine learning method that generates interpretable classification rules to predict the consequences of urban fires. Using historical data (casualties, containment time, meteorological/demographic parameters), GE produces classification rules in human readable form. The rules achieve over 85% accuracy, revealing critical correlations. For example, high temperatures ( $>35^{\circ}\text{C}$ ) combined with irregular building layouts exponentially increase fatality risks, while firefighter response time proves more critical than fire intensity itself. Applications include dynamic evacuation strategies (real-time adaptation), preventive urban planning (fire-resistant materials, green buffer zones), and targeted awareness campaigns for at-risk groups. Unlike "black-box" machine learning techniques, GE offers transparent, human-readable rules, enabling firefighters and authorities to make rapid, informed decisions. Future advancements could integrate real-time data (IoT sensors, satellites) and extend the methodology to other natural disasters. Protecting urban centers from fires is not only a technological challenge but also a moral imperative to safeguard human lives and societal cohesion.

**Keywords:** Urban fires; Machine learning; Neural networks; Genetic Programming; Grammatical Evolution.

Received:

Revised:

Accepted:

Published:

**Citation:** Kopitsa, C.; Tsoulos, I.G.; Miliadous, A.; Charilogis, V.

Predicting the damage of urban fires with Grammatical Evolution. *Journal Not Specified* **2025**, *1*, 0.

<https://doi.org/>

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Submitted to *Journal Not Specified* for possible open access publication under the terms and conditions of the

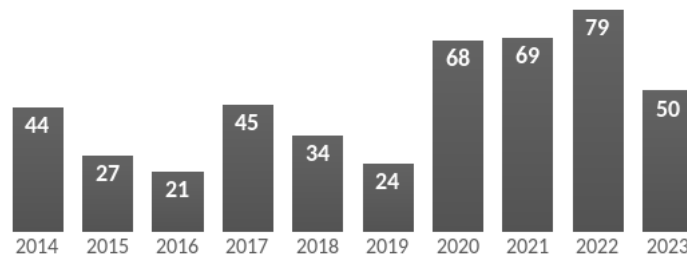
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## 1. Introduction

Whereas, fires can be triggered by various causes significant fires are frequently outcome from the following disasters: storms, transportation accidents, criminal activity / terrorism, droughts, hazardous materials spills [1] and forest fires. Also, Urban fires are predominantly attributed to negligent cooking practices, whereas rural fires often stem from faulty electrical installations, malfunctions in heating systems, or even natural causes such as lightning strikes [2]. Small scale urban fires often do not have a significant impact on an area, nevertheless on the other hand they still are equally hazardous to human life, in the socio-economic stability of a community, or even they contribute to increased insurance premiums [1].

Referring to human lives, let us examine the numerical data provided by the Hellenic Fire Service, which is available as open data in accordance with the European Union Directive (2013/37/EE) aimed at enhancing transparency [3]. Consequently, as presented

in Figure 1, an increase in fatalities associated with urban fires, has been observed since 2020, with a slight decline in this trend, in 2023.



**Figure 1.** A graph presenting the deaths from fires in Greece for a period from 2014 to 2023.

Beyond this, it is observed that in 2018, the human casualties from the devastating fire in Mati, Attica, have not been accounted for, as previously mentioned in the Abstract [4,5]. This is likely due to the classification of this particular fire as a wildfire rather than an urban fire.

According to a study conducted, in America, by the National Fire Protection Association (NFPA), there was an approximate 4% rise in residential fires and a 13% increase in deliberately ignited structural fires in 2018 [2]. Thus, based on the official fire situation report, *Fire Loss in the United States During 2017*, published by the National Fire Protection Association, fire departments across the United States responded to an estimated 1,319,500 fire incidents in 2017. These incidents led to approximately 3,400 civilian fatalities, 14,670 civilian injuries, and an estimated \$23 billion in direct property damage [2].

Additionally, the World Health Organization (WHO), an estimated three million fires occur globally each year, resulting in approximately 180,000 fatalities [6]. Moreover, the majority of these disasters take place in major urban centers, within low - income countries, where various economic, social, and environmental factors contribute to an increased risk of fire incidents.

Nevertheless, the data demonstrate that wildfires are not solely an issue confined to low socio-economic status countries. Notably, the Black Summer of Australia in 2019–2020 remains a significant historical event. Tragically, the fires claimed 33 lives and impacted thousands through smoke inhalation and other effects. By the end of the season, they had burned a record 19 million hectares, destroyed over 3,000 homes, displaced tens of thousands, and caused the loss of billions of animals [7,8]. Furthermore, in July 2024, wildfires occurred in the Arctic plains of Russia's Far East, posing significant challenges to containment efforts [9,10]. That summer, wildfires had already devastated nearly 5 million hectares of forest in Russia. Wildfires in Russia's Siberian and Far East regions, which occur annually during the summer, have become more severe in recent years due to climate change, which has intensified the hot and dry conditions that fuel these fires [11]. Climate change projections, indicate that urban environments may face increasing, fire hazards [12]. A stark example of the interconnectedness between climate change, and wildfires, is evident in the fires that occurred in Los Angeles in January 2025, and in Japan in February of the same year. In this connection, Climate scientists are working to identify the impact of climate change on wildfires. However, the most substantial human influence may lie in the ignition sources, as no lightning storms were present at the time, in L.A, to naturally trigger the fires [13]. As the relentless wildfire advanced into urban areas, driven by wind speeds exceeding 80 miles per hour, it destroyed over 16,000 homes and buildings [13]. By February 4, a total of 29 fatalities had been reported [14]. Another technologically and socioeconomically advanced nation, Japan, was struck by an uncontrolled wildfire on February 26, 2025 [15]. The fire scorched over 2,100 hectares and destroyed more

