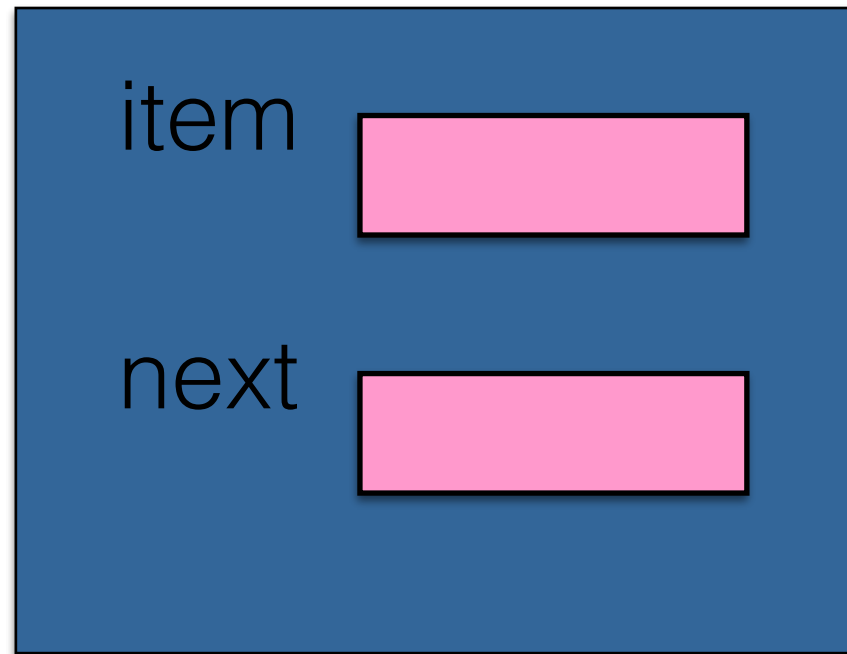
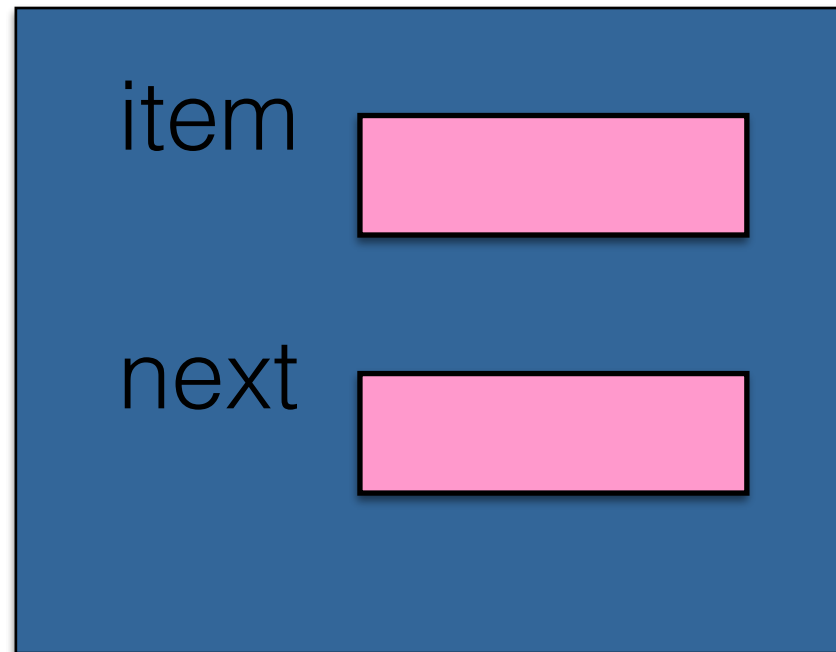


Did you watch the video?

Node

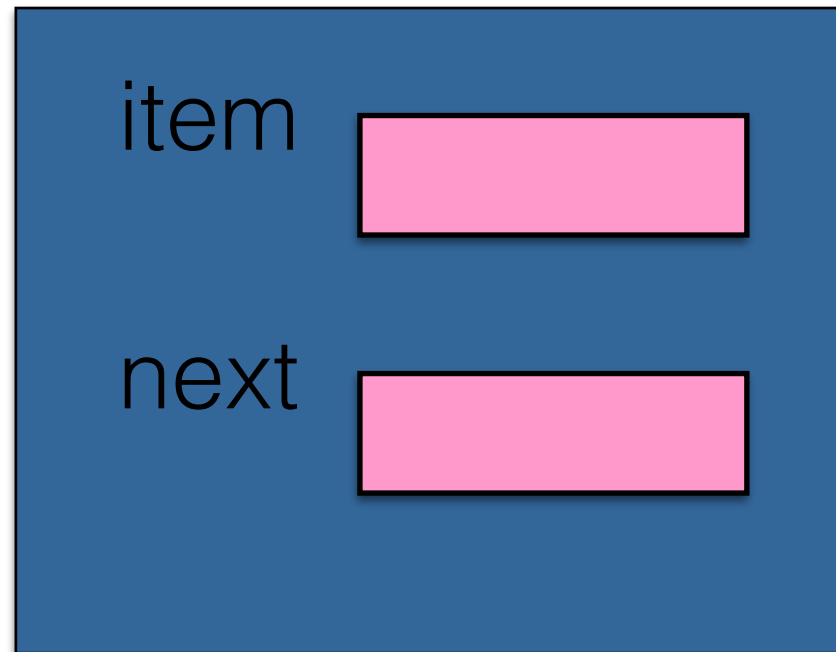


Node



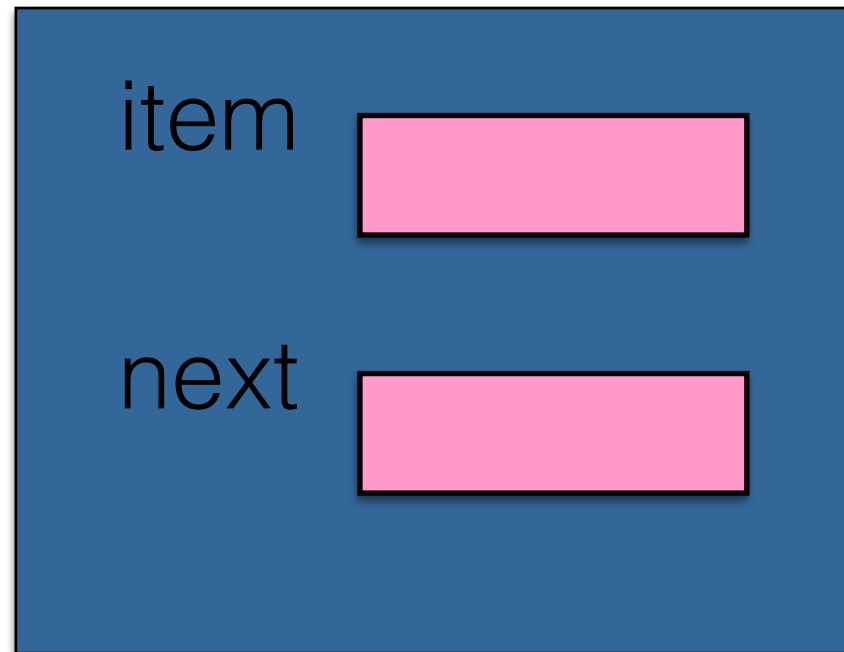
```
class Node:  
    def __init__(self, item, link):  
        self.item = item  
        self.next = link
```

Node



```
class Node:  
    def __init__(self, item = None, link= None):  
        self.item = item  
        self.next = link
```

Node

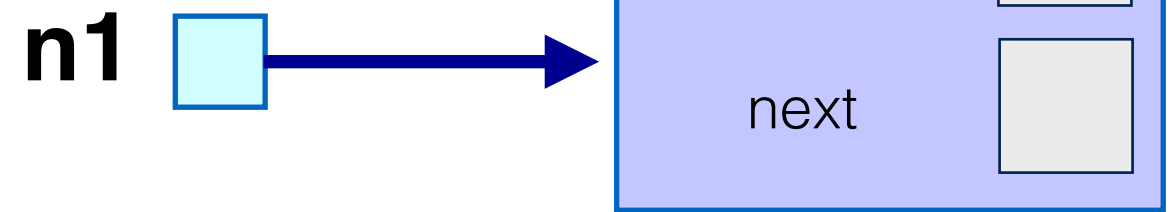


default values, if not supplied

```
class Node:
    def __init__(self, item = None, link= None):
        self.item = item
        self.next = link
```

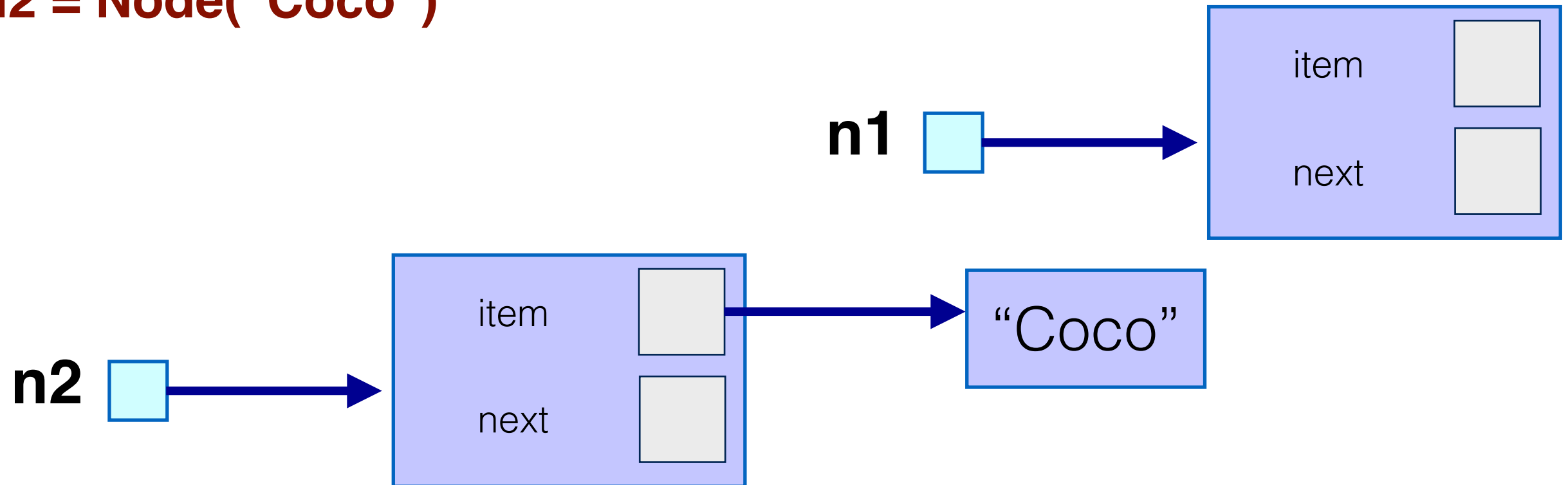
An orange dashed line connects the text "default values" to the default values `item = None` and `link= None` in the code.

n1 = Node()



n1 = Node()

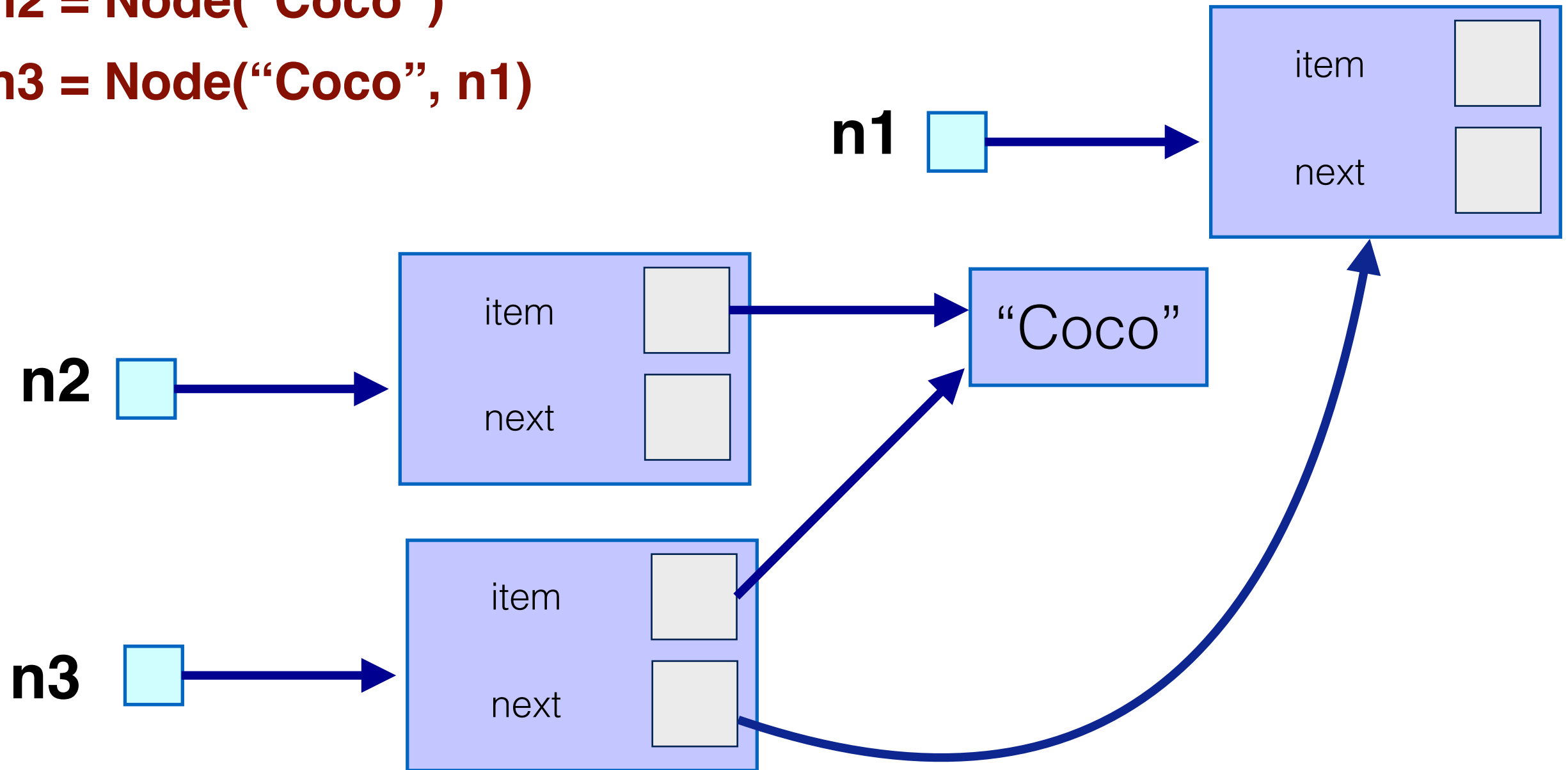
n2 = Node("Coco")



n1 = Node()

n2 = Node("Coco")

n3 = Node("Coco", n1)

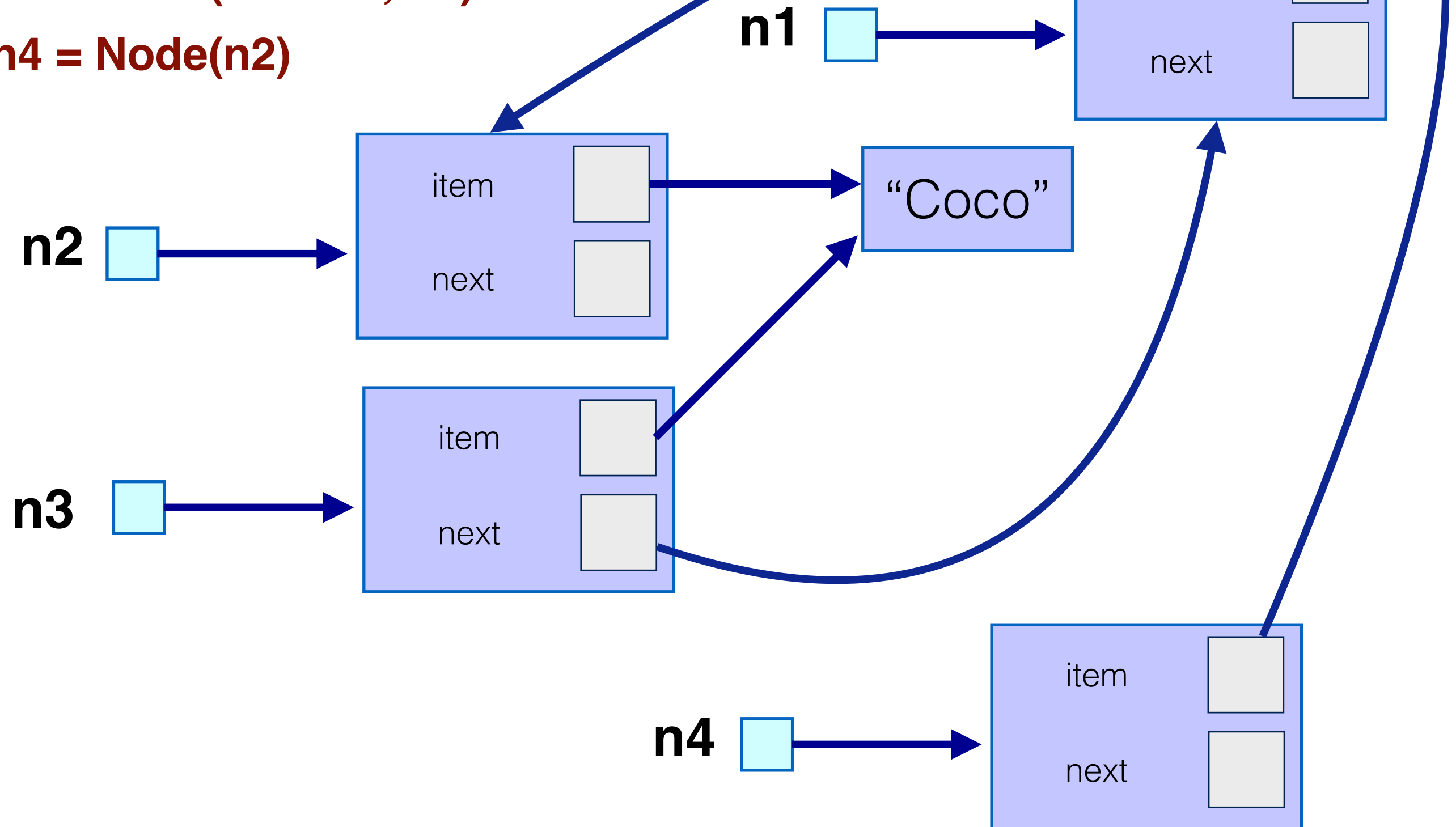


n1 = Node()

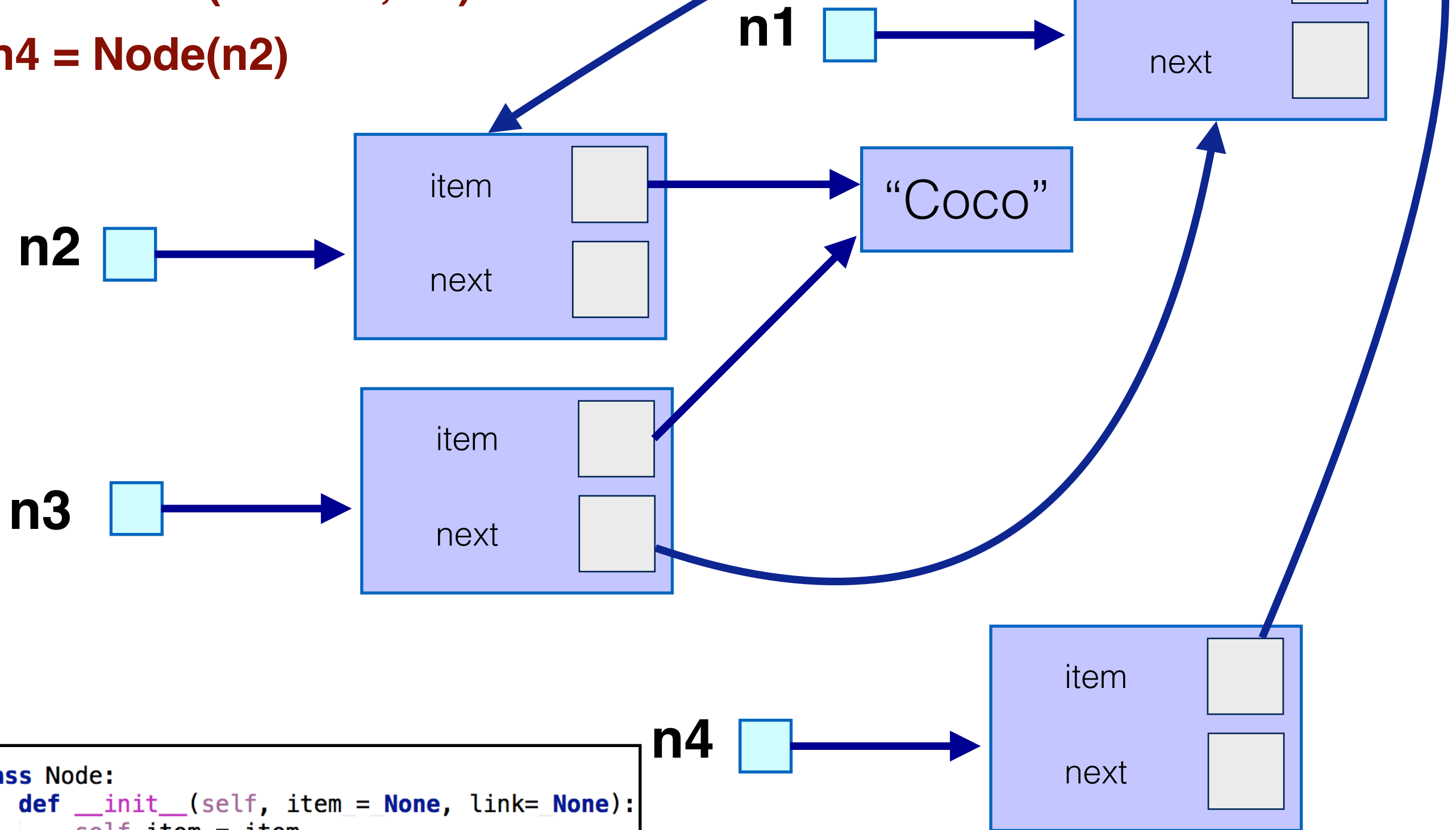
n2 = Node("Coco")

n3 = Node("Coco", n1)

n4 = Node(n2)

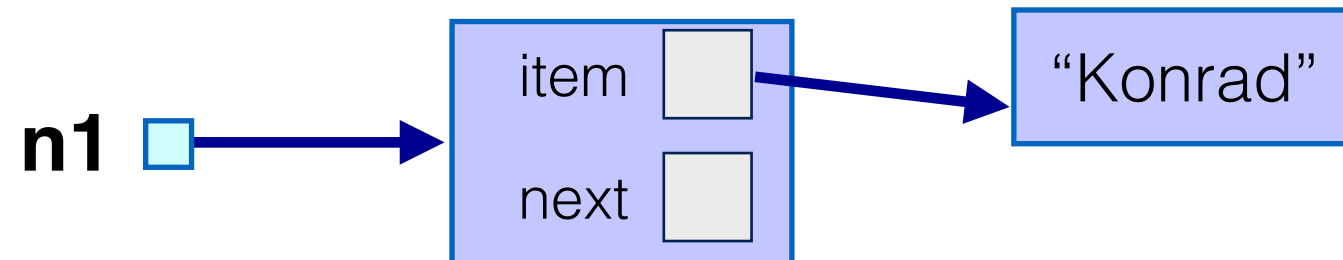


n1 = Node()
n2 = Node("Coco")
n3 = Node("Coco", n1)
n4 = Node(n2)

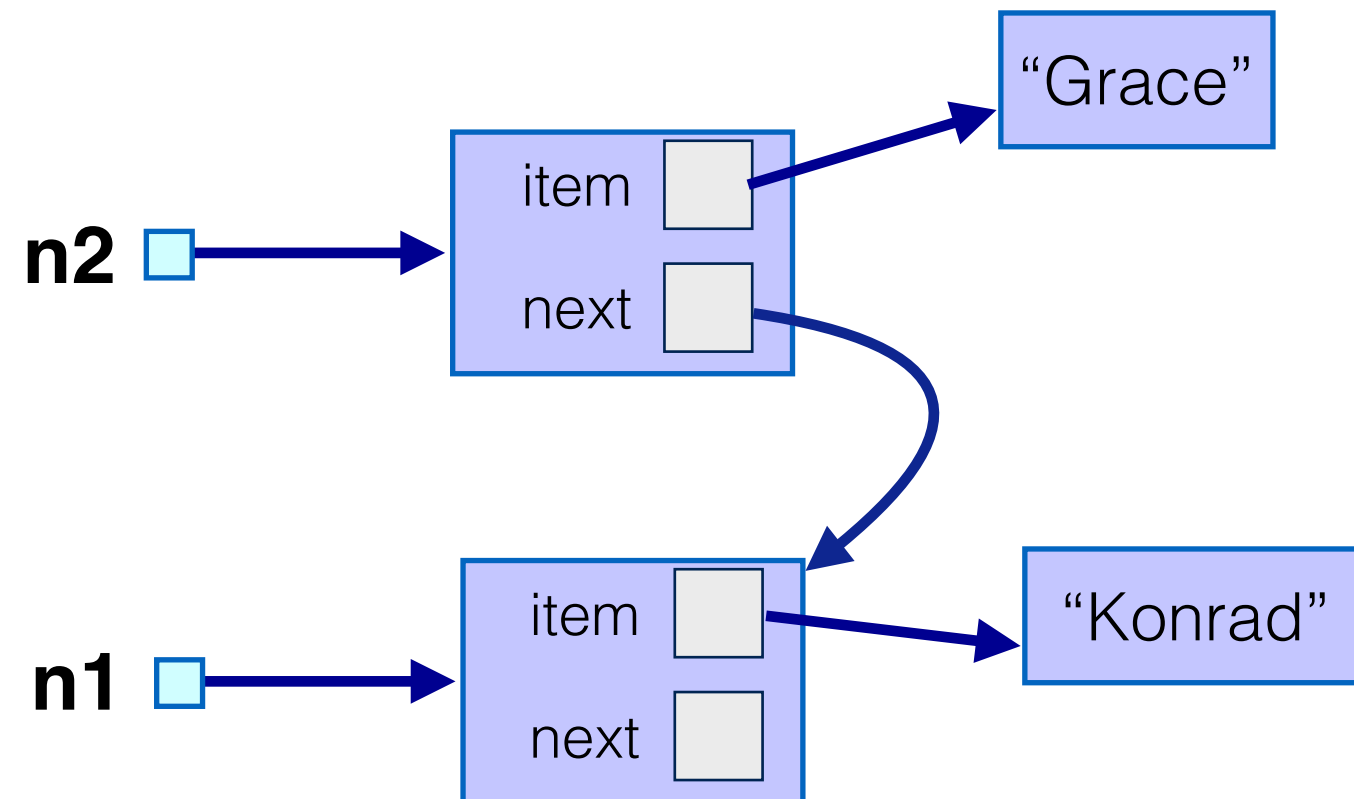


```
class Node:  
    def __init__(self, item = None, link= None):  
        self.item = item  
        self.next = link
```

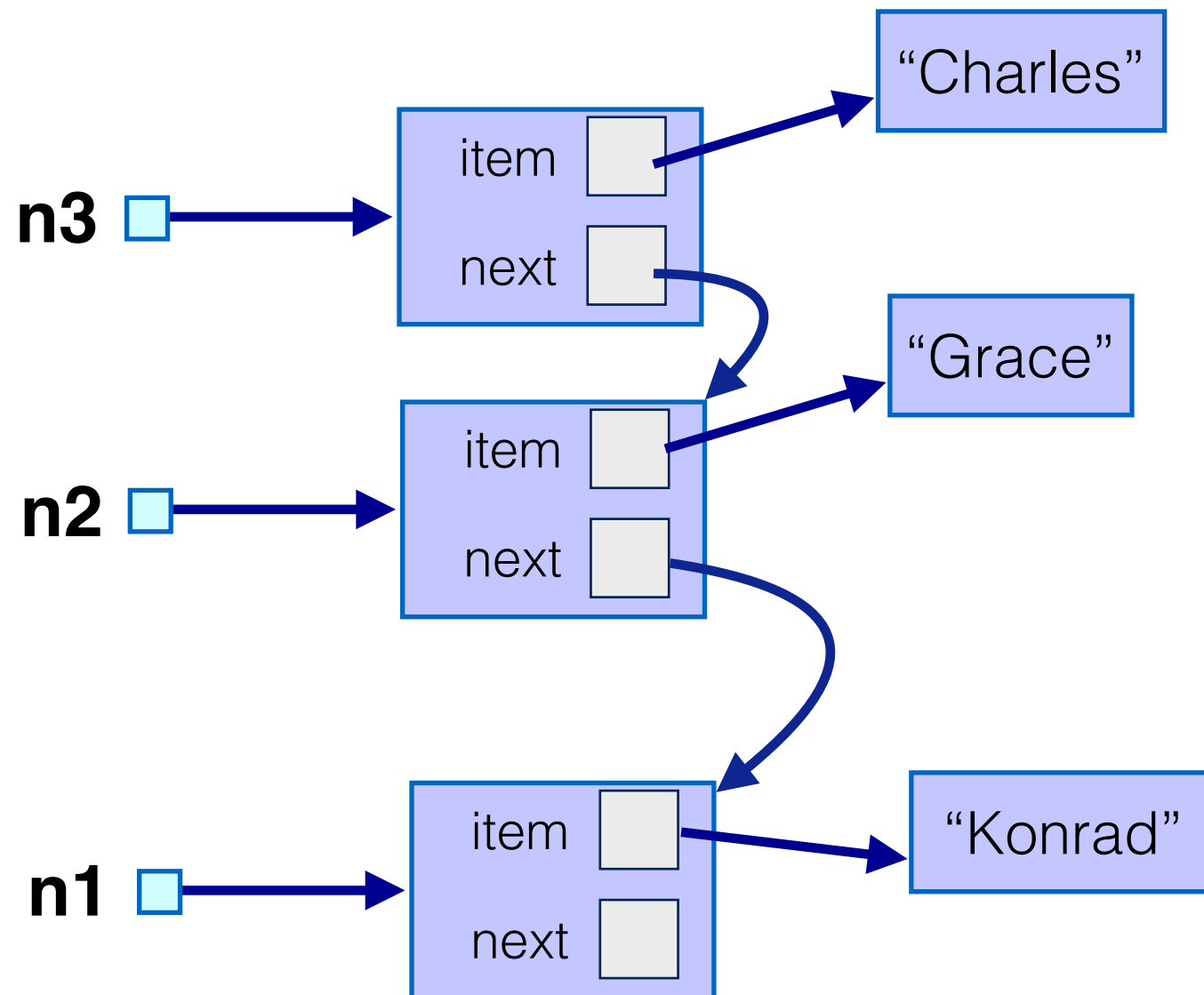
```
>>> n1 = Node("Konrad")
```



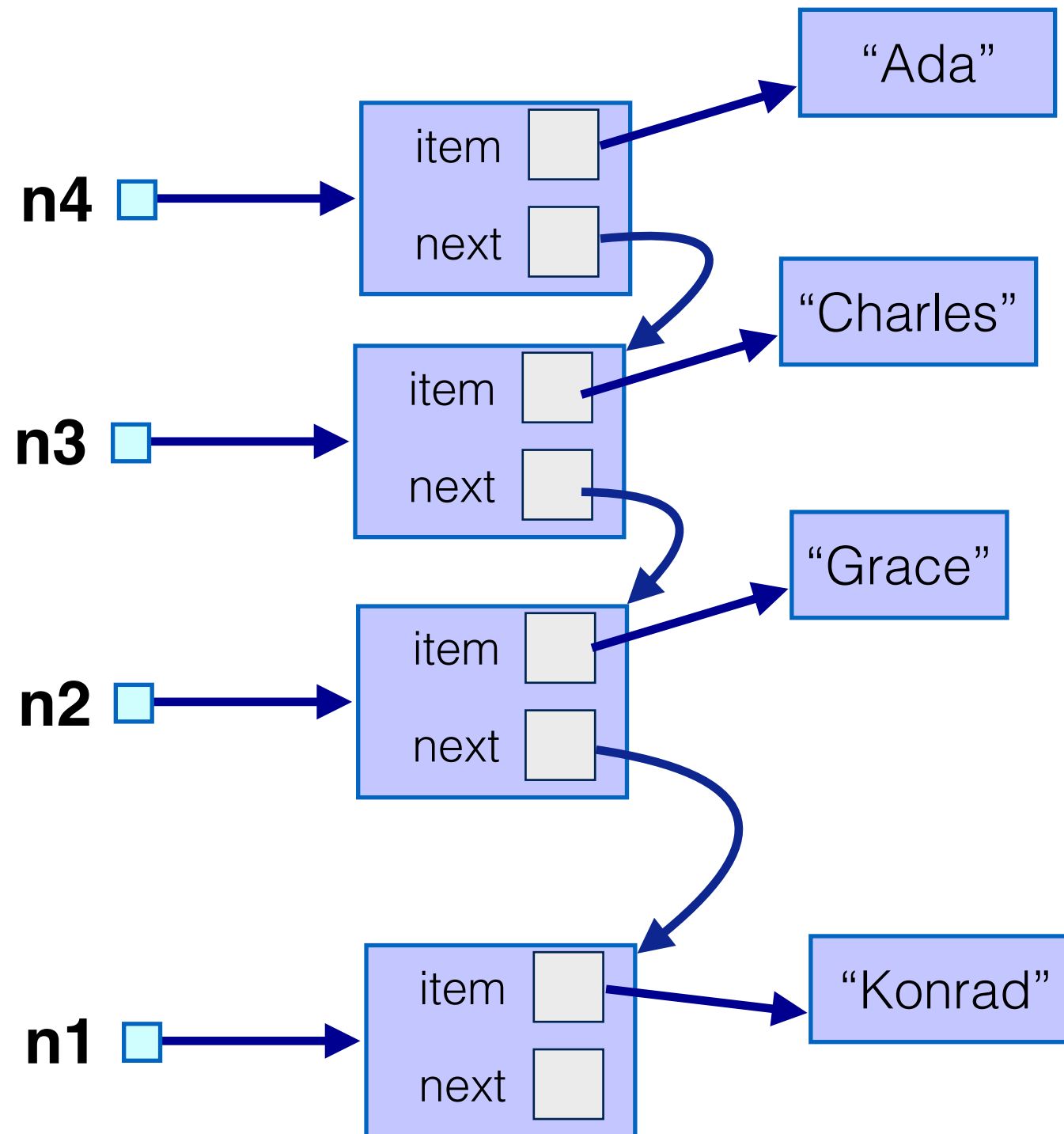
```
>>> n1 = Node("Konrad")  
>>> n2 = Node("Grace", n1)
```



