

## Lecture 12 Parsing

Slides by Graham Farr (2017), with some by David Albrecht (2011).

FIT2014 Theory of Computation

## Overview

- Definitions
- Examples
- Shift-reduce parser
- Lex & Yacc

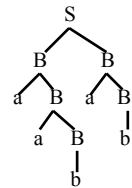
## Parsing

- Suppose you have a Context Free Grammar, and a string of letters.
- **Parsing:** determining whether the string
  - is a word in the language, and if it is,
  - finding a **parse tree**, or a **derivation**, for it.
- **Parser:** a program that does this.
- Two main types:
  - **Top-down parsers**
  - **Bottom-up parsers**
    - **reduce** the string to the Start symbol
    - repeatedly apply production rules in reverse

$a^*ba^*b$

$S \rightarrow BB$   
 $B \rightarrow aB$   
 $B \rightarrow b$

Input: aabab

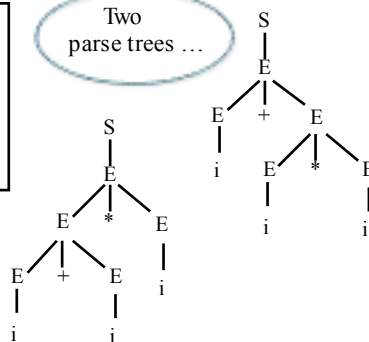


## Plus-Times-A

Input:  $i + i * i$

$S \rightarrow E$  (1)  
 $E \rightarrow E + E$  (2)  
 $E \rightarrow E * E$  (3)  
 $E \rightarrow i$  (4)

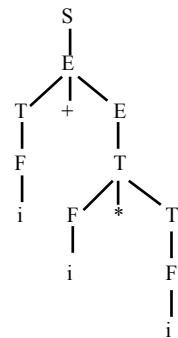
This grammar is ambiguous.



## Plus-Times-B

Input:  $i + i * i$

$S \rightarrow E$   
 $E \rightarrow T + E$   
 $E \rightarrow T$   
 $T \rightarrow F * T$   
 $T \rightarrow F$   
 $F \rightarrow i$



## LR Parser

- Bottom-up Parser
- Scan input **Left to Right**
- Construct a **Rightmost** derivation in reverse
- Implemented using a Deterministic Pushdown Automaton (DPDA).
- Not all CFGs have one: DCFL  $\neq$  CFL
- We'll look at one type of LR parser: **shift-reduce parser**

## Shift-reduce Parser

- a particular type of LR Parser
- Has:
  - a **stack**: terminals and non-terminals processed so far, and
  - a **buffer**: the rest of the input string (yet to be processed)
- Initially:
  - Stack is empty
  - Buffer contains the entire input string
- Repeatedly ...
  - **Shift** input letters onto the stack, OR
  - When a string of top-most stack symbols equal the right-hand side of a production rule:
    - **Reduce** that string, i.e., use production rule in reverse
- ...until Stack only has Start symbol, and Buffer is empty.

**a\*b\*a\*b**

Input: abb

$S \rightarrow BB$  (1)  
 $B \rightarrow aB$  (2)  
 $B \rightarrow b$  (3)

	abb	shift
a	bb	shift
ab	b	reduce, (3)
aB	b	reduce, (2)
B	b	shift
Bb		reduce, (3)
BB		reduce, (1)
S		ACCEPT

**Plus-Times-A**

Input: i + i\*i

$S \rightarrow E$  (1)  
 $E \rightarrow E + E$  (2)  
 $E \rightarrow E * E$  (3)  
 $E \rightarrow i$  (4)

	i+i*i	shift
i	+i*i	reduce, (4)
E	+i*i	shift
E+	i*i	shift
E+i	*i	reduce, (4)
E+E	*i	

*To shift, or  
to reduce?*

**Plus-Times-A**

Input: i + i\*i

$S \rightarrow E$  (1)  
 $E \rightarrow E + E$  (2)  
 $E \rightarrow E * E$  (3)  
 $E \rightarrow i$  (4)

	i+i*i	shift
i	+i*i	reduce, (4)
E	+i*i	shift
E+	i*i	shift
E+i	*i	reduce, (4)
E+E	*i	shift
E+E*	i	shift
E+E*i		reduce, (4)
E+E*i		reduce, (3)
E+E		reduce, (2)
E		reduce, (1)
S		ACCEPT

**Plus-Times-A**

Input: i + i\*i

$S \rightarrow E$  (1)  
 $E \rightarrow E + E$  (2)  
 $E \rightarrow E * E$  (3)  
 $E \rightarrow i$  (4)

	i+i*i	shift
i	+i*i	reduce, (4)
E	+i*i	shift
E+	i*i	shift
E+i	*i	reduce, (4)
E+E	*i	

*To shift, or  
to reduce?*

## Plus-Times-A

Input:  $i + i * i$

$S \rightarrow E$  (1)  
 $E \rightarrow E + E$  (2)  
 $E \rightarrow E * E$  (3)  
 $E \rightarrow i$  (4)

	$i + i * i$	shift
i	$+ i * i$	reduce, (4)
E	$+ i * i$	shift
E+	$i * i$	shift
E+i	$* i$	reduce, (4)
E+E	$* i$	reduce, (2)
E	$* i$	shift
E*	i	shift
E*i		reduce, (4)
E*iE		reduce, (3)
E		reduce, (1)
S		ACCEPT

→ shift-reduce conflict.  
 Also: reduce-reduce conflict: letters on top of stack correspond to more than one production rule.

## Yacc

- Yet Another Compiler-Compiler
- A parser-generator
- Input: a Context-Free Grammar ...
- Output: parser, in file `y.tab.c`
- Typically used with a lexical analyser, e.g., Lex.

## Lex

- Lexical Analyser
- Input: regular expression for each token ...
- Output: lexical analyser, in file `lex.yy.c`
- Both are widely available in Unix/Linux

## Lex: lexical analysis

filename.l

definitions ...  
 %%  
 regexps + code, for each token ...  
 %%  
 C code ...

lex

lex.yy.c

..... yylex() .....

## Yacc: parser generation

Filename.y

declarations (incl. token names) ...  
 %%  
 Grammar: production rules ...  
 %%  
 C code ...

yacc

y.tab.c

..... yyparse() .....

calls yylex()  
to get tokens

## Lex & Yacc

- Compile `y.tab.c` and `lex.yy.c` using, say, `cc`.
- Obtain an executable parser.
- It can evaluate as it parses.
- See Assignment 2.
- Conflict resolution in Yacc:
  - Shift-reduce: shift
  - Reduce-reduce: use the rule listed first.

## Revision

- Construct a parse tree for given string and grammar.
- Understand how a Shift-reduce Parser works.
- Start using Lex and Yacc.