BLG335E Analysis of Algorithms I, Fall 2023 Project 3

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Implementation

You are going to implement Binary Search Tree (BST) and Red-Black Tree (RBT) algorithm with the following functionalities. You are going to store population data of cities in the trees. Keep in mind that you may need more functions (i.e. helper functions) than specified in skeleton code.

Hint: Since most of the functions are similar, after implementing one of the algorithms, you may slightly change the structure to implement the other one.

Tree Structure

Node structure is already given in skeleton codes. You should not delete that structure and implement on your own. You should set the color attribute of the struct as **0** for "black" nodes and **1** for "red" nodes. Otherwise, your code may get an error during the evaluation of color rules in main function

TREE-INSERT [20 pts]

After you managed to create a structure for nodes and trees, you need to implement "insertion" function. Beware that the insertion procedure differs in *RBT* to preserve the *RBT* rules along with *BST* property (*left subtree values are smaller than the parent*, *right subtree values are greater than the parent*). You may need additional helper function to fix the tree structure after insertion in red-black trees. This function can be void.

Important Note: If you encounter the same population value during comparison in insertion procedure, you should insert the node in the right subtree. So, the new inserted node should be treated as the successor of the compared node (e.g. to-be-inserted node (z), with value 20, one of the tree's nodes (x) with value 20, z should be placed in a relevant location in the right subtree of the z as its successor. Hint: This applies for before fix-up in RBTrees, after fixing the tree, z's location might be changed in the tree regarding different cases to preserve RBT rules (e.g. z might become x's parent after fixup calls.).

TREE-DELETE [20 pts]

This function is used to delete a given node from the tree. Even though deletion procedure is similar in BST and RBT, deletion procedure in RBT is slightly different to ensure that tree

structure meets the *RBT* rules. You may need additional helper function to fix the tree structure after deletion in red-black trees. This function can be void.

TREE-SEARCH [10 pts]

The searching procedure is same in *RBT* and *BST*. Aim is to retrieve the node with specified value. This function should return a pointer to the Node structure.

Sorting - Walking Functions [10 pts]

Using the tree, a function should return the ordered list in ascending order. You should implement the walking functions.

Other fundamental operations [10 pts]

Implement simple operations that are called **from the main function** such as finding **minimum, maximum, successor and predecessor.** These functions should return a pointer to the Node structure.

Deliverables

Code Structure [70 pts]

- 1. **redblacktree.cpp** and **bst.cpp** should be submitted. Skeleton code gives you the idea of which functions should be implemented. You may need helper functions, if so, please implement such functions. **Do not change the names** of the given functions.
- 2. Those cpp files should work seamlessly with the main function.
- 3. Your code should produce log.txt, rb_out.csv and bst_out.csv. The generation of these files should be done automatically when code is executed, so do not send these files. Expected outputs are given in Ninova, ensure that your code's output is same. Beware that selected cities in the main.cpp can be changed while evaluating the solutions.
 - a. rb_out.csv should contain the population data along with cities in ascending (increasing) order for RBT, while bst_out.csv should contain data for BST.

Log Structure:

```
RBT:
Height: 24 // height of the red-black tree
Nodes: 13807 // total number of nodes in red-black tree
Min: Agdam // get city name with minimum population in red-black tree
Max: Tokyo // get city name with maximum population in red-black tree
BST:
Height: 12204 // height of the binary search tree
Nodes: 13807 // total number of nodes in binary search tree
Min: Agdam // get city name with minimum population in binary search tree
Max: Tokyo // get city name with maximum population in binary search tree
```

```
Searching for Paris(B) with population 9904000 // City Name is given with color as B if color is black, and R if color is red RBT:

P(B):Guangzhou;L(B):Lagos;R(B):Moscow;S:Istanbul;Pr:Seoul // P: parent, L: left child, R: right child, S: successor, Pr: predecessor of searched city (Paris in this case)

BST:

P:Istanbul;L:Seoul;S:Istanbul;Pr:Seoul // there is no color information as this is the binary search tree

Deleting a city with population 9904000 // deletion operation

RBT nodes: 13806 // number of nodes is decreased by one

BST nodes: 13806 // number of nodes is decreased by one
```

Running the code:

```
g++ main.cpp -o main
./main <DATASET_FILE_NAME>.csv out.csv v
```

Debugging:

To debug; you may modify .vscode/launch.json to change the runtime arguments in "args". Then start debugging with "F5" which starts the debugging with specified arguments.

Report Structure [30 pts]

Answer the following questions in your report with using your own words.

- 1. What are the **differences** between binary search trees and red-black trees? How the set of the red-black tree rules **change the structure** of the tree? What are the apparent **advantages** of those set of **rules**? Discuss it with the **logged height of the resulting RBTree and BSTree under different versions of population data. How different versions of data affected the height? Why?**
- 2. What is the maximum height of the RBTree with n nodes? Prove.
- 3. Write **big-o complexity for each operation** (searching, walking...) of RBTree and BSTree that you have implemented. Explain the reason behind the complexities in worst-case scenarios.

Guidelines

- 1. Copying from various sources (blogs, books, friends) will be considered as plagiarism. Avoid using co-pilot softwares to not end up in high similarity rate with others. You may use pseudocodes given in class resources (slides, reference book...) to <u>understand</u> and <u>implement</u> the algorithms.
- 2. Please **do not publish your solution through online code-sharing platforms** like GitHub before the deadline.
- 3. You can not use any built-in algorithms. The assignment can be solved without any third party libraries.
- 4. If your code cannot be executed in Docker environment, there will be a high penalty. Please work within the Docker environment.
- 5. Your code should be readable with supporting comments.

- 6. **Do not change any code within the main.cpp**. Main function is prepared to ensure Code evaluation will be supported with output matching, so your outputs should match with expected output **character by character**.
- 7. Your code should work as expected when selected cities in main.cpp differs.