than 80 buildings. Determining whether climate change has directly caused or intensified specific wildfires is challenging, as other factors, such as land-use changes, also play a role. However, the IPCC asserts that climate change is increasing the likelihood of weather conditions that facilitate the spread of wildfires [16].

From these real events, it is inferred that an unpredictable natural disaster, such as a wildfire, does not discriminate between low and high-socioeconomic areas. Furthermore, it highlights the precarious balance (sword of Damocles) between climate change, and urban expansion into forested regions. This underscores the critical importance of our research in predicting the impacts damages of an urban fire. Next, we will refer to relevant studies focused on the field of urban fire prediction. A team of researchers, used data from Ankara region, of Turkey, for analysis of the spatial and temporal patterns of residential fires, can enable decision-makers to strategically allocate resources for fire management, based on the intensity of fire clustering over time and across different locations [17]. Next, we proceed with an article that examines existing research on the social, economic, and building stock characteristics associated with residential fire risk in urban neighborhoods [18]. From Australia in 2010, we have the first study utilizing the Bayesian approach, to produce detailed spatial forecasts of residential household fires, across metropolitan South-East Queensland [19]. Also, from Australia, a study employs a Markov chain approach to estimate the likelihood of residential fire occurrences based on historical fire data. Utilizing fire incident records collected over a decade in Melbourne, Australia, the spatially integrated fire risk model forecasts potential fire events by incorporating spatial and temporal variables as key predictive factors [20]. Subsequently, the following study builds upon the methodology and effectiveness of a firefighter-led public education campaign on fire prevention, which successfully decreased both the frequency, and severity, of residential structure fires in high-risk areas of Surrey, British Columbia [21]. In the sequel, some studies have used GIS methods, to analyze the fire risk in urban areas. In Turkey, a study examines fires that have occurred in various locations across Turkey, including cold storage facilities, factories, and manufacturing plants. The case data was utilized to calculate risk scores using Geographic Information System (GIS), Analytical Hierarchy Process (AHP), and Inverse Distance Weight (IDW) methods [22]. In China, in order to select the best suitable fire brigade zone, they analyze: fire-risk areas, traffic congestion, land cover, and location. They employ various methods, including Geographic Information Systems (GIS), Multi-Criteria Decision Making (MCDM), and Location-Allocation (L-A) techniques, along with multi-source geospatial data such as land cover, points of interest, drive time, and statistical yearbooks. Additionally, they used Analytic Hierarchy Processes (AHP) to thoroughly assess undeveloped areas based on factors such as location, topography, and potential fire-risk zones [23]. The next study conducted in Greece, to develop a fire risk estimation model that integrates recent land cover changes alongside other critical risk factors. They implemented a Support Vector Machine (SVM) algorithm [24] combined with the Analytic Hierarchy Process (AHP), within a Geographic Information System (GIS) platform. This approach allowed for a more precise assessment of fire-prone areas. As a case study, they applied this methodology to the Dadia-Lefkimi - Soufli National Forest Park, ensuring a comprehensive evaluation of fire risk in the region [25].

Afterwards, a study seeks to assess fire risk in urban areas by analyzing 19 factors related to economic, social, and built environment aspects, as well as past fire incidents. It employs Multi-Criteria Decision Making (MCDM) techniques, specifically the Analytic Hierarchy Process (AHP) to determine the significance and weighting of each criterion. To illustrate the method's effectiveness, the research develops an urban vulnerability index map for Ardabil, Iran, using the Fuzzy-VIKOR approach within a Geographic Information System (GIS) framework [26]. Building upon, Analytic Hierarchy Process, the paper from

Taiwan, evaluated the severity of building fires across 17 villages in Taishan District, New Taipei City. A comprehensive literature review was conducted to examine the influence of fire severity assessment criteria, which served as the foundation for identifying key factors, and developing evaluation items, within the (AHP) framework [27].

