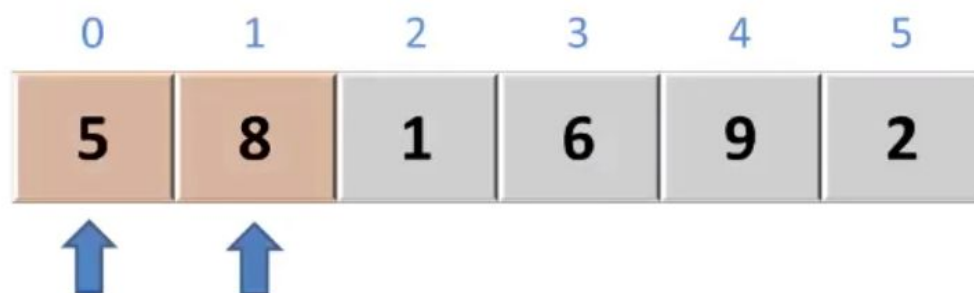


## Bubble Sort

Given an array of items, sort them in increasing order

Large items bubbles at right

## Bubble Sort

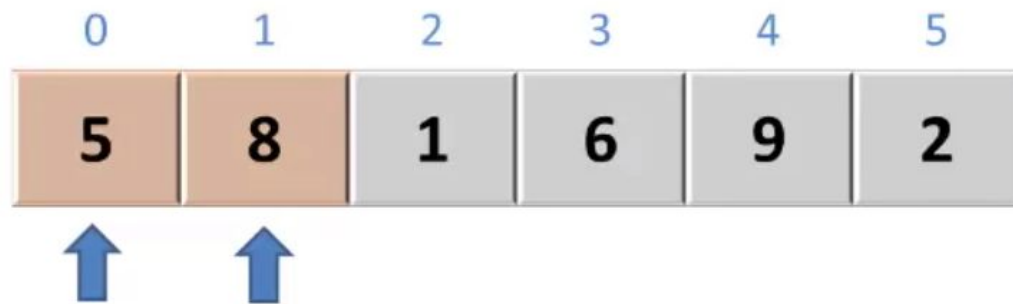


Repeatedly compares adjacent items.

Larger items “bubble” right.

