

Large Aperture X-ray Monitors for Beam Profile Diagnostics

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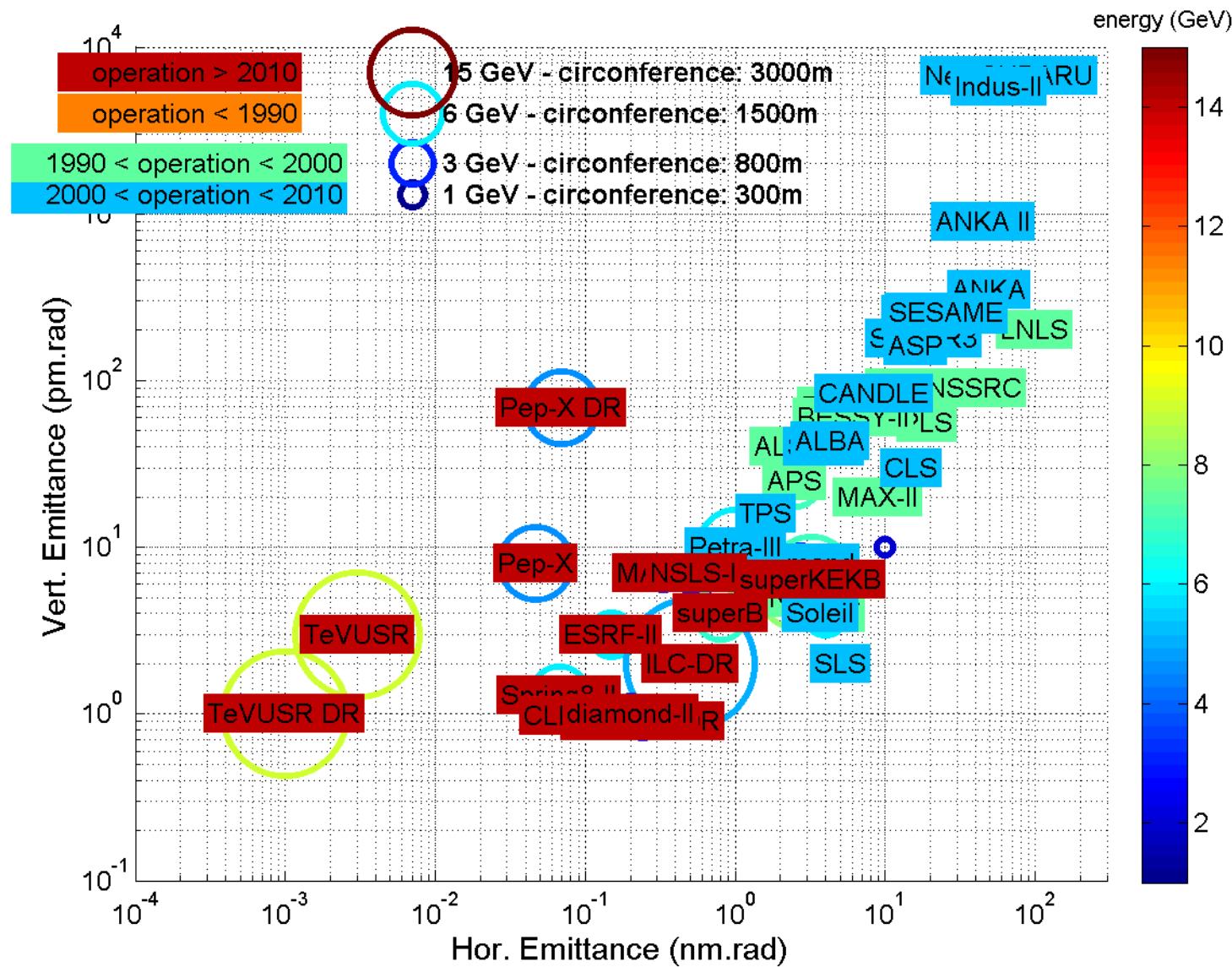
Content

- Source
 - Emittance, Storage rings, Ultimate Storage Rings
 - Photon beam: Bending Magnet, Undulators
- Image
 - Large Aperture definition
 - Coherent and incoherent imaging
 - Resolution, Deconvolution techniques, etc.
- Coded Apertures
 - URA, MURA, etc, masks
 - Zone Plates
- CRL
- Comparison with other profile measurement systems
- Conclusion

Source

- Emittance, Storage rings, Ultimate Storage Rings
 - Emittance trend reduces over the SR generations,...

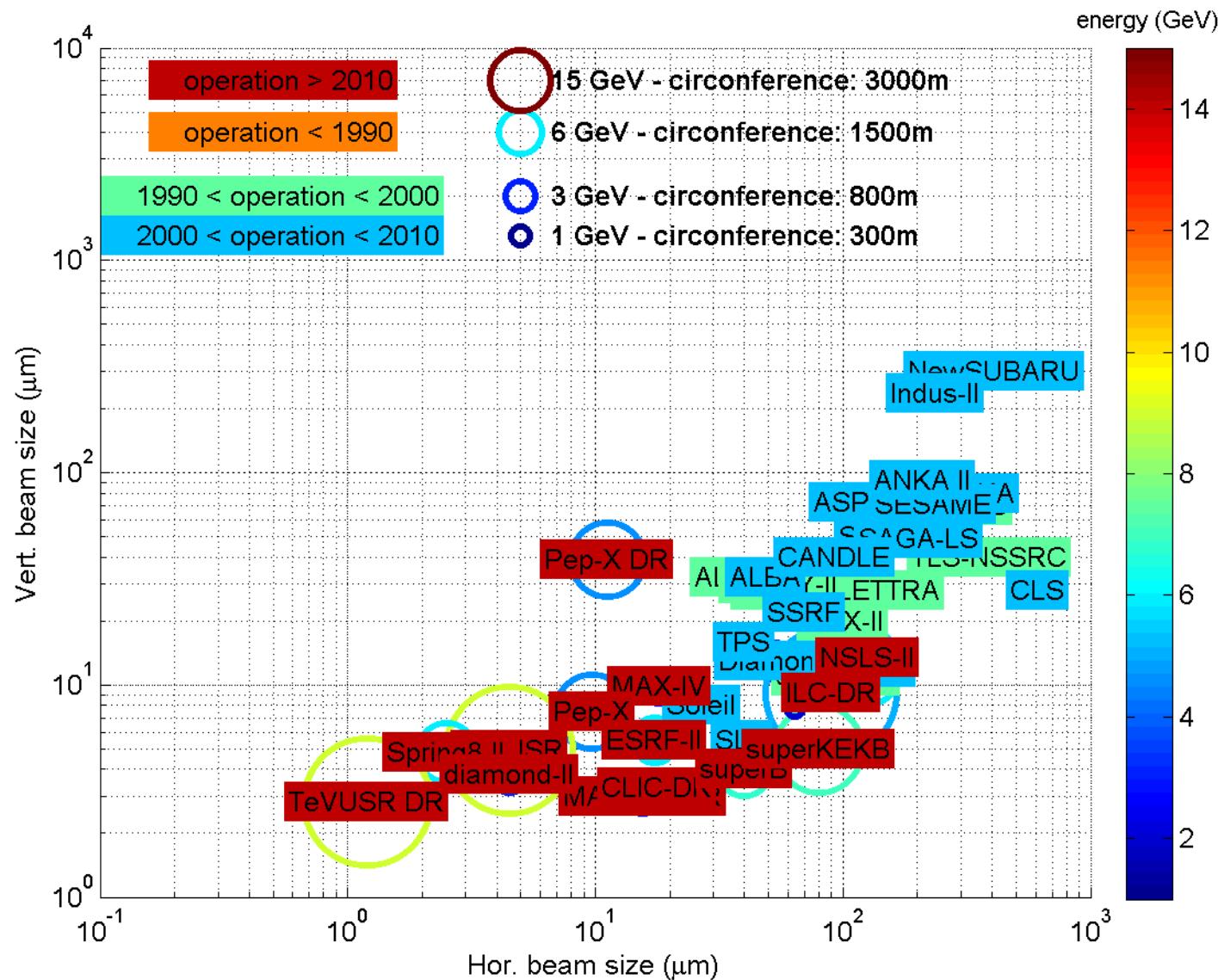
Source



Source

- Emittance, Storage rings, Ultimate Storage Rings
 - Emittance trend reduces over the SR generations, and so the beam size

Source

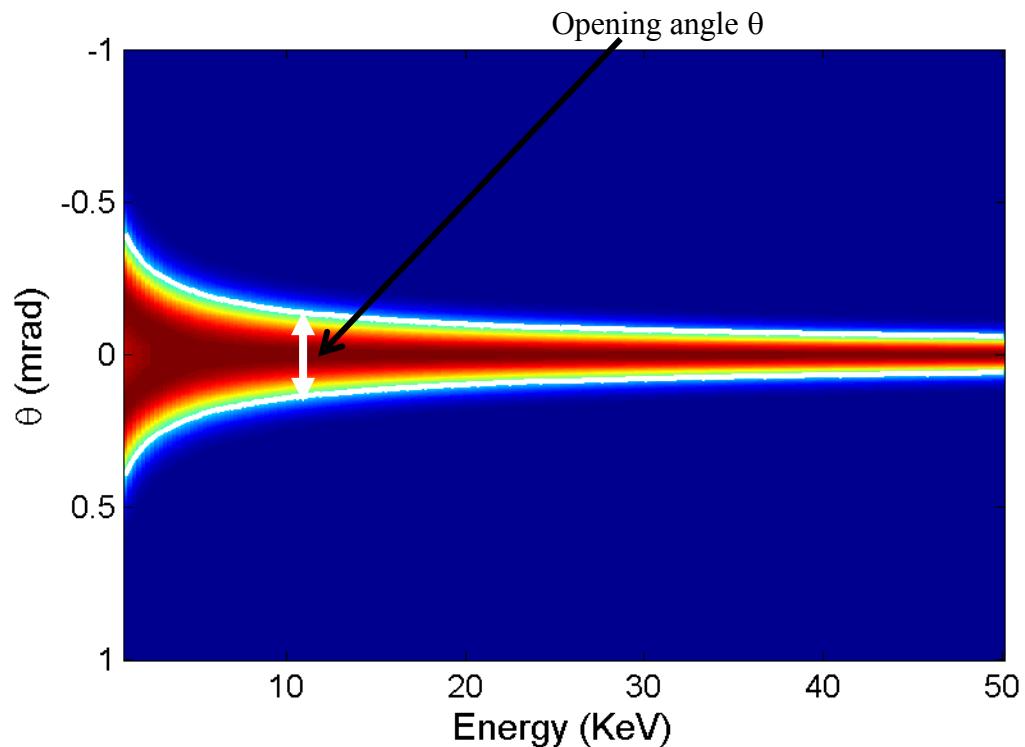


Source

- Bending Magnet source properties
 - Quasi-homogeneous X-ray source
 - Non-stationary (pulsed)

- Known solution of the source expression and of the spectral degree of coherence
- Behaves like a laser beam in vertical plane and like a infinite diverging source in the horizontal plane
- For X-ray beam, photon beam emittance much larger than the wavelength: geometrical optics approach can be used

Geloni *et al*, Statistical Optics approach to the design of beamlines for Synchrotron Radiation
arXiv:physics/0603269



Source

- Undulator Source properties
 - Quasi-homogeneous source (incoherent) provided
$$\hat{N} = \frac{\sigma_{x,y}^2 \omega}{c L_w} \gg 1 \text{ and } \hat{D} = \frac{\sigma_{x',y'}^2 \omega L_w}{c} \gg 1$$
 - Non-homogeneous source (partially coherent)
$$\hat{N} = \frac{\sigma_{x,y}^2 \omega}{c L_w} \simeq 1 \text{ and } \hat{D} = \frac{\sigma_{x',y'}^2 \omega L_w}{c} \simeq 1$$
 - Non-homogeneous source (coherent)
$$\hat{N} = \frac{\sigma_{x,y}^2 \omega}{c L_w} \ll 1 \text{ and } \hat{D} = \frac{\sigma_{x',y'}^2 \omega L_w}{c} \ll 1$$
 - Non-stationary (pulsed)

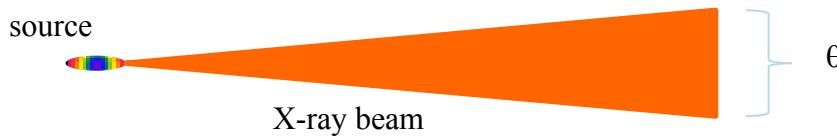
Source

- Undulator Source properties
 - Intensity profile: laser beam like with opening angle:
$$\theta_{u,n} = \sqrt{\frac{\lambda_n}{2L_u}}$$
 - Flux:
$$\frac{d\Phi_n}{d\Omega} \text{ [Photons/s/0.1%/mrad}^2\text{]} = 1.744 \cdot 10^{14} N_w^2 E_{[GeV]}^2 I_{[A]} F_n(K)$$
- Diamond U23 with N=90, 3rd Harmonic at 10keV
 - $\Phi_n \approx 10^{18}$ Photons/s/0.1%bw
 - $\theta_{u,3} \approx 5 \mu\text{rad}$

Source

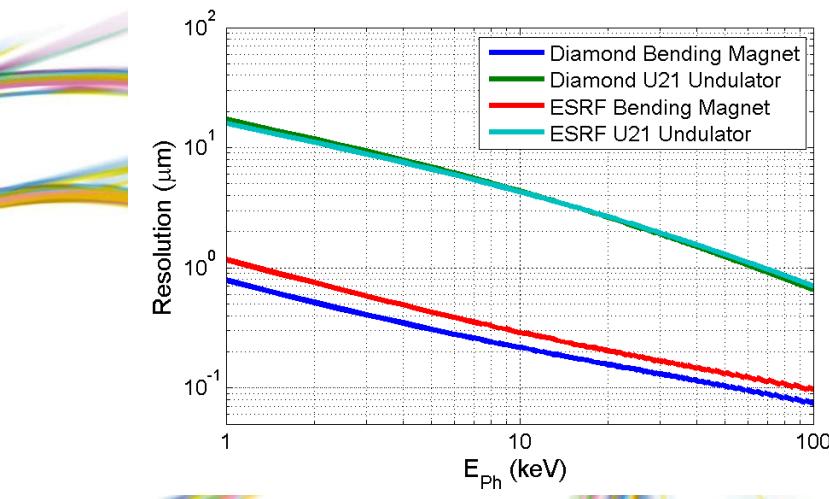
- Large Aperture definition

- Imaging device that has a numerical aperture comparable or larger than the X-ray beam numerical aperture



Numerical Aperture:
 $NA = \sin(\theta)$

Resolution:
 $R = \lambda / 2 NA$



Source	NA @ 10 keV	Resolution (μm) @ 10 keV	Aperture (mm) @ D = 10 m
U21 undulator (Diamond)	1.4×10^{-5}	4.2	0.14
U21 undulator (ESRF)	1.4×10^{-5}	4.2	0.14
Bending Magnet (Diamond)	2.8×10^{-4}	0.2	2.8
Bending Magnet (ESRF)	2.2×10^{-4}	0.3	2.2

Image

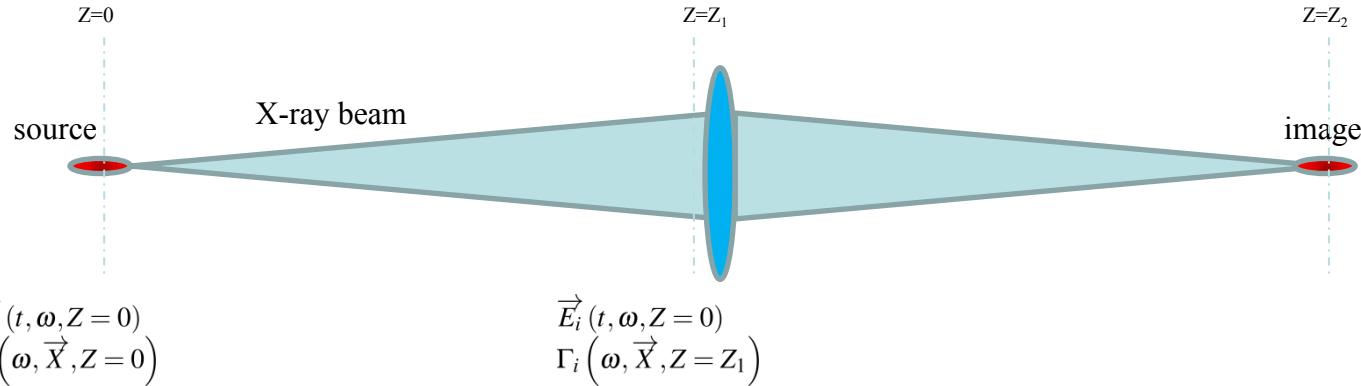


Image: 2D Fourier Transform, scaled source

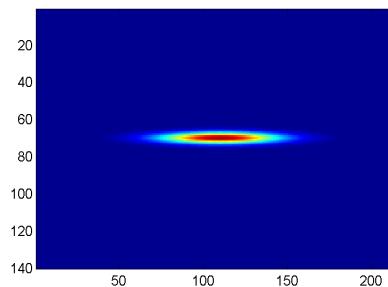
$$I(x, y) = \frac{1}{(\lambda z)^2} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \widetilde{P}(\Delta\xi, \Delta\eta) \Gamma_i(\Delta\xi, \Delta\eta) e^{i\frac{2\pi}{\lambda z}(x\Delta\xi + y\Delta\eta)} d\Delta\xi d\Delta\eta$$

Fourier transform of the pupil autocorrelation

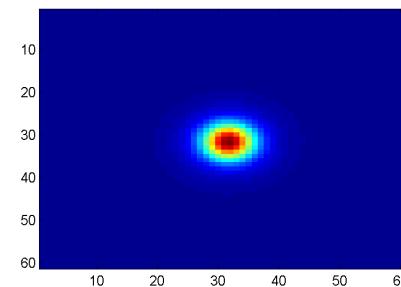
$$\widetilde{P}(\Delta\xi, \Delta\eta) = \frac{1}{(\lambda z)^2} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} P(\bar{\xi} - \frac{\Delta\xi}{2}, \bar{\eta} - \frac{\Delta\eta}{2}) P^*(\bar{\xi} + \frac{\Delta\xi}{2}, \bar{\eta} + \frac{\Delta\eta}{2}) e^{i\frac{2\pi}{\lambda z}(x\Delta\xi + y\Delta\eta)} d\Delta\xi d\Delta\eta$$

Γ_i Mutual Coherence in front of the lens

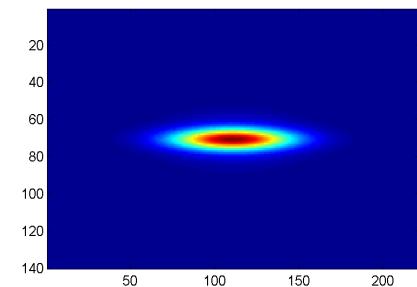
Image: Incoherent imaging and Deconvolution



