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ICP NOTES

LEETCODE PROBLEMS

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Counting Bits / 338

```
for i in range(1, n+1):
```

```
    if offset * 2 == i:
```

```
        offset = i    # Update offset to new power of 2
```

```
    dp[i] = 1 + dp[i - offset] # Add 1 to the bit count of i - offset
```

```
return dp
```

Why It Works

- Every number can be expressed as:

$$i = \text{offset} + x$$

- Where offset is the **largest power of 2** $\leq i$, and $x < \text{offset}$.
- Since offset has only one 1-bit, **$\text{dp}[i] = 1 + \text{dp}[i - \text{offset}]$** .
- Dry Run for **$n = 5$** :

i	offset	dp[i]	Explanation
1	1	1	$1 + \text{dp}[0] = 1$
2	2	1	offset updates to 2, $\text{dp}[2] = 1 + \text{dp}[0]$
3	2	2	$\text{dp}[3] = 1 + \text{dp}[1] = 2$
4	4	1	offset updates to 4
5	4	2	$\text{dp}[5] = 1 + \text{dp}[1] = 2$

Output: [0, 1, 1, 2, 1, 2]

⌚ Time and Space Complexity

- Time:** $O(n)$
- Space:** $O(n)$

Missing Number / 268

class Solution:

```
def missingNumber(self, nums: List[int]) -> int:
```

```
    n = len(nums)
```

```
    expected_sum = n * (n + 1) // 2
```

```
    actual_sum = sum(nums)
```

```
    return expected_sum - actual_sum
```

Why It Works

- The numbers are from 0 to n, but one number is missing.
- The **sum of first n natural numbers** (0 to n) can be computed with the formula:

$$\text{Expected_Sum} = [n * (n + 1)] / 2$$

- actual_sum is just the sum of the numbers present in the array.
- The **difference between the expected sum and actual sum** gives the missing number:

$$\text{missing} = \text{expected_sum} - \text{actual_sum}$$

Dry Run (Example)

Input: nums = [3, 0, 1]

Step	n	expected_sum	actual_sum	missing (return value)	Explanation
1	3	$3*4//2=6$ $3 * 4 // 2 = 6$	$3+0+1=4$ $3+0+1=4$	$6-4=2$ $= 26-4=2$	2 is the missing number

Output: 2

Time and Space Complexity

- **Time Complexity:**
 - Calculating expected_sum $\rightarrow O(1)$
 - Calculating actual_sum (using sum()) $\rightarrow O(n)$
 - Total:** $O(n)$
- **Space Complexity:**
 - Only a few variables are used $\rightarrow O(1)$ (constant space)

Number of 1 Bits / 191

class Solution:

```
def hammingWeight(self, n: int) -> int:
```

```
    res = 0
```

```
    while n:
```

```
        # res += n % 2
```

```
        n &= n - 1
```

```
        # n = n >> 1
```

```
        res += 1
```

```
    return res
```

Why It Works

- **Goal:** Count how many 1 bits are present in the binary representation of n.
- The trick: $n \& (n-1)$ removes the **rightmost set bit** from n.
 - Example: $n = 10110 \rightarrow n-1 = 10101 \rightarrow n \& (n-1) = 10100$ (rightmost 1 removed)
- Each loop iteration removes one 1 bit and increments res.
- Loop continues until n becomes 0, meaning all 1 bits have been counted.

This approach is more efficient than checking every bit individually because it only loops once per set bit.

Dry Run (Example)

Input: $n = 11$ (binary = 1011)

Iteration	n (binary)	n-1 (binary)	n & (n-1)	res	Explanation
Start	1011	1010	1010	1	Rightmost 1 removed
2	1010	1001	1000	2	Rightmost 1 removed
3	1000	0111	0000	3	Rightmost 1 removed, $n = 0 \rightarrow$ stop

Output: 3 (because 11 has three 1's in its binary form)

Time and Space Complexity

- **Time Complexity:**
 - Runs once for every set bit in $n \rightarrow O(k)$, where k = number of 1-bits.
 - Worst case: $O(\log n)$ (when all bits are 1).
- **Space Complexity:** Only uses constant variables $\rightarrow O(1)$

Reverse Bits / 190

class Solution:

```
def reverseBits(self, n: int) -> int:
```

```
    res = 0
```

```
    for i in range(32):
```

```
        bit = (n >> i) & 1
```

```
        res = res | (bit << (31 - i))
```

```
    return res
```

Why It Works

- **Goal:** Reverse the bits of a 32-bit unsigned integer.
- **Step-by-step logic:**
 1. $(n \gg i) \& 1$ extracts the i -th bit from the right.
 2. $(bit \ll (31 - i))$ places that bit into its **reversed position** (mirrored around center).
 3. $res \mid \dots$ sets that bit in res without affecting previously set bits.
- After looping through all 32 bits, res contains the bit-reversed number.

