

# Introduction to LLRFLibsPy Library

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# Outline

- Motivation
- LLRFLibsPy Overview
- Library Functions
  - RF Simulation
  - RF Control
  - RF Detection and Actuation
  - RF Noise Analysis
  - RF Calibration
  - RF System Identification
  - Other functions
- Status and Outlook

# Motivation

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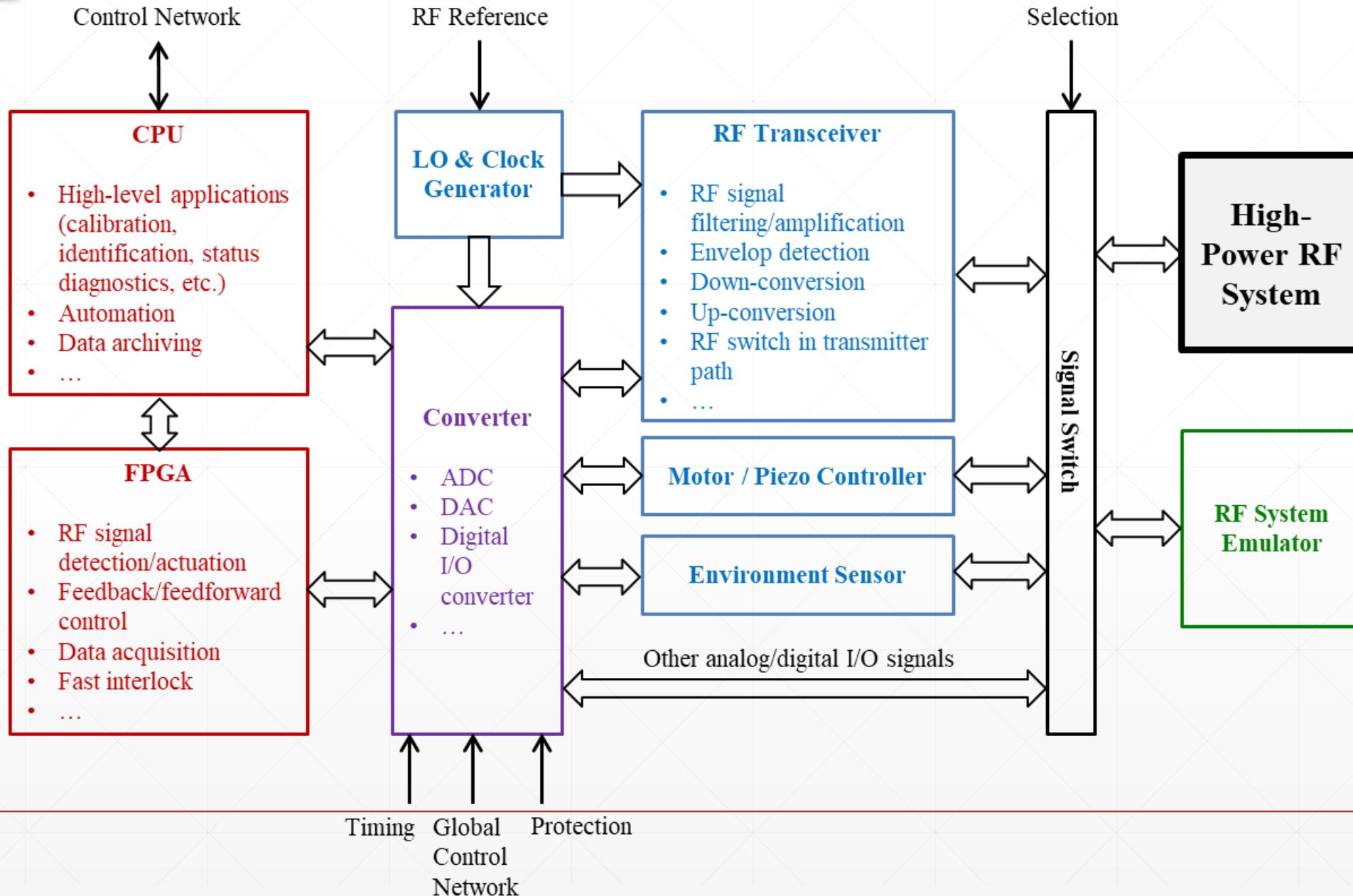


# State-of-the-art LLRF System R&D Topics

- **Push RF field control performance to extreme** (e.g., very-low-noise RF signal detector, ultra-large control bandwidth with minimum loop delay, high-frequency synthesizer with fast DACs, enhanced RF-mechanical control strategies, etc.)
- **Apply advanced control algorithms** (e.g., optimal control, robust control, disturbance-observer-based control, adaptive feedback/feedforward, etc.)
- **Improve the automation level and intelligence** (e.g., large-scale state machine, optimization of RF system operation with machine learning surrogate models, smart exception detection and handling, etc.)
- **RF control strategy for new scenarios** (e.g., multiple-harmonic beam-loading control in wide-band cavities, etc.)
- **Standardization** (e.g., standard hardware like MicroTCA or cPCI-serial, firmware libraries, software libraries, etc.)



# Functional Architecture of a LLRF System

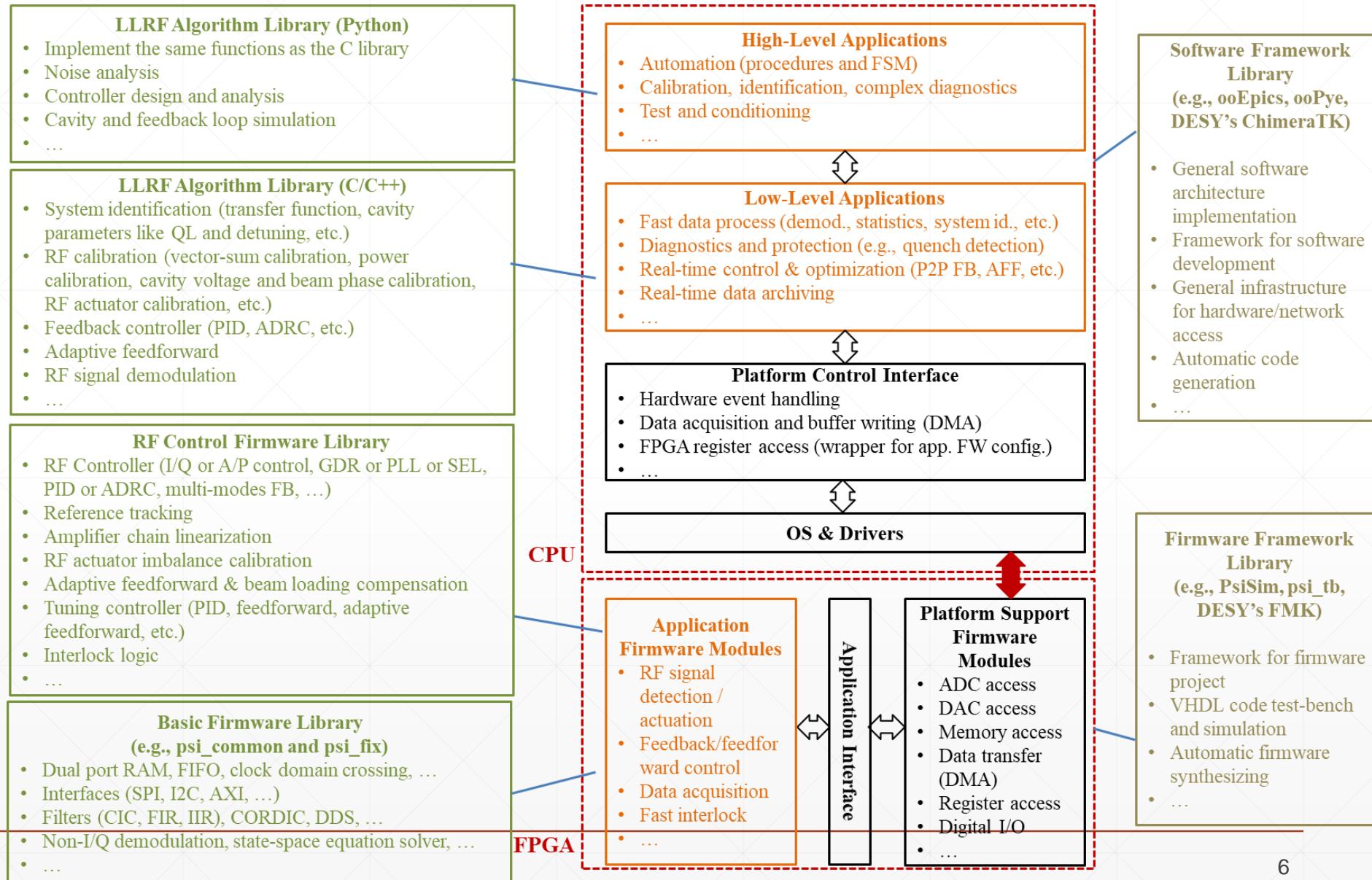




# Functional Architecture of LLRF Firmware & Software

## Firmware Libraries

- **Firmware Framework Library**
  - Construct the firmware project structure
  - Simulate the firmware code
  - Automate the firmware synthesize
  - Access common components (e.g., ADC, DAC, etc.)
- **Basic Firmware Library**
  - Collect firmware build components common for different applications
- **RF Control Firmware Library**
  - Implement high-level LLRF control modules
  - Can be assembled and configured for fast prototyping of LLRF controllers





# Functional Architecture of LLRF Firmware & Software (cont.)

## Software Libraries

### ▪ Software Framework Library

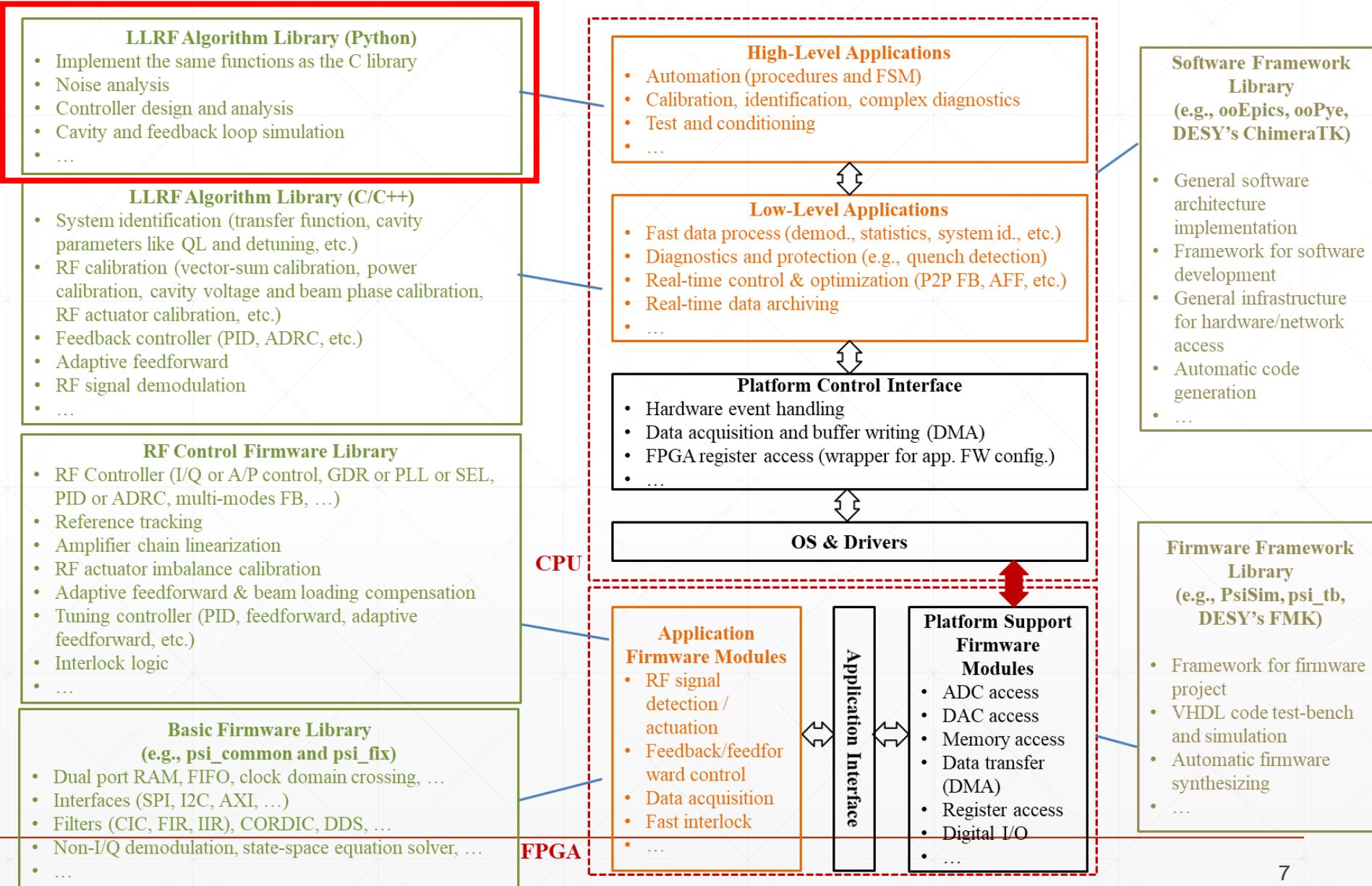
- Define a common software architecture
- Implement infrastructures for multi-threading, hardware access, and network access

### ▪ LLRF Algorithm Library (C/C++)

- Implement RF control domain algorithms
- Support soft-real-time applications

### ▪ LLRF Algorithm Library (Python)

- Implement same algorithms as the C/C++ library
- Also implement features like noise analysis, feedback controller design, and system simulation
- For high-level applications and automation



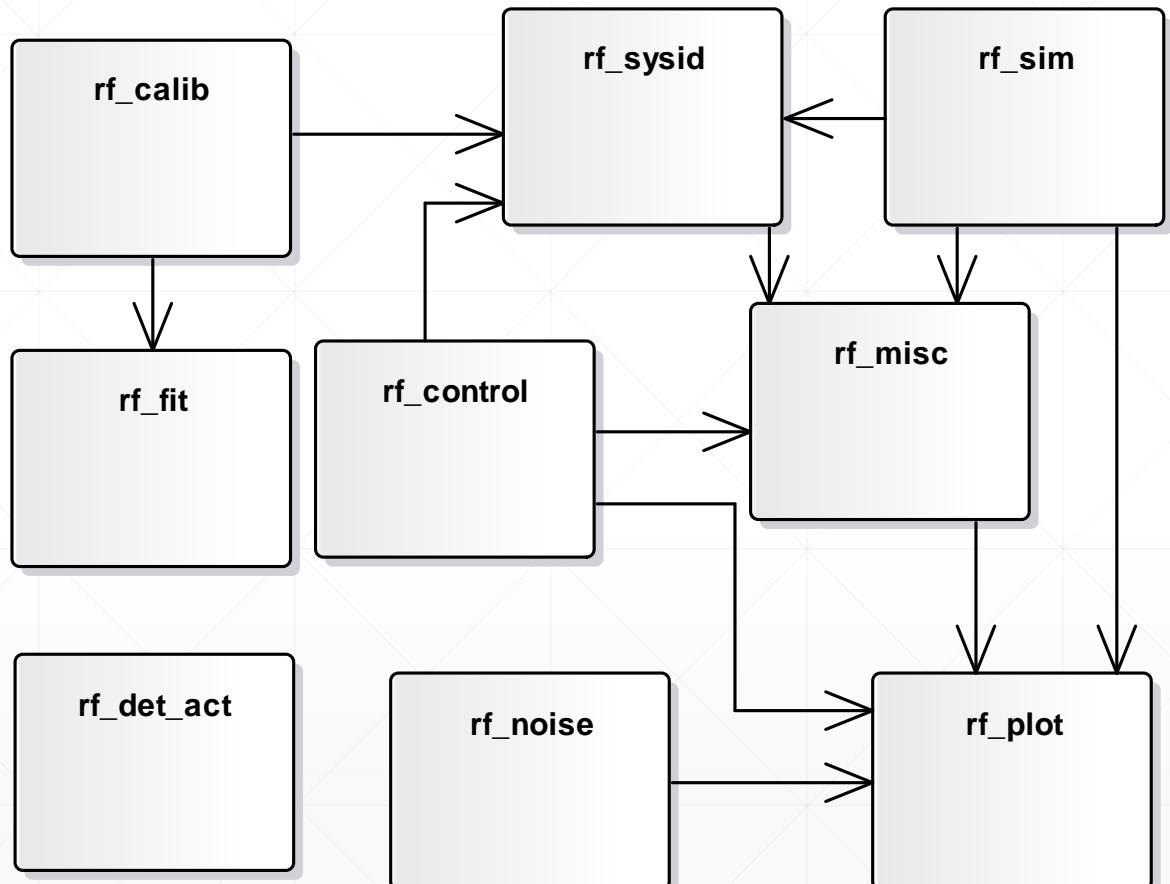
# **LLRFLibsPy Overview**

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# Contents of LLRFLibsPy

class System



Python modules in LLRFLibsPy

| Name          | Date modified    | Type        | Size  |
|---------------|------------------|-------------|-------|
| doc           | 08.09.2023 15:18 | File folder |       |
| example       | 01.09.2023 14:23 | File folder |       |
| test          | 31.08.2023 17:09 | File folder |       |
| Makefile      | 16.08.2023 17:37 | File        | 1 KB  |
| README.md     | 08.09.2023 09:21 | MD File     | 13 KB |
| rf_calib.py   | 21.08.2023 14:25 | Python File | 23 KB |
| rf_control.py | 18.08.2023 11:09 | Python File | 29 KB |
| rf_det_act.py | 18.08.2023 11:31 | Python File | 11 KB |
| rf_fit.py     | 18.08.2023 13:43 | Python File | 7 KB  |
| rf_misc.py    | 21.08.2023 14:25 | Python File | 8 KB  |
| rf_noise.py   | 30.08.2023 15:37 | Python File | 20 KB |
| rf_plot.py    | 21.08.2023 14:23 | Python File | 8 KB  |
| rf_sim.py     | 21.08.2023 10:43 | Python File | 19 KB |
| rf_ssid.py    | 21.08.2023 14:25 | Python File | 26 KB |



# Contents of LLRFLibsPy (cont.)

## Description of Modules

|                   |   |
|-------------------|---|
| <b>rf_sim</b>     | Simulate the cavity response; determine the operation parameters  |
| <b>rf_control</b> | Design and analyze RF feedback/feedforward controllers  |
| <b>rf_det_act</b> | Measure RF amplitude and phase from ADC samples   |
| <b>rf_noise</b>   | Noise analysis, generation, and filtering   |
| <b>rf_calib</b>   | RF calibrations like virtual probe, RF actuator offset/imbalance, forward and reflected, and power calibrations |
| <b>rf_sysid</b>   | Identify the system transfer function and characteristic parameters (e.g., cavity QL and detuning)              |
| <b>rf_fit</b>     | Fit data to sine/cosine, circle, ellipse or Gaussian functions  |
| <b>rf_misc</b>    | Misc. functions like saving data to files and reading data from files   |
| <b>rf_plot</b>    | Plot functions for internal usage   |

Note: the library relies on “numpy” and “scipy”, “matplotlib” is also loaded if any plot function is enabled.

