

Introduction to Accelerator Physics

Part 1

Pedro Castro / Accelerator Physics Group (MPY)
 Introduction to Accelerator Physics
 DESY, 24th July 2017



	length	lab	run	particles	energy	dipole field
PETRA	2.3 km	DESY	1978-1986	e-/e+	2x19 GeV	0.33 T
PETRA II	2.3 km	DESY	1987-2007	e- or e+ p	12 GeV 40 GeV	0.21 T 0.7 T
PETRA III	2.3 km	DESY	2009- ?	e-	6 GeV	0.10 T
HERA	6.3 km	DESY	1992-2007	e- or e+ p	27.5 GeV 920 GeV	0.274 T 5 T
LEP	27 km	CERN	1989-2000	e-/e+	2x105 GeV	0.135 T
LHC	27 km	CERN	2010- ?	p/p	2x7000 GeV	8.3 T
FLASH	0.3 km	DESY	2004- ?	e-	1.2 GeV	
XFEL	3 km	DESY	2016- ?	e-	17.5 GeV	
ILC	30 km	?	?	e-/e+	2x250 GeV	

DESY CERN

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Applications of accelerators

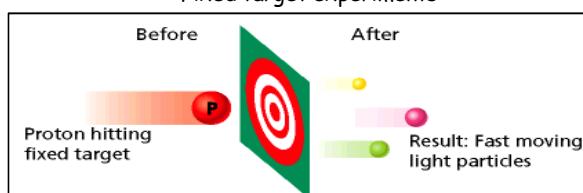
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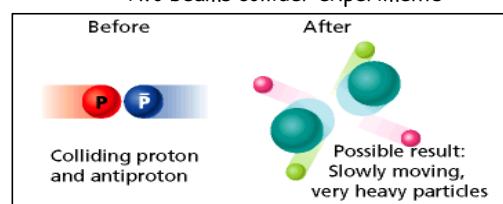
Applications of Accelerators (1)

Particle colliders for High Energy Physics (HEP) experiments

Fixed target experiments



Two beams collider experiments



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Applications of Accelerators (1)

Particle colliders for High Energy Physics experiments

Example: the Large Hadron Collider (LHC) at CERN

Lake Geneva Mont Blanc Geneva

8.6 km

built between 2001 and 2009
Higgs discovery: July 2012

superconducting magnets (inside a cryostat)

Worldwide ...

- About 120 accelerators for research in "nuclear and particle physics" http://en.wikipedia.org/wiki/List_of_accelerators_in_particle_physics

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Applications of Accelerators (2)

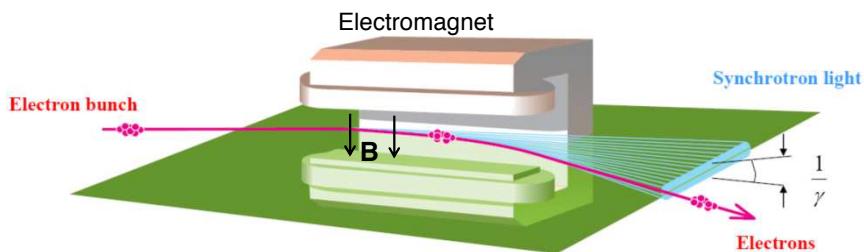
Light sources for biology, physics, chemistry... experiments

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Applications of Accelerators (2)

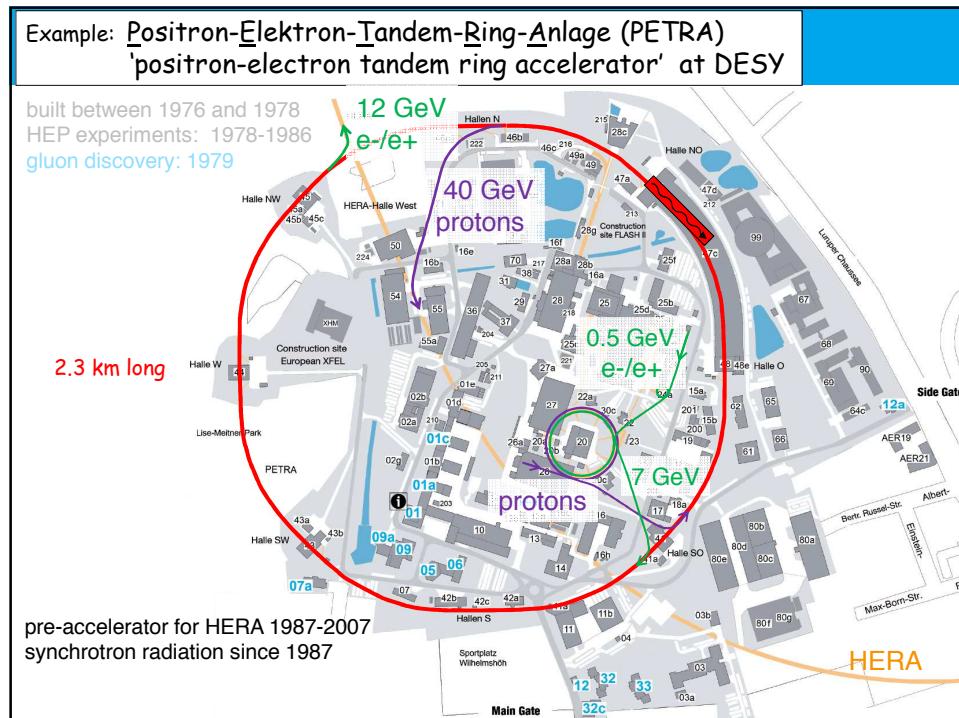
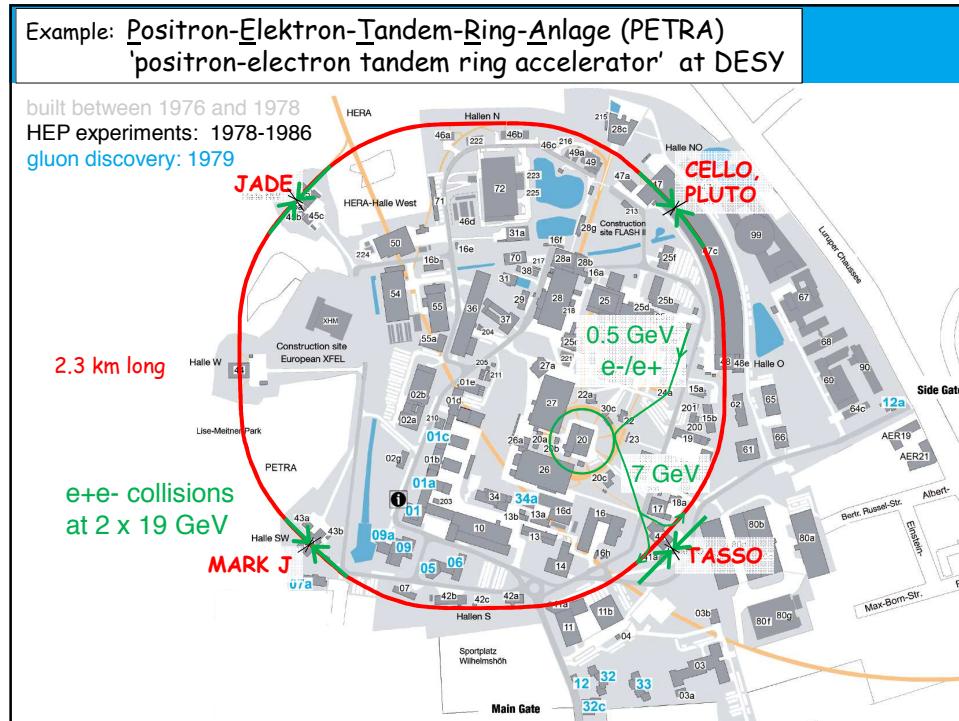
Light sources for biology, physics, chemistry... experiments

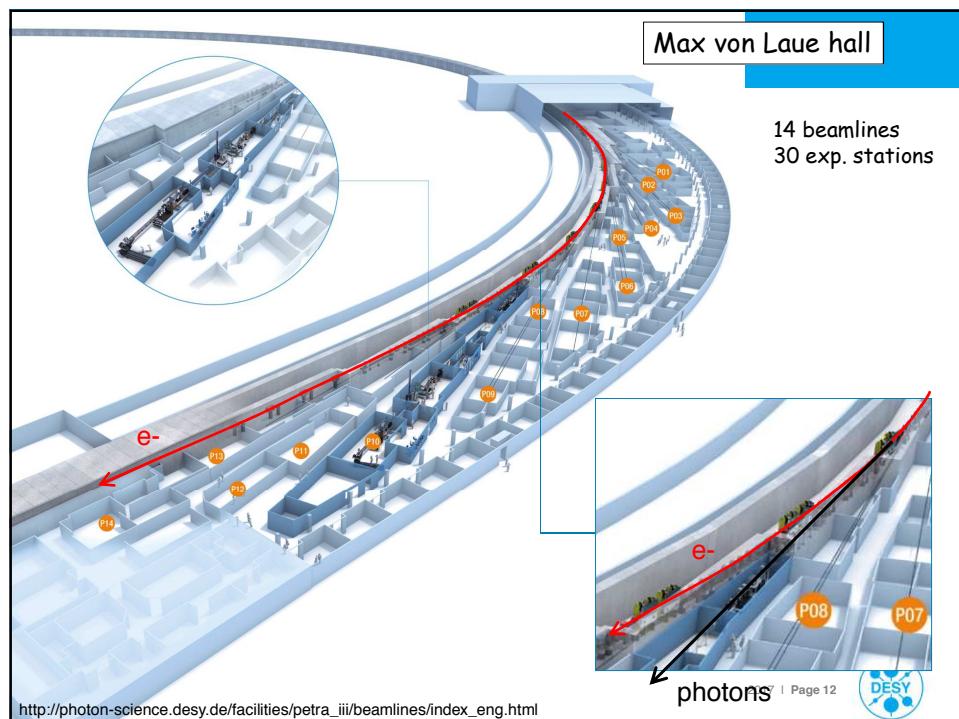
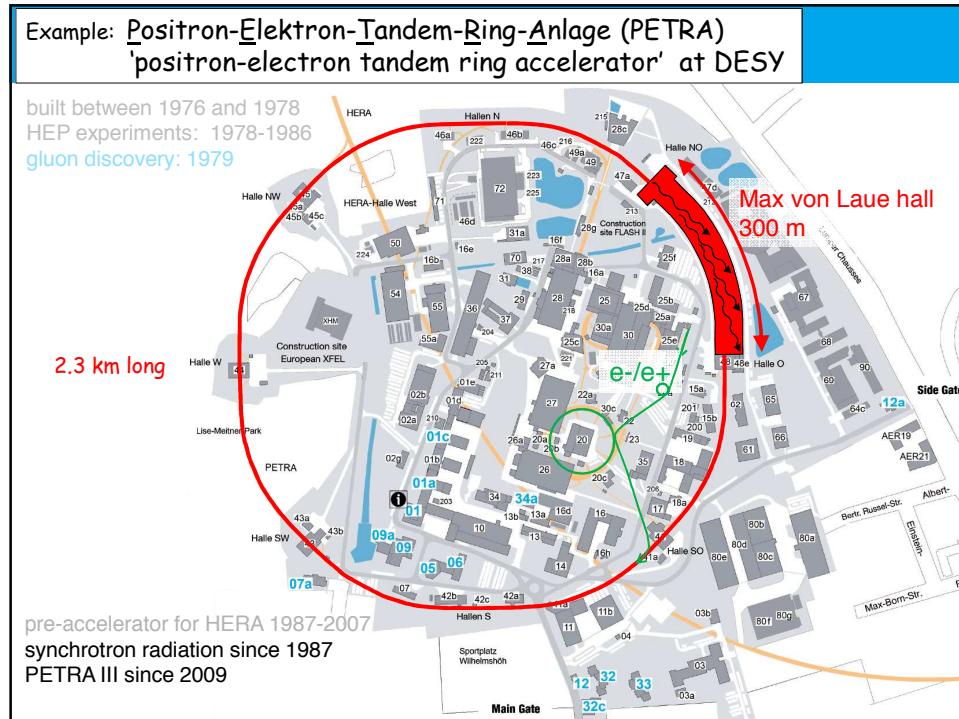


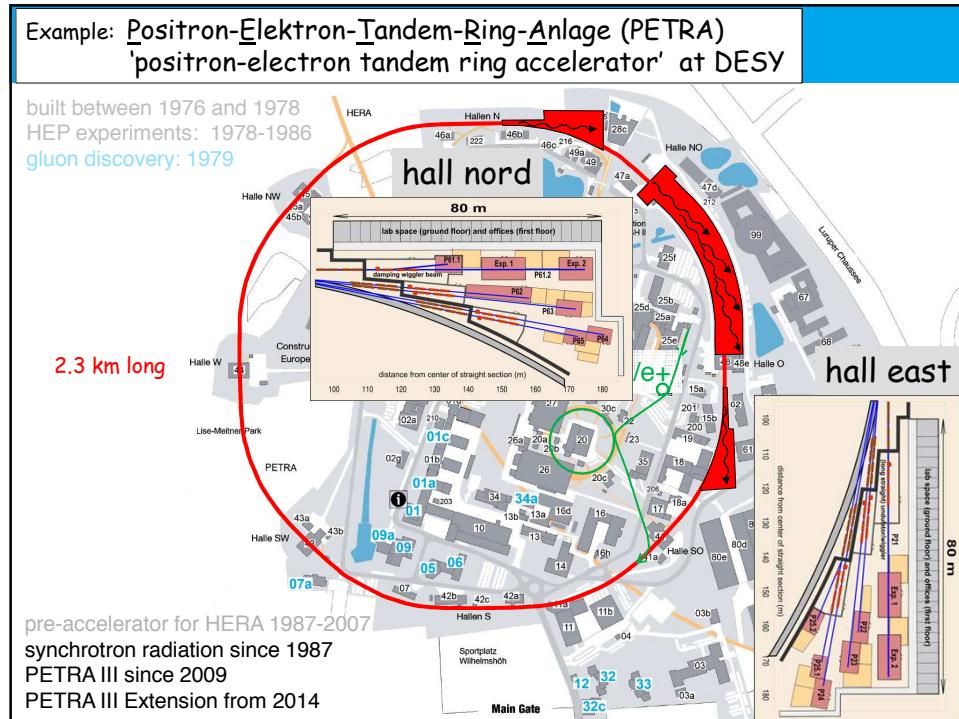
- structural analysis of crystalline materials
- X-ray crystallography (of proteins)
- X-ray microscopy
- X-ray absorption (or emission) spectroscopy
- ...

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Worldwide ...