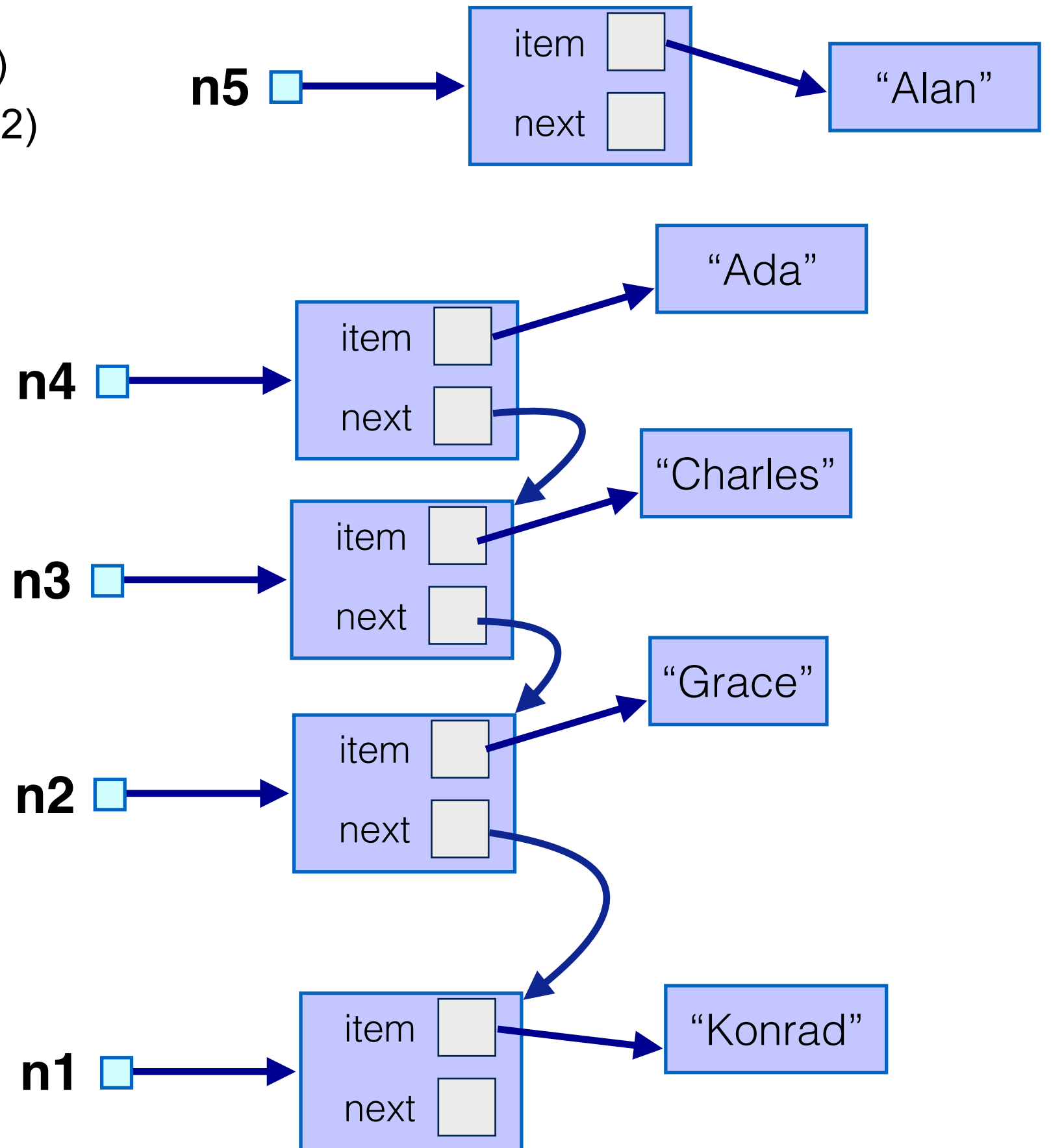
```
>>> n1 = Node("Konrad")  
>>> n2 = Node("Grace", n1)  
>>> n3 = Node("Charles", n2)
```



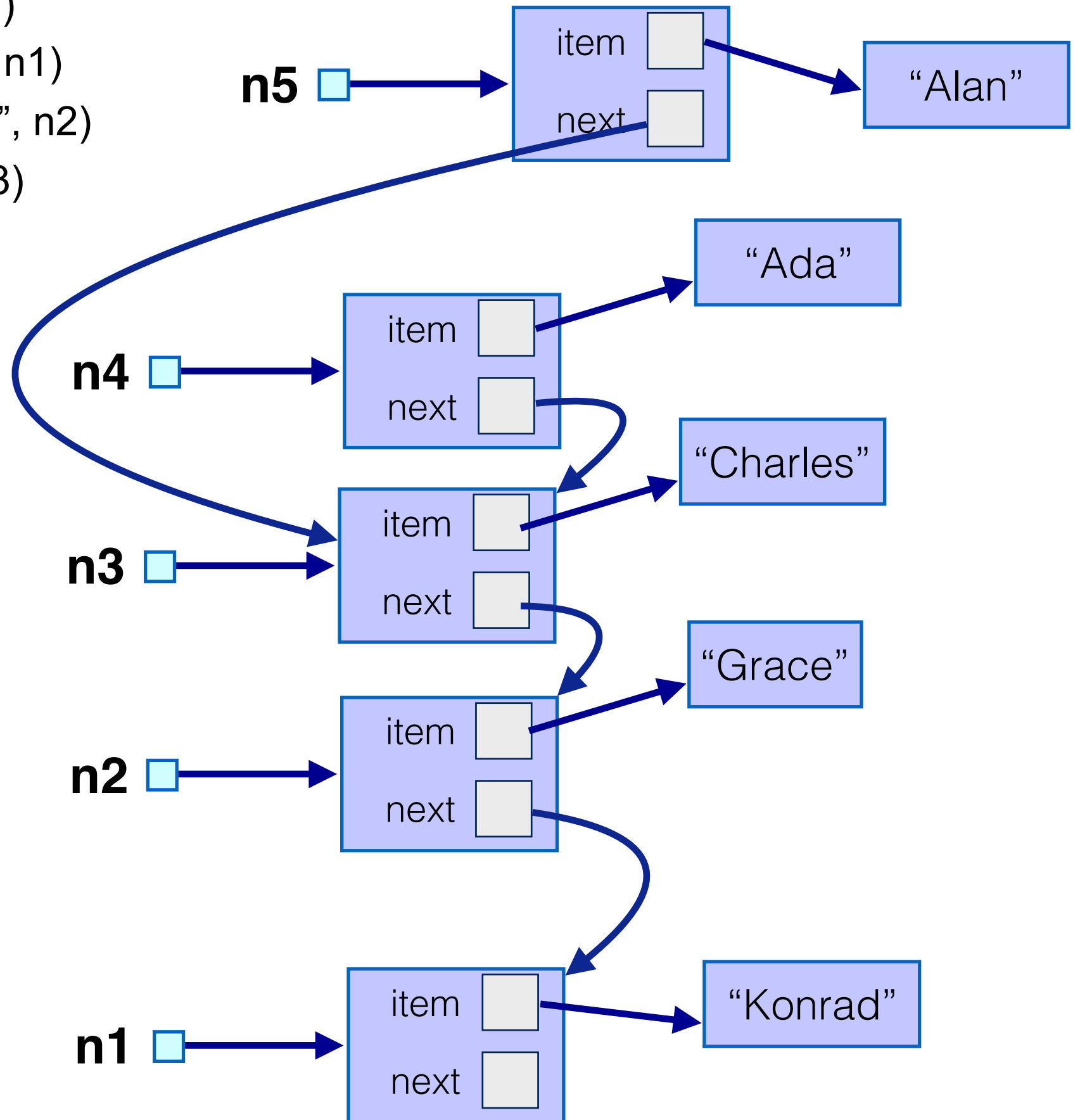
```
>>> n1 = Node("Konrad")
>>> n2 = Node("Grace", n1)
>>> n3 = Node("Charles", n2)
>>> n4 = Node("Ada", n3)
```



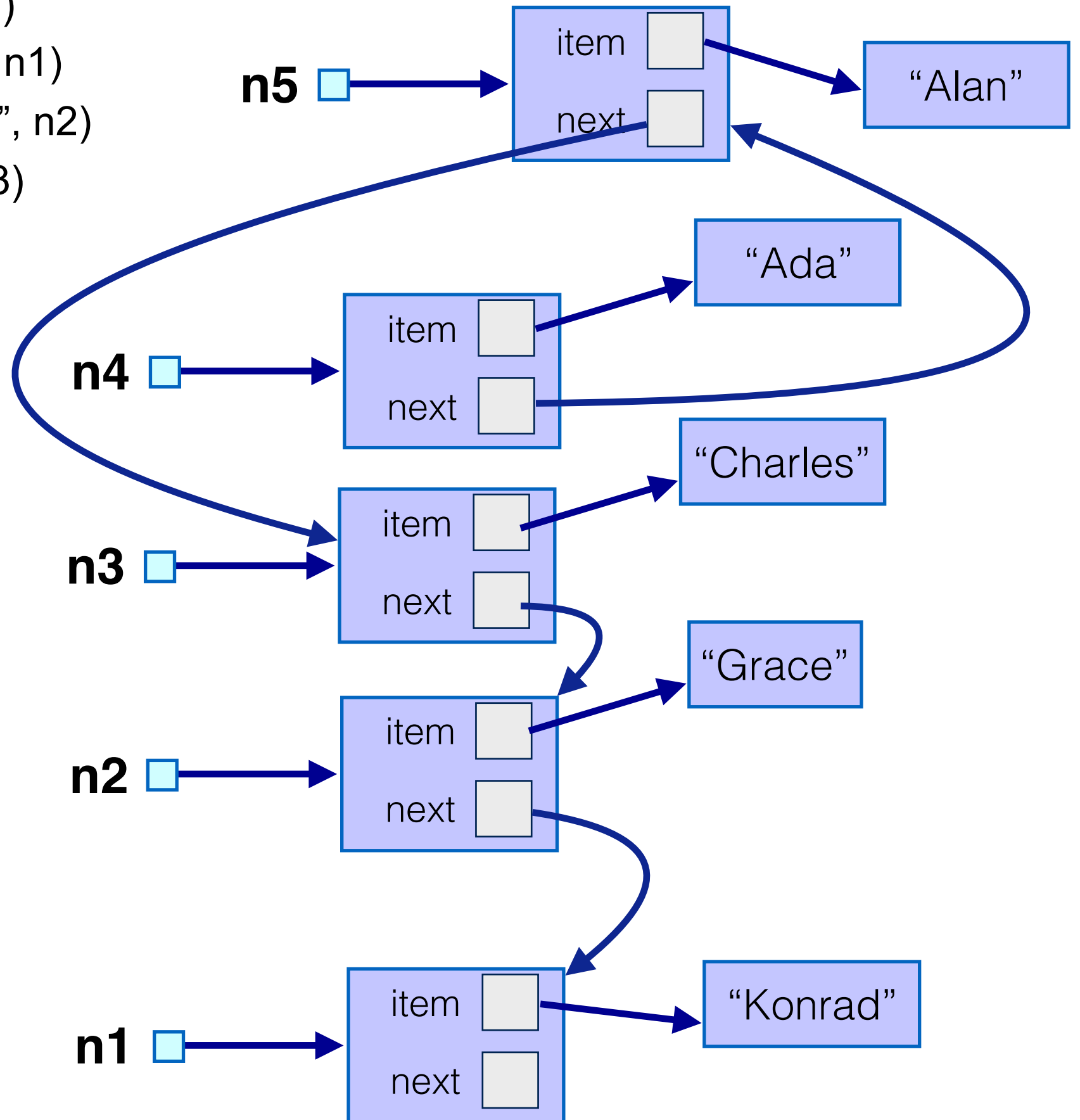
```
>>> n1 = Node("Konrad")
>>> n2 = Node("Grace", n1)
>>> n3 = Node("Charles", n2)
>>> n4 = Node("Ada", n3)
>>> n5 = Node("Alan")
```

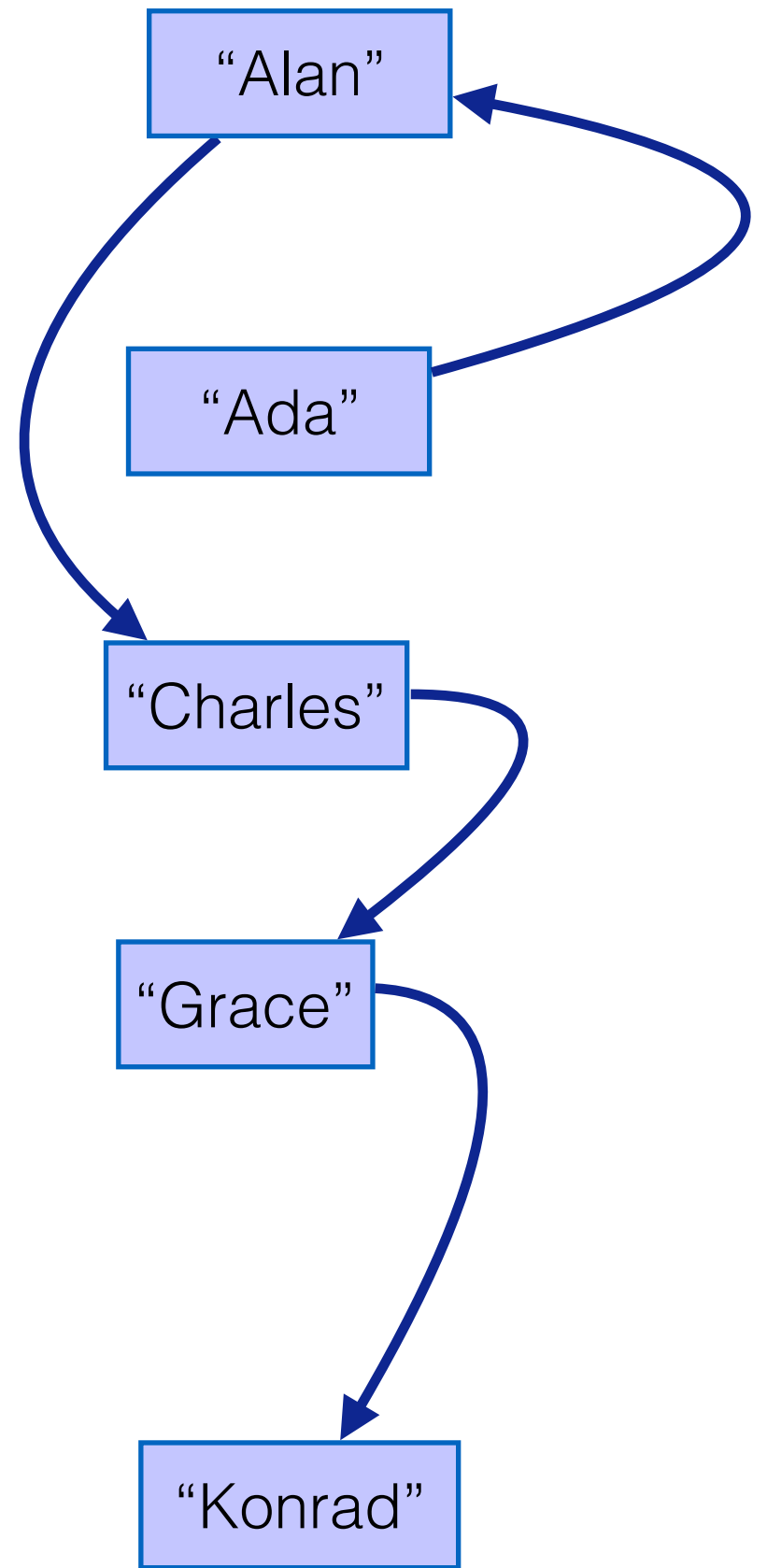


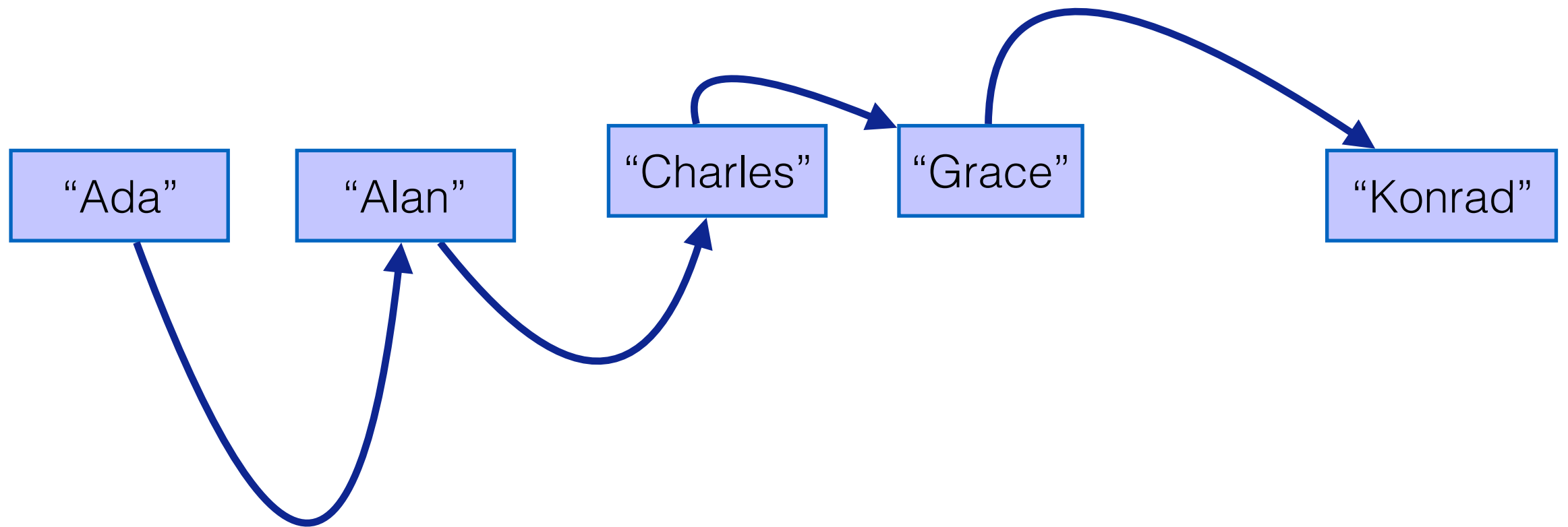
```
>>> n1 = Node("Konrad")
>>> n2 = Node("Grace", n1)
>>> n3 = Node("Charles", n2)
>>> n4 = Node("Ada", n3)
>>> n5 = Node("Alan")
>>> n5.next = n3
```




```
>>> n1 = Node("Konrad")
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>>> n3 = Node("Charles", n2)
>>> n4 = Node("Ada", n3)
>>> n5 = Node("Alan")
>>> n5.next = n3
>>> n4.next = n5
```







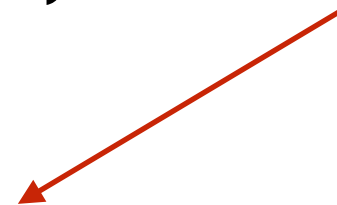
```
def print_structure(node):  
    current_node = node  
    while current_node is not None:  
        | print(current_node)  
        | current_node = current_node.next
```



Check if two things are **the same** , use **is**

Check if two things are **identical**, use **==**

calls `__eq__(self, other)`



Lecture 24

Linked Stacks

FIT 1008
Introduction to Computer Science



COMMONWEALTH OF AUSTRALIA

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Objectives for these this lecture

- To understand:
 - The concept of **linked data structures**
 - Their use in **implementing stacks**
- To be able to:
 - Implement, use and modify linked stacks
 - Decide when it is appropriate to use them (rather than arrays)

Where are we at?

- Implemented container ADT using arrays
- Know about Linked Structures
- Have implemented Nodes

How many of the following characteristics does a linked data structure has?

- Fixed size
- Data stored sequentially
- Each item occupies the same amount of space

A) 0

B) 1

C) 2

D) 3

How many of the following characteristics does a linked data structure has?

- Fixed size
- Data stored sequentially
- Each item occupies the same amount of space

A) 0

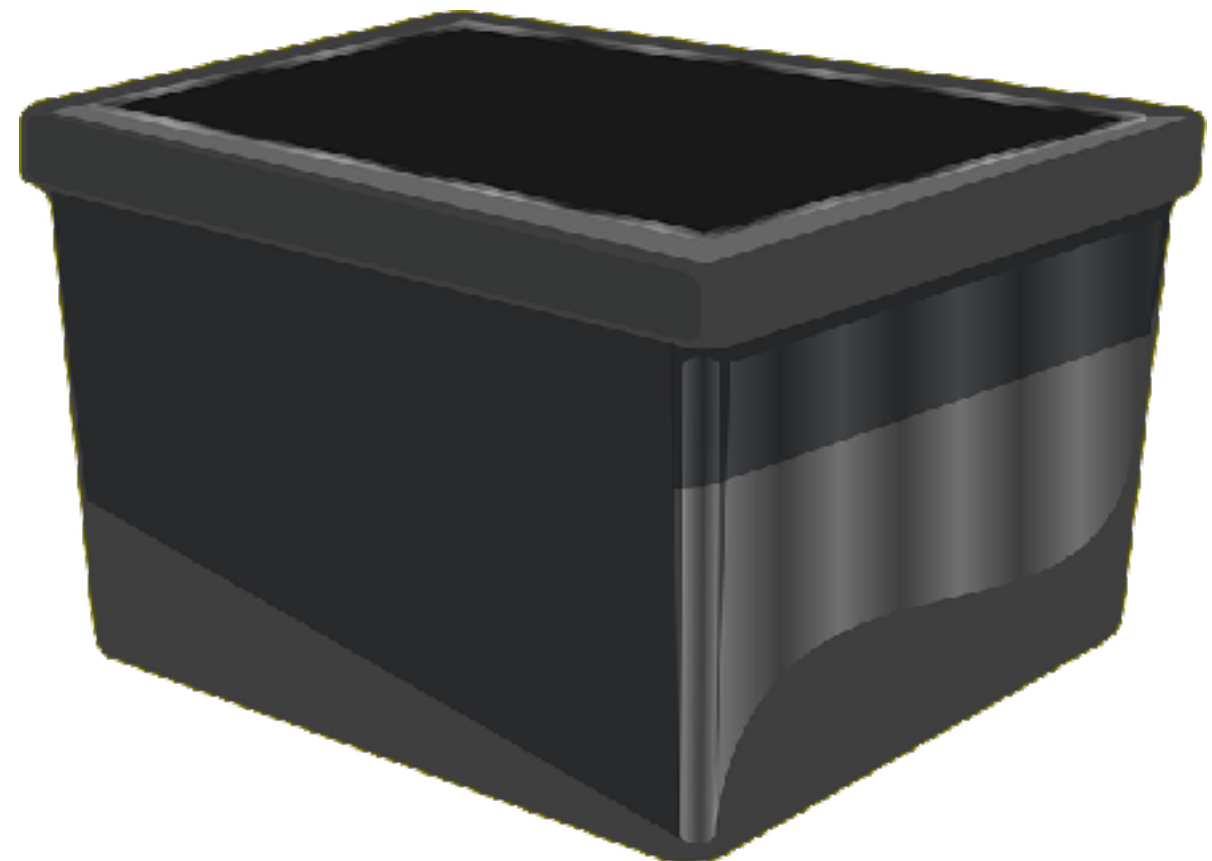
B) 1

C) 2

D) 3

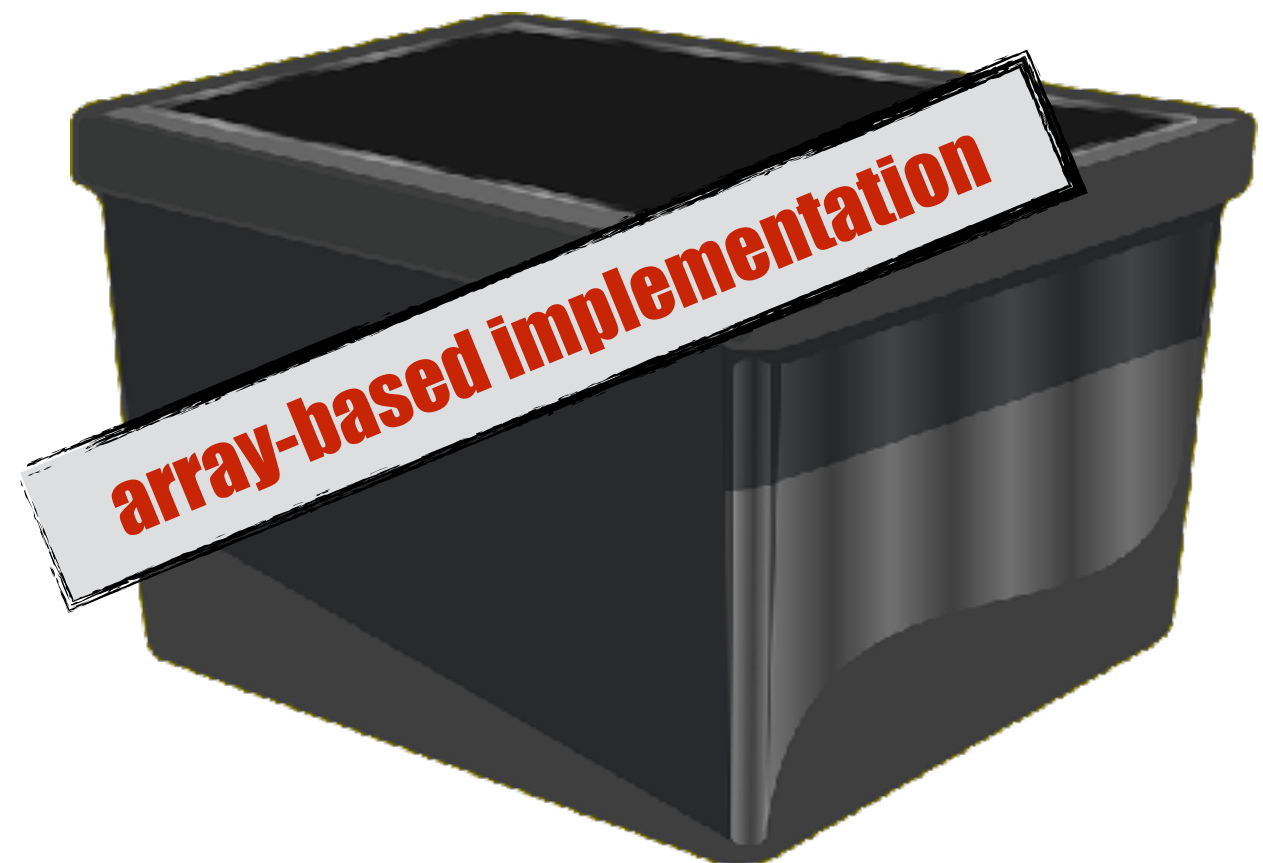
Container ADTs

- **Stores** and **removes** items **independent of contents**.
- **Examples** include:
 - List ADT ☒
 - Stack ADT ☒
 - Queue ADT. ☒
- Core **operations**:
 - ➔ add item
 - ➔ remove item



Container ADTs

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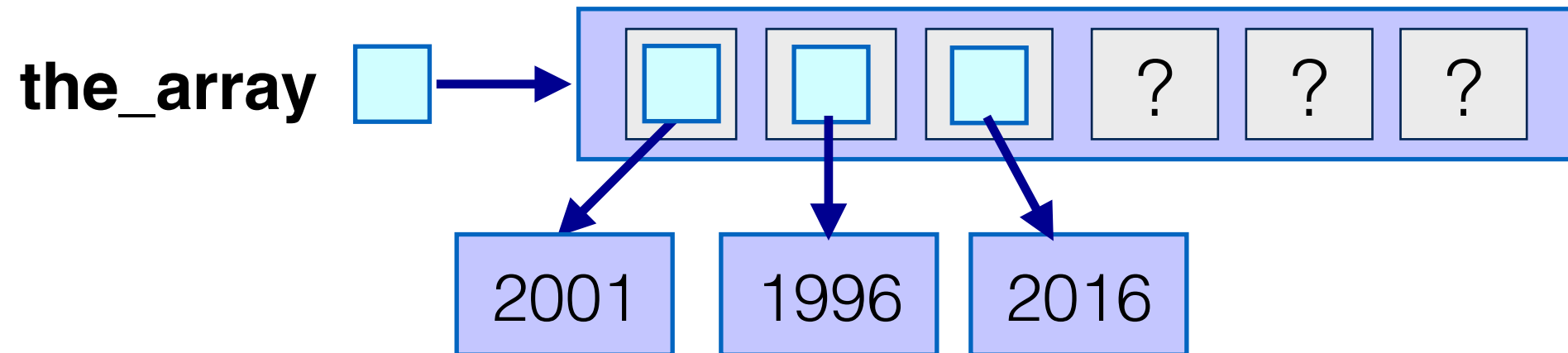


Array implementation

- Array **characteristics**:
 - Fixed size
 - Data items are stored sequentially
 - Each item occupies exactly the same amount of space