Dry Run (Example)

Input: $n = 13$ (binary = 000000000000000000000000000001101)

i	Extracted Bit $(n \gg i) \& 1$	Shift $(bit \ll (31-i))$	res (after setting)
0	1	Bit goes to position 31	10000000000000000000000000000000
1	0	Nothing added	10000000000000000000000000000000
2	1	Bit goes to position 29	10100000000000000000000000000000
3	1	Bit goes to position 28	10110000000000000000000000000000
...	Remaining bits are 0	No changes	Final Result

Output: $res = 2952790016$ (binary = 10110000000000000000000000000000)

Time and Space Complexity

- **Time Complexity:**
 - Loop runs exactly 32 times $\rightarrow O(32) \rightarrow O(1)$ (constant time)
- **Space Complexity:**
 - Only uses a few integer variables $\rightarrow O(1)$ (constant space)

Middle of the Linked List / 876

Definition for singly-linked list.

class ListNode:

def __init__(self, val=0, next=None):

self.val = val

self.next = next

class Solution:

def middleNode(self, head: Optional[ListNode]) -> Optional[ListNode]:

slow, fast = head, head

while fast and fast.next:

slow = slow.next

fast = fast.next.next

return slow # slow now points to the middle node

Why It Works

- Uses **two pointers**:
 - slow moves one step at a time.
 - fast moves two steps at a time.
- When fast reaches the end of the list:
 - slow will be at the middle.
- This works because slow progresses at **half the speed** of fast, so when fast has traveled the full length, slow has traveled half.
-

Dry Run (Example)

Input: head = [1, 2, 3, 4, 5]

Step	slow (value)	fast (value)	Explanation
Start	1	1	Both at head
1st Iteration	2	3	slow moves 1 step, fast moves 2 steps
2nd Iteration	3	5	slow moves 1 step, fast moves 2 steps
3rd Iteration	-	-	fast.next is None → stop

Output: slow points to 3 (the middle node).

Time and Space Complexity

- **Time Complexity:**
 - Both pointers traverse the list at most once $\rightarrow O(n)$
- **Space Complexity:**
 - Only uses two pointers $\rightarrow O(1)$

Linked List Cycle / 141

Definition for singly-linked list.

class ListNode:

def __init__(self, x):

self.val = x

self.next = None

class Solution:

def hasCycle(self, head: Optional[ListNode]) -> bool:

slow, fast = head, head

while fast and fast.next:

slow = slow.next

fast = fast.next.next

if slow is fast: # Cycle detected

return True

return False # No cycle

Why It Works

- Uses **Floyd's Cycle Detection Algorithm** (Tortoise and Hare method).
- slow moves one step, fast moves two steps.
- **Two possible outcomes:**
 1. If there is **no cycle**, fast will reach None (end of list) \rightarrow return False.
 2. If there **is a cycle**, eventually fast will "lap" slow, and they will meet \rightarrow return True.

This works because in a circular path, a faster pointer will always catch up to a slower pointer.

Dry Run (Example)

Input: head = [3, 2, 0, -4] with cycle connecting -4 \rightarrow 2

Step	slow (value)	fast (value)	Explanation

Start	3	3	Both at head
1st Iteration	2	0	slow moves 1 step, fast moves 2 steps
2nd Iteration	0	2	slow moves 1 step, fast moves 2 steps
3rd Iteration	-4	-4	slow moves 1 step, fast moves 2 steps → they meet → cycle found

Output: True

Time and Space Complexity

- **Time Complexity:**
 - Worst case: $O(n)$ (both pointers traverse nodes until they meet or fast reaches the end)
- **Space Complexity:**
 - No extra data structures used → $O(1)$

Linked List Cycle II / 142

Definition for singly-linked list.

class ListNode:

def __init__(self, x):

self.val = x

self.next = None

class Solution:

def detectCycle(self, head: Optional[ListNode]) -> Optional[ListNode]:

if not head:

return None

slow, fast = head, head

Phase 1: Detect cycle (Floyd's Tortoise & Hare)

while fast and fast.next:

slow = slow.next

fast = fast.next.next

if slow == fast:

break

else:

No cycle detected (while loop exited normally)


```
return None
```

```
# Phase 2: Find the cycle start
```

```
fast = head
```

```
while fast != slow:
```

```
    fast = fast.next
```

```
    slow = slow.next
```

```
return fast
```

Why It Works

This uses **Floyd's Cycle Detection Algorithm** with an additional step to find the **start node of the cycle**.