Building upon, Analytic Hierarchy Process, the paper from Taiwan, evaluated the severity of building fires across 17 villages in Taishan District, New Taipei City. A comprehensive literature review was conducted to examine the influence of fire severity assessment criteria, which served as the foundation for identifying key factors, and developing evaluation items, within the (AHP) framework [28]. American researchers, have introduced two machine learning models, utilizing Random Forest [29,30] and Extreme Gradient Boosting (XGBoost) [31], to forecast future service demand in urban areas based on spatial data analysis, in collaboration with Victoria Fire Department, U.S.A [32]. A similar study was conducted by Turkish researchers in 2020, and from China in 2021 [25]. Specifically, the Turkish colleagues proposed a group decision-making (GDM) approach, integrating the recently developed Best–Worst Method (BWM) [33], a multi-criteria decision-making (MCDM) technique [34], with Geographic Information Systems (GIS) to identify optimal locations for new emergency facilities in Istanbul. Their analysis incorporated the input of two decision-makers [35]. Moving forward, another fire risk model was implemented within the Pittsburgh Bureau of Fire (PBF), and initial risk models was developed for predicting residential property fire risk [36].

Furthermore, the subsequent study, is a novel deep sequence learning model, referred to as the Fire Situation Forecasting Network (FSFN), is introduced to enhance the processing of information and the analysis of Spatio-temporal correlations within regional urban fire alarm datasets [37]. Building upon a prior method, on fire statistics, a weighted fire risk calculation method was developed, incorporating the frequency of fire occurrences, direct economic losses, and fire-related casualties. According this approach, and with enhancements to the K-means clustering algorithm [38], this study introduced a fire risk K-means clustering model. This model offers an improved solution for the automated classification of fire risk levels [39]. The next study, seeks to expand the limited empirical research on urban fires in the Global South by analyzing their causes and dynamics. Focusing on disaggregated fire incident data from Kathmandu Metropolitan City (KMC), Nepal, the research identifies key contributing factors and examines both the spatial and temporal distribution of urban fires [40]. The following study, was conducted in Iran, sought to apply machine learning algorithms to enhance the accuracy of predicting firefighting operation duration in urban areas, while also identifying the key factors that significantly impact this timeframe [41]. The subsequent paper, employs an unsupervised deep learning (DL) approach to categorize hazard levels at fire sites and utilizes an autoregressive integrated moving average (ARIMA) model to predict temperature variations, leveraging the extrapolation capabilities of a random forest regressor [42]. In the sequel, studies from Japan integrate the earthquake factor as a cause of urban fires. The following article introduces the development of a stochastic model designed for time series forecasting of post-earthquake fire ignitions in buildings, aiming to enhance post-earthquake fire risk assessment [43]. The same researcher, also developed a physics-based urban fire spread model that incorporates the stochastic occurrence of spot fires in the wooden residential areas of Itoigawa City. Utilizing the Monte Carlo method, they compared the simulated results with the actual fire damage recorded in 2016 [44]. Concluding with Japan, a probabilistic approach is introduced to evaluate the cascading risks associated with ground shaking and post-earthquake fires, on a regional scale [45].

This paper proposes the use of modern machine learning techniques based on Grammatical Evolution [46] to predict the potential damage caused by urban fires. This prediction

was based on data that has been collected and subsequently digitized by the Greek Fire Service. After digitizing the original data, three categories were created depending on the size of the disaster that has been caused: small - scale disaster, medium - scale disaster and large - scale disaster. Therefore, the problem of predicting the magnitude of the disaster was transformed into a classification problem so that machine learning techniques could be applied to it. The techniques used in the conducted experiments include construction of neural networks [47,48], feature construction of artificial features from the original ones using Grammatical Evolution and production of classification rules. The obtained results are compared against the results from various traditional machine learning methods and a discussion is provided on the Results section of this manuscript.

The rest of this manuscript is divided as follows: in section 2 the proposed methods are presented in detail, in section 3 the experiments are illustrated and discussed and finally, in section 4 some conclusions are presented.

## 2. Materials and Methods

This section initiates with a detailed description of the used datasets and it continues with a brief presentation of the Grammatical Evolution technique and concludes with the full description of the used techniques.

### 2.1. The used datasets

The dataset utilized in this research was sourced from the Hellenic Fire Service in compliance with open data guidelines established by the European Union Directive (2013/37/EU), aiming to promote transparency and open access to governmental records. The dataset contains comprehensive records detailing urban fire incidents specifically for the calendar years 2014-2023.

For each urban fire event documented, detailed information was systematically collected, including the date and precise time of occurrence, allowing for temporal analysis and identification of patterns over various time intervals. The geographic location for each incident was also reported with a municipality code. In addition, specific characteristics relevant to each fire event were captured, including the probable cause or origin of the fire, which helps in identifying common fire risk factors within urban settings. Data regarding the structural properties involved, such as building type or property classification, was also documented, contributing to a comprehensive risk profile for urban infrastructure.

Furthermore, human casualty data detailing the number of fatalities and injuries associated with each incident were recorded. The dataset indicated an average of 0.002 fatalities per incident, with a maximum of 2 fatalities observed in a single event. Injuries averaged at approximately 0.0008 per incident, with a maximum of 1 injury recorded per event. Additionally, instances of burn injuries were relatively infrequent, averaging around 0.002 per incident, with a maximum count of 2 burn cases reported.

