Lecture 31 Collision Resolution II

FIT 1008 Introduction to Computer Science



```
def insert(self, key, data):
    position = self.hash(key)
    for _ in range(self.table_size):
        if self.array[position] is None: # found empty slot
            self.array[position] = (key, data)
            self.count += 1
            return
        elif self.array[position][0] == key: # found key
            self.array[position] = (key, data)
            return
        else: # not found, try next
            position = (position + 1) % self.table_size
    self.rehash()
    self.insert(key, data)
```

```
def __setitem__(self, key, data):
    position = self.hash(key)
    for _ in range(self.table_size):
        if self.array[position] is None: # found empty slot
            self.array[position] = (key, data)
            self.count += 1
            return
        elif self.array[position][0] == key: # found key
            self.array[position] = (key, data)
            return
        else: # not found, try next
            position = (position + 1) % self.table_size
    self.rehash()
    self.__setitem__(key, data)
```

```
def __str__(self):
    result = ""
    for item in self.array:
        if item is not None:
            (key, value) = item
            result += "(" + str(key) + "," + str(value) + ")"
    return result
```

Open Addressing: Linear Probing

- Search for an item with hash value N:
 - Perform a linear search from array[N] until either the item or an empty space is found
- But careful, you must deal again with:
 - Full table (to avoid going into an infinite loop)
 - Restarting from position 0 if the end of table is reached.

search(key)

- Get the position N using the hash function, N = hash(key)
- If array[N] is empty return None.
- → If there is <u>already an item there</u>:
 - → If there is already something there, with the **same key** return the associated data.
 - If there is already something there with a different key, you need to find the key and return data

__setitem_(self, key, data)

insert or update item (key, data)

__getitem_(self, key)

give me the data associated to a key

```
def __getitem__(self, key):
```

```
def __getitem__(self, key):
    position = self.hash_value(key)
```

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```

Get position using hash function

```
def __getitem__(self, key):
    position = self.hash_value(key)

    if self.array[position] is None: # found empty slot
        raise KeyError(key)
```

```
def __getitem__(self, key):
    position = self.hash_value(key)

    if self.array[position] is None: # found empty slot
        raise KeyError(key)
```

If there is nothing in the corresponding position...

```
def __getitem__(self, key):
    position = self.hash_value(key)

    elif self.array[position][0] == key: # found it
        return self.array[position][1]
```

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def __getitem__(self, key):
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```

If the key is found return the data

```
the key of the tuple
    currently living at
    array[position]

elif self.array[position][0] == key: # found it
    return self.array[position][1]
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If the key is found return the data

```
the key of the tuple
                                                      currently living at
def __getitem__(self, key):
                                                       array[position]
    position = self.hash_value(key)
         elif self.array[position][0] == key:
                                                   # found it
             return self.array[position][1]
                                                    the data of the tuple
                                                      currently living at
                                                       array[position]
```

If the key is found return the data

```
def __getitem__(self, key):
    position = self.hash_value(key)
```

```
else:
    # there is something there, but different key
    # linear probing, so try next position
    position = (position + 1) % self.table_size
```

keep searching

```
def __getitem__(self, key):
    position = self.hash_value(key)
    for _ in range(self.table_size):

    else:
        # there is something there, but different key
        # linear probing, so try next position
        position = (position + 1) % self.table_size
```

keep searching for at most *table_size* positions

```
def __getitem__(self, key):
    position = self.hash_value(key)
    for _ in range(self.table_size):
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            raise KeyError(key)
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        else:
            # there is something there, but different key
            # linear probing, so try next position
            position = (position + 1) % self.table_size
        raise KeyError(key)
```

raise a KeyError if the item is not found

```
def __getitem__(self, key):
    position = self.hash_value(key)
    for _ in range(self.table_size):
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```