1. Phase 1 – Detect the Cycle:

- slow moves 1 step at a time, fast moves 2 steps.
- If slow and fast meet, a cycle exists.
- If fast reaches None, there is no cycle → return None.

2. Phase 2 – Locate the Start of Cycle:

- Reset fast to head.
- Move both slow and fast one step at a time.
- The node where they meet is the **entry point of the cycle**.

Why Phase 2 Works:

- When slow and fast first meet, slow has traveled k steps into the cycle.
- Distance from head to cycle start = a, distance from cycle start to meeting point = k.
- Resetting one pointer to head ensures they both meet at cycle_start after a steps.

Dry Run (Example)

Input: head = [3, 2, 0, -4] with cycle connecting -4 → 2

Step	slow (value)	fast (value)	Explanation
Start	3	3	Both at head
Iter 1	2	0	slow +1, fast +2
Iter 2	0	2	slow +1, fast +2
Iter 3	-4	-4	slow +1, fast +2 → meet → cycle detected
Phase 2 Start	slow = -4, fast reset = 3	-	Reset fast to head
Phase 2 Iter 1	slow = 2, fast = 2	-	They meet at 2, cycle start found

Output: Node with value 2 (start of cycle)

Time and Space Complexity

- **Time Complexity:**
 - Phase 1 takes $O(n)$ in worst case (detecting cycle).
 - Phase 2 takes at most $O(n)$ more steps to find start.
Total: $O(n)$
- **Space Complexity:**
 - Only uses two pointers $\rightarrow O(1)$

Reverse Linked List / 206

class Solution:

```
def reverseList(self, head: Optional[ListNode]) -> Optional[ListNode]:
```

```
    # Recursive approach: Time =  $O(n)$ , Space =  $O(n)$  (due to recursion stack)
```

```
    if not head:
```

```
        return None # Base case: empty list
```

```
    newHead = head
```

```
    if head.next:
```

```
        # Recursively reverse the rest of the list
```

```
        newHead = self.reverseList(head.next)
```

```
        # Reverse the current link
```

```
        head.next.next = head
```

```
        head.next = None
```

```
    return newHead
```

Why It Works

- **Recursion unwinds from the last node back to the first node.**
- Each call reverses **one link**:
 1. `newHead = self.reverseList(head.next)` reverses the sublist after head.
 2. `head.next.next = head` points the next node back to head.
 3. `head.next = None` breaks the old forward link.
- When recursion fully unwinds, `newHead` points to the new head of the reversed list.

Dry Run (Example)

Input: head = [1, 2, 3]

Recursion Level	head	newHead after recursion	Operation Performed
Call 1	1	returned from reversing [2,3]	2.next → 1, 1.next = None
Call 2	2	returned from reversing [3]	3.next → 2, 2.next = None
Call 3	3	head.next is None → return 3	Base case reached

Output: newHead = 3 → 2 → 1 → None

Time and Space Complexity

- **Time Complexity:**
 - Each node is visited once → $O(n)$
- **Space Complexity:**
 - Recursion stack holds up to n frames in worst case → $O(n)$

Remove Nth Node from End of List / 19

class Solution:

```
def removeNthFromEnd(self, head: Optional[ListNode], n: int) -> Optional[ListNode]:  
    dummy = ListNode(0)    # Dummy node simplifies edge cases  
    dummy.next = head  
    ahead = behind = dummy  
    # Move ahead pointer n+1 steps ahead  
    for _ in range(n + 1):  
        ahead = ahead.next  
    # Move both pointers until ahead reaches the end  
    while ahead:  
        ahead = ahead.next  
        behind = behind.next  
    # behind is just before the node we want to remove  
    behind.next = behind.next.next  
    return dummy.next    # Return new head
```

Why It Works

- **Dummy Node:** Handles edge cases cleanly (e.g., removing the head itself).
- **Two-pointer approach:**
 1. Move ahead pointer $n+1$ steps forward.
 2. Move ahead and behind together until ahead reaches the end.
 3. At this point, behind points to the node **just before** the node to remove.
 4. Skip the target node by `behind.next = behind.next.next`.