Information on the resources deployed was also comprehensively documented. On average, each incident involved approximately 1.65 firefighting vehicles, with a maximum of 24 vehicles responding to the most severe incidents. Personnel deployment averaged about 4.18 firefighters per incident, with an interquartile range from 2 to 5 firefighters, and up to 67 personnel attending a single event in extreme cases.

The dataset underwent thorough preprocessing procedures to ensure high-quality data for analysis. These procedures included validation checks for data accuracy, consistency, completeness, and the removal or correction of any identified errors or inconsistencies. Such rigorous preprocessing steps were critical for enhancing the reliability and validity of the analytical processes that followed.



Based on data from the Hellenic Fire Service, we isolated and processed the pre-registered categories of Small, Medium, and Large Fires, excluding other categories that were not relevant to the scope of our research. The classification of a fire as Small, Medium, or Large may be determined in the field by firefighters, particularly when additional flammable materials are present in the surrounding area, when chemical substances that can accelerate the fire are involved, or when there is an exceptional risk to human lives. Furthermore, according to our data, urban fires have been recorded at 146 distinct locations, each assigned a unique identification number (code). For example, as an indicative reference, in 2023, the fire department responded to 21,606 fire incidents in apartment buildings (code 18), 9,106 on streets, 5,219 (code 22) in single-family homes (code 39), 4,971 in vacant lots (code 35), 2,389 in vehicles (code 6), 1,322 in duplex houses (code 37), and 1,270 in waste disposal areas (code 54). Beyond these, some unusual locations were also recorded, including 140 firefighting interventions in wells (code 143), 38 in cemetery (code 82), 106 in marine areas (code 69), 4 in public toilets (code 112), and so forth. Hence, the problem of predict the extend of damage caused by urban fires can be considered as a classification problem, where any optimization method can be used to minimize the following training error:

$$E(M(\vec{x}, \vec{p})) = \sum_{i=1}^M (M(\vec{x}_i, \vec{p}) - t_i)^2 \quad (1)$$

Where the function  $M(\vec{x}, \vec{p})$  represents a machine learning model and the vector  $\vec{p}$  represents the parameters of the model that should be estimated by any optimization method. The set  $T = \{(x_1, t_1), (x_2, t_2), \dots, (x_M, t_M)\}$  represents the training set of the input problem, where the vectors  $x_i$  stand for the input patterns and the values  $t_i$  are the expected outputs.

## 2.2. Grammatical Evolution

The algorithm of Grammatical evolution can be considered as a genetic algorithm where the chromosomes, which are series of positive integer values, denote production rules of any given BNF (Backus–Naur form) grammar [49]. The method has been incorporated in various cases from real - world applications, such as data fitting [50,51], solution of trigonometric equations [52], composition of music [53], neural network construction [54,55], producing numeric constraints[56], video games [57,58], energy problems [59], combinatorial optimization [60], cryptography [61] etc. The BNF grammars are used to describe the syntax of programming languages and they can be defined as sets  $G = (N, T, S, P)$  where

- The set  $N$  represents the non-terminal symbols of the grammar. Each non - terminal symbol can be replaced to a series of terminal symbols with the assistance of some associated production rules.
- The set  $T$  contains the terminal symbols.
- $S$  is considers as the start symbol of the grammar with the assumption  $S \in N$ .
- The set  $P$  contains the production rules of the grammar, used to replace non - terminal symbols with series of terminal ones.

The production procedure of Grammatical Evolution starts from the symbol  $S$  and through a series of steps creates valid programs by replacing non - terminal symbols with series of terminal symbols following the selected rules. Every production rule is is selected usig the following steps:

- Obtain the next element  $V$  from the chromosome that is processed.
- Select the production rule as: Rule =  $V \bmod R$ , where  $R$  defines the total number of production rules for the non – terminal symbol that is under processing.

### 2.3. Neural Network Construction using Grammatical Evolution

The Neural Network Construction method was initial presented in the paper of Tsoulos et al [62] and it is used to determine the optimal architecture of artificial neural networks as well as the optimal set of parameters for the network. The Neural Network construction mechanism utilizes the Grammatical Evolution procedure in order to produce artificial neural networks in the form:

$$N(\vec{x}, \vec{w}) = \sum_{i=1}^H w_{(d+2)i-(d+1)} \sigma \left( \sum_{j=1}^d x_j w_{(d+2)i-(d+1)+j} + w_{(d+2)i} \right) \quad (2)$$