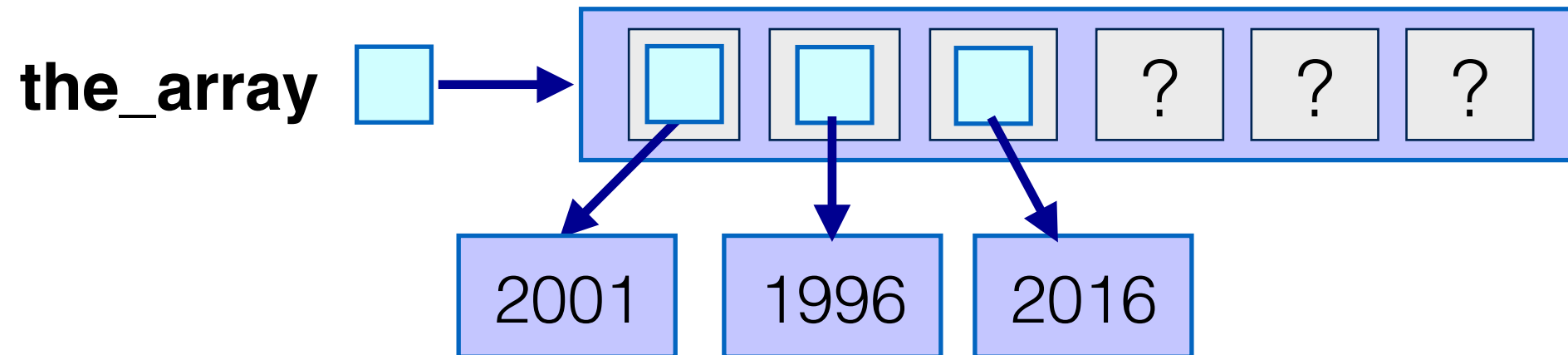
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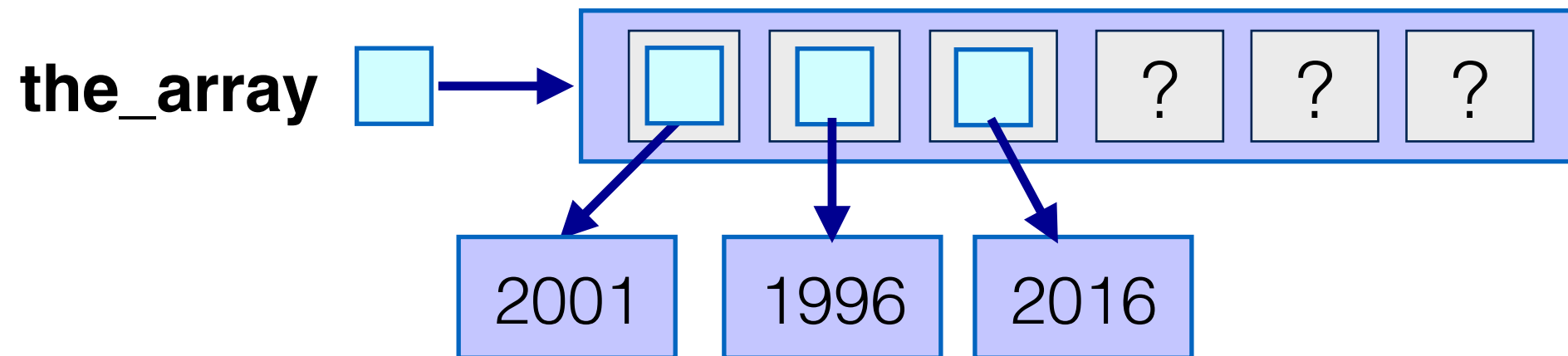
- Array **characteristics**:
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 - Each item occupies exactly the same amount of space



- Main **advantages**:
 - Very **fast** access $O(1)$
 - Very **compact** representation if the array is full

Array implementation

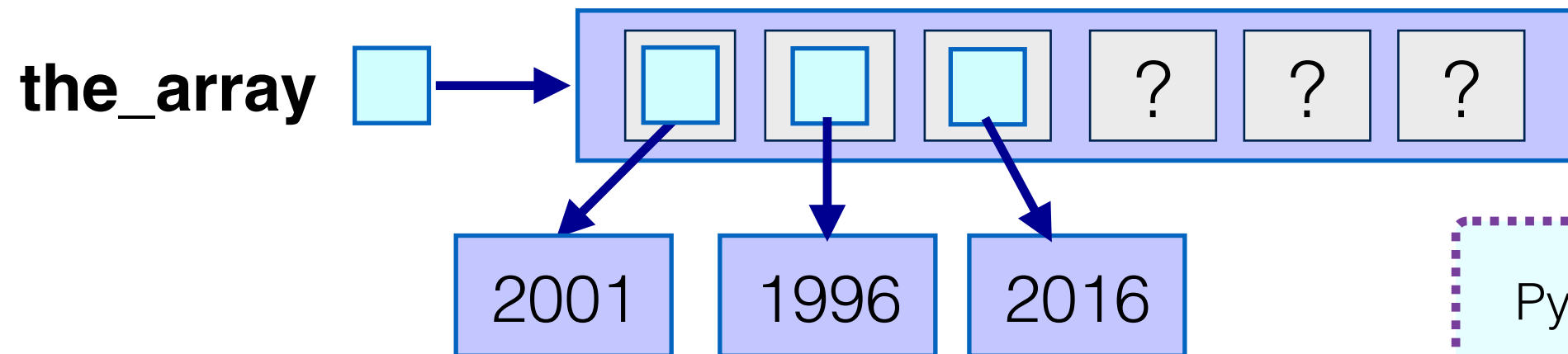
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- Main **disadvantages**:
 - Non-resizable: maximum size specified on creation
 - Changing size is costly: **create a new array + copy all items**
 - Slow operations if shuffling elements is required

Array implementation

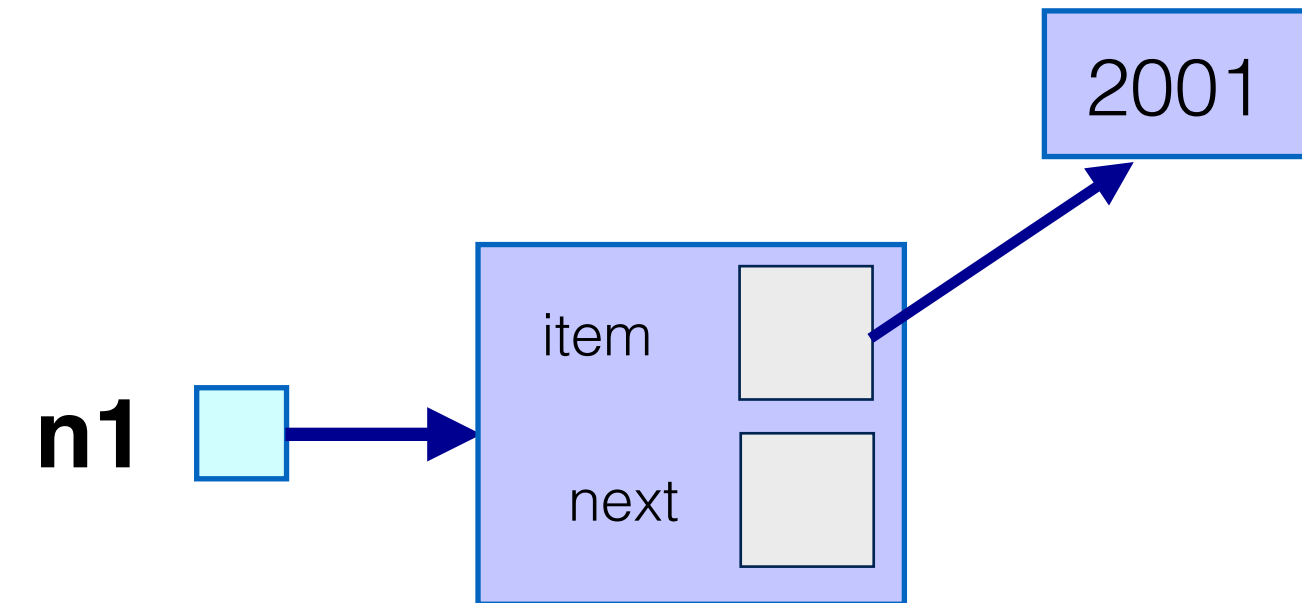
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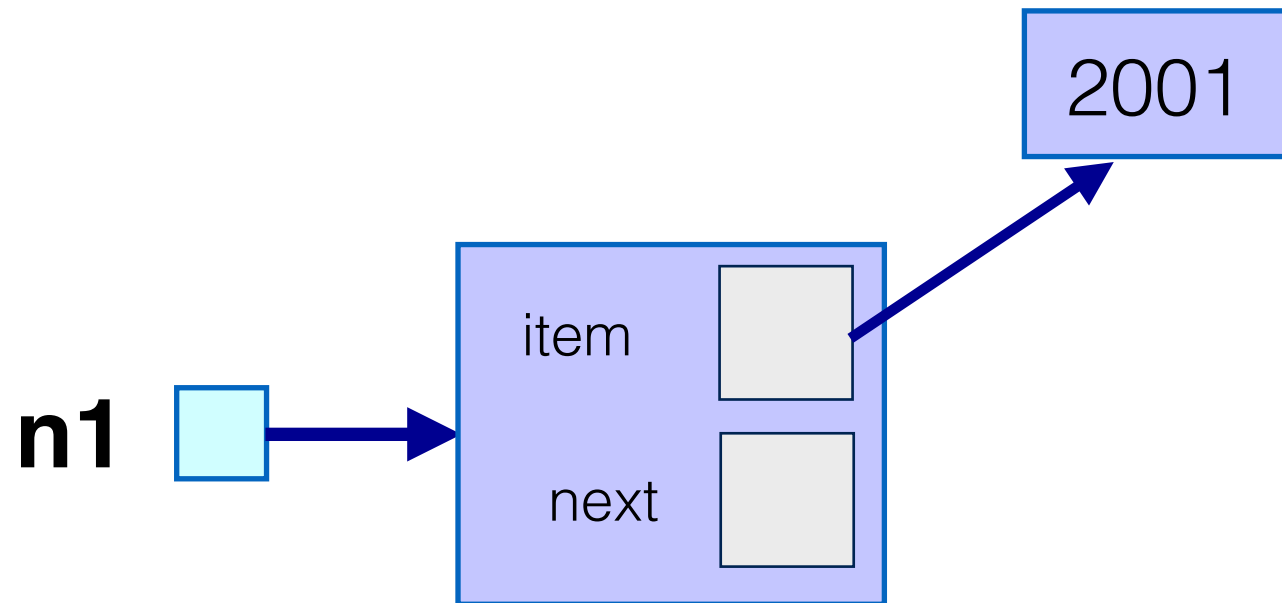
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 - Slow operations if shuffling elements is required

Python lists: array growth pattern is 0, 4, 8, 16, 25, 35, 46, 58, 72, 88,...

Linked Data Structures

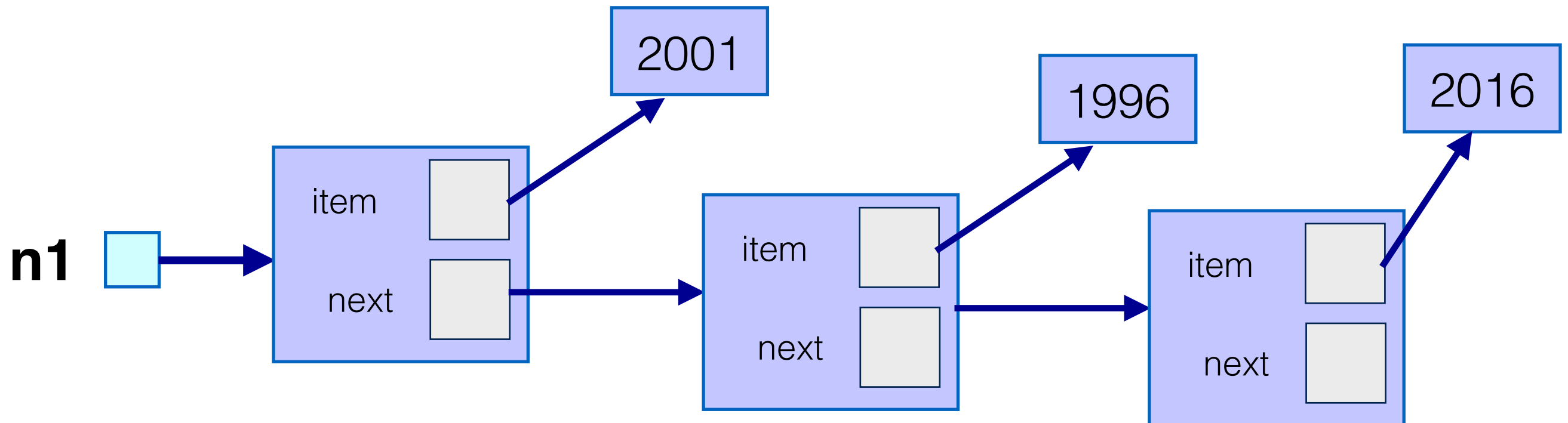


Linked Data Structures



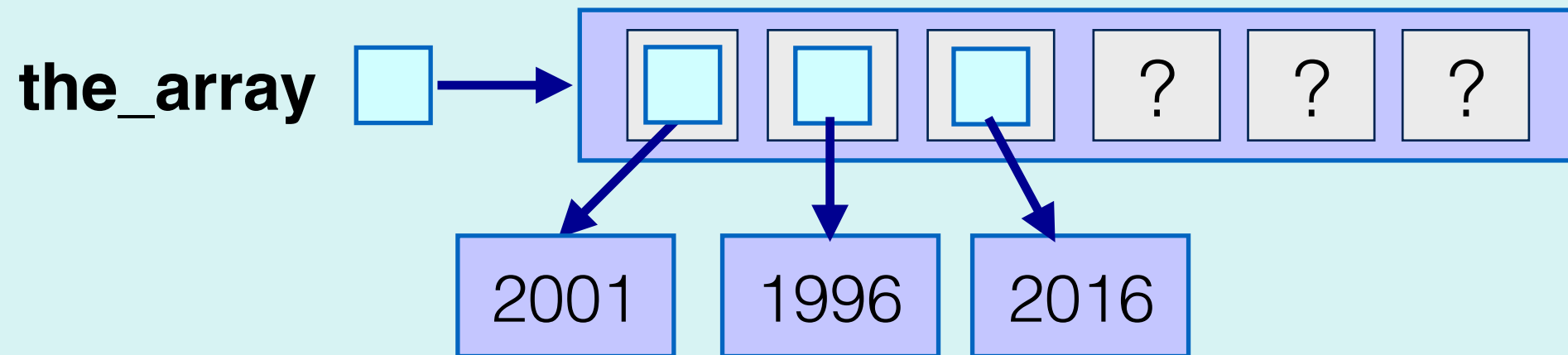
- Collection of nodes
- Each node contains:
 - One or more **data items**
 - One or more **links to other nodes**

Linked Data Structures

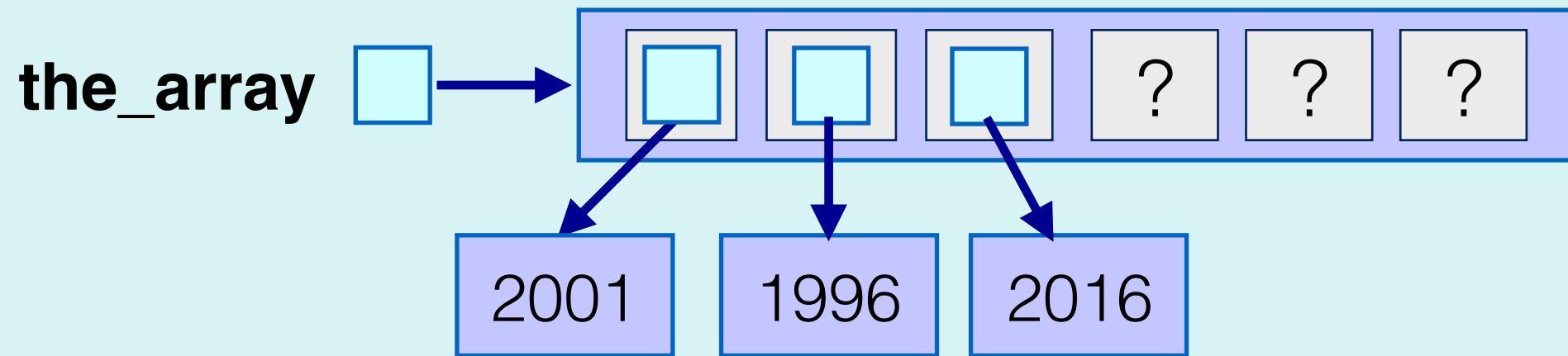


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Array-based Data Structures:

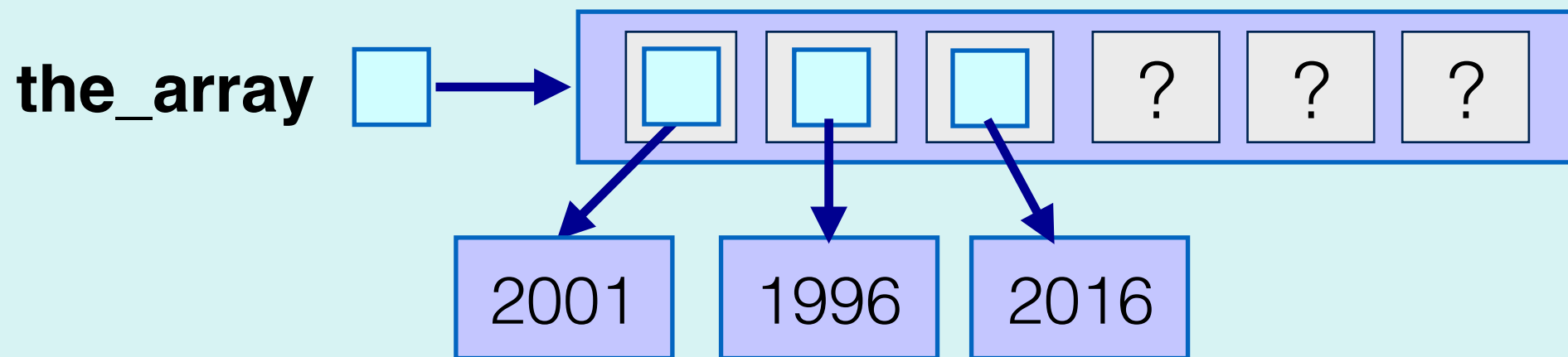


Array-based Data Structures:

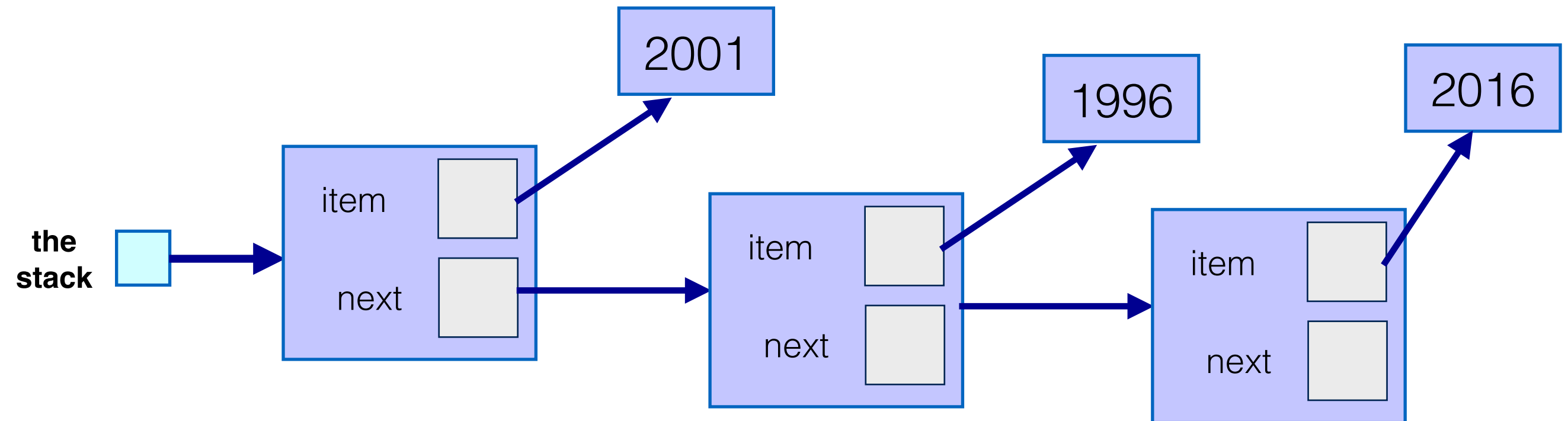


Linked Data Structures:

Array-based Data Structures:



Linked Data Structures:



Linked Data Structures: **Advantages**

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- **Fast** insertions and deletions of items
(no need for reshuffling)

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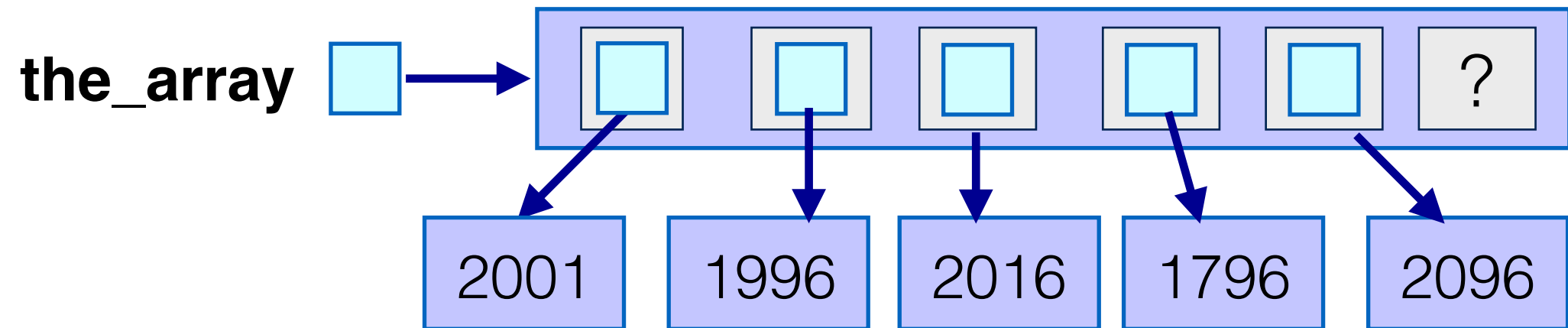
Linked Data Structures: **Advantages**

- **Fast** insertions and deletions of items (no need for reshuffling)
- Easily **resizable**: just create/delete node
- Never full (only if no more memory left)

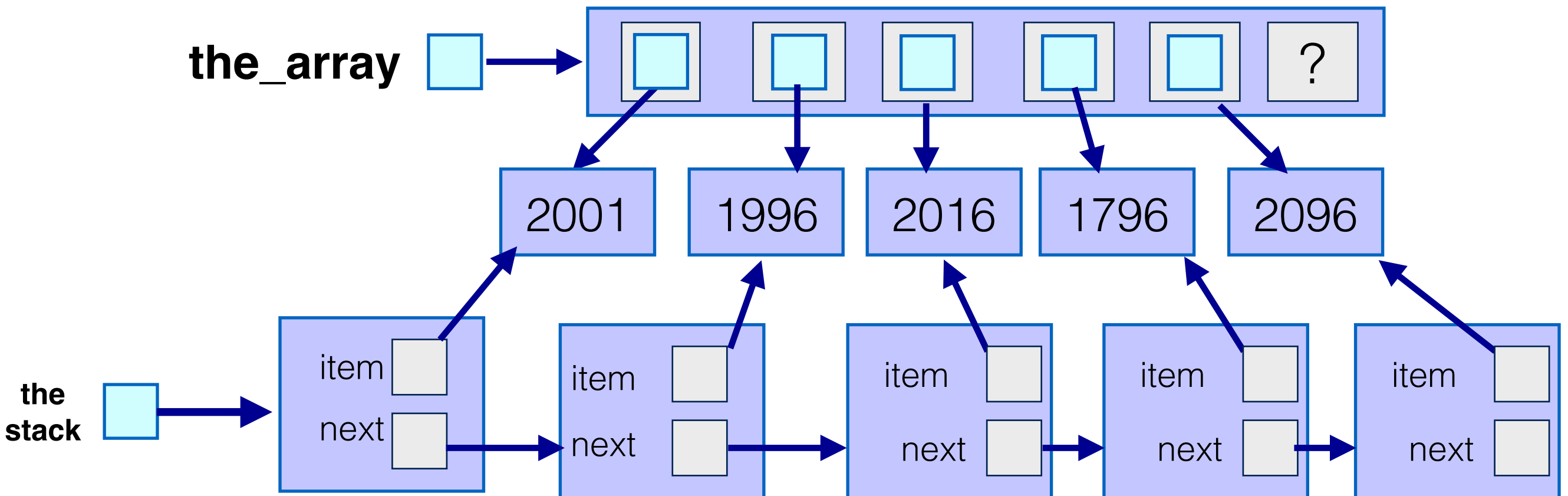
Linked Data Structures: **Advantages**

- **Fast** insertions and deletions of items (no need for reshuffling)
- Easily **resizable**: just create/delete node
- Never full (only if no more memory left)
- Less memory used than an array if the array-based implementation is relatively empty

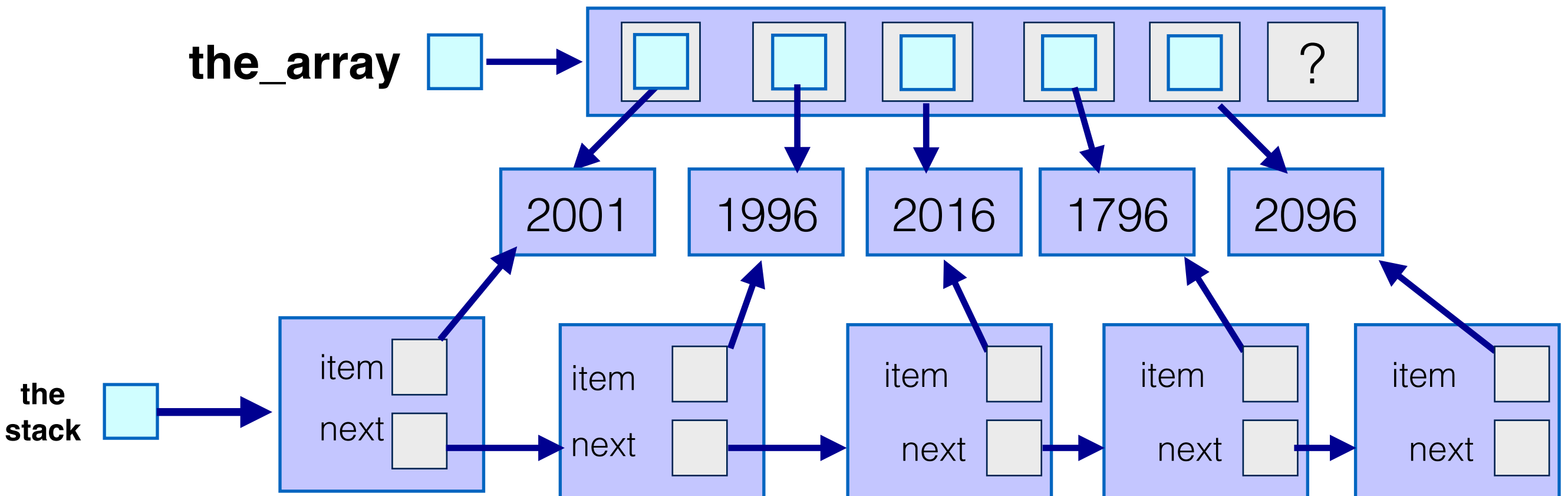
Linked Data Structures: **Disadvantages**



Linked Data Structures: **Disadvantages**

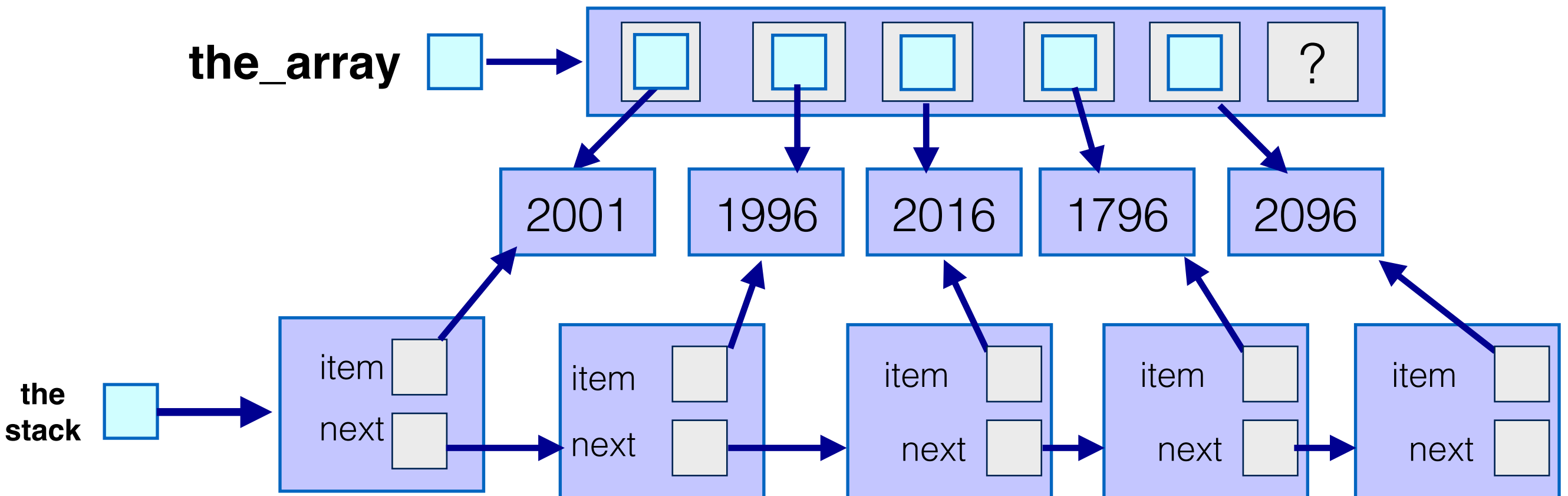


Linked Data Structures: **Disadvantages**

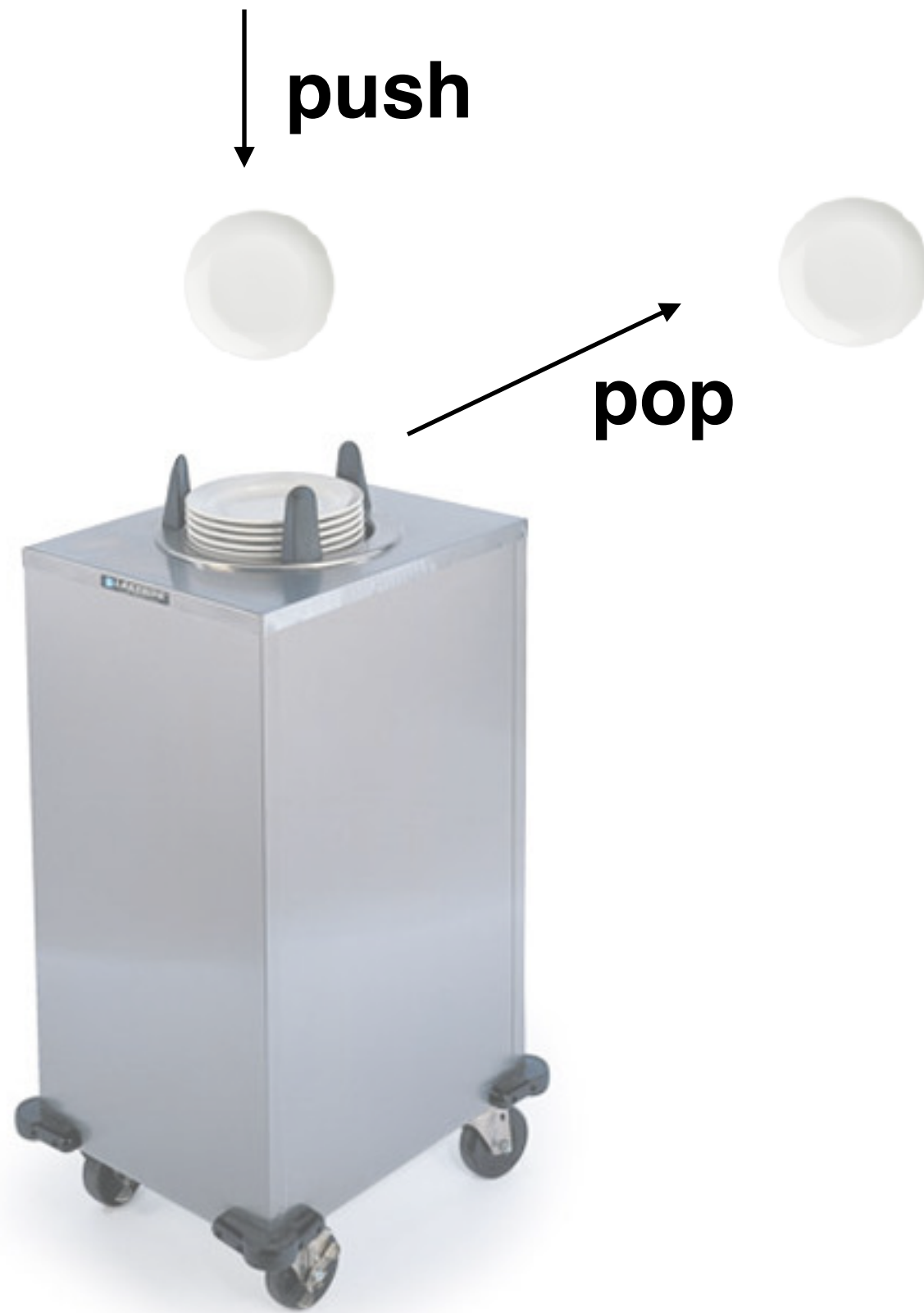


- More **memory** used than an array if the array is relatively full (Reason: every data item has an associated link)

