



Lecture 12

Parsing

Slides by Graham Farr (2017), with some by David Albrecht (2011).

FIT2014 Theory of Computation



Overview

- Definitions
- Examples
- Shift-reduce parser
- Lex & Yacc

Parsing

- Suppose you have a Context Free Grammar, and a string of letters.
- **Parsing:** determining whether the string
 - is a word in the language, and if it is,
 - finding a **parse tree**, or a **derivation**, for it.
- **Parser:** a program that does this.
- Two main types:
 - **Top-down parsers**
 - **Bottom-up parsers**
 - **reduce** the string to the Start symbol
 - repeatedly apply production rules in reverse

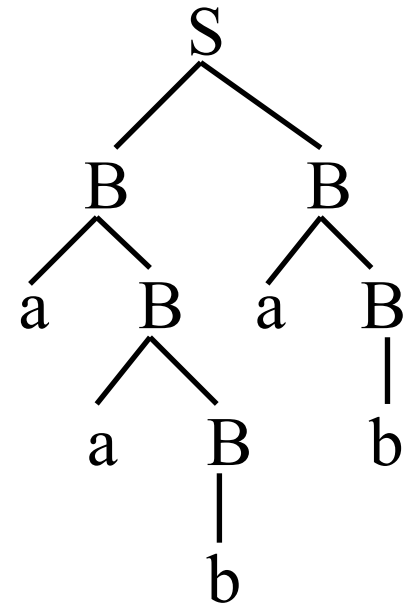
a^*ba^*b

$S \rightarrow BB$

$B \rightarrow aB$

$B \rightarrow b$

Input: aabab



Plus-Times-A

Input: $i + i * i$

$S \rightarrow E$ (1)

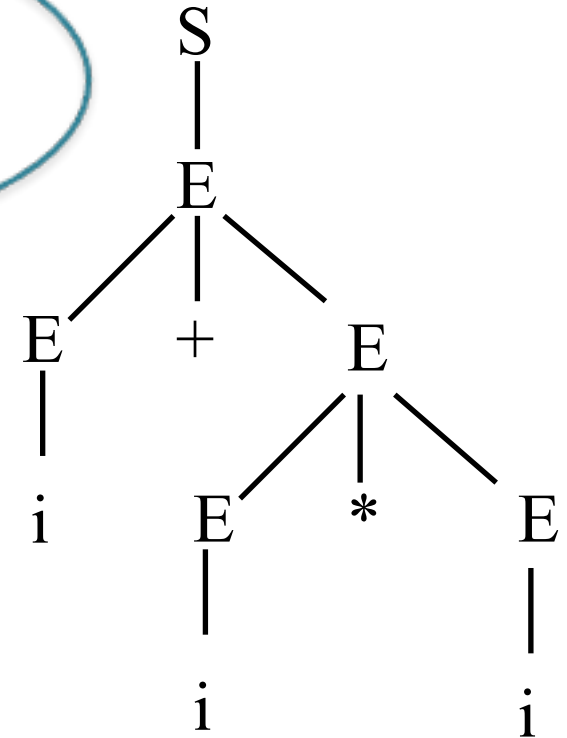
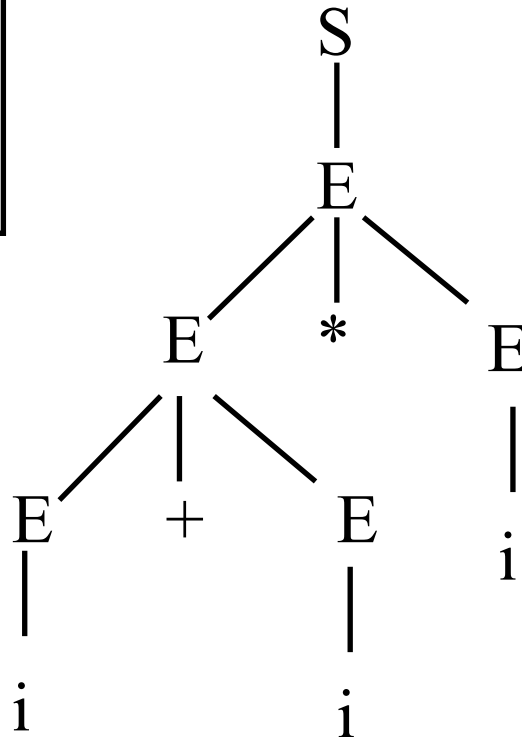
$E \rightarrow E + E$ (2)

$E \rightarrow E * E$ (3)

$E \rightarrow i$ (4)

This grammar is
ambiguous.

Two
parse trees ...