- About 120 accelerators for research in "nuclear and particle physics" http://en.wikipedia.org/wiki/List_of_accelerators_in_particle_physics
- About 70 electron storage rings and electron linear accelerators used as light sources (so-called 'synchrotron radiation sources')
http://en.wikipedia.org/wiki/List_of_synchrotron_radiation_facilities

Applications of Accelerators (3)

Accelerators in medicine

For radioisotope production

proton beam + stable isotope $\xrightarrow{\text{transmutation}}$ radioactive isotope

For radiotherapy and radiosurgery:

- x-rays and gamma-rays
- ions (from protons to atoms with atomic number up to 18, Argon)
- neutrons

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Applications of Accelerators (3)

Accelerators in medicine

For radioisotope production

For example:

cyclotron

18 MeV proton accelerator



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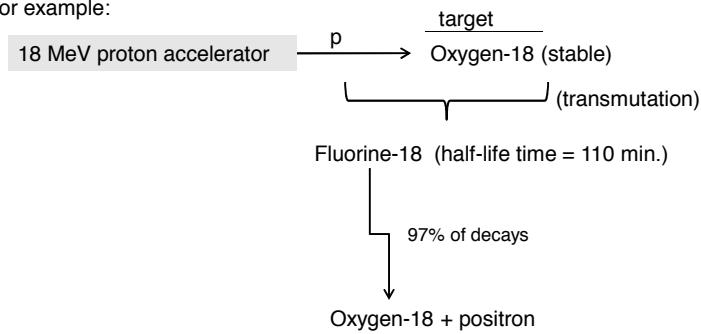


Applications of Accelerators (3)

Accelerators in medicine

For radioisotope production

For example:



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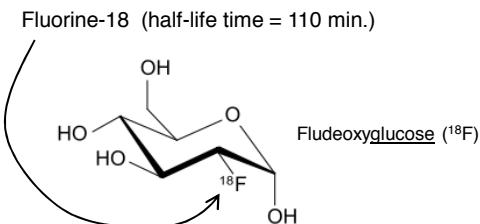
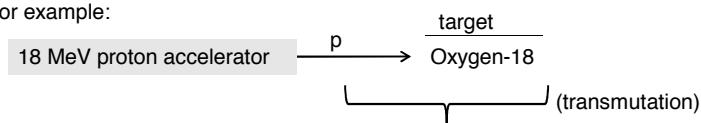


Applications of Accelerators (3)

Accelerators in medicine

For radioisotope production

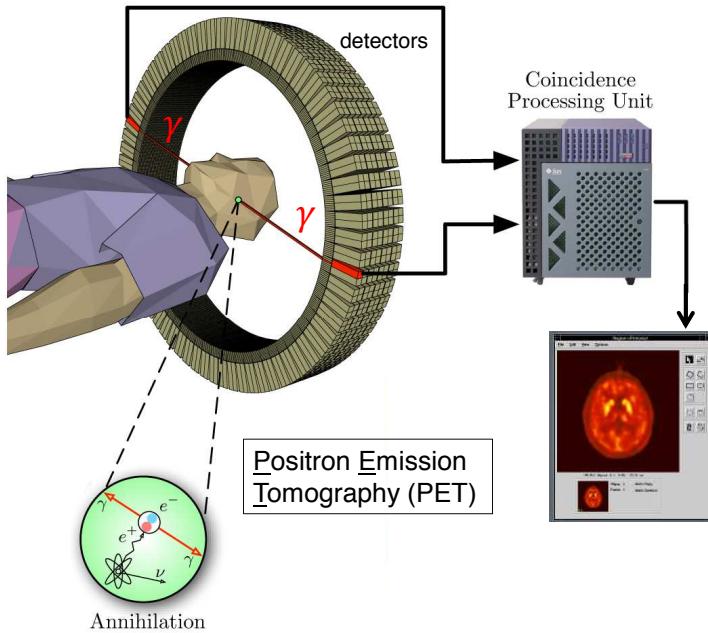
For example:



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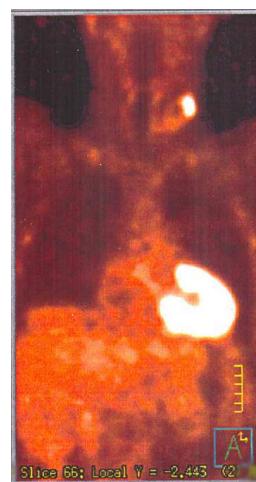
Applications of Accelerators (3)



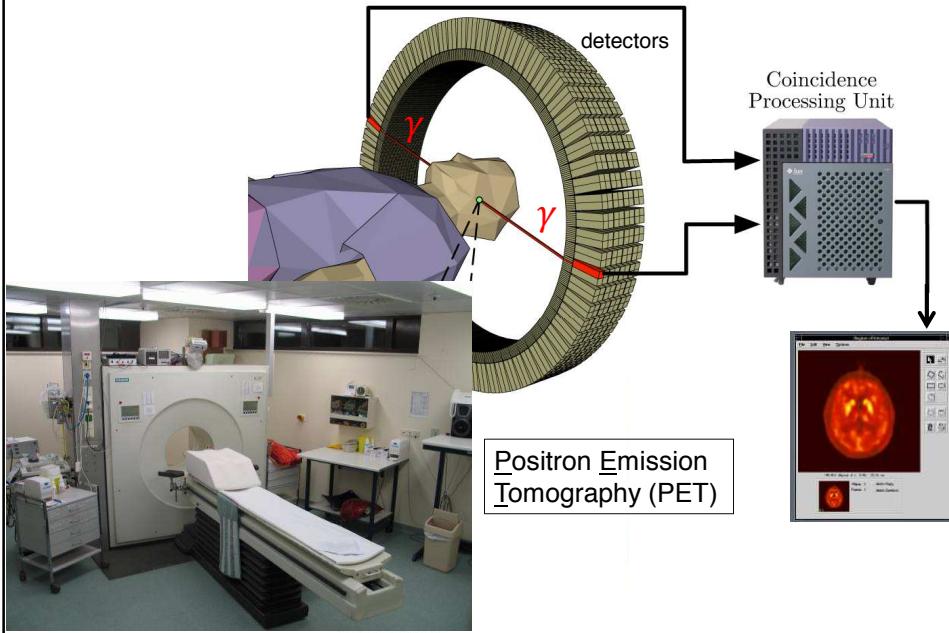
Positron Emission Tomography (PET)

Annihilation

PET



Applications of Accelerators (3)



Worldwide ...

- > About 120 accelerators for research in "nuclear and particle physics"
- > About 70 electron storage rings and electron linear accelerators used as light sources (so-called 'synchrotron radiation sources')

- > More than 7,000 accelerators for medicine
radiotherapy (>7,500), radioisotope production (200)

Applications of Accelerators (4)

For industrial applications:

Application	
Ion implantation	~ 9500
Electron cutting and welding	~ 4500
Electron beam and x-ray irradiators	~ 2000
Ion beam analysis (including AMS)	~ 200
Radioisotope production (including PET)	~ 900
Nondestructive testing (including security)	~ 650
Neutron generators (including sealed tubes)	~ 1000

approx. numbers from 2007 (worldwide)

with energies up to 15 MeV

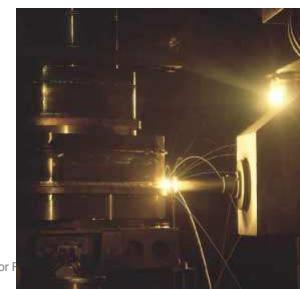
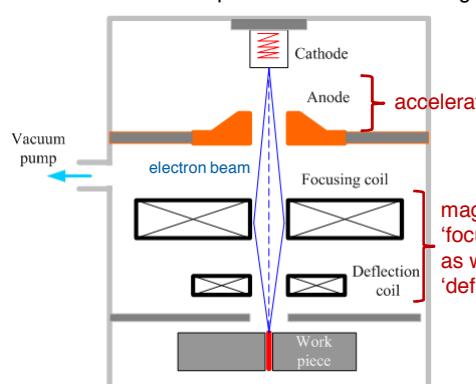
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Applications of Accelerators (4)

For industrial applications:

an example: electron beam welding



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Worldwide ...

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- > More than 7,000 accelerators for medicine
radiotherapy (>7,500), radioisotope production (200)
- > More than 18,000 industrial accelerators
ion implantation (>9,000) , electron cutting and welding (>4,000) ...

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Worldwide ...

- > About 120 accelerators for research in "nuclear and particle physics"
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radiotherapy (>7,500), radioisotope production (200)
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ion implantation (>9,000) , electron cutting and welding (>4,000) ...

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Worldwide ...

- > About 120 accelerators for research in "nuclear and particle physics"
- > About 70 electron storage rings and electron linear accelerators used as light sources (so-called 'synchrotron radiation sources')

...and there is more !!!

- > More than 7,000 accelerators for medicine
radiotherapy (>7,500), radioisotope production (200)
- > More than 18,000 industrial accelerators
ion implantation (>9,000) , electron cutting and welding (>4,000) ...

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Applications of Accelerators (5)

Many millions of television sets, oscilloscopes using CRTs (Cathode Ray Tube)



TV



oscilloscope

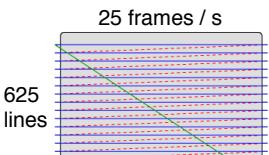
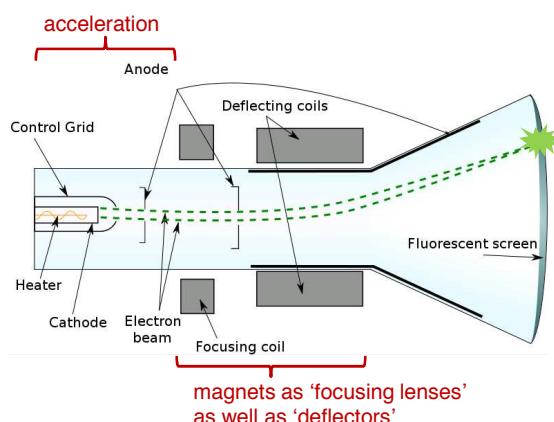


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Applications of Accelerators (5)

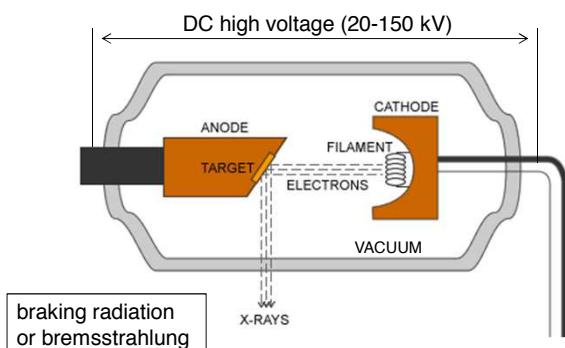
Many millions of television sets, oscilloscopes using CRTs (Cathode Ray Tube)



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Applications of Accelerators (6)

X-ray tubes



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Working with accelerators in the control room ...

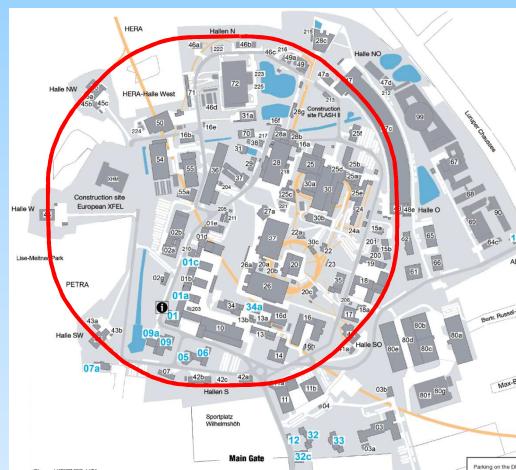
...requires:

- a lot of (accelerator) physics knowledge
- a lot of (accelerator) engineering knowledge
- some Sherlock Holmes' skills

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The case begins...



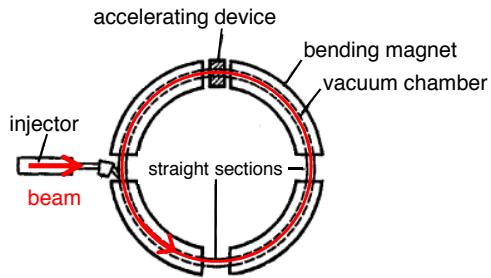
Accelerator Control Room
Hamburg, DESY
Sat. 12th June 2010
2 o'clock a.m.
PETRA runs with a beam current of 75 mA

02:24 a.m.: beam lost

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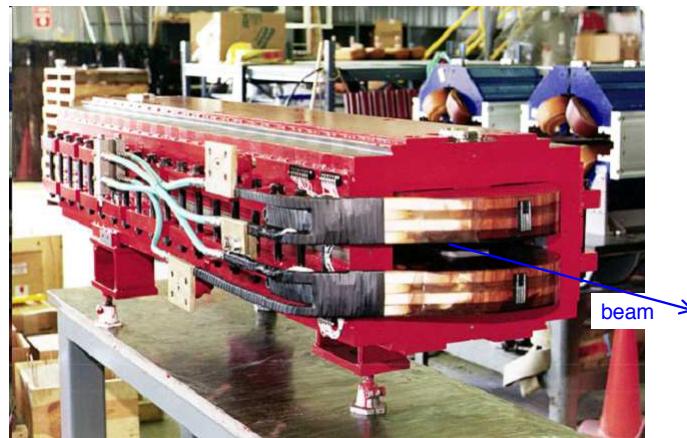
Circular accelerators: the synchrotron