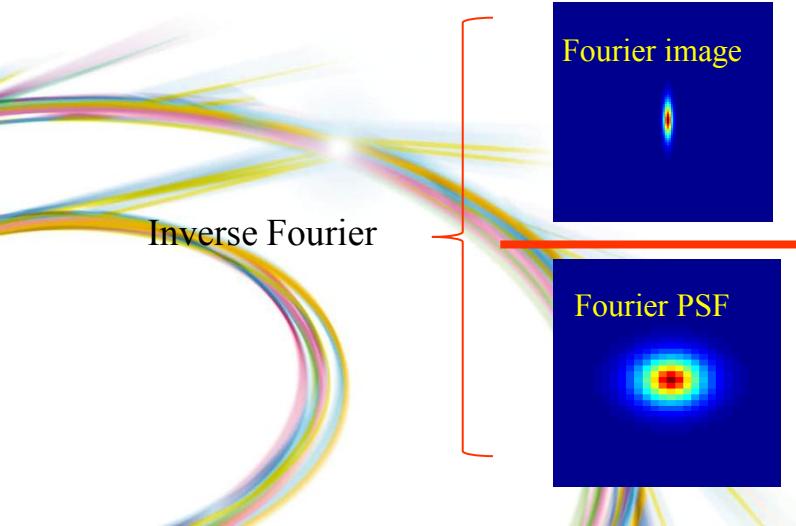
object



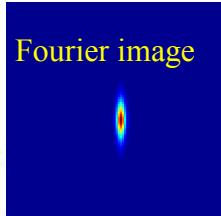
imaging system:
PSF



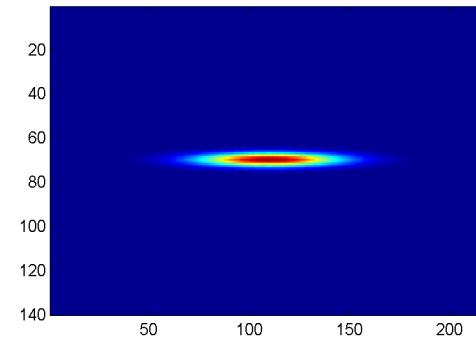
image



Inverse Fourier



Fourier PSF



object

Deconvolution and Noise Limitation

- Major Problem: Noise in the image

$$g(x,y) = h(x,y) \otimes o(x,y) + n(x,y)$$

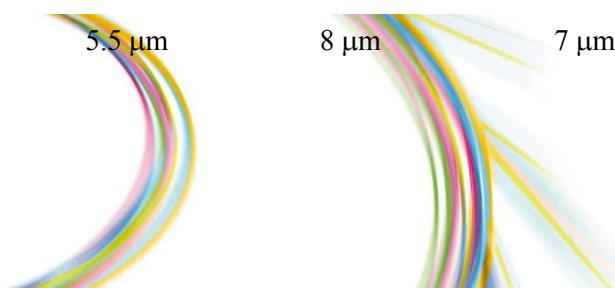
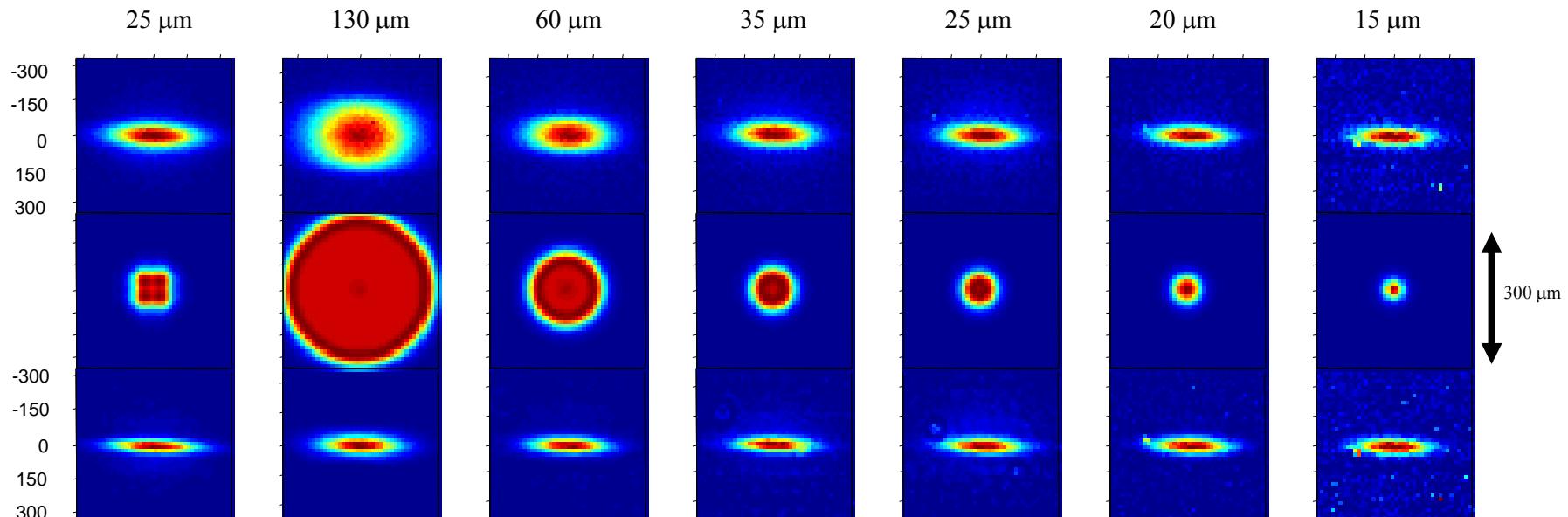
in the Fourier space:

$$G(v,\eta) = H(v,\eta) O(v,\eta) + N(v,\eta)$$

- Solution: introduce a noise filter in the deconvolution algorithm
 - Example: Wiener filter:
 - » the algorithm seek an estimate $o(x,y)$ that minimises the statistical error function $|g - F^{-1}(G ./ H + N)|^2$ and in which a low pass filter is introduced
- Other solution: iterative nonlinear algorithm
 - Example Lucy-Richardson:
 - » based on maximum-likelihood formulation in which the image is modelled with Poisson statistics
 - » Rapid convergence to the real solution:
 - » G. Zech, doi <http://dx.doi.org/10.1016/j.nima.2013.03.026>

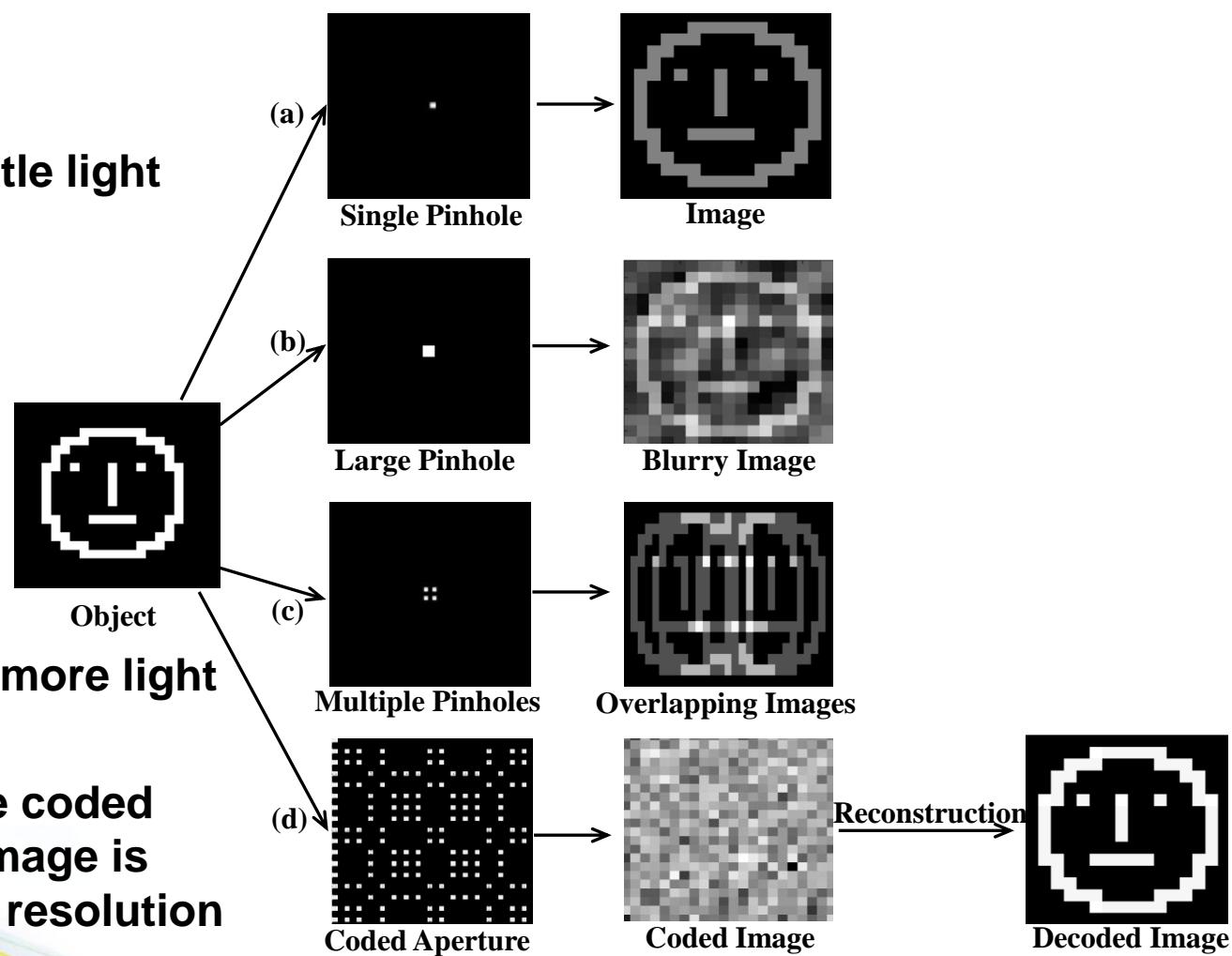
Deconvolved beam size with a range of defined apertures

- Vertical emittance $\varepsilon \approx 1.3 \text{ pm.rad}$, $\sigma \approx 5.5 \mu\text{m}$



- **Small pinhole allows little light**
→ inefficient
- **Several pinholes allow more light**
→ overlapping images

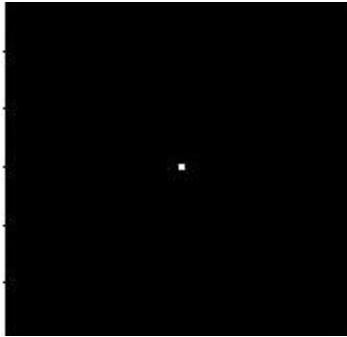
By choosing a suitable coded aperture pattern the image is decoded with a better resolution





Numerous Coded Aperture Patterns

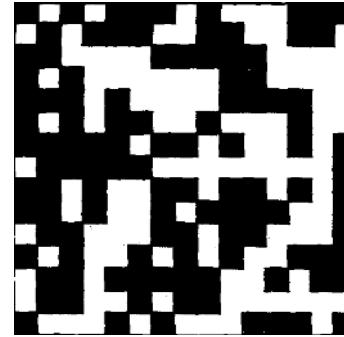
Courtesy of A. Haboub



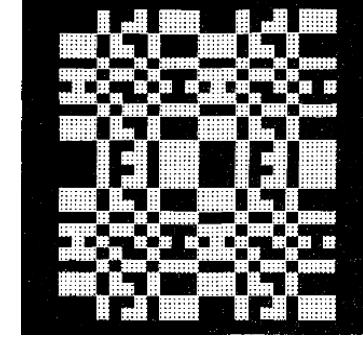
Pinhole



Fresnel Zone Plate (FZP)

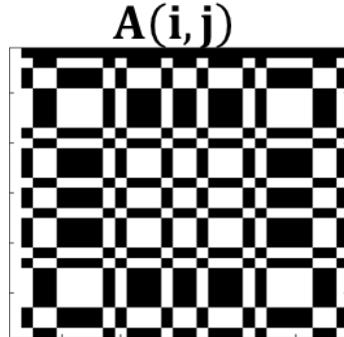


random mask



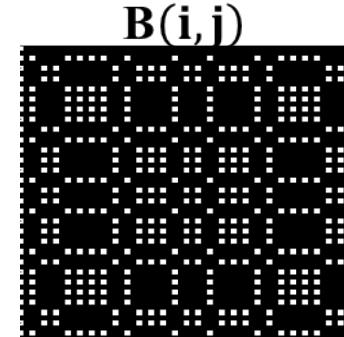
URA mask

MURA
50% open area



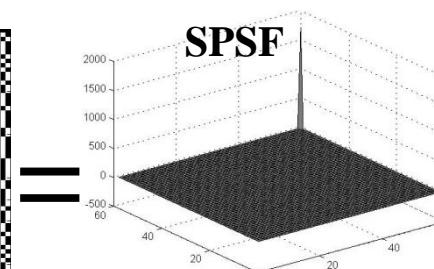
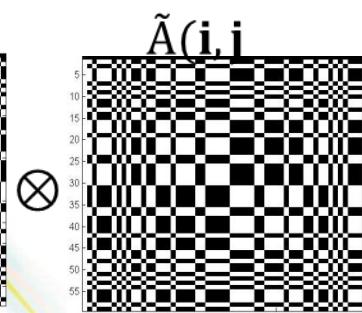
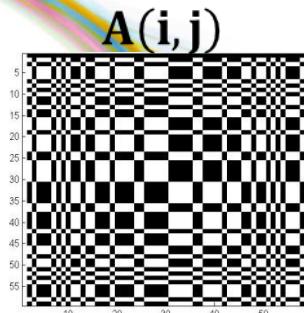
Modified Uniformly
Redundant Array (MURA)

$$\begin{aligned} B &= \text{kron}(A, h) \\ h &= \text{zeros}(2) \\ h(1, 1) &= 1 \end{aligned}$$



Non Two Holes
Touching (NTHT)

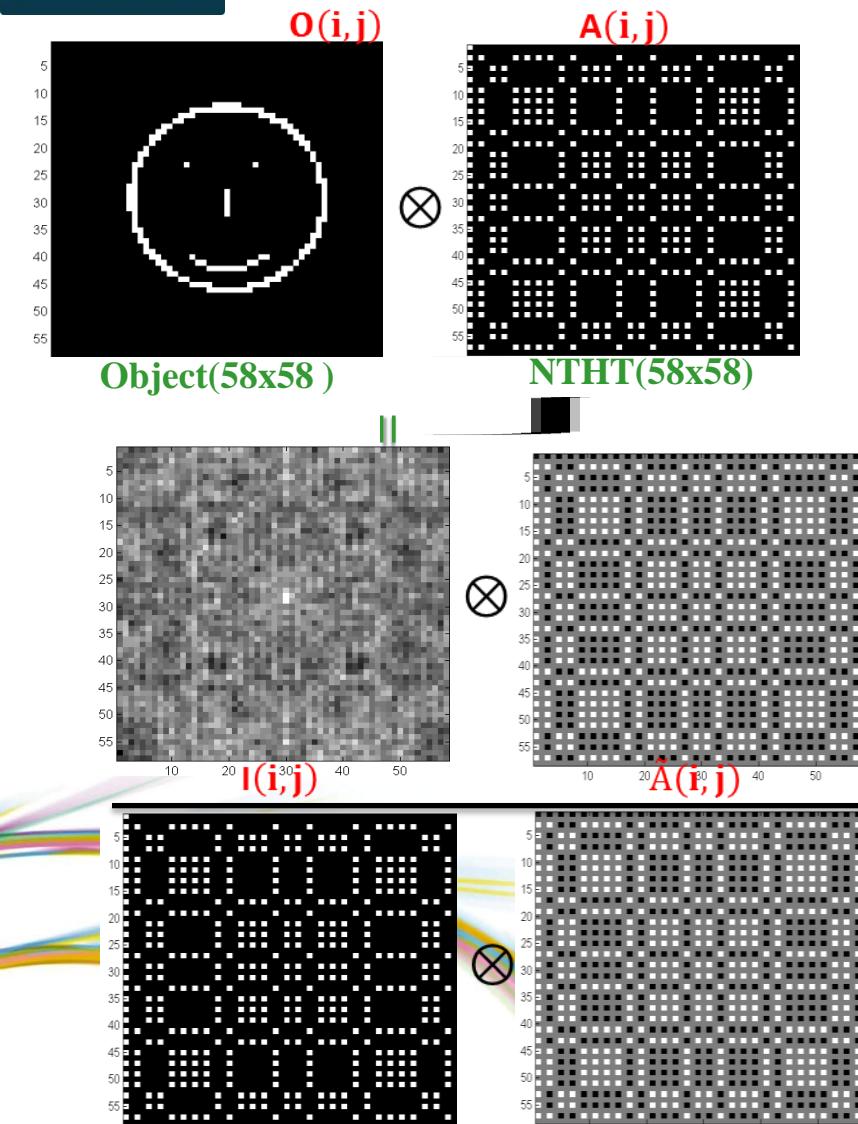
NTHT MURA
0.4% open area



$A(i, j) \otimes \tilde{A}(i, j) = \delta$


Coded aperture imaging simulation

Courtesy of A. Haboub



$$I(i,j) = O(i,j) \otimes A(i,j) \quad (1)$$

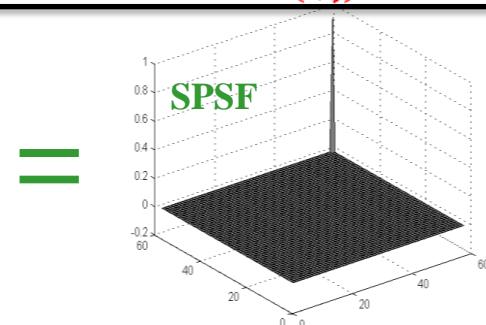
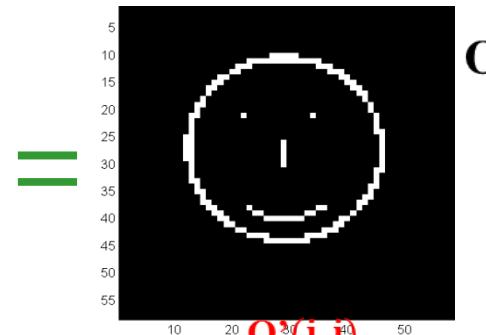
The detected flux at pixel j and k is:

$$I_{jk} = \sum_l \sum_k A_{j+l, k+l} O_{li} \quad (2)$$

By deriving \tilde{A} : $\tilde{A} = \text{ifft2}(1./\text{fft2}(A)) \quad (3)$

The reconstructed image O' is:

$$O'(i,j) = I(i,j) \otimes \tilde{A}(i,j) \quad (3)$$



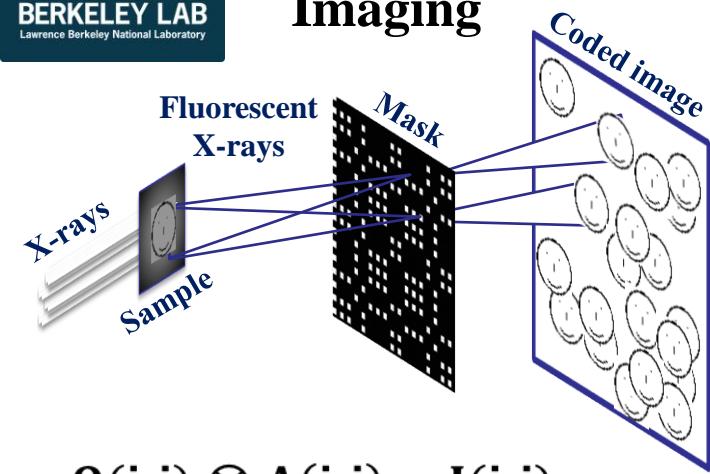
$$A(i,j) \otimes \tilde{A}(i,j) = \delta \quad (4)$$

For cosmic rays, Coded aperture imaging using NTHT works with simple convolution because the coded image and NTHT pattern has the same size.