# Library Functions

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# RF Simulation

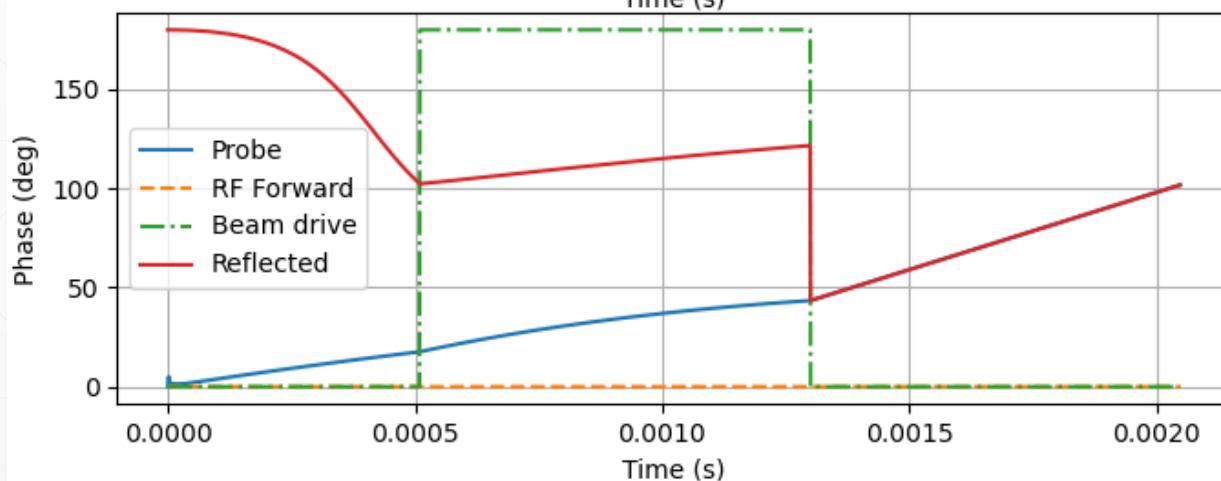
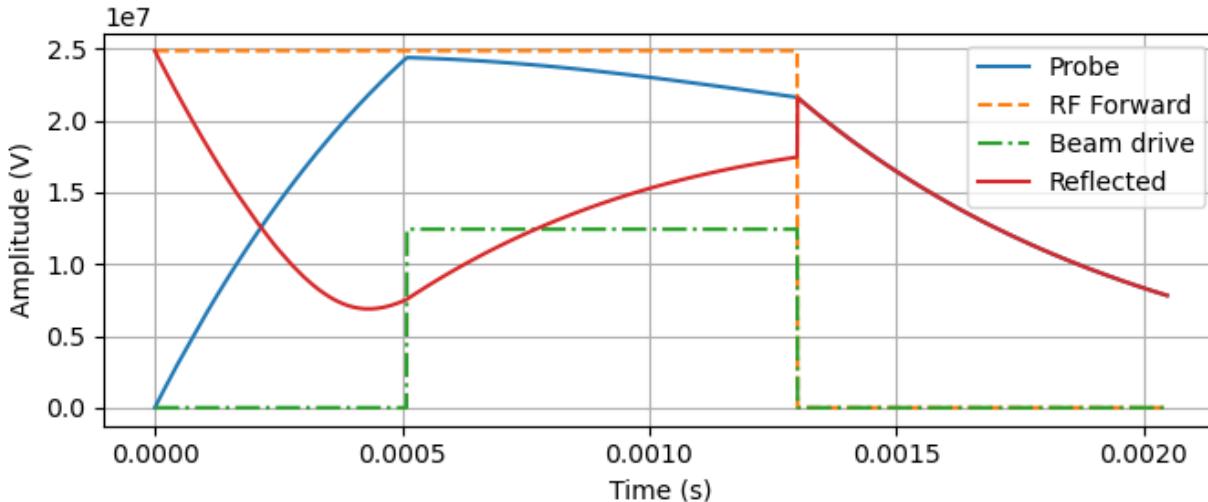
| Function                          | Example   | Comments  |
|-----------------------------------|---|---|
| <code>cav_ss</code>               | <code>example_sim_cavity_basic.py</code>                                | Derive a continuous state-space equation of a cavity  |
| <code>cav_ss_mech</code>          |   | Cavity state-space equation with mechanical modes<br>(to be implemented)  |
| <code>cav_impulse</code>          | <code>example_aff_ilc.py</code>   | Derive the cavity impulse response from the cavity parameters   |
| <code>sim_ncav_pulse</code>       | <code>example_sim_cavity_basic.py</code>                                | Simulate cavity (with constant QL and detuning) response to a pulsed input  |
| <code>sim_ncav_step</code>        | <code>example_sim_cavity_basic.py</code>                                | Simulate cavity (with constant QL and detuning) response for a time step  |
| <code>sim_ncav_step_simple</code> | <code>example_sim_cavity_basic.py</code>                                | Simulate cavity (with constant QL and detuning) response for a time step (simplified cavity equation only with the fundamental passband mode) |
| <code>rf_power_req</code>         | <code>example_power_req.py</code><br><code>example_power_req2.py</code> | Calculate the required RF power for desired cavity voltage and beam current   |
| <code>opt_QL_detuning</code>      | <code>example_power_req.py</code><br><code>example_power_req2.py</code> | Calculate the optimal QL and detuning for minimizing the reflection power   |



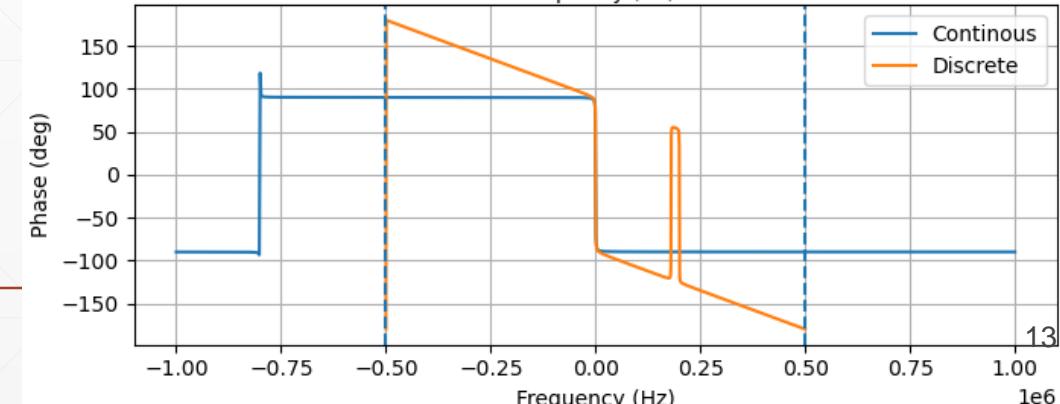
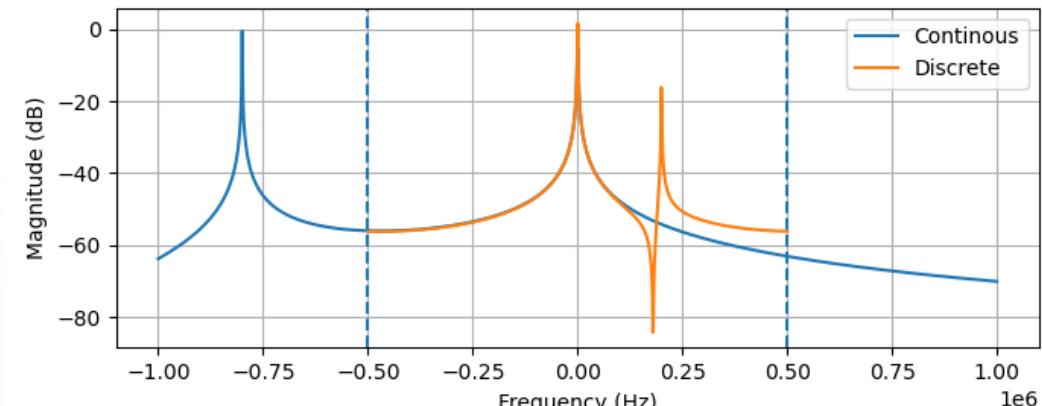
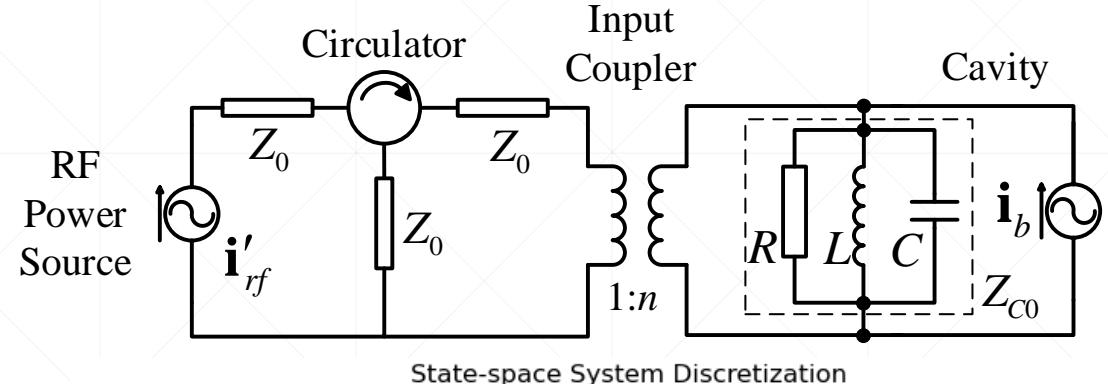
# RF Simulation (cont.)

$$\begin{bmatrix} \dot{v}_{CI} \\ \dot{v}_{CQ} \end{bmatrix} = \begin{bmatrix} -\omega_{1/2} & -\Delta\omega \\ \Delta\omega & -\omega_{1/2} \end{bmatrix} \begin{bmatrix} v_{CI} \\ v_{CQ} \end{bmatrix} + \omega_{1/2} R_L \begin{bmatrix} i_{CI} \\ i_{CQ} \end{bmatrix}$$

Cavity Response Simulated with Continuous State-space Model



`example_sim_cavity_basic.py`

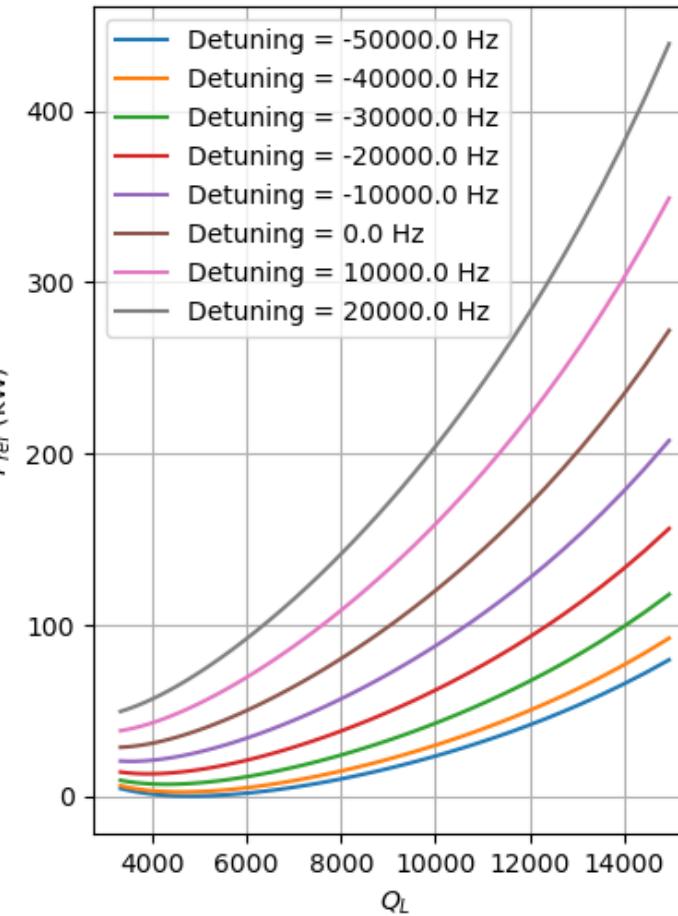
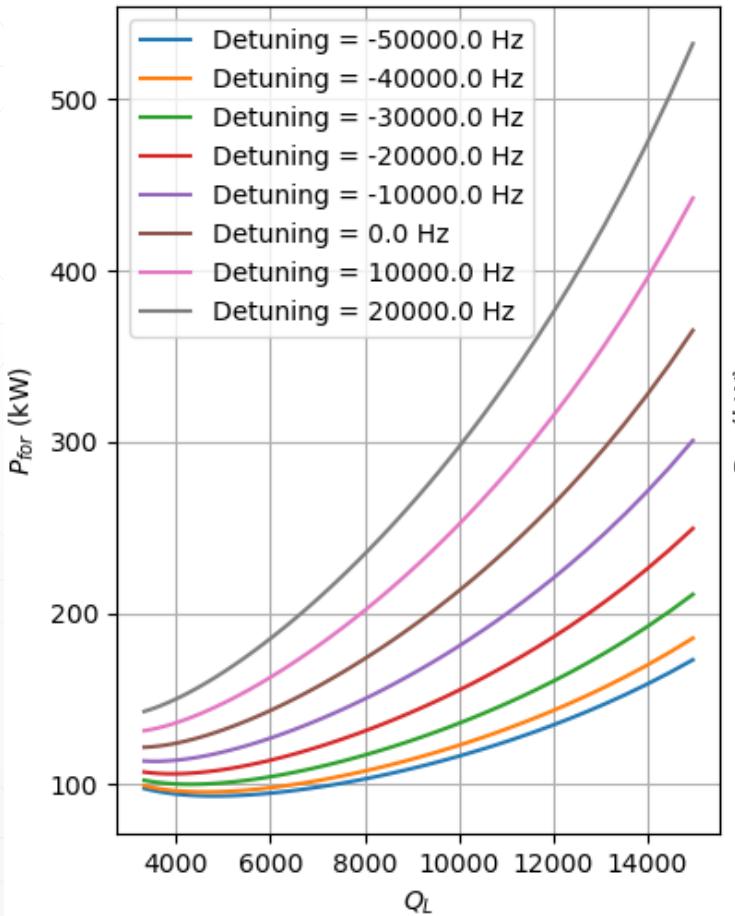




# RF Simulation (cont.)

$$P_{for} = \frac{\beta+1}{\beta} \frac{v_{c0}^2}{8R_L} \left[ \left( 1 + \frac{2R_L i_{b0} \cos \varphi_b}{v_{c0}} \right)^2 + \left( \tan \psi + \frac{2R_L i_{b0} \sin \varphi_b}{v_{c0}} \right)^2 \right]$$

$$P_{ref} = \frac{\beta+1}{\beta} \frac{v_{c0}^2}{8R_L} \left[ \left( \frac{\beta-1}{\beta+1} - \frac{2R_L i_{b0} \cos \varphi_b}{v_{c0}} \right)^2 + \left( \tan \psi + \frac{2R_L i_{b0} \sin \varphi_b}{v_{c0}} \right)^2 \right]$$



example\_power\_req2.py

Required RF power for a cavity with following parameters:

- Cavity resonance frequency: **499.5935 MHz**
- Cavity voltage: **0.35 MV**
- Beam average current: **0.4 A**
- Beam sync. phase (ring convention): **147.6 deg**
- Cavity Q0: **29909**
- $r/Q = 3.4/Q0 \text{ M}\Omega$