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Dipole magnet

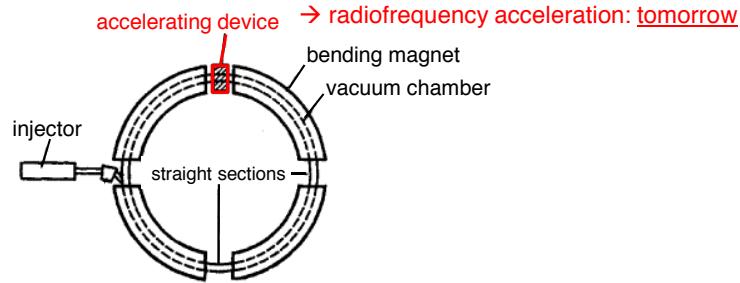


→ dipole magnets: tomorrow

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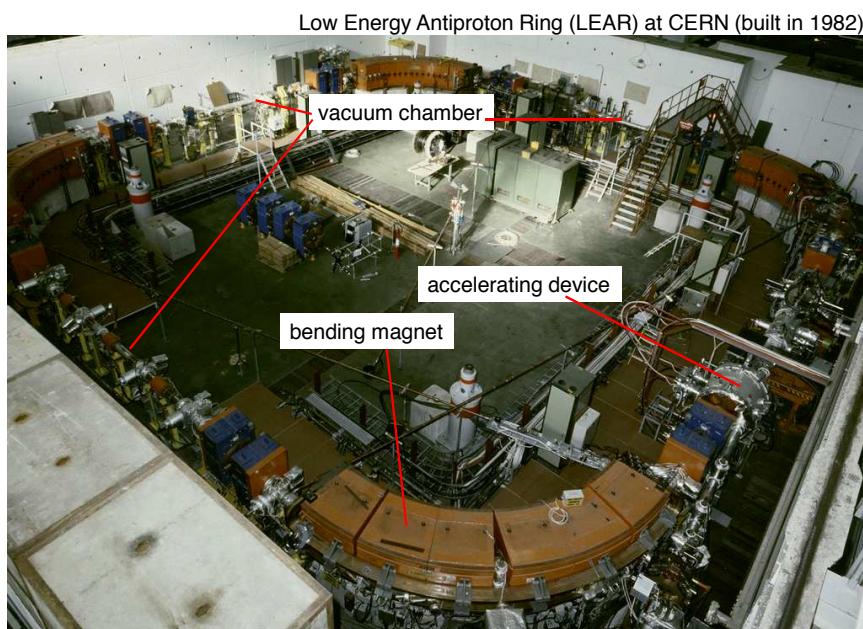
Circular accelerators: the synchrotron



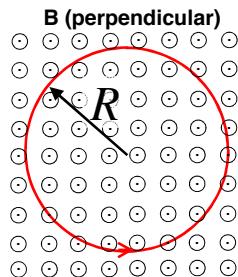
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Circular accelerators: the synchrotron



Circular accelerators: the synchrotron



$$\vec{F} = \frac{d\vec{p}}{dt} = q\vec{v} \times \vec{B}$$

momentum charge velocity
of the particle

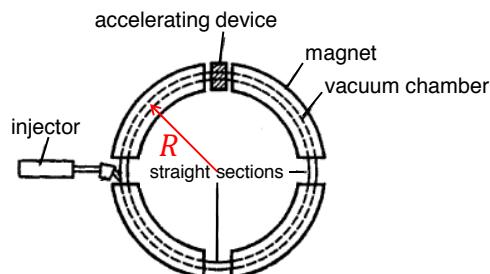
magnetic field

$$\left. \begin{aligned} \vec{B} \perp \vec{v} &\rightarrow F = qvB \\ \vec{F} \perp \vec{v} &\rightarrow F = m \frac{v^2}{R} \end{aligned} \right\} \quad \text{(circular motion)} \quad qB = \frac{mv}{R} \rightarrow R = \frac{mv}{qB}$$

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Circular accelerators: the synchrotron

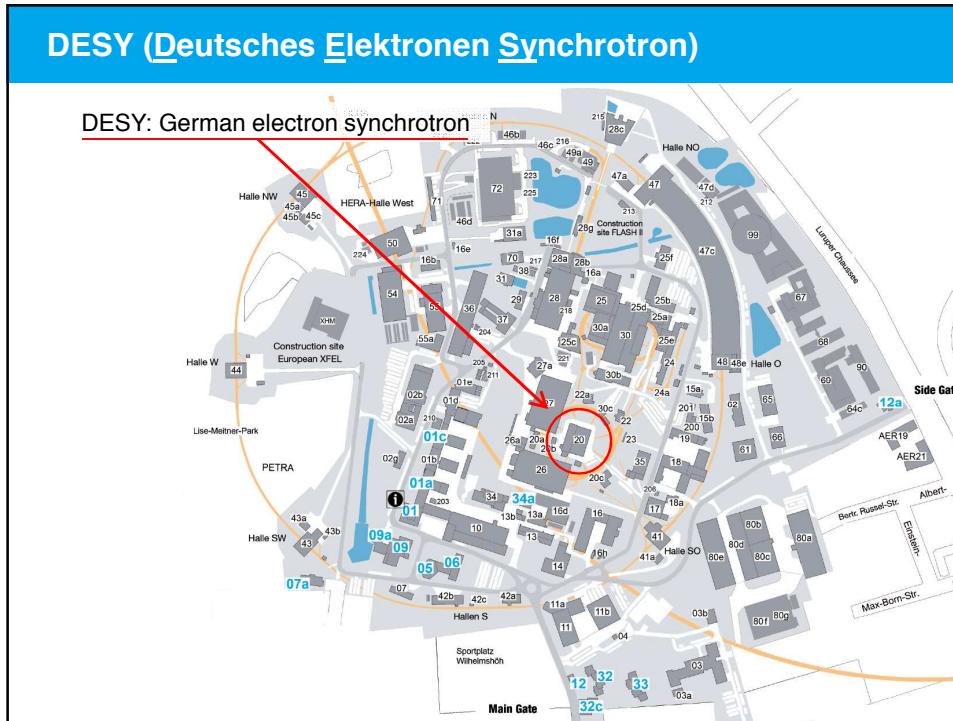


$$\left. \begin{aligned} \vec{B} \perp \vec{v} &\rightarrow F = qvB \\ \vec{F} \perp \vec{v} &\rightarrow F = m \frac{v^2}{R} \end{aligned} \right\} \quad \text{(circular motion)} \quad qB = \frac{mv}{R} \rightarrow R = \frac{mv}{qB} = \text{constant}$$

→ increase B **synchronously**
with $p = mv$ of particle

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02:24 a.m.: beam lost

The Main Accelerator Control Room

Hamburg, DESY
Sat. 12th June 2010

02:24 a.m.: beam lost

beam current [mA]

time

Sat Jun 12 00:00:59 CEST 2010

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PETRA runs with beam around the clock

PETRA Energy: 6.083 GeV Lifetime: 1.36 h Current: 89.55 mA

Beam Current [mA]

Und.	Gap	Status
PU01a	17.91	green
PU01b	18.13	green
PU02	10.51	green
PU03	11.04	green
PU04	23.46	green
PU05	10.56	green

building 25f, HASYLAB

Number of Bunches: 40

Orbit Control: On

User Operations

User Run, 40 Bu

17th July 2015 16:45

PETRA runs with beam around the clock

PETRA Energy: 6.083 GeV Lifetime: 1.36 h Current: 89.55 mA

Beam Current [mA]

24 hours

Und.	Gap	Status
PU01a	17.91	
PU01b	18.13	
PU02	10.51	
PU03	11.04	
PU04	23.46	
PU05	10.56	
PU06	12.42	
PU07	10.26	
PU08	17.00	
PU09	15.87	
PU10	11.74	
PU11	19.95	
PU12	20.10	
PU13	10.77	
PU14	11.02	

Number of Bunches: 40 Mean Vacuum Pressure: 1.404E-08 mbar

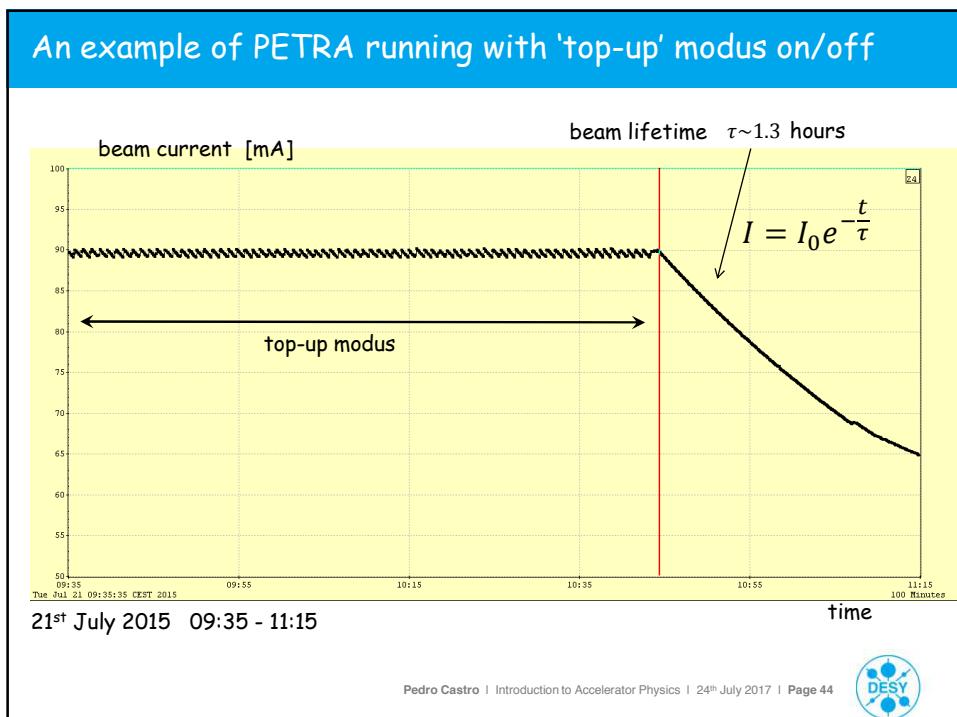
Orbit Control: On Top-Up Operation: 0.94 mA (Max-Min)

User Operations->Experiments

User Run, 40 Bunches, 90 mA

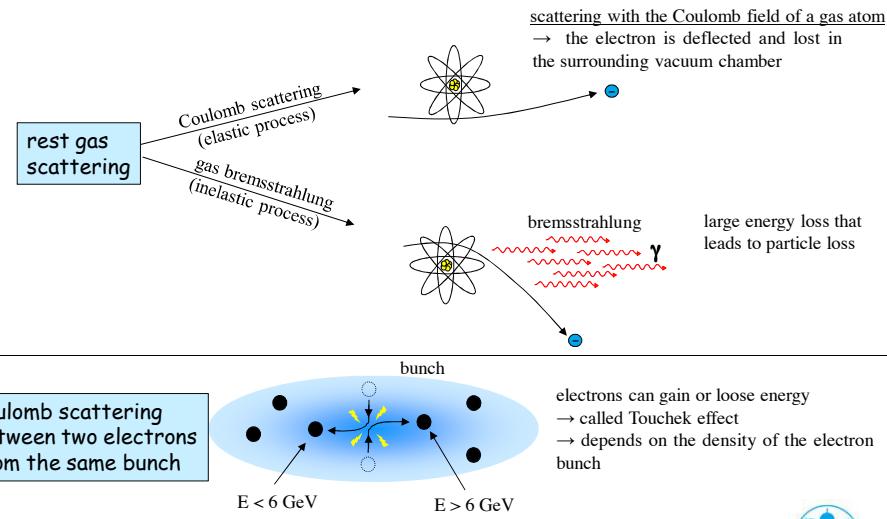
17th July 2015 16:45

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Beam lifetime

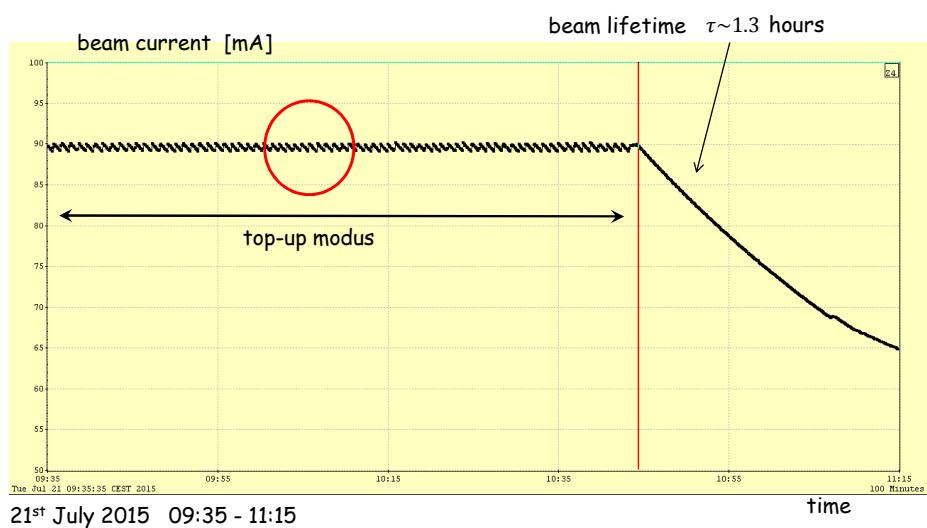
The lifetime of an electron beam is mainly limited by two effects:



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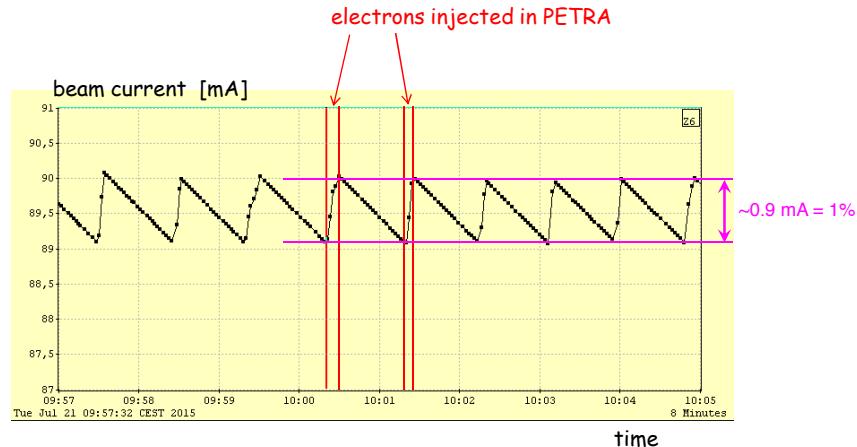
An example of PETRA running with 'top-up' modus on/off



