



Data Structures and Algorithms Design

BITS Pilani

Hyderabad Campus



CONTACT SESSION 6-PLAN

Contact Sessions(#)	List of Topic Title	Text/Ref Book/external resource
6	Graphs - Terms and Definitions, Properties, Representations (Edge List, Adjacency list, Adjacency Matrix), Graph Traversals (Depth First and Breadth First Search)	T1: 6.1, 6.2, 6.3

Depth-First Search

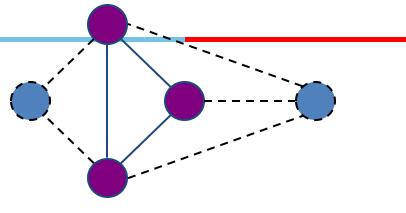
- Definitions
 - Subgraph
 - Connectivity
 - Spanning trees and forests
- Depth-first search
 - Algorithm
 - Example
 - Properties
 - Analysis
- Applications of DFS
 - Cycle finding
 - Path finding

SUBGRAPHS

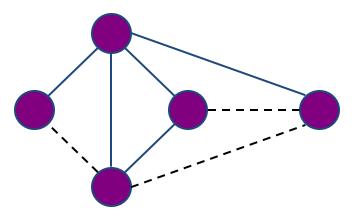
- Subgraphs
- A subgraph S of a graph G is a graph such that
 - The vertices of S are a subset of the vertices of G
 - The edges of S are a subset of the edges of G
- A spanning subgraph of G is a subgraph that contains all the vertices of G



SUBGRAPHS



Subgraph

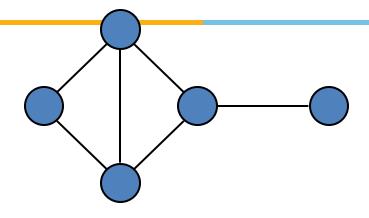


Spanning subgraph

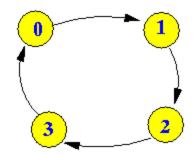
Connectivity

- A graph is **connected** if there is a path between every pair of vertices
- A connected component of a graph G is a maximal connected subgraph of G
- A directed graph G is **strongly connected** if:
 - For any two vertices u and v:
 - There is a directed path $u \rightarrow v$, and
 - There is a directed path $v \rightarrow u$

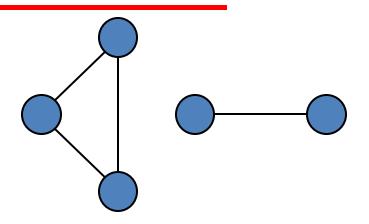
Connected graph



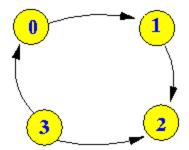
Connected graph



Strongly Connected



Non connected graph with two connected components

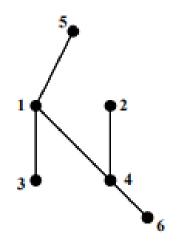


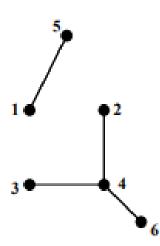
Not Strongly Connected



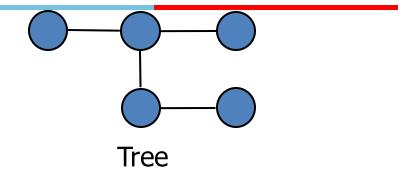
Trees and Forests

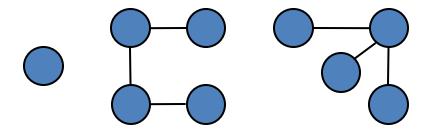
- A tree is a connected graph with no cycles.
- A forest is a graph with each connected component a tree





Trees and Forests





Forest

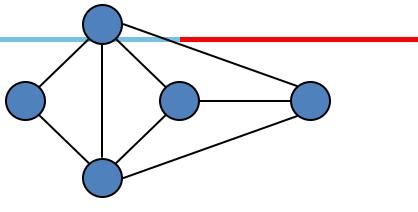


Spanning Trees

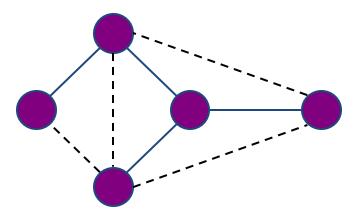
- A spanning tree of a connected graph is a spanning subgraph that is a tree:
- which includes all of the vertices of *G*, with minimum possible number of edges

Spanning Tree





Graph



Spanning tree



Subgraphs, trees-Example

- Perhaps the most talked about graph today is the Internet, which can be viewed as a graph whose vertices are computers and whose (undirected) edges are communication connections between pairs of computers on the Internet.
- The computers and the connections between them in a single domain, like http://www.bits-pilani.ac.in/, form a subgraph of the Internet. If this subgraph is connected, then two users on computers in this domain can send e-mail to one another without having their information packets ever leave their domain.
- Suppose the edges of this subgraph form a spanning tree. This implies that, even if a single connection goes down (for example, because someone pulls a communication cable out of the back of a computer in this domain), then this subgraph will no longer be connected.

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THANK YOU!

BITS Pilani

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