Optimal beta = 5.17, QL = 4848, detuning = -54775 Hz

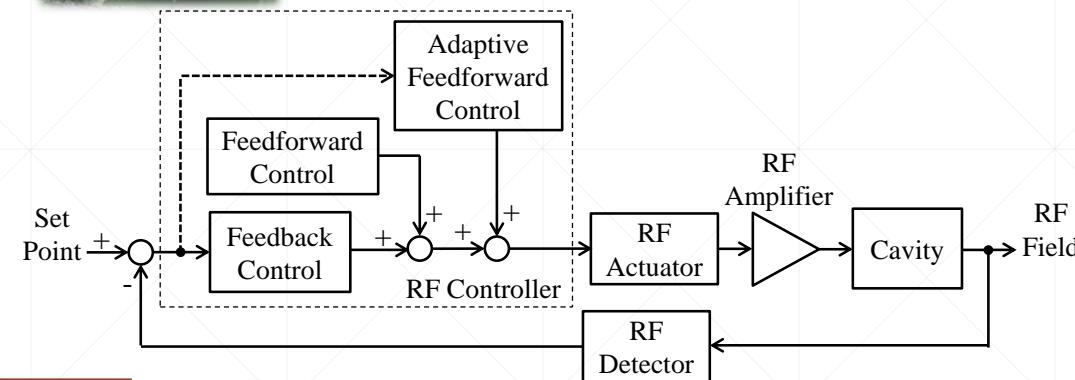


# RF Control

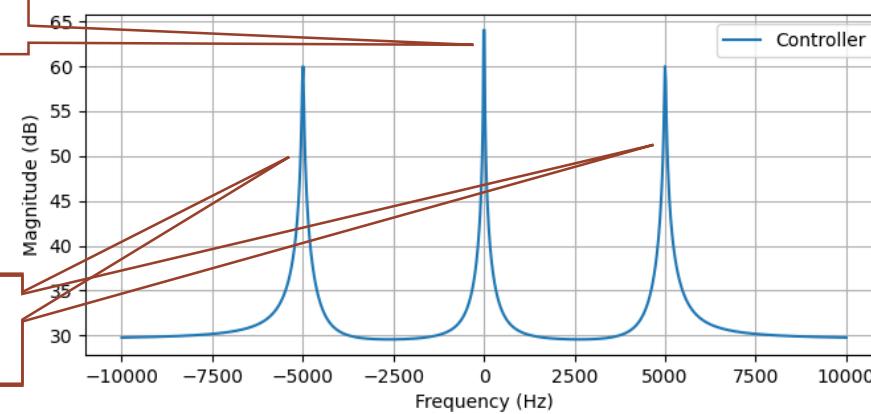
| Function                         | Example                                   | Comments  |
|----------------------------------|---|---|
| <code>ss_discrete</code>         | <code>example_sim_cavity_basic.py</code>  | Discretize a continuous state-space system and compare the frequency responses            |
| <code>ss.Cascade</code>          | <code>example_feedback_analysis.py</code> | Cascade two state-space systems (either continuous or discrete - C/D)                     |
| <code>ss.freqresp</code>         | <code>example_feedback_analysis.py</code> | Calculate and plot the frequency response of a state-space system (C/D)                   |
| <code>basic_rf_controller</code> | <code>example_feedback_basic.py</code>    | Derive a basic continuous RF I/Q controller: P + I + frequency notches                    |
| <code>control_step</code>        | <code>example_feedback_basic.py</code>    | Perform one time-step execution of the discretized controller                             |
| <code>loop_analysis</code>       | <code>example_feedback_analysis.py</code> | Analyze the sensitivity/complementary sensitivity of an RF control loop (C/D)             |
| <code>cav_sp_ff</code>           | <code>example_sp_ff.py</code>             | Derive the setpoint and feedforward waveforms for desired cavity voltage and beam loading |
| <code>ADRC_controller</code>     | <code>example_feedback_adrc.py</code>     | Derive a basic ADRC controller (the observer and gain)                                    |
| <code>ADRC_control_step</code>   | <code>example_feedback_adrc.py</code>     | Perform one time-step execution of the discretized controller including the ADRC observer |
| <code>AFF_timerev_lpf</code>     | <code>example_aff_timerev_lpf.py</code>   | Time-reversed low pass filter-based adaptive feedforward                                  |
| <code>AFF_ilc_design</code>      | <code>example_aff_ilc.py</code>           | Derive the ILC gain matrix from the impulse response and weighting matrices               |
| <code>AFF_ilc</code>             | <code>example_aff_ilc.py</code>           | Apply the ILC algorithm to calculate the feedforward correction signal                    |
| <code>resp_inv_svd</code>        | <code>example_resp_matrix_inv.py</code>   | Response matrix inversion with SVD (with singular value filtering)                        |
| <code>resp_inv_lsm</code>        | <code>example_resp_matrix_inv.py</code>   | Response matrix inversion with least-square method (with regularization)                  |



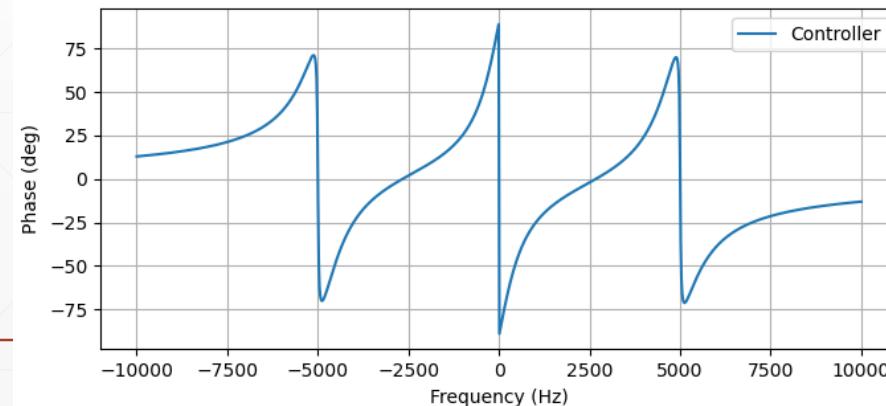
# RF Control (cont.)



**PI Control**



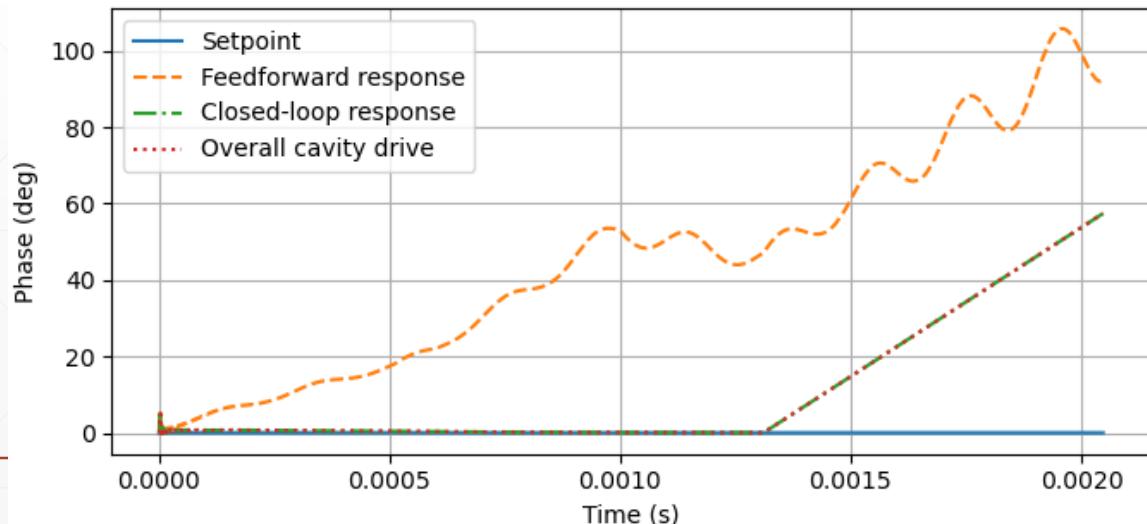
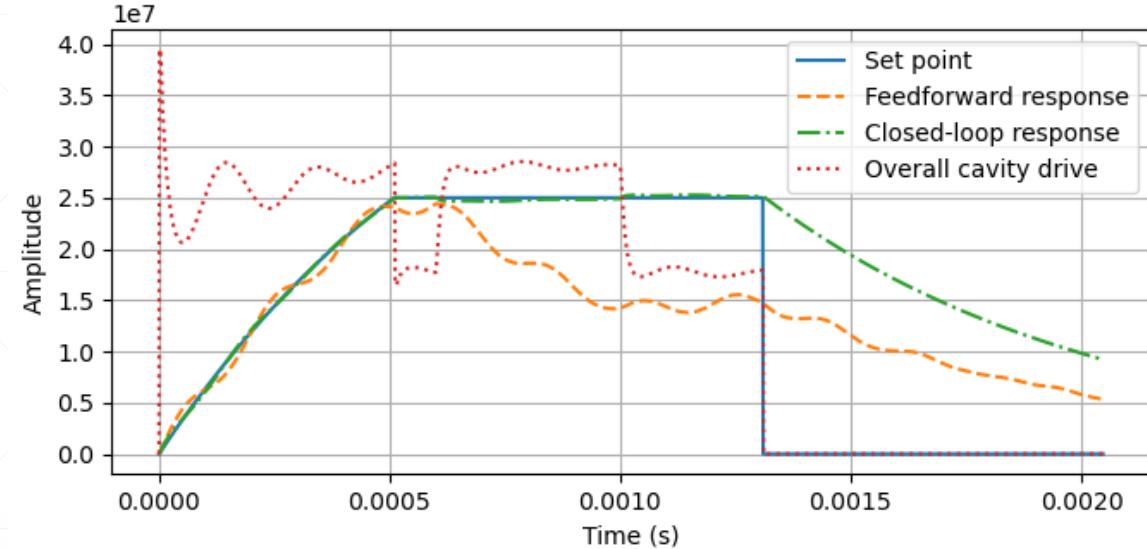
**Notch filter**



Basic RF Controller frequency response

example\_feedback\_basic.py

$$K(\hat{s}) = K_P + \frac{K_I}{\hat{s}} + \sum_{i=1}^n \frac{g_i \omega_{1/2,i}}{\hat{s} + \omega_{1/2,i} - j\omega_{notch,i}} + \sum_{i=1}^n \frac{g_i \omega_{1/2,i}}{\hat{s} + \omega_{1/2,i} + j\omega_{notch,i}}$$



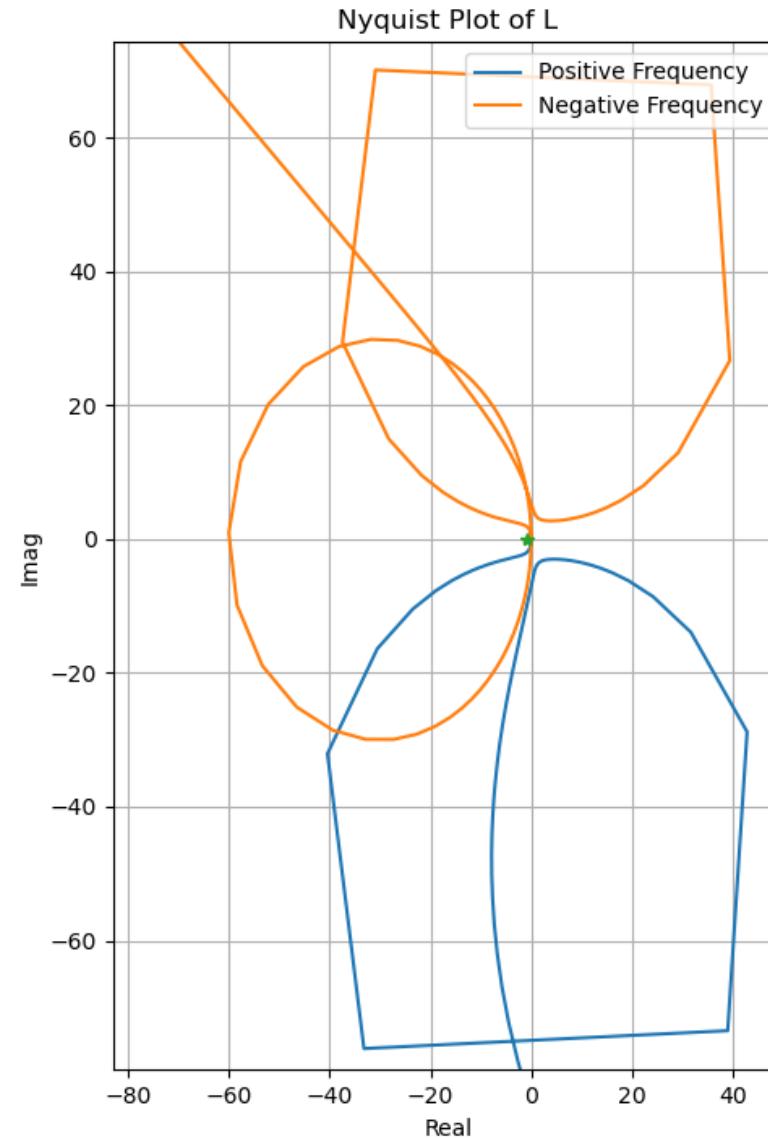
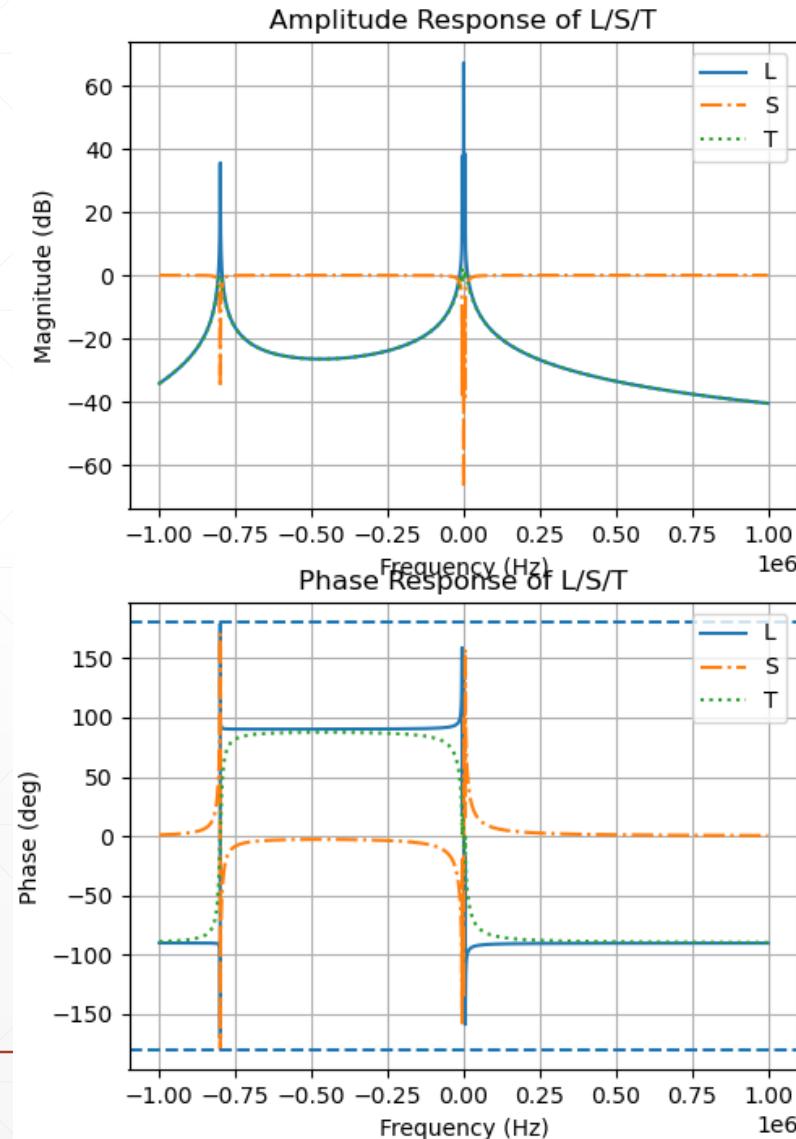
Cavity response with feedforward or/and feedback



# RF Control (cont.)

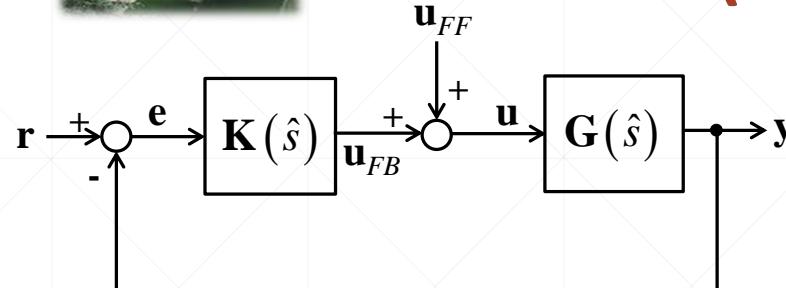
Feedback Loop Analysis Continuous without Notch Filter

example\_feedback\_analysis.py

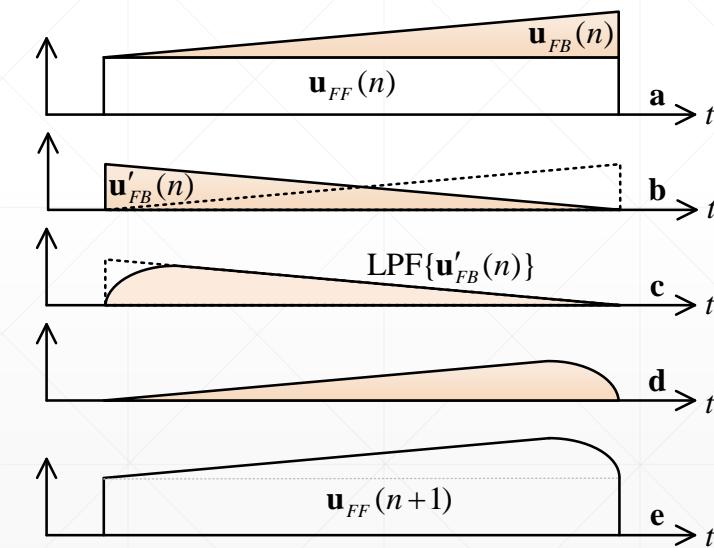




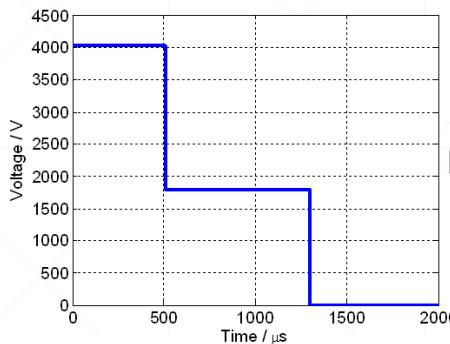
# RF Control (cont.)