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'top-up' modus



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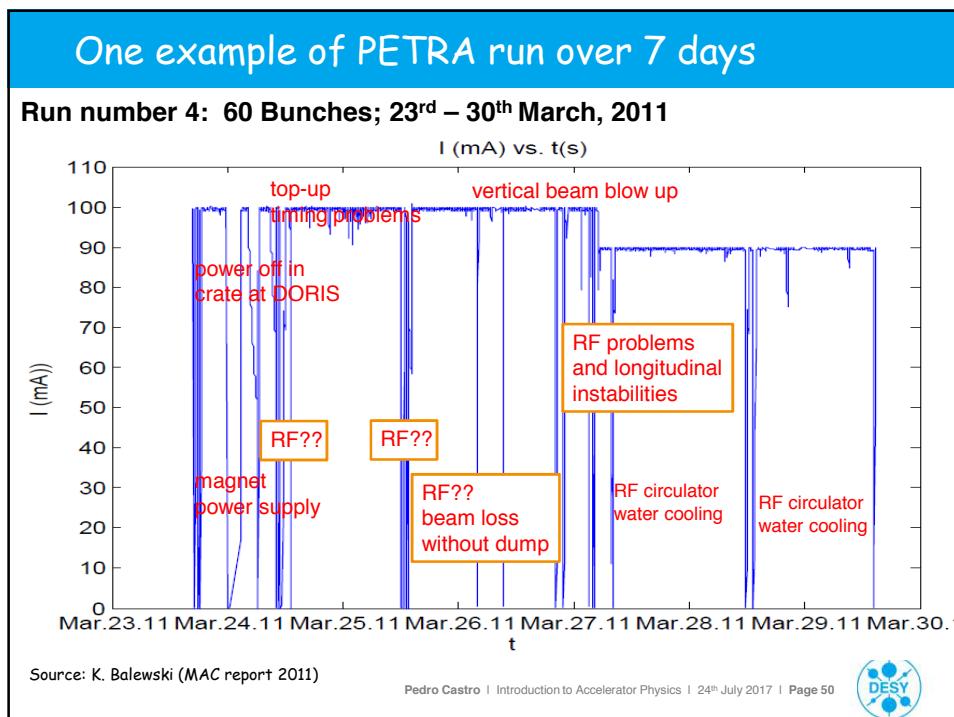
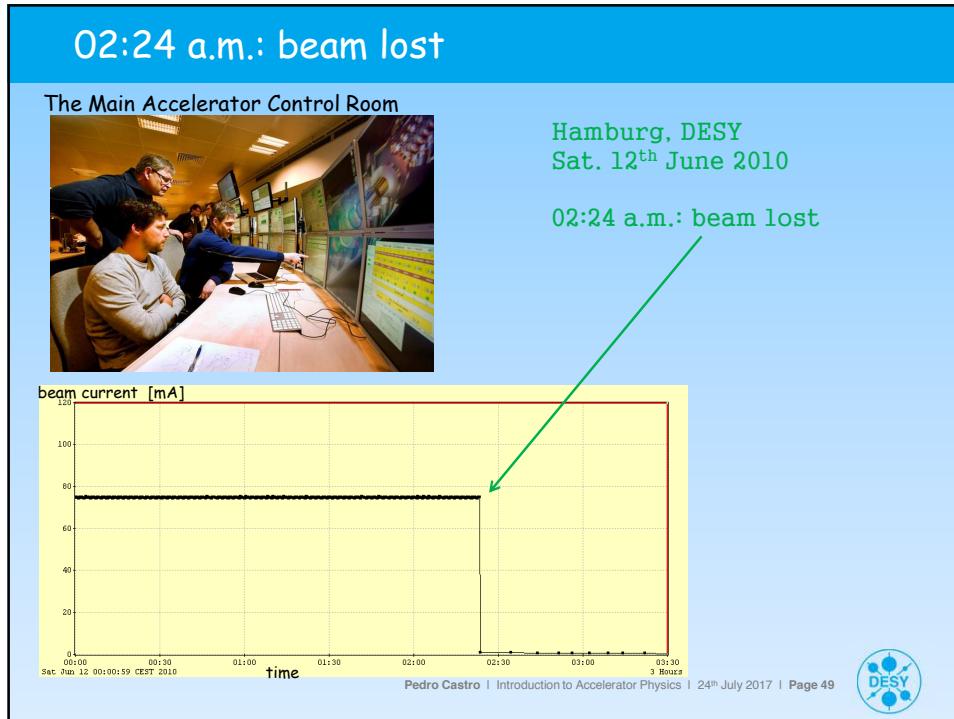
'top-up' modus

What are the advantages of running in 'top-up' modus?

- stable intensity conditions for measurements
- constant heat load on optical components (mirrors, filters, crystals...)
 - stable photon beam angle and position ('pointing stability')
 - stable wavelength
- constant heat load on accelerator vacuum chamber
- increased stability of all systems
- diagnostics: small dynamic range

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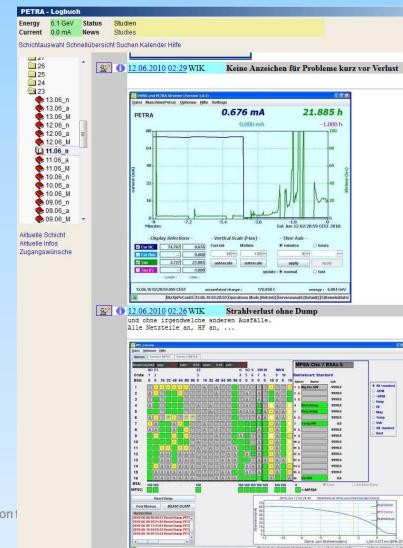


Beam lost at 02:24 a.m.

The link to the electronic logbook:

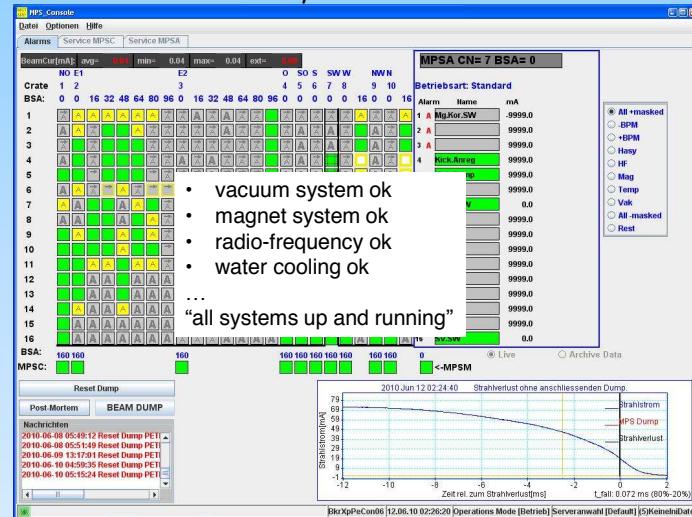
http://ttfinfo.desy.de/petra/show.jsp?dir=/2010/23/11.06_n&pos=2010-06-12T02:26:30

What to do?



The first suspect released: MPS is not guilty

The Machine Protection System status from 12th June 2010 at 02:26

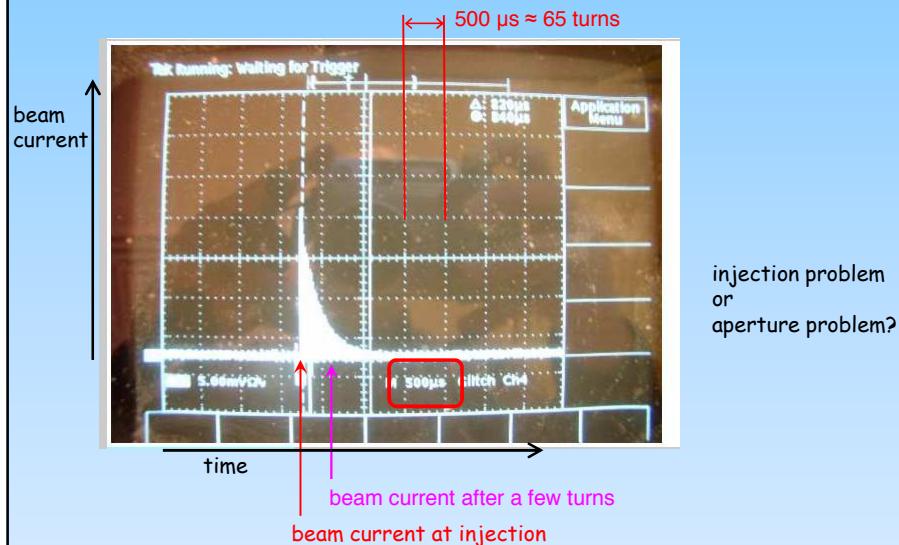


12th June 2010 02:26

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Electrons can be injected but cannot be stored !



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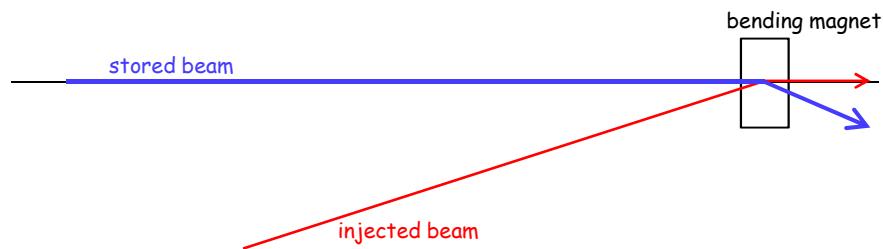
Next suspect: injection



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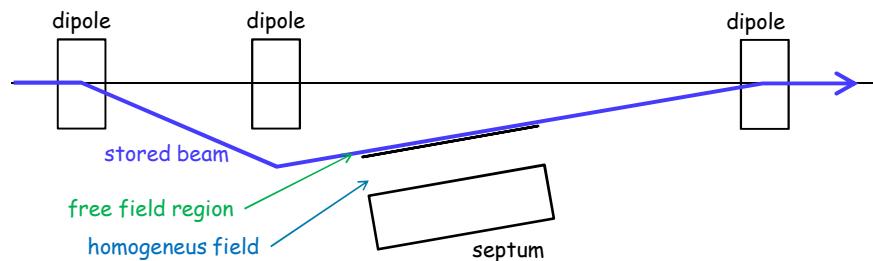
Next suspect: injection



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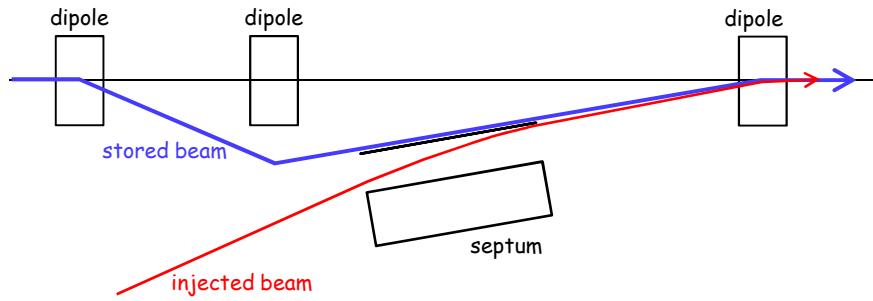
Next suspect: injection



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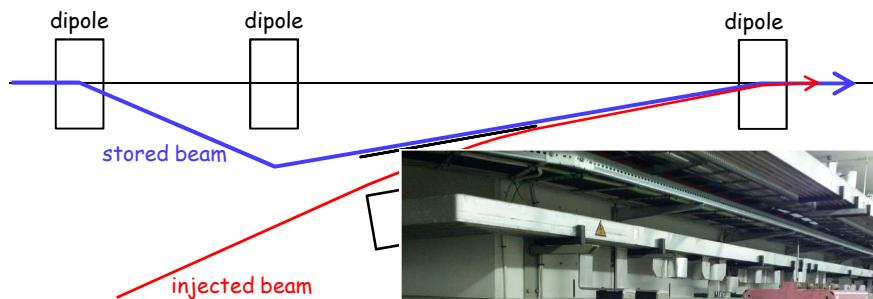
Next suspect: injection + accumulation



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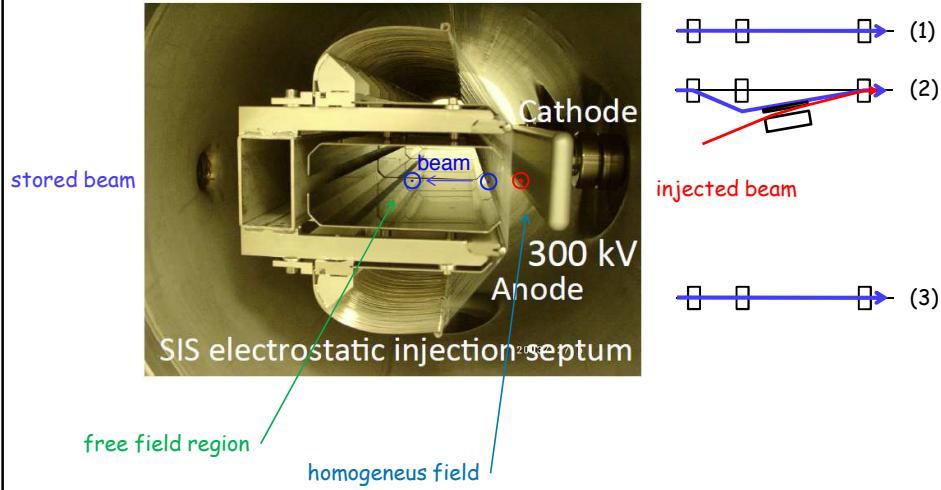
Next suspect: injection + accumulation



Pedro

Next suspect: injection + accumulation

septum at the Proton Synchrotron Booster (PSB) at CERN

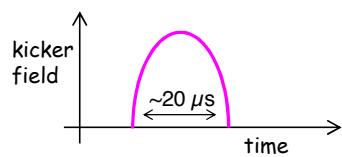
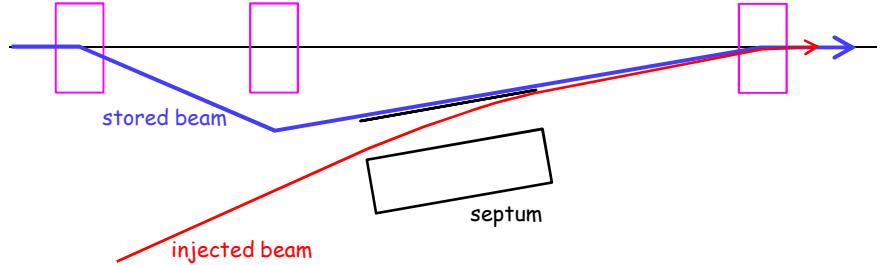


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Next suspect: injection + accumulation

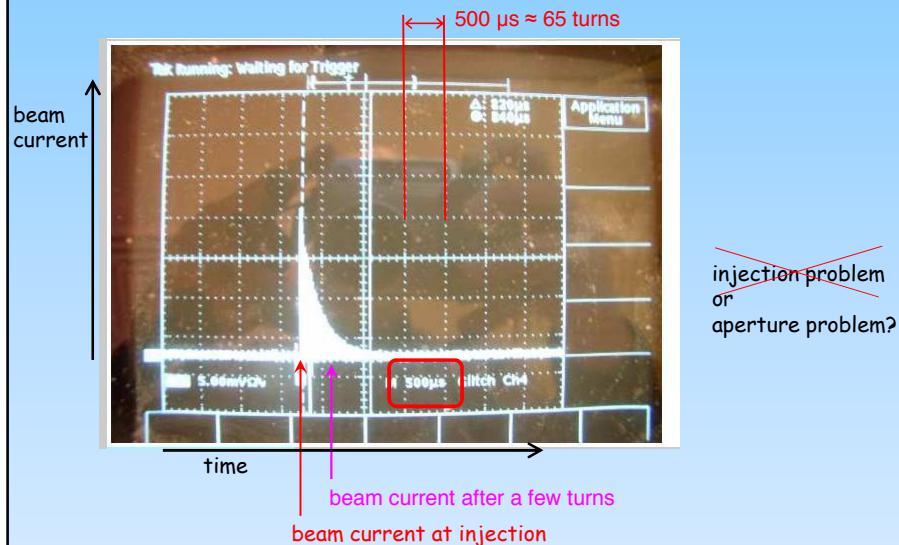
kicker (very fast dipole) kicker (very fast dipole) kicker (very fast dipole)



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Electrons can be injected but cannot be stored !