This guarantees exactly one pass through the list, maintaining $O(n)$ time complexity.

Dry Run (Example)

Input: head = [1, 2, 3, 4, 5], n = 2

Step	ahead (val)	behind (val)	Action
Init	dummy	dummy	Setup
Move ahead 3 steps (n+1)	ahead points to node 3	behind still dummy	Create gap of n between pointers
Iter 1	ahead → 4	behind → 1	Both move one step
Iter 2	ahead → 5	behind → 2	Both move one step
Iter 3	ahead → None	behind → 3	Stop loop
Remove	behind.next = behind.next.next → 4 skips 4	New list: 1 → 2 → 3 → 5	

Output: head = [1, 2, 3, 5]

Time and Space Complexity

- **Time Complexity:**
 - Single traversal of the list → $O(n)$
- **Space Complexity:**
 - Constant extra space (dummy + pointers) → $O(1)$

Valid Parentheses / 20

class Solution:

```
def isValid(self, s: str) -> bool:
```

```
    hashmap = {'(': '(', ')': '}', '[': '[', ']': ']'}
```

```
    stk = []
```

```
    for c in s:
```

```
        if c not in hashmap:
```

```
            stk.append(c) # Opening bracket
```

```
        else:
```

```
            if not stk or stk.pop() != hashmap[c]:
```

```
                return False
```

```
    return not stk # True if stack is empty (all matched)
```

Why It Works

- Stack-based approach:

1. Push every opening bracket ((, {, [) onto the stack.
2. When encountering a closing bracket, check:
 - If stack is empty → invalid (no opening match).
 - If top of stack is not the matching opening bracket → invalid.
 - Otherwise pop the opening bracket from the stack (pair matched).
3. At the end, if the stack is empty → all brackets matched → return True.
Otherwise → there are unmatched opening brackets → return False.

Dry Run (Example)

Input: s = "({[]})"

Step	c	Stack Before	Action	Stack After
1	([]	Push	[(
2	{	[(Push	[(, {
3	[[(, {	Push	[(, {, [
4]	[(, {, [Pop (match [)	[(, {
5	}	[(, {	Pop (match {)	[(
6)	[(Pop (match ()	[]

Output: True (all brackets matched, stack empty)

Time and Space Complexity

- **Time Complexity:**
 - Each character is processed once $\rightarrow O(n)$
- **Space Complexity:**
 - Stack holds at most n characters in worst case $\rightarrow O(n)$

Find Median from Data Stream / 295

```
import heapq
```

```
class MedianFinder:
```

```
    def __init__(self):
```

```
        # small = max heap (store as negative numbers)
```

```
        # large = min heap
```

```
        self.small, self.large = [], []
```

```
    def addNum(self, num: int) -> None:
```

```
        # Step 1: Push into max-heap (small)
```

```
        heapq.heappush(self.small, -num)
```

```
        # Step 2: Ensure order property: max(small) <= min(large)
```

```
        if self.small and self.large and (-self.small[0] > self.large[0]):
```

```
            val = -heapq.heappop(self.small)
```

```
            heapq.heappush(self.large, val)
```

```
        # Step 3: Balance sizes (difference can't exceed 1)
```

```
        if len(self.small) > len(self.large) + 1:
```

```
            val = -heapq.heappop(self.small)
```

```
            heapq.heappush(self.large, val)
```

```
        elif len(self.large) > len(self.small) + 1:
```

```
            val = heapq.heappop(self.large)
```

```
            heapq.heappush(self.small, -val)
```

```
    def findMedian(self) -> float:
```

```
        if len(self.small) > len(self.large):
```

```
            return -self.small[0]
```

```
        elif len(self.large) > len(self.small):
```

```
            return self.large[0]
```

else:

```
return (-self.small[0] + self.large[0]) / 2
```

Why It Works

- **Maintain two heaps:**
 - small (max-heap) stores the smaller half of numbers.
 - large (min-heap) stores the larger half of numbers.
- **Insertion logic:**
 1. Push number into small (max-heap using negative values).
 2. Ensure **order property**: largest in small \leq smallest in large.
 3. Balance sizes so the difference in length ≤ 1 .
- **Median calculation:**
 - If one heap is larger \rightarrow median is the top of that heap.
 - If heaps are equal \rightarrow median = average of tops.