Linked Data Structures: **Disadvantages**



- More **memory** used than an array if the array is relatively full (Reason: every data item has an associated link)
- For some data types certain operations are more time consuming (e.g., no random access)

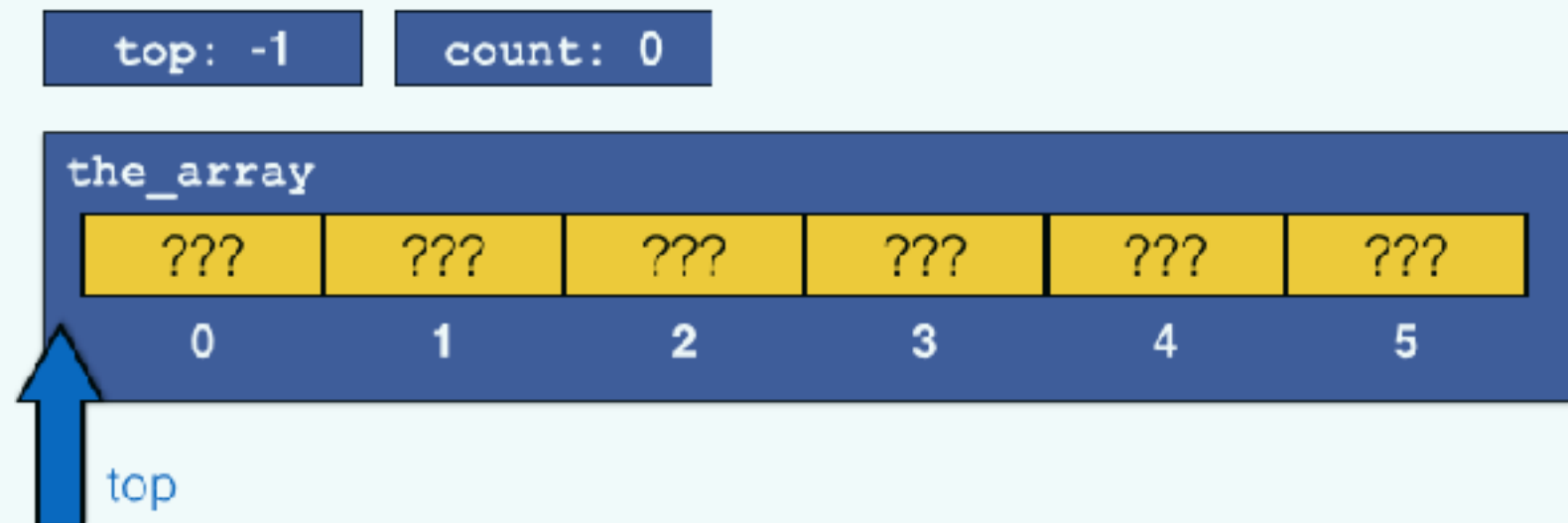


Stack Data Type

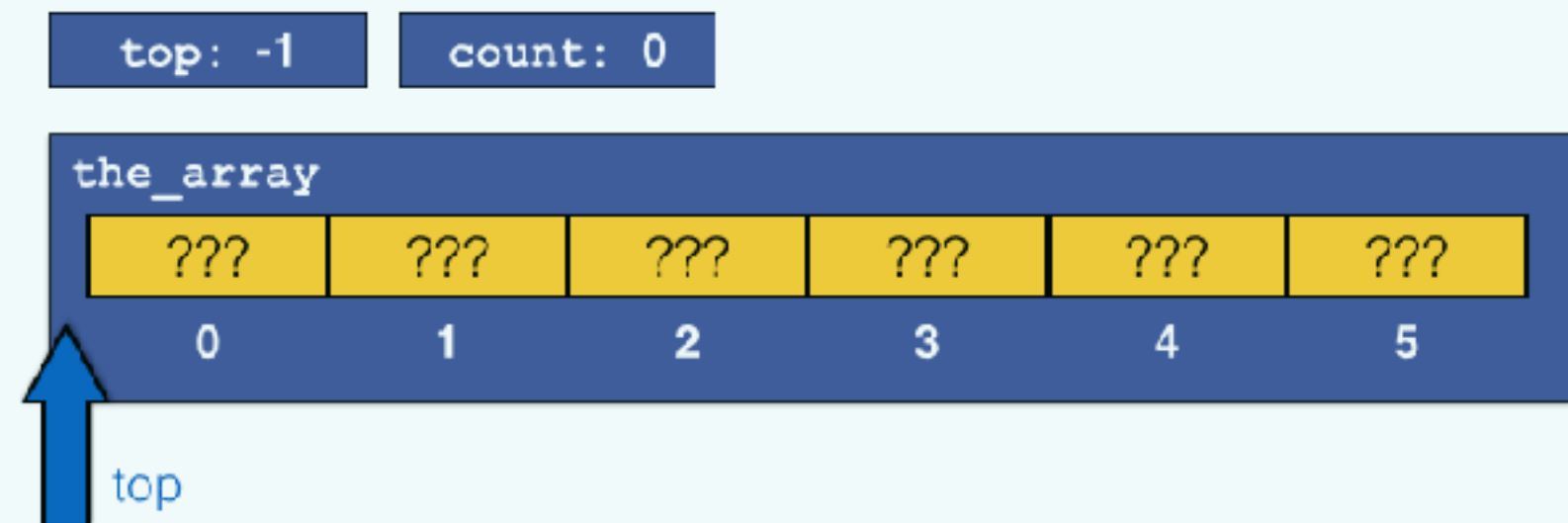
- Follows a **LIFO model**
- Its **operations** (interface) are :
 - **Create** a stack (Stack)
 - Add an item to the top (**push**)
 - Take an item off the top (**pop**)
 - Look at the item on top, don't alter the stack (top/**peek**)
 - Is the stack **empty**?
 - Is the stack **full**?
 - Empty the stack (**reset**)

Remember: it only provides access to the element at the top of the stack (last element added)

Array Stack Implementation



Array Stack Implementation

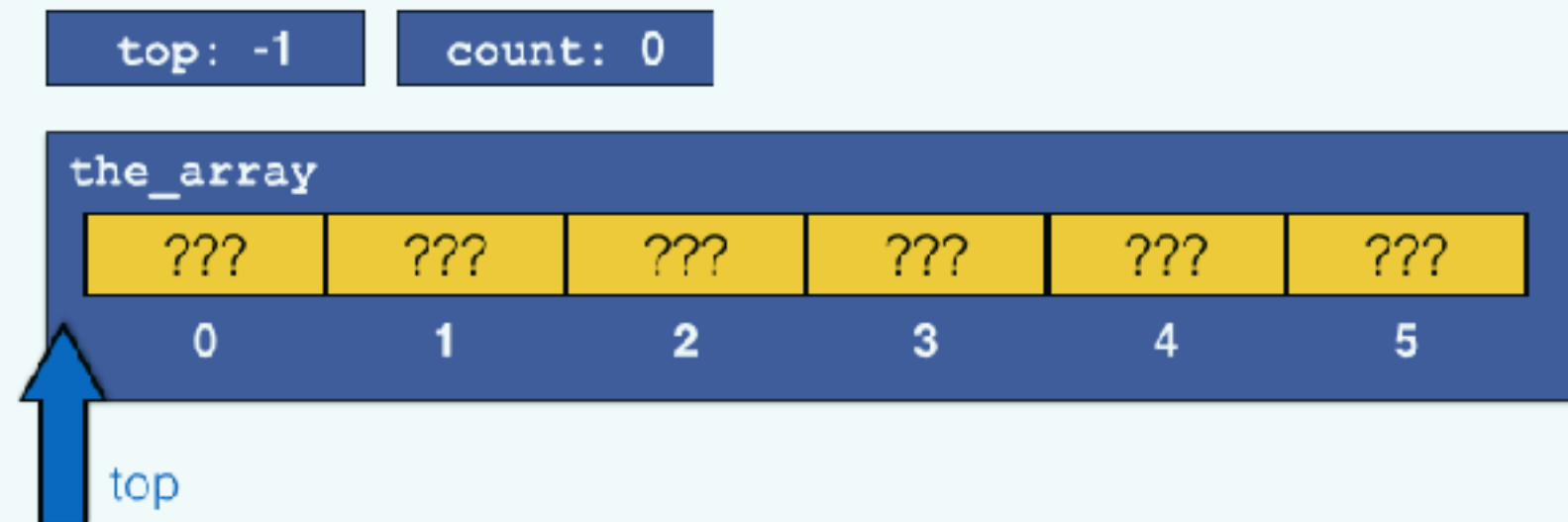


What do we need for a linked implementation?

Nodes!

Linked Stack Implementation

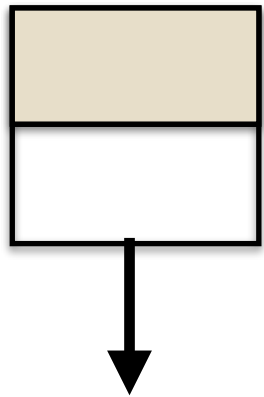
Array Stack Implementation



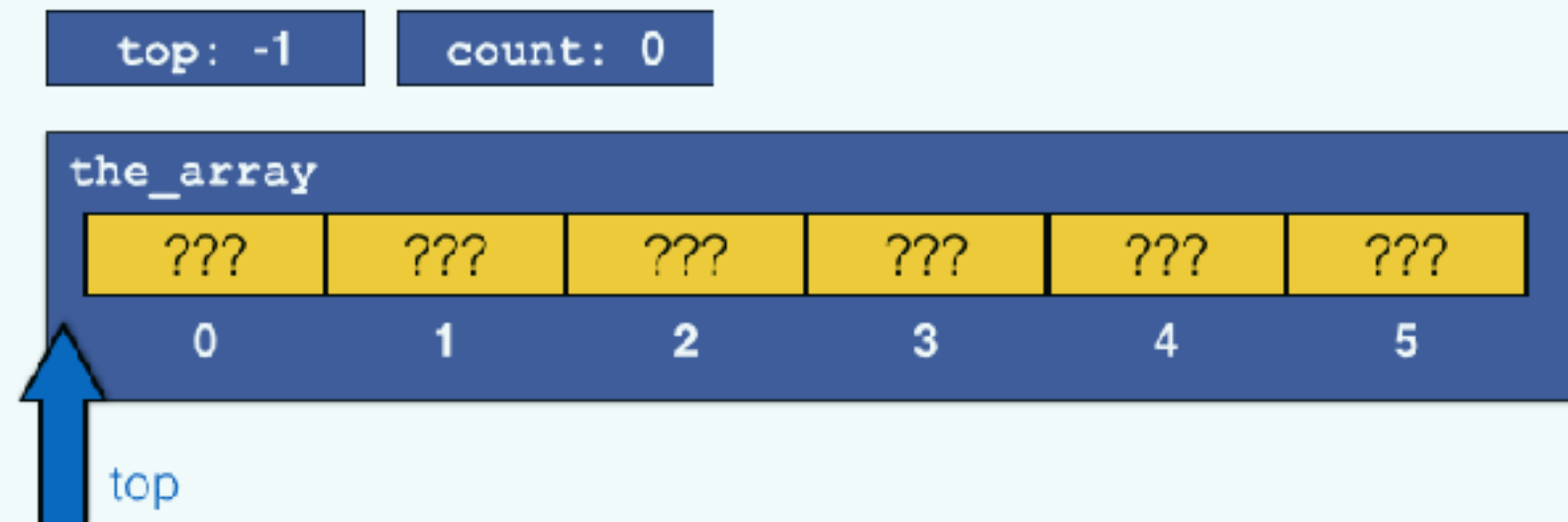
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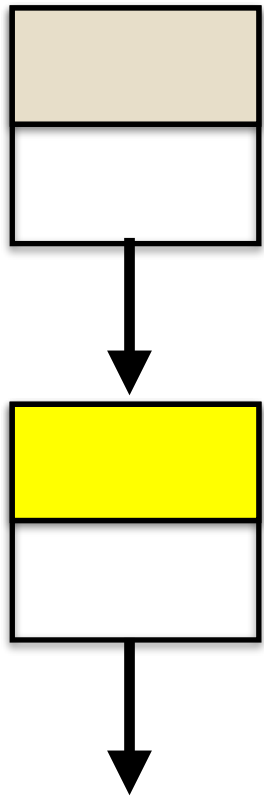
Array Stack Implementation



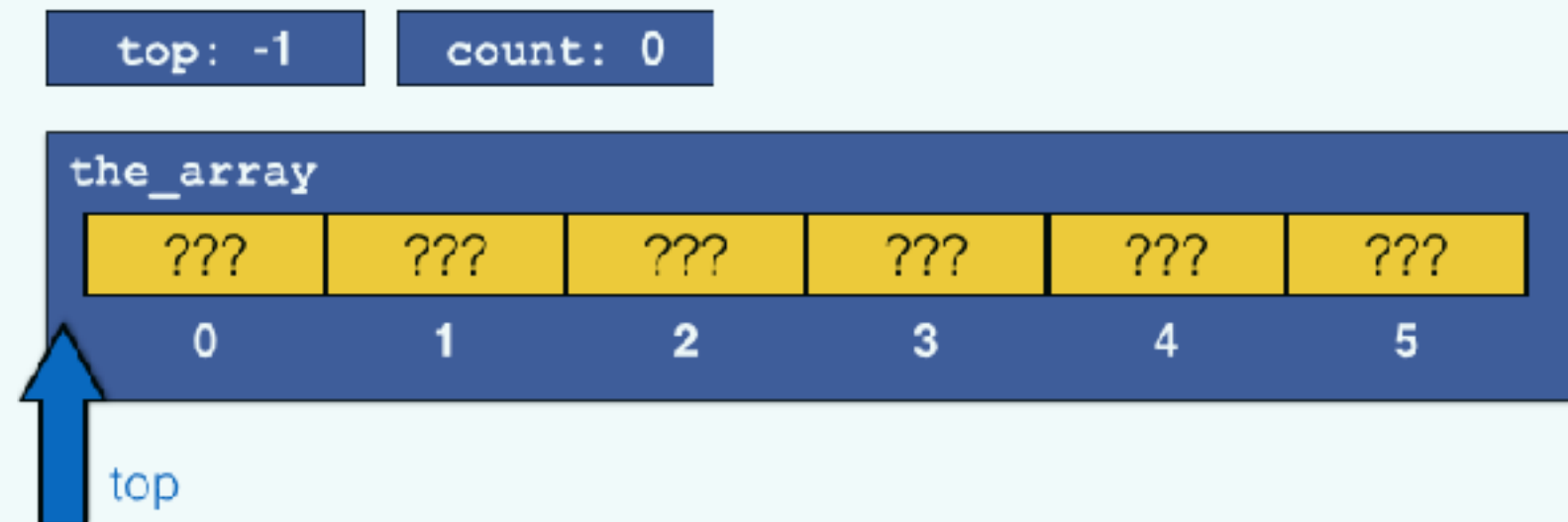
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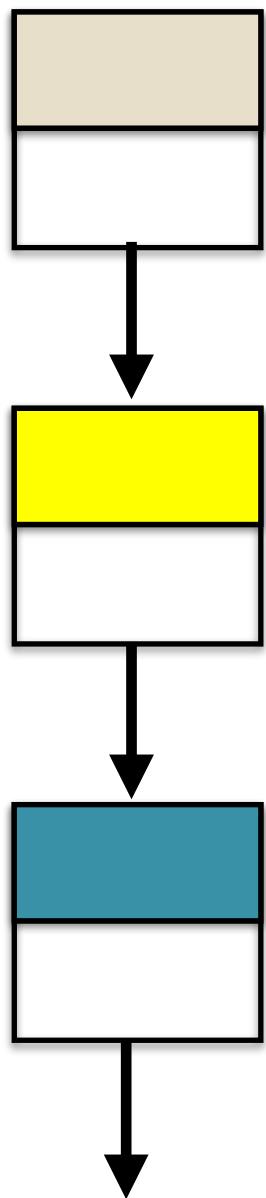
Array Stack Implementation



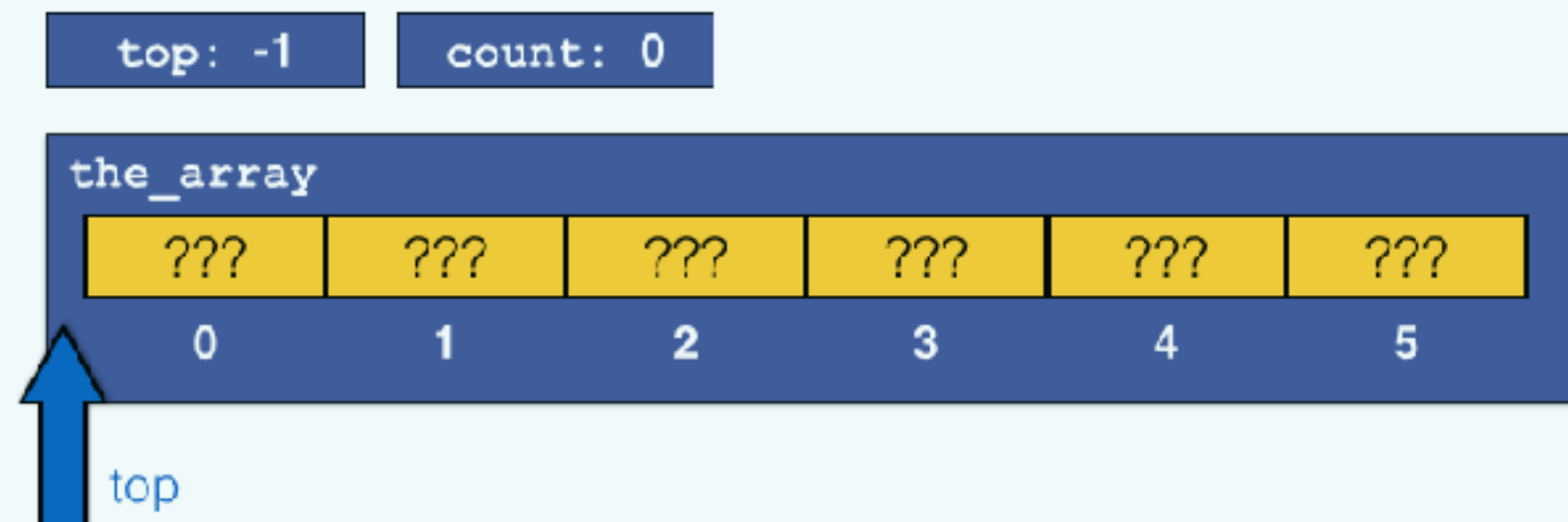
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Linked Stack Implementation



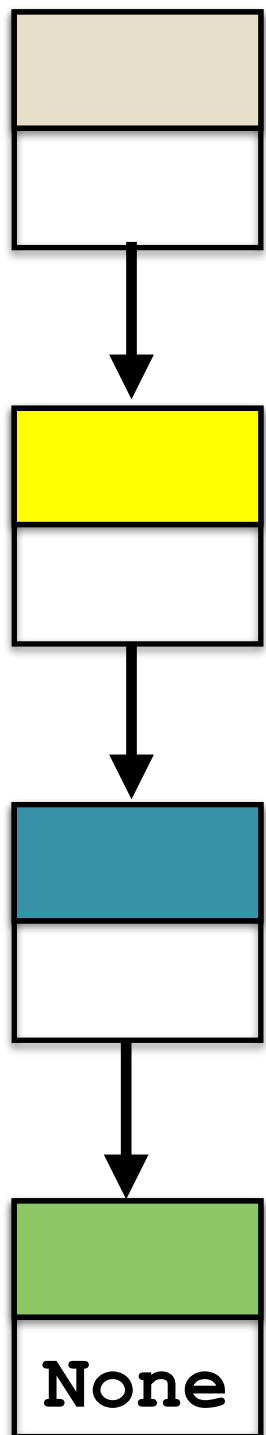
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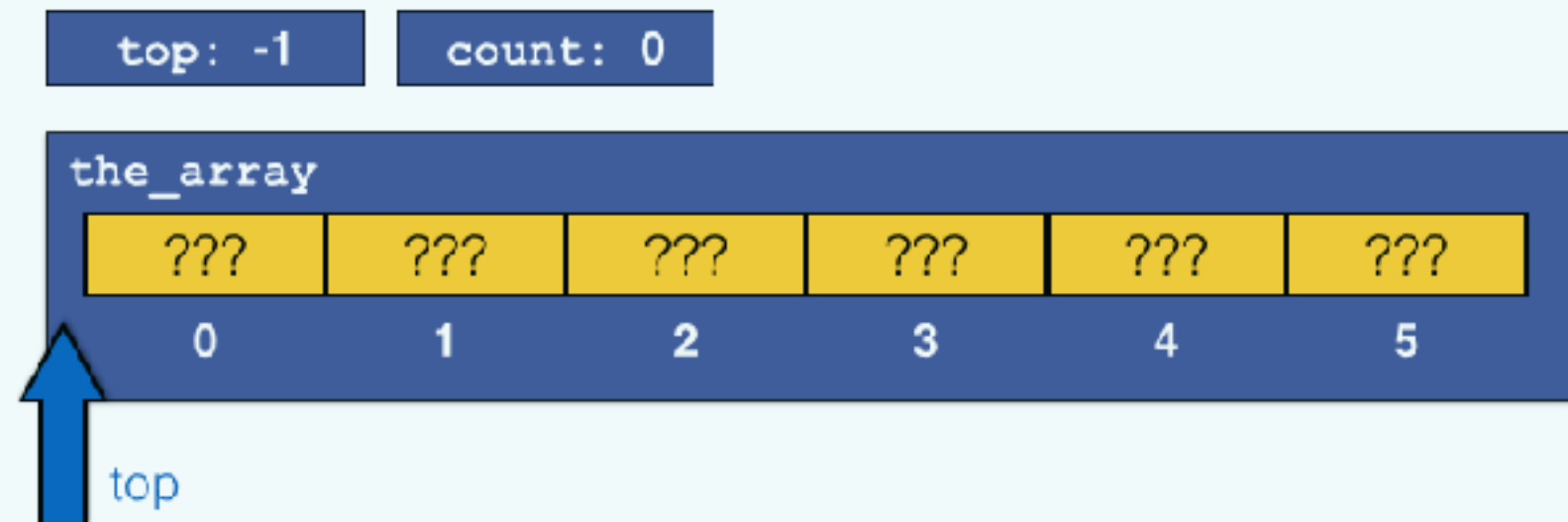
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Linked Stack Implementation



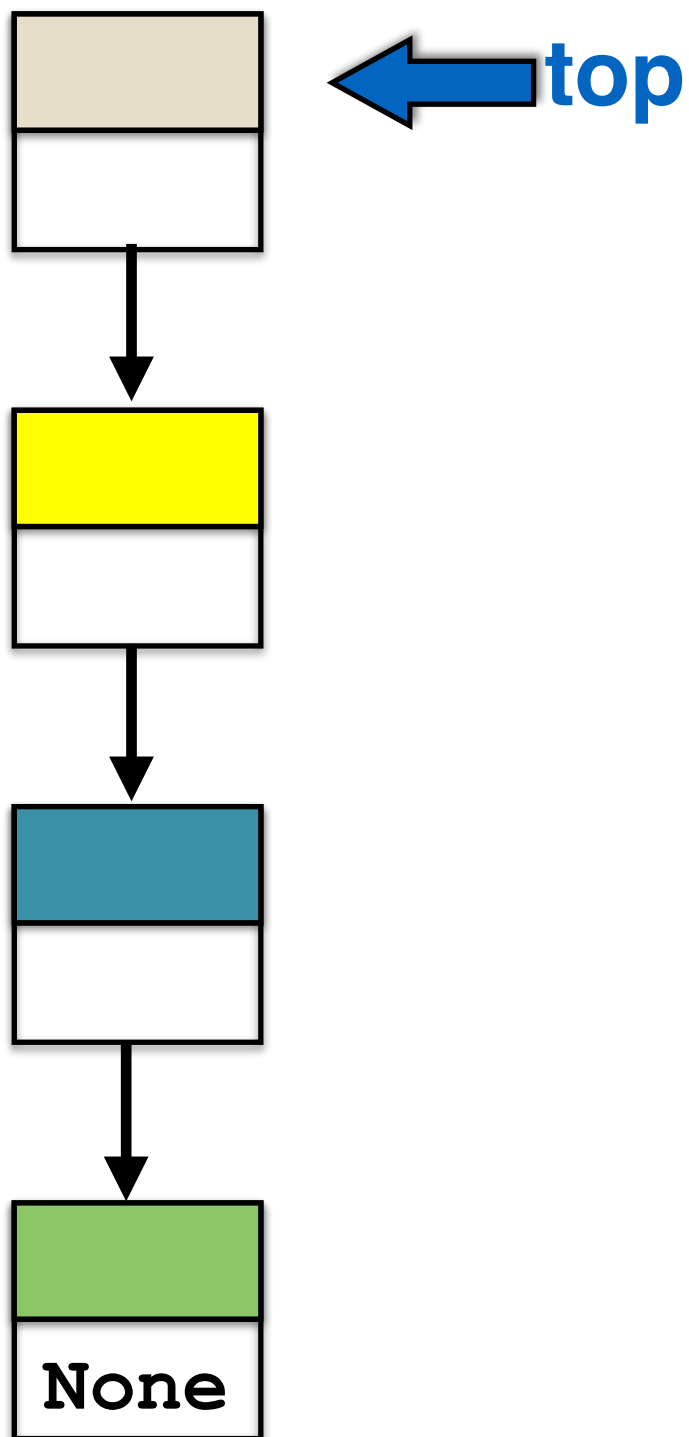
Array Stack Implementation



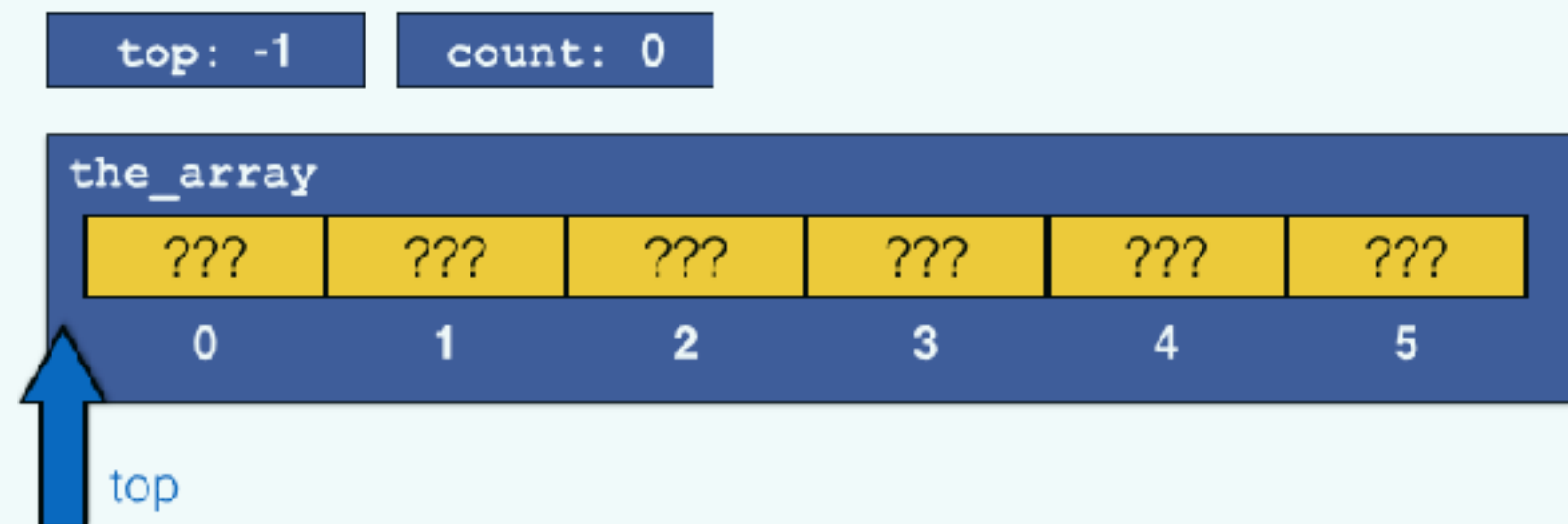
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Nodes!

Linked Stack Implementation



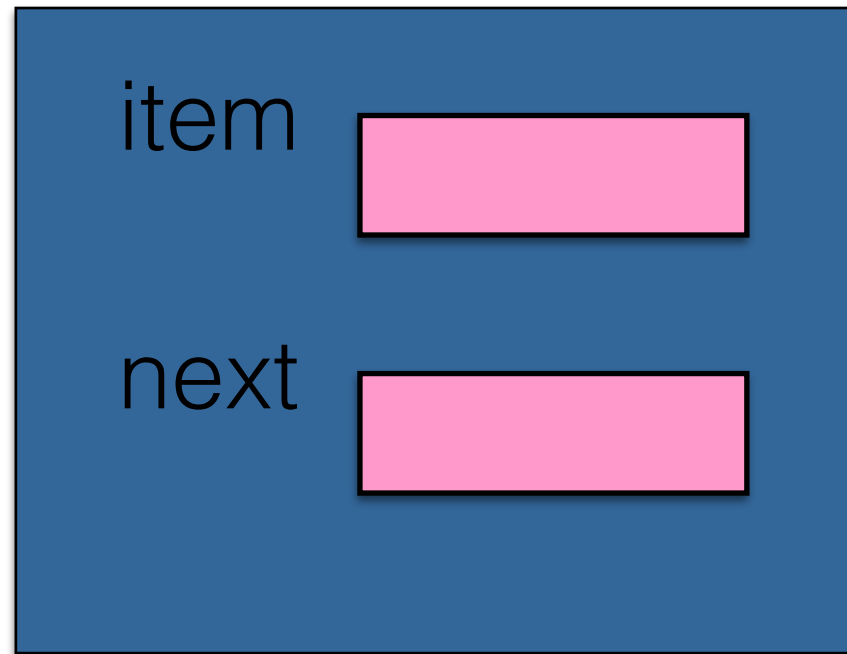
Array Stack Implementation



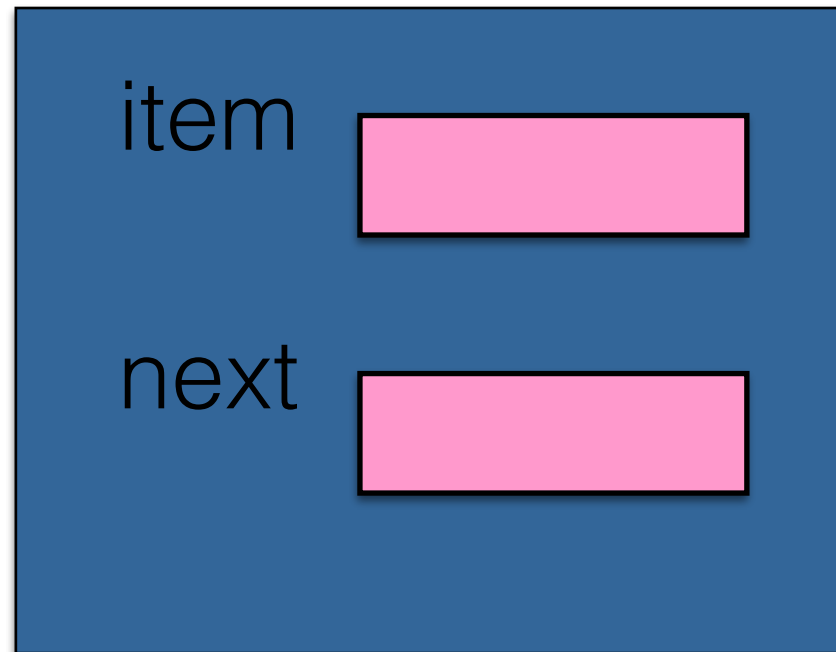
What do we need for a linked implementation?