Plus-Times-B

$S \rightarrow E$

$E \rightarrow T + E$

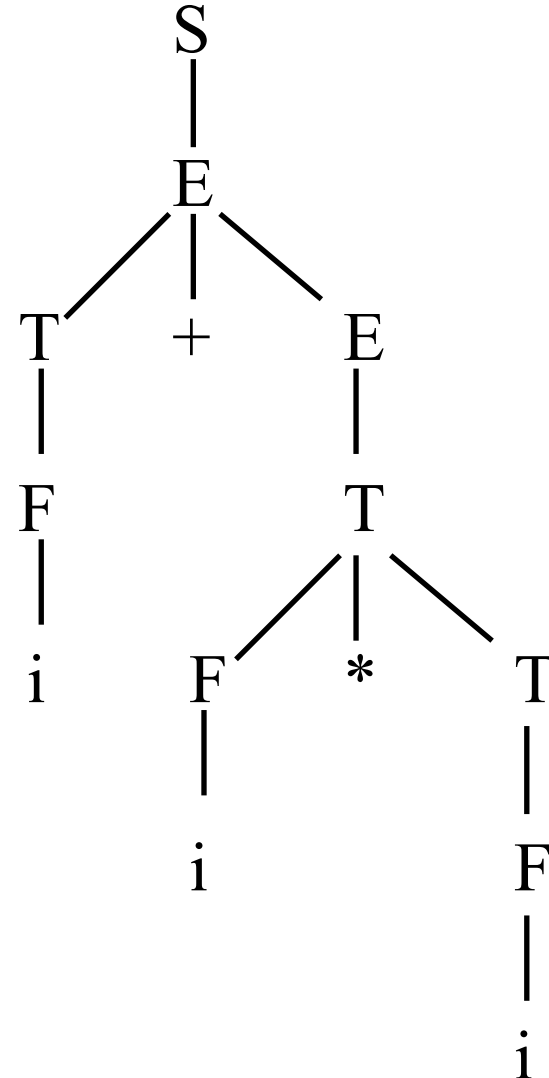
$E \rightarrow T$

$T \rightarrow F * T$

$T \rightarrow F$

$F \rightarrow i$

Input: $i + i * i$



LR Parser

- Bottom-up Parser
- Scan input **L**eft to Right
- Construct a **R**ightmost derivation in reverse
- Implemented using a Deterministic Pushdown Automaton (DPDA).
- Not all CFGs have one: $DCFL \neq CFL$
- We'll look at one type of LR parser:
shift-reduce parser

Shift-reduce Parser

- a particular type of LR Parser
- Has:
 - a **stack**: terminals and non-terminals processed so far, and
 - a **buffer**: the rest of the input string (yet to be processed)
- Initially:
 - Stack is empty
 - Buffer contains the entire input string
- Repeatedly ...
 - **Shift** input letters onto the stack, *OR*
 - When a string of top-most stack symbols equal the right-hand side of a production rule:
 - **Reduce** that string, i.e., use production rule in reverse
- ...until Stack only has Start symbol, and Buffer is empty.

$a*ba*b$

Input: abb

$S \rightarrow BB$ (1)

$B \rightarrow aB$ (2)

$B \rightarrow b$ (3)

	abb	shift
a	bb	shift
ab	b	reduce, (3)
aB	b	reduce, (2)
B	b	shift
Bb		reduce, (3)
BB		reduce, (1)
S		ACCEPT

Plus-Times-A

Input: $i + i * i$

$S \rightarrow E$ (1)

$E \rightarrow E + E$ (2)

$E \rightarrow E * E$ (3)

$E \rightarrow i$ (4)

	$i + i * i$	shift
i	$+ i * i$	reduce, (4)
E	$+ i * i$	shift
E +	$i * i$	shift
E + i	$* i$	reduce, (4)
E + E	$* i$	

*To shift, or
to reduce?*

Plus-Times-A

Input: $i + i * i$

$S \rightarrow E$ (1)

$E \rightarrow E + E$ (2)

$E \rightarrow E * E$ (3)

$E \rightarrow i$ (4)

	$i + i * i$	shift
i	$+ i * i$	reduce, (4)
E	$+ i * i$	shift
E +	$i * i$	shift
E + i	$* i$	reduce, (4)
E + E	$* i$	shift
E + E *	i	shift
E + E * i		reduce, (4)
E + E * E		reduce, (3)
E + E		reduce, (2)
E		reduce, (1)
S		ACCEPT

Plus-Times-A

Input: $i + i * i$

$S \rightarrow E$ (1)

$E \rightarrow E + E$ (2)

$E \rightarrow E * E$ (3)

$E \rightarrow i$ (4)

	$i + i * i$	shift
i	$+ i * i$	reduce, (4)
E	$+ i * i$	shift
E +	$i * i$	shift
E + i	$* i$	reduce, (4)
E + E	$* i$	

*To shift, or
to reduce?*

Plus-Times-A

Input: $i + i * i$

$S \rightarrow E$ (1)

$E \rightarrow E + E$ (2)

$E \rightarrow E * E$ (3)

$E \rightarrow i$ (4)

	$i+i*i$	shift
i	$+i*i$	reduce, (4)
E	$+i*i$	shift
E+	$i*i$	shift
E+i	$*i$	reduce, (4)
E+E	$*i$	reduce, (2)
E	$*i$	shift
E*	i	shift
E*i		reduce, (4)
E*E		reduce, (3)
E		reduce, (1)
S		ACCEPT

→ **shift-reduce conflict.**

Also: **reduce-reduce conflict:** letters on top of stack correspond to more than one production rule.

Yacc

- **Yet Another Compiler-Compiler**
- **A parser-generator**
- Input: a Context-Free Grammar ...
- Output: parser, in file `y.tab.c`
- Typically used with a lexical analyser, e.g., **Lex**.

Lex

- **Lexical Analyser**
- Input: regular expression for each token ...
- Output: lexical analyser, in file `lex.yy.c`
- Both are widely available in Unix/Linux

Lex: lexical analysis

filename.l

definitions ...

%%

regexps + code, for each token ...

%%

C code ...

lex

lex.yy.c

..... yylex()

Yacc: parser generation

Filename.y

declarations (incl. token names) ...

%%

Grammar: production rules ...

%%

C code ...

yacc

y.tab.c

..... yyparse()

calls yylex()
to get tokens

Lex & Yacc

- Compile `y.tab.c` and `lex.yy.c` using, say, `cc`.
- Obtain an executable parser.
- It can evaluate as it parses.
- See Assignment 2.

- Conflict resolution in Yacc:
 - Shift-reduce: shift
 - Reduce-reduce: use the rule listed first.

Revision

- Construct a parse tree for given string and grammar.
- Understand how a Shift-reduce Parser works.
- Start using Lex and Yacc.