Adapt feedforward with feedback on

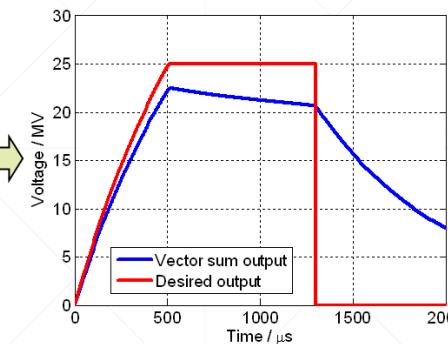


Adaptive feedforward with time-reversed low-pass filter

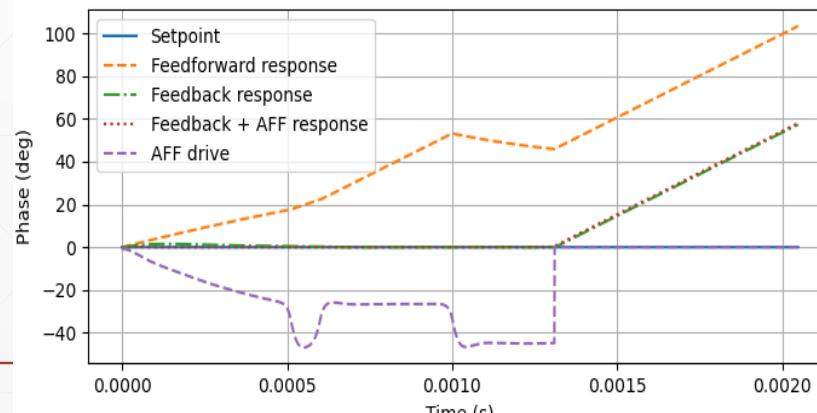
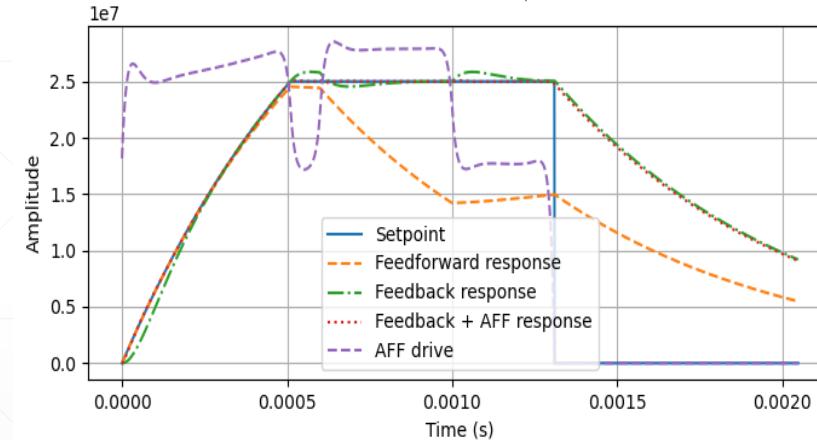


RF System

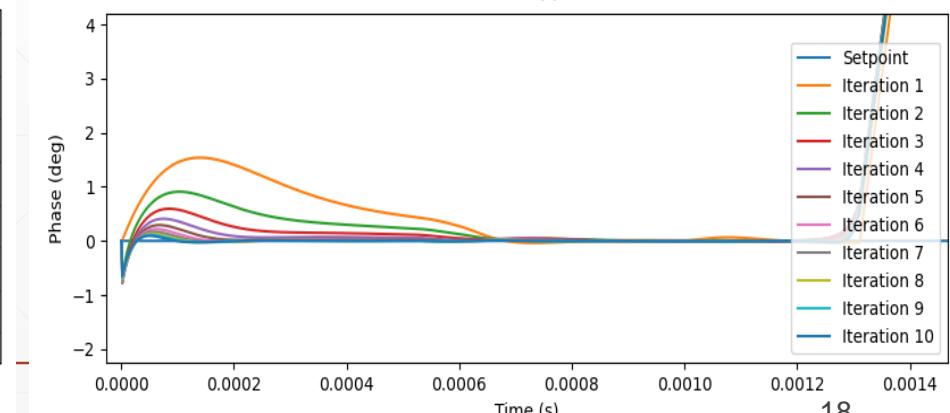
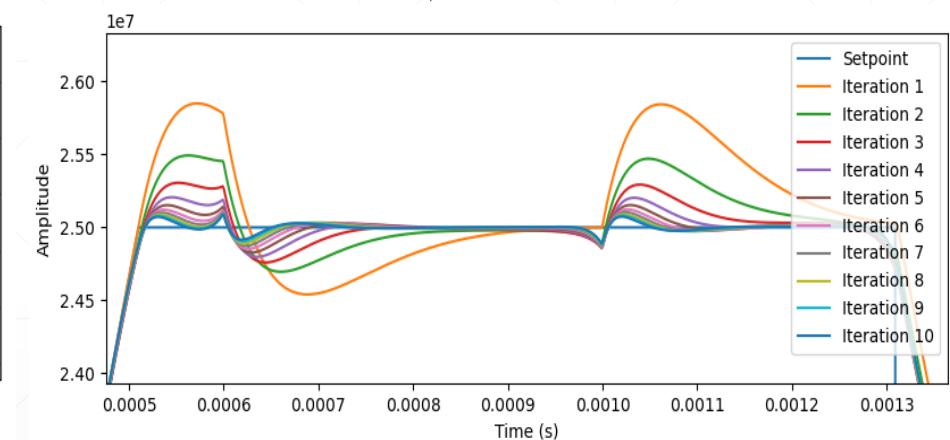
example\_aff\_timerev\_lpf.py



Feedforward Control



Cavity response after 10 iterations



Flattop amplitude/phase convergence



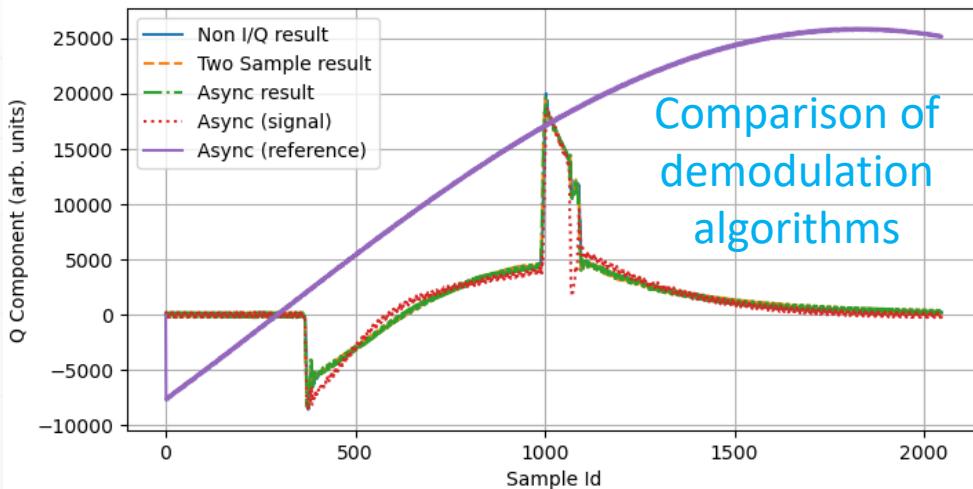
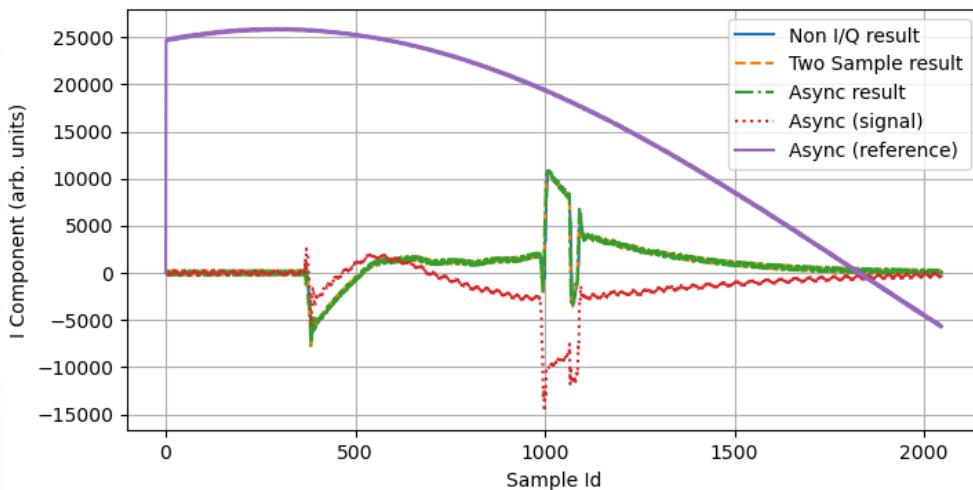
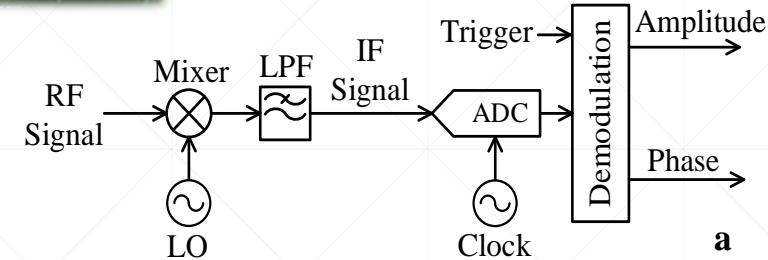
# RF Detection and Actuation

| Function                   | Example                       | Comments  |
|----------------------------|-------------------------------|---|
| <code>noniq_demod</code>   | <code>example_demod.py</code> | Perform non-I/Q demodulation of a given raw sampling waveform                                 |
| <code>twop_demod</code>    | <code>example_demod.py</code> | Demodulate raw waveform with every two samples  |
| <code>asyn_demod</code>    | <code>example_demod.py</code> | Demodulate raw waveform sampled by asynchronous clock (a reference signal waveform is needed) |
| <code>self_demod_ap</code> | <code>example_demod.py</code> | Demodulate raw waveform with Hilbert transform, returning the amplitude and phase waveforms   |
| <code>iq2ap_wf</code>      | <code>example_demod.py</code> | Convert I/Q waveforms to amplitude/phase waveforms  |
| <code>ap2iq_wf</code>      |                               | Convert amplitude/phase waveforms to I/Q waveforms  |
| <code>norm_phase</code>    |                               | Normalize phase (scalar or waveform) to a specific range (default $\pm 180^\circ$ )           |
| <code>pulse_info</code>    |                               | Derive the pulse info like pulse width, pulse offset, etc.                                    |



# RF Detection and Actuation (cont.)

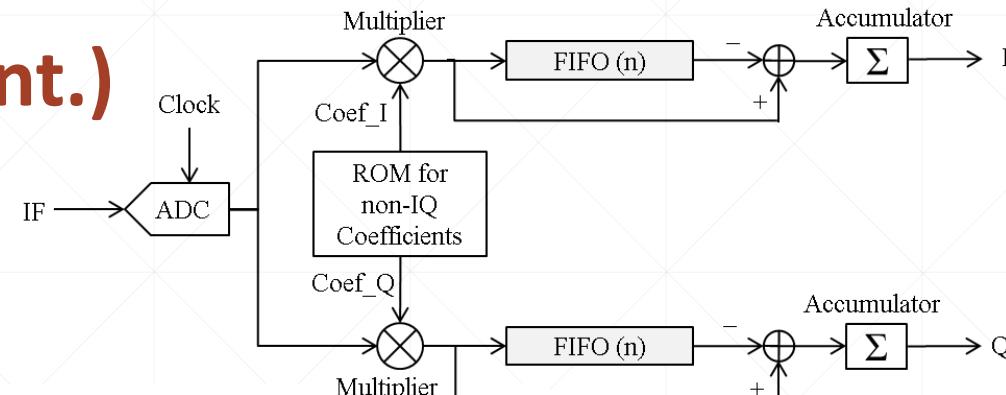
RF signal detection scheme



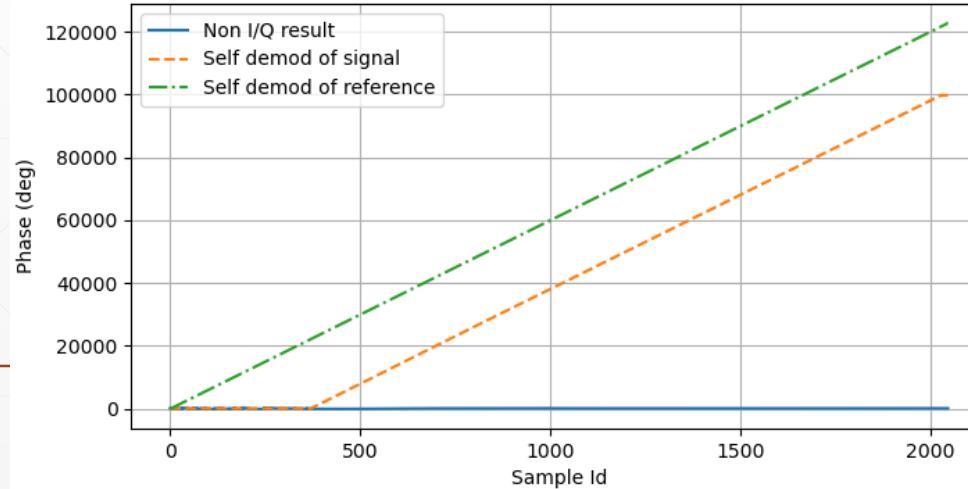
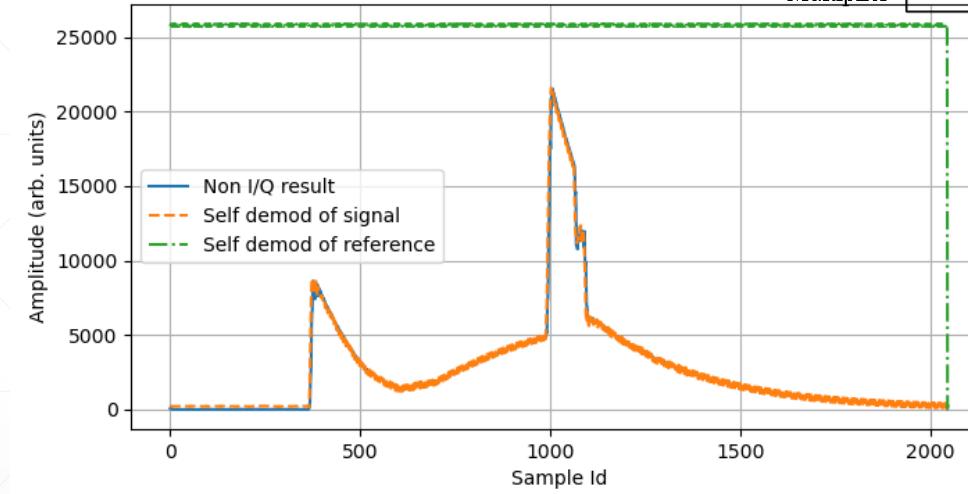
Comparison of demodulation algorithms

$$I_k = \frac{2}{n} \sum_{l=k-n+1}^k x_l \sin(l\Delta\varphi)$$

$$Q_k = \frac{2}{n} \sum_{l=k-n+1}^k x_l \cos(l\Delta\varphi)$$



Implementation of non-I/Q demodulation algorithm



Self-demodulation with Hilbert Transform

example\_demod.py



# RF Noise Analysis

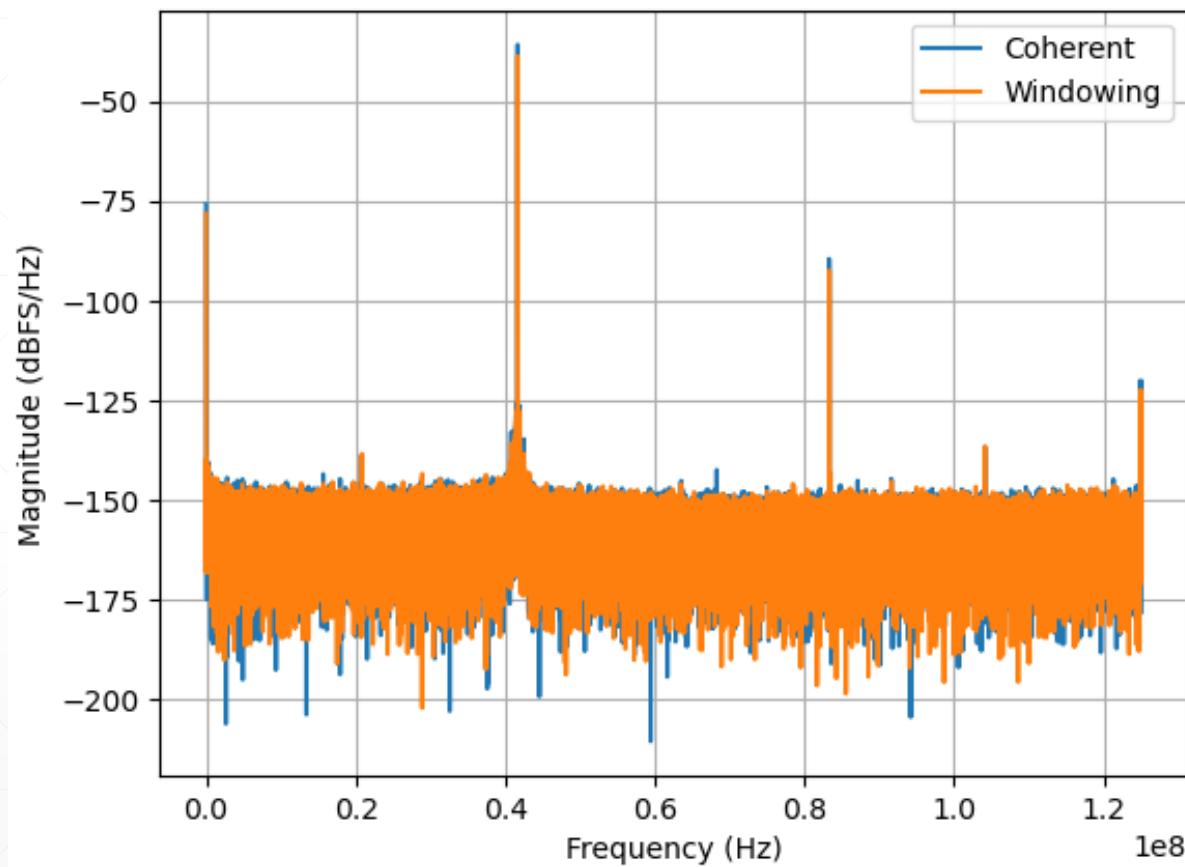
| Function                   | Example                            | Comments   |
|----------------------------|------------------------------------|--|
| <b>calc_psd_coherent</b>   | example_noise_psd.py               | Calculate the power spectral density (PSD) of a coherent sampled data series |
| <b>calc_psd</b>            | example_noise_psd.py               | Calculate the PSD of a general data series                                   |
| <b>rand_unif</b>           |                                    | Generate uniform distributed random numbers                                  |
| <b>gen_noise_from_psd</b>  | example_noise_time_series.py       | Generate noise series from a given PSD spectrum                              |
| <b>calc_rms_from_psd</b>   | example_noise_time_series.py       | Calculate the RMS jitter from a given PSD spectrum                           |
| <b>notch_filt</b>          | example_calib_for_ref_sc_cavity.py | Apply notch filter to a data series  |
| <b>design_notch_filter</b> | example_feedback_analysis.py       | Design a notch filter in state-space format                                  |
| <b>filt_step</b>           | example_feedback_basic.py          | Apply a single time step of state-space filter                               |
| <b>moving_avg</b>          |                                    | Moving average without compensating for the group delay                      |