Nodes!

Node



Node



```
class Node:  
    def __init__(self, item, link):  
        self.item = item  
        self.next = link
```

```
from node import Node
```

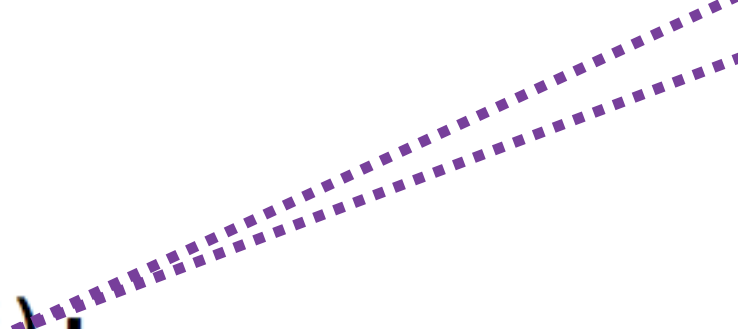
```
from node import Node
```

```
class Stack:
```

```
from node import Node
```

```
class Stack:  
    def __init__(self):  
        self.top = None
```

No need for size when
initialising the object



```
from node import Node
```

```
class Stack:
```

```
    def __init__(self):  
        self.top = None
```

```
    def is_empty(self):  
        return self.top is None
```



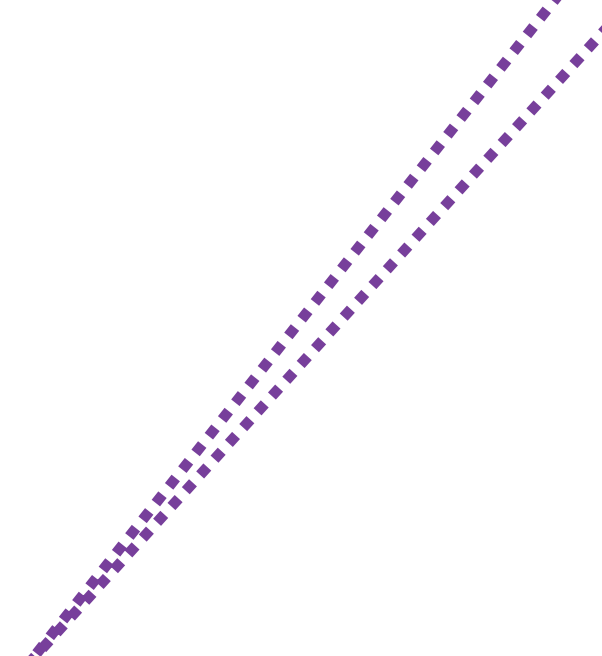
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True if pointing to the
same object.



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class Stack:
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```
    def __init__(self):  
        self.top = None
```

```
    def is_empty(self):  
        return self.top is None
```

True if pointing to the same object.

self.top == **None** ?
== can be overloaded
implementing
__eq__(self, rhs)

```
from node import Node
```

```
class Stack:
```

```
    def __init__(self):  
        self.top = None
```

```
    def is_empty(self):  
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```

```
    def is_full(self):  
        return False
```

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```

```
class Stack:
```

```
    def __init__(self):  
        self.top = None
```

```
    def is_empty(self):  
        return self.top is None
```

```
    def is_full(self):  
        return False
```

```
    def reset(self):  
        self.top = None
```

Push: algorithm

Array implementation:

Push: algorithm

Array implementation:

- If the array is full raise exception
- Else
 - Add item in the position marked by top
 - Increase top

Push: algorithm

Array implementation:

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Linked implementation:

Push: algorithm

Array implementation:

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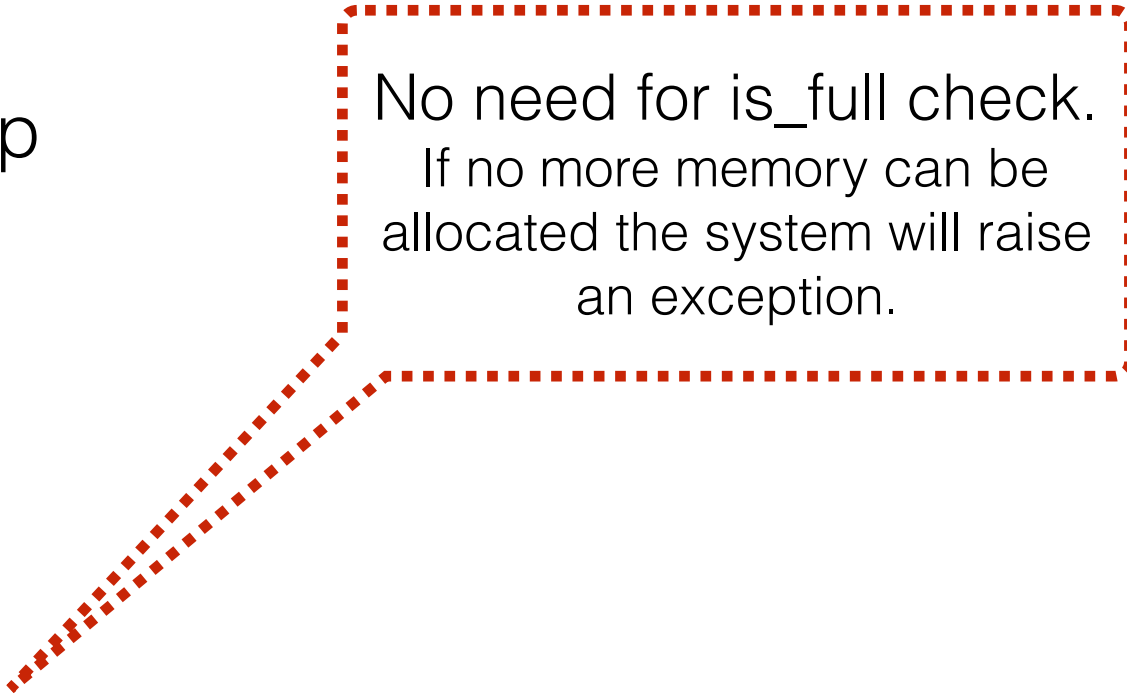
Linked implementation:

- Create a **new node** that contains the new item and is linked to the current top
- Make the **new node** the **new top**

Push: algorithm

Array implementation:

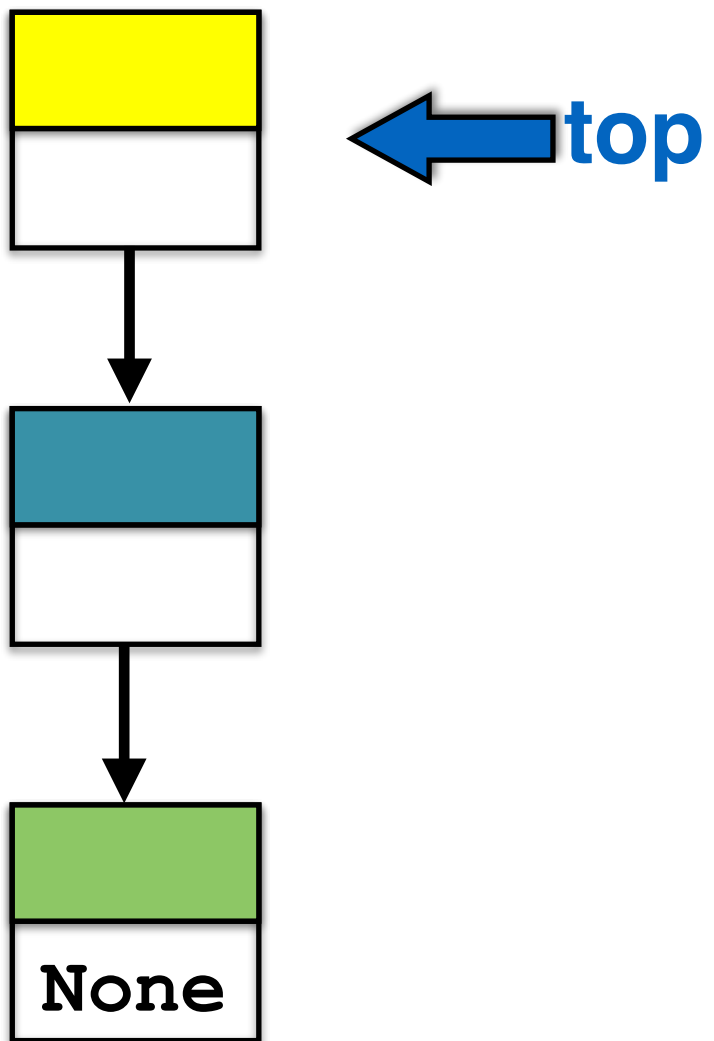
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 - Add item in the position marked by top
 - Increase top



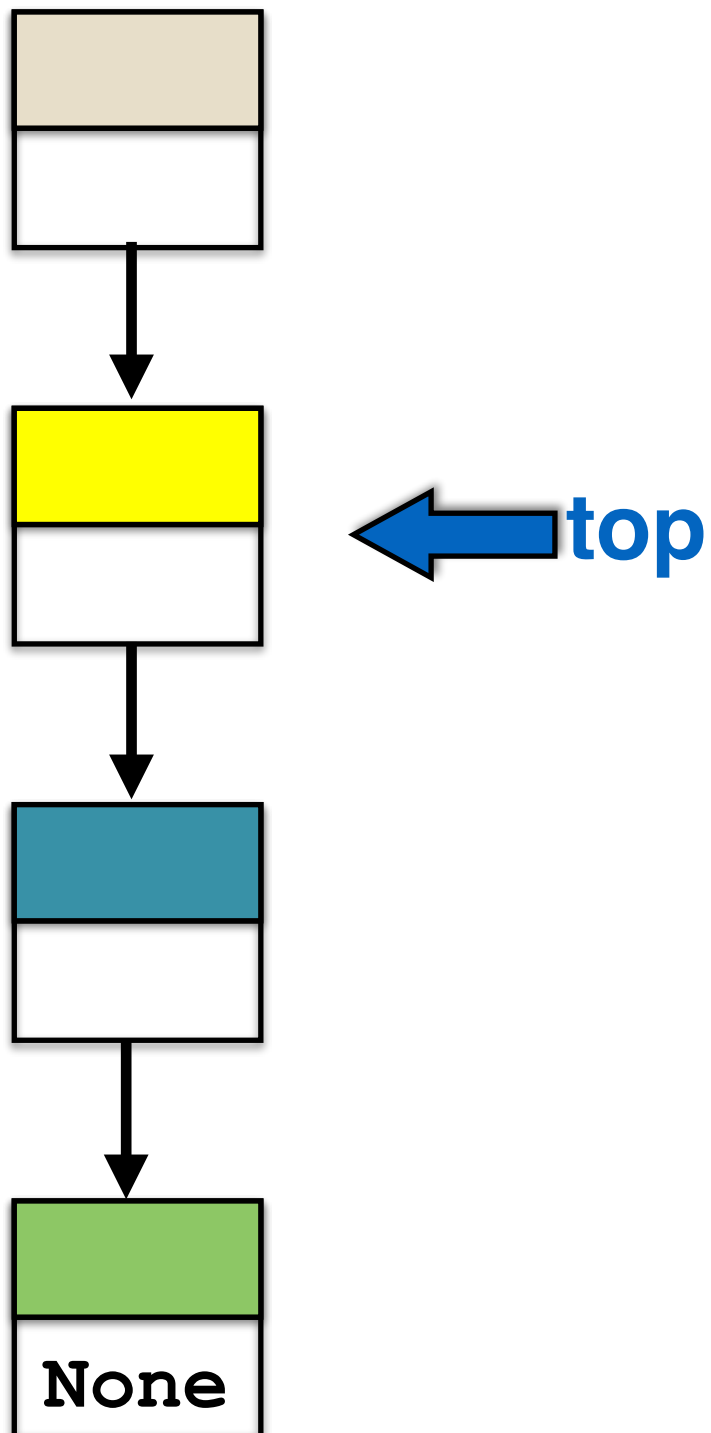
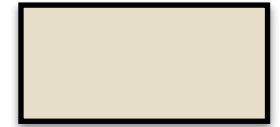
No need for is_full check.
If no more memory can be
allocated the system will raise
an exception.

Linked implementation:

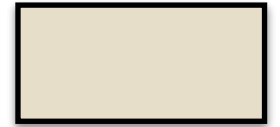
- Create a **new node** that contains the new item and is linked to the current top
- Make the **new node** the **new top**



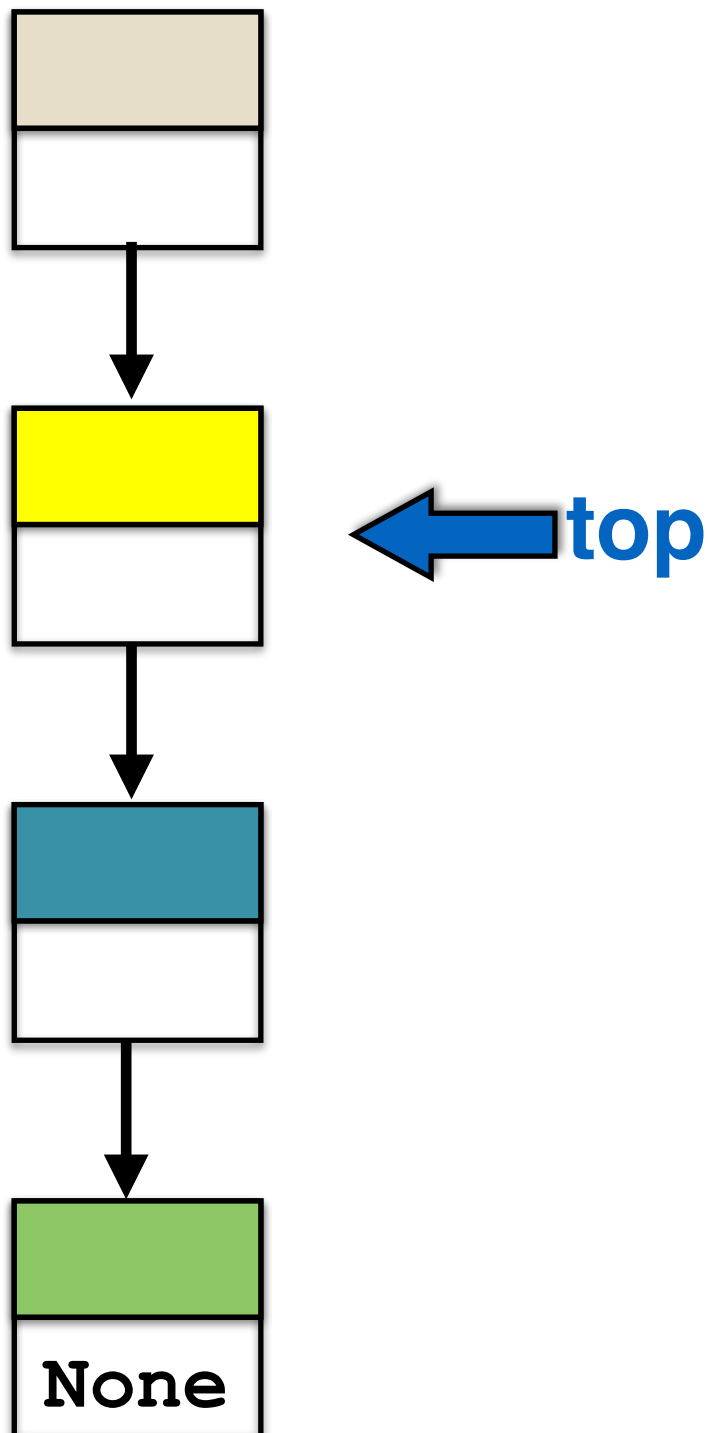
Create a new node with the new item.
linked to the current top



Create a new node with the new item.
linked to the current top



Make the new node the new **top**

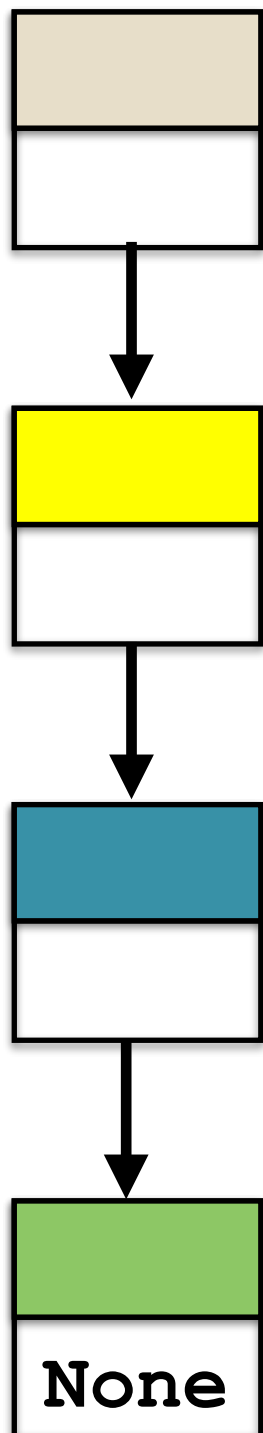


Create a new node with the new item.
linked to the current top

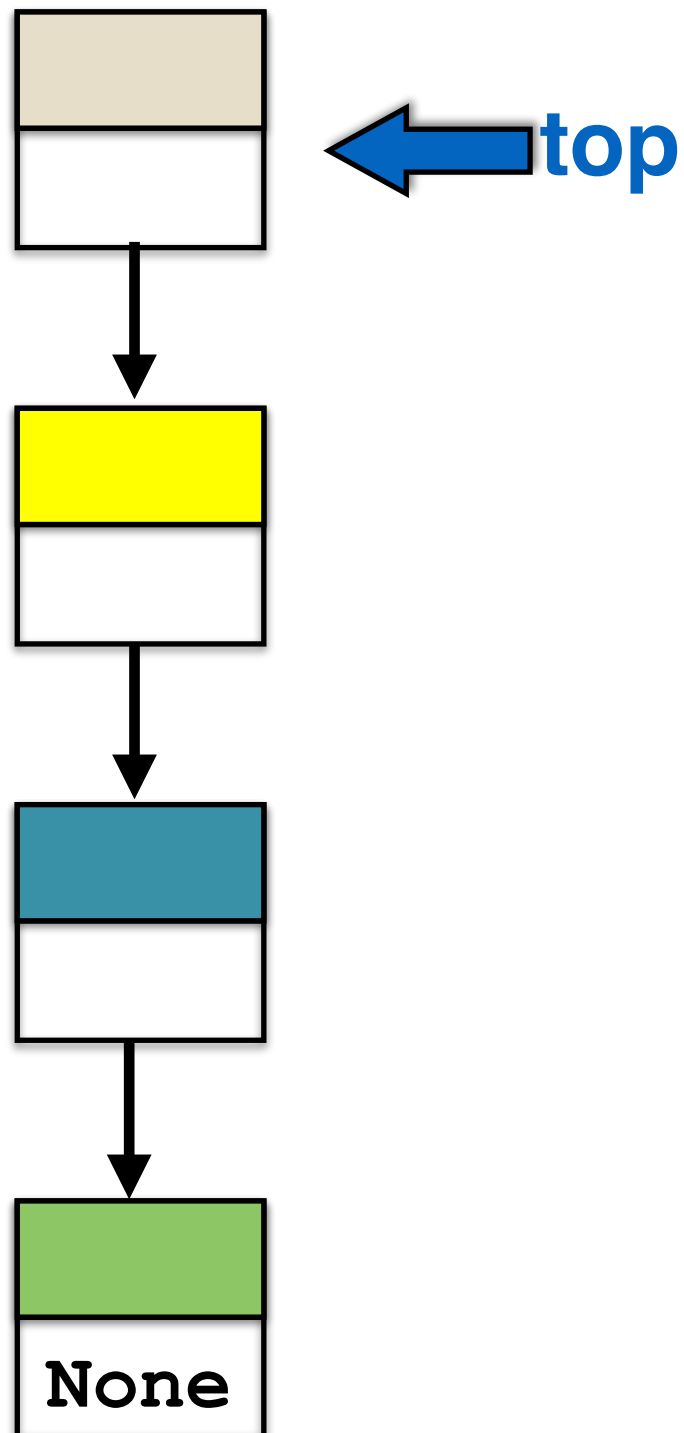


← **top**

Make the new node the new **top**

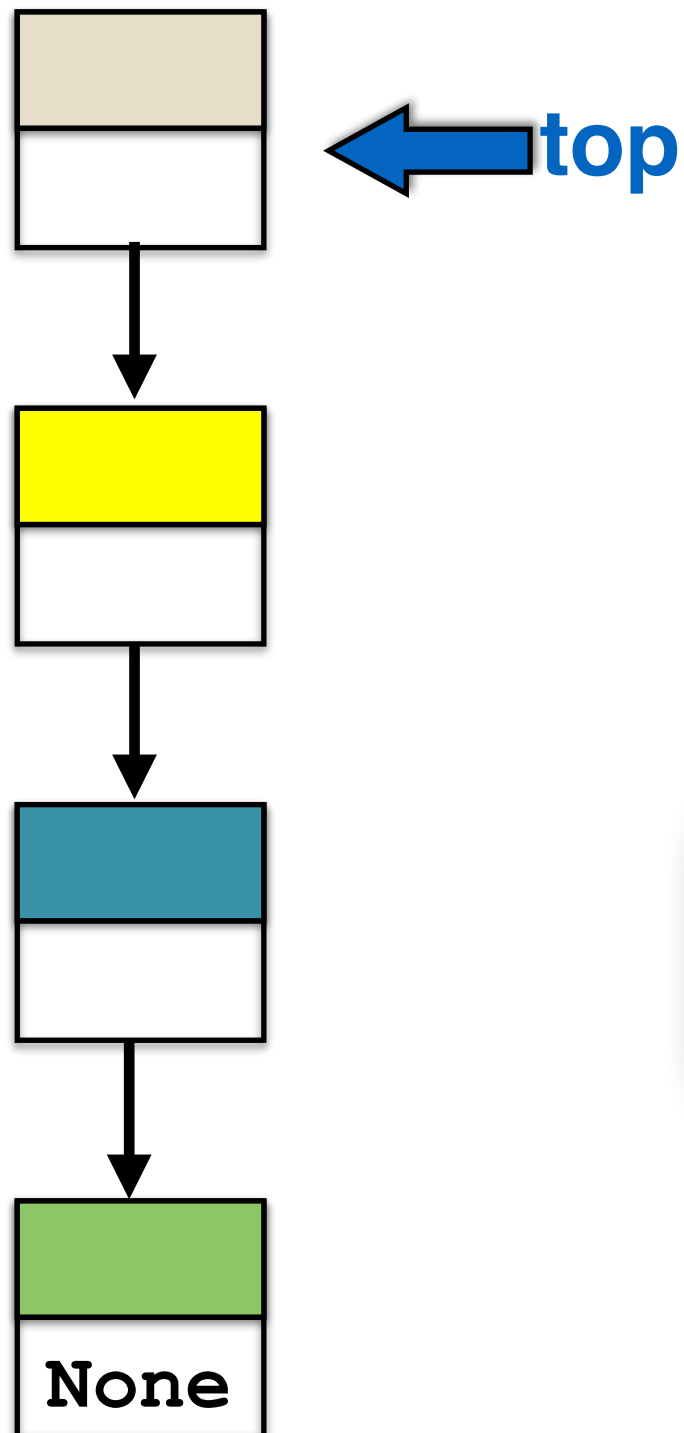


Create a new node with the new item.
linked to the current top



Make the new node the new **top**

Create a new node with the new item.
linked to the current top



Make the new node the new **top**

```
def push(self, item):  
    self.top = Node(item, self.top)
```

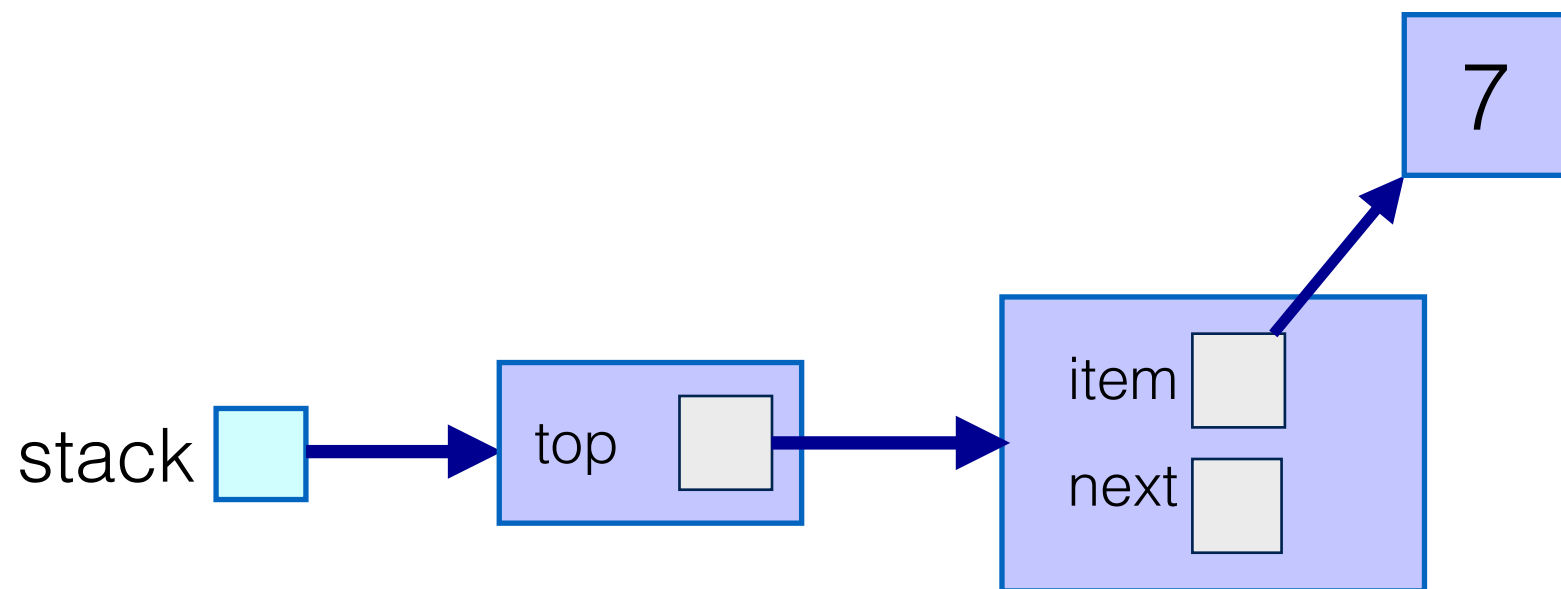
Consider a stack
with **7** on top

stack.push(41)

```
def push(self, item):  
    self.top = Node(item, self.top)
```