This allows **$O(\log n)$** insertion and **$O(1)$** median retrieval.

Dry Run (Example)

Input: [1, 2, 3]

Step	small (max-heap)	large (min-heap)	Median
Add 1	[-1]	[]	1
Add 2	[-1]	[2]	$(1+2)/2 = 1.5$
Add 3	[-2, -1]	[3]	2

Time and Space Complexity

- **addNum():** $O(\log n) \rightarrow$ heap insertion and balancing
- **findMedian():** $O(1) \rightarrow$ just access heap tops
- **Space Complexity:** $O(n) \rightarrow$ all numbers stored in heaps

Spiral Matrix / 54

from typing import List

class Solution:

```
def spiralOrder(self, matrix: List[List[int]]) -> List[int]:
```

```
    res = []
```

```
    if not matrix:
```

```
        return res
```

```
    left, right = 0, len(matrix[0])
```

```
    top, bottom = 0, len(matrix)
```

```
    while left < right and top < bottom:
```

```
        # Traverse top row
```

```
        for i in range(left, right):
```

```
            res.append(matrix[top][i])
```

```
        top += 1
```

```
        # Traverse right column
```

```
        for i in range(top, bottom):
```

```
            res.append(matrix[i][right - 1])
```

```
        right -= 1
```

```
        if not (left < right and top < bottom):
```

```
            break
```

```
        # Traverse bottom row (right to left)
```

```
        for i in range(right - 1, left - 1, -1):
```

```
            res.append(matrix[bottom - 1][i])
```

```
        bottom -= 1
```

```
        # Traverse left column (bottom to top)
```

```
        for i in range(bottom - 1, top - 1, -1):
```

```
            res.append(matrix[i][left])
```

```
        left += 1
```

```
    return res
```


Why It Works

- **Maintain boundaries:** top, bottom, left, right define the current rectangle to traverse.
- **Traversal order (spiral):**
 1. Top row → left to right
 2. Right column → top to bottom
 3. Bottom row → right to left
 4. Left column → bottom to top
- After each traversal, **shrink boundaries** to move inward.
- Repeat until $\text{left} \geq \text{right}$ or $\text{top} \geq \text{bottom}$, meaning the entire matrix is traversed.

Dry Run (Example)

Input:

```
matrix = [  
  [1, 2, 3],  
  [4, 5, 6],  
  [7, 8, 9]  
]
```

Step	Operation	Added to res	Boundaries (top,bottom,left,right)
1	Top row	1,2,3	top=1, bottom=3, left=0, right=3
2	Right column	6,9	top=1, bottom=3, left=0, right=2
3	Bottom row	8,7	top=1, bottom=2, left=0, right=2
4	Left column	4	top=2, bottom=2, left=1, right=2
5	Top row	5	top=3, bottom=2, left=1, right=2 → exit loop

Output: [1,2,3,6,9,8,7,4,5]

Time and Space Complexity

- **Time Complexity:**
 - Each element visited once → $O(m \times n)$ for an $m \times n$ matrix
- **Space Complexity:**
 - Result array stores all elements → $O(m \times n)$

Set Matrix Zeroes / 73

from typing import List

class Solution:

def setZeroes(self, matrix: List[List[int]]) -> None:

ROWS, COLS = len(matrix), len(matrix[0])

rowZero = False # Whether the first row needs to be zeroed

Step 1: Use first row/col as markers

for r in range(ROWS):

for c in range(COLS):

if matrix[r][c] == 0:

matrix[0][c] = 0

if r > 0:

matrix[r][0] = 0

else:

rowZero = True

Step 2: Set zeroes based on markers (skip first row/col)

for r in range(1, ROWS):

for c in range(1, COLS):

if matrix[0][c] == 0 or matrix[r][0] == 0:

matrix[r][c] = 0

Step 3: Zero first column if needed

if matrix[0][0] == 0:

for r in range(ROWS):

matrix[r][0] = 0

Step 4: Zero first row if needed

if rowZero:

for c in range(COLS):

matrix[0][c] = 0

Why It Works

- **Goal:** Set entire row and column to 0 if a cell is 0, **in-place**.
- **Strategy:** Use **first row and first column as markers** to avoid extra space.
 1. Loop through matrix; if `matrix[r][c] == 0`, mark `matrix[0][c] = 0` and `matrix[r][0] = 0`.
 - Special handling for first row using `rowZero` boolean.
 2. Loop through matrix (excluding first row/col); if row or column marker is 0, set the cell to 0.
 3. Zero first column if `matrix[0][0] == 0`.
 4. Zero first row if `rowZero` is True.