Simulation of the image reconstruction from Coded Aperture Imaging

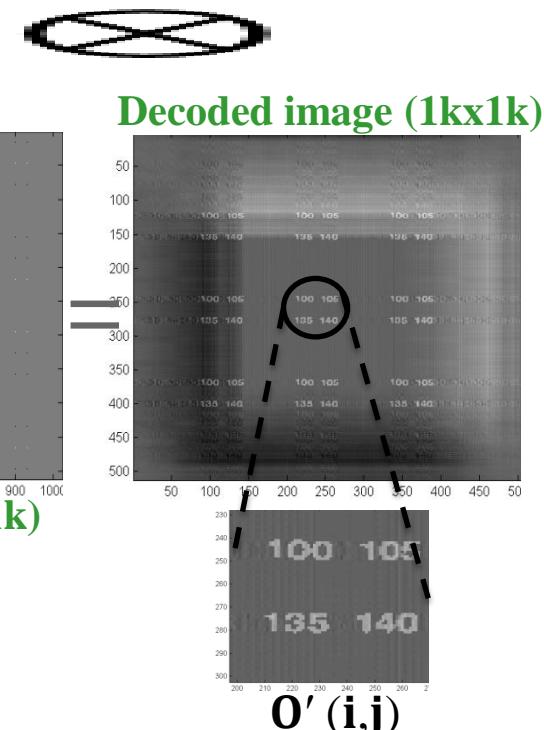
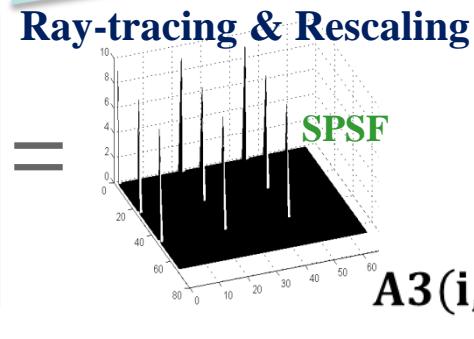
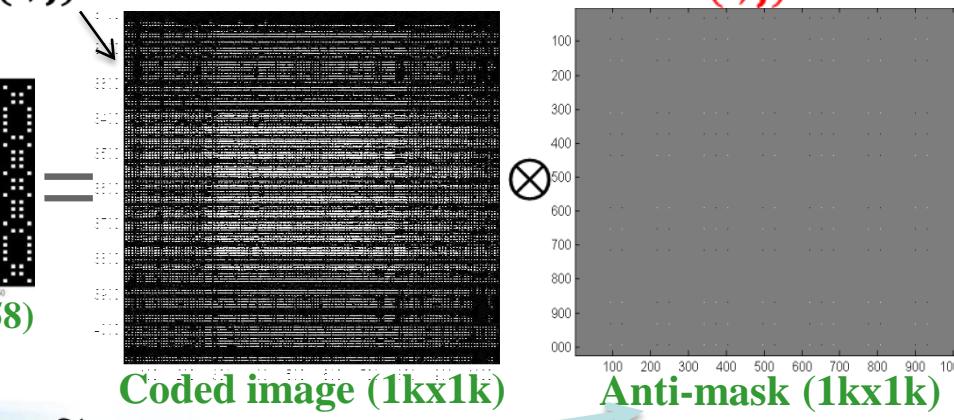
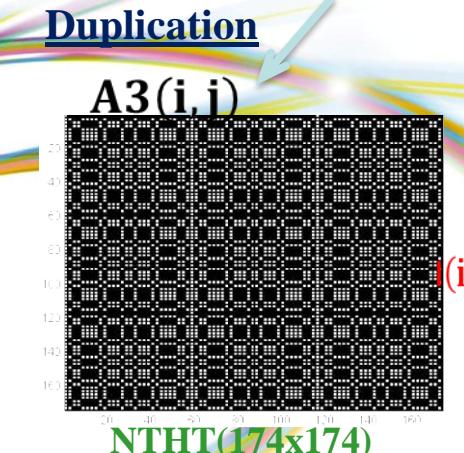
Courtesy of A. Haboub



$$O(i,j) \otimes A(i,j) = I(i,j)$$

Object (60x60)

NTHT (58x58)



 diamond

Coded Aperture Measurement Principles

- Coded Aperture Imaging:

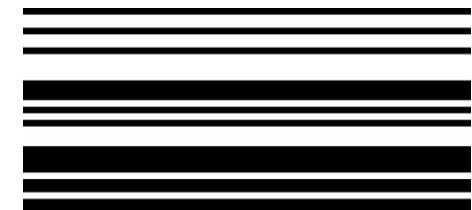
- Technique developed by x-ray astronomers using a mask to modulate incoming light. Resulting image must be deconvolved through mask response (including diffraction and spectral width) to reconstruct object.
- Open aperture of 50% gives high flux throughput for bunch-by-bunch measurements. Heat-sensitive and flux-limiting monochromator not needed.
 - We need such a wide aperture, wide spectrum technique for shot-by-shot (single bunch, single turn) measurements.

- URA (Uniformly Redundant Array) mask

- Pseudo-random pattern gives relatively flat spatial frequency response.
- In noiseless, geometric limit, detector image can in principle be inverted directly to give source profile
- Unfortunately, we don't operate in that limit.
- Need something like recursive or template fitting.
 - In this talk will discuss latter approach.

R.H. Dicke, Astrophys. Journ., 153, L101, (1968).

E.E. Fenimore and T.M. Cannon,
Appl. Optics, V17, No. 3, p. 337
(1978).



What the detector sees

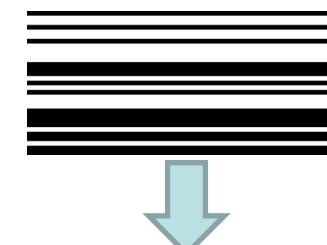
- Source SR wavefront amplitudes:

$$\begin{bmatrix} A_\sigma \\ A_\pi \end{bmatrix} = \frac{\sqrt{3}}{2\pi} \gamma \frac{\omega}{\omega_c} (1 + X^2) (-i) \begin{bmatrix} K_{2/3}(\eta) \\ \frac{iX}{\sqrt{1+X^2}} K_{1/3}(\eta) \end{bmatrix},$$

where

$$X = \gamma\psi,$$

$$\eta = \frac{1}{2} \frac{\omega}{\omega_c} (1 + X^2)^{3/2},$$



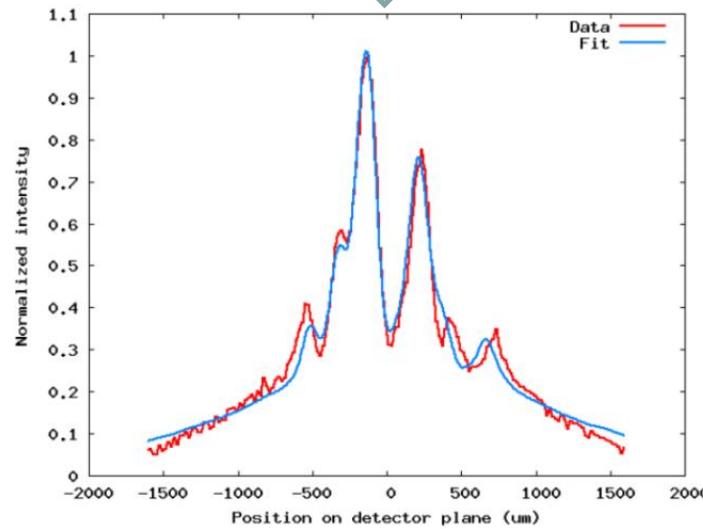
K.J. Kim, AIP Conf. Proc. 184 (1989).

J.D. Jackson, "Classical Electrodynamics," (Second Edition), John Wiley & Sons, New York (1975).

- Kirchhoff integral over mask (+ detector response)
- Detected pattern:

$$A_{\sigma,\pi}(Detector) = \frac{iA_{\sigma,\pi}(Source)}{\lambda} \times \int_{mask} \frac{t(y_m)}{r_1 r_2} e^{\frac{i2\pi}{\lambda}(r_1 + r_2)} \left(\frac{\cos \theta_1 + \cos \theta_2}{2} \right) dy_m$$

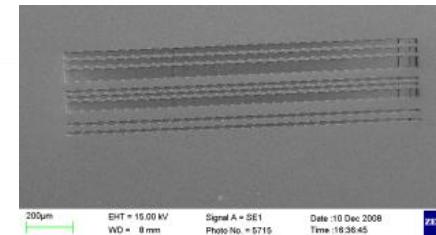
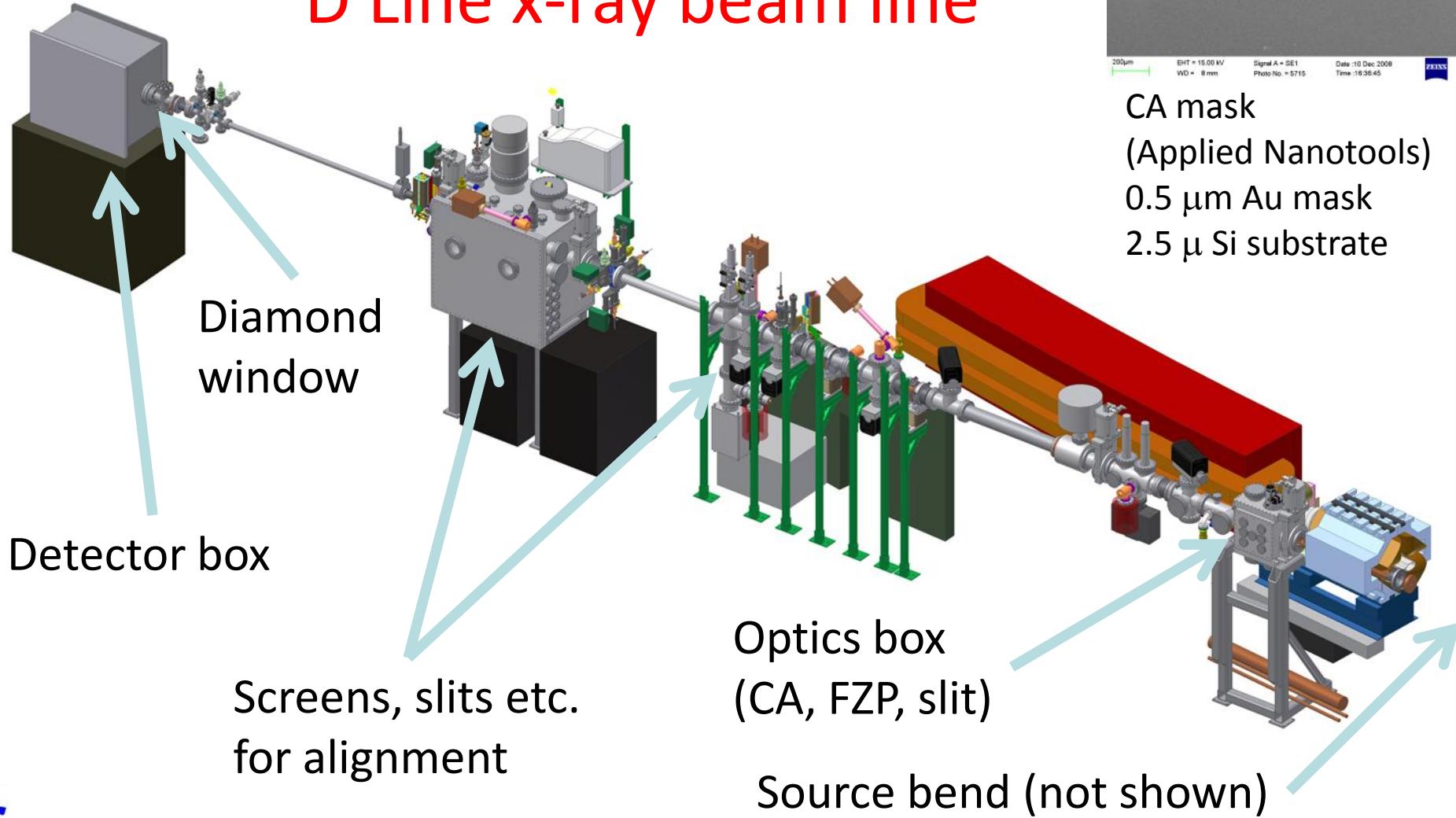
- $t(y_m)$ is complex transmission of mask element at y_m .
- Sum intensities of each polarization and wavelength component.
- Sum weighted set of detector images from point sources.
 - The source beam is considered to be a vertical distribution of point sources.
 - Can also be applied to sources with non-zero angular dispersion and longitudinal extent, for more accurate simulation of emittance and source-depth effects.
 - For machines under consideration here these effects are small, so for computational speed we restrict ourselves to 1-D vertical distributions.



Measured slow-scan detector image (red) at CesrTA, used to validate simulation (blue)

Measurements at CesrTA

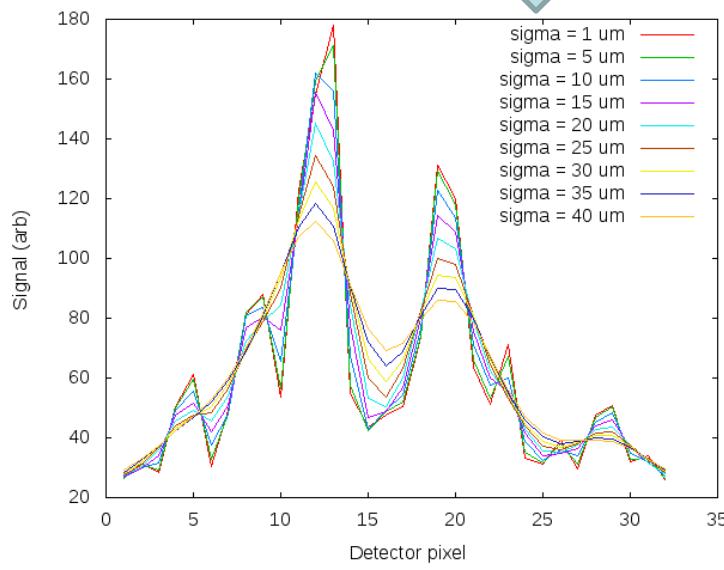
D Line x-ray beam line



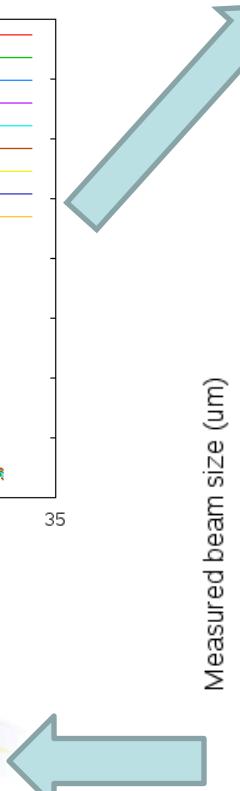
CA mask
(Applied Nanotools)
0.5 μ m Au mask
2.5 μ Si substrate

10 μm , 31-element CA mask @ D Line 2 GeV

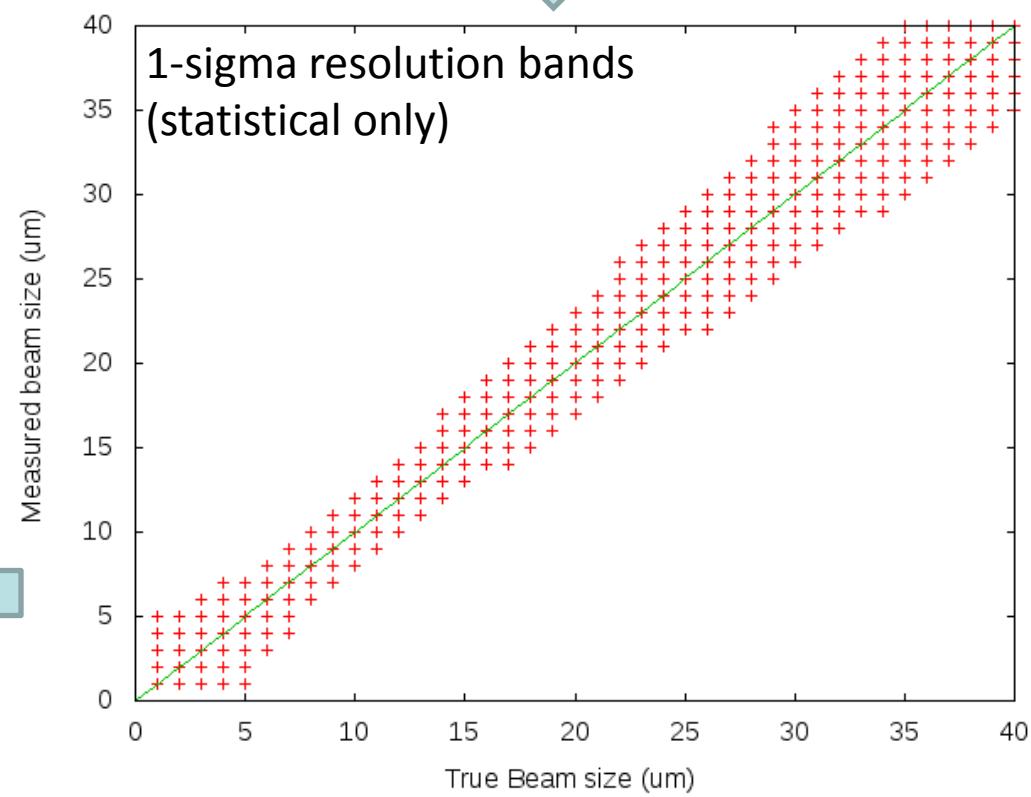
Generate detector images for various beam sizes:



Statistical single-shot resolution at 10 μm beam size = +/- ~2 μm
(Assuming ideal detector.)