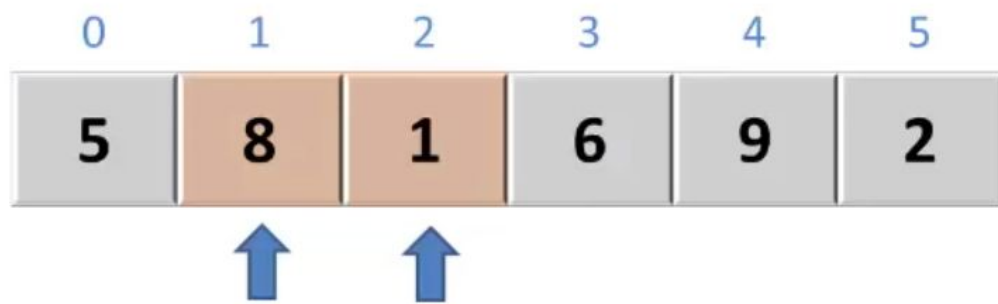
1st Iteration

## Bubble Sort



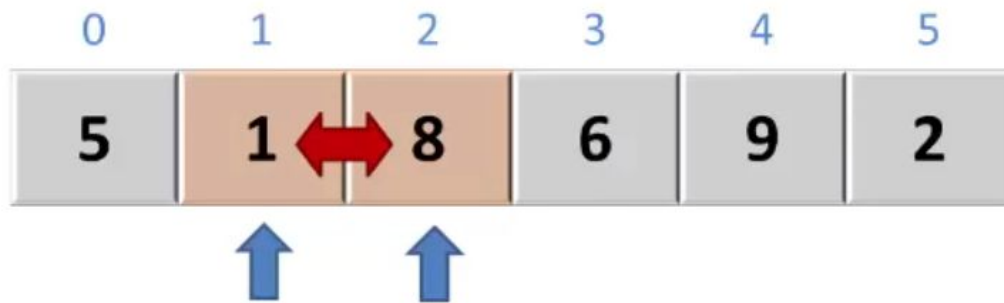
5 > 8 ? -> swap

## Bubble Sort



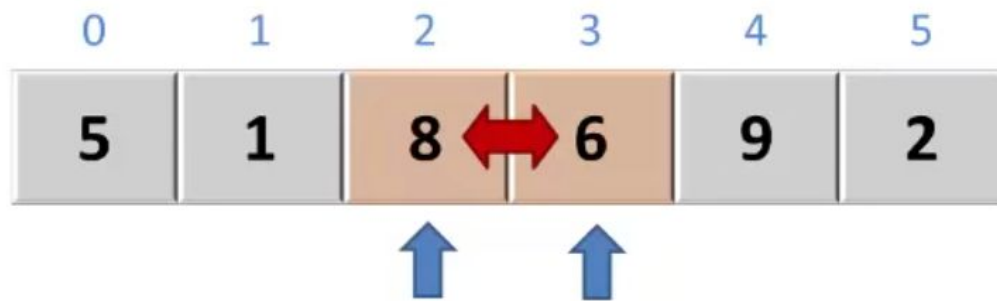
$8 > 1 ? \rightarrow \text{swap}$

## Bubble Sort



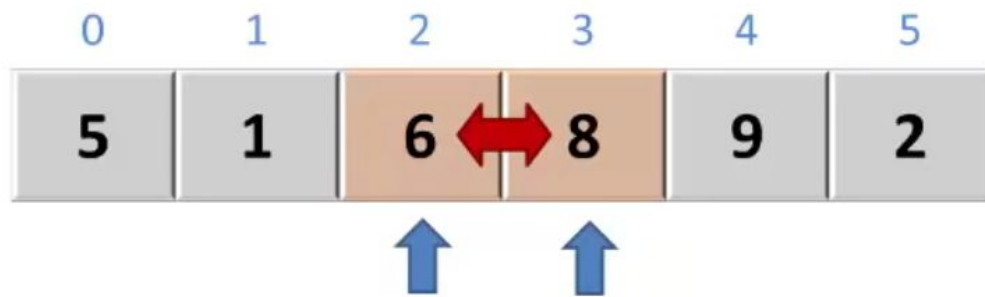
$8 > 1 ? \rightarrow \text{swap}$

## Bubble Sort

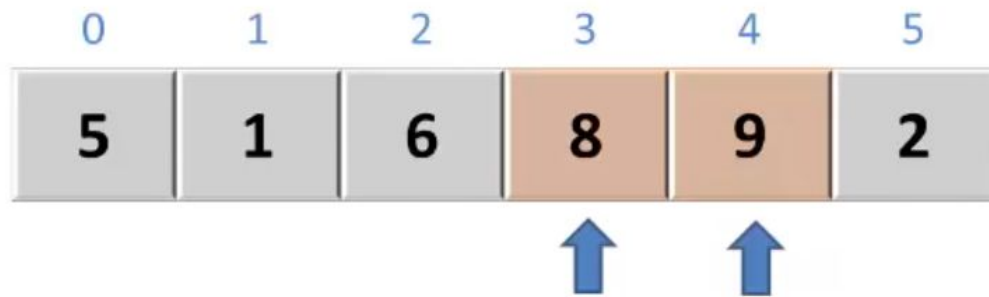


$8 > 6 ? \rightarrow \text{swap}$

## Bubble Sort

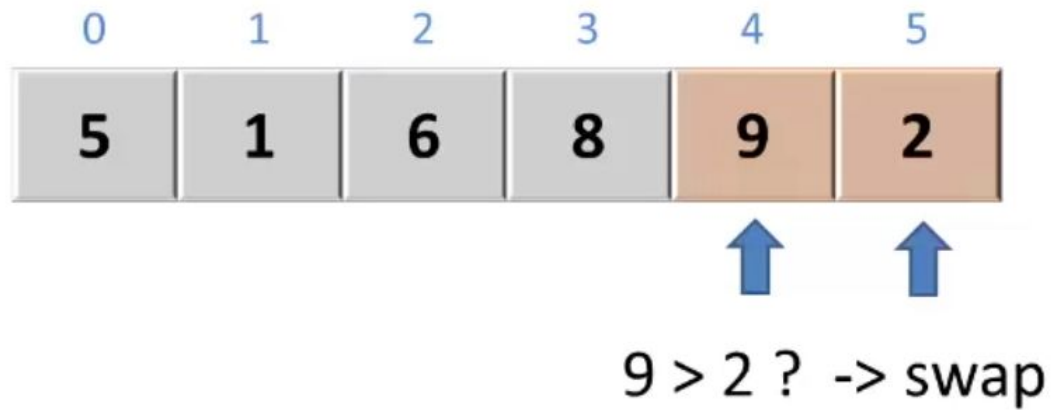


## Bubble Sort



8 > 9 ? -> swap

## Bubble Sort



After 1st iteration, first item bubbles to right



## Bubble Sort

0      1      2      3      4      5

Original list:

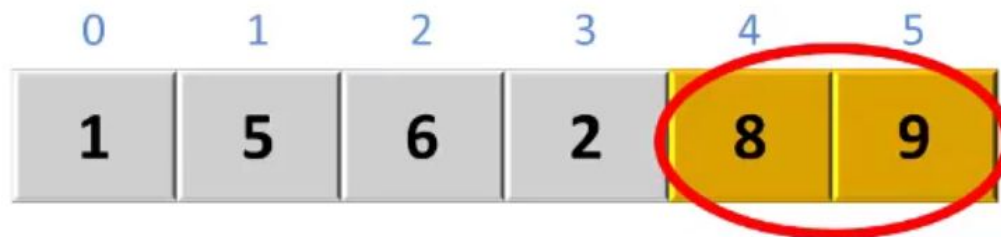
5	8	1	6	9	2
---	---	---	---	---	---

After 1 iteration:

5	1	6	8	2	9
---	---	---	---	---	---

After 2nd iteration

## Bubble Sort



After 3rd iteration

## Bubble Sort

0	1	2	3	4	5
1	5	2	6	8	9

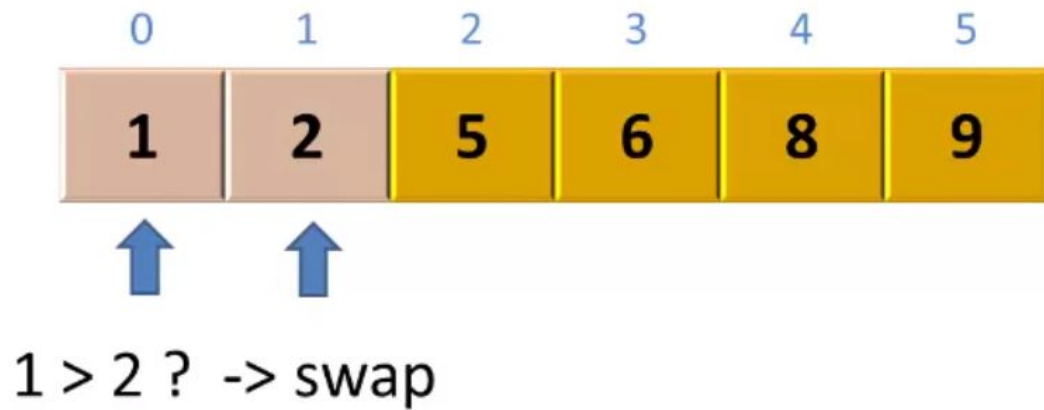
After 4th iteration

## Bubble Sort

0	1	2	3	4	5
1	2	5	6	8	9

After 5th iteration

## Bubble Sort



For 6 elements, it took 5 iterations.

Code:

## Bubble Sort – Java Code

```
public int[] bubbleSort (int[] list) {  
    int i, j, temp = 0;  
    for (i = 0; i < list.length - 1; i++) {  
        for (j = 0; j < list.length - 1 - i; j++) {  
            if (list[j] > list[j + 1]) {  
                temp = list[j];  
                list[j] = list[j + 1];  
                list[j + 1] = temp;  
            }  
        }  
    }  
    return list;  
}
```

Big o analysis:

In Bubble Sort,  $n-1$  comparisons will be done in the 1st pass,  $n-2$  in 2nd pass,  $n-3$  in 3rd pass and so on. So the total number of comparisons will be,

$$(n-1) + (n-2) + \dots + 3 + 2 + 1$$

$$\text{Sum} = n(n-1)/2$$

$$\text{i.e } O(n^2)$$

The **space complexity** for Bubble Sort is  **$O(1)$** , because only a single additional memory space is required

Also, the **best case time complexity** will be  **$O(n)$** , it is when the list is already sorted.

Following are the Time and Space complexity for the Bubble Sort algorithm.

- Worst Case Time Complexity [ Big-O ]:  **$O(n^2)$**
- Best Case Time Complexity [Big-omega]:  **$O(n)$**
- Average Time Complexity [Big-theta]:  **$O(n^2)$**

- Space Complexity:  $O(1)$

## Bubble Sort – Big Oh Analysis

Bubble Sort is not an efficient sorting algorithm because it uses nested loops.

It is useful only for small data sets.

It runs in  $O(n^2)$ .