In this equation the term  $H$  represents the number of processing units (weights) of the network. The function  $\sigma(x)$  stands for the sigmoid function. The grammar used by Grammatical Evolution to produce neural networks in the form of Equation 2 is outlined in Figure 2. This method has been incorporated in problems such as, chemistry problems [63], estimation of solutions of differential equations etc.

```

S:=<Sigval>
<Sigval>::=<Node>
          | <Node> + <Sigval>
<Node>::=<Number>*sig(<Sum>+<Number>)
<Sum>::= <Number>*<Xlist>
          |      <Sum>+<Sum>
<Xlist>::= x1      (0)
          |      x2  (1)
          |      .....
          |      xd  (d-1)
<Number>::= (<Dlist>.<Dlist>)
          |  (-<Dlist>.<Dlist>)
<Dlist>::= <Digit>      (0)
          | <Digit><Dlist> (1)
<Digit>::= 0      (0)
          |  1  (1)
          |  .....
          |  9  (9)

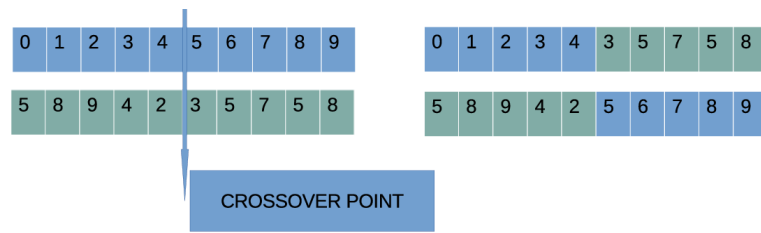
```

**Figure 2.** The proposed grammar neural network construction procedure.

The main steps of the algorithm used to produce neural networks are outlined below:

1. **Initialization Step.**
  - (a) **Set** as  $N_c$  the number of chromosomes and as  $N_g$  the number of allowed generations.
  - (b) **Set** as  $p_s$  the selection rate with  $p_s \leq 1$  and as  $p_m$  the mutation rate with  $p_m \leq 1$ .
  - (c) **Initialize** randomly each chromosome  $c_i$ ,  $i = 1, \dots, N_c$  as a set of randomly selected integers.
  - (d) **Set**  $k = 0$ , as the generation counter.
2. **Fitness Calculation Step.**
  - (a) **For**  $i = 1, \dots, N_c$  **do**
    - i. **Create** using the grammar of Figure 2 the corresponding neural network  $N_i(x)$  for the chromosome  $c_i$ .
    - ii. **Set** as the fitness  $f_i$  of the chromosome  $g_i$  the training error of neural network  $N_i(x)$ .
  - (b) **End For**

3. **Application of Genetic Operations.**
  - (a) **Application of selection.** The best  $p_s \times N_c$  chromosomes are copied to the next generation. The remaining are substituted by chromosomes produced during crossover and mutation.
  - (b) **Application of crossover.** During this procedure new chromosomes will be created from selected chromosomes from the current generation. For each pair  $(z, w)$  of produced chromosomes two chromosomes  $p_1$  and  $p_2$  will be selected from the current population using tournament. selection. The new chromosomes will be produced using one - point crossover, which is graphically illustrated in Figure 3.
  - (c) **Application of mutation.** For every element of each chromosome a random number  $r \leq 1$  is drawn. The corresponding element is altered randomly when  $r \leq p_m$ .
4. **Termination Check Step.**
  - (a) **Set**  $k = k + 1$
  - (b) **If**  $k < N_g$  **then go to** Fitness Calculation Step.
5. **Testing step.**
  - (a) **Obtain** the chromosome  $c^*$  with the lowest fitness value in the population.
  - (b) **Create** the corresponding neural network  $N^*(x)$  and apply it to the test set and report the associated error.



**Figure 3.** An example of the one - point crossover procedure.

#### 2.4. Feature construction using Grammatical Evolution

The next method used in the performed experiments is the Feature Construction technique, initially presented in the work of Gavrilis et al [65]. The method utilizes the Grammatical Evolution procedure to create artificial features from the original ones and hence it can be used to enhance the effectiveness of any applied machine learning model to the artificial data. The artificial features are non - linear mappings of the original ones and the grammar used by the method to construct such features is shown in Figure 4.



**Figure 4.** The grammar used in Feature Construction method.

```

S ::= <expr>      (0)
<expr> ::= ( <expr> <op> <expr> )
          | <func> ( <expr> )
          | <terminal>
<op> ::= +
        | -
        | *
        | /
<func> ::= sin
        | cos
        | exp
        | log
<terminal> ::= <xlist>
            | <digitlist> . <digitlist>
<xlist> ::= x1
          | x2
          | .....
          | xN
<digitlist> ::= <digit>
              | <digit> <digit>
              | <digit> <digit> <digit>
<digit> ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

```

The features produced by this procedure can be evaluated using any machine learning method, although the Radial Basis Function (RBF) networks [66,67] were used due to the speed of their corresponding training procedure. The main steps of this procedure are the following:

1. **Initialization step.**
  - (a) **Define** as  $N_c$  the number of chromosomes and as  $N_g$  the number of allowed generations.
  - (b) **Define** the selection rate  $p_s$  and the mutation rate  $p_m$ .
  - (c) **Define** as  $N_f$  the number of constructed features.
  - (d) **Initialize** the  $c_i$ ,  $i = 1, \dots, N_c$  chromosomes as vectors of randomly selected integers.
  - (e) **Set**  $k = 0$ , the generation counter.
2. **Fitness calculation step.**
  - (a) **For**  $i = 1, \dots, N_c$  **do**
    - i. **Create**  $N_f$  artificial features  $y_1, y_2, \dots, y_{N_f}$  for the chromosome  $c_i$ . The production is performed using the grammar of Figure 4.
    - ii. **Modify** the train set of the objective problem using the features  $y_1, y_2, \dots, y_{N_f}$ .
    - iii. **Apply** a machine learning model to the modified set and define as the fitness value  $f_i$  the corresponding training error.
  - (b) **End For**
3. **Application of genetic operations.** Apply the same genetic operations as in the case of Neural Construction method of subsection 2.3.
4. **Termination check step.**
  - (a) **Set**  $k = k + 1$
  - (b) **If**  $k < N_g$  **go to** Fitness calculation step.

## 5. Testing step.

- (a) **Obtain** the chromosome  $c^*$  with the lowest fitness value.
- (b) **Produce** the features  $y_1^*, y_2^*, \dots, y_{N_f}^*$  for this chromosome.
- (c) **Modify** the test set of the objective problem using the previously created features.
- (d) **Apply** any machine learning model to the test set and report the associated error.

### 2.5. Create classification rules using Grammatical Evolution

The third method used in the conducted experiments which is based on Grammatical Evolution is the method that produces classification rules [68]. This method has also been published as a software recently [69]. The BNF grammar used by this method is shown in Figure 5.

**Figure 5.** The grammar used by the method that produces classification rules using Grammatical Evolution.

```

<S> ::= if(<BEXPR>) CLASS=0 else CLASS=1
<BEXPR> ::= <XLIST><BOOLOP><EXPR>
           | !(<BEXPR>)
           | <XLIST><BOOLOP><EXPR>&<BEXPR>
           | <XLIST><BOOLOP><EXPR> | <BEXPR>
<BOOLOP> ::= >
           | >=
           | <
           | <=
<EXPR> ::= (<EXPR><BINARYOP><EXPR>)
           | <FUNCTION>(<EXPR>)
           | <TERMINAL>
<BINARYOP> ::= +
           | -
           | *
           | /
<FUNCTION> ::= sin | cos | exp | log
<TERMINAL> ::= <XLIST>
           | <DIGITLIST>.<DIGITLIST>
           | (-<DIGITLIST>.<DIGITLIST>)
<XLIST> ::= x1 | x2 | ... | xD
<DIGITLIST> ::= <DIGIT>
           | <DIGIT><DIGIT>
           | <DIGIT><DIGIT><DIGIT>
<DIGIT> ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

```

The main steps of this method have as follows:

## 1. Initialization step.

- (a) **Define** as  $N_c$  the total number of chromosomes and with  $N_g$  the allowed number of generations.
- (b) **Define** the selection rate  $p_s$  and the mutation rate  $p_m$ .
- (c) **Initialize** as vectors of randomly selected integers the chromosomes  $c_i$ ,  $i = 1, \dots, N_c$ .
- (d) **Set**  $k = 0$ , the generation counter.

## 2. Fitness calculation step.

- (a) **For**  $i = 1, \dots, N_c$  **do**

- i. **Create** using the Grammatical evolution procedure and the grammar depicted in Figure 5 a classification program  $G_i$  for the corresponding chromosome  $c_i$ .
- ii. **Set** the fitness  $f_i$  as

$$f_i = \sum_{j=1}^M (G_i(x_j) - t_j)^2 \quad (3)$$

for the corresponding training set  $T = \{(x_1, t_1), (x_2, t_2), \dots, (x_M, t_M)\}$ . The values  $x_i$  denote the input patterns and the value  $t_i$  the expected outcome for pattern  $x_i$ .

(b) **End For**

3. **Genetic operations step.** Apply the same genetic operations as in the case of Neural Construction method of subsection 2.3.
4. **Termination check step.**
  - (a) **Set**  $k = k + 1$
  - (b) **If**  $k < N_g$  then go to Fitness calculation step.
5. **Testing step.**
  - (a) **Obtain** the best chromosome  $c^*$  and produce the associated classification program  $G^*$ .
  - (b) **Apply** the classification program to the test set of the problem and report the result.

### 3. Results

The code used in the experiments was implemented in C++ programming language with the assistance of Optimus optimization environment, freely available from <https://github.com/itsoulos/GlobalOptimus/> (accessed on 2 April 2025). Also, the freely available programming tool of WEKA [70] was used for some of the experiments, that can be downloaded also freely from <https://ml.cms.waikato.ac.nz/weka/> (accessed on 2 April 2025). For the validation of the experiments the method of ten - fold cross validation was incorporated. All the experiments were conducted on a machine running Debian Linux with 128GB of RAM. The values for the experimental settings are shown in Table 1.