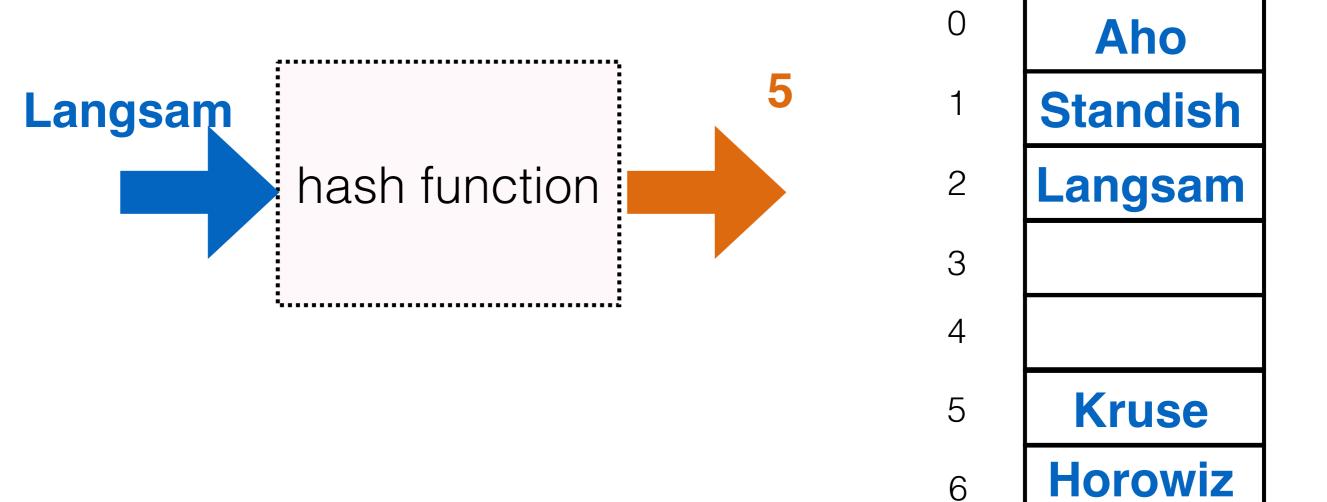
key: Langsam

hash function

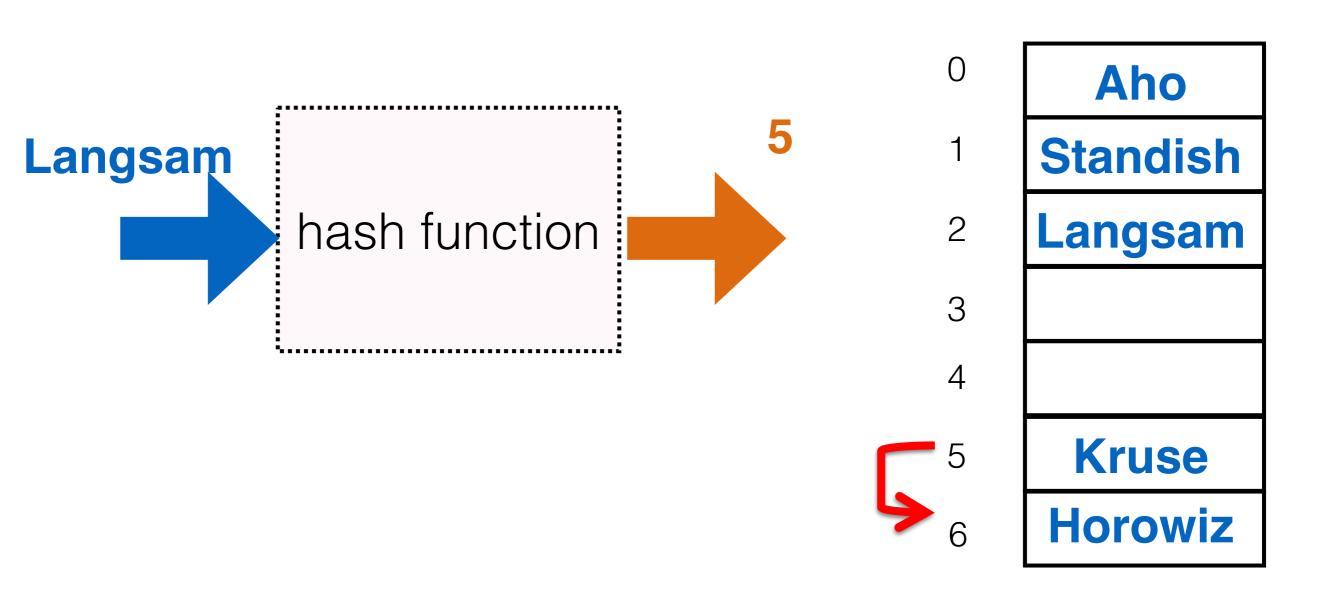
hash table

Aho
Standish
Langsam
Kruse
Horowiz

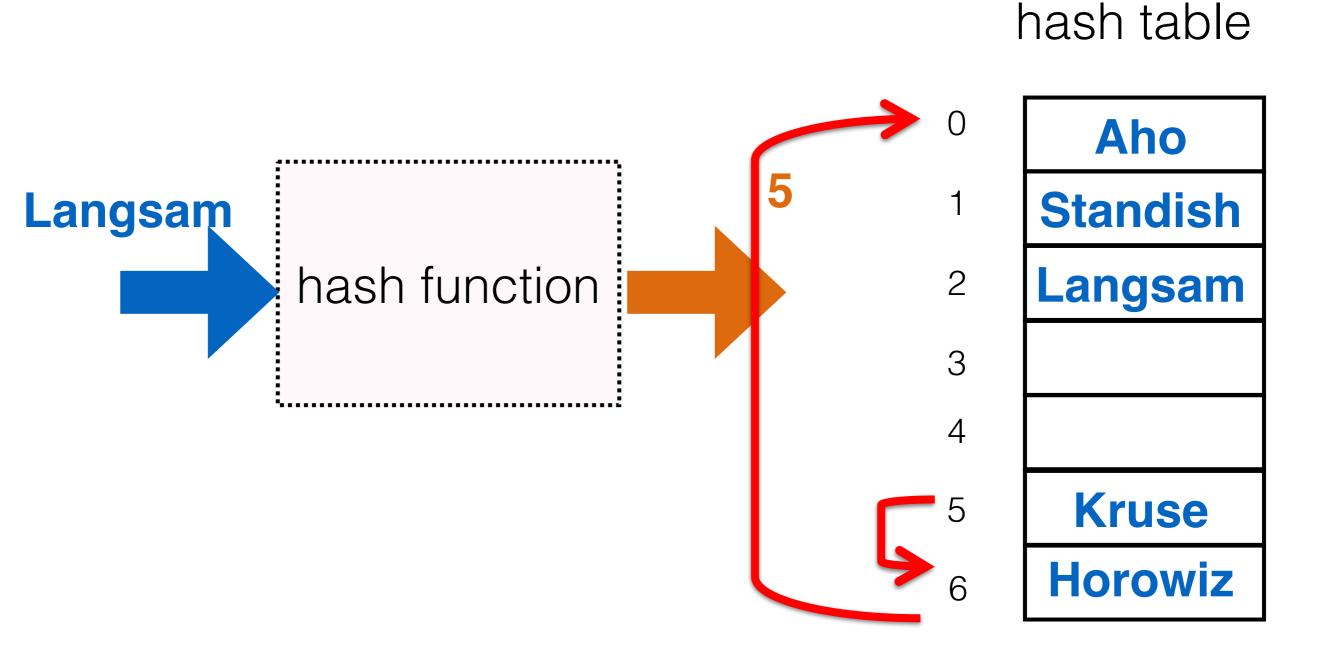
key: Langsam



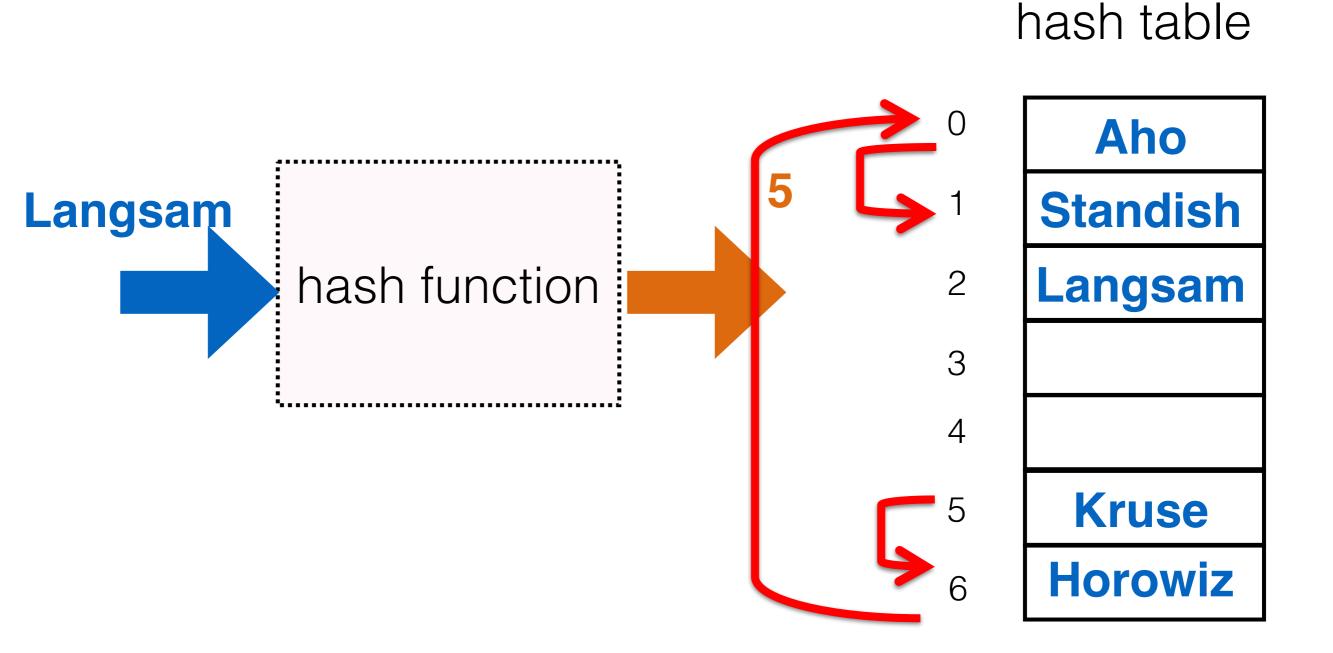
key: Langsam



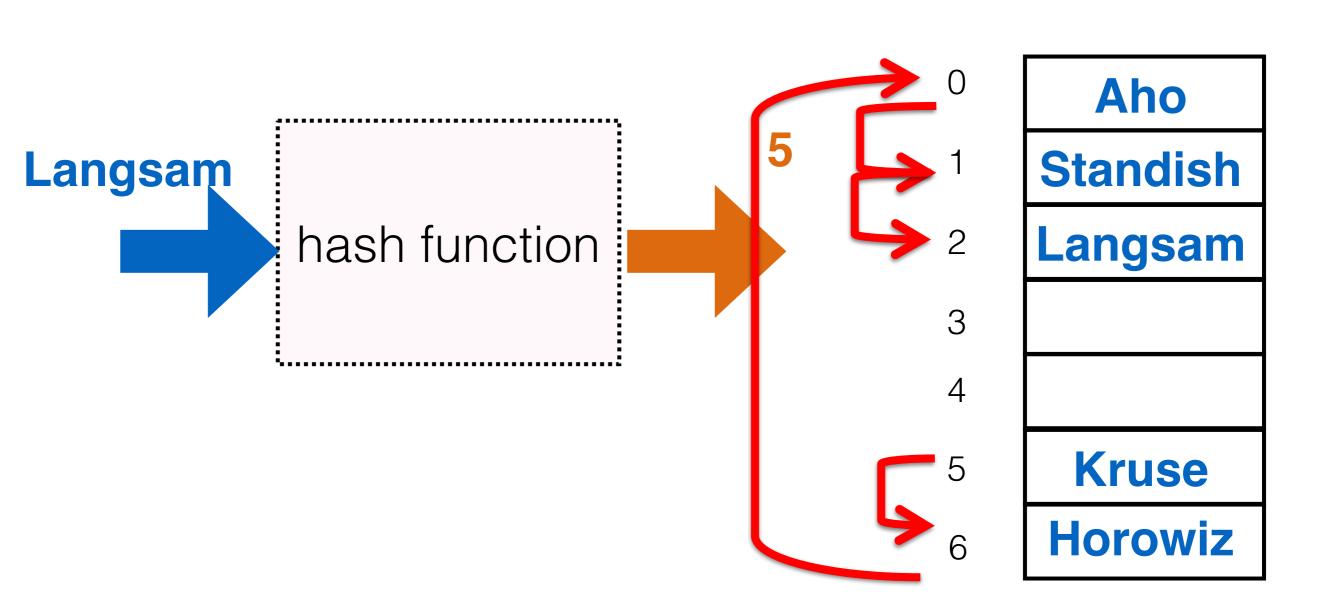
key: Langsam



key: Langsam



key: Langsam



key: Langsam

hash table

Aho **Standish** Langsam hash function Langsam 3 Kruse Found after probe chain of length 4 **Horowiz**