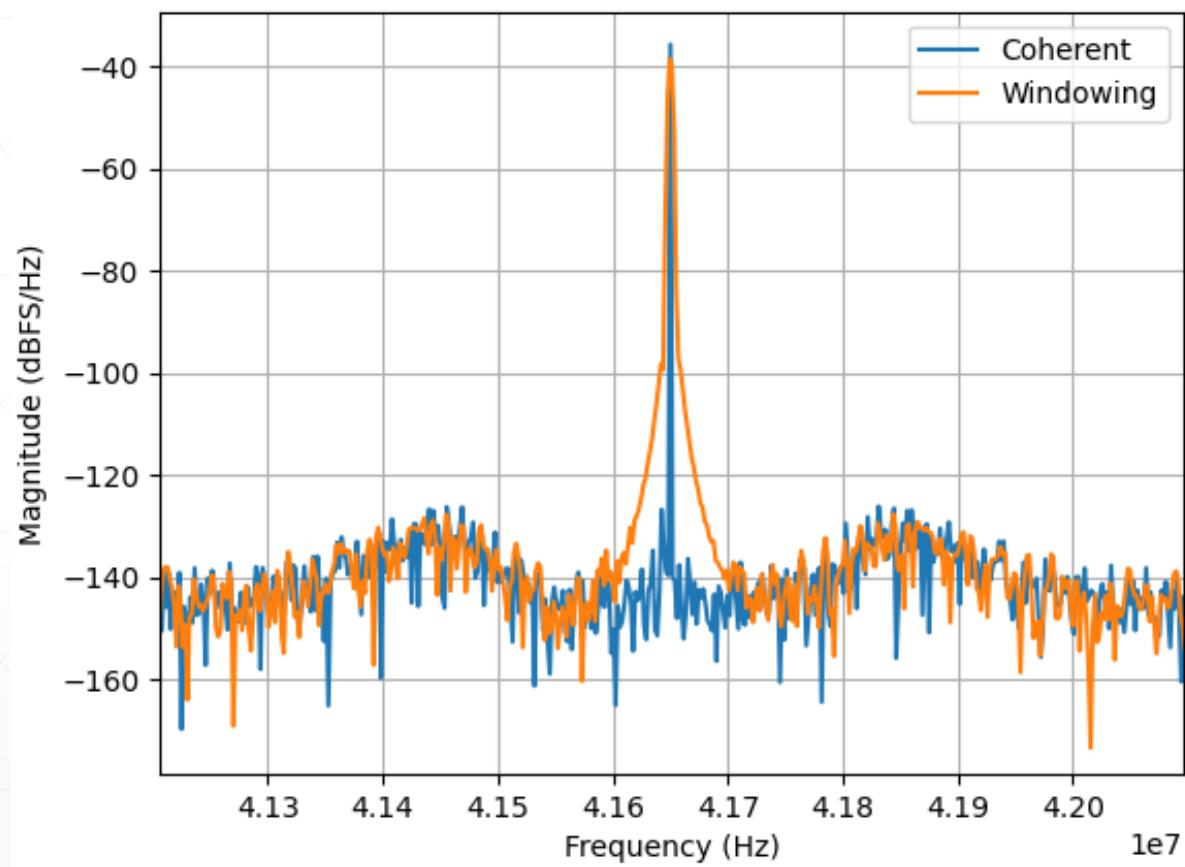
# RF Noise Analysis (cont.)

example\_noise\_psd.py

PSD of ADC Raw Waveform



PSD of ADC Raw Waveform



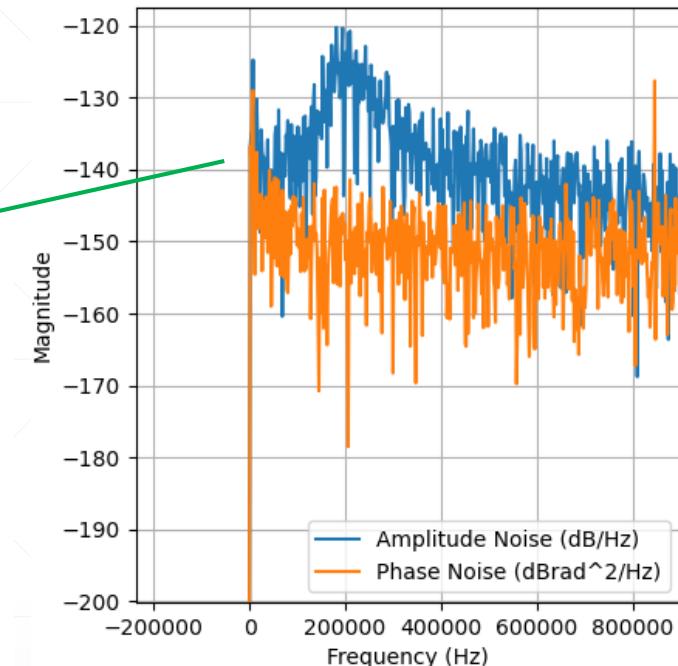
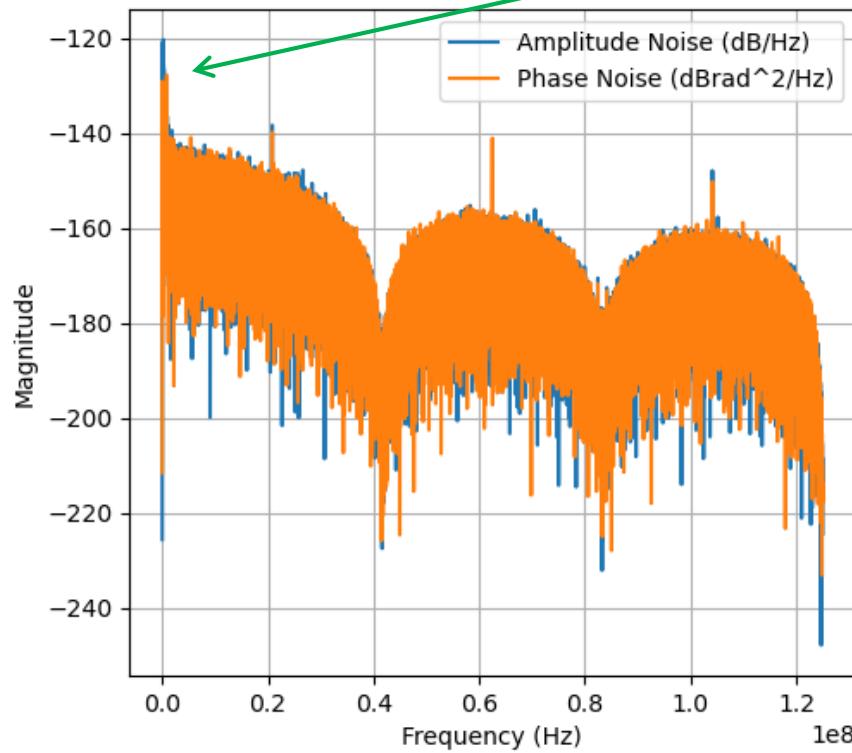
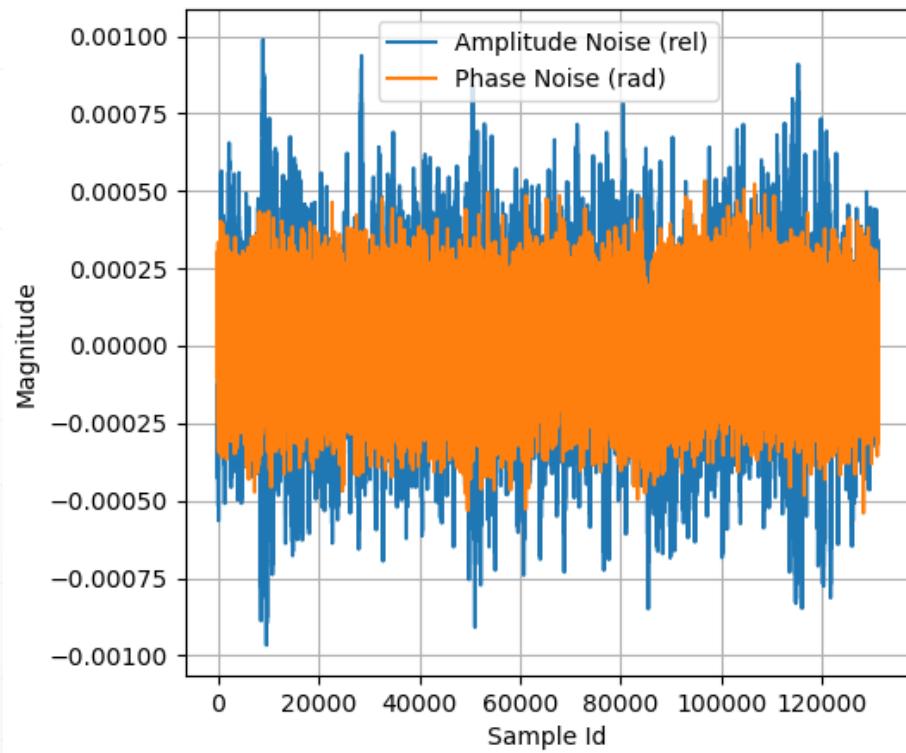
Calculate the Power Spectral Density (PSD) spectrum of ADC raw data from SwissFEL S-band. Compare the spectrum precision of coherent sampling (data covers full IF periods) with that with Blackman windowing



# RF Noise Analysis (cont.)

example\_noise\_psd.py

Amplitude & Phase Noise Time Series and PSD



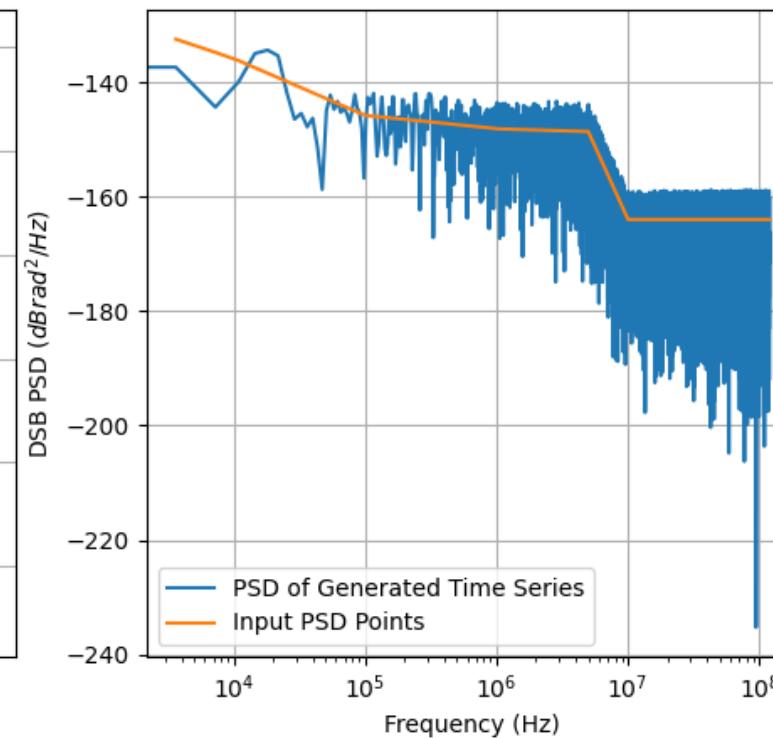
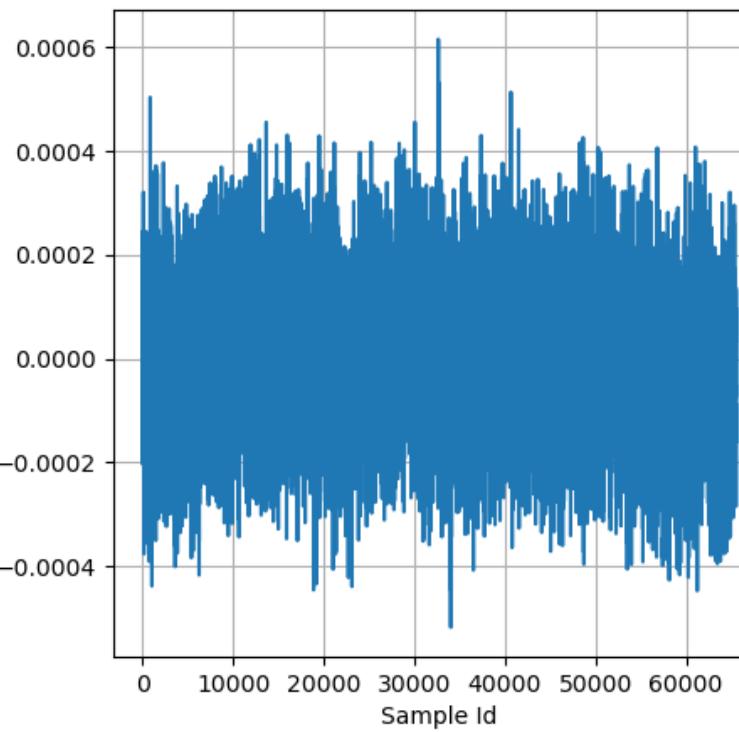


# RF Noise Analysis (cont.)

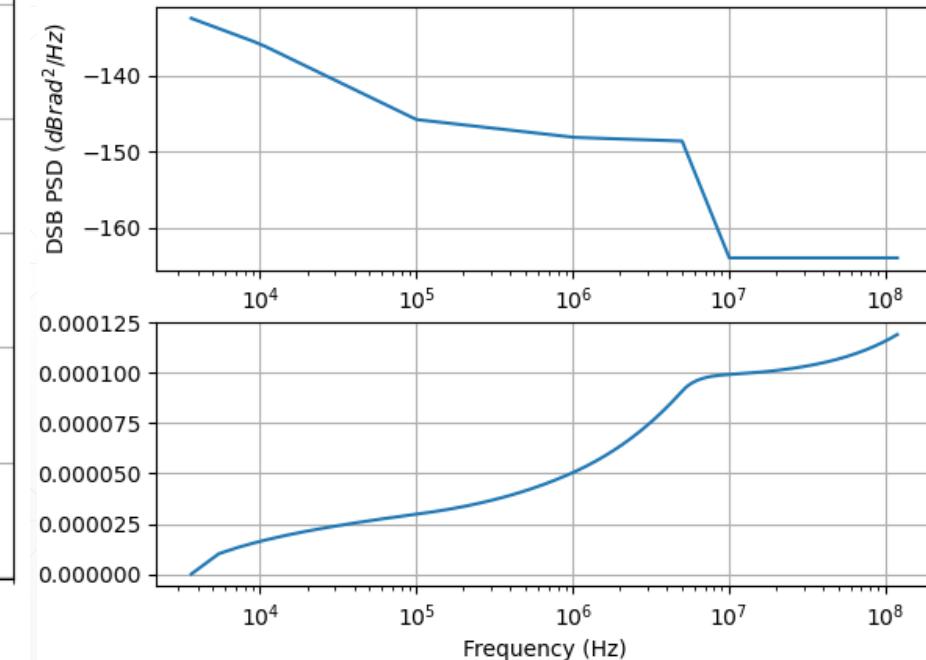
example\_noise\_time\_series.py

Input PSD values:

|  |        |         |         |         |         |         |         |      |
|--|--------|---------|---------|---------|---------|---------|---------|------|
| Offset Frequency (Hz)                    | 10     | 100     | 1e3     | 10e3    | 100e3   | 1e6     | 5e6     | 10e6 |
| Noise PSD (dB $\text{rad}^2/\text{Hz}$ ) | -82.03 | -107.07 | -128.22 | -135.86 | -145.81 | -148.15 | -148.62 | -164 |