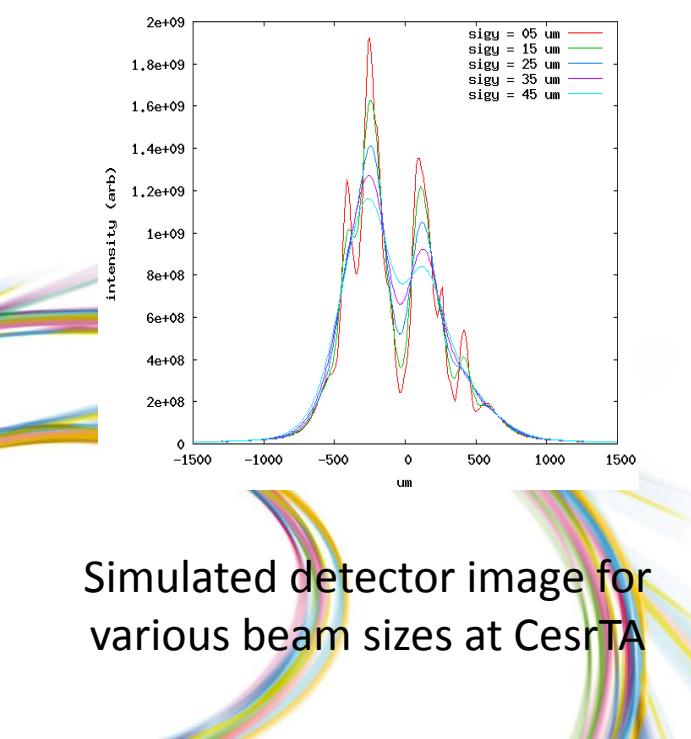


Cross-fit between beam sizes.
Plot 1-sigma statistical confidence regions,
Assuming 200 photons/pixel average
(=> 0.56 mA at 2 GeV):

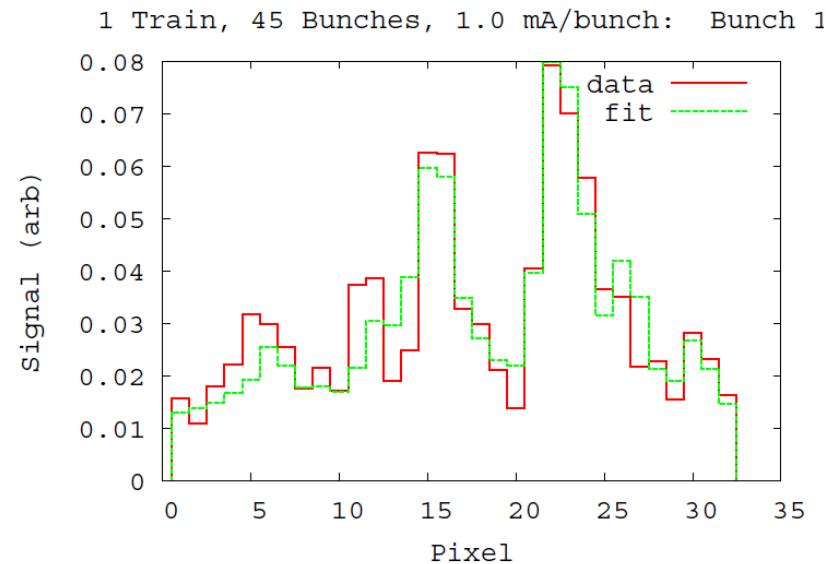


Data Analysis

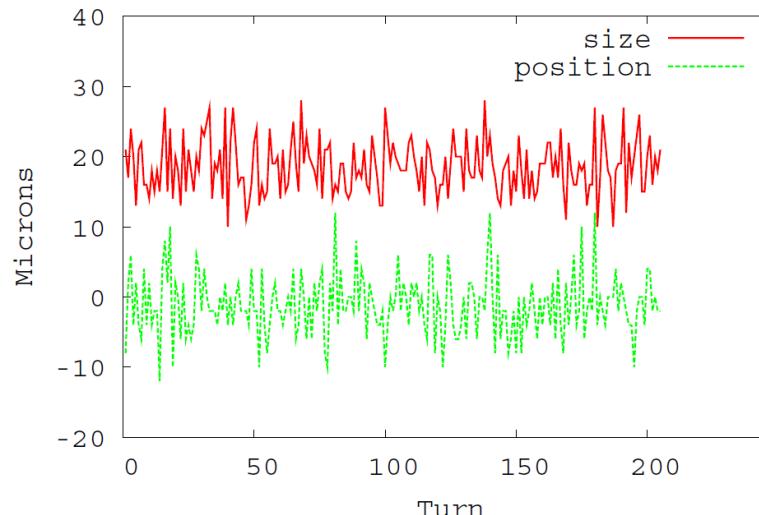
- 1) Simulate point response functions (PRFs) from various source positions to detector, taking into account beam spectrum, attenuations and phase shifts of mask and beamline materials, and detector response.
- 2) Add PRFs, weighted to possible proposed beam distributions.
- 3) Find best fit to detector data.



Simulated detector image for various beam sizes at CesrTA



Example of single-shot data
(single-bunch, single-turn)

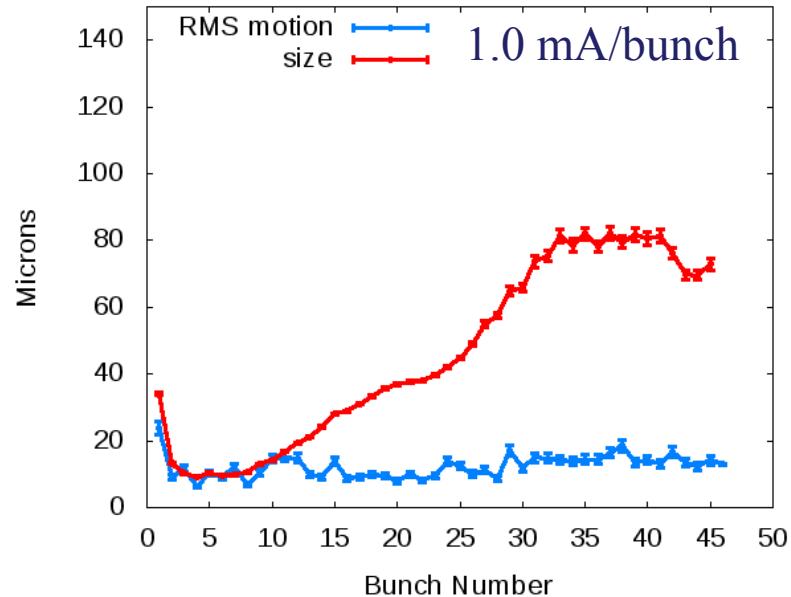
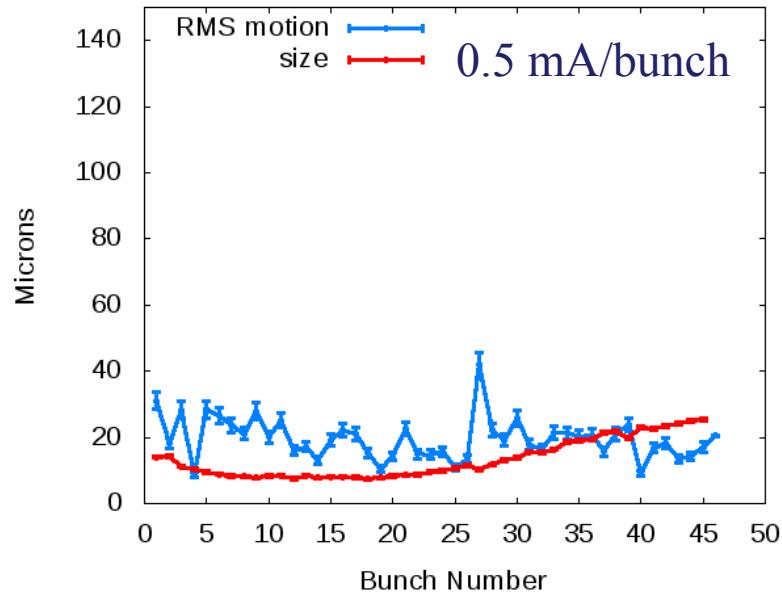


Example of turn-by-turn data (one bunch out of train)

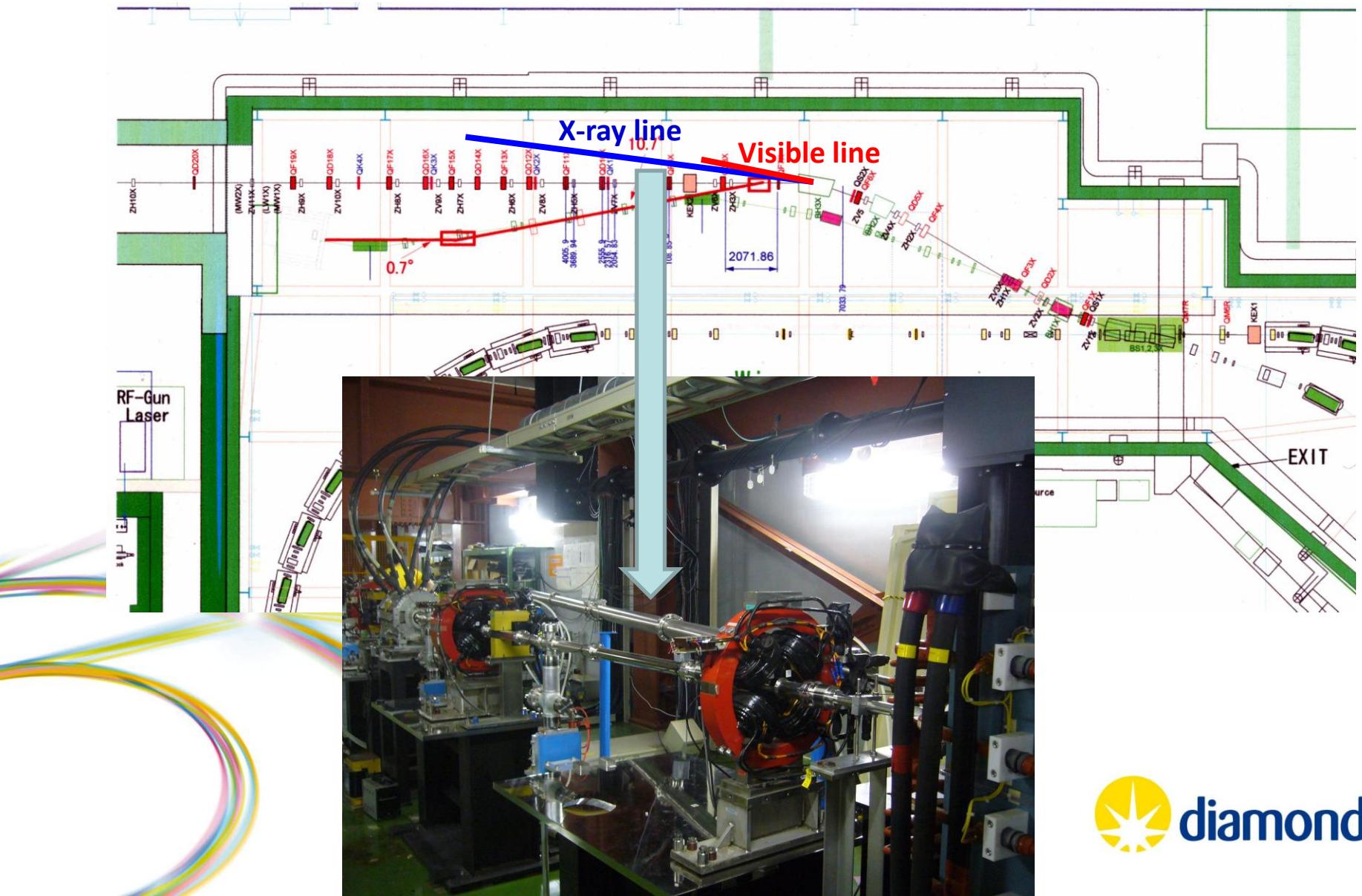
amond

Electron-cloud study data

- Study of how of electron clouds change bunch-by-bunch beam sizes along a train.
- Beam sizes down to $\sim 10 \mu\text{m}$ have been measured at CesarTA.

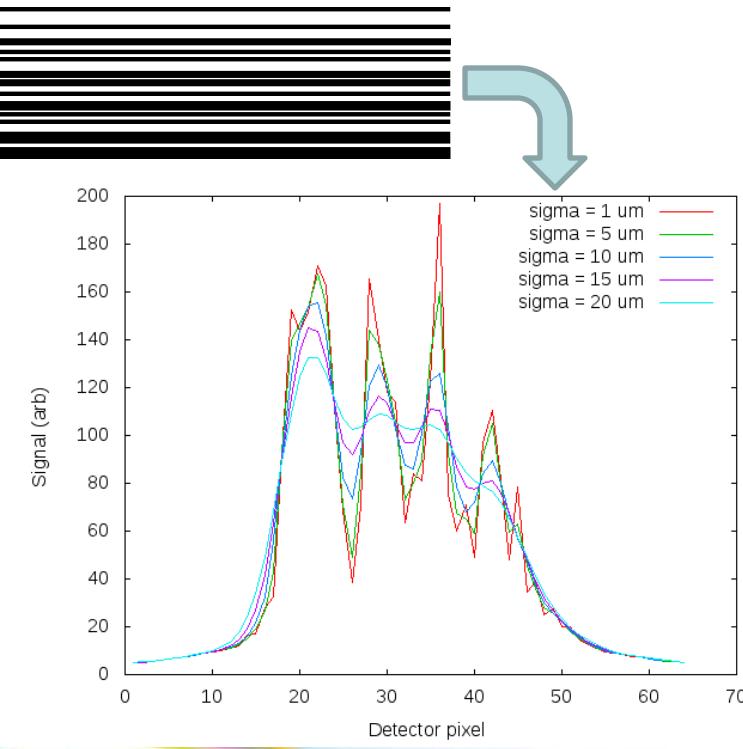


Coded Aperture tests at ATF2



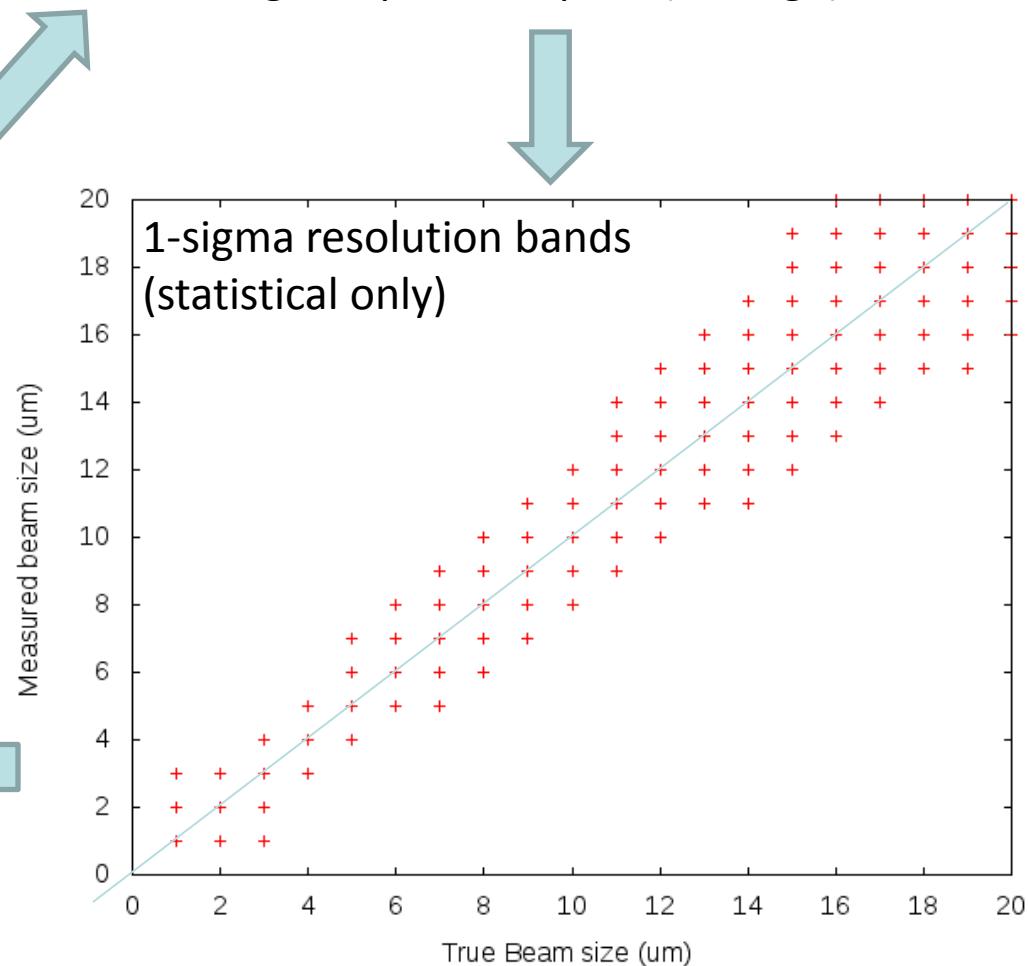
47-element, 5 $\mu\text{m}/\text{element}$ URA mask @ ATF2

Generate detector images for various beam sizes:



Statistical single-shot resolution at 4 μm beam size
= $\pm \sim 1 \mu\text{m}$
(Assuming ideal detector.)