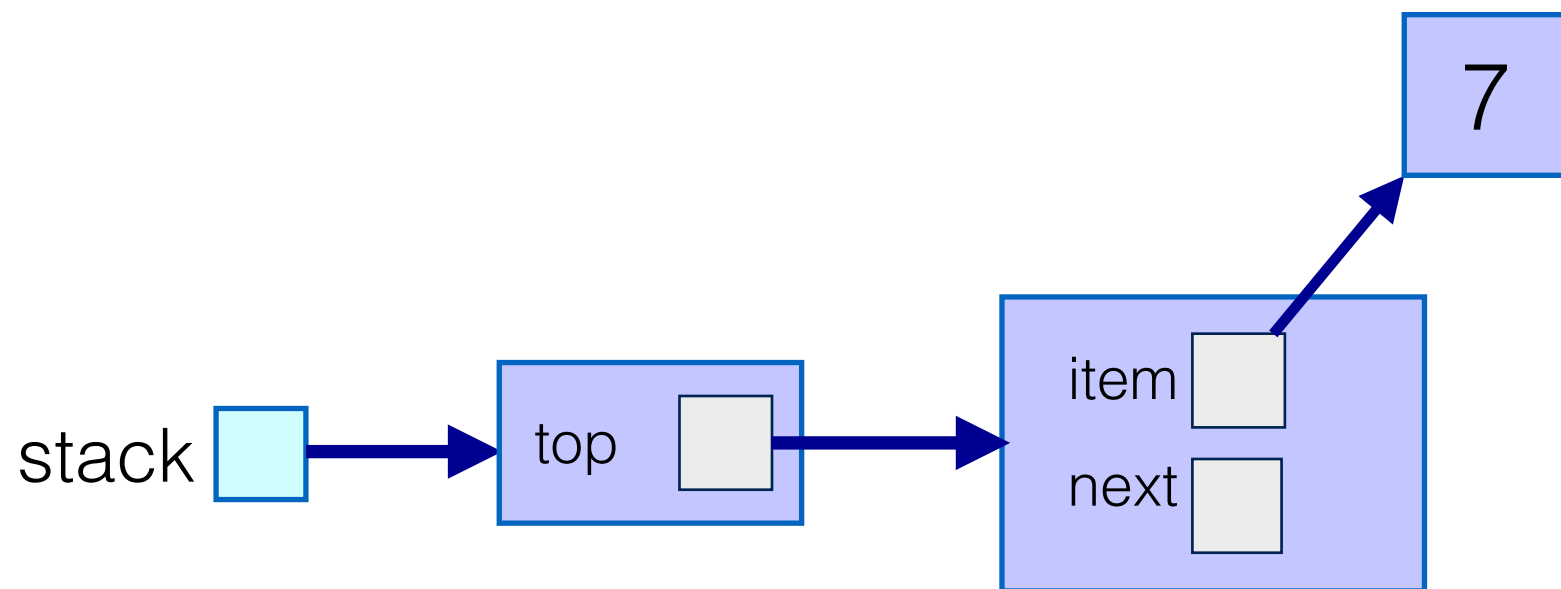

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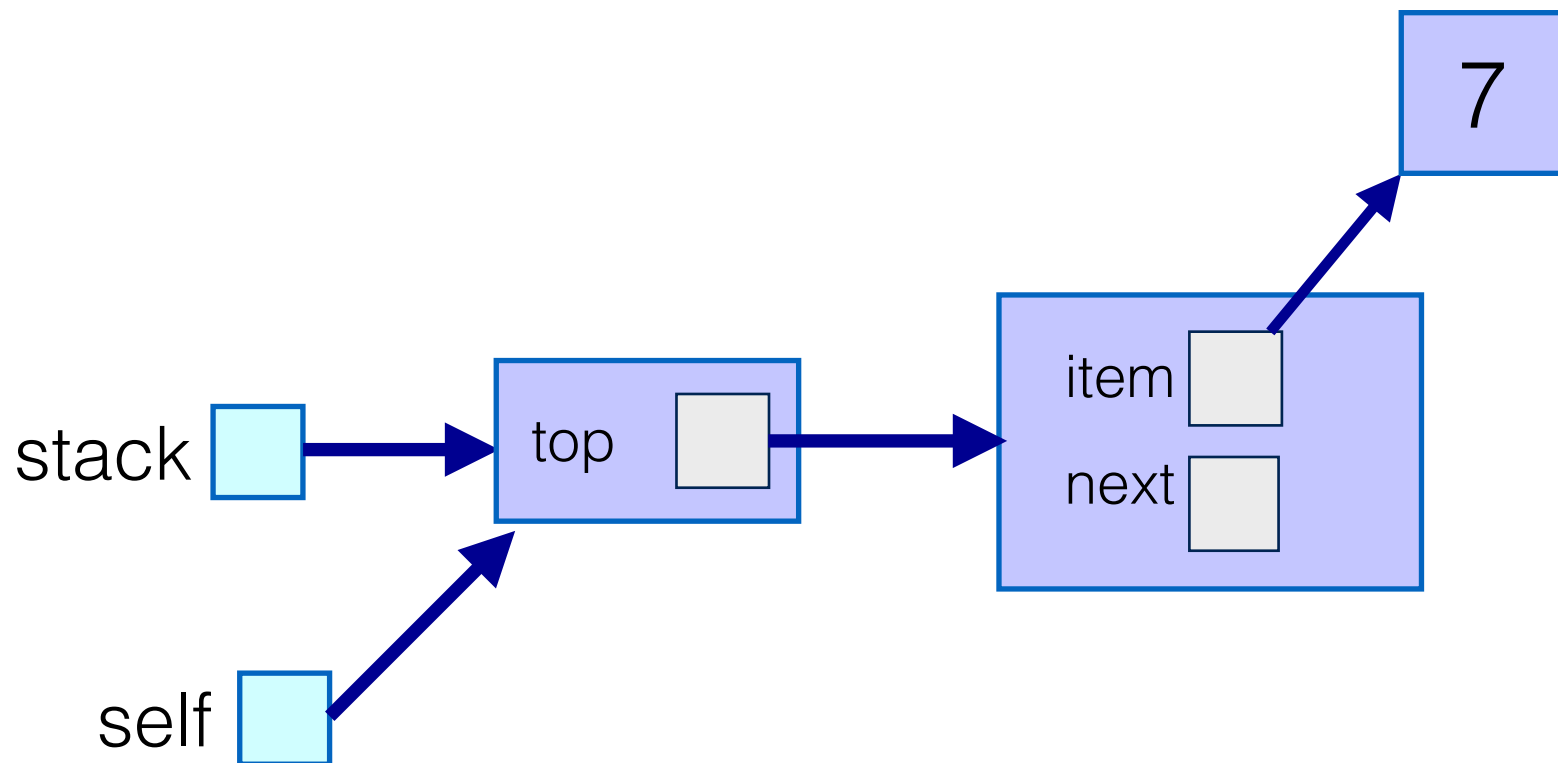
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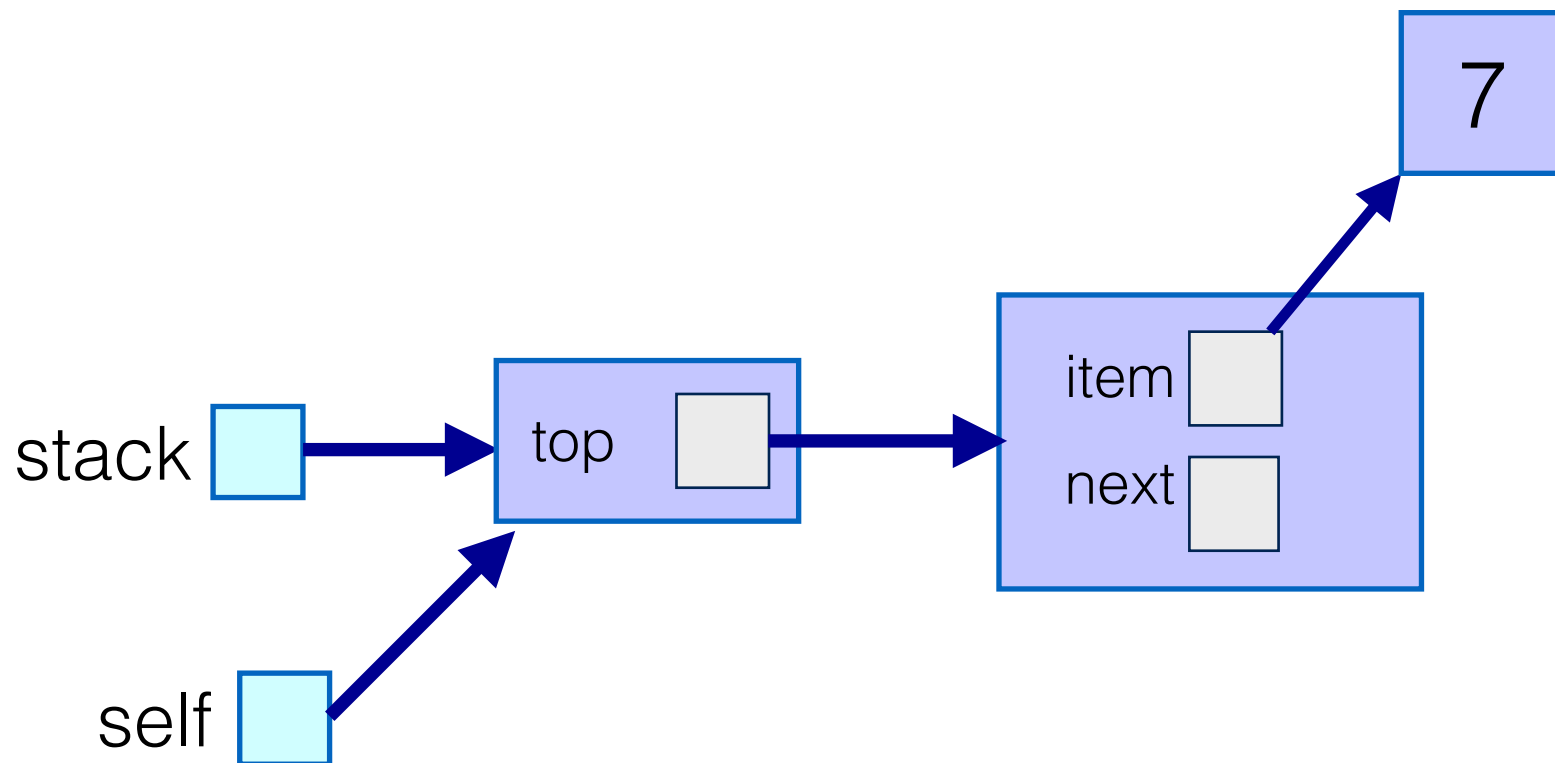
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stack.push(41)

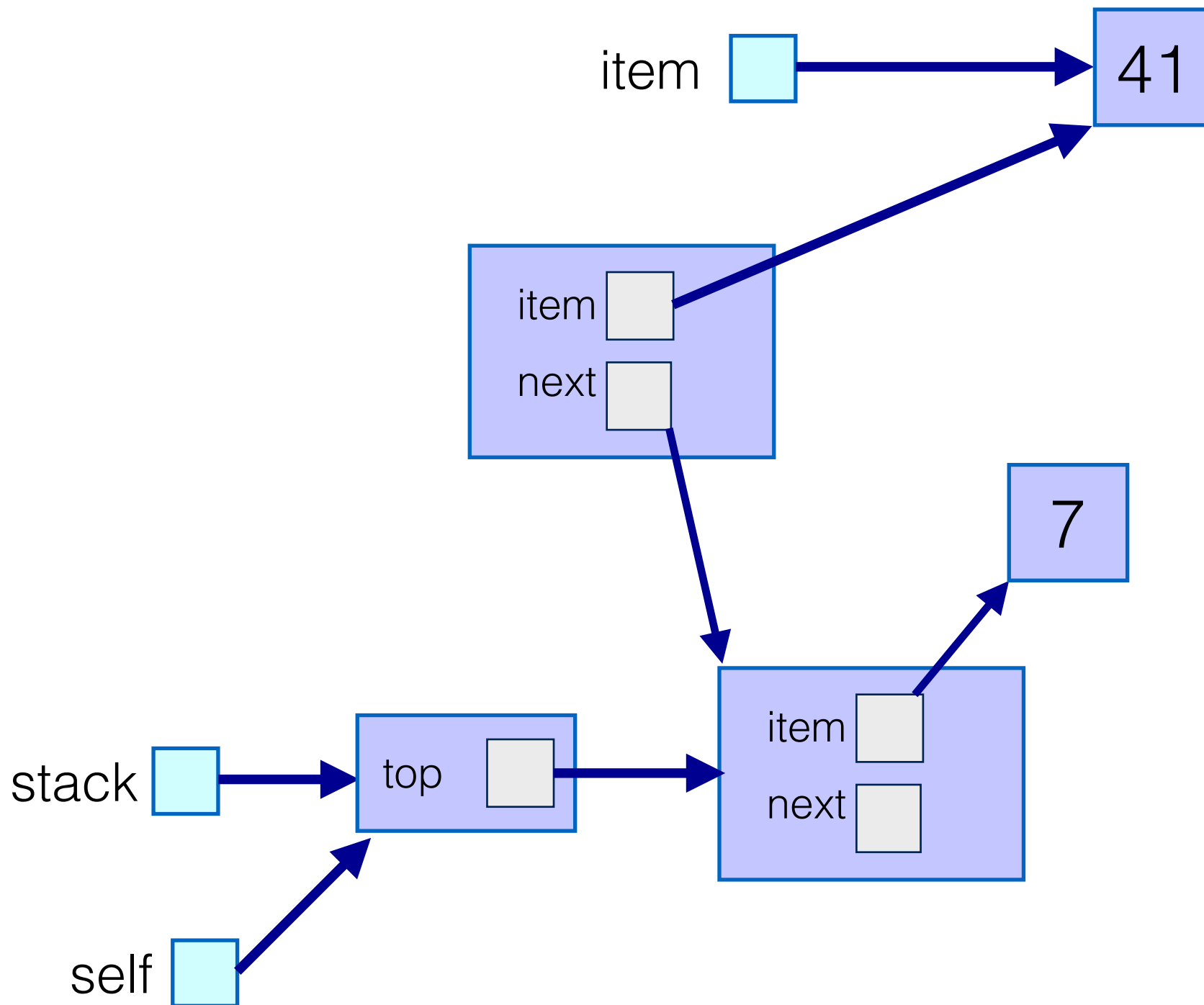
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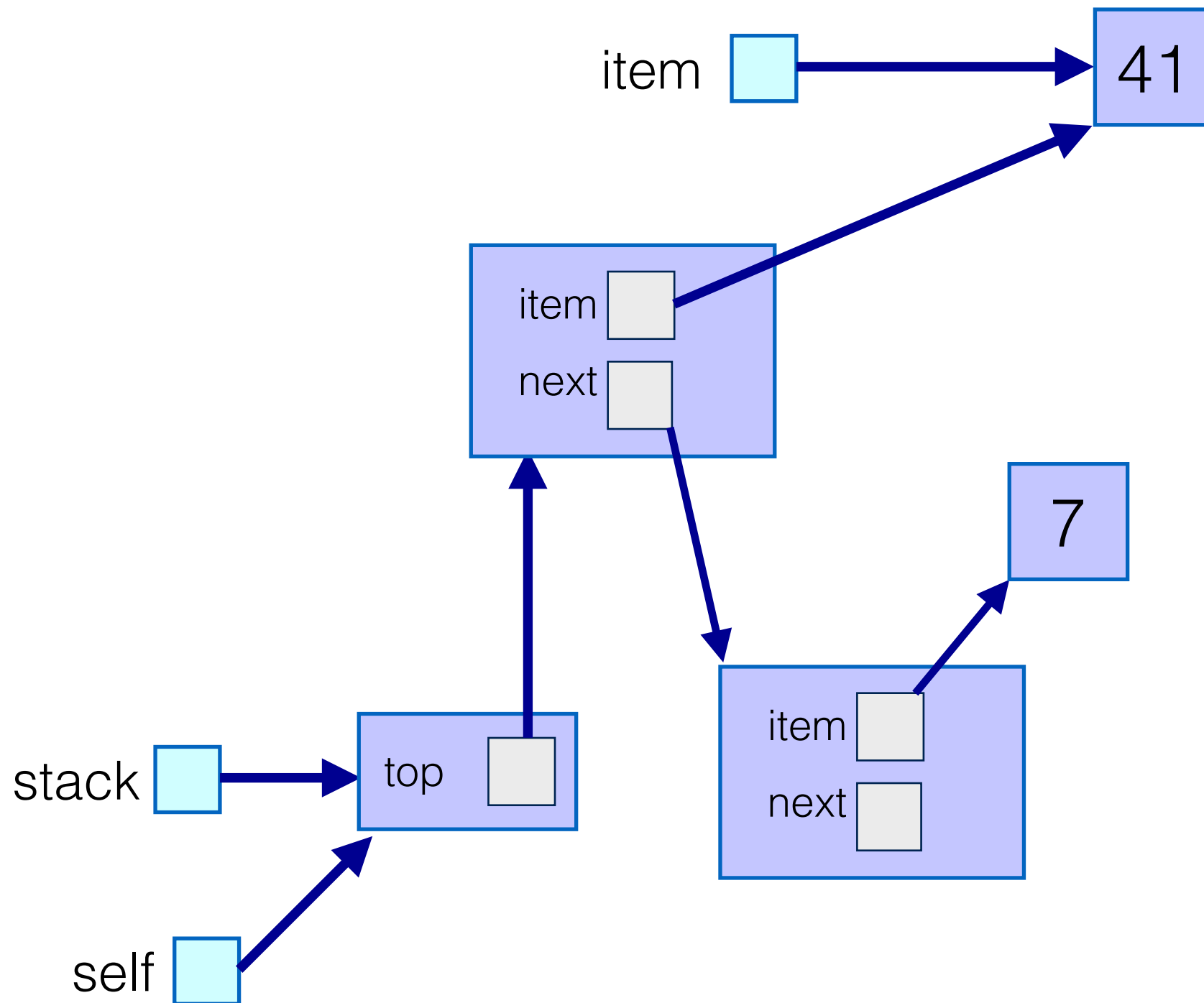
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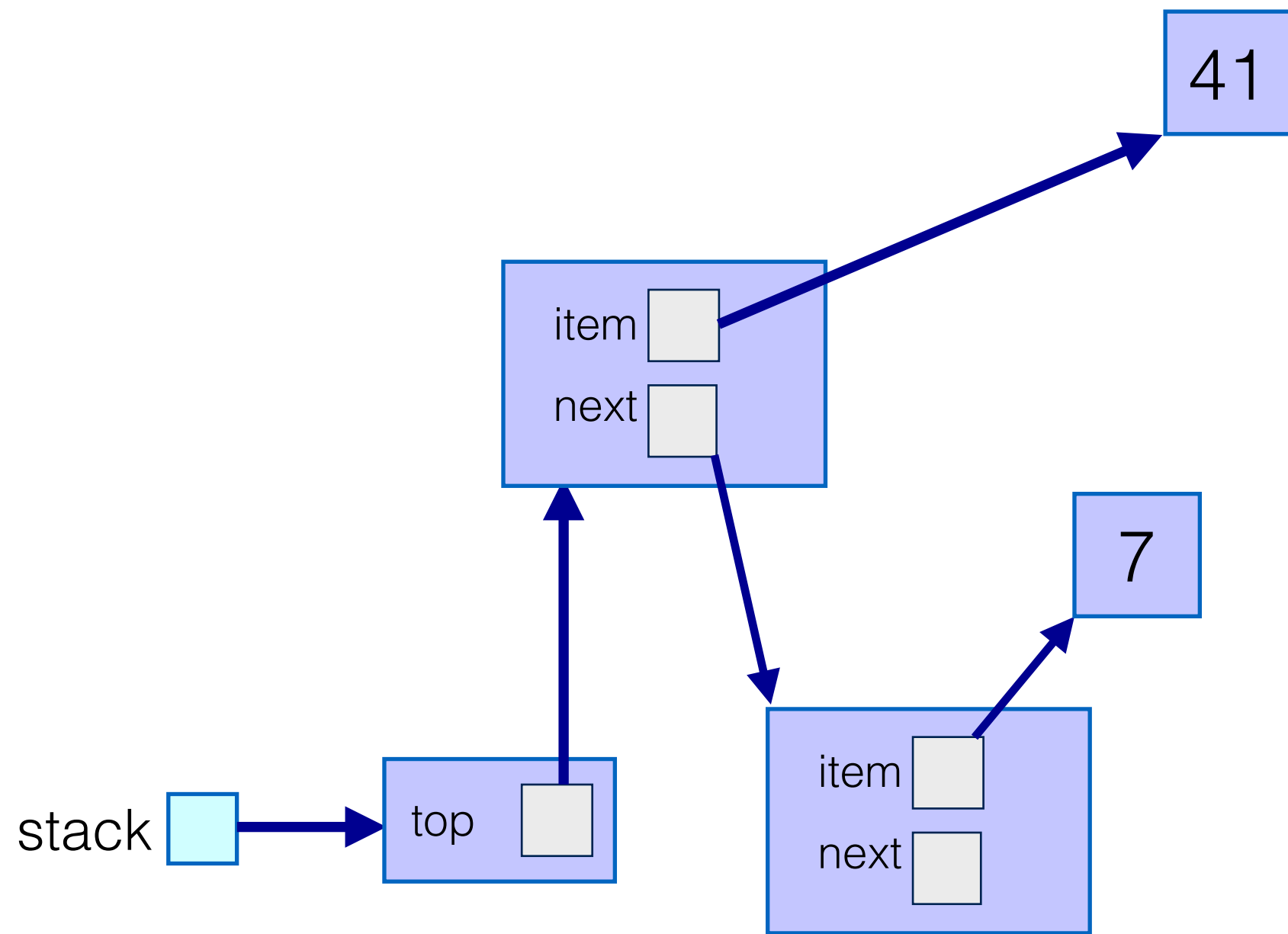


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with **7** on top

stack.push(41)

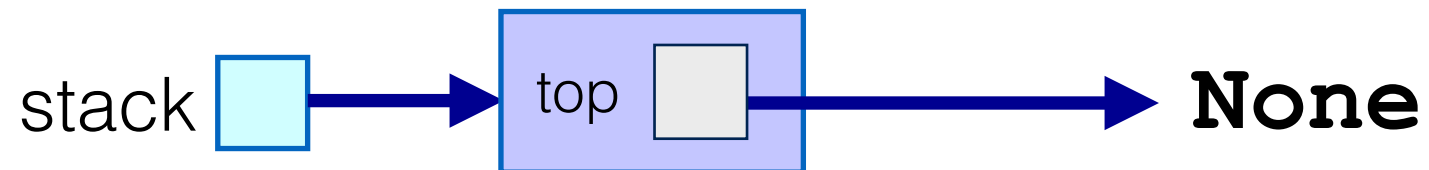
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def push(self, item):  
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```
class Stack:  
    def __init__(self):  
        self.top = None  
  
