

Q1: List Equality

a. (2 marks) $[W, X, Y \mid Z]$ and $[1, 2, 3, 4, 5 \mid [6, 7, X]]$

L.H.S

R.H.S

$$\Rightarrow [W, X, Y \mid Z] = [1, 2, 3, 4, 5, 6, 7, X]$$

$$W = 1$$

$$X = 2$$

$$Y = 3$$

$$Z = [4, 5, 6, 7, 2]$$

match

b. (2 marks) $[p \mid [q \mid [r \mid [s \mid [t \mid [V]]]]]]$ and $[X, Y \mid Z]$.

LHS

RHS

$$[p \mid [q \mid [r \mid [s \mid [t \mid [V]]]]]] = [X, Y \mid Z]$$

$$[p, q, r, s, t, V] = [X, Y \mid Z]$$

$$X = p$$

$$Y = q$$

$$Z = [r, s, t, V]$$

$$V = V$$

match

c. (2 marks) $[[Z \mid [x, y]], e, f, g]$ and $[[a, [x, y]] \mid V]$

$$\Rightarrow [[Z \mid [x, y]], e, f, g] \neq [[a, [x, y]] \mid V]$$

$$[[Z, x, y], e, f, g] \neq [[a, [x, y]] \mid V]$$

$$[Z, x, y] \neq [a, [x, y]]$$

Not a match because the first element on LHS contains a list with 3 elements whereas on RHS, the first element contains 2 elements, hence cannot equal LHS.

d. (2 marks) $[[a], B, C \mid D]$ and $[[a \mid [B]] \mid [C \mid D]]$

LHS

RHS

$$[[a], B, C \mid D] \neq [a, [B], C \mid D]$$

$$[a] \neq a$$

$$B \neq [B]$$

Part d Explanation: Not a match because the first element in LHS is a list containing "a" whereas in RHS, it's a single element. Second element in LHS is a variable whereas in RHS, it's a list containing a singleton variable.

e. (3 marks) $[minus \mid [Y, X \mid [minus, Y \mid [X]]]]$ and $[X, plus, minus \mid [X, Y, minus]]$

$$[minus, Y, X, minus, Y, X] = [X, plus, minus, X, Y, minus]$$

$$\begin{aligned} X &= minus \\ Y &= plus \end{aligned}$$

match

f. (3 marks) $[bike \mid A]$ and $[C \mid [C \mid [C \mid [C \mid [C]]]]]$

$$[bike \mid A] = [C, C, C, C, C]$$

$$\begin{aligned} C &= bike \\ A &= [bike, bike, bike, bike] \end{aligned}$$

match

g. (3 marks) $[a, b \mid [C \mid [D, E \mid C]]]$ and $[F \mid [G, H, [], [D]]]$

$$[a, b, C, D, E \mid C] = [F, G, H, [], [D]]$$

$$\begin{aligned} F &= a \\ G &= b \\ H &= [] \\ D &= [] \\ E &= [[]] \\ C &= [] \end{aligned}$$

match

h. (3 marks) $[Fox, [[in], socks], [on], box, on \mid [[knox]]]$ and $[[The, cat], [[in], The], Hat \mid [Comes \mid Back]]$

$$[Fox, [in], socks, on, box, on, [knox]] = [The, cat, in, The, Hat, Comes, Back]$$

$$\begin{aligned} Fox &= [The, cat] \\ Fox &= [socks, cat] \\ [in], socks &= [in], The \\ The &= socks \\ Hat &= [on] \\ Comes &= box \\ Back &= [on, [knox]] \end{aligned}$$

match