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Next suspect: an aperture problem

Hamburg, DESY
Sat. 12th June 2010

02:24 a.m.: beam lost
07:00 a.m.: visual inspection
in accelerator

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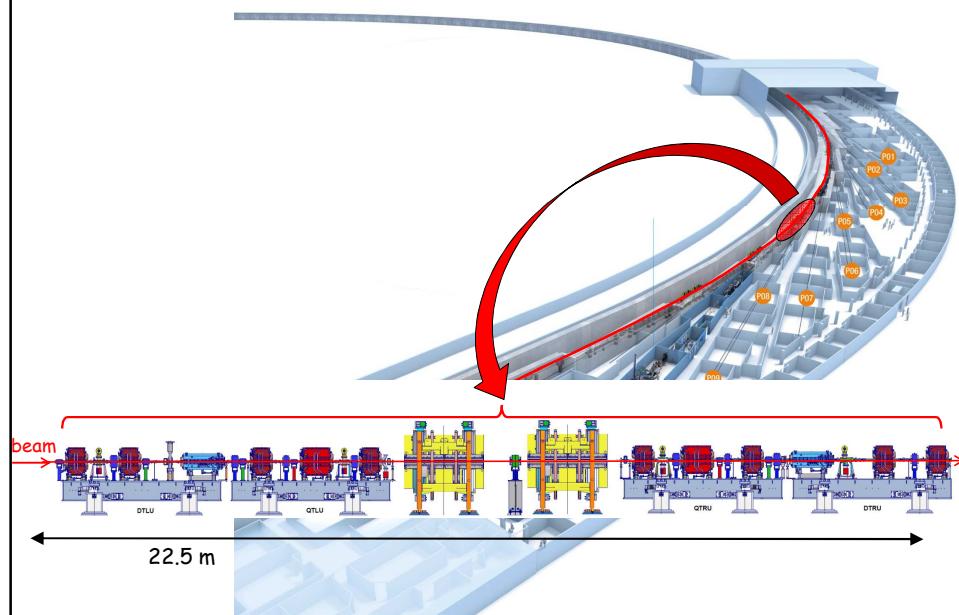
Next suspect: the new octant in 'Max von Laue hall'



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Next suspect: the new octant in 'Max von Laue hall'



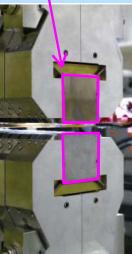
Next suspect: the new octant in 'Max von Laue hall'

Undulator PU 10

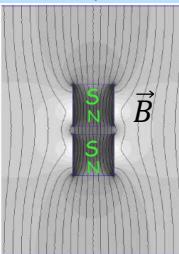


Hamburg, DESY
Sat. 12th June 2010

02:24 a.m.: beam lost
07:00 a.m.: visual inspection
in new octant



permanent
magnets



undulator field lines
 \vec{B}



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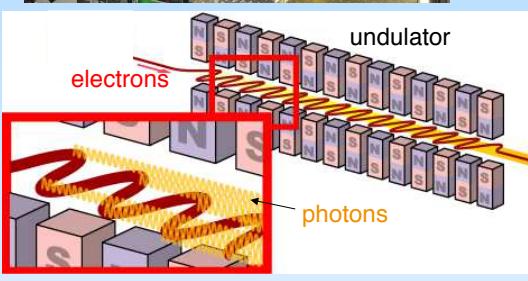
Next suspect: the new octant in 'Max von Laue hall'

Undulator PU 10

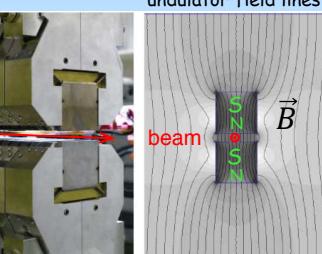


Hamburg, DESY
Sat. 12th June 2010

02:24 a.m.: beam lost
07:00 a.m.: visual inspection
in new octant



undulator
electrons
photons



undulator field lines
 \vec{B}
beam



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Next suspect: the new octant in 'Max von Laue hall'

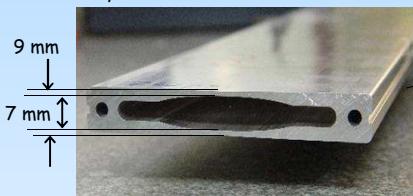
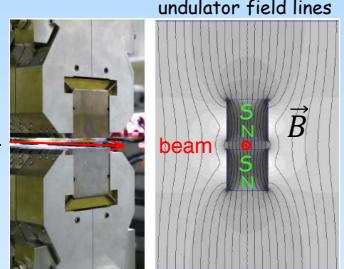
Undulator PU 10



Hamburg, DESY
Sat. 12th June 2010

02:24 a.m.: beam lost
07:00 a.m.: visual inspection
in new octant

very flat undulator vacuum chambers

undulator field lines

beam

\vec{B}

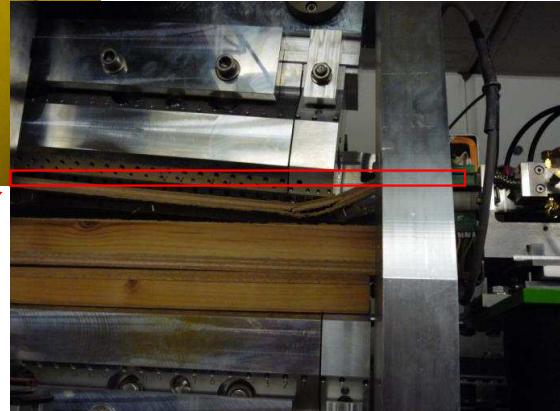
S N O S N

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Next suspect: the new octant in 'Max von Laue hall'

a couple of months earlier...

vacuum chamber

citation from the logbook: "What we have tried so far; ..."

↑
time
of
entries

12.06.2010 10:34 Sonstiges Kuehl, Vogt, Keil **Was haben wir alles versucht:**

- Optische Inspektion des neuen Achtels (nichts gefunden). Nur BPM nach Undulator PU03 zeigt 6 $\mu\text{Sv}/\text{h}$ während im Rest immer Werte unter 1 $\mu\text{Sv}/\text{h}$ gemessen werden.
- Sender-Untersuchungen:
 - Sender beide aus = 100 μs Strahl
 - Sender SR aus ein (9 MV) = 700 μs Strahl
 - Sender SR aus SE ein (9 MV) = 700 μs Strahl
 - Beide Sender ein = 700 μs Strahl
 - Sender SR um 180 Grad verstellt (Gegenphase) = ca. 100 μs Strahl
- 500 MHz-Frequenz kontrolliert; Synchronisation kontrolliert; Orbit liegt auf dem ersten Turn mittig (damit sollte Energie stimmen). Turn-By-Turn Daten zeigen, daß Energienpassung stimmt.
- First-Turn hat nicht unübliche Amplituden (H: 5 mm, V: 2mm); horizontale Tune stimmt; vertikaler Tune ist nicht zu messen
- Einzelne Spulen vertikal und horizontal mit Phasenvorschub gedreht und die Apertur ausgeleuchtet. Es ist damit keine Vermessung zu erreichen; nach beiden Richtungen wir die Injektion schlechter (d.h. noch weniger Turns).
- 3er Beule im Norden und Westen über die Wigglerrstrecken (H + V), jeweils mit Phasenverschiebung. Keine Verbesserung.
- 3er Beulen über jeweils einen halben Ring (H + V), jeweils mit Phasenverschiebung. Keine Verbesserung.
- Alle Ventile geschlossen und wieder geöffnet. Hilft nichts.
- Schirm hinter Septum rein und raus gefahren.
- Mit den letzten Spulen im Transportweg (V) sowie IME und Septum gewedelt: man kann damit die Injektion nur noch schlechter machen
- On Axis Injektion aufgesetzt (Kicker 3/Septum durchgefahrene)
- Pulsatoren-Scanner ausgefahren. Keine Verbesserung
- Tunekreis gedreht. Keine Verbesserung
- Trans. Feedbacks und long. Feedback ein/aus: Keine Verbesserung

12.06.2010 07:52 Sonstiges Kuehl, Vogt, Keil **Optische Inspektion des neuen Achtels, keine Auffälligkeiten**
Naja, bis auf den BPM nach Undulator PU03 dort haben wir 6 $\mu\text{Sv}/\text{h}$ gemessen, alle anderen < 1 $\mu\text{Sv}/\text{h}$.

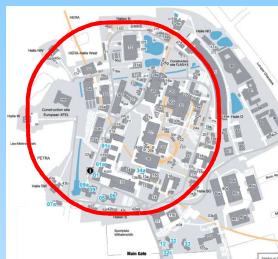
12.06.2010 07:02 Sonstiges has Frühschicht: Kühl, Schulz, Hansen, Wierzcholek
Schichtbeginn kein gespeicherter Strahl. Nur ca. 1000 Umläufe, keine Ausfälle

citation from the logbook: "Visual inspection of new octant: no findings"

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Next suspect: an aperture problem



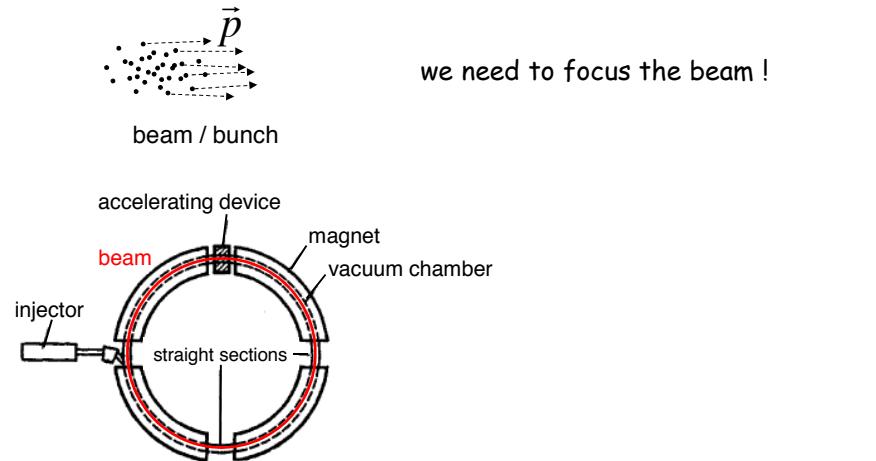
Hamburg, DESY
Sat. 12th June 2010

02:24 a.m.: beam lost
07:00 a.m.: visual inspection
in new octant
11:52 a.m.: start aperture scan

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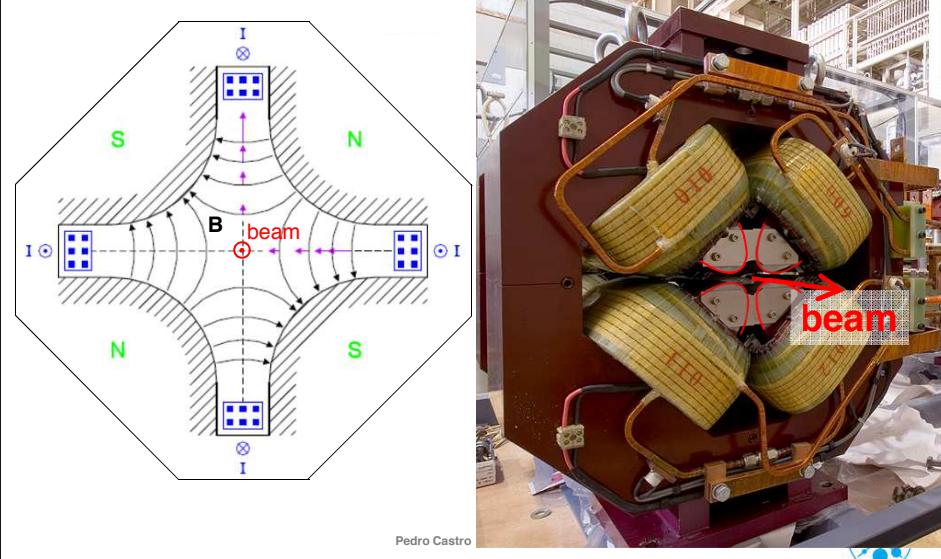
Need of focusing



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Quadrupole magnets

quadrupole magnet:



Pedro Castro

Quadrupole magnets

quadrupole magnet:
four iron pole shoes of hyperbolic contour

$$B_x = g \cdot y$$

$$B_y = -g \cdot x$$

$$g = \frac{\mu_0 I}{R^2} \text{ (quadrupole gradient)}$$

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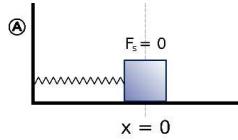
Quadrupole magnets

$$B_y = -g \cdot x \Rightarrow F_x = -g \cdot x$$

$$\vec{F} = q\vec{v} \times \vec{B} \text{ (Lorentz force)}$$

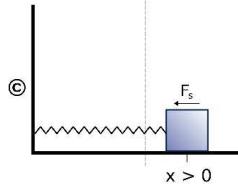
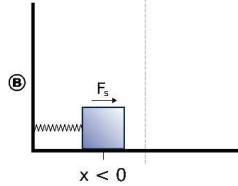
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Classical mechanics: harmonic oscillator



restoring force:

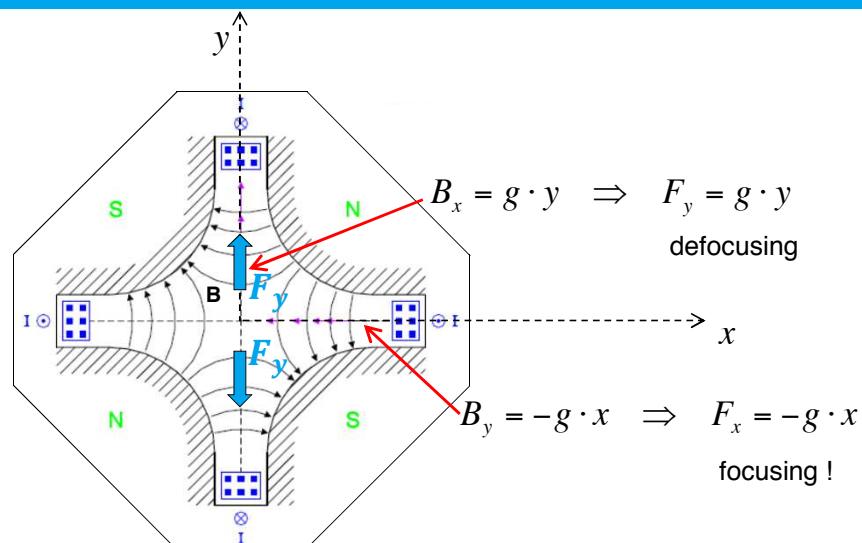
$$F = -kx$$



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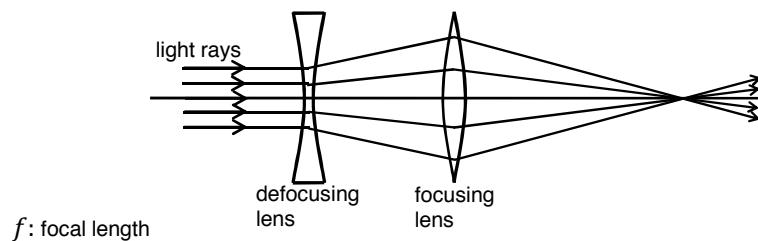
Quadrupole magnets



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In light optics...



$$f^*: \text{system focal length} \quad \frac{1}{f^*} = \frac{1}{f_D} + \frac{1}{f_F} - \frac{d}{f_D f_F} \quad (\text{light optics})$$

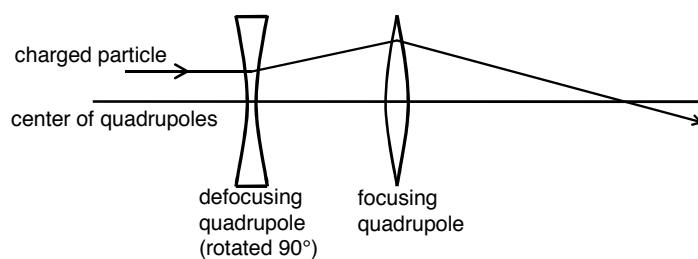
$$\text{if } f_D = -f_F = f \quad \frac{1}{f^*} = \frac{d}{f^2} > 0$$

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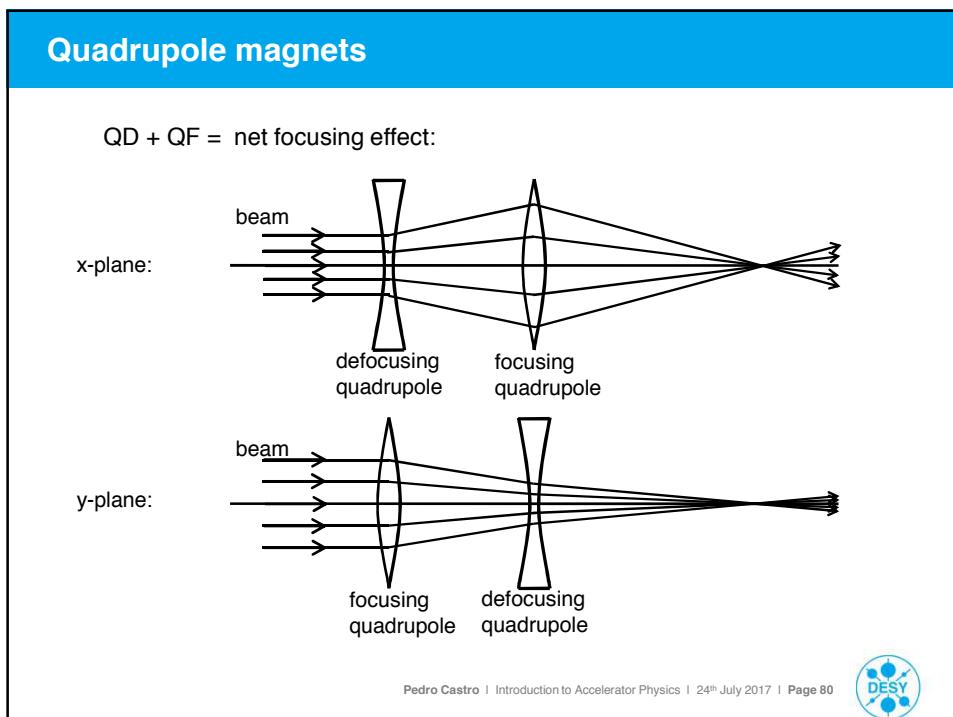
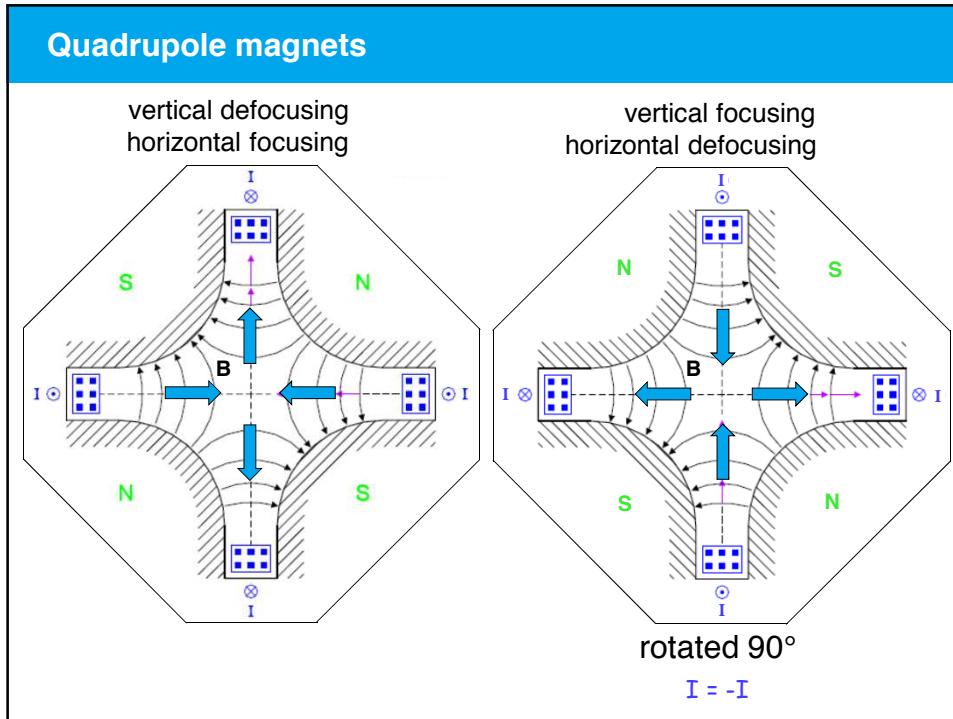
Quadrupole magnets

QD + QF = net focusing effect:



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Quadrupole magnets

QD + QF = net focusing effect:

x-plane:

beam

defocusing quadrupole

focusing quadrupole

QF

QD

focusing quadrupole

defocusing quadrupole

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Circular accelerator

PETRA

focusing quadrupole

dipole magnet

QF

QD

B

defocusing quadrupole

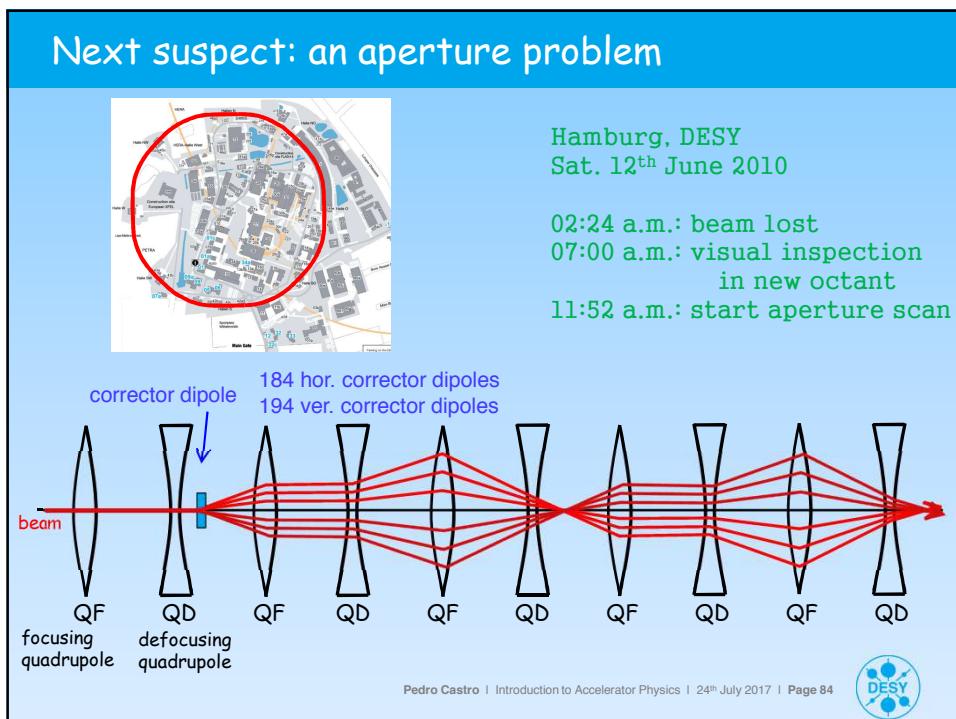
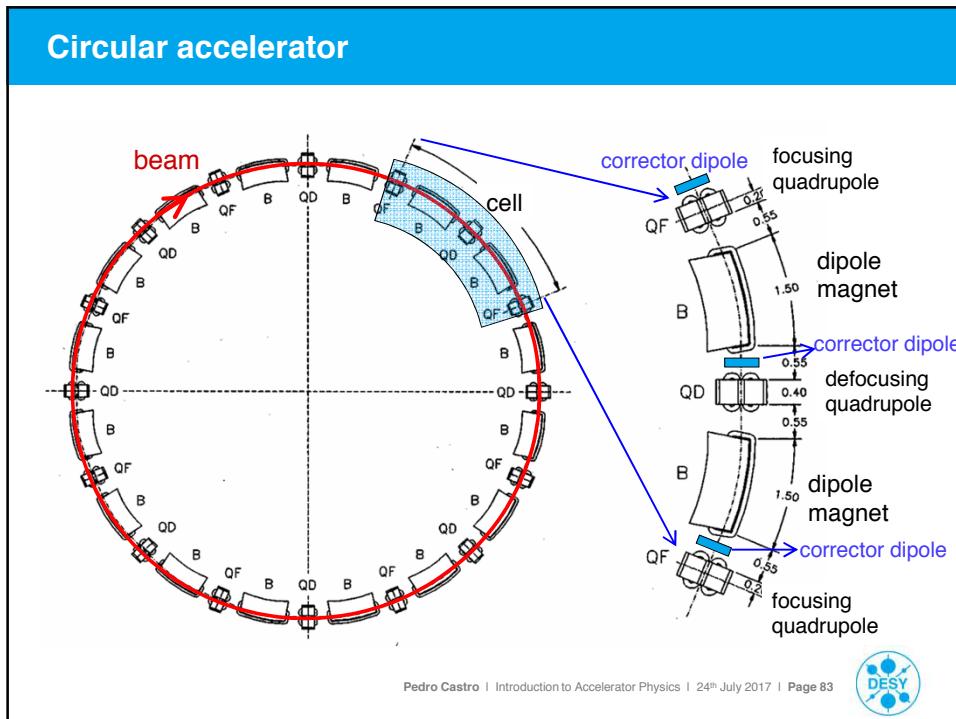
dipole magnet

QF

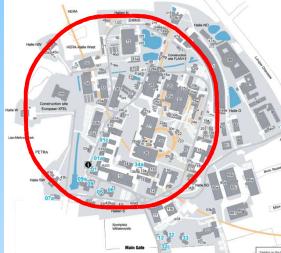
QD

B

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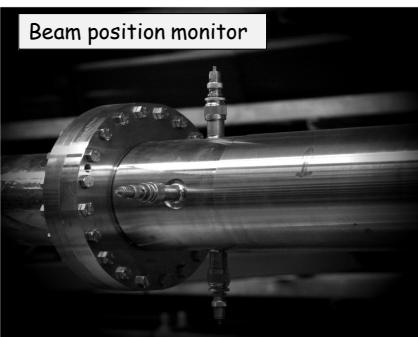
First useful hint: aperture problem



Hamburg, DESY
Sat. 12th June 2010

02:24 a.m.: beam lost
07:00 a.m.: visual inspection
in new octant
11:52 a.m.: start aperture scan
13:20 a.m.: beam stored

Beam position monitor

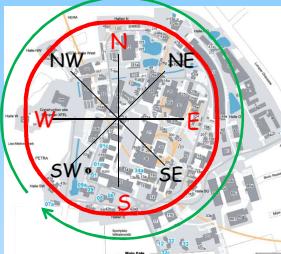


244 beam position monitors

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First useful hint: aperture problem



Hamburg, DESY
Sat. 12th June 2010

02:24 a.m.: beam lost
07:00 a.m.: visual inspection
in new octant
11:52 a.m.: start aperture scan
13:20 a.m.: beam stored