Time series generation and PSD spectrum verification



Noise PSD spectrum -> jitter estimation

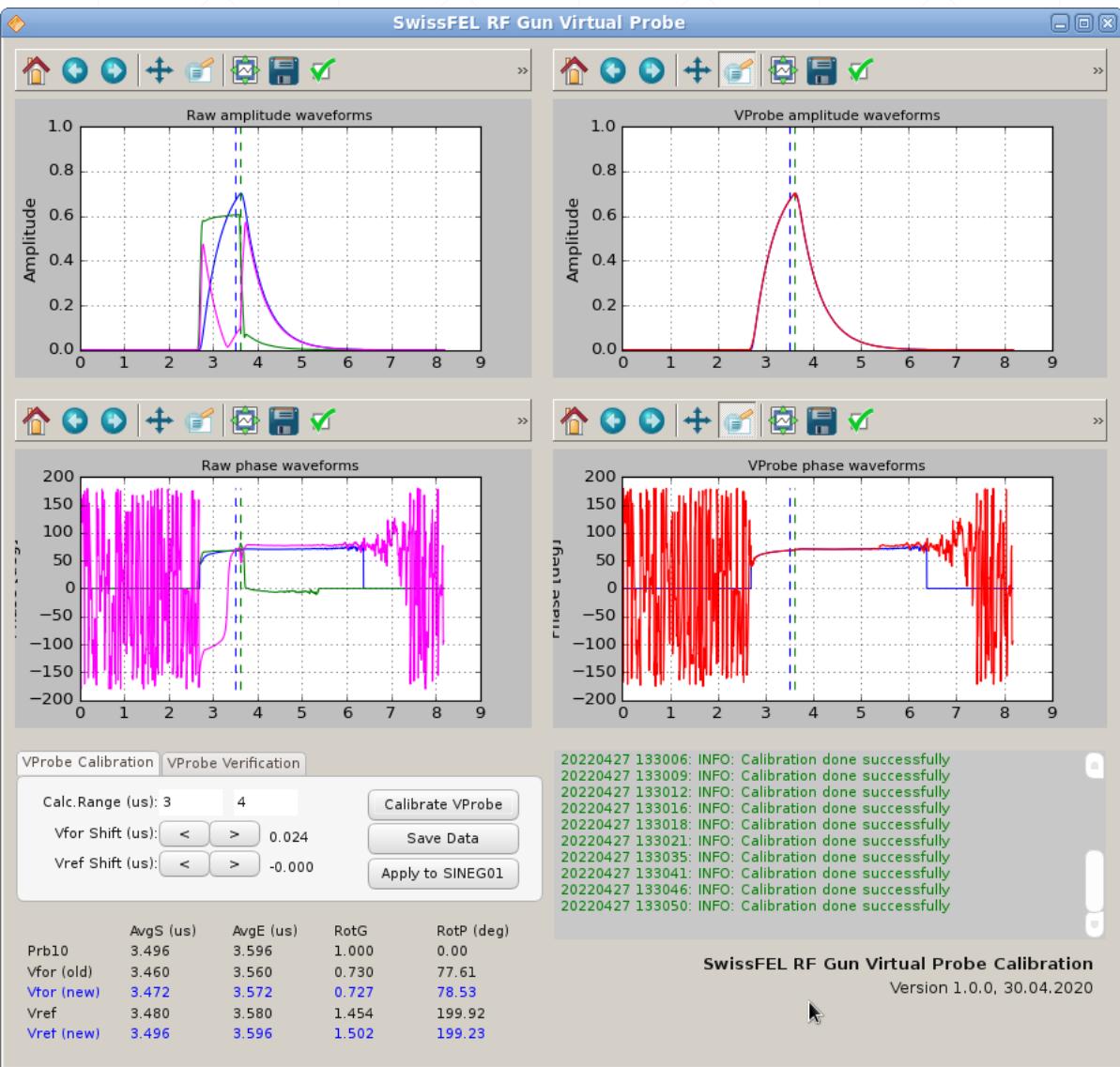


# RF Calibration

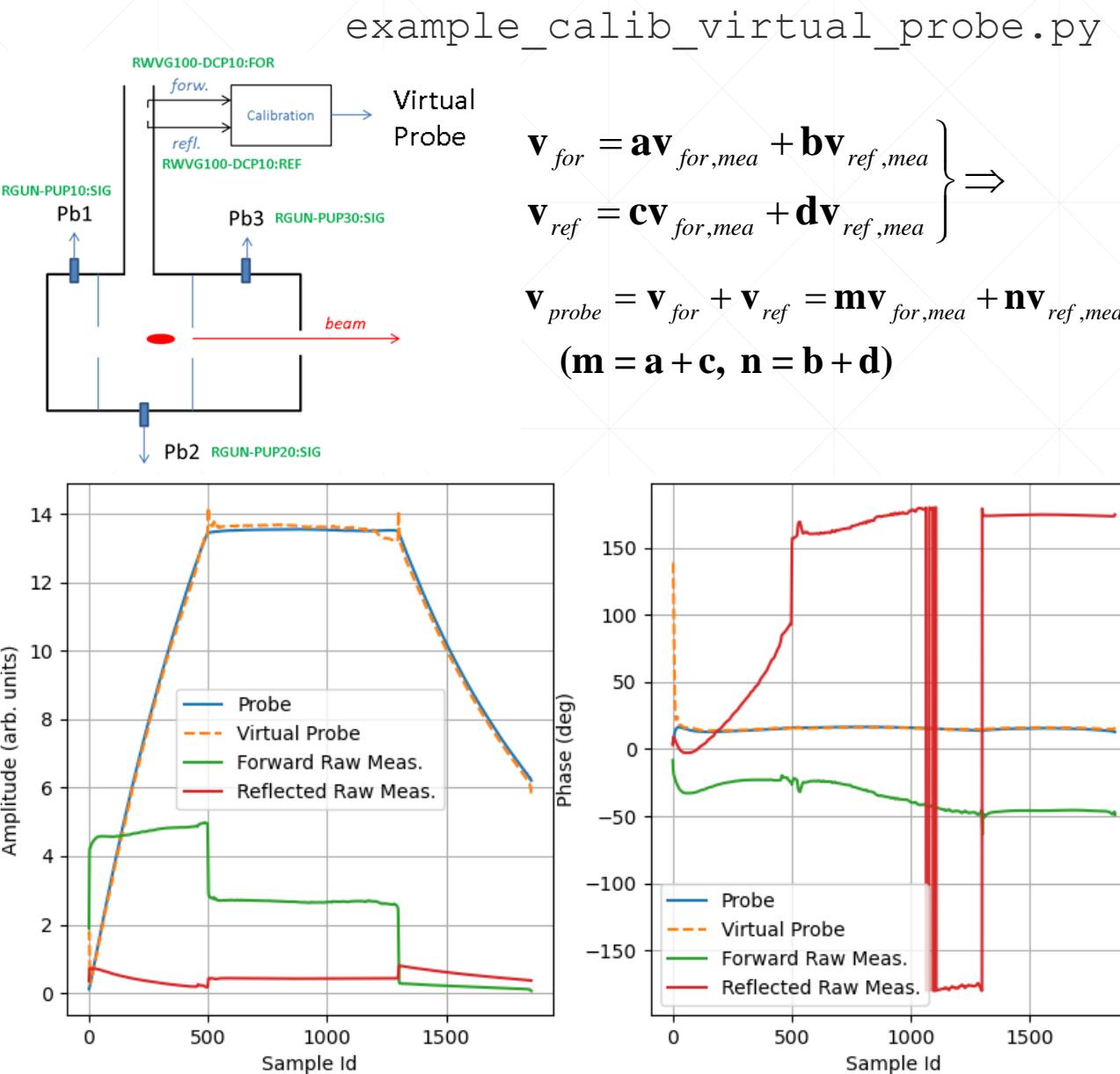
| Function                        | Example  | Comments   |
|---------------------------------|--|--|
| <code>calib_vprobe</code>       | <code>example_calib_virtual_probe.py</code>      | Calibrate cavity virtual probe with the forward & reflected signals                      |
| <code>calib_dac_offs</code>     | <code>example_calib_dac_offs.py</code>           | Calibrate DAC offset for I/Q modulator used in direct upconversion                       |
| <code>calib_iqmod</code>        | <code>example_calib_iqm.py</code>                | Calibrate I/Q modulator imbalance for direct upconversion                                |
| <code>calib_cav_for</code>      | <code>example_calib_for_ref_nc_cavity.py</code>  | Calibrate cavity forward signal using forward and probe                                  |
| <code>calib_ncav_for_ref</code> | <code>example_calib_for_ref_nc_cavity.py</code>  | Calibrate cavity forward & reflected signals with constant QL and detuning               |
| <code>calib_scav_for_ref</code> | <code>example_calib_for_ref_sc_cavity.py</code>  | Calibrate cavity forward & reflected signals with time-varying QL and detuning           |
| <code>for_ref_volt2power</code> | <code>example_sim_cavity_basic.py</code>         | Calibrate forward & reflected power from forward & reflected voltage                     |
| <code>phasing_energy</code>     | <code>example_fit_funcs.py</code> (demo fitting) | Calibrate energy gain and beam phase with phase scan and energy measurement              |
| <code>egain_cav_power</code>    | <code>example_power_to_vacc.py</code>            | Estimate steady-state standing-wave cavity voltage from drive power                      |
| <code>egain_cgstr_power</code>  | <code>example_power_to_vacc.py</code>            | Estimate constant-gradient traveling-wave structure ACC voltage from drive power         |
| <code>calib_vsum_poor</code>    |  | Calibrate vector sum by rotating and scaling all signals referring to a selected channel |
| <code>calib_sys_gain_pha</code> | <code>example_calib_sys_gain_phase.py</code>     | Calibrate system gain and system phase   |



# RF Calibration (cont.)



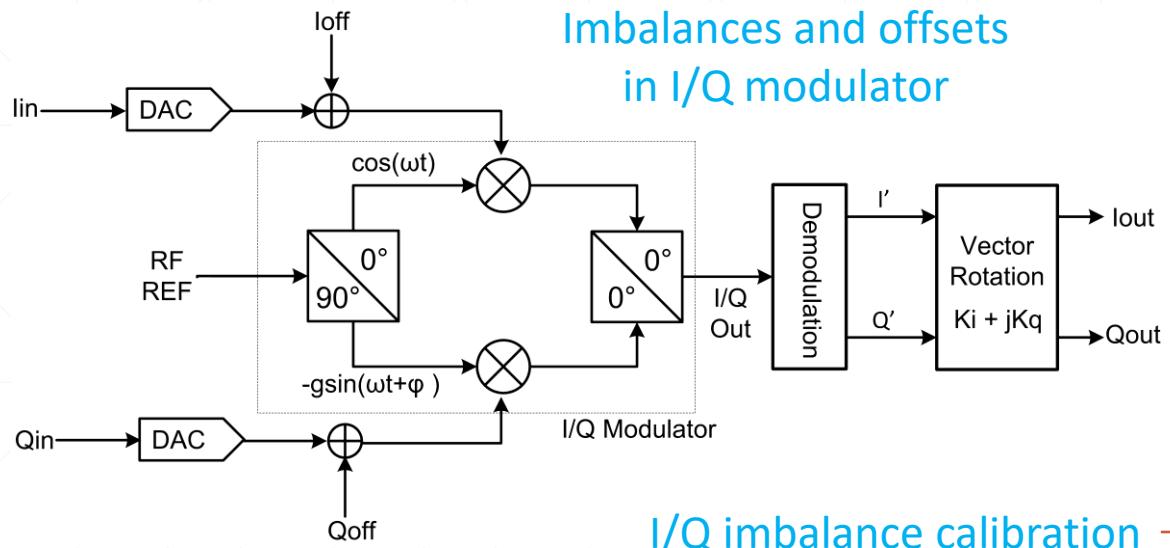
Virtual probe calibration of SwissFEL Gun



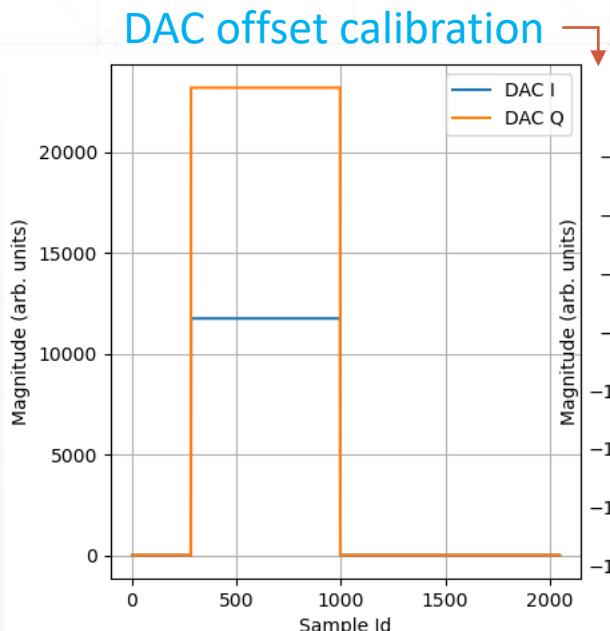
Virtual probe calibration of a TESLA cavity



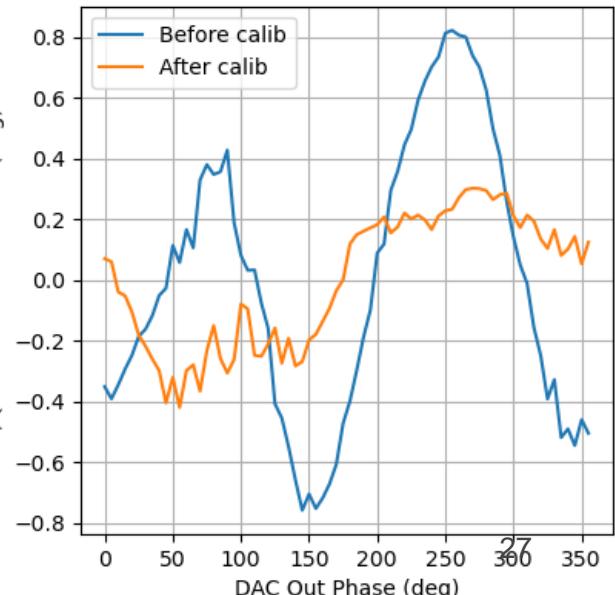
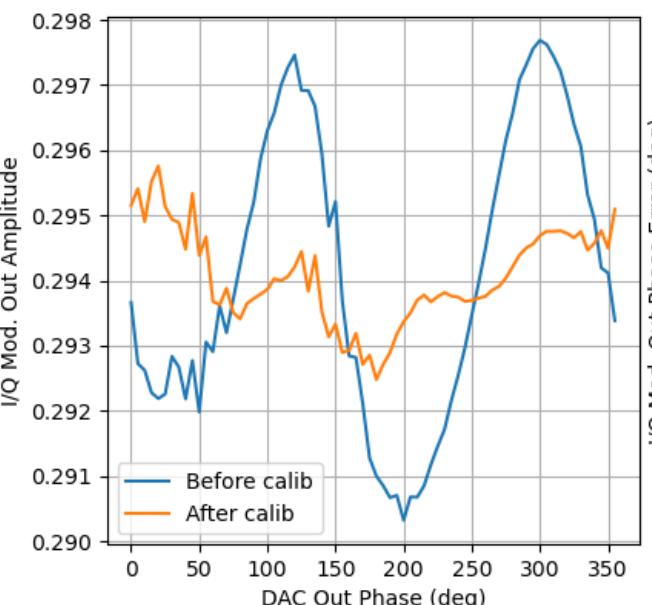
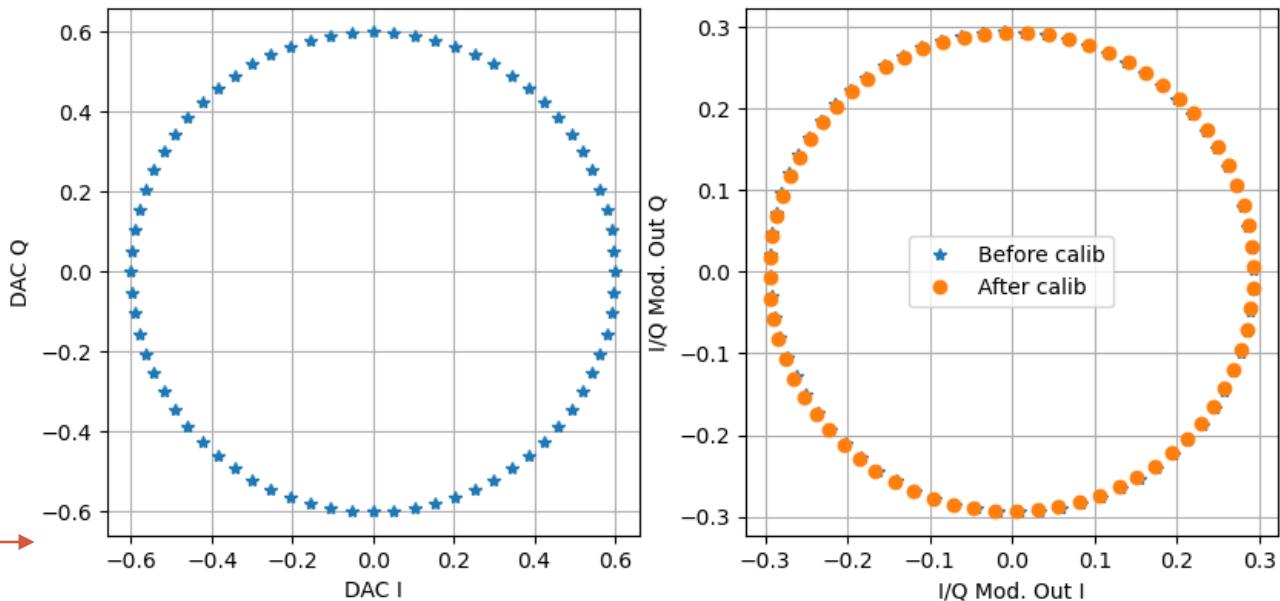
# RF Calibration (cont.)