key: Knuth

hash function

hash table

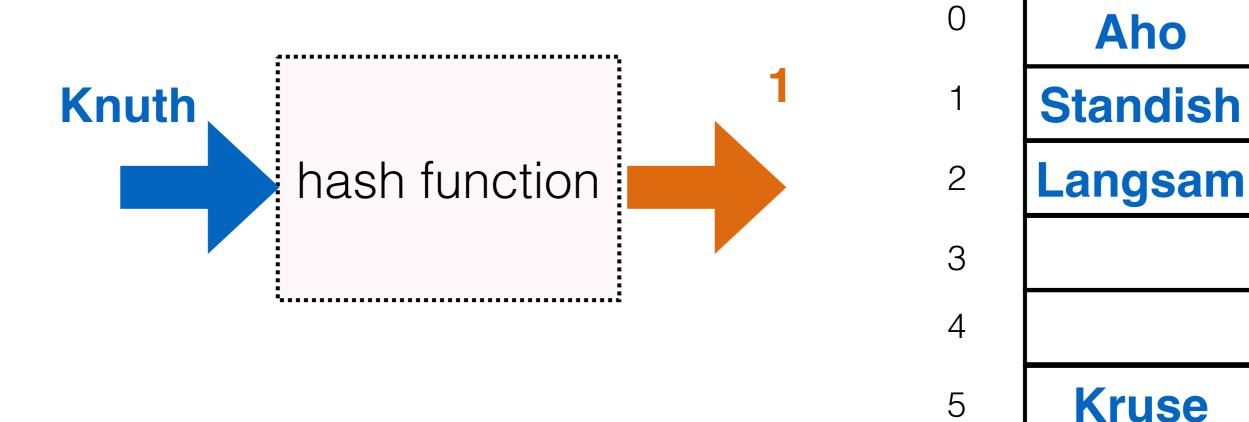
Aho
Standish
Langsam
Kruse
Horowiz

key: Knuth

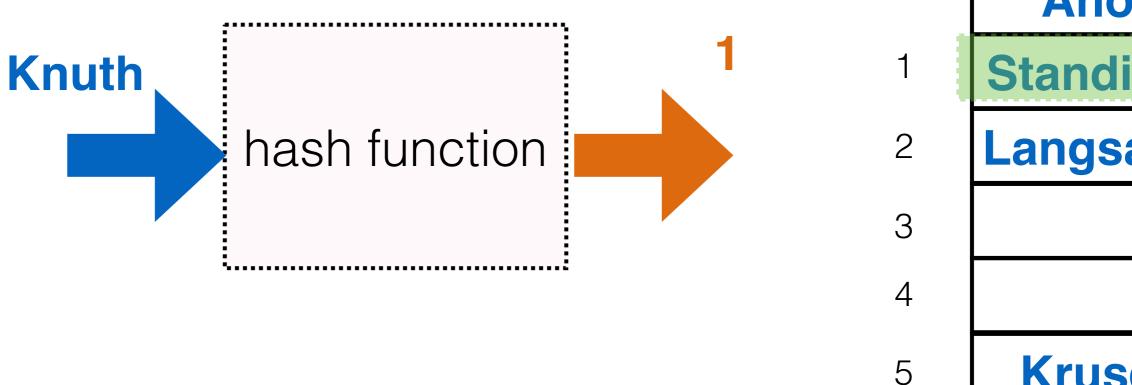
hash table

Horowiz

6



key: Knuth



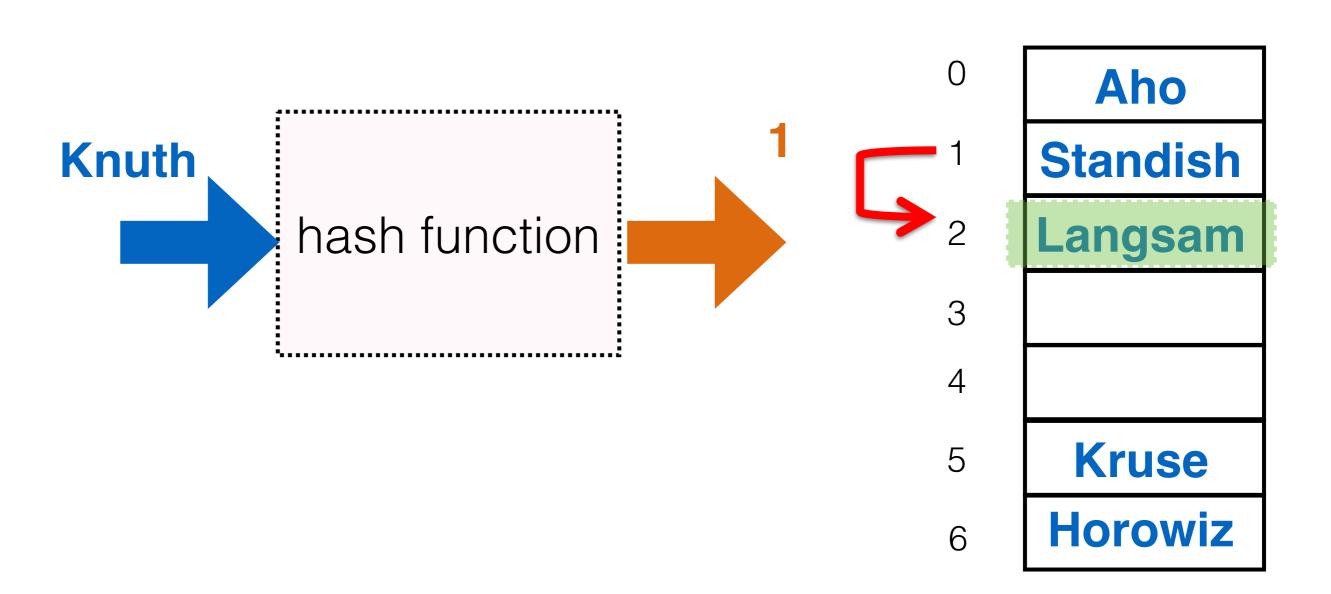
hash table

0

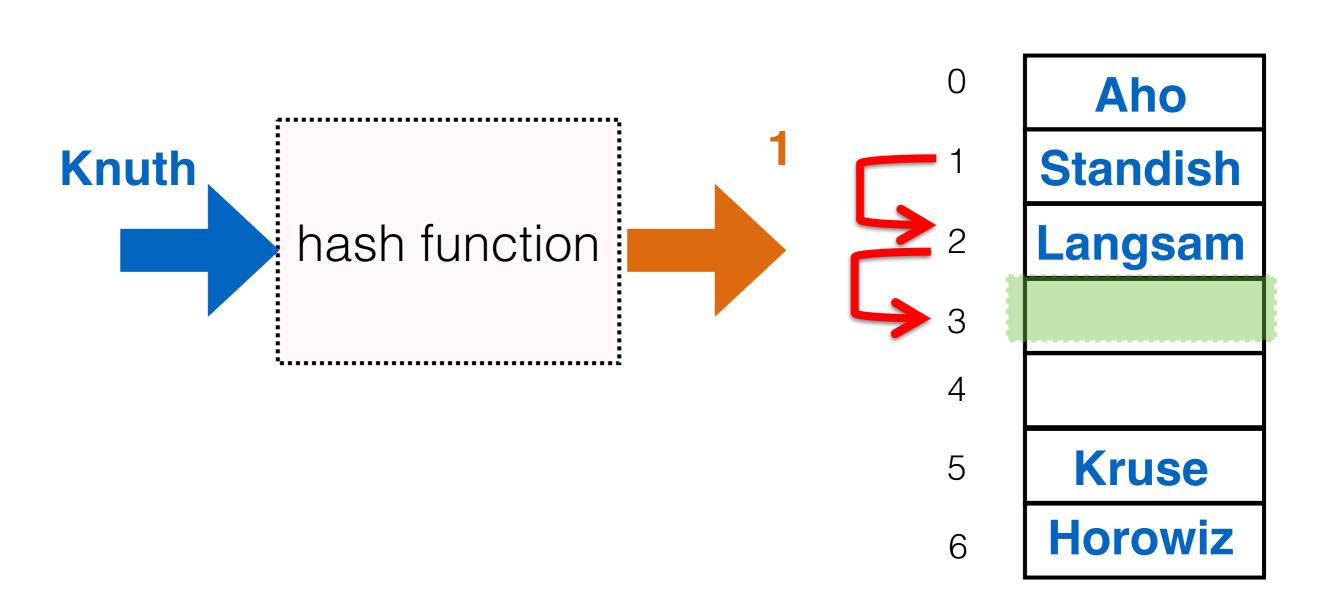
6

Aho **Standish** Langsam Kruse **Horowiz**

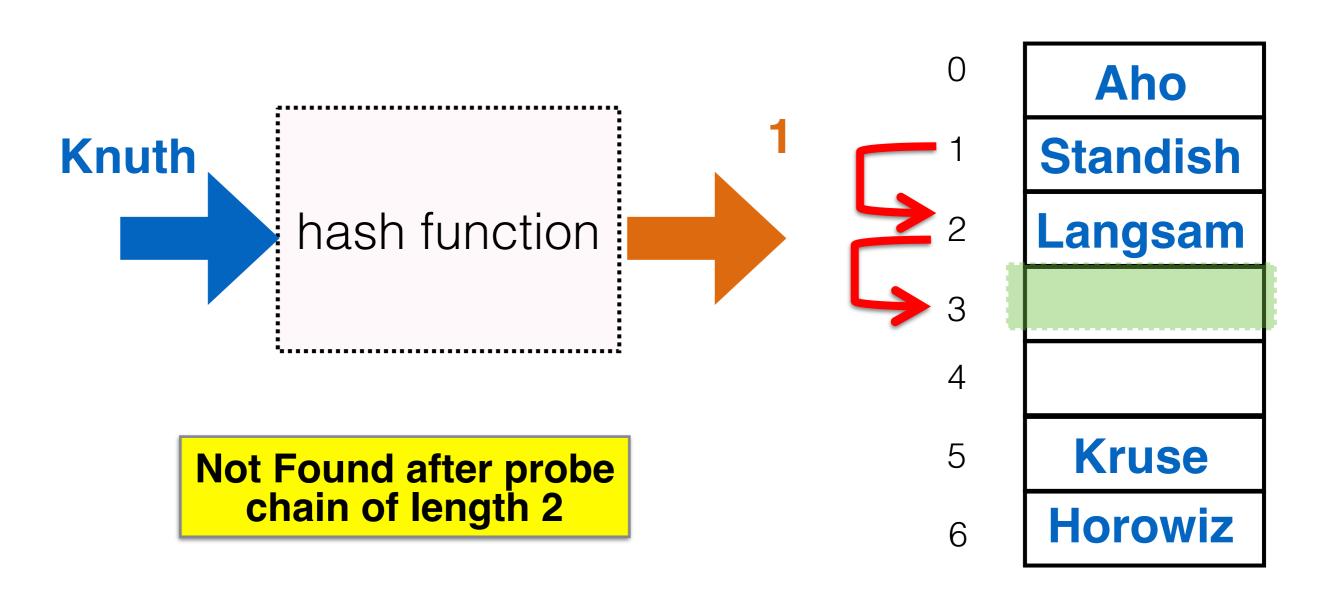
key: Knuth



key: Knuth



key: Knuth



```
def __setitem__(self, key, data):
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   self.rehash()
   self. setitem (key, data)
 def __getitem__(self, key):
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```

Idea: use a function for linear probe, make it more compact

Open Addressing: Linear Probing

- What about delete?
- One possibility:
 - Use the search function to find the item
 - If found at N delete and reinsert every item from N+1 to the first empty position

Time consuming! (though should not be many)

What if I do not reinsert?

search may incorrectly report some items as not found

key: Kruse

hash function

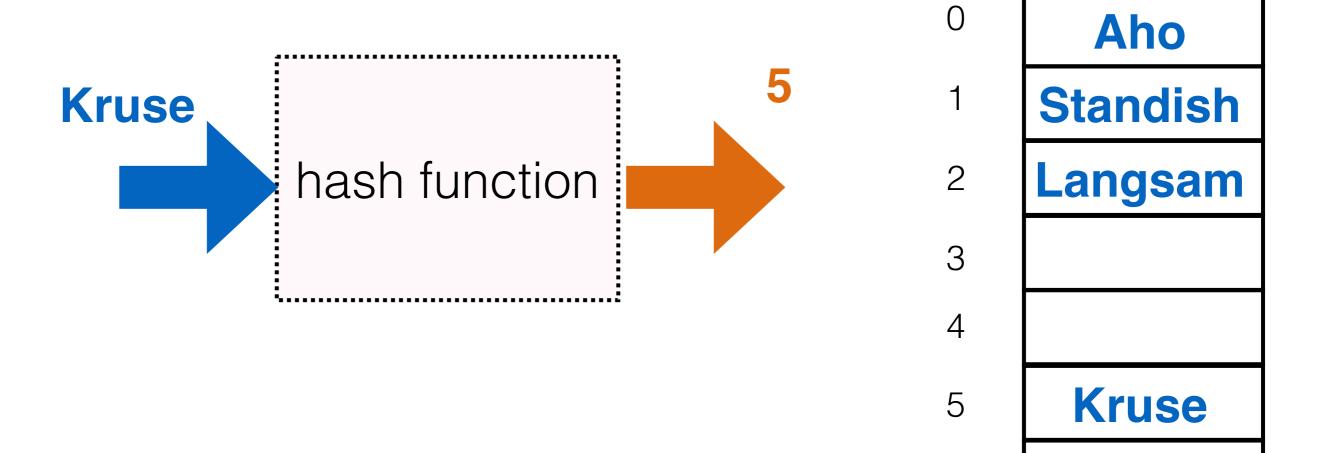
hash table

Aho
Standish
Langsam
Kruse
Horowiz

key: Kruse

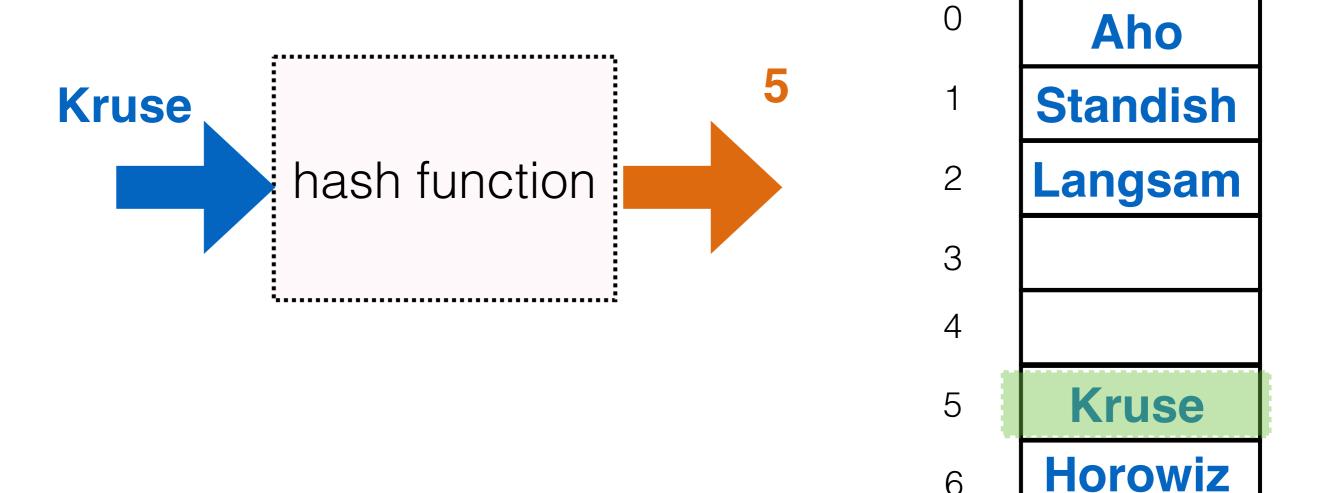
hash table

Horowiz



key: Kruse

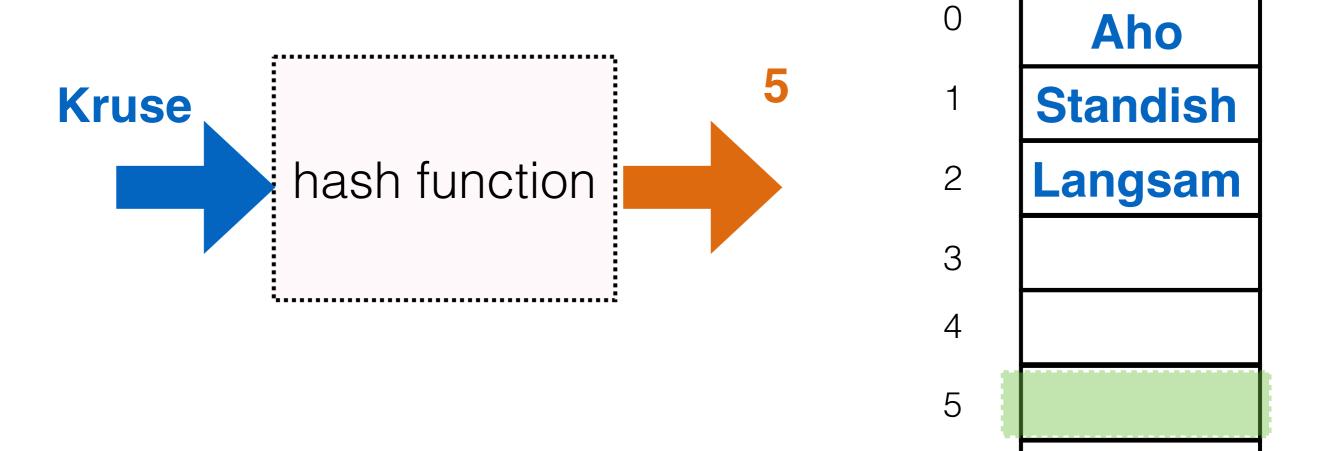
hash table

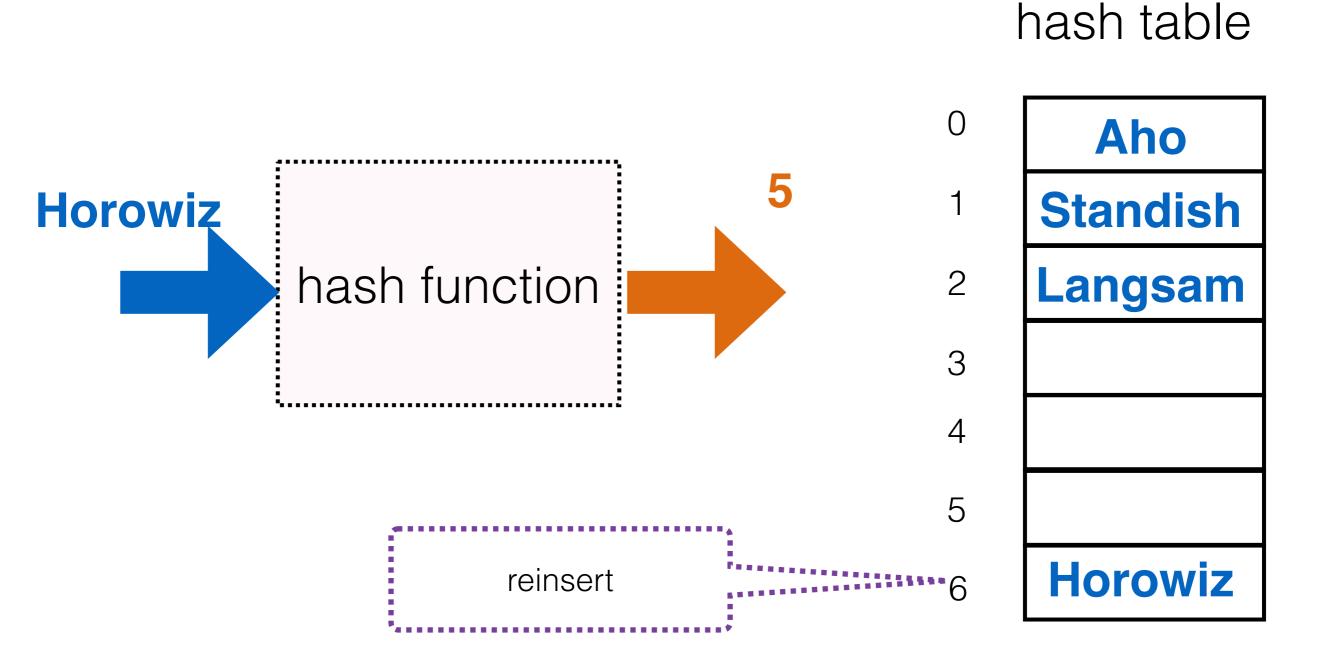


key: Kruse

hash table

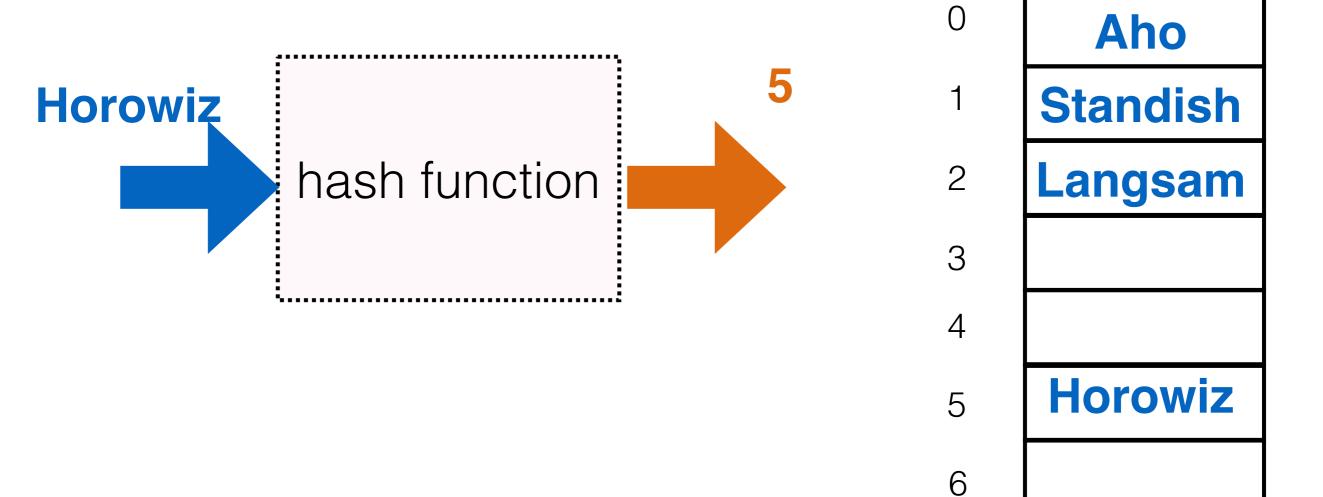
Horowiz

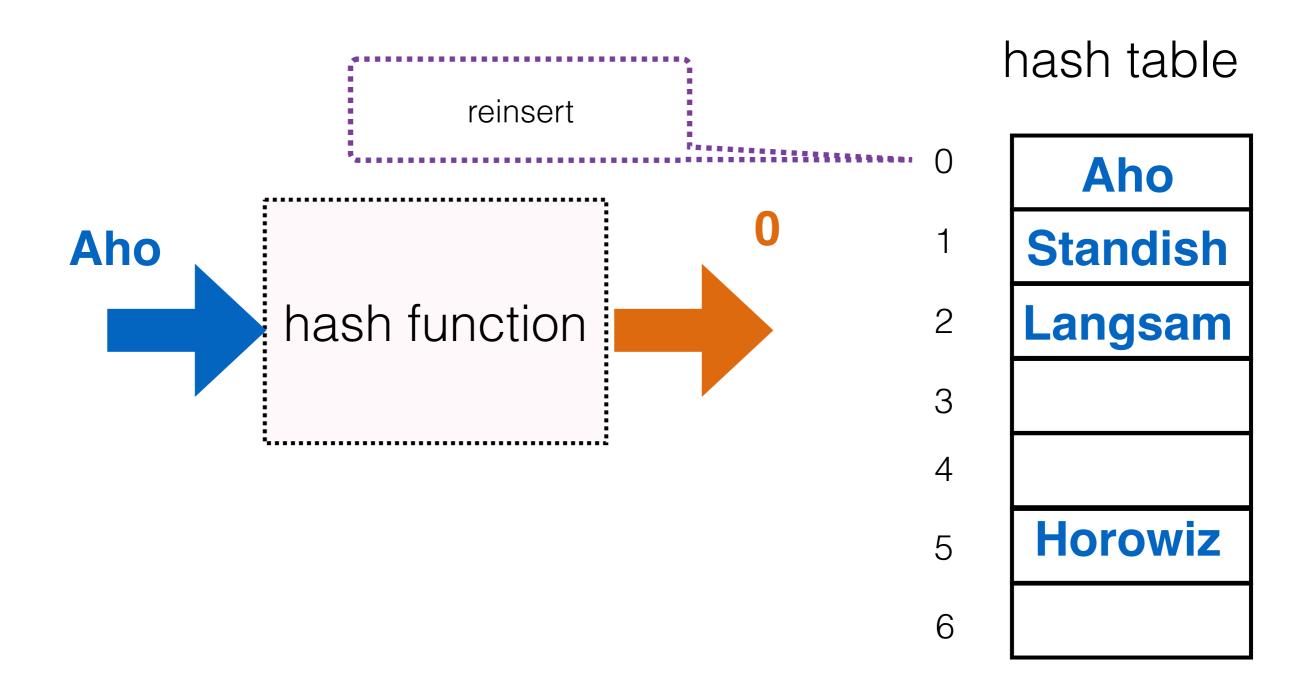