Cross-fit between beam sizes.
Plot 1-sigma statistical confidence regions,
Assuming 200 photons/pixel (average):



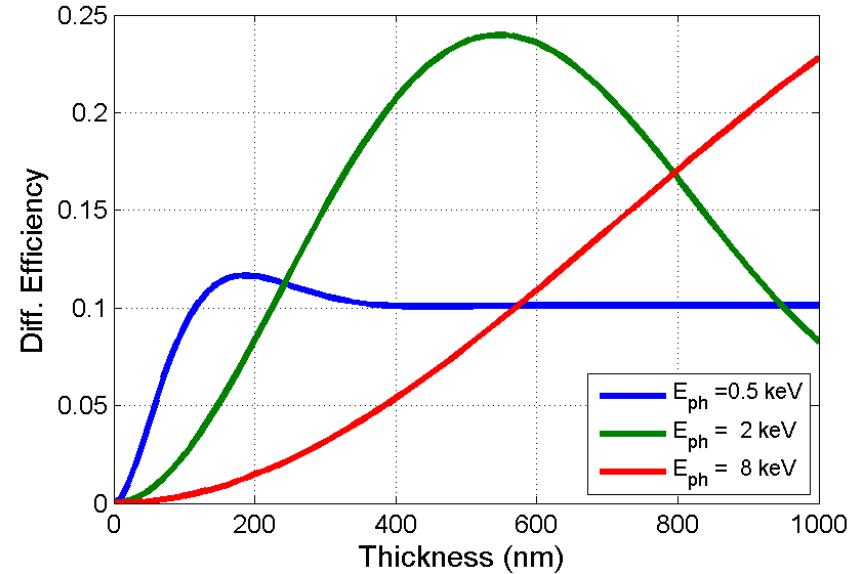
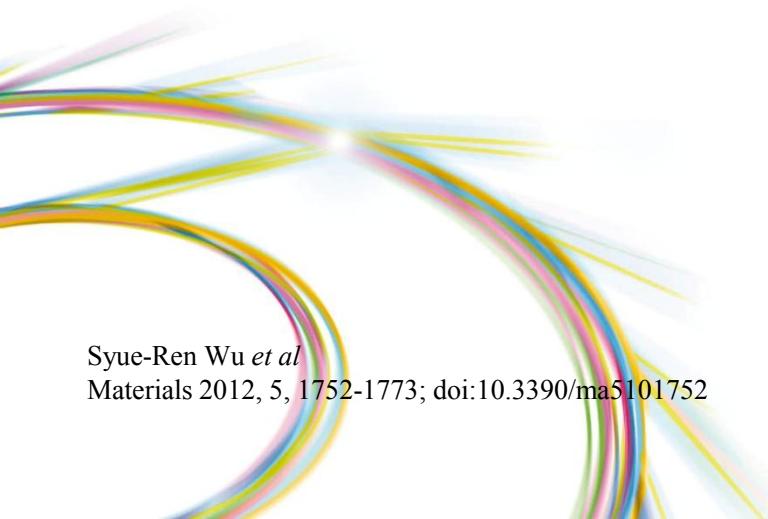
Coded Apertures

- Fresnel Zone Plate:
 - Construction:
 - Alternating zones from opaque to transparent with their radii r_n as:
$$r_n^2 = n \lambda f + n^2 \lambda^2 / 4$$
 - Resolution:
 - $R = 1.22 \Delta r_N$
 - Fraction of power focussed (classical expression based on 100% absorption and 100% transmission):
 - $E = 1/(q \pi)^2$, $q = 1, 2, 3, \text{etc.}$ and $E = 0.25$ for $q=0$
 - First order max diffraction efficiency: 10.3%

- Performance of FZP
 - Improved performance by the choice of material and also manufacture process
 - Resolution: Δr outer rings radii difference
 - Depth of field: $1 / NA^2$
 - Efficiency: material and thickness
 - Aberrations: imperfection of the lens, NA
- Construction tolerance:
 - resolution and efficiency: high aspect ratio

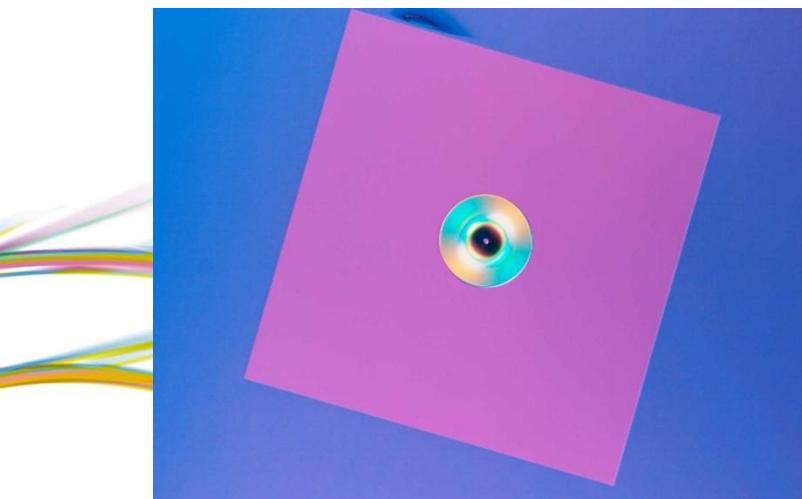
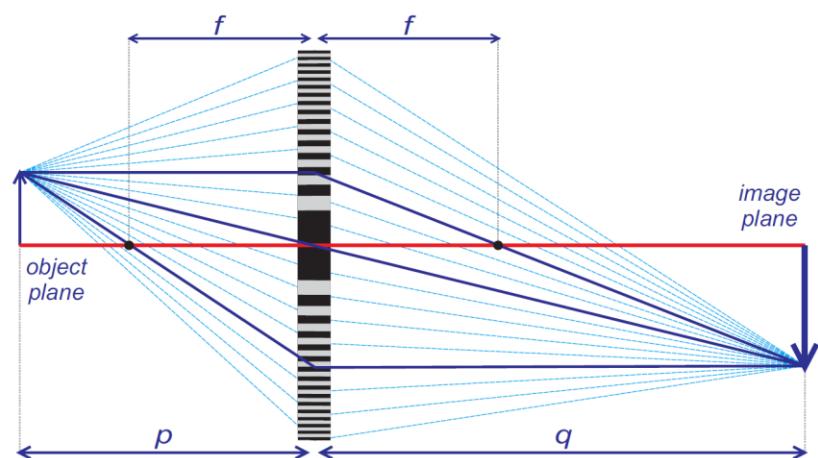
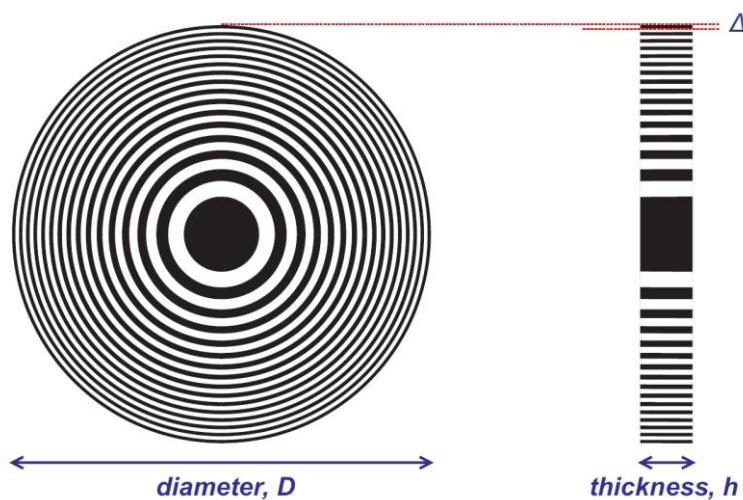
- FZP diffraction efficiency for Au, taking into account phase effects of the absorbing material

$$E = \left(\frac{1}{\pi q} \right)^2 \left(1 + e^{-4\pi \frac{T\beta}{\lambda}} - 2e^{-2\pi \frac{T\beta}{\lambda}} \cos 2\pi \frac{T\delta}{\lambda} \right)$$

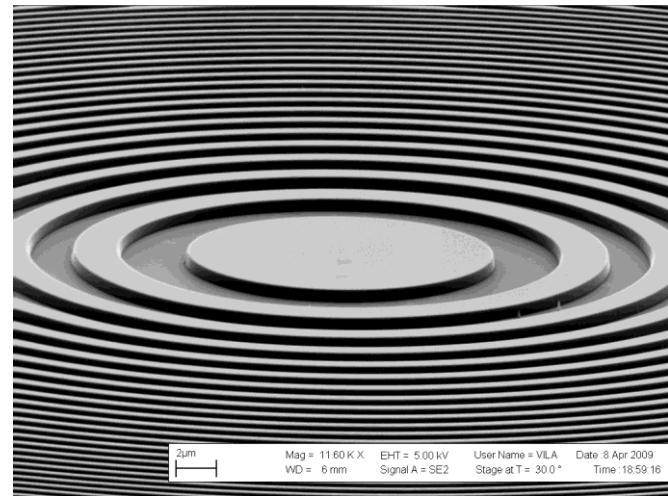


- Examples of FZP with X-ray beam
 - Beam size measurement: KEK, Spring8, etc
 - Achieved measured beam size, ATF-KEK: $4\mu\text{m}$
 - Beam focussed for X-ray experiment
 - Achieved image beam size: 20nm

Fresnel Zone Plates



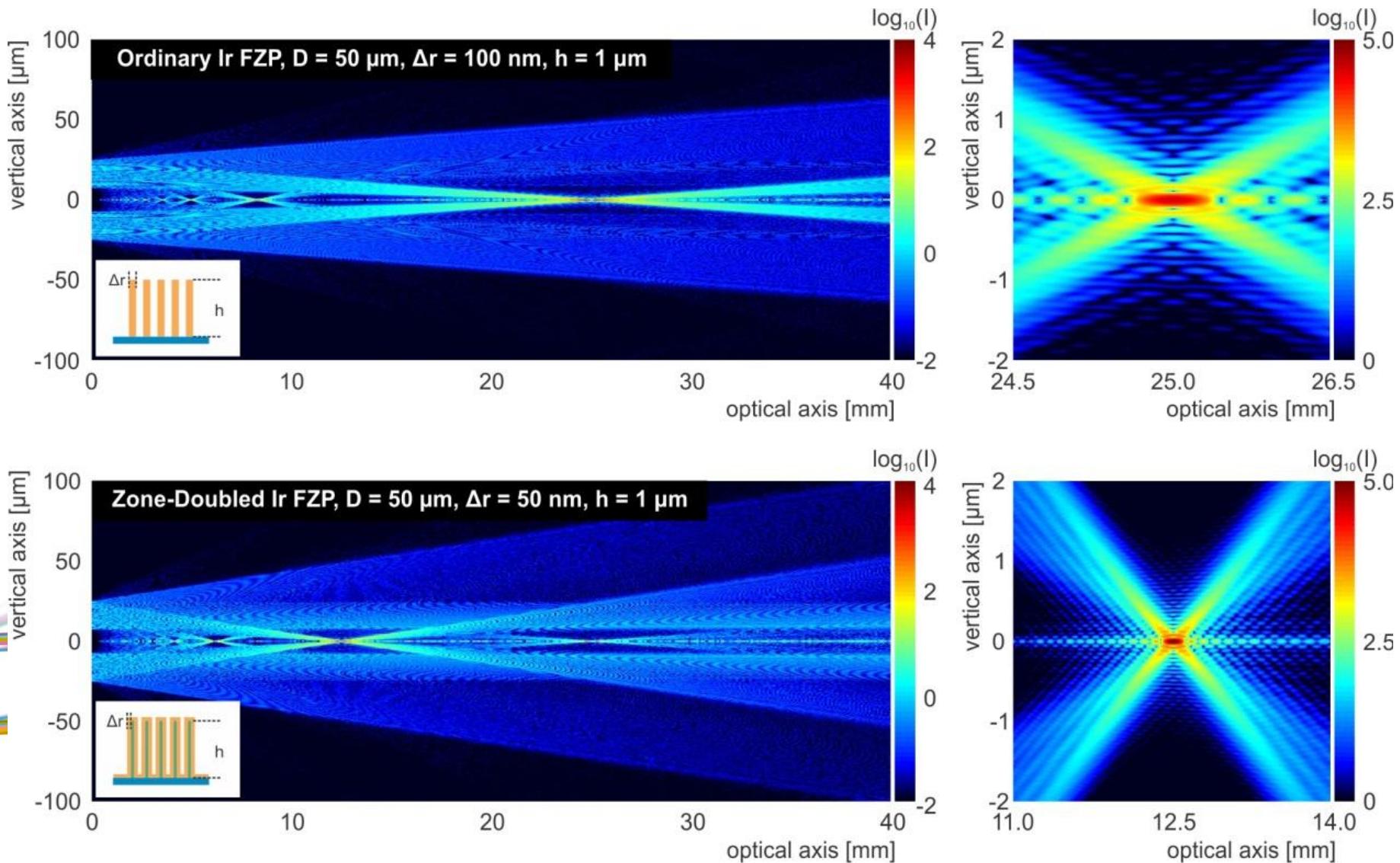
Fresnel zone plate on Si_3N_4 membrane



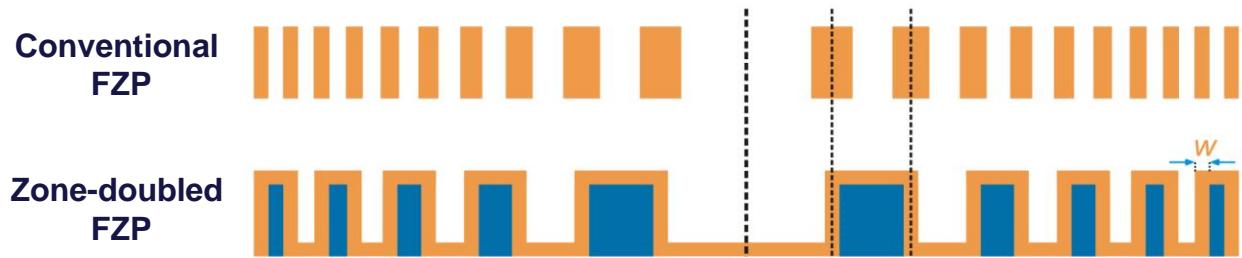
SEM image of Fresnel zone plate



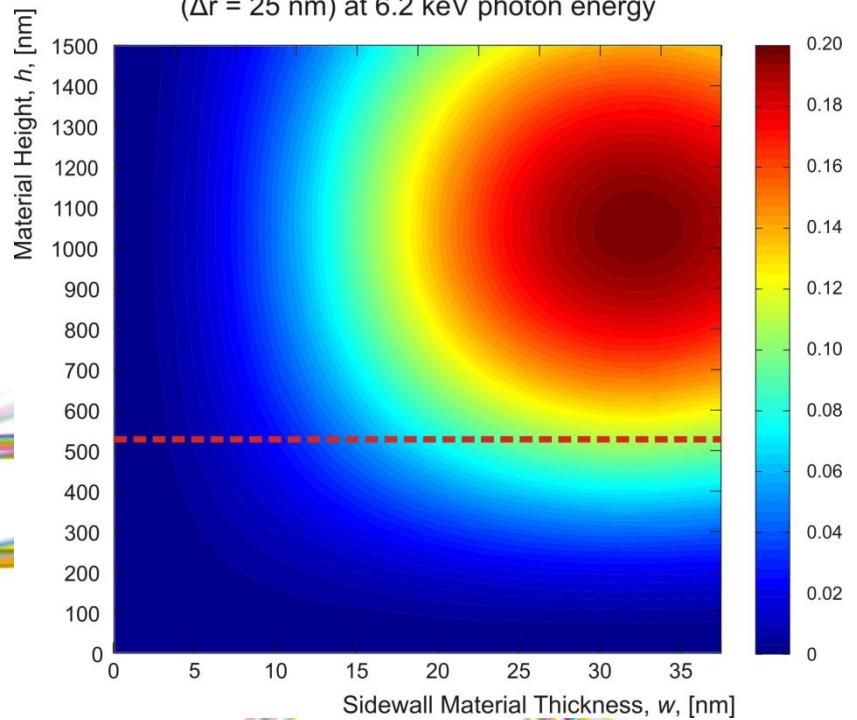
Fresnel Zone Plate Modeling: Zone-doubling



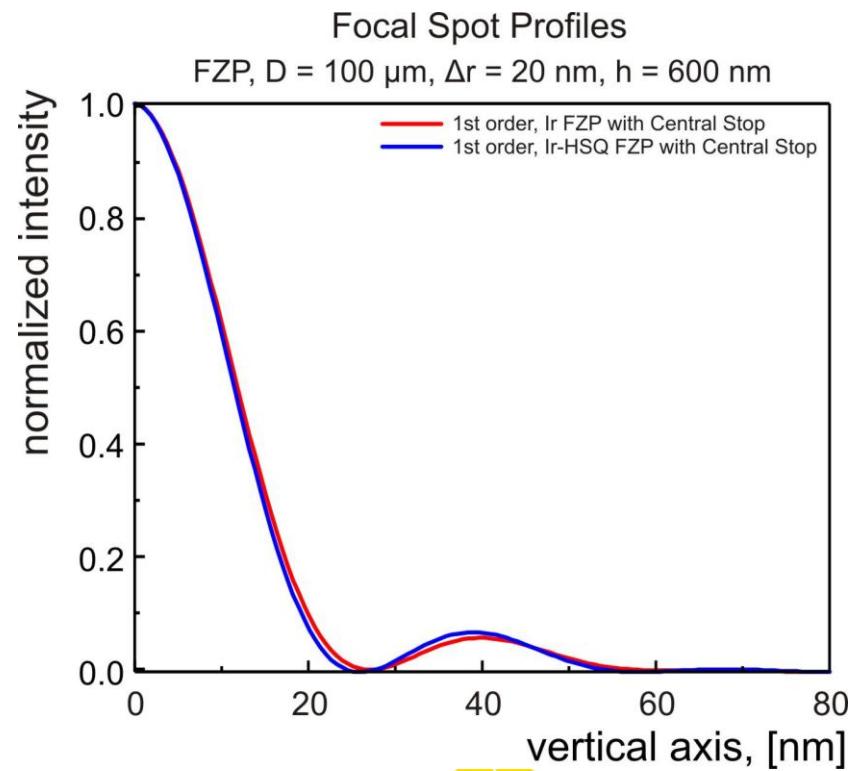
Fresnel Zone Plate Modeling: Zone-doubling



Diffraction Efficiency for an Ir-SiO₂ zone-doubled FZP
($\Delta r = 25$ nm) at 6.2 keV photon energy