I/Q imbalance calibration →

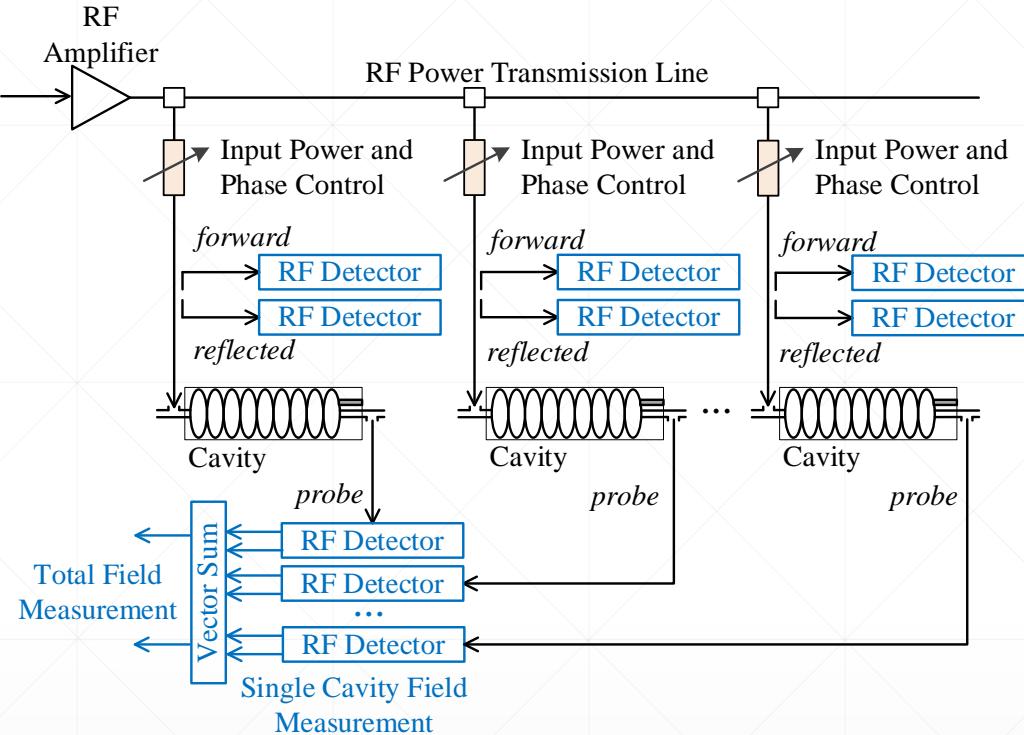


example\_calib\_dac\_offs.py  
example\_calib\_iqm.py





# RF Calibration (cont.)



$$\mathbf{v}_{C,cal} = \mathbf{v}_{for,cal} + \mathbf{v}_{ref,cal},$$

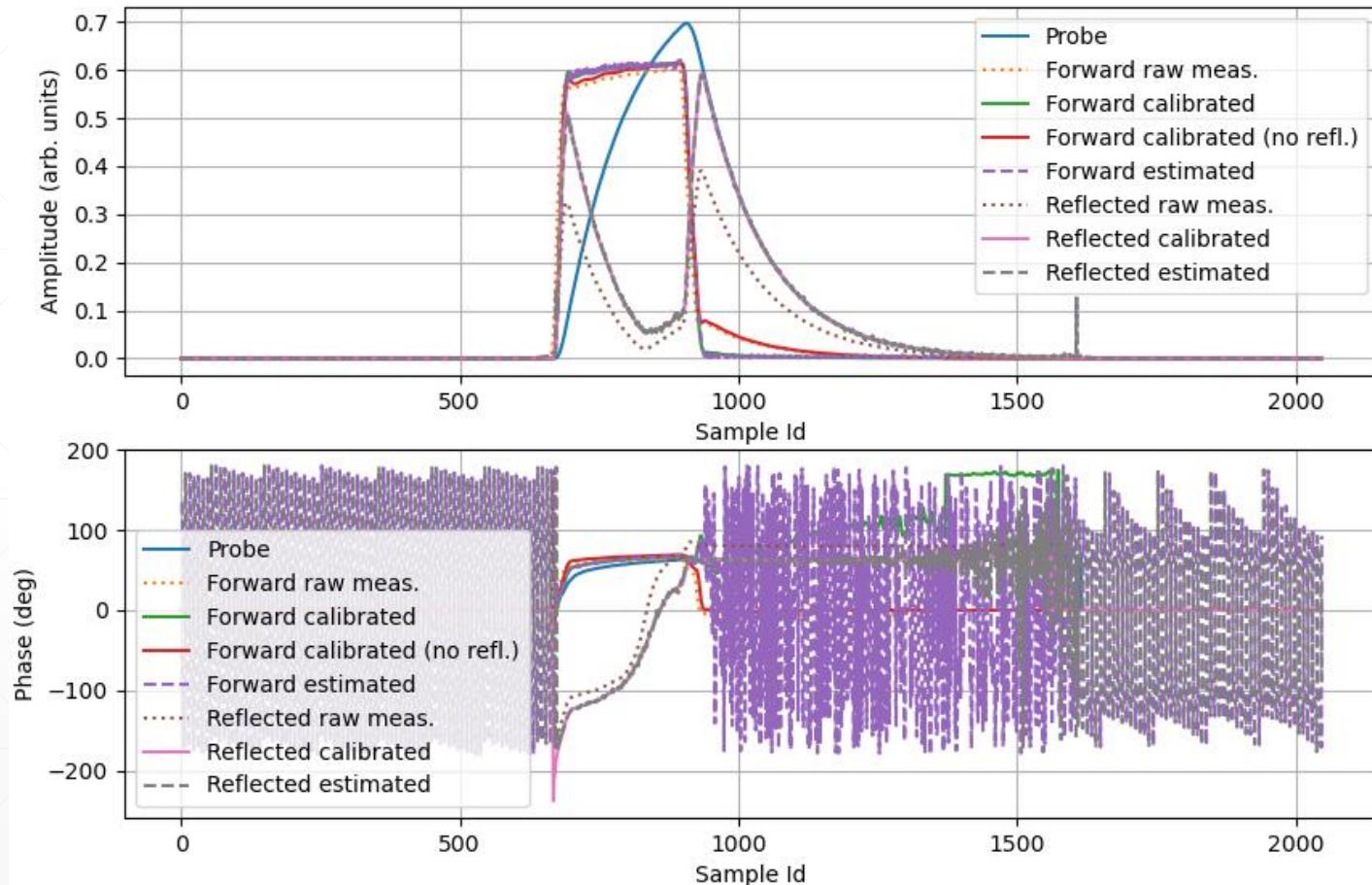
$$\mathbf{v}_{for,cal} = \mathbf{a}\mathbf{v}_{for,mea} + \mathbf{b}\mathbf{v}_{ref,mea},$$

$$\mathbf{v}_{ref,cal} = \mathbf{c}\mathbf{v}_{for,mea} + \mathbf{d}\mathbf{v}_{ref,mea}.$$

Calibrate the directional coupler directivity  
and arbitrary measurement path

`example_calib_for_ref_nc_cavity.py`

Calibration of Forward/Reflected Signals





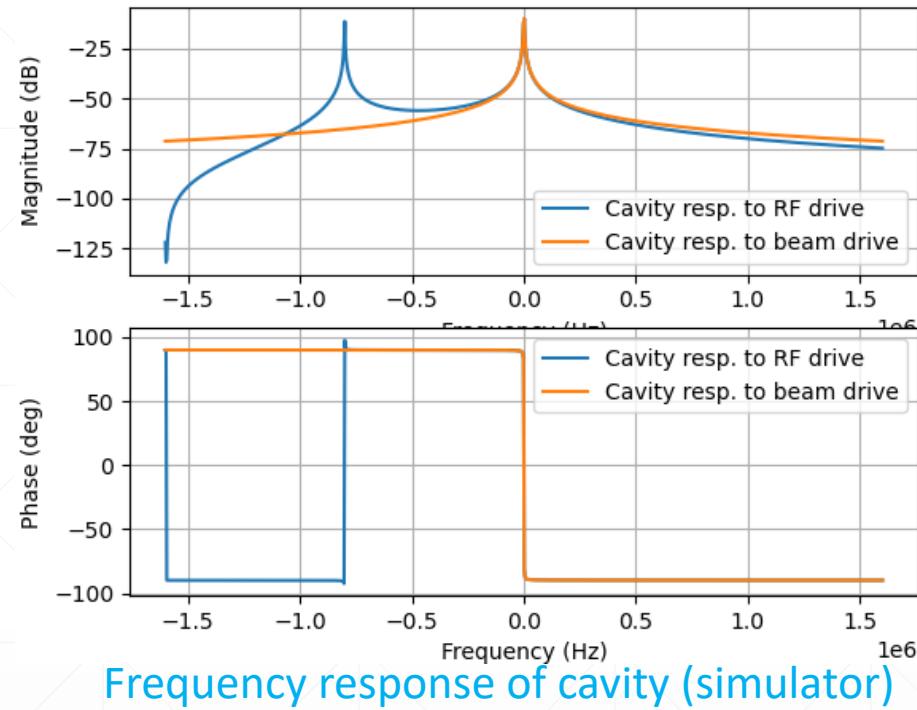
# RF System Identification

| Function                  | Example  | Comments   |
|---------------------------|--|--|
| <b>prbs</b>               | example_sysid_prbs_etfe.py                                   | Produce the PRBS signal for system identification  |
| <b>etfe</b>               | example_sysid_prbs_etfe.py                                   | Empirical Transfer Function Estimation (ETFE)  |
| <b>half_bw_decay</b>      | example_calib_for_ref_sc_cavity.py                           | Calculate the cavity half-bandwidth from the RF pulse decay stage  |
| <b>detuning_decay</b>     | example_calib_for_ref_sc_cavity.py                           | Calculate the cavity detuning from the RF pulse decay stage  |
| <b>cav_drv_est</b>        | example_calib_for_ref_nc_cavity.py                           | Estimate the cavity drive and reflected signals from probe signal  |
| <b>cav_par_pulse</b>      | example_calib_for_ref_sc_cavity.py<br>example_sysid_caveq.py | Calculate the cavity parameters (half-bandwidth and detuning) within the pulse by directly solving the cavity equation |
| <b>cav_par_pulse_obs</b>  | example_calib_for_ref_sc_cavity.py<br>example_sysid_caveq.py | Calculate the cavity parameters (half-bandwidth and detuning) within the pulse using the ADRC observer                 |
| <b>cav_beam_pulse_obs</b> | example_sysid_caveq.py                                       | Calculate the beam drive voltage within the pulse using the ADRC observer  |
| <b>cav_observer</b>       |  | Construct the ADRC observer and estimate the denoised cavity voltage and the general disturbances                      |
| <b>iden_impulse</b>       | example_aff_ilc.py   | Identify the impulse response of a real/complex SISO system from data  |
| <b>beta_powers</b>        |  | Identify the cavity input coupling factor using steady-state forward & reflected powers                                |

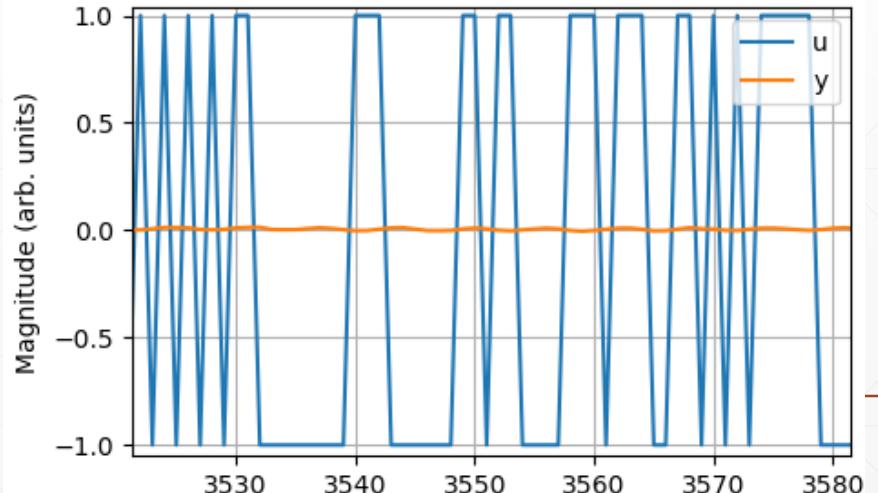


# RF System Identification (cont.)

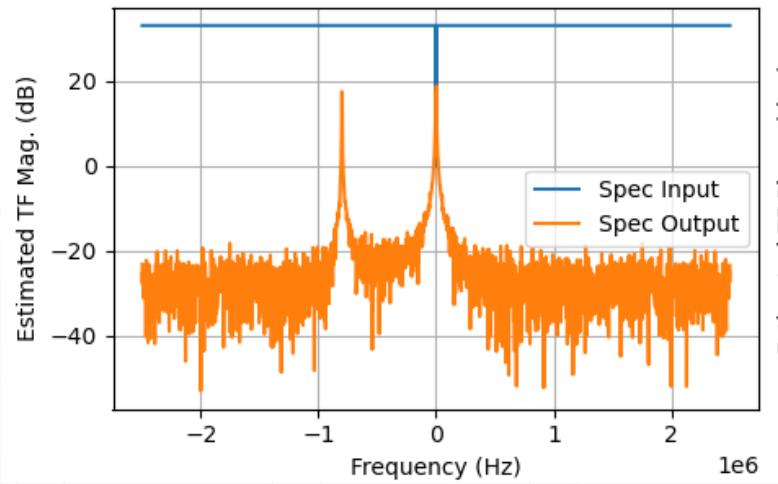
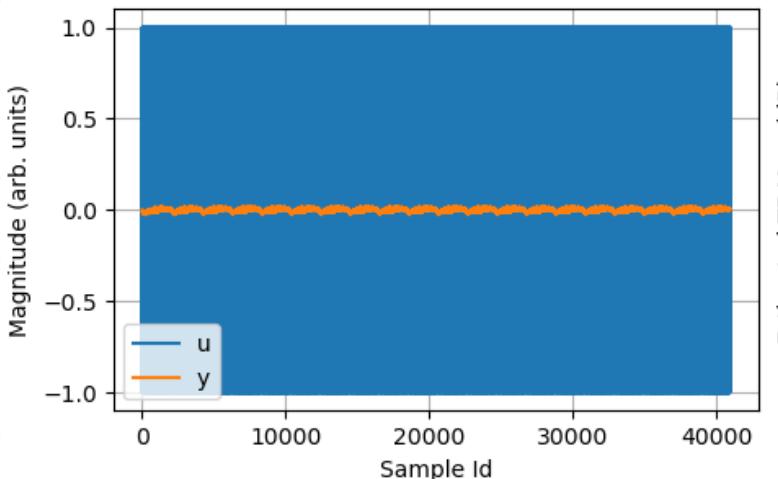
example\_sysid\_prbs\_etfe.py



Frequency response of cavity (simulator)