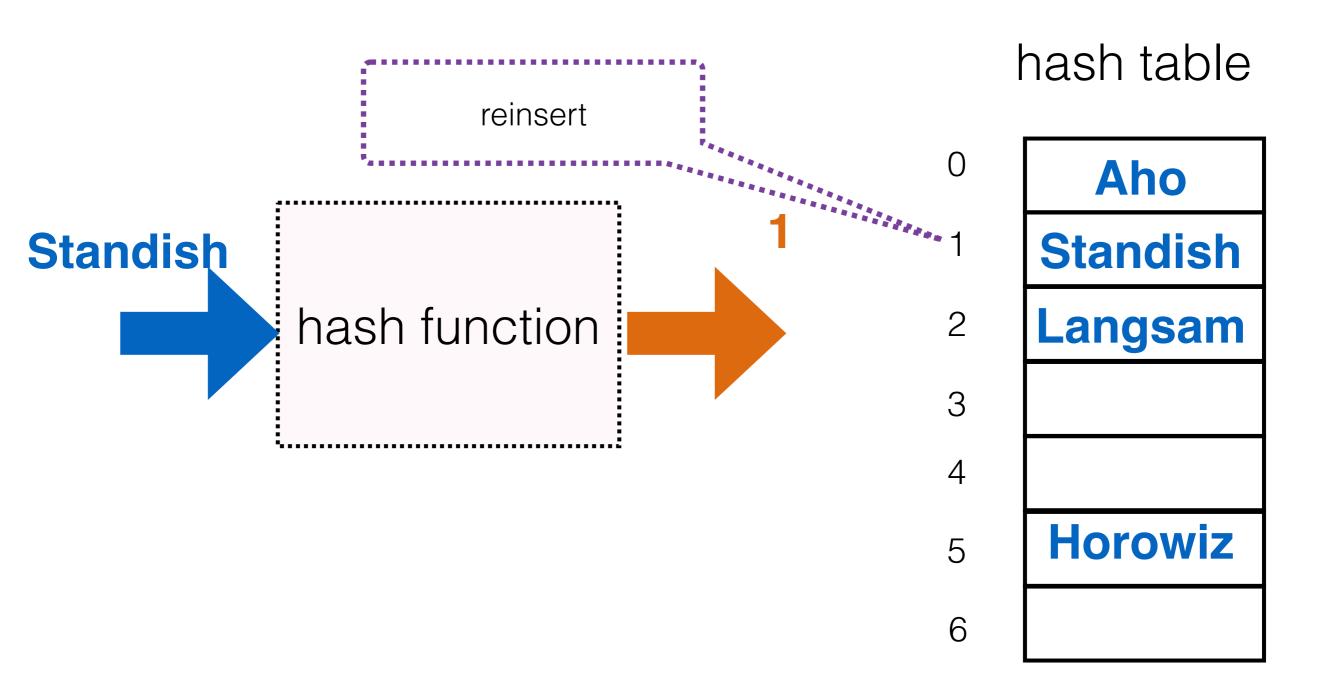


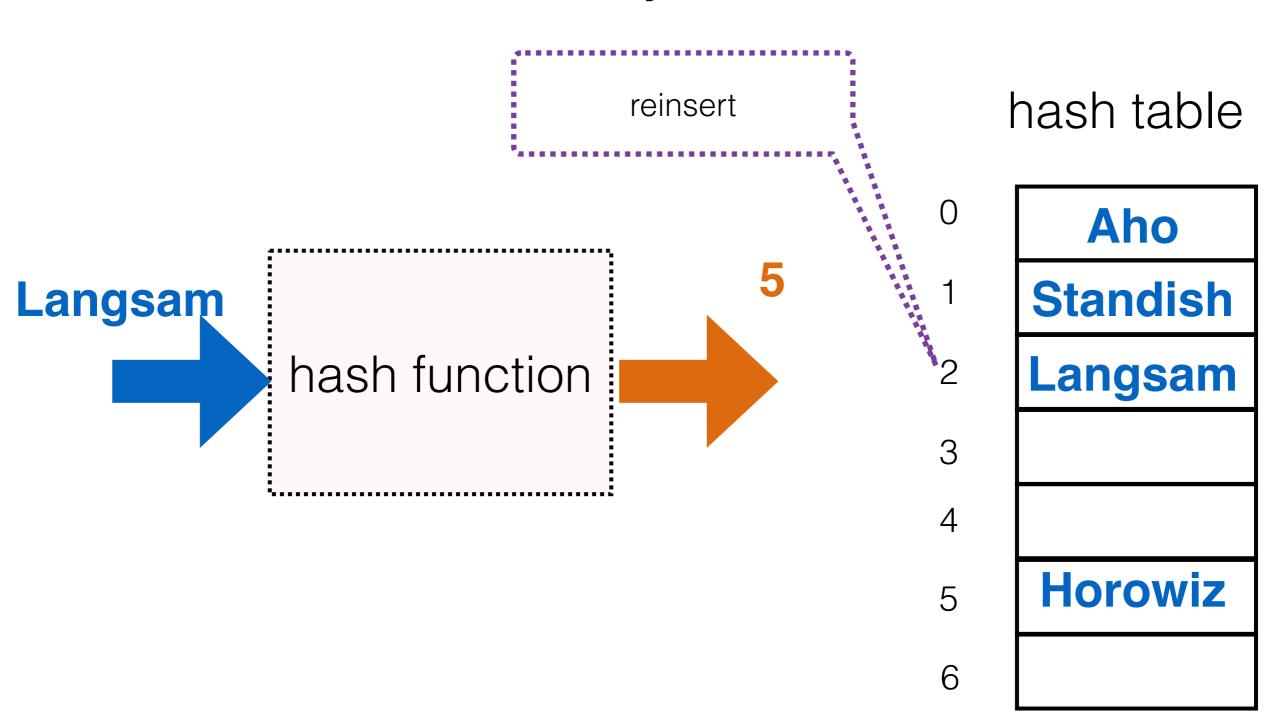
key: Kruse

hash table



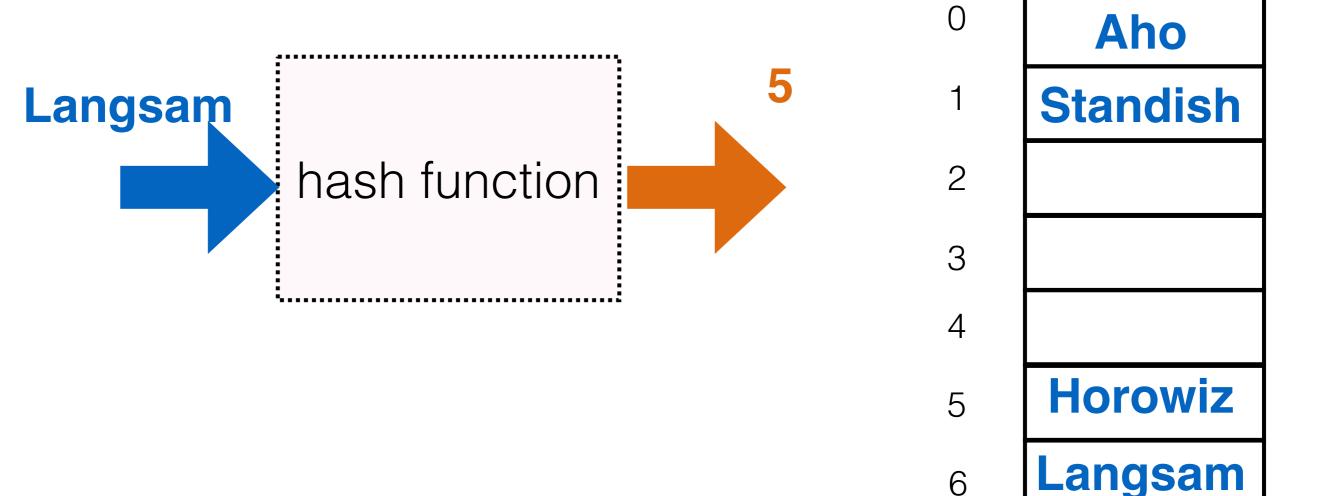






key: Langsam

hash table



key: Langsam

Found empty so I am done

hash function

hash table

Aho

0

4

5

6

Standish

Horowiz

Langsam

Open Addressing: Linear Probing

- Load factor: total number of items/TABLESIZE
- Cluster: sequence of full hash table slots (i.e., without an empty slot)
- Clusters once formed, tend to grow...
 - → Items that hash to a value within the cluster, get inserted at the end making it bigger
 - → This might involve more than one hash value
- Cluster can form even when the load is small

Example of cluster

- All 5 elements are part of a cluster
- Langsam, Kruse and Horowiz all have same hash value (5)
- Aho and Standish have values 0 and 1
- From then on, any element mapped to 0,1,2,5 or 6 will be part of the cluster

hash table

Aho

Standish

Langsam

4

5

2

3

0

Kruse

Horowiz

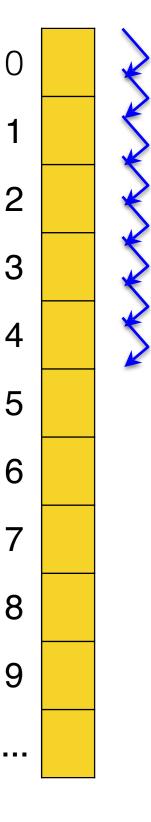
Linear Probing: Problems

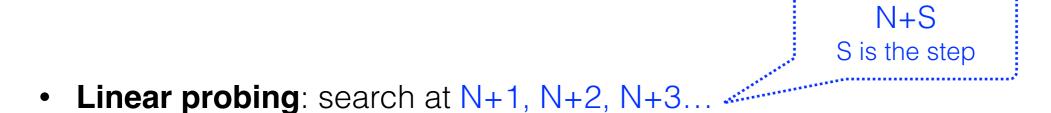
- Tendency for clustering to occur as the load is > 0.5
- Low speed on clustering. We start under-delivering on the promise of constant time search and insert.
- Deletion of records is difficult
- If implemented in arrays table may become full fairly quickly, resizing is time and resource consuming

Can we reduce clustering by taking bigger and bigger steps?