This avoids using extra $O(m+n)$ space for marker arrays.

Dry Run (Example)

```
matrix = [  
  [1,1,1],  
  [1,0,1],  
  [1,1,1]  
]
```

Step	Operation	Matrix State
Step 1	Mark zeros	<code>[1,0,1],[0,0,1],[1,1,1]</code> → first row/col markers set
Step 2	Set zeros based on markers	<code>[1,0,1],[0,0,0],[1,0,1]</code>
Step 3	First column check	<code>matrix[0][0] != 0</code> → no change
Step 4	First row check	<code>rowZero=False</code> → no change

Time and Space Complexity

- **Time Complexity:**
 - Two nested loops over matrix → $O(m \times n)$
- **Space Complexity:**
 - Only uses variables for markers → $O(1)$ (in-place)

Two Sum

from typing import List

class Solution:

```
def twoSum(self, nums: List[int], target: int) -> List[int]:
```

```
    prevMap = {} # value -> index
```

```
    for i, n in enumerate(nums):
```

```
        diff = target - n
```

```
        if diff in prevMap:
```

```
            return [prevMap[diff], i]
```

```
    prevMap[n] = i
```

Why It Works

- **Goal:** Find indices of two numbers whose sum equals target.
- **Hash map approach:**
 1. Iterate through array, for each number n:
 - Compute $\text{diff} = \text{target} - n$.
 - Check if diff exists in prevMap.
 - If yes \rightarrow return $[\text{prevMap}[\text{diff}], i]$.
 - Otherwise, store n in prevMap with its index.
- Ensures **one-pass solution** with $O(1)$ lookup for complements.

Dry Run (Example)

Input: `nums = [2, 7, 11, 15], target = 9`

i	n	diff = target - n	prevMap	Action
0	2	7	{}	Store 2 \rightarrow prevMap = {2:0}
1	7	2	{2:0}	2 found \rightarrow return [0,1]

Output: `[0, 1]`

Time and Space Complexity

- **Time Complexity:**
 - Single pass through array $\rightarrow O(n)$
- **Space Complexity:**
 - Hash map stores up to n elements $\rightarrow O(n)$

Contains Duplicate

from typing import List

class Solution:

```
def containsDuplicate(self, nums: List[int]) -> bool:
```

```
    seen = set()
```

```
    for n in nums:
```

```
        if n in seen:
```

```
            return True
```

```
        seen.add(n)
```

```
    return False
```

Why It Works

- **Goal:** Check if the array contains any duplicates.
- **Approach:**
 1. Initialize an empty set seen.
 2. Iterate through each number n:
 - If n is already in seen, a duplicate exists → return True.
 - Otherwise, add n to seen.
 3. If the loop completes without returning, no duplicates exist → return False.
- **Rationale:** Sets allow $O(1)$ average lookup and insertion, making detection efficient.

Dry Run (Example)

Input: `nums = [1, 2, 3, 1]`

Step	n	seen before	Action	Duplicate Found?
1	1	{}	Add 1 → seen = {1}	No
2	2	{1}	Add 2 → seen = {1,2}	No
3	3	{1,2}	Add 3 → seen = {1,2,3}	No
4	1	{1,2,3}	1 in seen → return True	Yes

Output: `True`

Time and Space Complexity

- **Time Complexity:** $O(n)$ → each number checked once
- **Space Complexity:** $O(n)$ → set stores up to n elements

Valid Anagram

class Solution:

```
def isAnagram(self, s: str, t: str) -> bool:  
    return sorted(s) == sorted(t)
```

Why It Works

- **Goal:** Determine if t is an anagram of s (same letters, same frequency).
- **Approach:**
 1. Sorting both strings puts the same characters in the same order.
 2. If sorted versions are equal → all letters match in frequency → anagram.
 3. Otherwise → not an anagram.