**Table 1.** The values used for the experimental settings.

PARAMETER	MEANING	VALUE
$N_c$	Number of chromosomes	500
$N_g$	Maximum number of generations	200
$p_s$	Selection rate	0.10
$p_m$	Mutation rate	0.05
$N_f$	Number of produced features	2
$H$	Number or processing nodes	10

Also, the Table 2 contains the experimental results where the following notation is used:

1. The column YEAR denotes the year for which the methods were applied.
2. The column BAYES NET denotes the application of the Bayesian Network method [71,72].
3. The column MLP represents the incorporation of an artificial neural network with  $H = 10$  processing nodes, that was trained using the Back Propagation method [73,74].

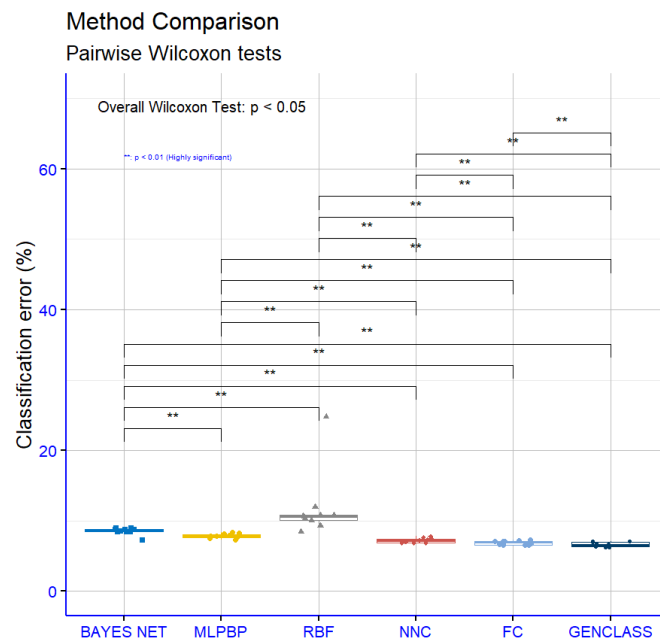
4. The column RBF denotes the usage of a Radial Basis Function network with  $H = 10$  processing nodes.
5. The column NNC represents the usage of the Neural Network construction method described in subsection 2.3.
6. The column FC stands for the usage of the Feature Construction method provided in subsection 2.4.
7. The column GENCLASS denotes the usage of the method that creates classification rules, described in subsection 2.5.
8. The final row AVERAGE represents the average classification error for all years between 2014 and 2023.

**Table 2.** Experimental results using various machine learning techniques. Numbers in cells represent average classification error as measured on the corresponding test set.

YEAR	BAYES NET	MLP	RBF	NNC	FC	GENCLASS
2014	9.01%	8.34%	11.97%	7.82%	7.35%	7.03%
2015	8.75%	7.63%	10.79%	7.13%	6.78%	6.65%
2016	8.99%	8.13%	10.73%	7.48%	7.10%	7.05%
2017	8.43%	8.29%	10.78%	7.68%	7.24%	7.13%
2018	8.38%	7.99%	9.33%	7.30%	7.11%	6.74%
2019	7.31%	7.78%	24.81%	7.33%	7.15%	6.26%
2020	8.70%	7.86%	10.03%	6.99%	6.66%	6.47%
2021	8.58%	7.88%	10.37%	6.87%	6.55%	6.39%
2022	8.80%	7.29%	8.45%	6.86%	6.52%	6.32%
2023	8.46%	7.50%	10.56%	6.87%	6.58%	6.20%
<b>AVERAGE</b>	<b>8.54%</b>	<b>7.87%</b>	<b>11.78%</b>	<b>7.23%</b>	<b>6.90%</b>	<b>6.62%</b>

In Table 2 GENCLASS demonstrates the lowest average classification error (6.62%), making it the most reliable model for wildfire prediction. It is followed by FC with an average error of 6.90% and NNC with 7.23%. Traditional models such as BAYES NET (8.54%) and MLP(BP) (7.87%) exhibit higher error rates, while RBF performs the worst with an average error of 11.78%, including an exceptionally high value in 2019 (24.81%), likely due to overfitting or sensitivity to outliers. GENCLASS not only has the lowest error but also shows consistent improvement over time. Starting at 7.03% in 2014, it decreased to 6.20% in 2023, with minor fluctuations in between. FC and NNC also display a declining trend but with greater variability. In contrast, MLP(BP) and BAYES NET show no clear improvement, with BAYES NET even experiencing a slight increase in error in 2022–2023. RBF, despite improving after 2019, remains unstable and less reliable. When comparing the top three models (GENCLASS, FC, NNC), GENCLASS consistently outperforms the others in all years except 2019, where FC had a marginally better performance. NNC, while superior to traditional methods, lags behind GENCLASS and FC. The remaining models (BAYES NET, MLP(BP), RBF) appear less competitive in accuracy compared to newer techniques. The data strongly supports GENCLASS as the optimal model for wildfire prediction due to its consistently low and stable error rate, as well as its progressive improvement over time. FC and NNC remain viable alternatives with good performance, but GENCLASS maintains a clear advantage. The other models, particularly RBF, may require further optimization to enhance reliability. The steady performance of GENCLASS makes it the safest choice for practical applications.