N+S S is the step

Linear probing: search at N+1, N+2, N+3...





• Quadratic probing: search at N+1, N+4, N+9, N+16

N+S²

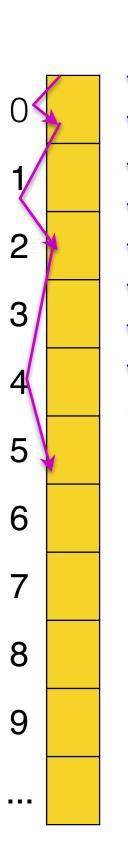


N+S
S is the step

Linear probing: search at N+1, N+2, N+3...

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N+S²



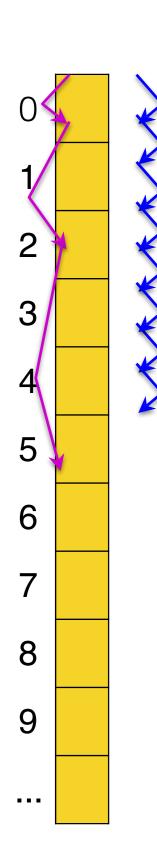
N+S
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Linear probing: search at N+1, N+2, N+3...

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N+S²

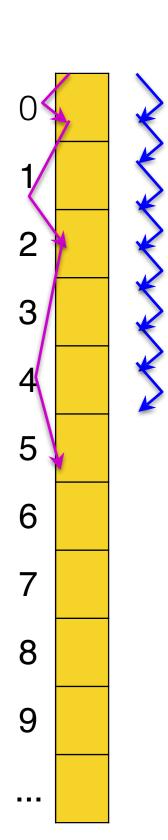
 <u>primary clustering</u>: keys with different hash values have same probe chains (as in linear probing)



N+S
S is the step

Linear probing: search at N+1, N+2, N+3...

- Quadratic probing: search at N+1, N+4, N+9, N+16
- primary clustering: keys with different hash values have same probe chains (as in linear probing)
- <u>secondary clustering</u>: keys with same hash values have the same probe chains

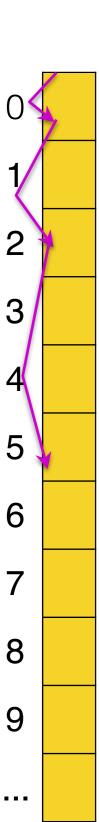


N+S S is the step

- Linear probing: search at N+1, N+2, N+3...
- Quadratic probing: search at N+1, N+4, N+9, N+16

N+S²

- <u>primary clustering:</u> keys with different hash values have same probe chains (as in linear probing)
- <u>secondary clustering</u>: keys with same hash values have the same probe chains

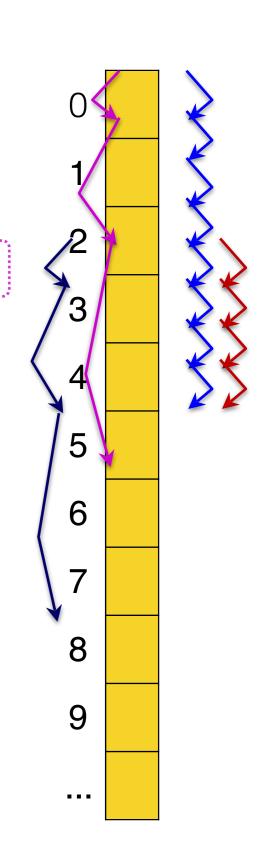


N+S
S is the step
Linear probing: search at N+1, N+2, N+3...

• Quadratic probing: search at N+1, N+4, N+9, N+16

N+S²