    def push(self, item):  
        self.top = Node(item, self.top)
```

stack = Stack()

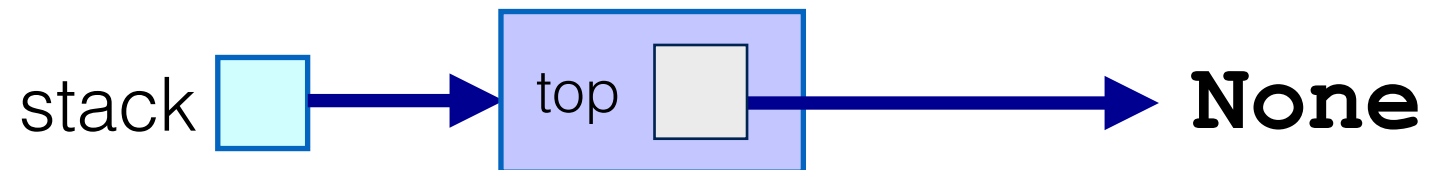



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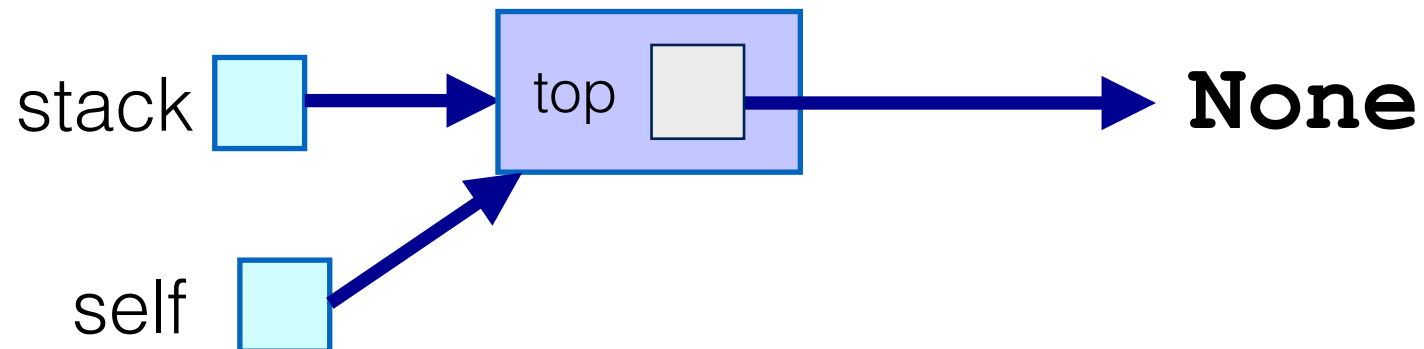
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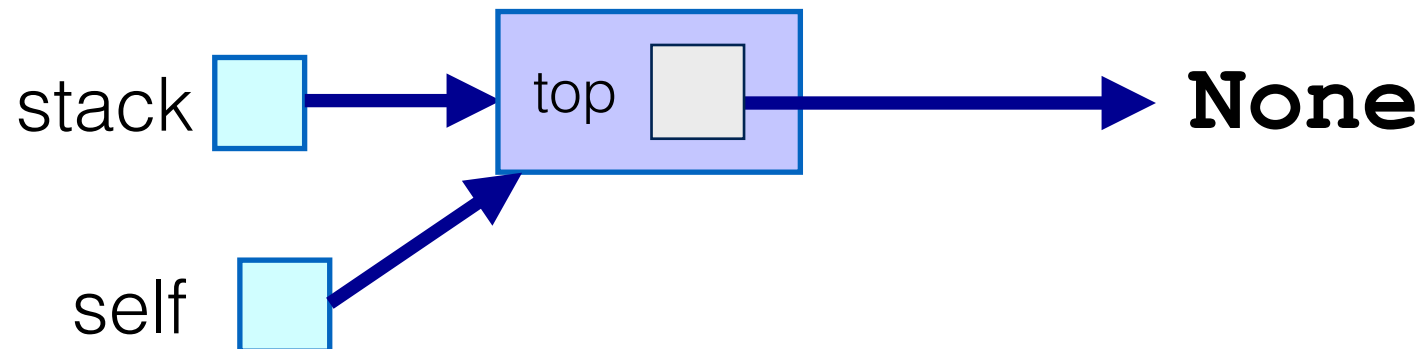
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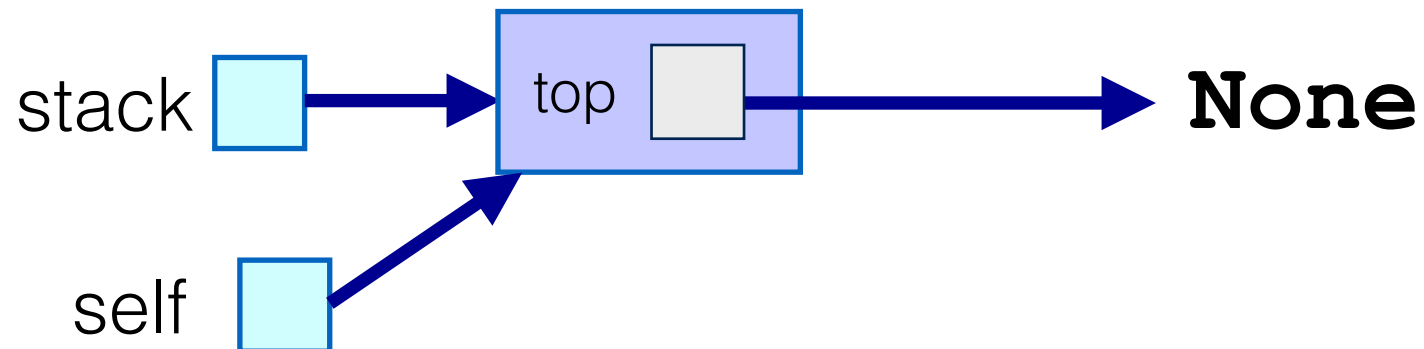
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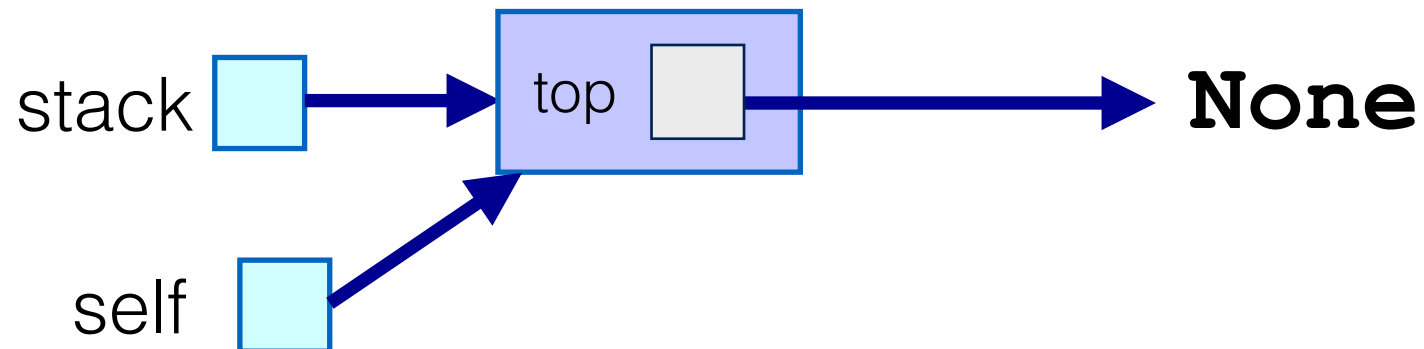
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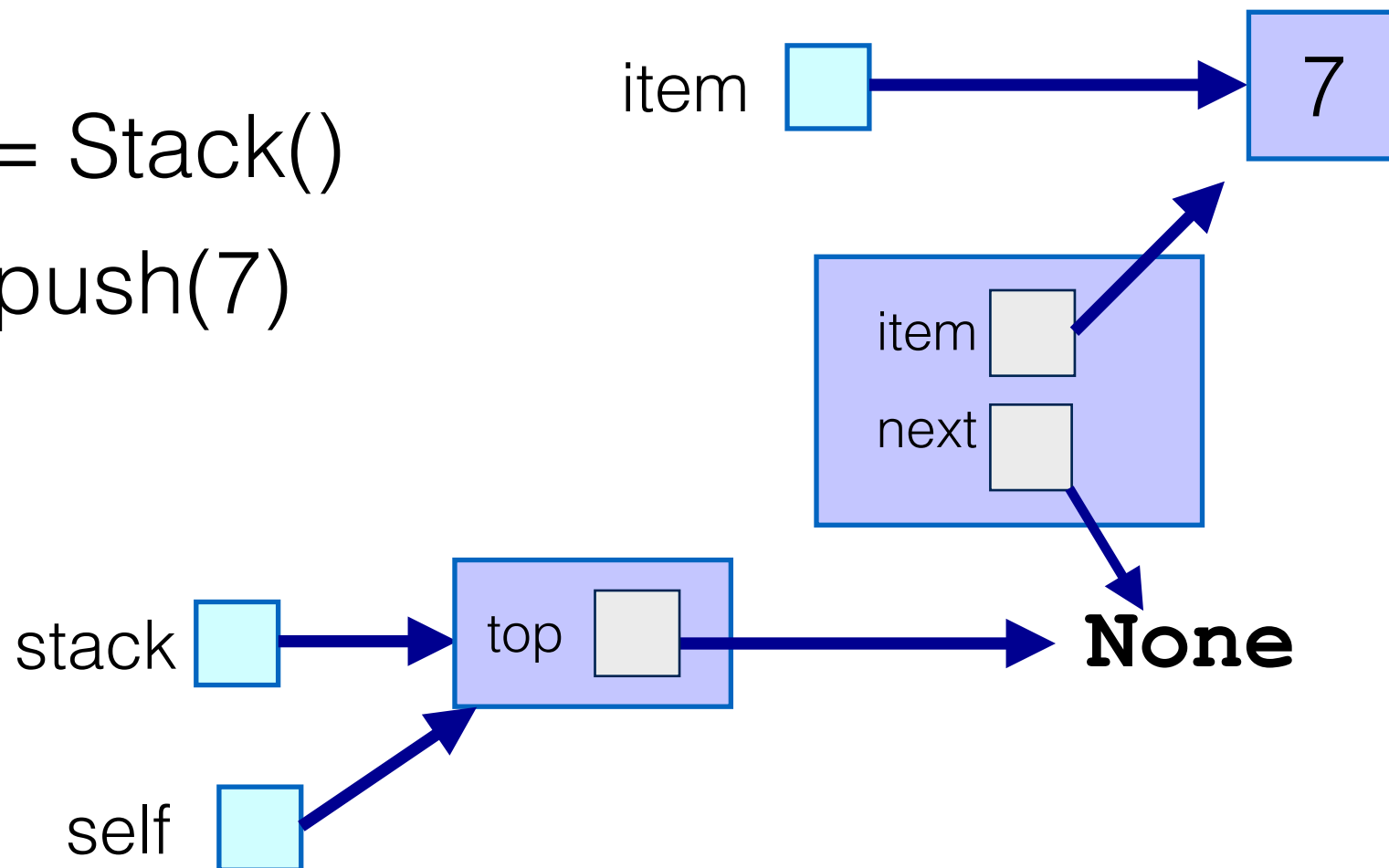
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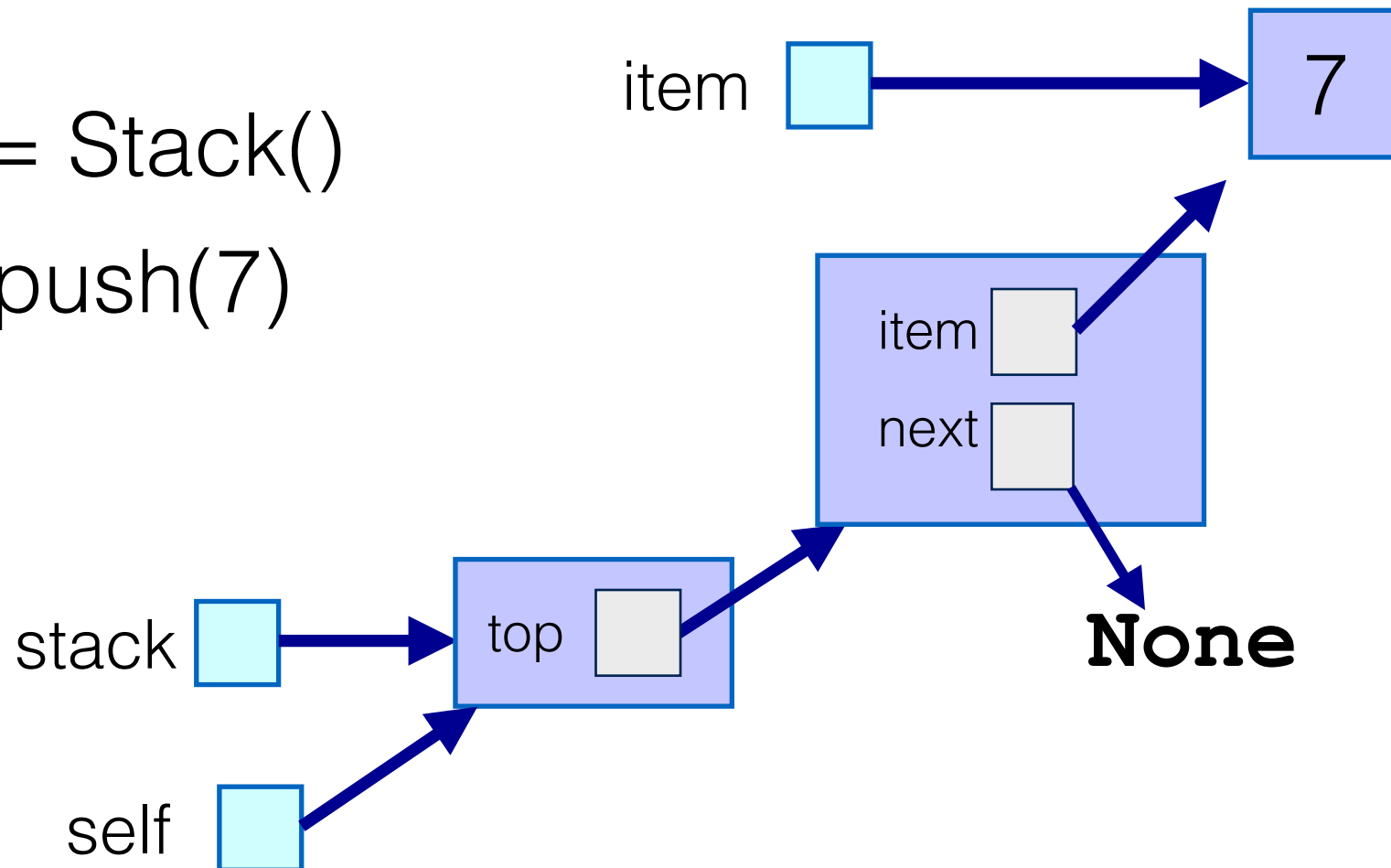
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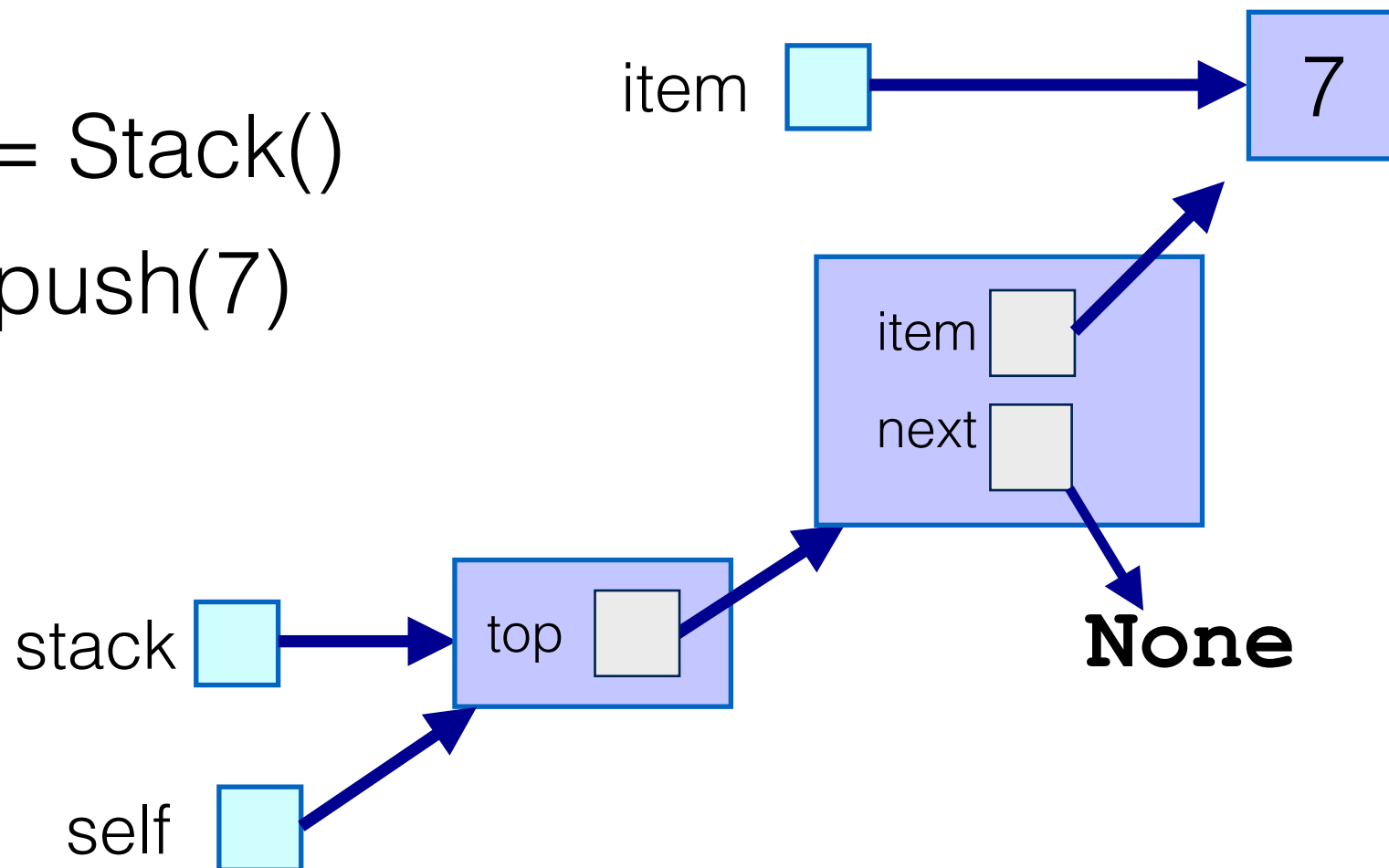
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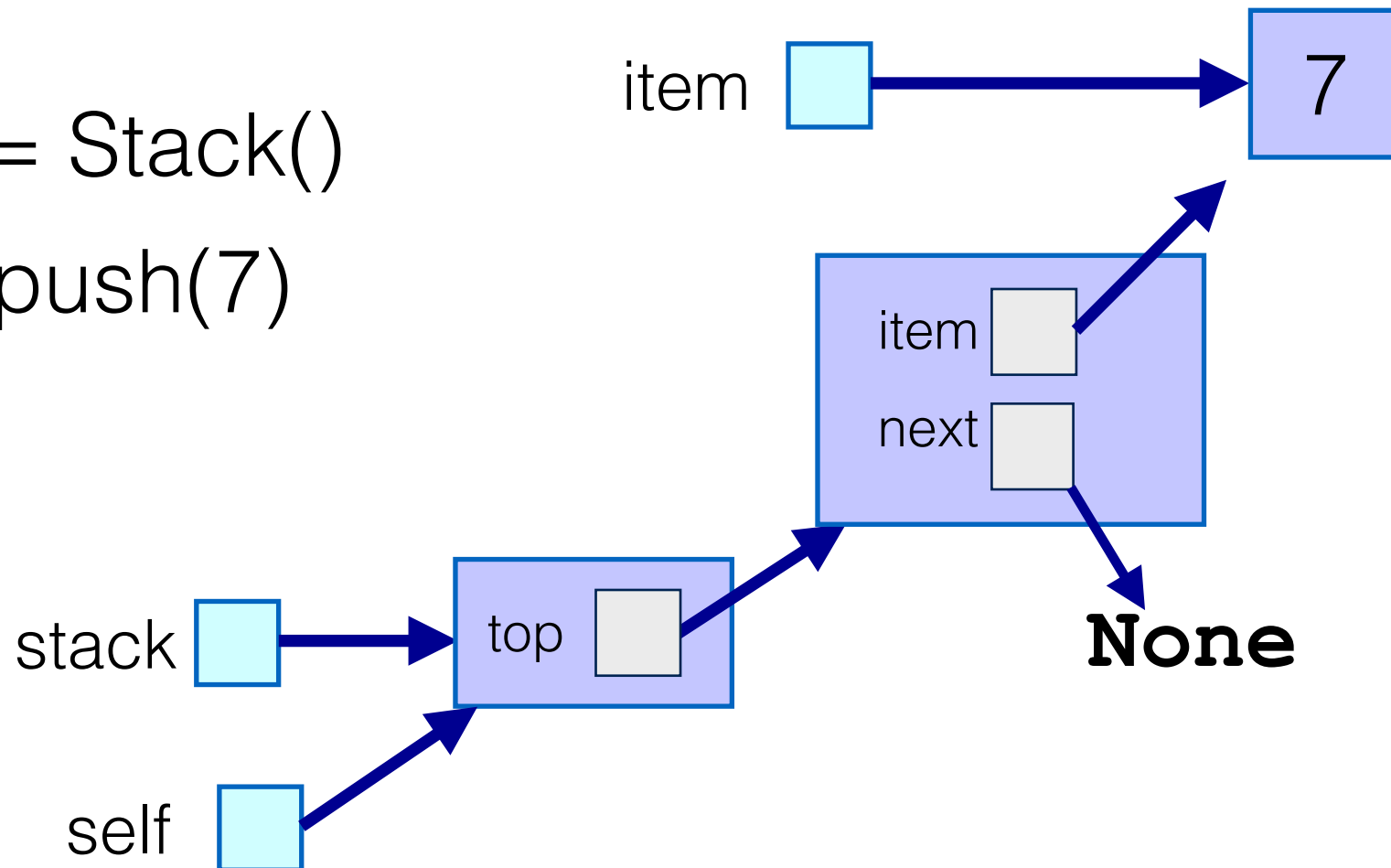
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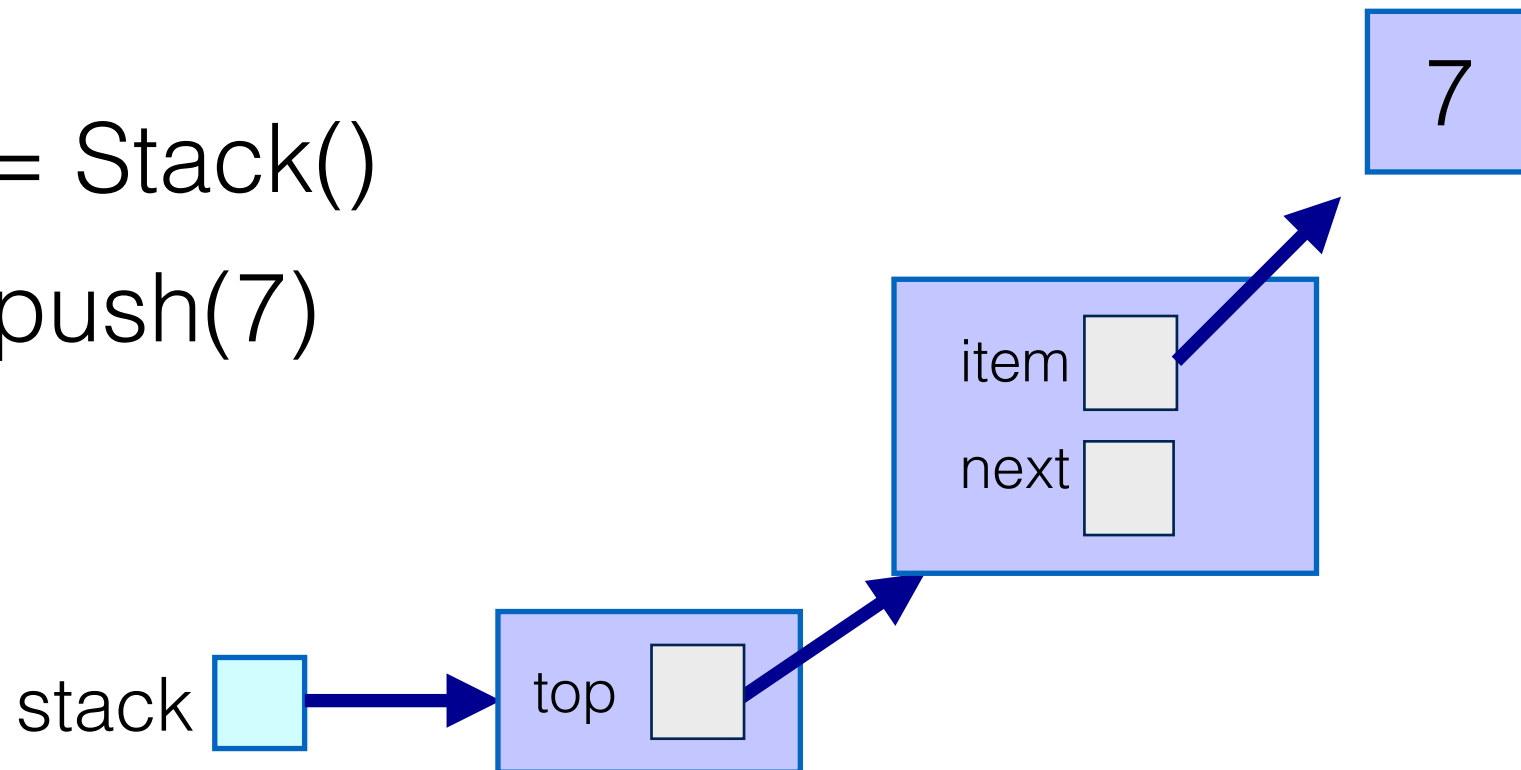


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stack.push(7)

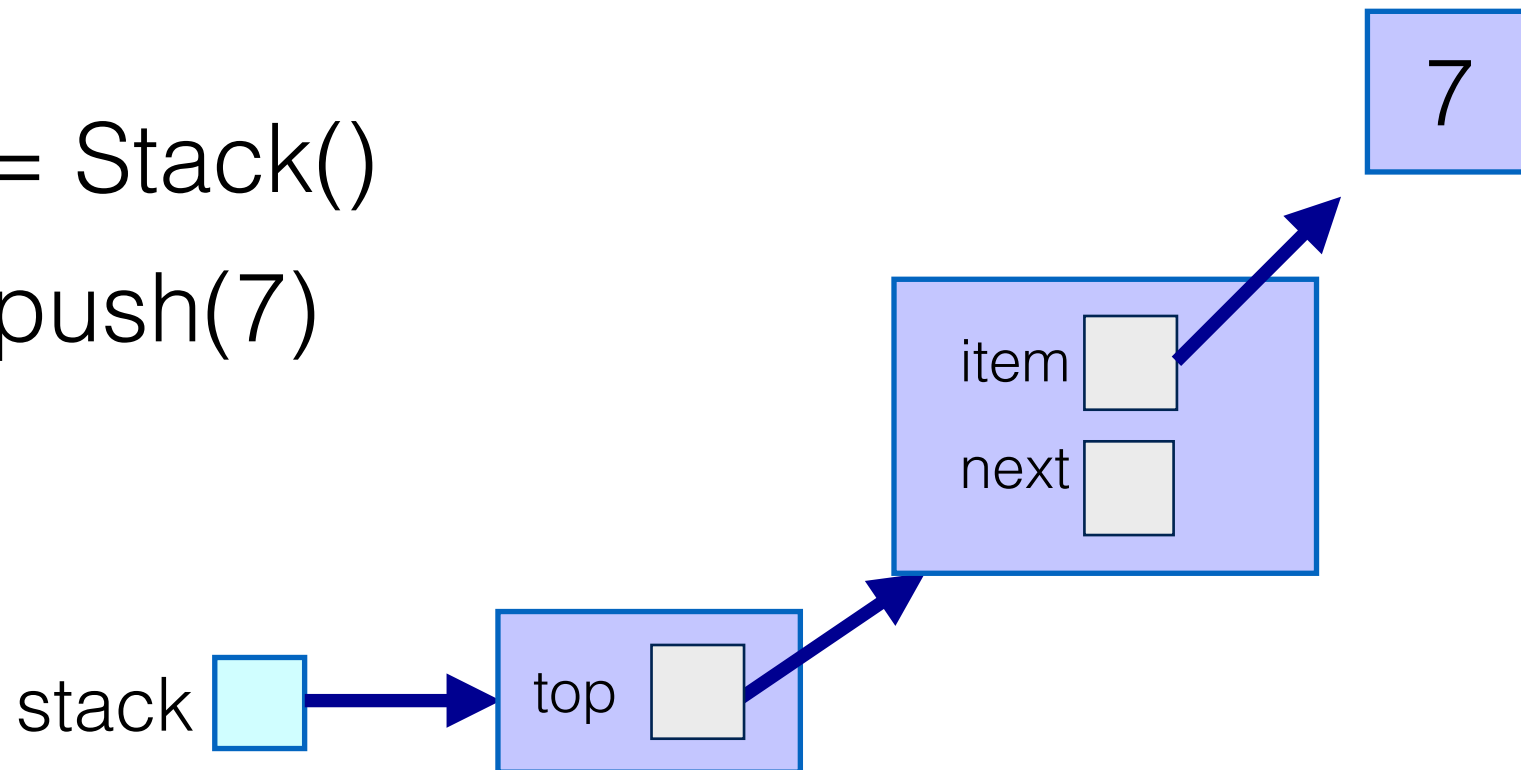


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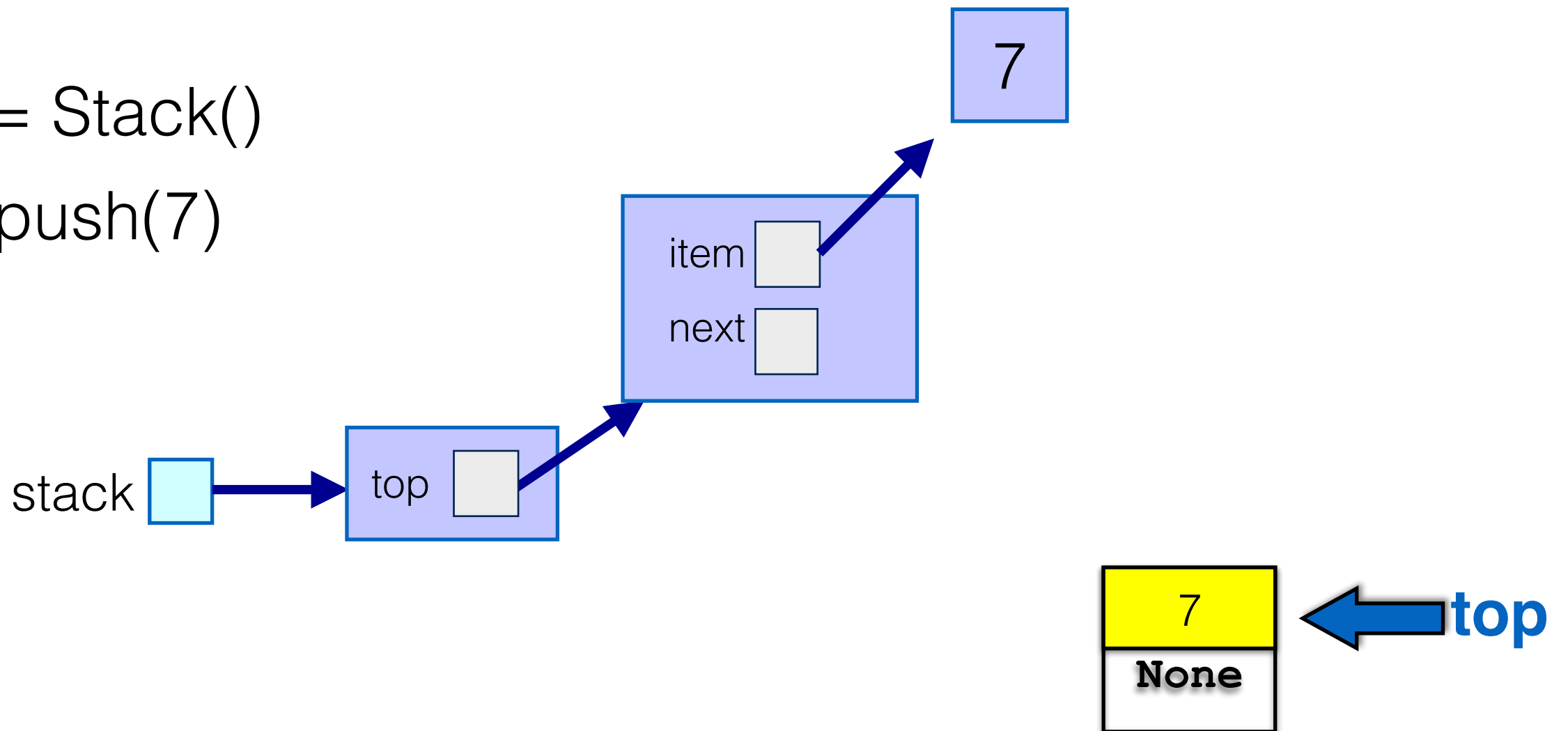
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```

stack = Stack()
stack.push(7)



Pop: algorithm

Array implementation:

Pop: algorithm

Array implementation:

- If the array is empty raise exception
- Else
 - Remember the top item
 - Decrease top
 - Return the item

Pop: algorithm

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Linked implementation:

Pop: algorithm

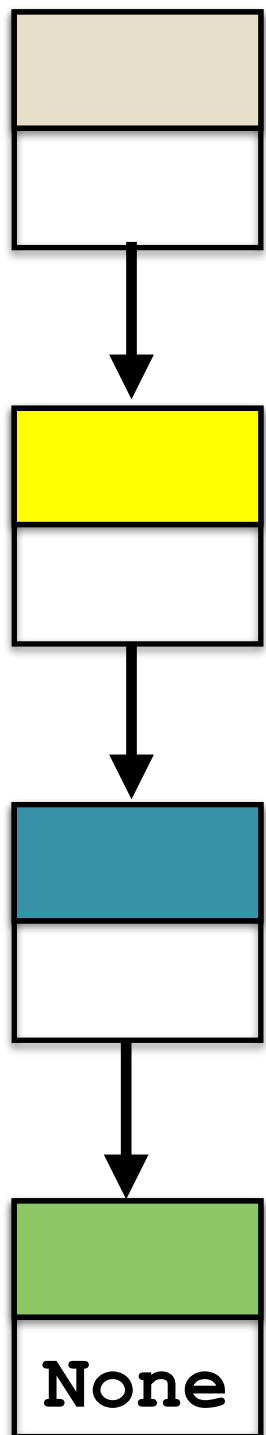
Array implementation:

- If the array is empty raise exception
- Else
 - Remember the top item
 - Decrease top
 - Return the item

Linked implementation:

- If the stack is empty raise exception
- Else
 - Remember the top item
 - **Change top to point to the next node**
 - Return the item

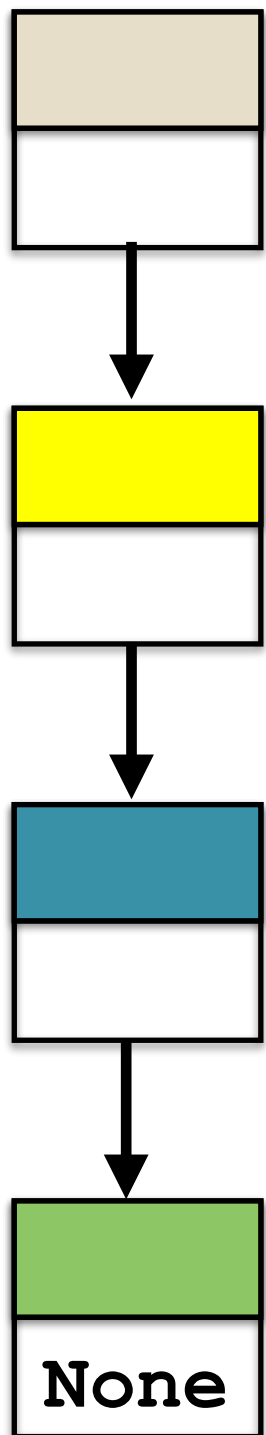
Pop: algorithm



← **top**

Check if the stack is empty

Pop: algorithm



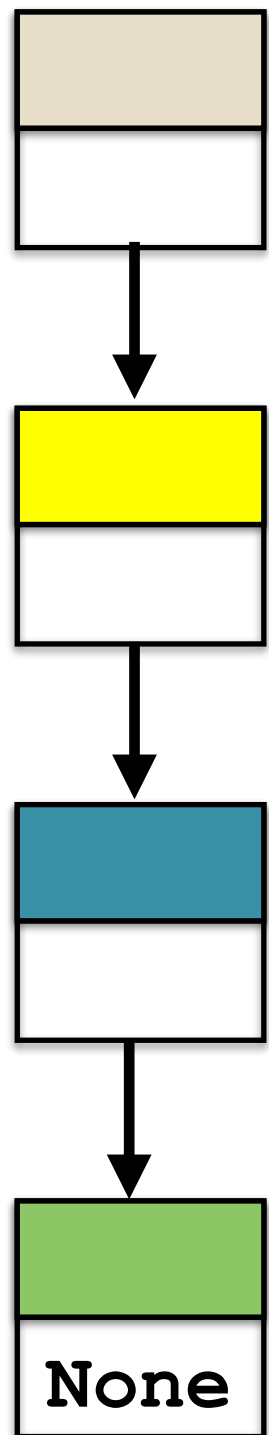
← **top**

Check if the stack is empty

Remember the item in the top node



Pop: algorithm



Check if the stack is empty

Remember the item in the top node



Make the next node the new top

Pop: algorithm

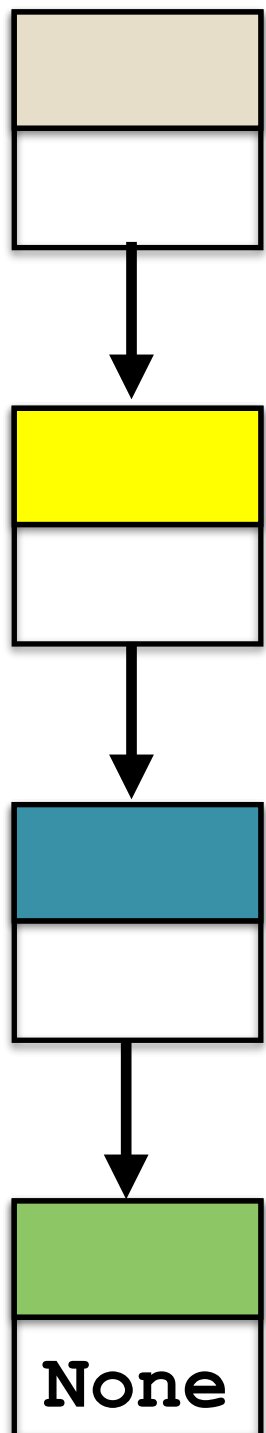
This node will be collected by the garbage collector

Check if the stack is empty

Remember the item in the top node

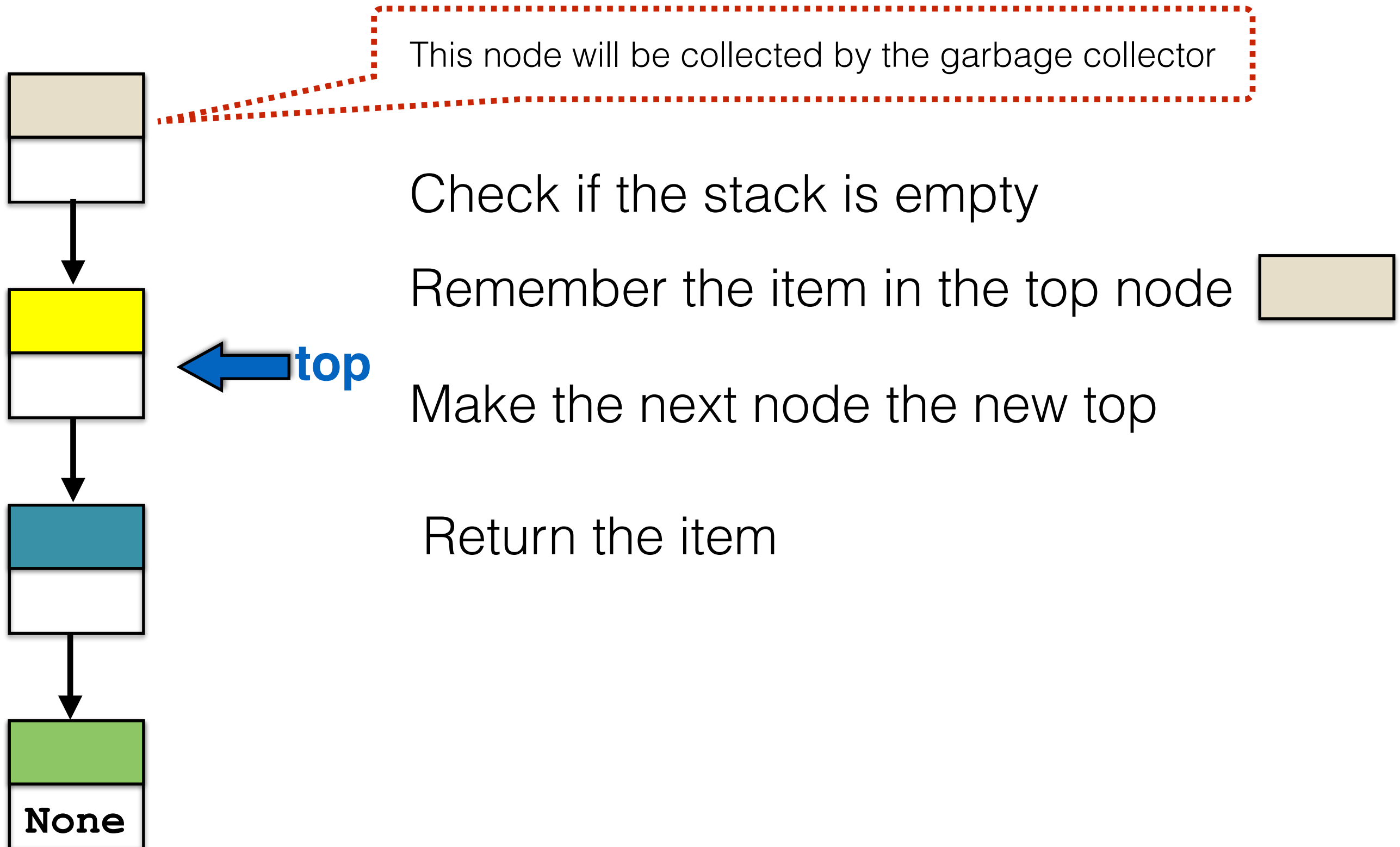


Make the next node the new top



← **top**

Pop: algorithm



```
def pop(self):
```

```
def pop(self):  
    assert not self.is_empty(), "Stack is empty"
```

```
def pop(self):  
    assert not self.is_empty(), "Stack is empty"  
    item = self.top.item
```



```
def pop(self):  
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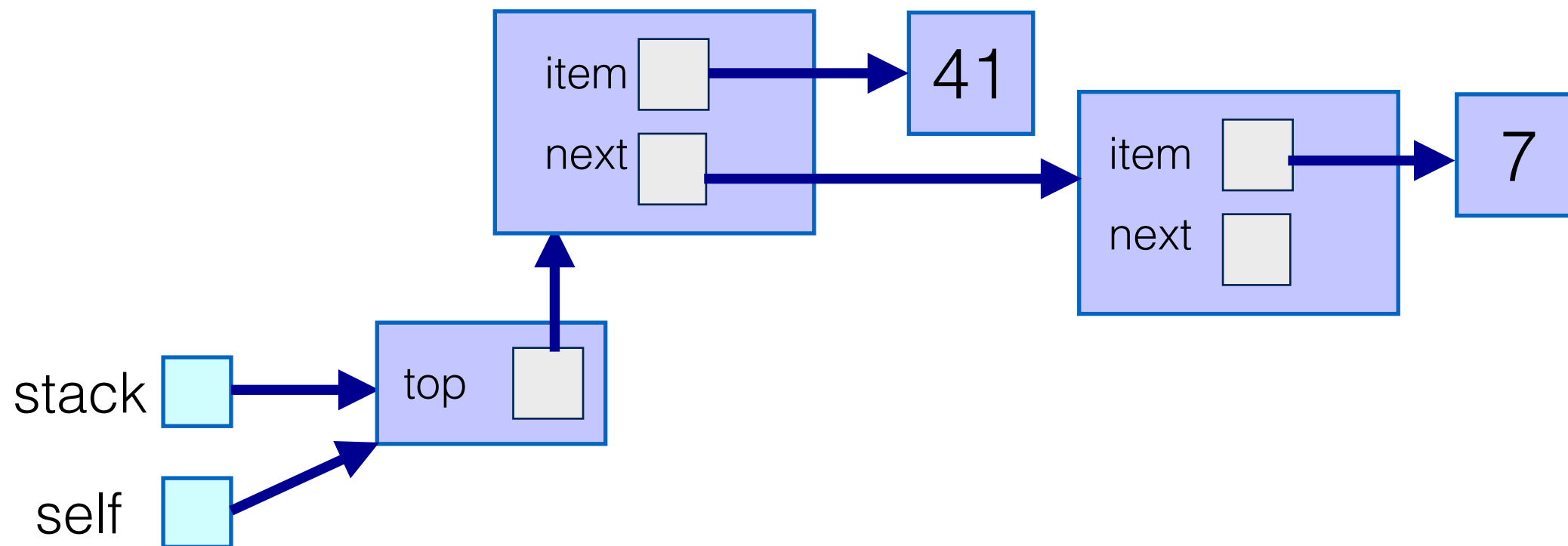


Note: it is **self.top.item** not **self.top**

```
def pop(self):  
    assert not self.is_empty(), "Stack is empty"  
    item = self.top.item  
    self.top = self.top.next
```