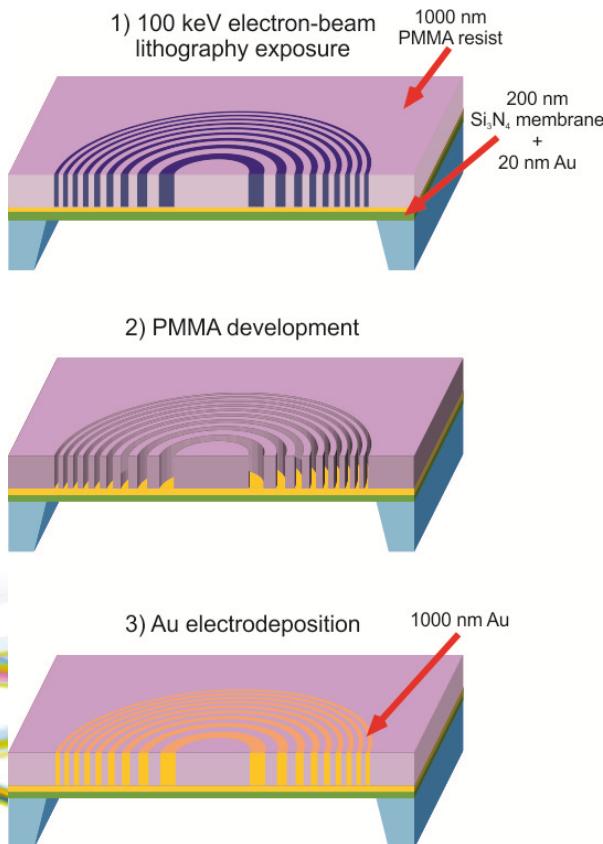


Focal Spot Profiles
FZP, D = 100 μ m, $\Delta r = 20$ nm, $h = 600$ nm



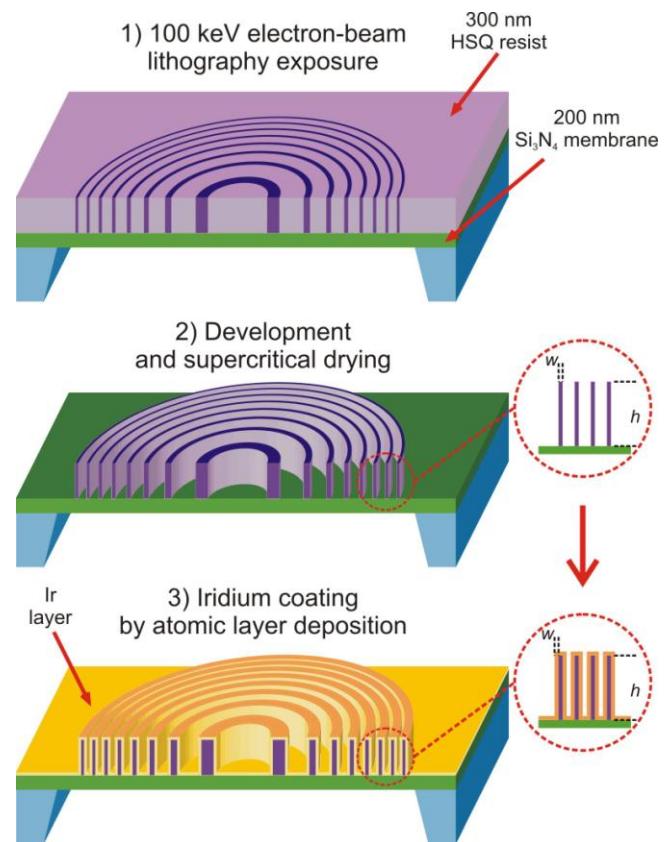
Nanofabrication techniques transferred to ANL-CNM from the Paul Scherrer Institut (Switzerland)

Au electroplating



S. Gorelick et al., Nanotechnology (2010)

Zone-doubling technique

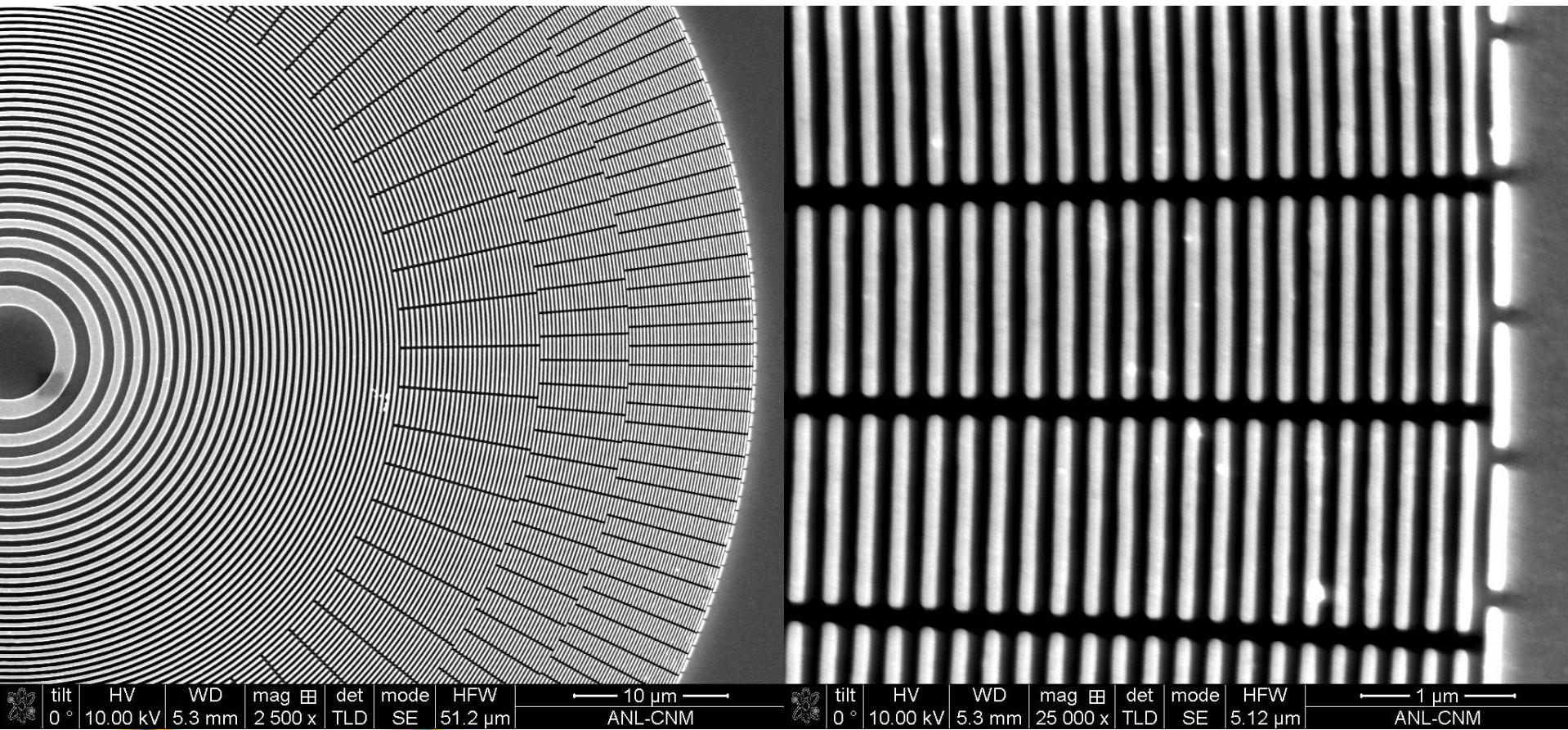


J. Vila-Comamala et al., Nanotechnology (2010)

J. Vila-Comamala et al., Optics Express (2011)

Au FZP for 8-12 keV photon energy

FZPs for sub 100-nm focusing



Au FZP, D = 100 μm , dr = 100 nm, t \sim 900 nm

20 nm Ir lines / 40 nm period and
after Ir ALD

Aspect Ratio of > 25
for 20 nm lines



200nm

Mag = 75.00 KX

WD = 10 mm

EHT = 10.00 kV

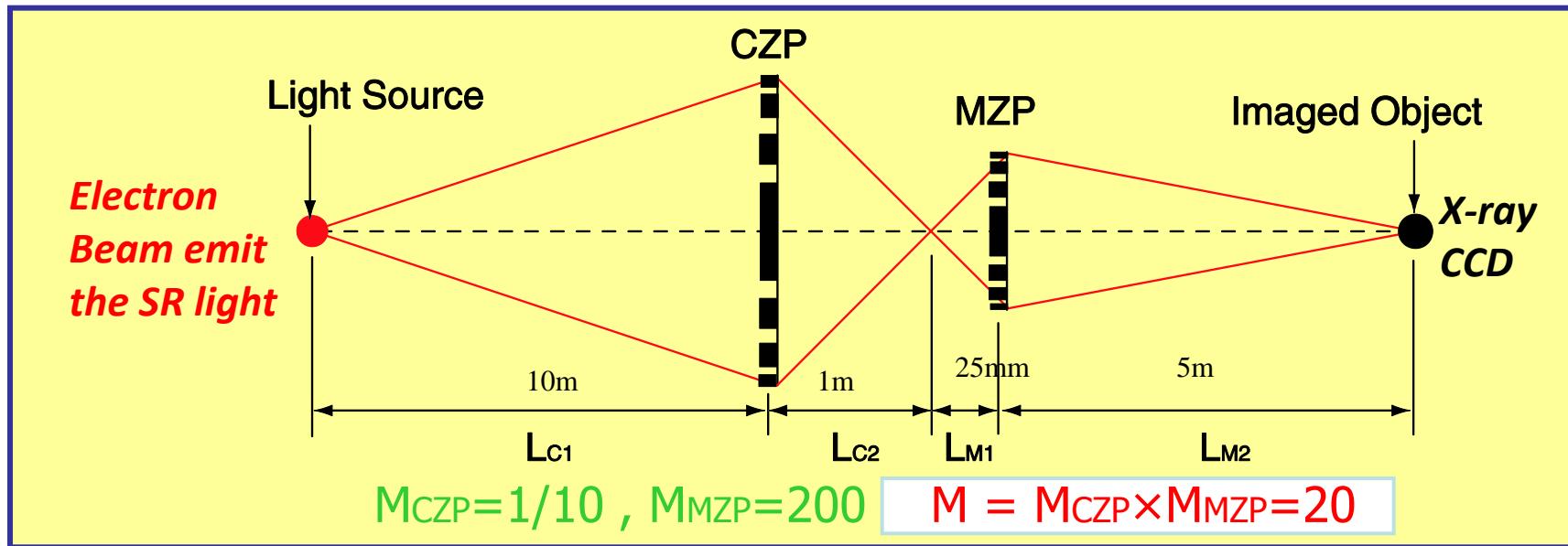
Signal A = SE2

User Name = VILA

Stage at T = 45.0 °

Date : 23 Oct 2010

Time : 16:03:21



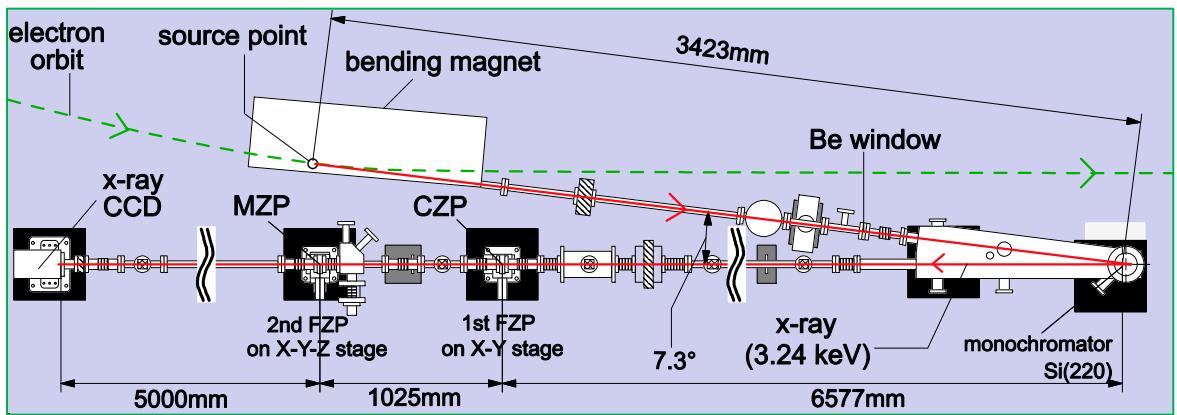
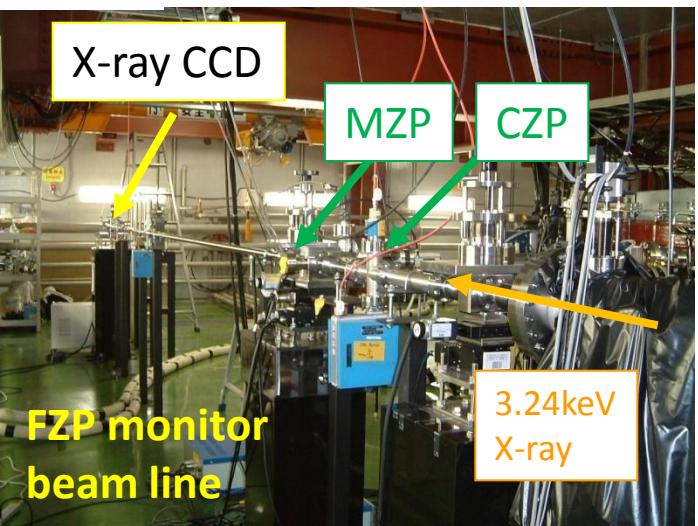
Expected spatial resolution

Features

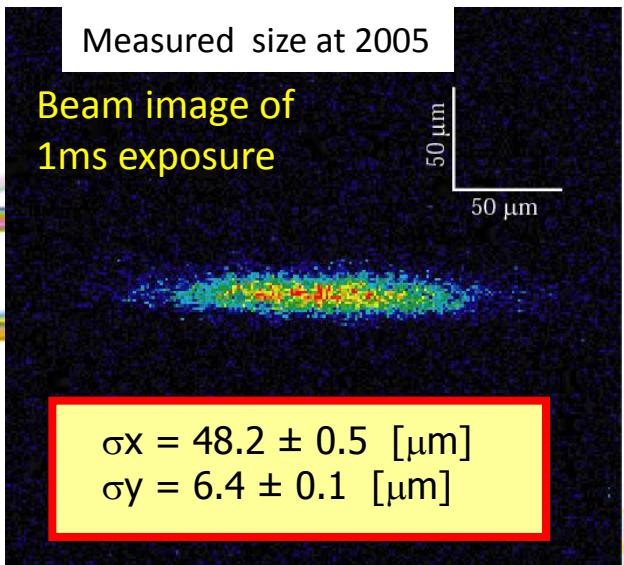
- 1) High spatial resolution ($<1 \mu\text{m}$)
- 2) Non-destructive measurement
- 3) 2-dimentional (x,y) beam profiling
- 4) Real time beam profile measurement ($<1\text{ms}$)

Parameters	Definition	Resolution(1σ)
Diffraction limit (3.235keV)	$\lambda/4\pi\sigma_{\text{SR}}$	0.24 $[\mu\text{m}]$
CZP ($\Delta r_N=116\text{nm}$)	$\sigma_{\text{CZP}} / M_{\text{CZP}}$	0.55 $[\mu\text{m}]$
MZP ($\Delta r_N=124\text{nm}$)	$\sigma_{\text{MZP}} / (M_{\text{CZP}} \times M_{\text{MZP}})$	0.002 $[\mu\text{m}]$
CCD (1 pixel= $24\mu\text{m} \times 24\mu\text{m}$)	$\sigma_{\text{CCD}} / (M_{\text{CZP}} \times M_{\text{MZP}})$	0.35 $[\mu\text{m}]$
Total	--	0.7 $[\mu\text{m}]$

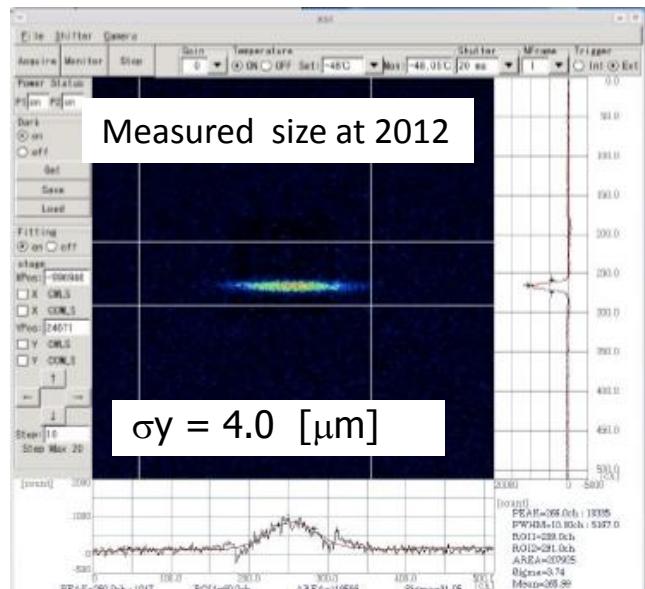
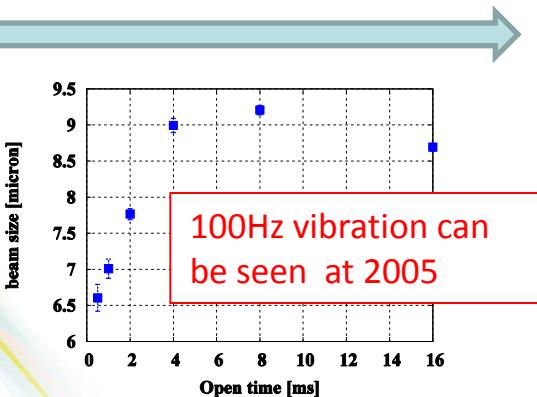
Setup



Results



Recently , by removing the vibration source come from air compressor near Si monochromator, 100Hz vibration disappeared and less than $4\mu\text{m}$ vertical beam size was measured.