Pseudorandom Binary Sequence (PRBS) input and output

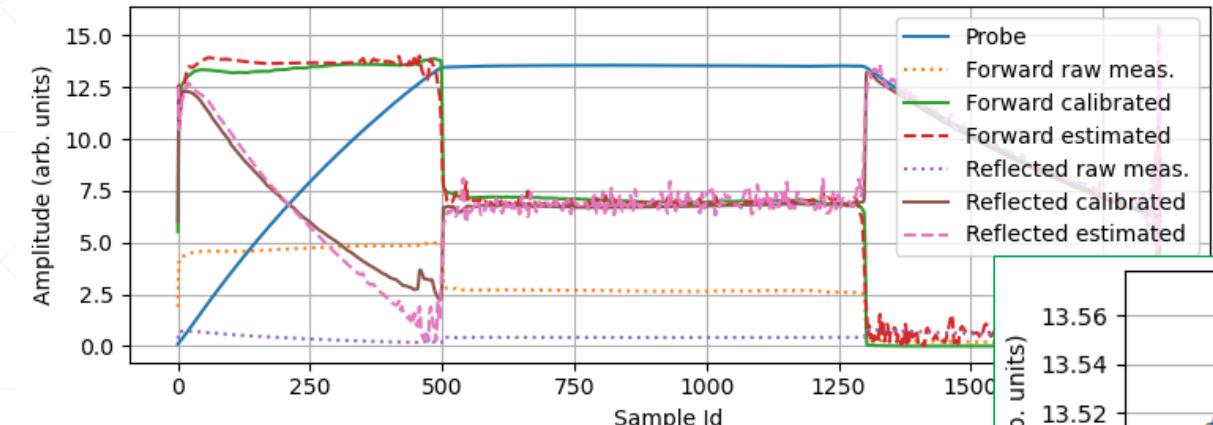


System identification with Empirical Transfer Function Estimation (ETFE) method

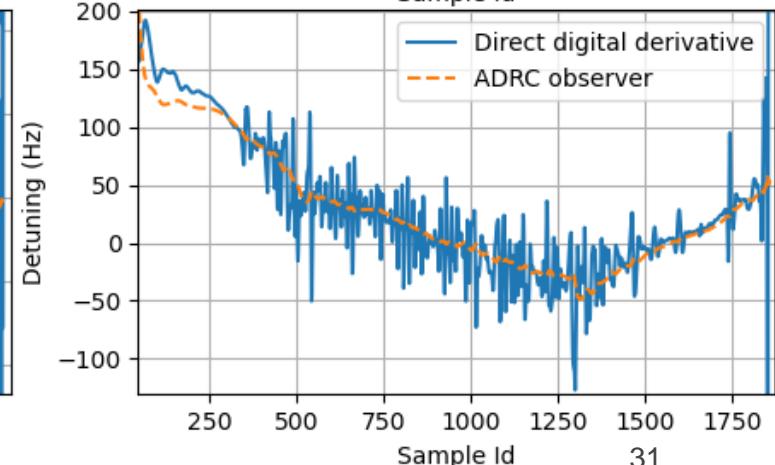
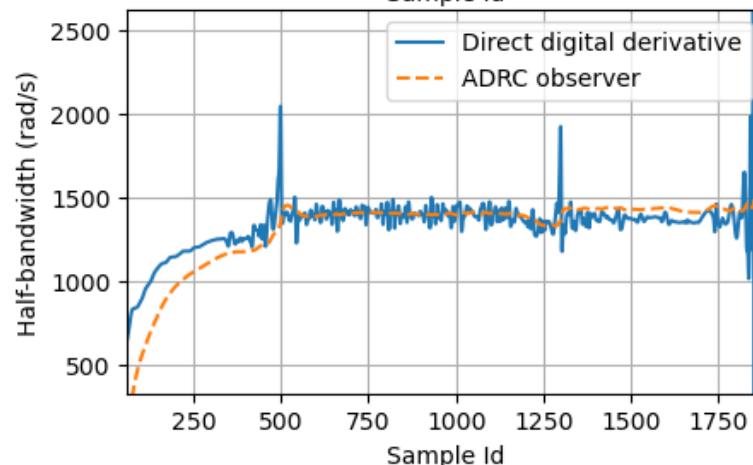
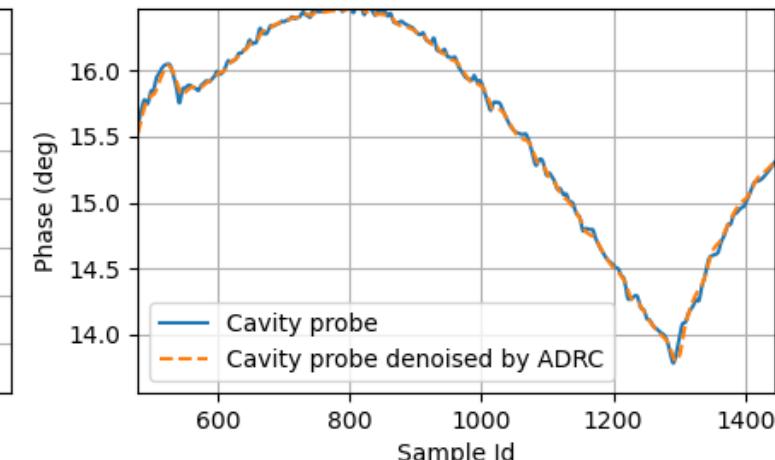
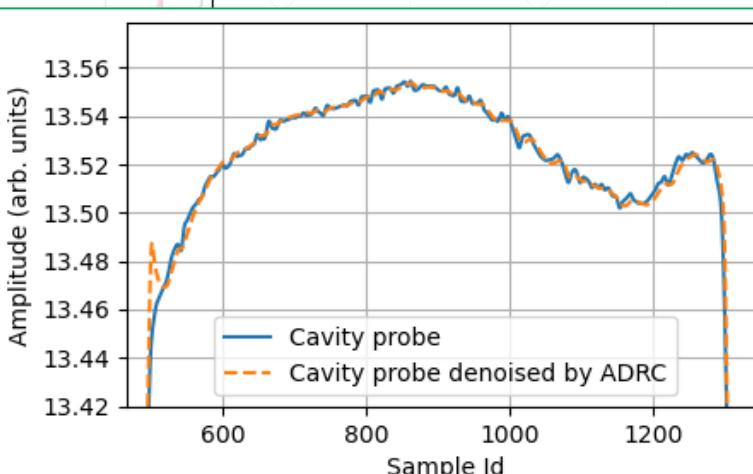
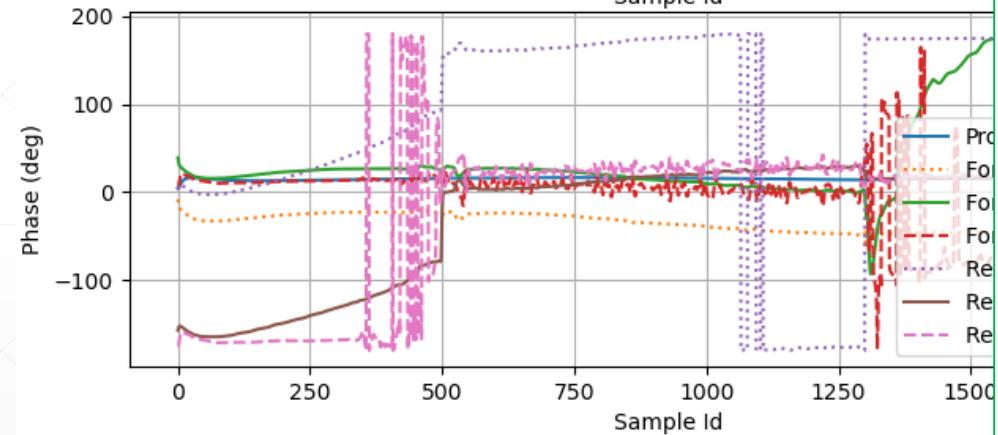


# RF System Identification (cont.)

example\_calib\_for\_ref\_sc\_cavity.py



Calibration of forward and reflected signals to the same reference plane of probe signal

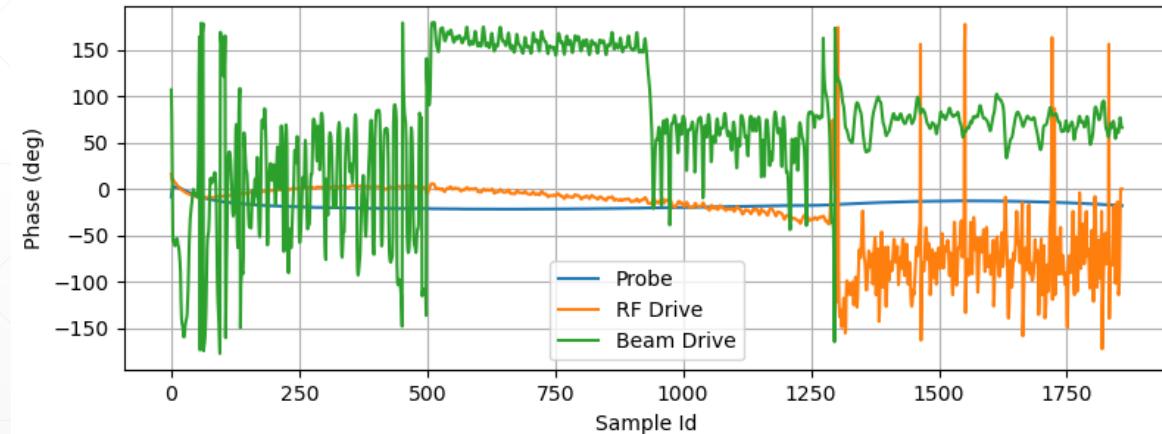
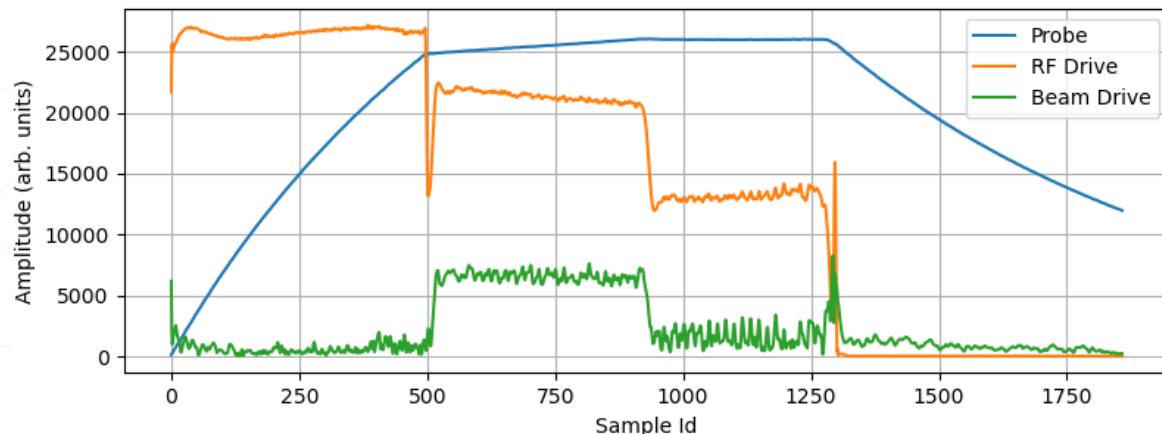


Smooth the cavity probe signal, and calculate the half-bandwidth and detuning of the cavity during the RF pulse

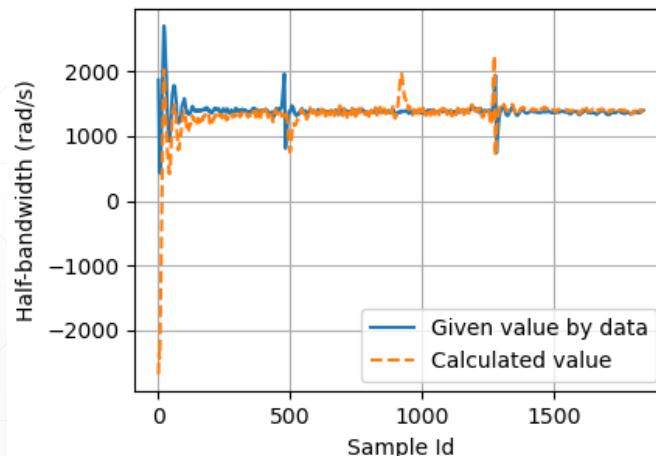
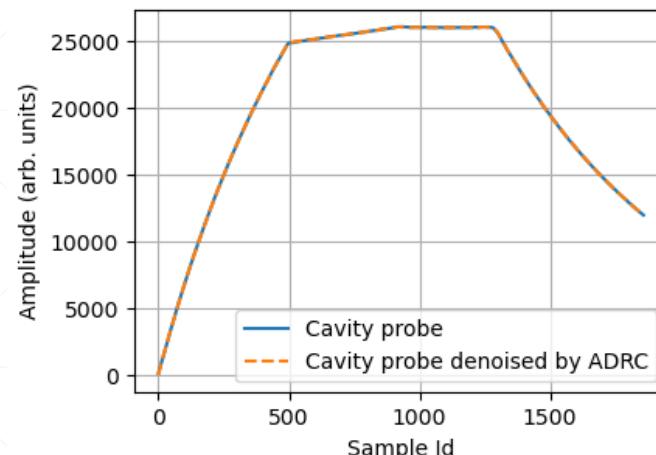


# RF System Identification (cont.)

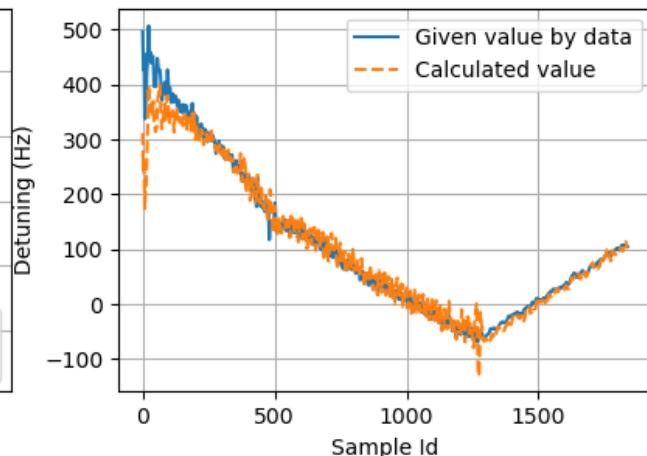
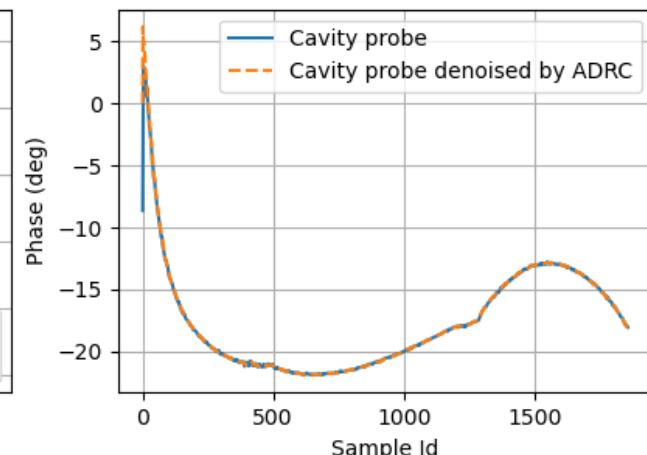
example\_sysid\_caveq.py



Cavity probe signal, RF drive signal and beam drive signal (already calibrated to the same reference plane as the probe)



Calculate the half-bandwidth and detuning during the pulse with beam on





# Other functions

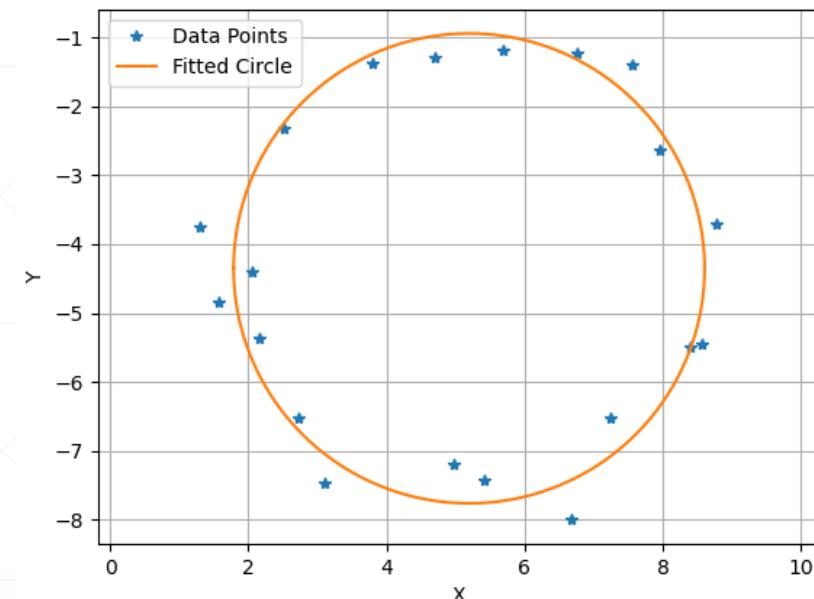
| Function                  | Example                           | Comments                                 |
|---------------------------|-----------------------------------|--|
| <code>fit_sincos</code>   | <code>example_fit_funcs.py</code> | Fit the sine or cosine function          |
| <code>fit_circle</code>   | <code>example_fit_funcs.py</code> | Fit the 2D points to a circle function   |
| <code>fit_ellipse</code>  | <code>example_fit_funcs.py</code> | Fit the 2D points to an ellipse function |
| <code>fit_Gaussian</code> | <code>example_fit_funcs.py</code> | Fit a 1D Gaussian function               |

| Function                     | Example                           | Comments   |
|------------------------------|-----------------------------------|--|
| <code>save_mat</code>        |                                   | Save a dictionary into a Matlab .mat file              |
| <code>load_mat</code>        |                                   | Load a Matlab .mat file into a dictionary              |
| <code>get_curtime_str</code> |                                   | Get a string of the current date/time                  |
| <code>get_bit</code>         |                                   | Get a bit of an integer                                |
| <code>add_tf</code>          |                                   | Adding two transfer functions in numerator/denominator |
| <code>plot_ellipse</code>    | <code>example_fit_funcs.py</code> | Plot an ellipse using its characteristics              |
| <code>plot_Gaussian</code>   | <code>example_fit_funcs.py</code> | Plot a 1D Gaussian distribution                        |

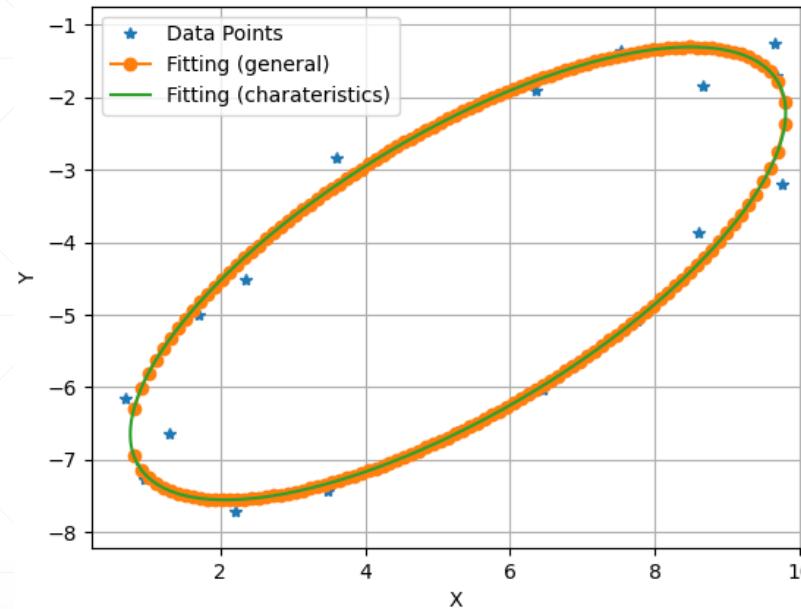


# Other functions (cont.)

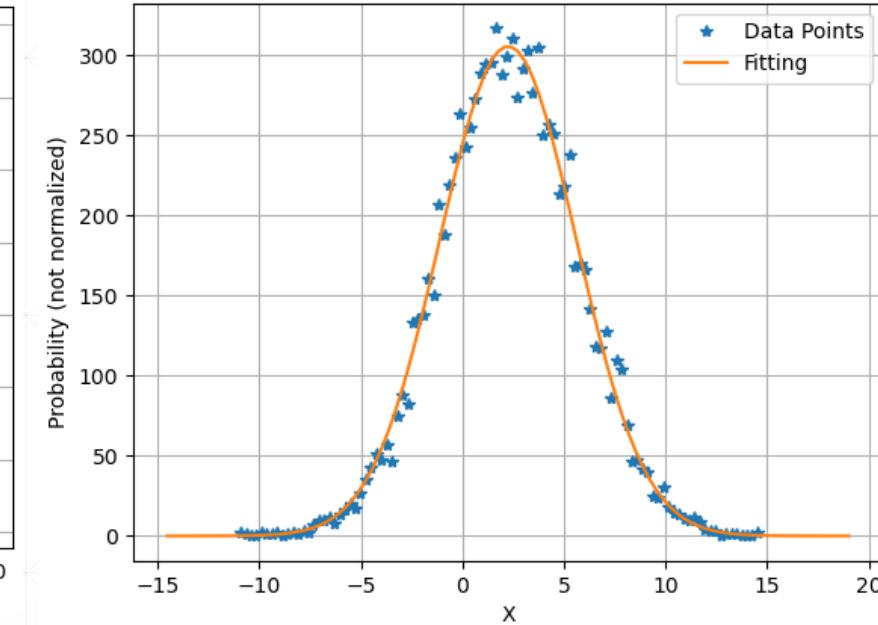
example\_fit\_funcs.py



Fit a circle



Fit an ellipse



Fit a Gaussian distribution

## **Status and Outlook**

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# Status and Outlook

- Basic functions implemented (<https://git.psi.ch/GFA/RF/Libraries/lrfllibspy>)
- Next steps:
  - Continue the development of library functions
  - Documentation
  - Open-source

**Thank you for attention!**