Dry Run (Example)

Input: s = "listen", t = "silent"

Step	Operation	Result
1	sorted(s)	['e','i','l','n','s','t']
2	sorted(t)	['e','i','l','n','s','t']
3	Compare	Equal → return True

Output: True

Time and Space Complexity

- **Time Complexity:** $O(n \log n)$ → sorting each string of length n
- **Space Complexity:** $O(n)$ → storing sorted lists

Group Anagrams / 49

```
from typing import List
```

```
from collections import defaultdict
```

class Solution:

```
def groupAnagrams(self, strs: List[str]) -> List[List[str]]:  
    res = defaultdict(list) # mapping: char count -> list of anagrams  
  
    for s in strs:  
        count = [0] * 26 # 26 letters for 'a' to 'z'  
  
        for c in s:
```

```
count[ord(c) - ord("a")] += 1
```

```
res[tuple(count)].append(s)
```

```
return list(res.values())
```

Why It Works

- **Goal:** Group words that are anagrams together.
- **Approach:**
 1. Use a **character count array** of size 26 to represent each word.
 - `count[i]` = number of occurrences of letter `chr(i + ord('a'))`.
 2. Convert the count array to a **tuple** (hashable) and use it as a key in a dictionary.
 3. Words with the same character counts are grouped together in the same list.
- Efficient because it avoids sorting each string, which would take $O(k \log k)$ per word (k = length of word).

Dry Run (Example)

Input: `strs = ["eat", "tea", "tan", "ate", "nat", "bat"]`

Word	Character Count Key	Added to Dictionary
"eat"	(1,0,0,...,1,1,0...)	{"eat"}
"tea"	(1,0,0,...,1,1,0...)	{"eat", "tea"}
"tan"	(1,0,0,...,1,0,1...)	{"tan"}
"ate"	(1,0,0,...,1,1,0...)	{"eat", "tea", "ate"}
"nat"	(1,0,0,...,1,0,1...)	{"tan", "nat"}
"bat"	(1,1,0,...,1,0,0...)	{"bat"}

Output: `[["eat", "tea", "ate"], ["tan", "nat"], ["bat"]]`

Time and Space Complexity

- **Time Complexity:** $O(n \times k)$
 - n = number of words, k = max length of a word
 - Counting characters is $O(k)$ per word, appending to dictionary is $O(1)$
- **Space Complexity:** $O(n \times k)$
 - Storage for dictionary and result lists

Top K Frequent Elements / 347

from typing import List

class Solution:

```
def topKFrequent(self, nums: List[int], k: int) -> List[int]:  
    count = {}  
    freq = [[] for _ in range(len(nums) + 1)]  
    # Count frequency of each number  
    for n in nums:  
        count[n] = 1 + count.get(n, 0)  
    # Bucket sort: place numbers into their frequency index  
    for n, c in count.items():  
        freq[c].append(n)  
    res = []  
    # Traverse buckets from highest freq to lowest  
    for i in range(len(freq) - 1, 0, -1):  
        for n in freq[i]:  
            res.append(n)  
            if len(res) == k:  
                return res
```

Why It Works

- **Goal:** Find k elements that appear most frequently in the array.
- **Approach:**
 1. Count the frequency of each element using a dictionary (count).
 2. Use **bucket sort**:
 - Create a list of lists freq where freq[i] contains elements that appear exactly i times.
 3. Traverse freq from **highest frequency to lowest**:
 - Collect elements until we have k elements.
- Efficient because we avoid full sorting by frequency and exploit the limited range (max frequency $\leq n$).

Dry Run (Example)

Input: nums = [1,1,1,2,2,3], k = 2

1. Count frequencies → count = {1:3, 2:2, 3:1}
2. Bucket sort → freq = [[], [3], [2], [1], [], [], []] (indices = frequencies)
3. Traverse freq from high →
 - i=3 → add 1 → res = [1]
 - i=2 → add 2 → res = [1,2] → k=2 reached → return [1,2]

Output: [1,2] (order can vary among same-frequency elements)

Time and Space Complexity

- **Time Complexity:** $O(n)$
 - Counting frequencies → $O(n)$
 - Bucket sort insertion → $O(n)$
 - Collect top k → $O(n)$ in worst case
- **Space Complexity:** $O(n)$
 - Dictionary + bucket array + result list

Is Subsequence / 392

class Solution:

```
def isSubsequence(self, s: str, t: str) -> bool:
```

```
    i, j = 0, 0
```

```
    while i < len(s) and j < len(t):
```

```
        if s[i] == t[j]:
```

```
            i += 1
```

```
            j += 1 # always move j forward
```

```
    return i == len(s)
```

Why It Works

- **Goal:** Determine if s is a subsequence of t.
- **Approach:** Two-pointer technique:
 1. i tracks position in s, j tracks position in t.
 2. Iterate through t (j moves forward always):
 - If $t[j] == s[i]$, move i forward (match found).
 - If not, just move j forward.