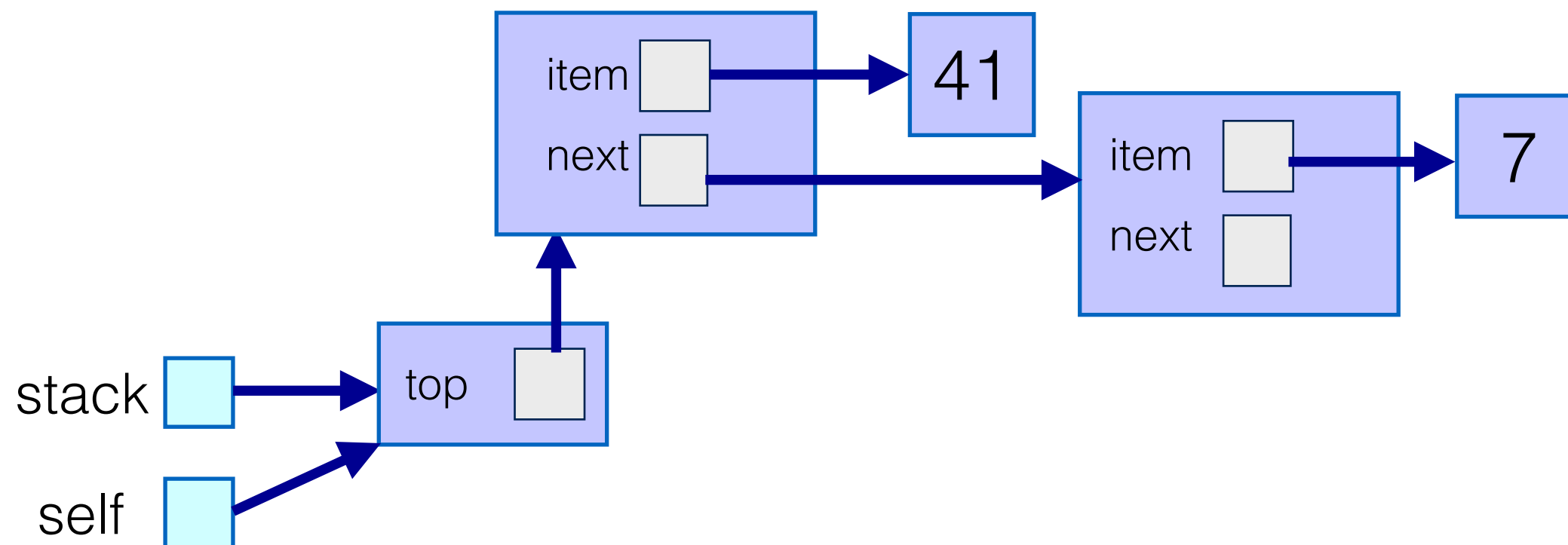
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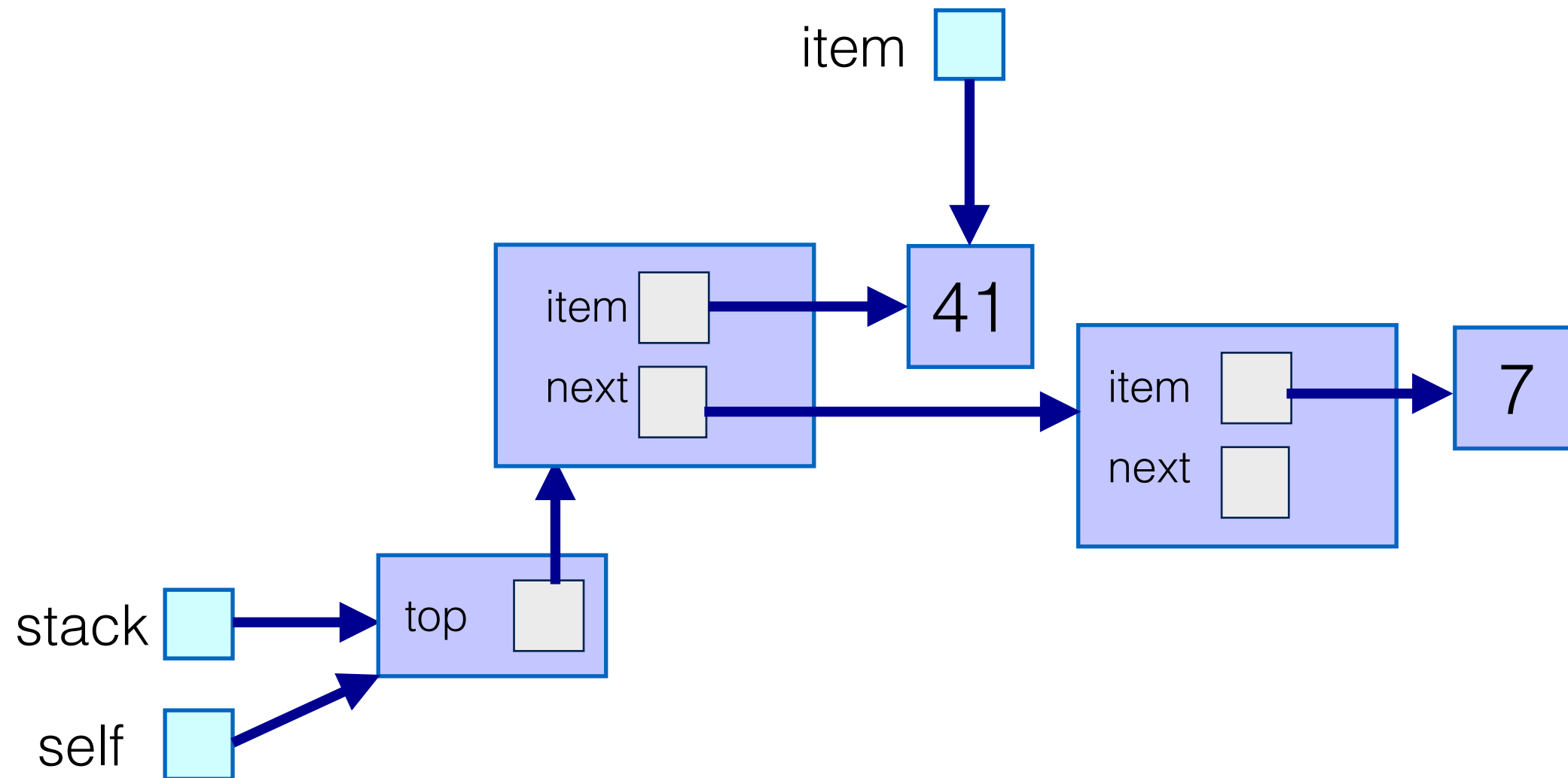
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stack.pop()



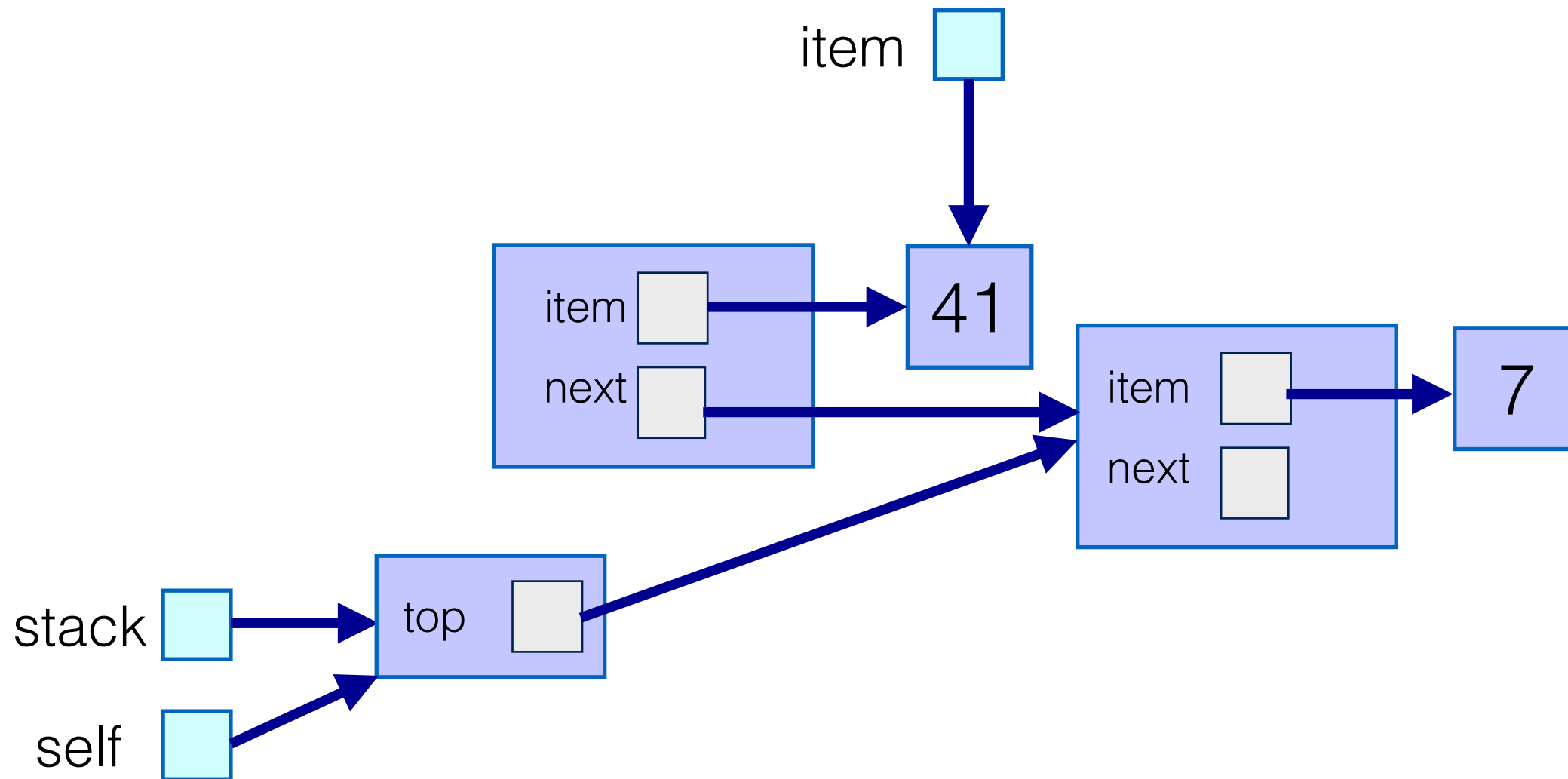
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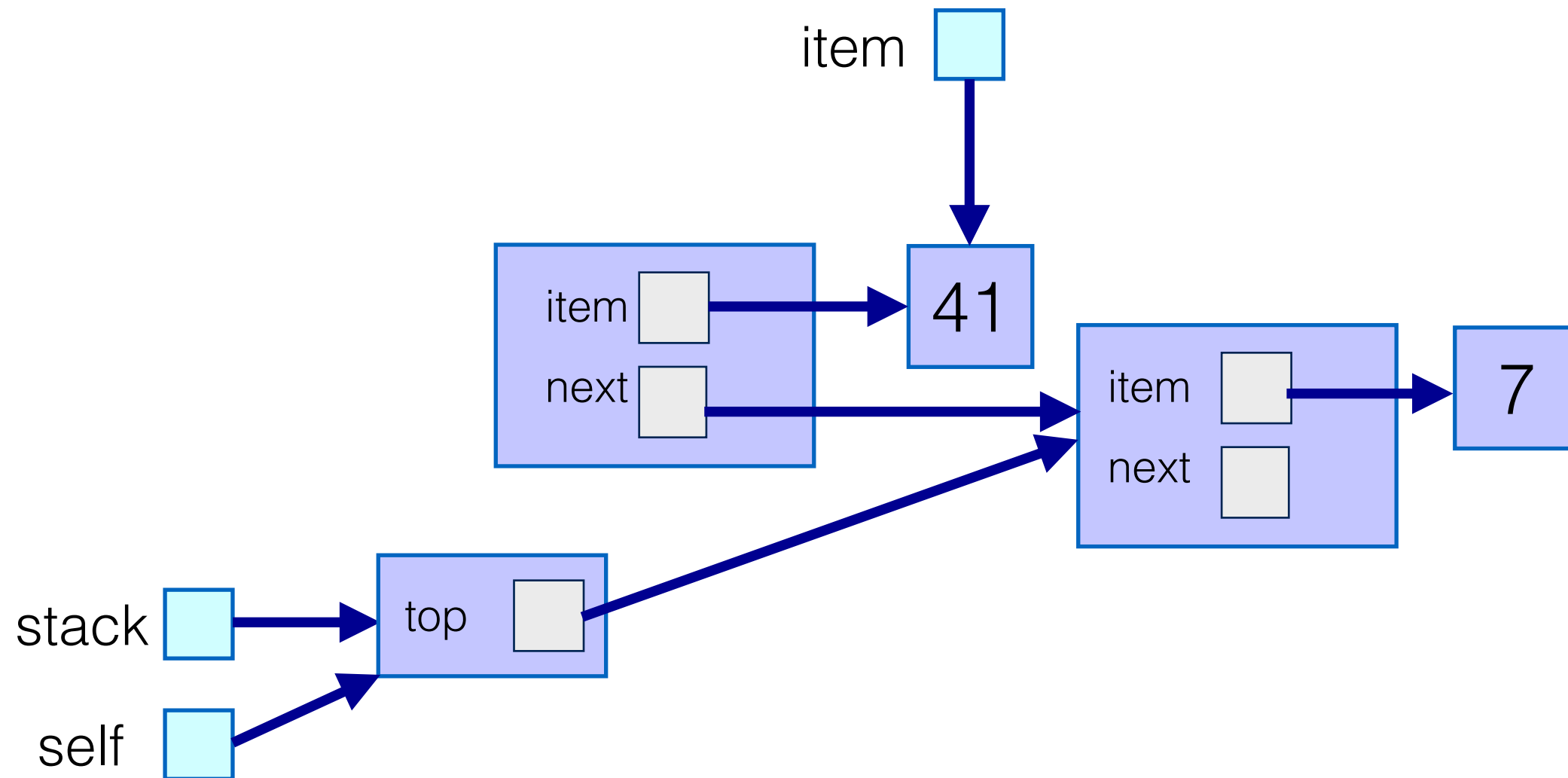
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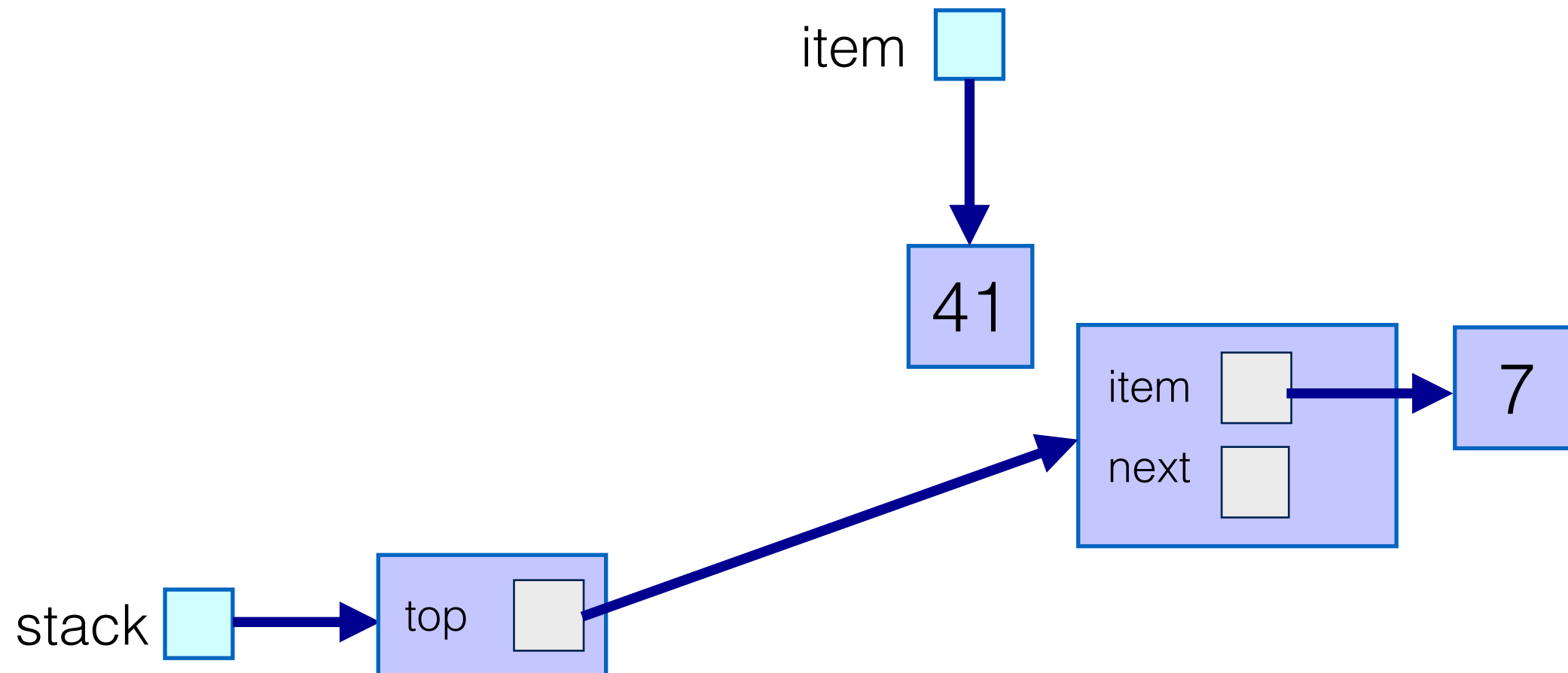
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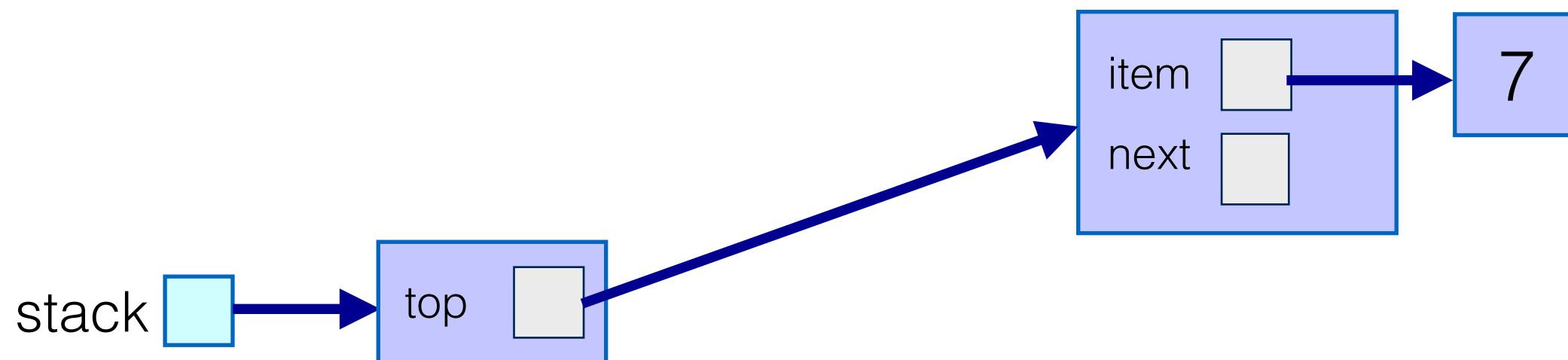

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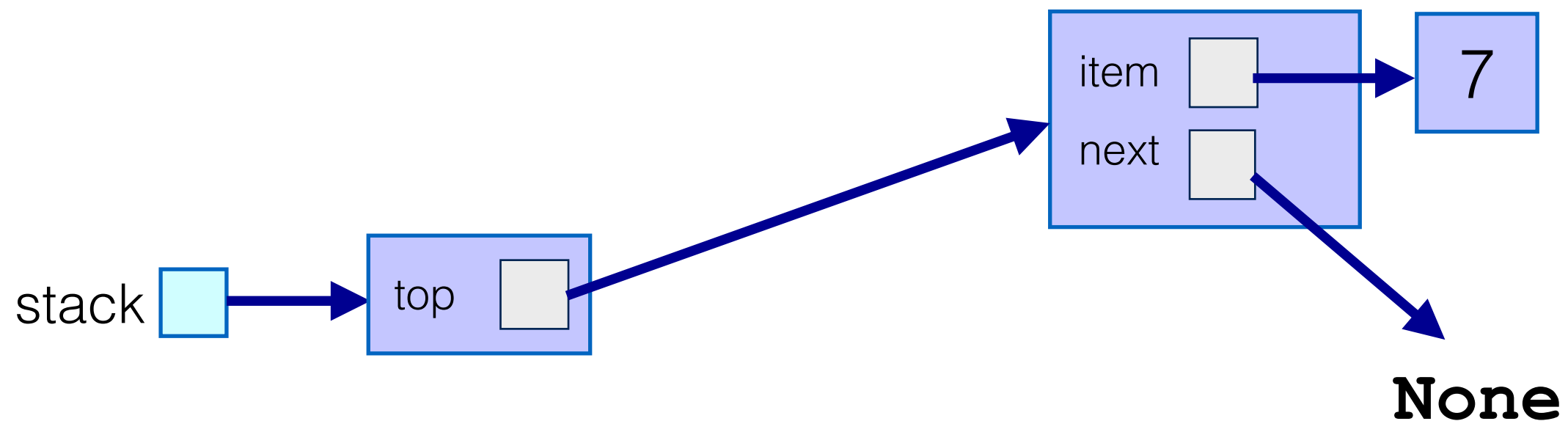
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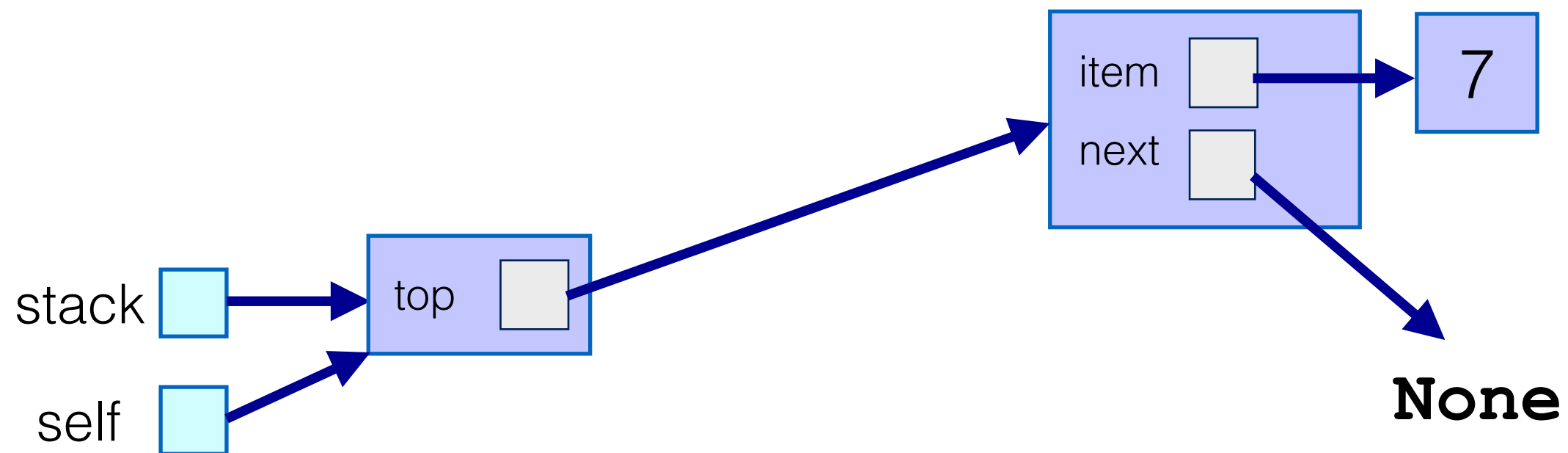
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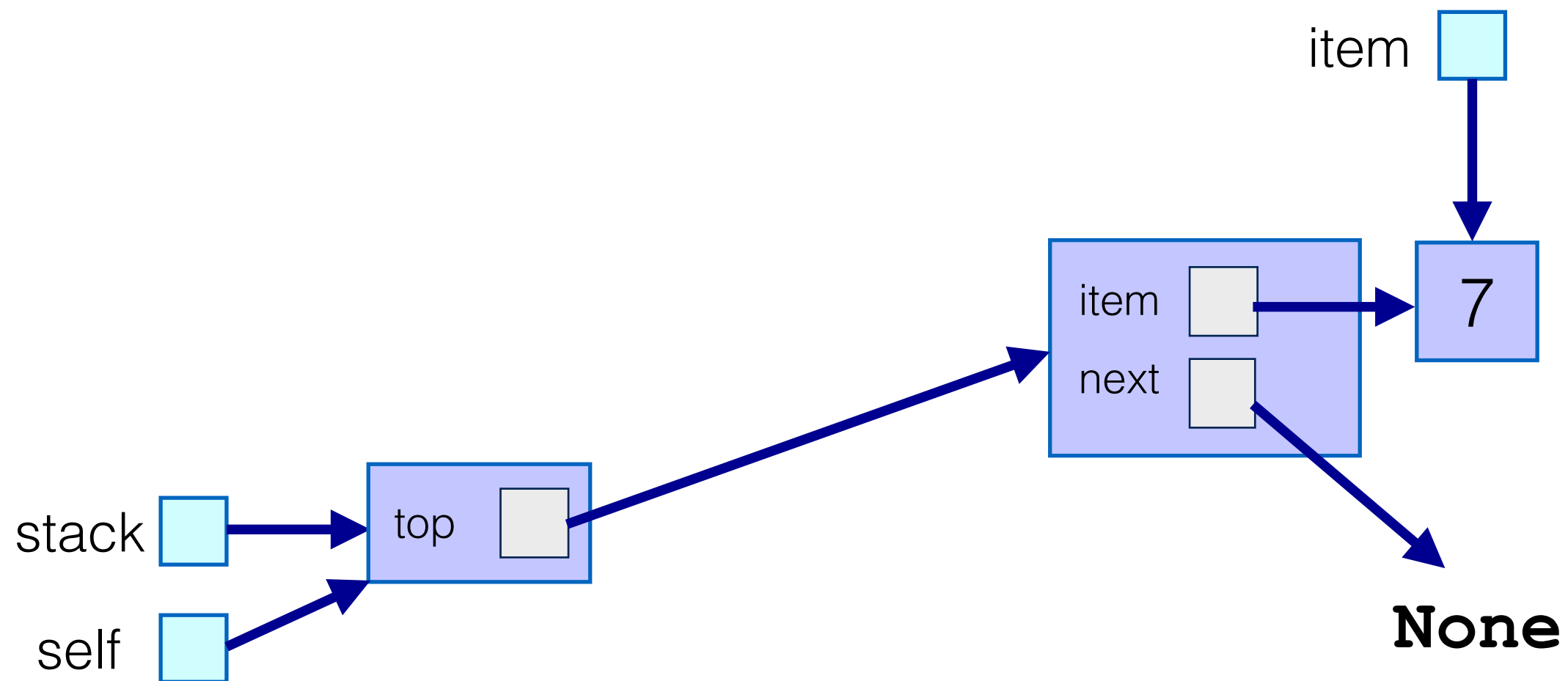
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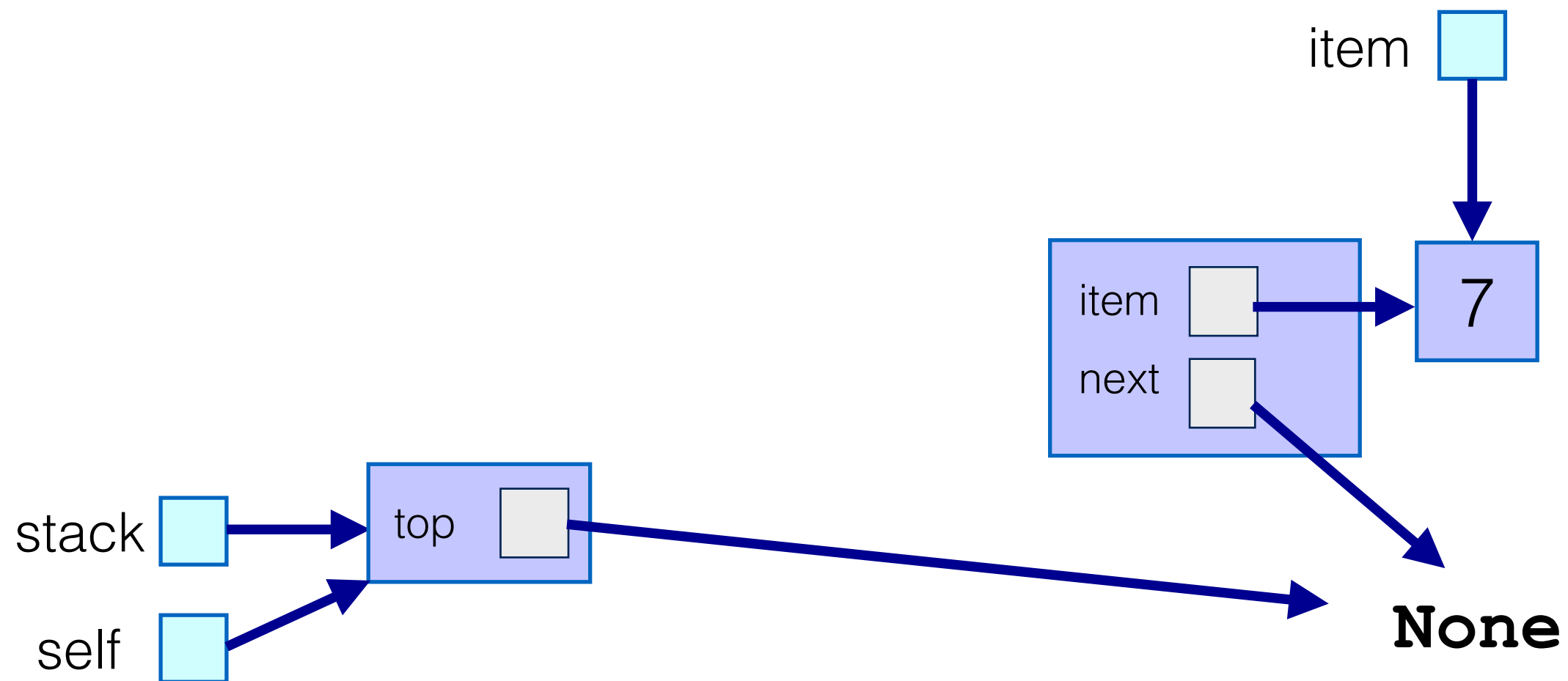
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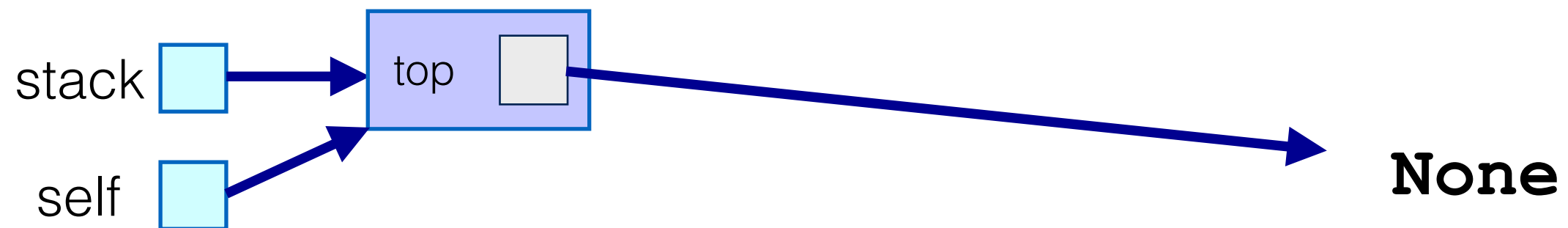
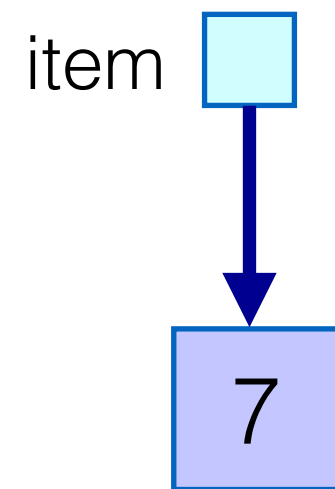
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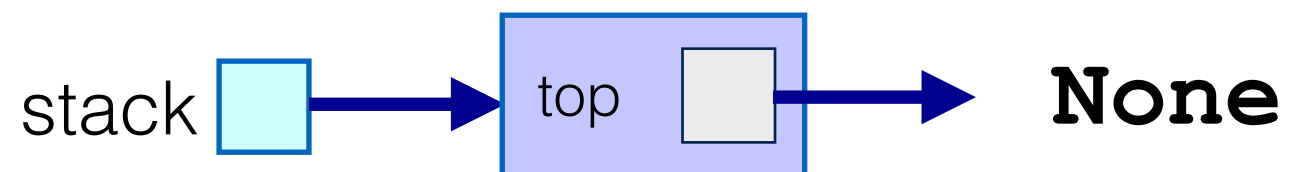
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    return item
```

stack.pop()




```
def reverse(a_string):  
    the_stack = Stack()  
    for item in a_string:  
        the_stack.push(item)  
  
    output = ""  
    while not the_stack.is_empty():  
        item = the_stack.pop()  
        output += str(item)  
    return output  
  
if __name__ == "__main__":  
    input_string = input("Enter a string: ")  
    print(reverse(input_string))
```

Summary

- Advantages and disadvantages of linked data structures
- Stacks implemented with linked data structures