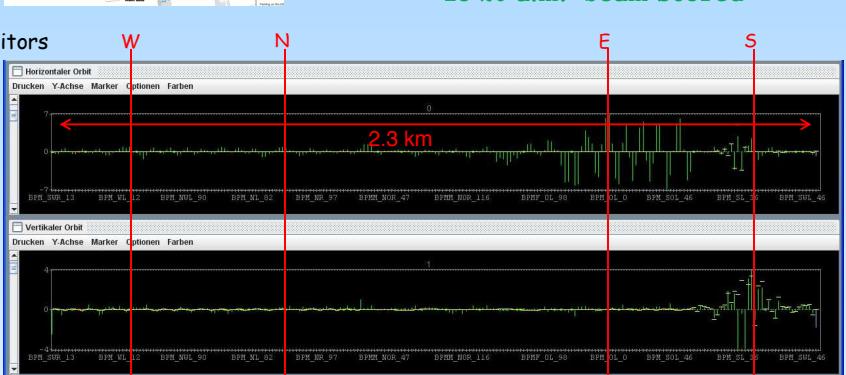
244 monitors

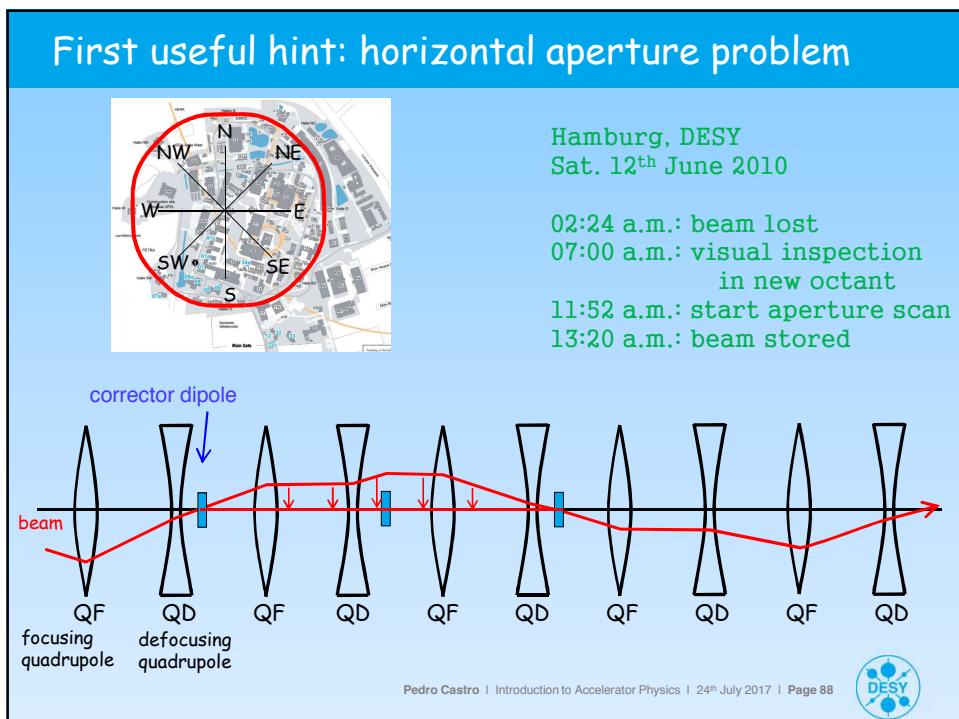
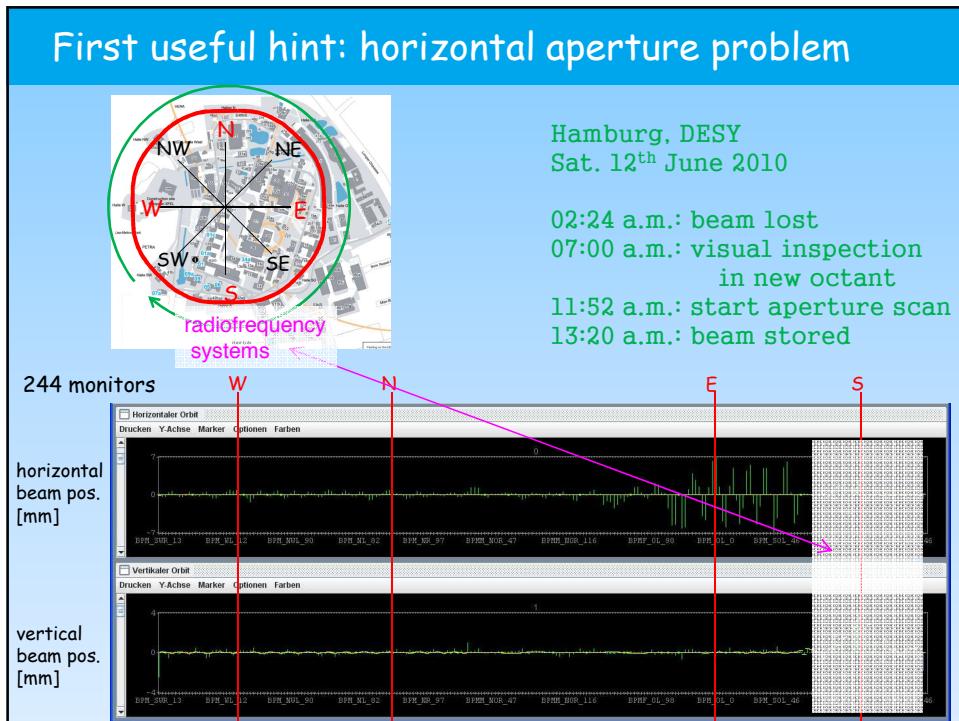
horizontal beam pos.
[mm]

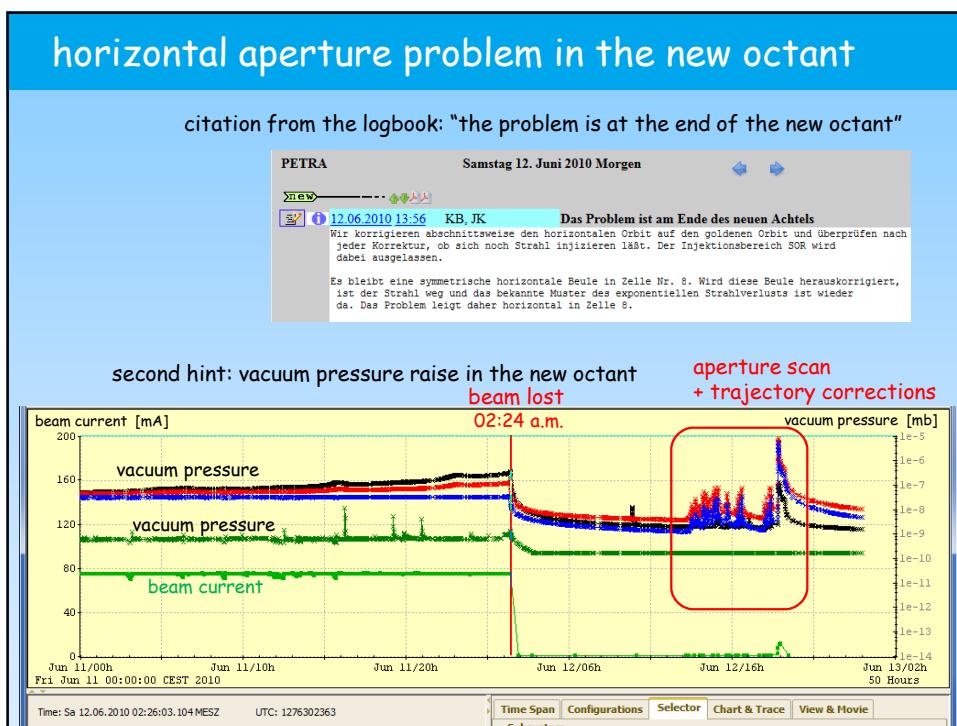
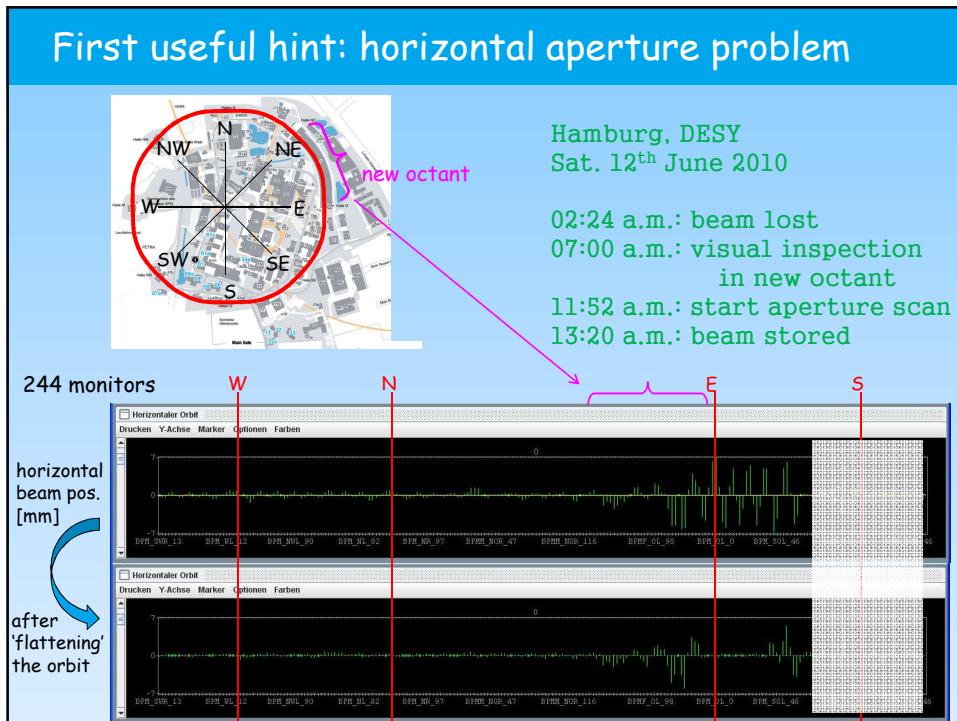
vertical beam pos.
[mm]

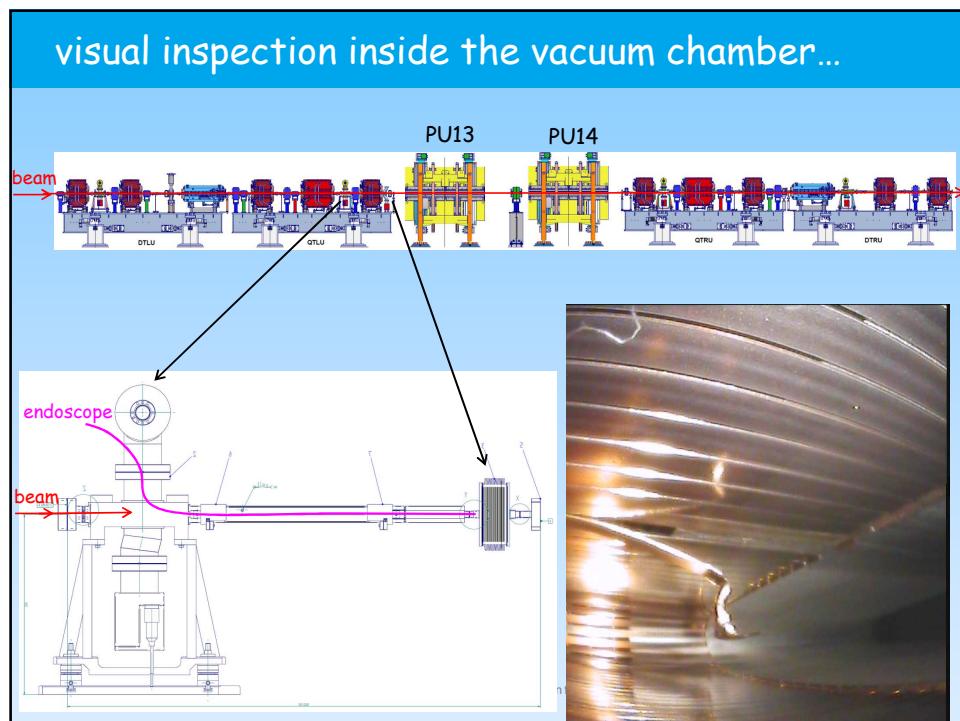
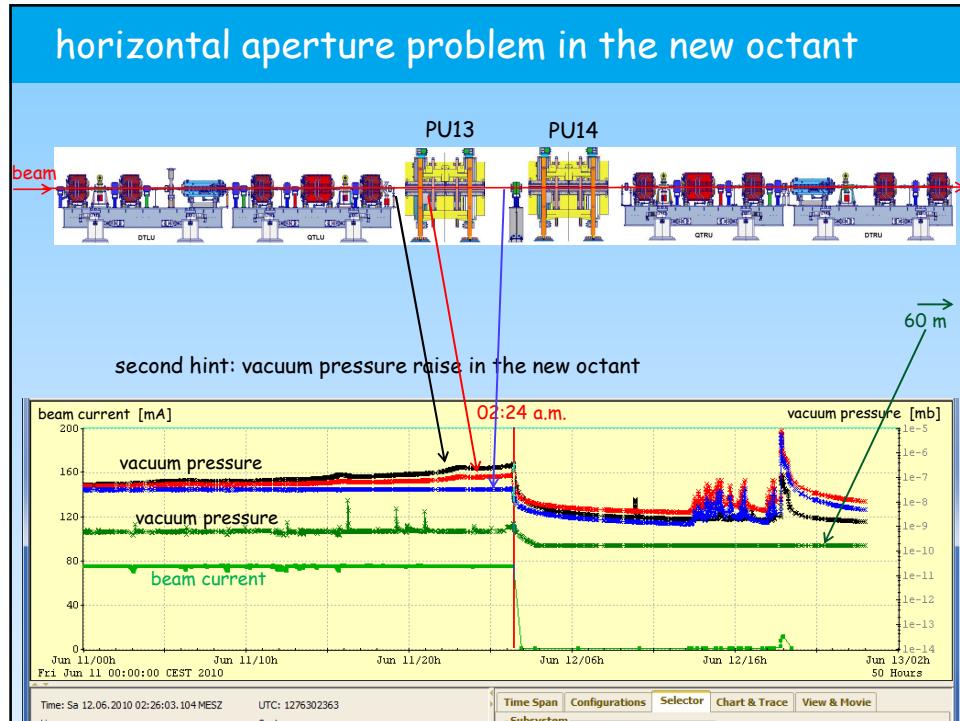
W N E S