3. After traversal, if $i == \text{len}(s)$, all characters of s were found in order $\rightarrow \text{True}$.
Otherwise $\rightarrow \text{False}$.

- **Rationale:** Only order matters; characters in between are ignored.

Dry Run (Example)

Input: $s = \text{"abc"}, t = \text{"ahbgdc"}$

i	j	s[i]	t[j]	Action
0	0	a	a	match $\rightarrow i=1, j=1$
1	1	b	h	no match $\rightarrow j=2$
1	2	b	b	match $\rightarrow i=2, j=3$
2	3	c	g	no match $\rightarrow j=4$
2	4	c	d	no match $\rightarrow j=5$
2	5	c	c	match $\rightarrow i=3, j=6$

Output: $i = \text{len}(s) = 3 \rightarrow \text{True}$

Time and Space Complexity

- **Time Complexity:** $O(\text{len}(t)) \rightarrow$ single pass through t
- **Space Complexity:** $O(1) \rightarrow$ only pointers i and j used

Product of Array Except Self / 238

```
from typing import List
```

```
class Solution:
```

```
    def productExceptSelf(self, nums: List[int]) -> List[int]:
```

```
        res = [1] * len(nums)
```

```
        prefix = 1
```

```
        for i in range(len(nums)):
```

```
            res[i] = prefix
```

```
            prefix *= nums[i]
```

```
        postfix = 1
```

```
        for i in range(len(nums) - 1, -1, -1):
```

```
            res[i] *= postfix
```

```
            postfix *= nums[i]
```

```
        return res
```

Why It Works

- **Goal:** Compute $\text{res}[i]$ = product of all $\text{nums}[j]$ except $\text{nums}[i]$ **without division**.
- **Approach:** Use **prefix and postfix products**:
 1. **Prefix pass:** $\text{res}[i]$ = product of all elements before i .
 - Keep a running prefix product.
 2. **Postfix pass:** Multiply $\text{res}[i]$ by product of all elements after i .
 - Keep a running postfix product from the end.
- This ensures each $\text{res}[i]$ = product of all elements except itself.

Dry Run (Example)

Input: $\text{nums} = [1, 2, 3, 4]$

i	prefix	res[i]	prefix after
0	1	1	$1 * 1 = 1$
1	1	1	$1 * 2 = 2$
2	2	2	$2 * 3 = 6$
3	6	6	$6 * 4 = 24$

res after prefix: $[1, 1, 2, 6]$

Postfix pass:

i	postfix	res[i]	postfix after
3	1	$6 * 1 = 6$	$1 * 4 = 4$
2	4	$2 * 4 = 8$	$4 * 3 = 12$
1	12	$1 * 12 = 12$	$12 * 2 = 24$
0	24	$1 * 24 = 24$	$24 * 1 = 24$

Output: $[24, 12, 8, 6]$

Time and Space Complexity

- **Time Complexity:** $O(n)$ → two passes through the array
- **Space Complexity:** $O(1)$ extra (res array does not count as extra)

Sum of Two Integers / 371

class Solution:

```
def getSum(self, a: int, b: int) -> int:

    while b != 0:

        c = a & b    # carry: bits where both a and b are 1

        a = a ^ b    # sum without carry (XOR)

        b = c << 1   # shift carry left to add in next iteration

    return a
```

Why It Works

- **Goal:** Compute $a + b$ without using $+$ or $-$.
- **Approach:** Simulate bitwise addition.
 1. $a \oplus b$ gives sum of bits without considering carry (like binary addition ignoring carry).
 2. $a \& b$ gives positions where carry will be generated (both bits are 1).
 3. Left shift the carry ($c \ll 1$) to add it in the next higher bit position.
 4. Repeat until carry (b) becomes zero \rightarrow no more carry to add.
- This is exactly how hardware performs binary addition.

Dry Run (Example)

Input: $a = 5$ (0101), $b = 3$ (0011)

Step	a (bin)	b (bin)	c = a&b	a = a^b	b = c<<1
Init	0101	0011	-	-	-
1	0101	0011	0001	0110	0010
2	0110	0010	0010	0100	0100
3	0100	0100	0100	0000	1000
4	0000	1000	0000	1000	0000

Output: $a = 1000$ (8)

Time and Space Complexity

- **Time Complexity:** $O(1)$ (bounded by number of bits \rightarrow 32 iterations max for 32-bit integers)
- **Space Complexity:** $O(1)$ (uses only variables a, b, c)