- <u>primary clustering:</u> keys with different hash values have same probe chains (as in linear probing)
- <u>secondary clustering</u>: keys with same hash values have the same probe chains

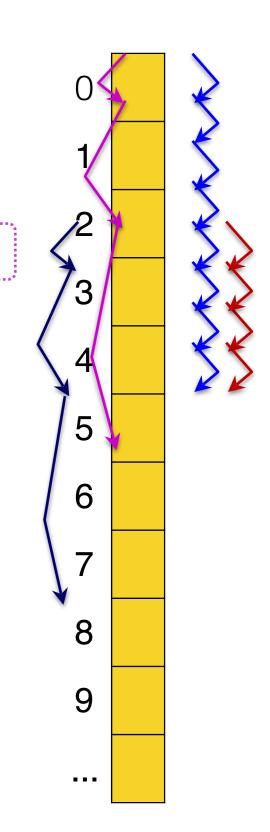


N+S
S is the step

Linear probing: search at N+1, N+2, N+3...

- Quadratic probing: search at N+1, N+4, N+9, N+16
- primary clustering: keys with different hash values have same probe chains (as in linear probing)
- <u>secondary clustering</u>: keys with same hash values have the same probe chains

 Advantage: Quadratic probing eliminates primary clustering, but can suffer from secondary clustering



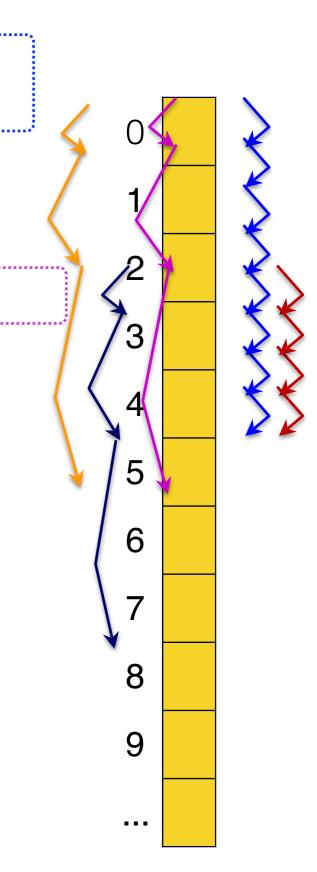
N+S

S is the step



- Quadratic probing: search at N+1, N+4, N+9, N+16
- <u>primary clustering:</u> keys with different hash values have same probe chains (as in linear probing)
- <u>secondary clustering</u>: keys with same hash values have the same probe chains

- Advantage: Quadratic probing eliminates primary clustering, but can suffer from secondary clustering
- There's a better method: Double Hashing



Open Addressing: Double Hashing

- If a collision occurs, use a second hash function to determine the step.
- Second hash function:
 - → Cannot hash to 0
 - → **Use primes**: table size & step size are co-primes (avoid revisiting the same positions)

Eliminates both primary and secondary clustering

Collisions: two main approaches

Open addressing:

- Each array position contains a single item
- Upon collision, use an empty space to store the item (which empty space depends on which technique)

Separate chaining:

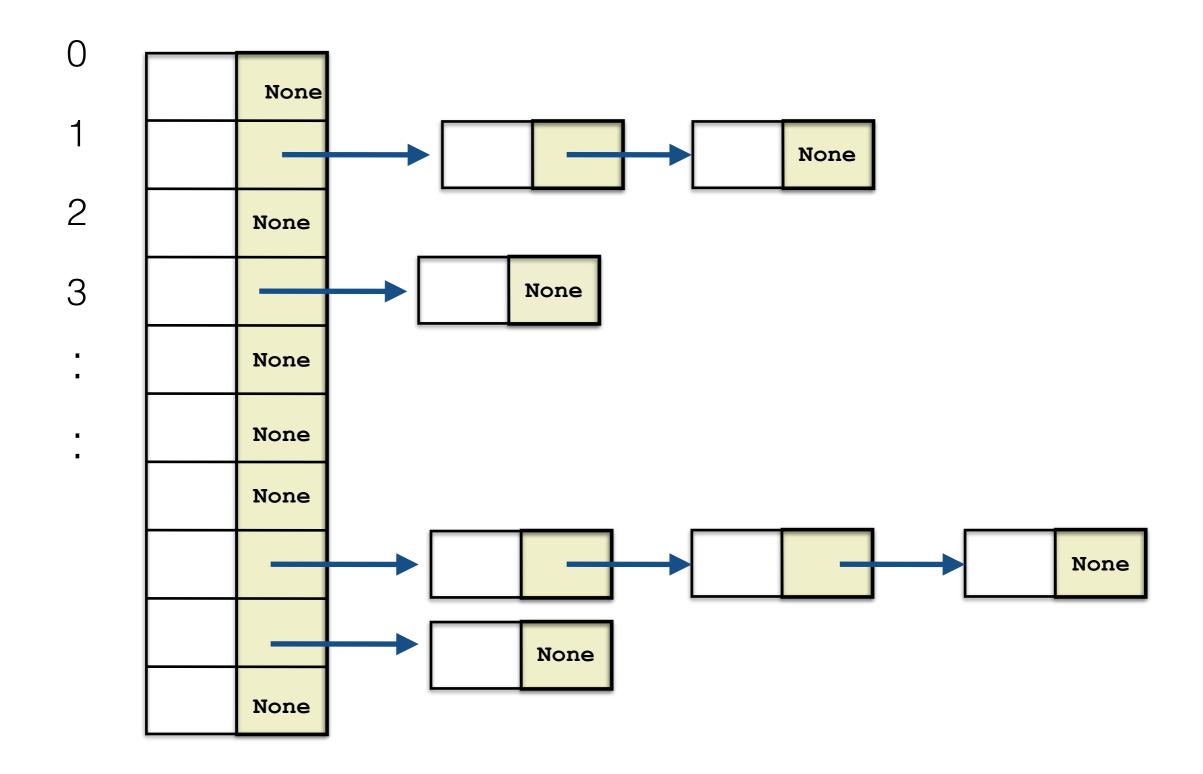
- Each array position contains a linked list of items
- Upon collision, the element is added to the linked list

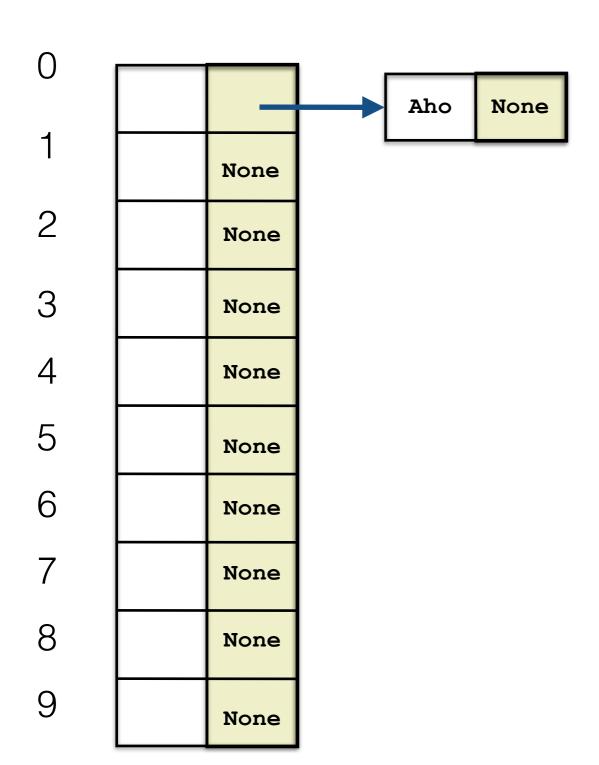
Separate Chaining

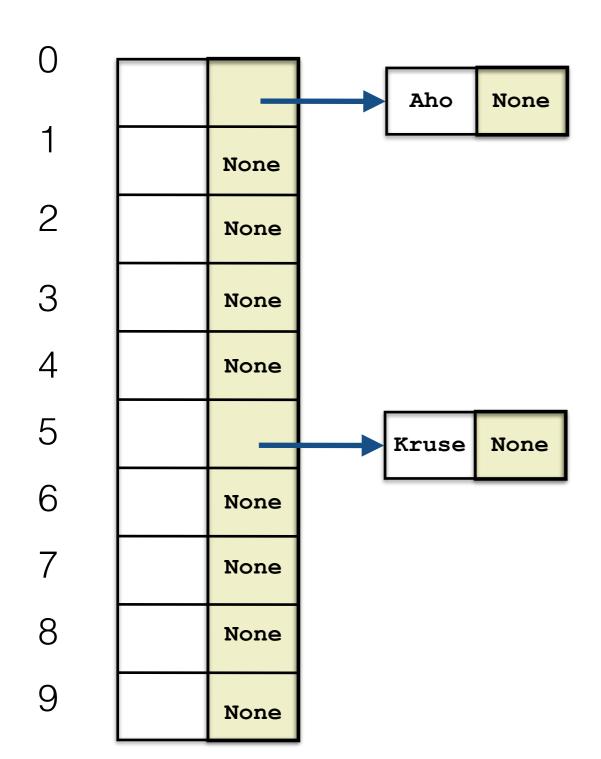
 Uses a Linked List at each position in the Hash Table.

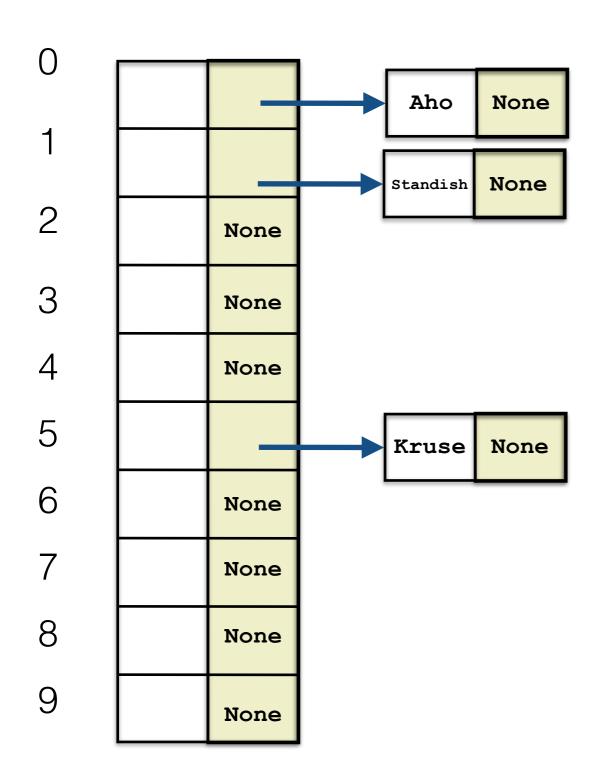
 Linked list at a position contains all the items that 'hash' to that position.

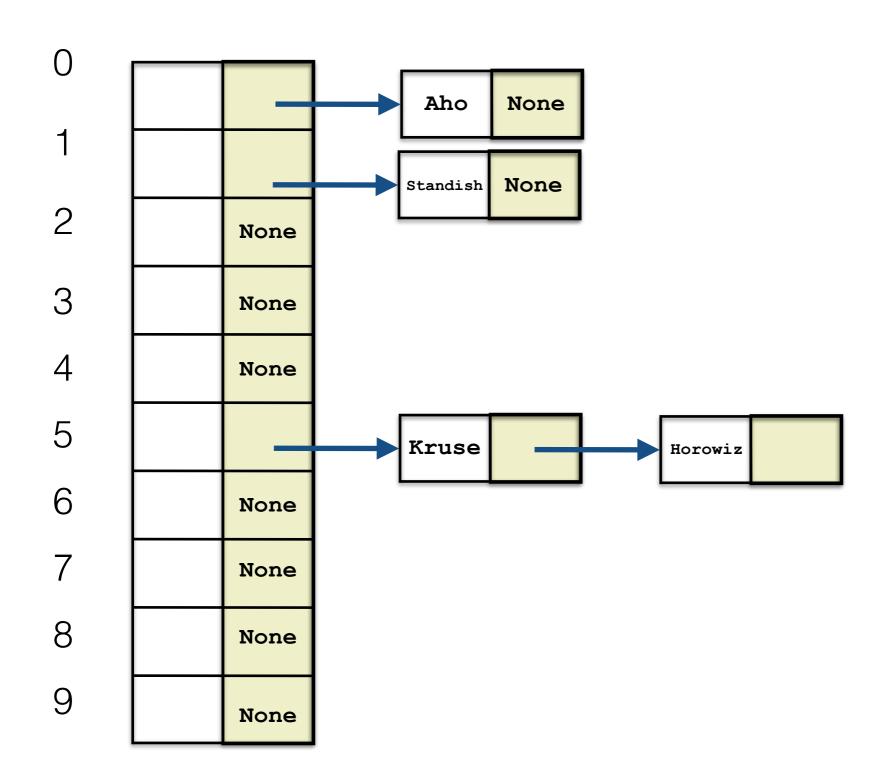
hash table

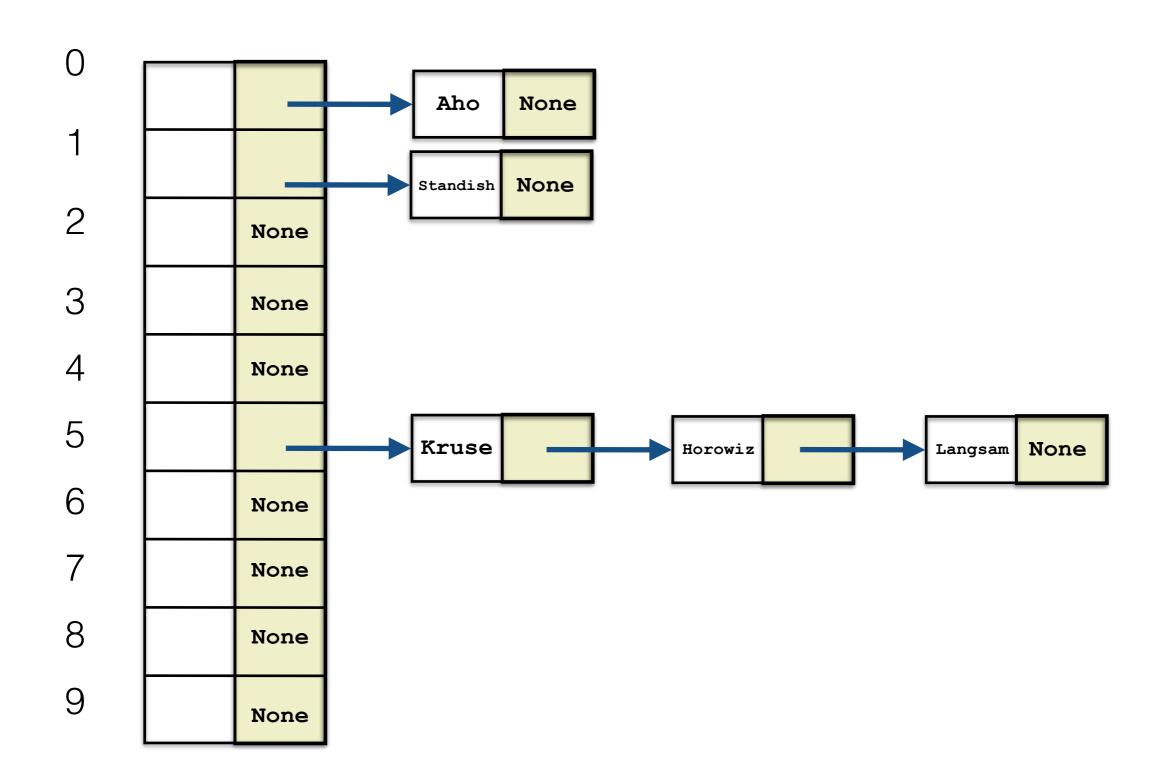


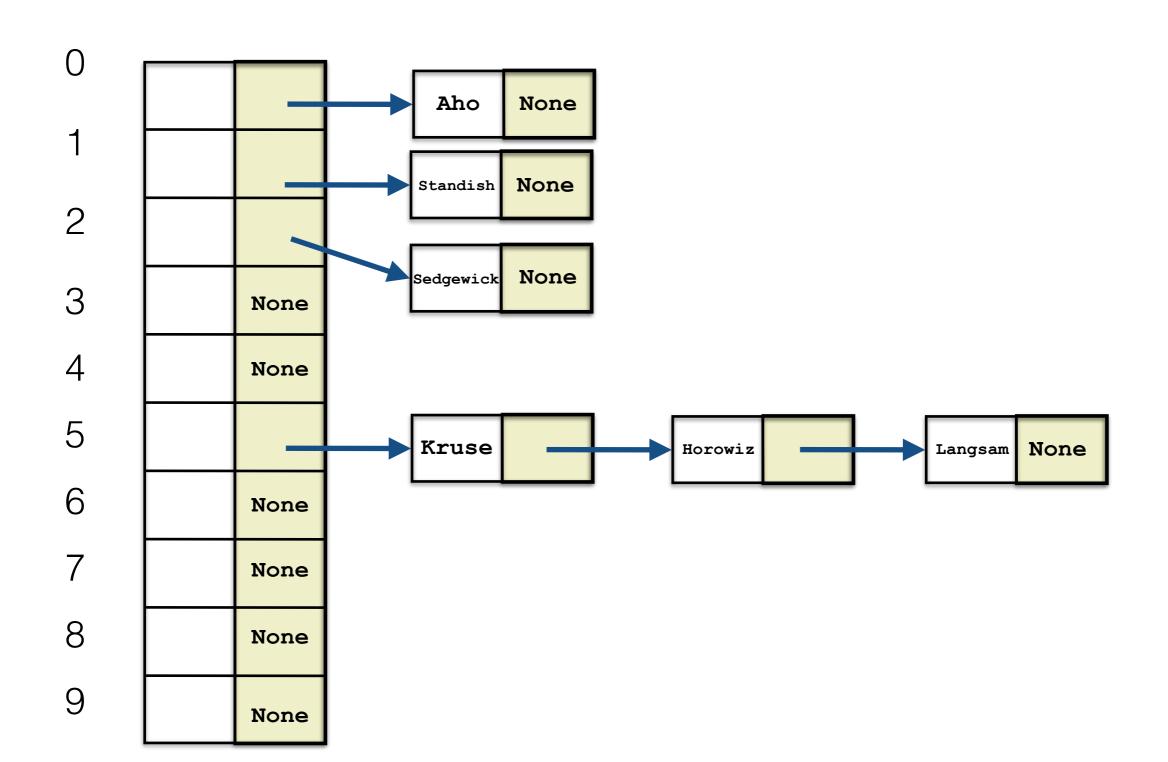


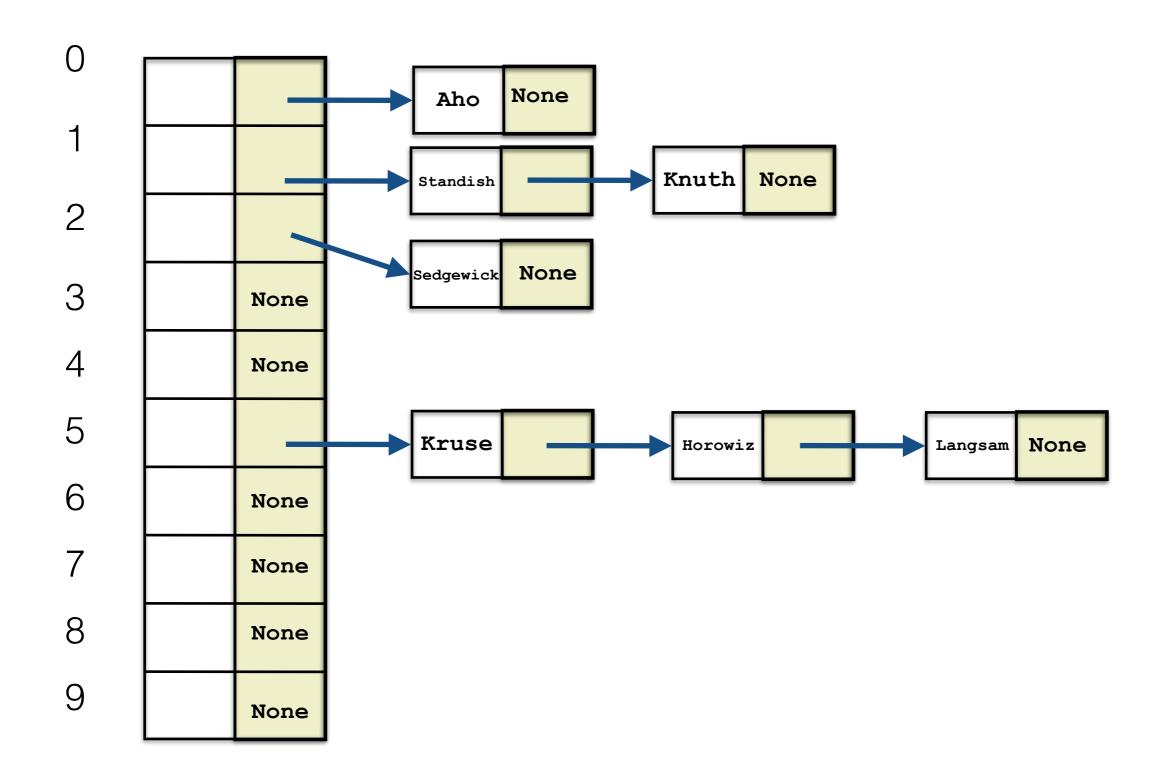


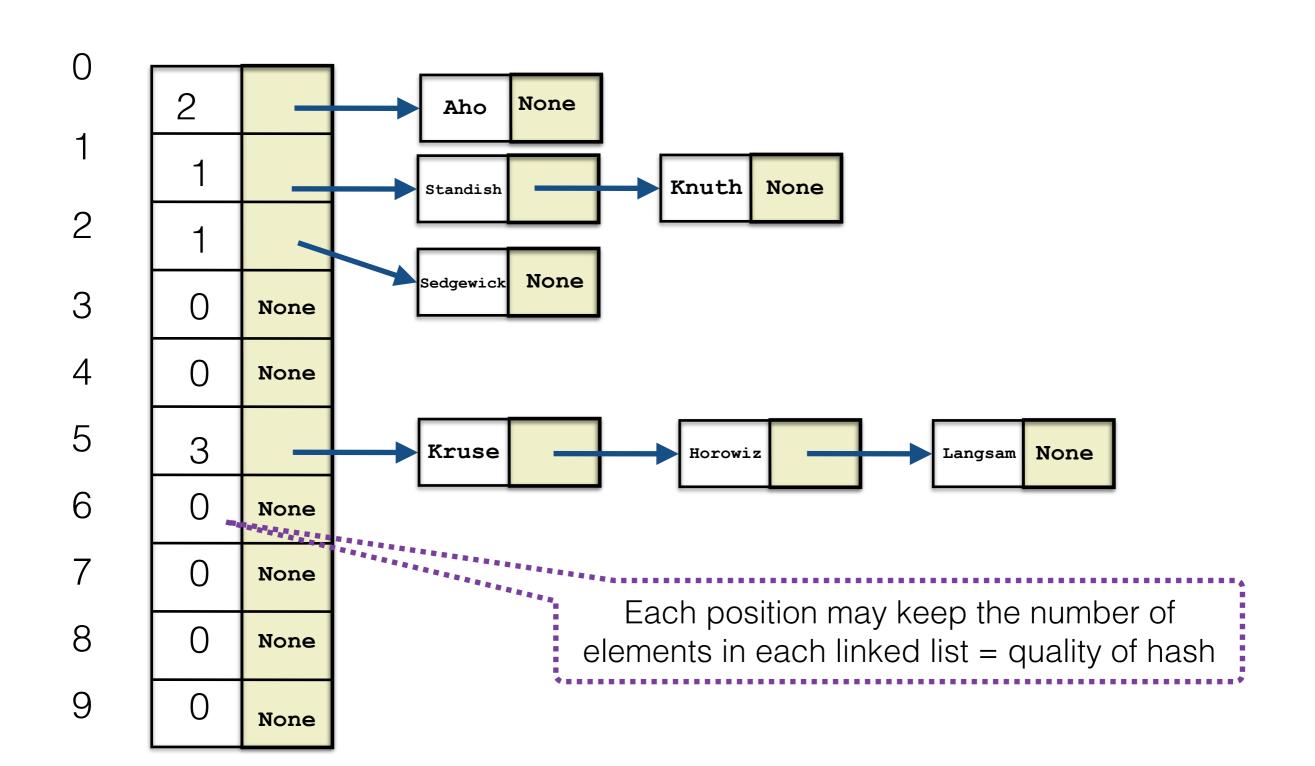


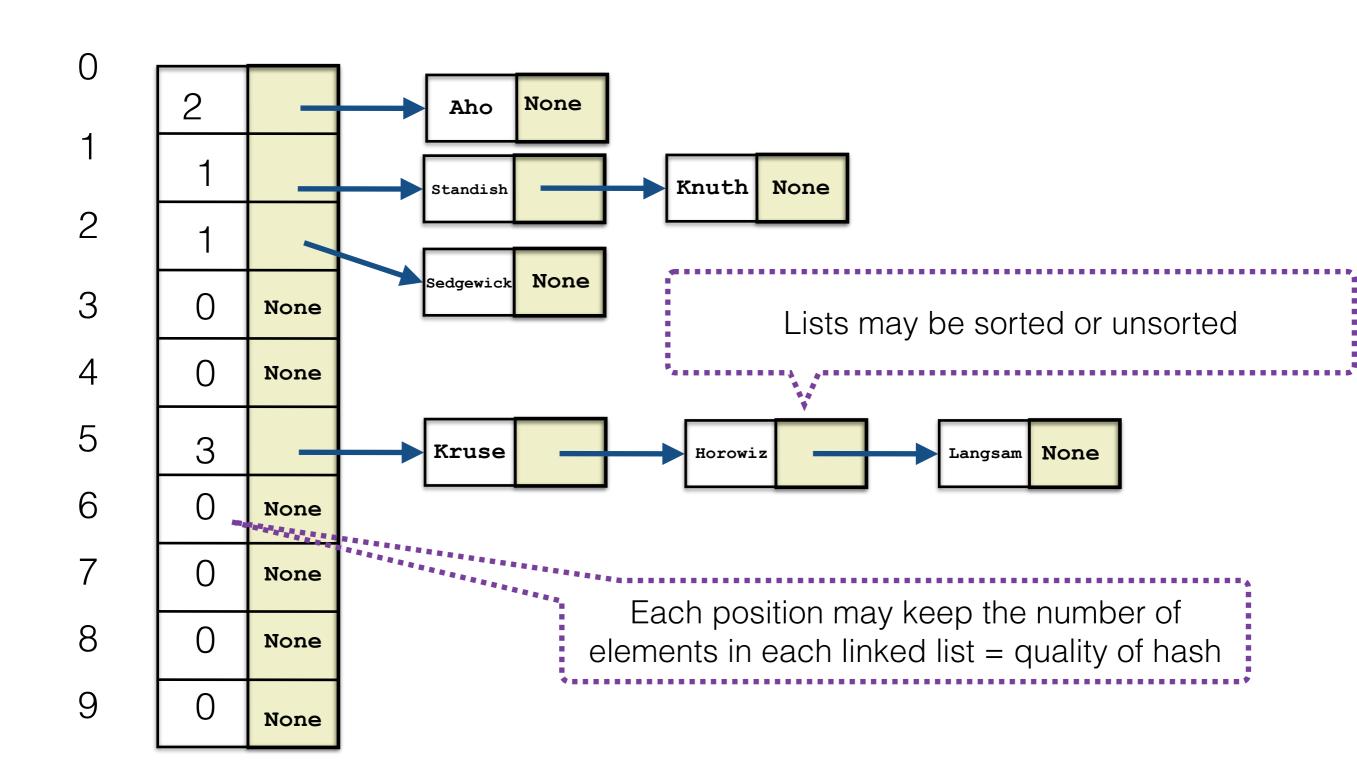












Separate Chaining

- Apply hash function to get a position N in the array
- Insert: Insert key into the Linked List at position N
- Search: Search for key in the Linked List at position N
- Delete: Search for key; delete the node in the Linked List at position N

Separate Chaining

Advantages:

- Conceptually simpler
- Insertions and deletions are easy and quick
- Naturally resizable, allows a varying number of records to be stored

Disadvantages

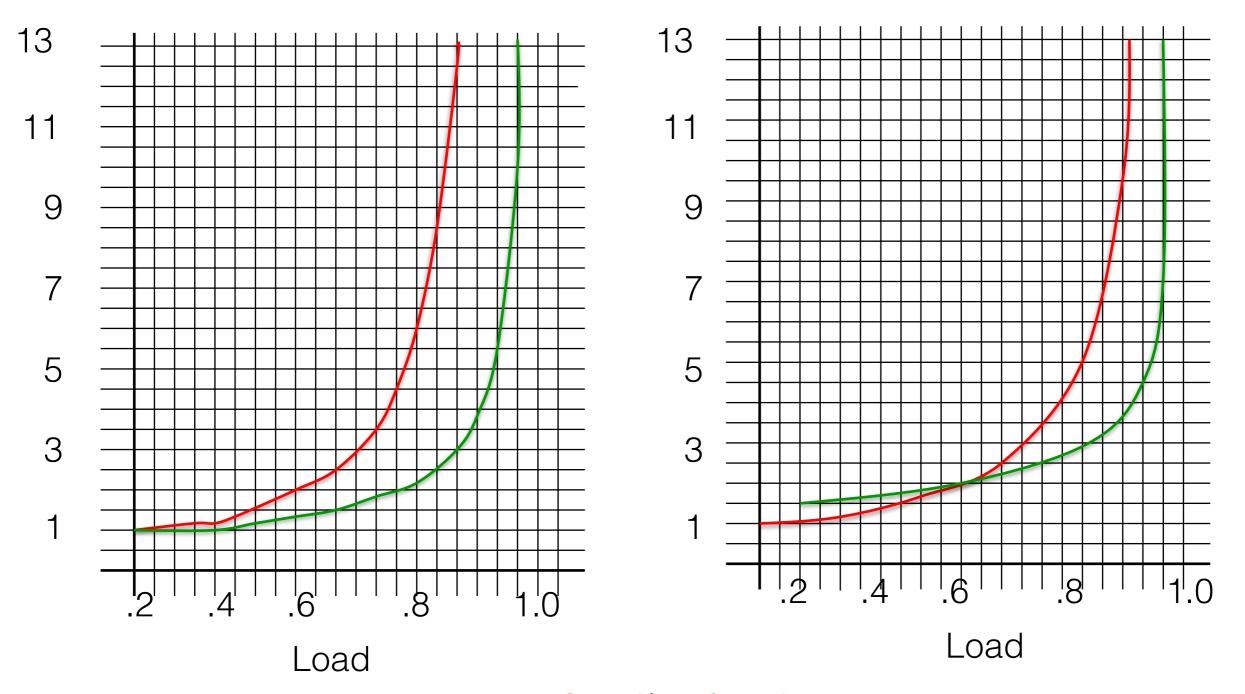
- Requires extra space for the links
- Requires linear search for elements in a list

Comparison: general