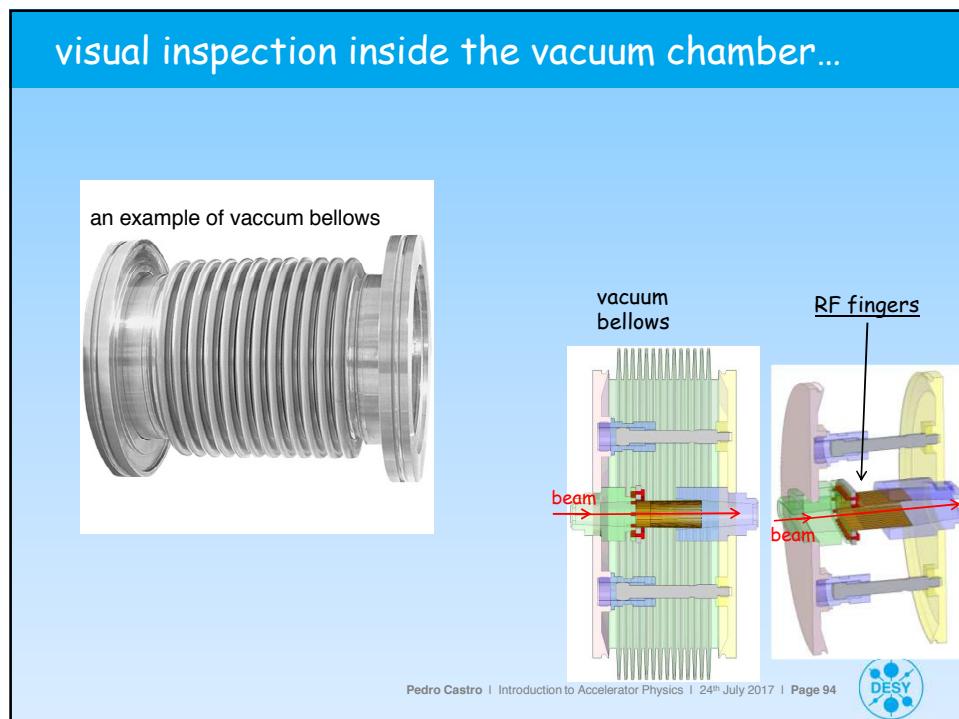
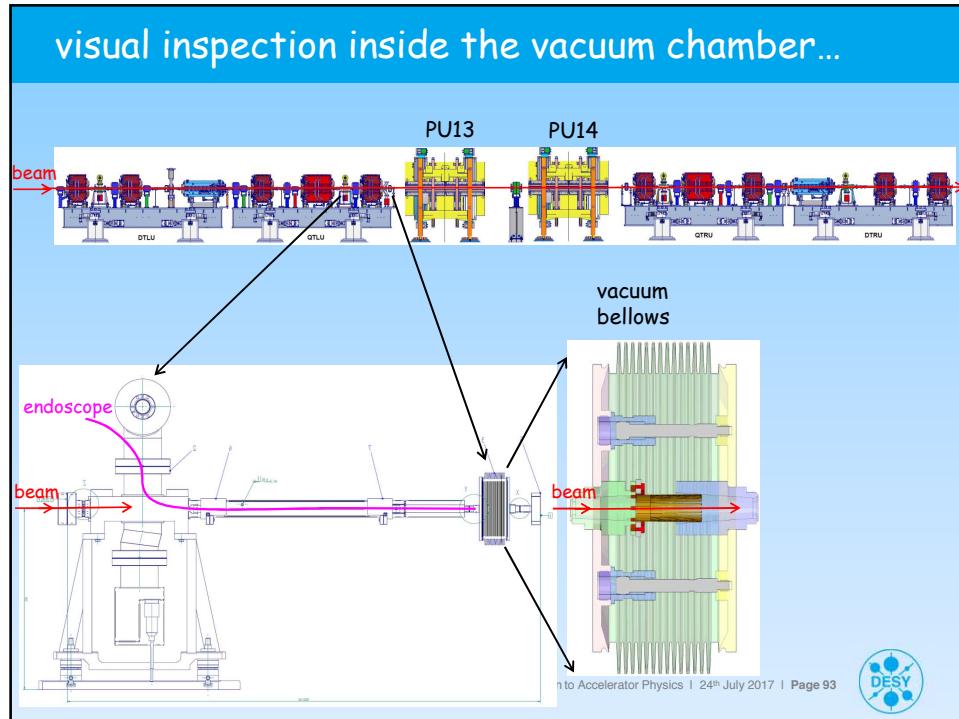
2.3 km



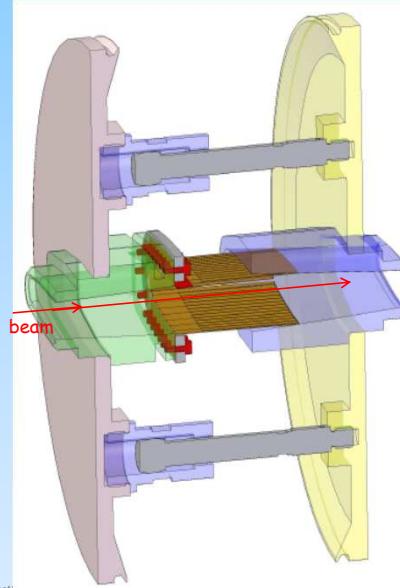
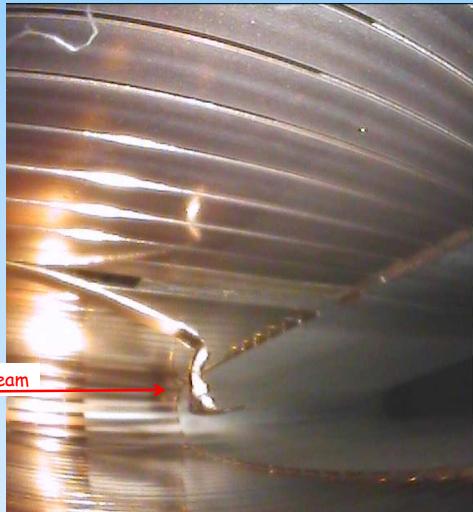








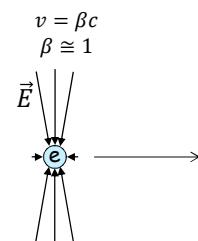
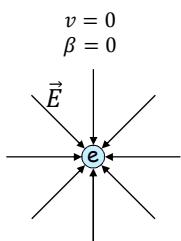
the problem was found: RF fingers



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electric field of a relativistic particle

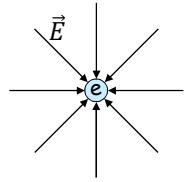


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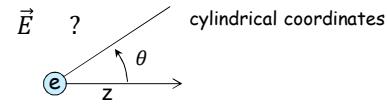


electric field of a relativistic particle

$$\begin{aligned}v &= 0 \\ \beta &= 0\end{aligned}$$



$$v = \beta c$$



$$\vec{E} = \frac{q}{4\pi\epsilon_0} \frac{(1 - \beta^2)}{(1 - \beta^2 \sin^2 \theta)^{3/2} r^2} \frac{\vec{r}}{r}$$

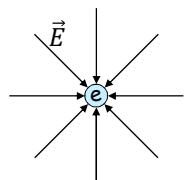
$$\gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

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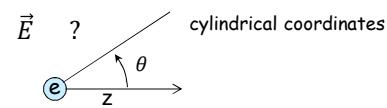


electric field of a relativistic particle

$$\begin{aligned}v &= 0 \\ \beta &= 0\end{aligned}$$



$$v = \beta c$$



$$\vec{E} = \frac{q}{4\pi\epsilon_0} \frac{1}{r^2} \frac{\vec{r}}{r}$$

$$\begin{aligned}\gamma &= 1 \\ \beta &= 0\end{aligned}$$

$$\vec{E} = \frac{q}{4\pi\epsilon_0} \frac{(1 - \beta^2)}{(1 - \beta^2 \sin^2 \theta)^{3/2} r^2} \frac{\vec{r}}{r}$$

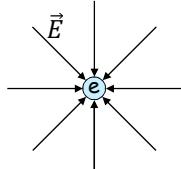
$$\gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

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electric field of a relativistic particle

$$v = 0 \\ \beta = 0$$



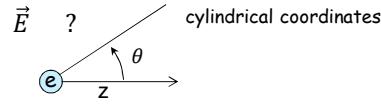
$$\vec{E} = \frac{q}{4\pi\epsilon_0} \frac{1}{r^2} \vec{r}$$

$$\gamma = 1 \\ \beta = 0$$

$$\vec{E} = \frac{q}{4\pi\epsilon_0} \frac{(1 - \beta^2)}{(1 - \beta^2 \sin^2 \theta)^{3/2} r^2} \frac{\vec{r}}{r}$$

$$\gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

$$v = \beta c$$



cylindrical coordinates

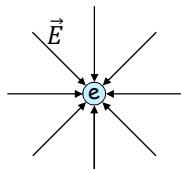
$$\left. \begin{aligned} E_z(\theta = 0) &= \frac{q}{4\pi\epsilon_0} \frac{1}{\gamma^2 r^2} \frac{\vec{r}}{r} \\ E_r(\theta = \frac{\pi}{2}) &= \frac{q}{4\pi\epsilon_0} \frac{\gamma}{r^2} \frac{\vec{r}}{r} \end{aligned} \right\}$$

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electric field of a relativistic particle

$$v = 0 \\ \beta = 0$$



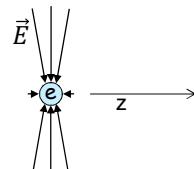
$$\vec{E} = \frac{q}{4\pi\epsilon_0} \frac{1}{r^2} \vec{r}$$

$$\gamma = 1 \\ \beta = 0$$

$$\vec{E} = \frac{q}{4\pi\epsilon_0} \frac{(1 - \beta^2)}{(1 - \beta^2 \sin^2 \theta)^{3/2} r^2} \frac{\vec{r}}{r}$$

$$\gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

$$v = \beta c \\ \beta \cong 1$$



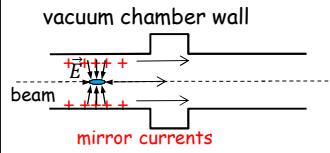
$$\gamma \gg 1 \\ \beta \cong 1$$

$$\left. \begin{aligned} E_z(\theta = 0) &= \frac{q}{4\pi\epsilon_0} \frac{1}{\gamma^2 r^2} \frac{\vec{r}}{r} \\ E_r(\theta = \frac{\pi}{2}) &= \frac{q}{4\pi\epsilon_0} \frac{\gamma}{r^2} \frac{\vec{r}}{r} \end{aligned} \right\} \begin{array}{l} \xrightarrow{\gamma \rightarrow \infty} 0 \\ \xrightarrow{\gamma \rightarrow \infty} \infty \end{array}$$

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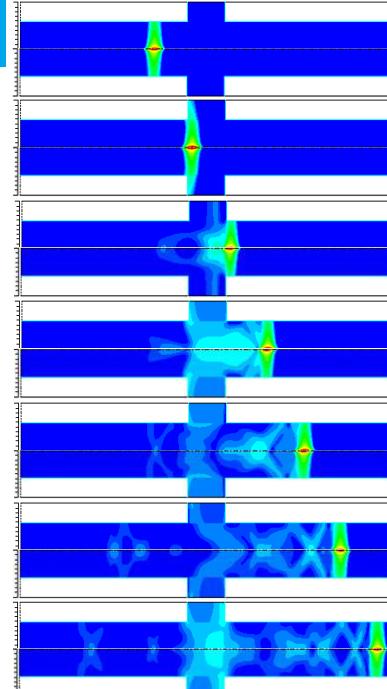
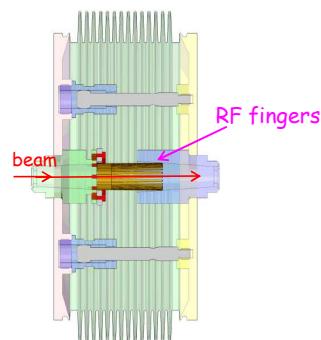
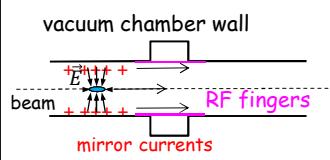
RF fingers and wakefields



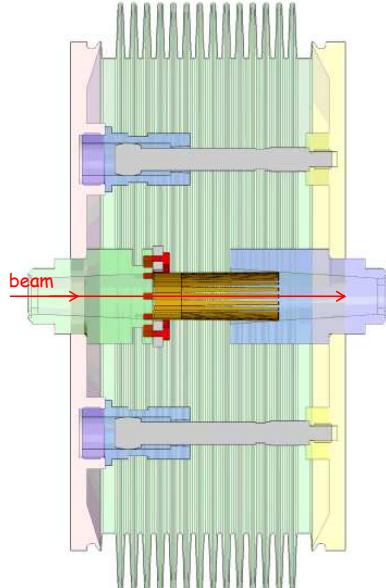
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RF fingers and wakefields



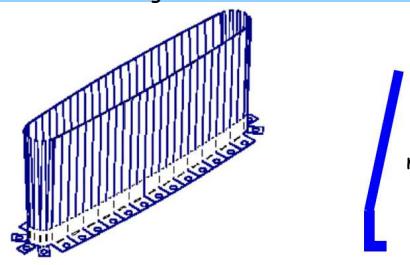
RF fingers and wakefields



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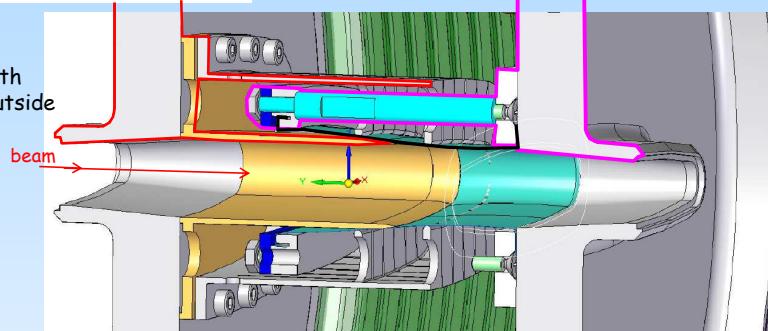
RF fingers: improvements done

old RF fingers were tilted outwards by 2 degrees



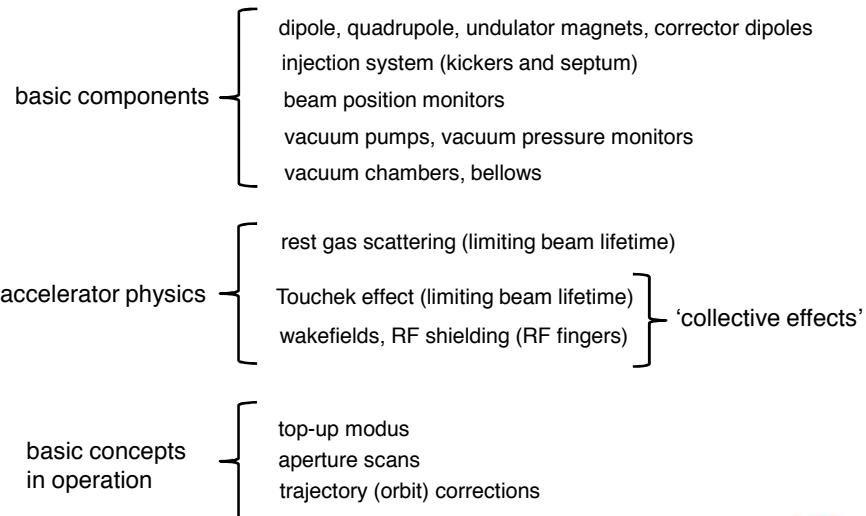
new RF fingers have stronger tilt, more tension

new design with
RF fingers outside



Summing-up of this part

Circular accelerators: the synchrotron



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Thank you for your attention

pedro.castro@desy.de

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