CRL Lenses

- Principle:

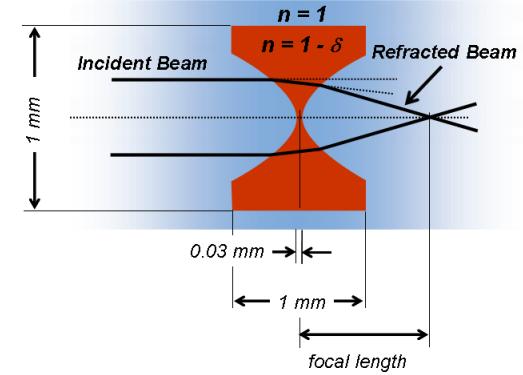
- Focal lens depends on material and wavelength λ :

$$F = \frac{R}{2N\delta}$$

$$\delta = \frac{r_0}{2\pi} \lambda^2 N_{at} \frac{mZ}{a^3}$$

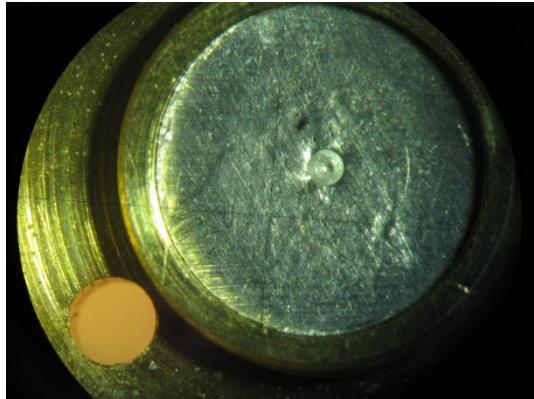
- Absorption: depends on material

- low Z material makes low absorption
 - high Z material makes short focal length

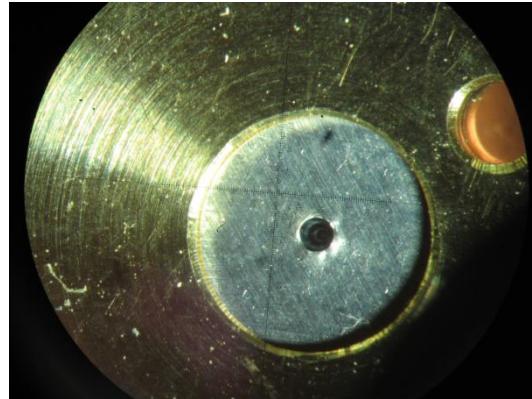


CRL Lenses

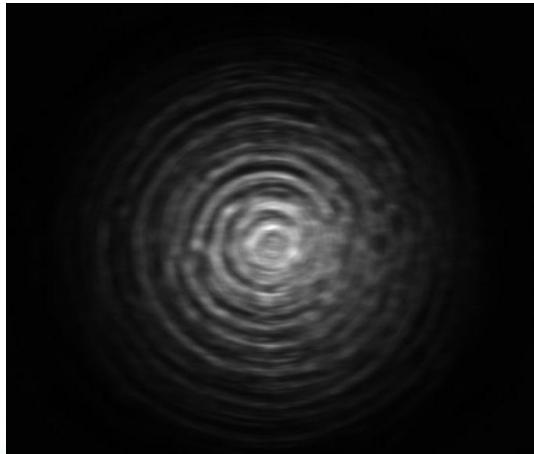
ESRF



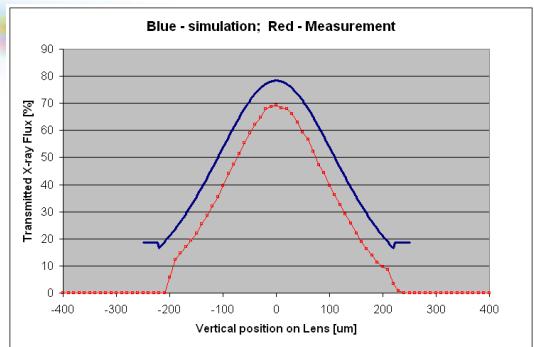
RWTH Aachen



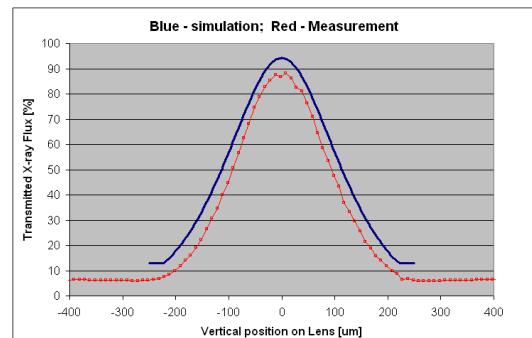
Microscope images



phase contrast imaging

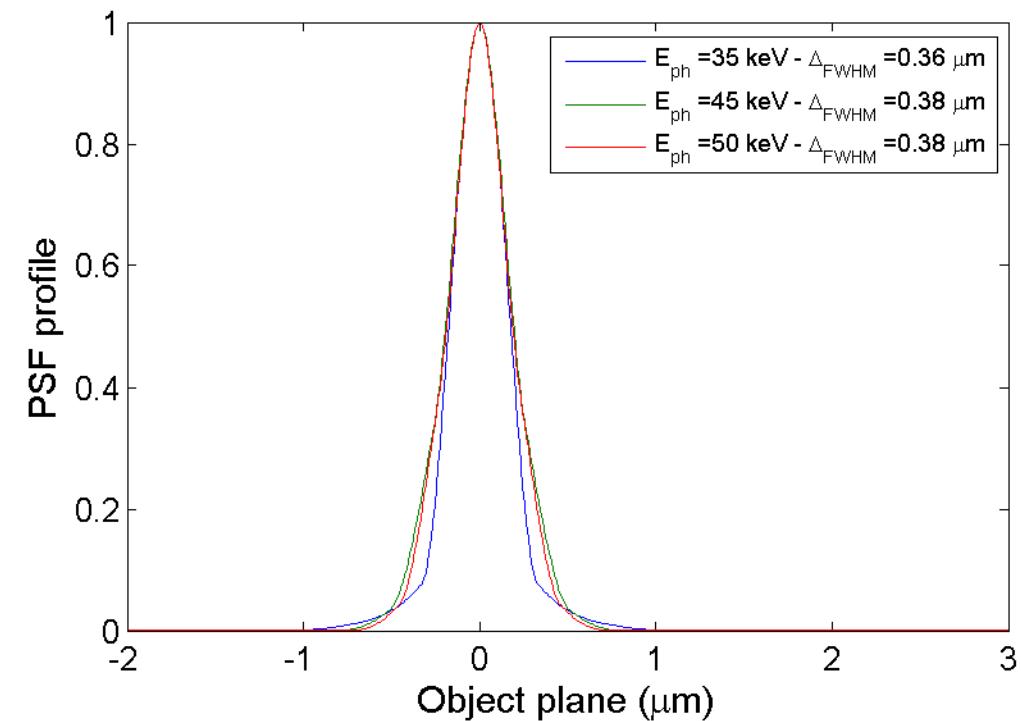


Measure and
computed lens aperture



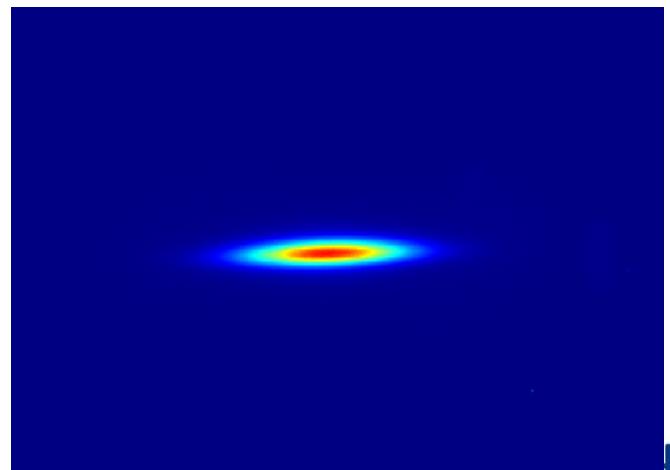
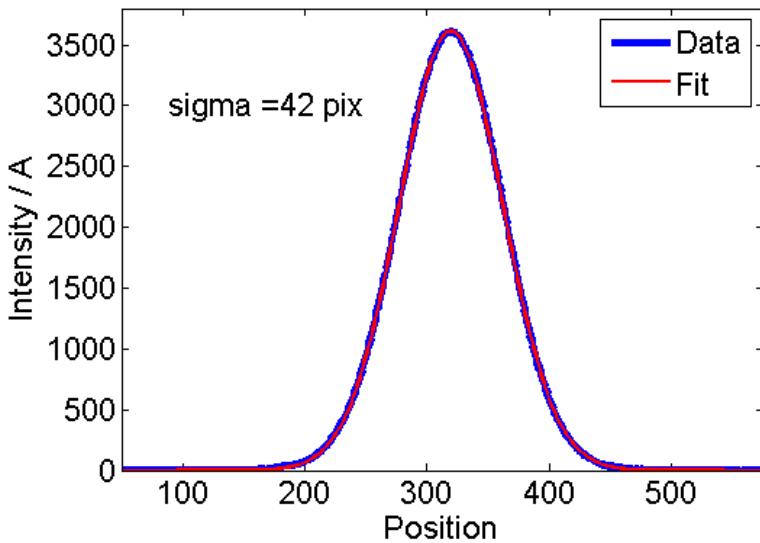
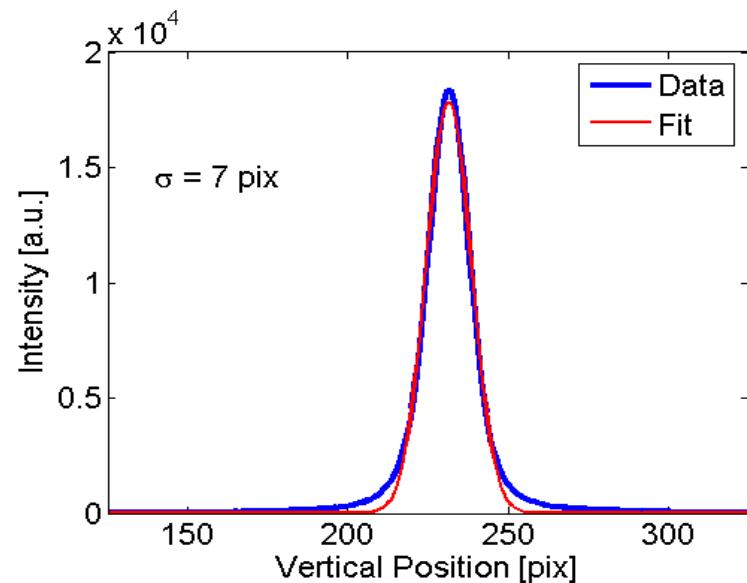
amond

- Resolution:
 - PSF from ‘perfect aperture’ calculated from absorption measurement



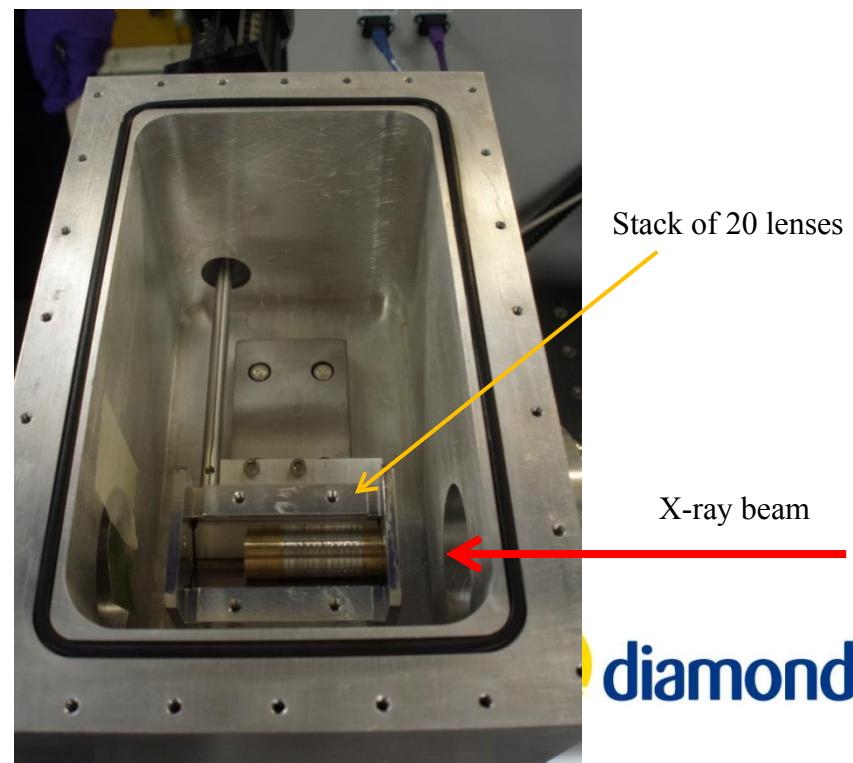
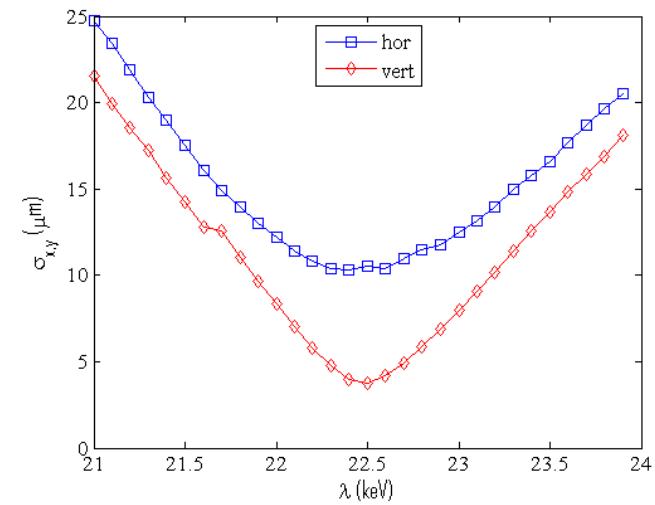
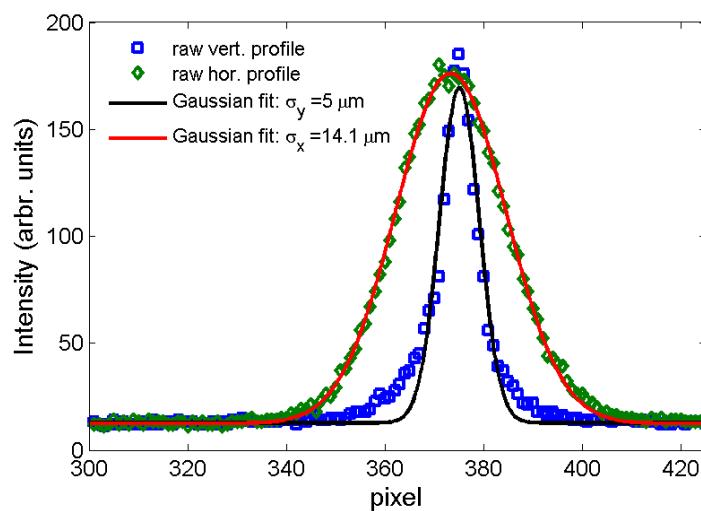
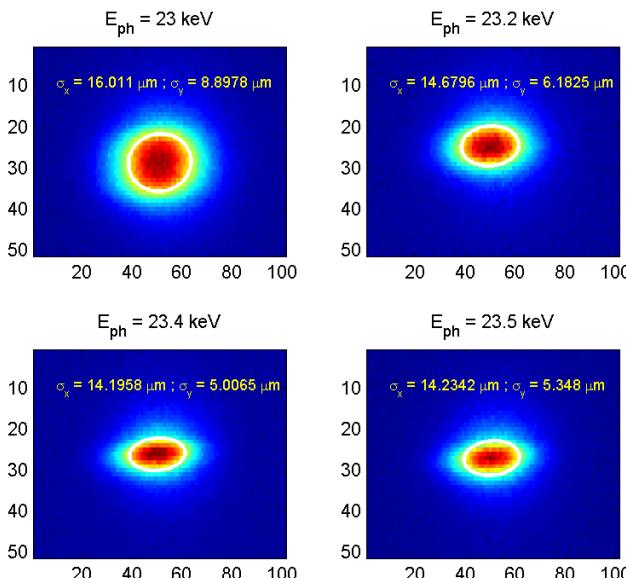
CRL Lenses

- ESRF beam
 - $\sigma_{x,y} = 84, 14 \mu\text{m}$
 - emittance: $\varepsilon_x \approx 4.5 \text{ nm}\cdot\text{rad}$
 - $\varepsilon_y \approx 5 \text{ pm}\cdot\text{rad}$



CRL Lenses

- Beamline I11 (Diamond)



Other Beam Profile Diagnostics

- Visible light, quasi-homogeneous source:
 - interferometer: $4.7 \mu\text{m}$ vertical beam size (T. Mitsuhashi - ATF KEK)
 - π -polarisation: $3.5 \mu\text{m}$ vertical beam size (V. Schlott- PSI)
- X-ray pinhole camera:
 - $5 \mu\text{m}$, (C Thomas – Diamond)

Commissioning, Operation, Cost, Performance

	Monochromatic	BM Resolution	Trans. Flux	Cost
CRL	Yes	Yes	Al ~80% of the illuminated aperture	+++
FZP	Yes	Yes	Max 25% of the illuminated aperture	+++
MURA	No	Yes/No	50% of the illuminated aperture	++
Pinhole camera	No	No	Fraction of the total flux	+
interferometer	Yes	Yes	Fraction of the total flux	+

Concluding remarks

- Sources reaching micron size in near future:
 - need to take into account the coherence of the source and more sophisticated model is needed to design profile monitors.
- Resolution of large aperture X-ray profile monitors can reach the natural resolution limit from the beam
 - Deconvolution can help to retrieve the real source profile: example of the X-ray pinhole showed that very small source size can be imaged with rather large aperture, assuming an accurate model of the PSF
- MURA etc., offer micron size resolution and high sensitivity, but processing of the image is required
- FZP and CRL have probably the best resolution, but they are not very sensitive - absorption or low efficiency, but also need monochromatic beam
 - Monochromatic beam imposes additional cost and effort for commissioning and operation
- Other possible profile measurement may be considered and compared to in terms of resolution, cost, commissioning, operation and maintenance

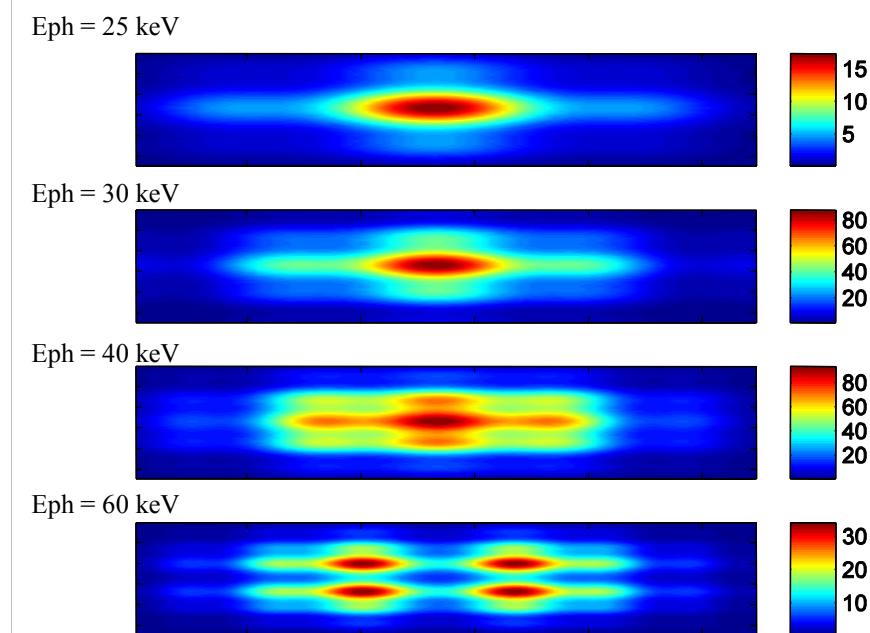
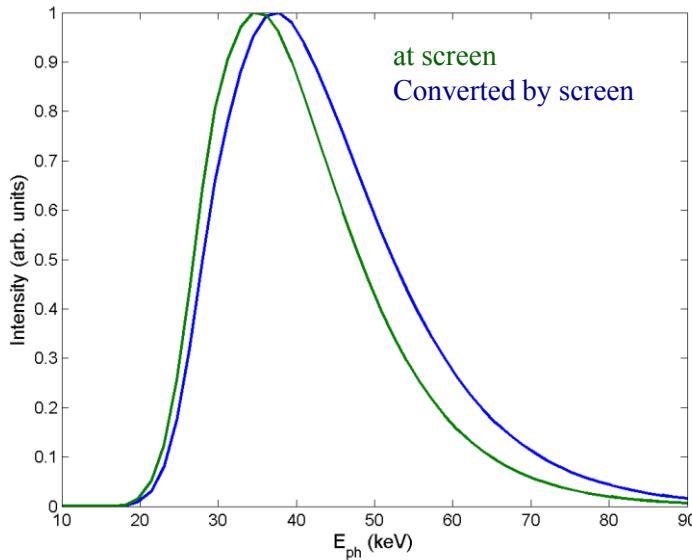
- Many thanks to
 - Diamond Diagnostics group (Chris Bloomer, Alun Morgan, Graham Cook) and Accelerator group (Dr. Riccardo Bartolini, Dr. Ian Martin)
 - Dr. Hiroshi Sakai (KEK)
 - Dr. Joan Vila-Comamala (Diamond)
 - Dr. Abdelmoula Haboub, Dr. Dula Parkinson (LBNL)
 - Dr. Gianluca Geloni (DESY)