- Choice depends on the particular application
 - <u>Linear Probing</u>: fast if memory allows for a large table.
 - <u>Double hashing</u>: efficient use of memory but needs to compute a second hash
 - <u>Separate chaining:</u> simple, extra memory, resizable, fast insert and fast delete
 - When the load approaches 1: double hashing far outperforms linear probing
 - Open addressing: keep load under 2/3 even better 1/2
 - Separate chaining: efficiency degrades linearly with load

Linear probe chain length

Double hashing probe chain length

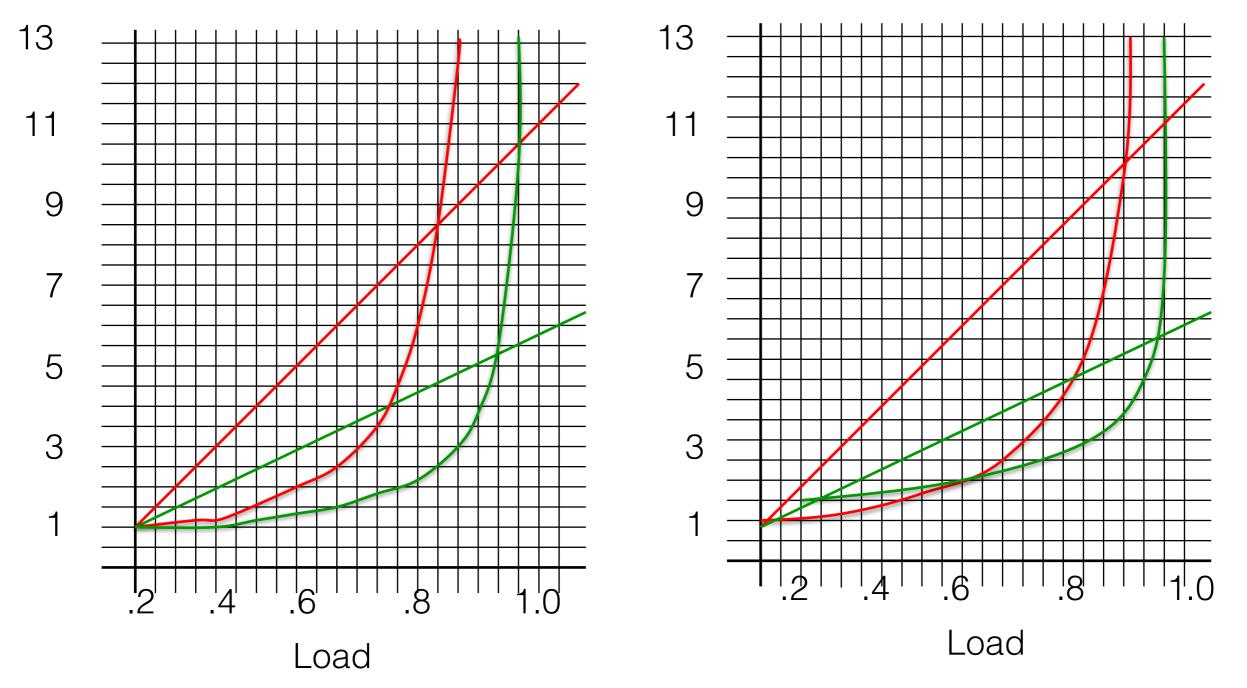


found/not found

Superimposing Separate Chaining

Linear probe chain length

Double hashing probe chain length



found/not found

Dynamic Hashing

- Each time the load in an open address method gets greater than desirable:
 - → 1/2 for linear probing
 - → 2/3 for double hashing

we expand the table by doubling its size

- At doubling the size:
 - Create a new array
 - Rehashing every item in the old table into the new one (due to the use of TABLESIZE in the hash function)

Conclusion

- Hash Tables are one of the most used data types
- You have a very good chance of using them in your career
- They are very simple conceptually.
- A significant amount of experimental evaluation is usually needed to fine-tune the hash function and the TABLESIZE
- Choice of hash function, collision handling and load factor are crucial to maintaining an efficient hash table