Within the framework of statistical analysis, R language scripts were executed to extract significance levels (p-values) for performance differences between the classification models. The results, shown in Figure 6, reveal statistically significant differences between the compared models. Specifically, all pairwise model comparisons yielded p-values below



**Figure 6.** Statistical comparison of the experimental results obtained by various machine learning methods.

the standard significance threshold (typically  $p < 0.05$ ), indicating statistically significant performance differences. The comparison between BAYES NET and MLP(BP) produced  $p = 0.0098$ , while BAYES NET's comparisons with RBF, NNC, FC and GENCLASS showed even smaller values ( $p = 0.0039$  and  $p = 0.002$ ), confirming that BAYES NET differs significantly from other models. Similarly, MLP(BP) comparisons with RBF, NNC, FC and GENCLASS all resulted in  $p = 0.002$ , demonstrating high statistical significance in their performance differences. The same holds true for RBF's comparisons with NNC, FC and GENCLASS ( $p = 0.002$ ), as well as for comparisons between NNC, FC and GENCLASS. The fact that all  $p$ -values are very small ( $p \leq 0.0098$ ) confirms that the models do not perform equally and that statistically significant differences exist between them. This is particularly evident in comparisons involving GENCLASS, which - as previous analysis has shown - stands out for its high accuracy. These results reinforce the conclusion that certain models (such as GENCLASS and FC) are clearly superior to others (like BAYES NET and RBF), a finding that should be considered in practical machine learning applications.

#### 4. Conclusions

This study implements the innovative technique of Grammatical Evolution to predict the consequences of urban fires, utilizing a decade of data from the Hellenic Fire Service. The results demonstrate the clear superiority of the GENCLASS method over other machine learning approaches, both in terms of accuracy and interpretability. The method's ability to generate human-readable classification rules constitutes a significant advantage over traditional "black-box" machine learning models. These rules reveal complex correlations between factors such as meteorological conditions, urban layout, and human activity, providing valuable insights for fire prevention and management. However, the research does face certain limitations that warrant discussion. The reliance on historical data reduces predictive capability in extreme or unprecedented scenarios, such as those caused by climate change. Additionally, the performance of some models, like RBF, shows significant instability in certain cases, likely due to overfitting or sensitivity to outliers. This

underscores the need for further algorithm optimization and the integration of additional data to enhance reliability.

The findings of this research confirm that Grammatical Evolution, particularly the GENCLASS method, offers a robust solution for predicting the impacts of urban fires. This method not only achieves the lowest average classification error but also provides transparent, interpretable rules that can be directly utilized by fire departments and urban planners. The generated rules uncover critical dependencies, such as the influence of temperature, emergency response times, and demographic characteristics on the extent of damage. This paves the way for developing dynamic evacuation strategies, implementing preventive measures in vulnerable areas, and raising public awareness of fire risks. Moreover, the consistent improvement in GENCLASS’s performance over time suggests its adaptability to changing conditions and its potential for enhancement with new data. However, it is important to recognize that the effectiveness of any predictive method depends heavily on the quality and completeness of available data, as well as the ability to account for new and unforeseen factors, such as climate change.

To further develop the findings of this research and strengthen their practical application, several directions for future exploration are proposed. First, the integration of real-time data from sensors and satellite systems could significantly improve the accuracy and timeliness of predictions, enabling dynamic model adjustments and rapid responses to emerging threats. Second, extending the method to other geographic regions with different urban and climatic characteristics could explore the generalizability of the findings and identify new factors influencing fire risk. Third, combining Grammatical Evolution with advanced deep learning techniques, such as neural networks for spatiotemporal analysis, could enhance predictive capabilities in complex scenarios involving multiple simultaneous hazards. Finally, developing simulations that account for the long-term impacts of climate change and urban expansion could provide valuable insights for designing more resilient and safer urban environments. These directions have the potential to transform the research findings into practical tools for safeguarding human lives and urban infrastructure.

**Author Contributions:** C.K., V.C. and I.G.T. conceived of the idea and the methodology, and C.K. and V.C. implemented the corresponding software. C.K. conducted the experiments, employing objective functions as test cases, and provided the comparative experiments. A.M. performed the necessary statistical tests. All authors have read and agreed to the published version of the manuscript.

**Funding:** This research received no external funding.

**Institutional Review Board Statement:** Not applicable.

**Informed Consent Statement:** Not applicable.

**Acknowledgments:** This research has been financed by the European Union : Next Generation EU through the Program Greece 2.0 National Recovery and Resilience Plan , under the call RESEARCH – CREATE – INNOVATE, project name “iCREW: Intelligent small craft simulator for advanced crew training using Virtual Reality techniques” (project code:TAEDK-06195).

**Conflicts of Interest:** The authors declare no conflicts of interest.

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