Back up Slides

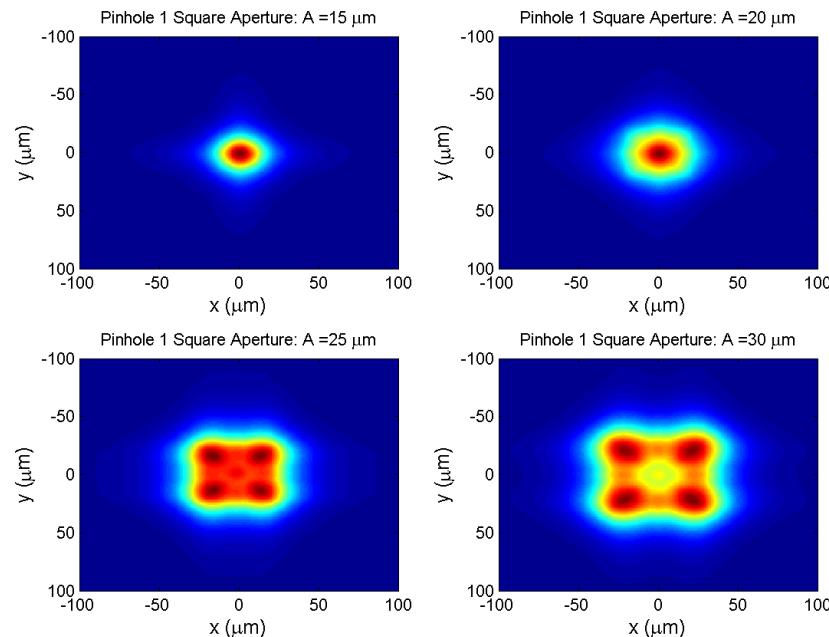
X-ray Pinhole PSF

- Pinhole PSF in the near field:
 - Fresnel diffraction integral
 - Weighted sum over the power spectrum in the screen
 - Convolve the PSF with the camera PSF



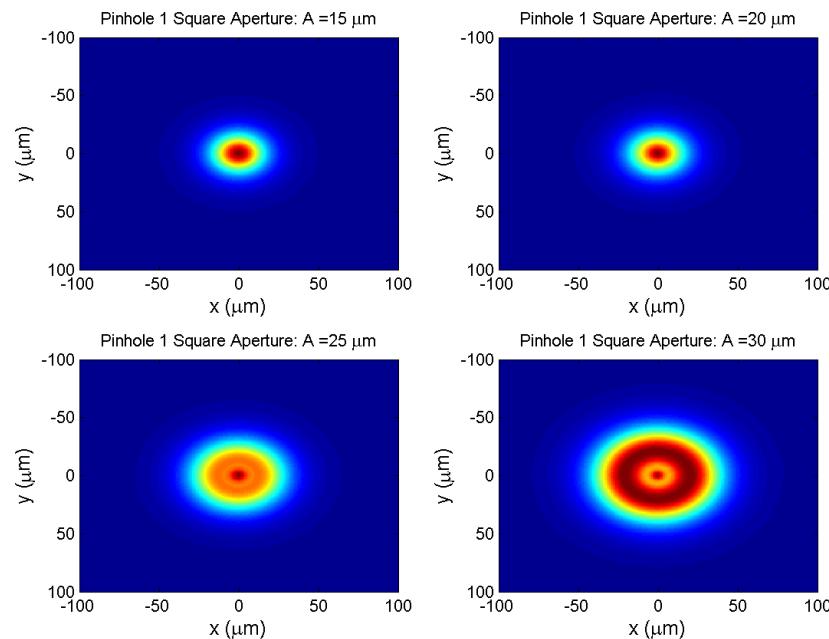
PSF of the X-ray pinholes

- Case of Diamond: Diagnostics Pinholes 1
- PSF for several square apertures



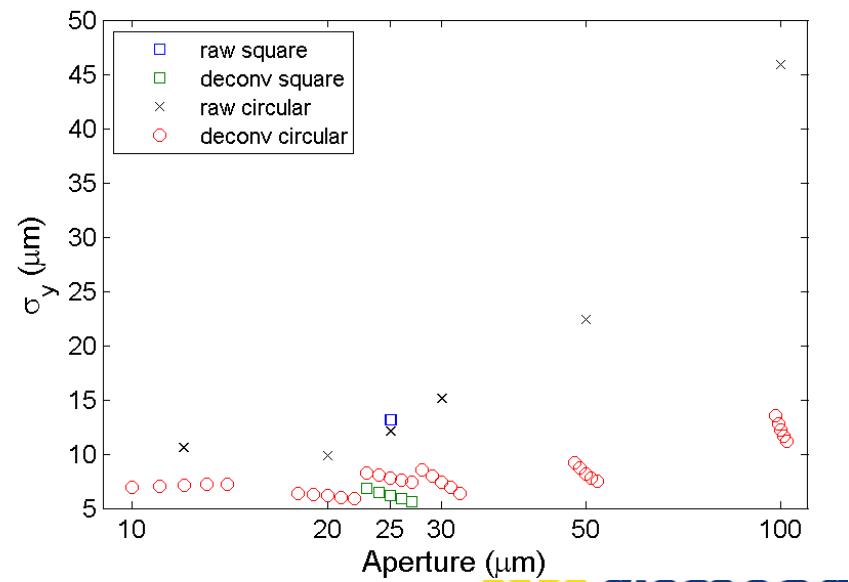
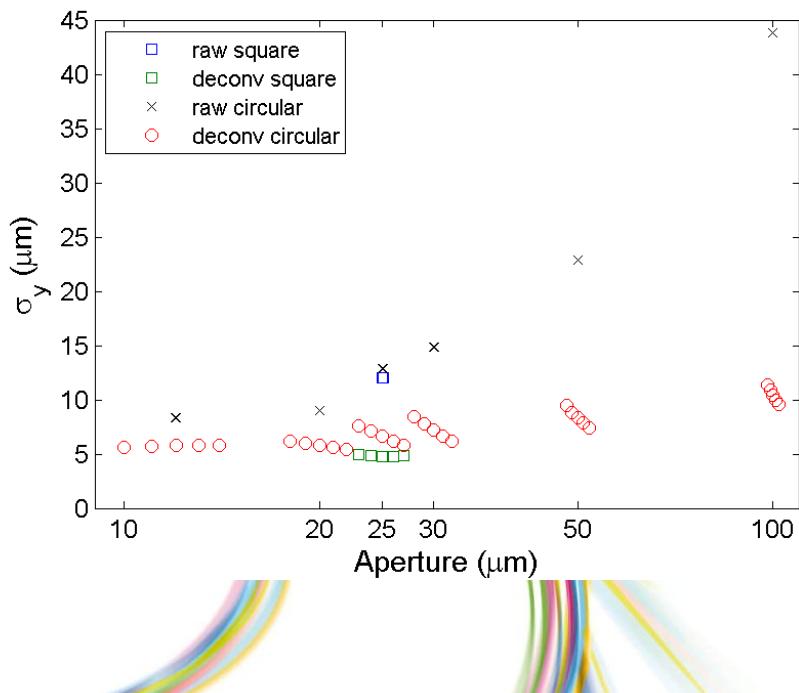
PSF of the X-ray pinholes

- Case of Diamond: Diagnostics Pinholes 1
- PSF for several circular apertures

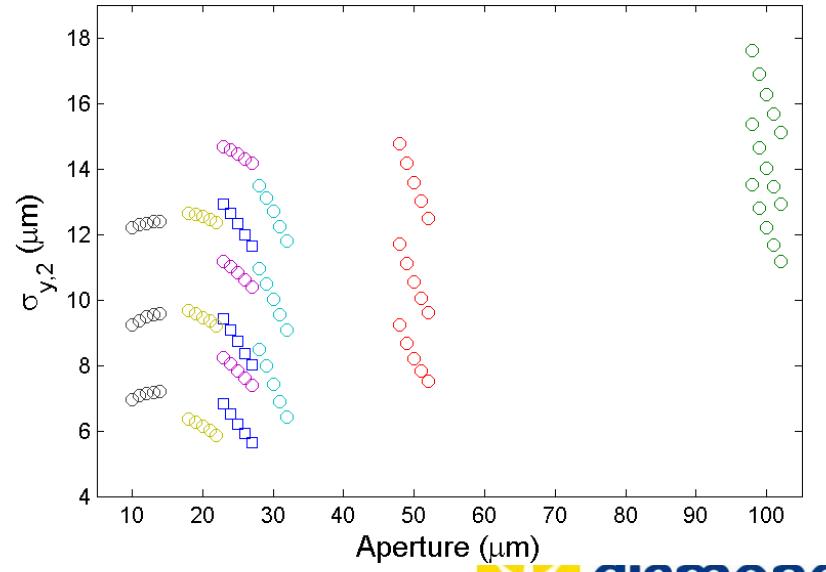
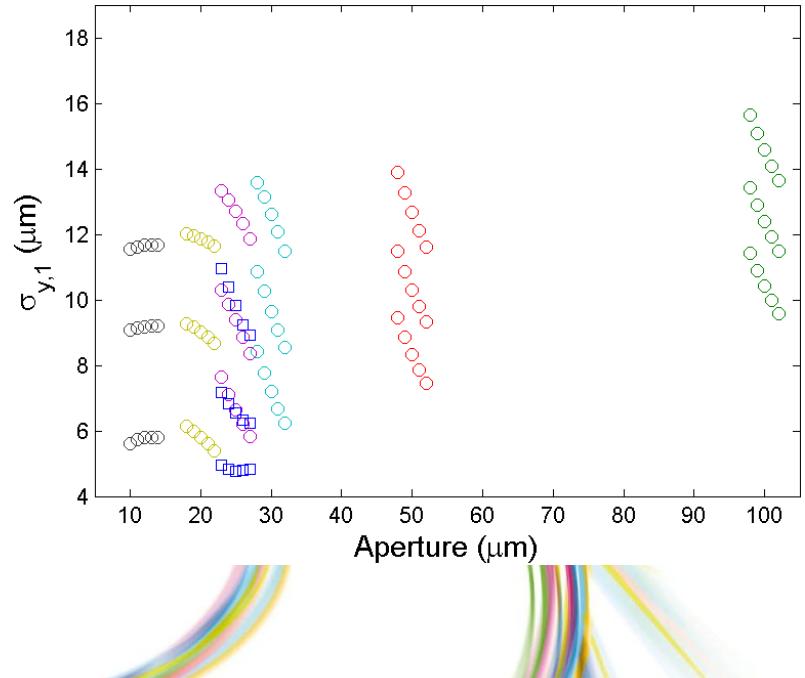


Deconvolved beam size with a range of defined apertures

- Beam size measured on raw images and on deconvolved images of both pinholes, for the same K



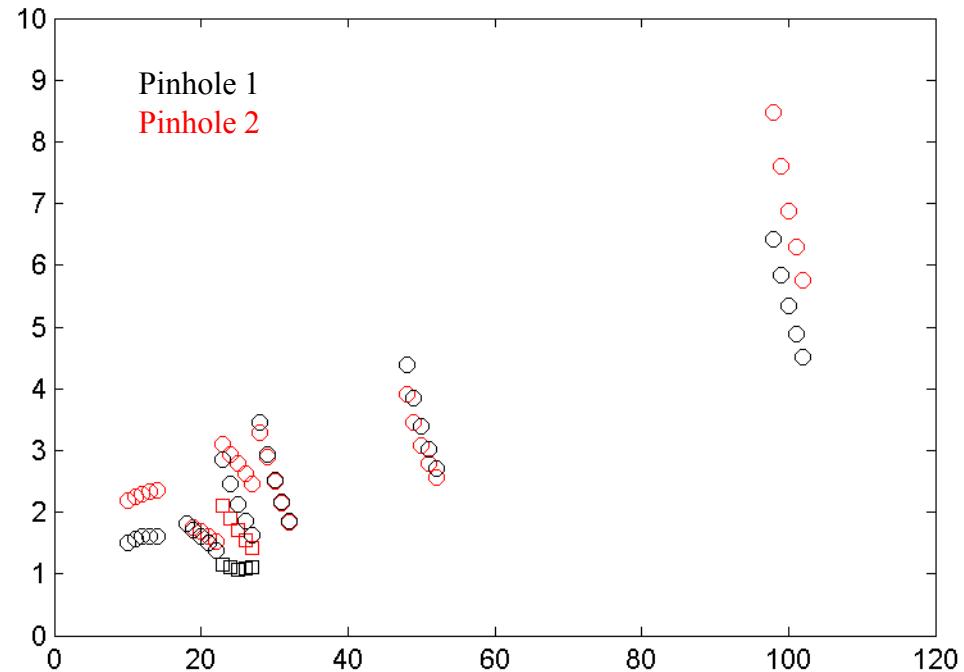
Deconvolved beam size with a range of defined apertures



Deconvolved beam size with a range of defined apertures

- Vertical Emittance:
 - Twiss parameters at source position from LOCO by interpolation
 - Dispersion measured at the source

$$\varepsilon_y = (\sigma_y^2 - (\eta \sigma_e)^2) / \beta$$



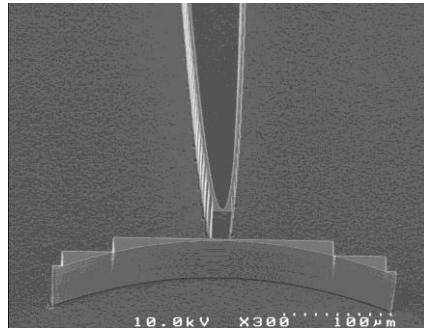
- Note:
 - if $\varepsilon_{x,y} \gg \lambda/2\pi$: Statistical Optics source description coincide with Geometrical Optics
 - This condition is necessary but not sufficient
 - Condition sufficient:
 - $C = \max([2\pi \varepsilon \beta/(L_f \lambda)], 1) \cdot \max([2\pi \varepsilon L_f /(\beta \lambda)], 1) \gg 1$
- L_f for Bending Magnet: $L_f = (\frac{\lambda \rho}{2\pi})^{\frac{1}{3}}$

- for Diamond BM: C

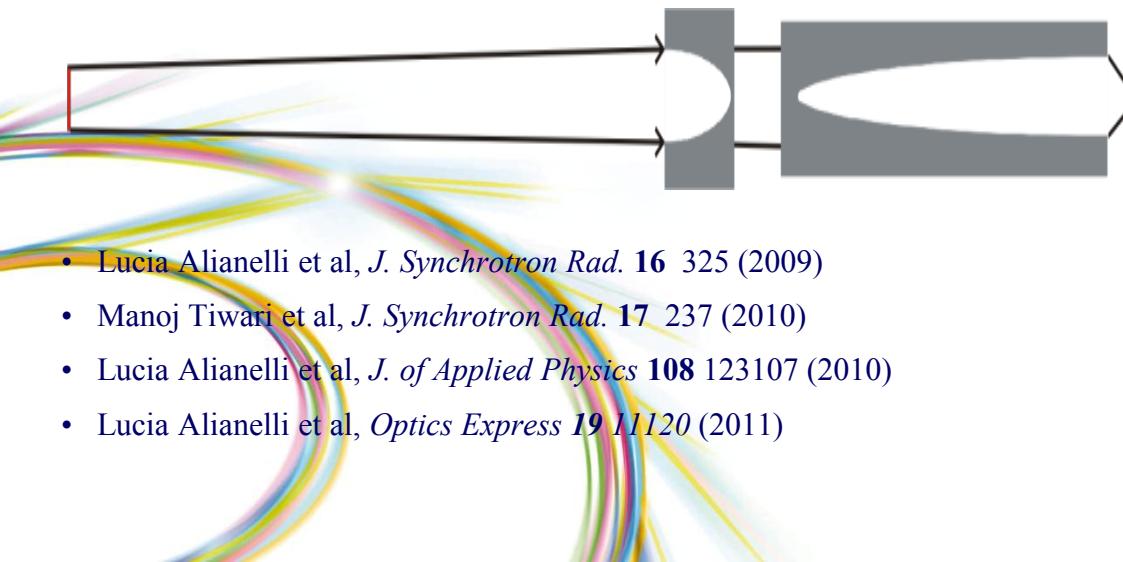
ε_v (pm.rad)	$\lambda=500\text{nm}$	$\lambda=40\text{pm}$
10	1	$88 \cdot 10^3$
1	1	$8.8 \cdot 10^3$

Kinoform lenses

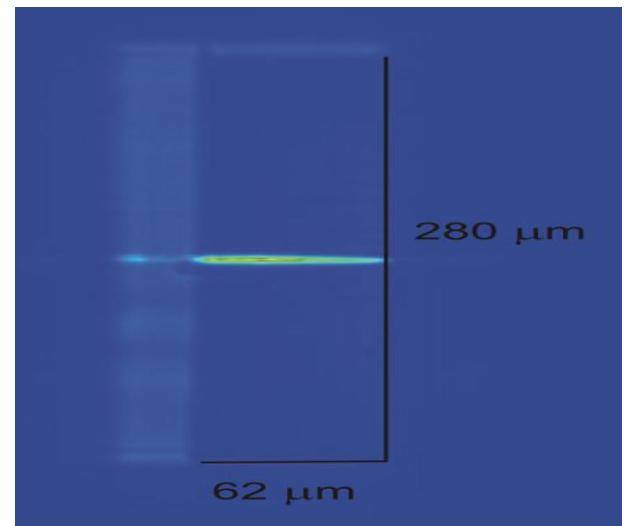
- ## Experimental results



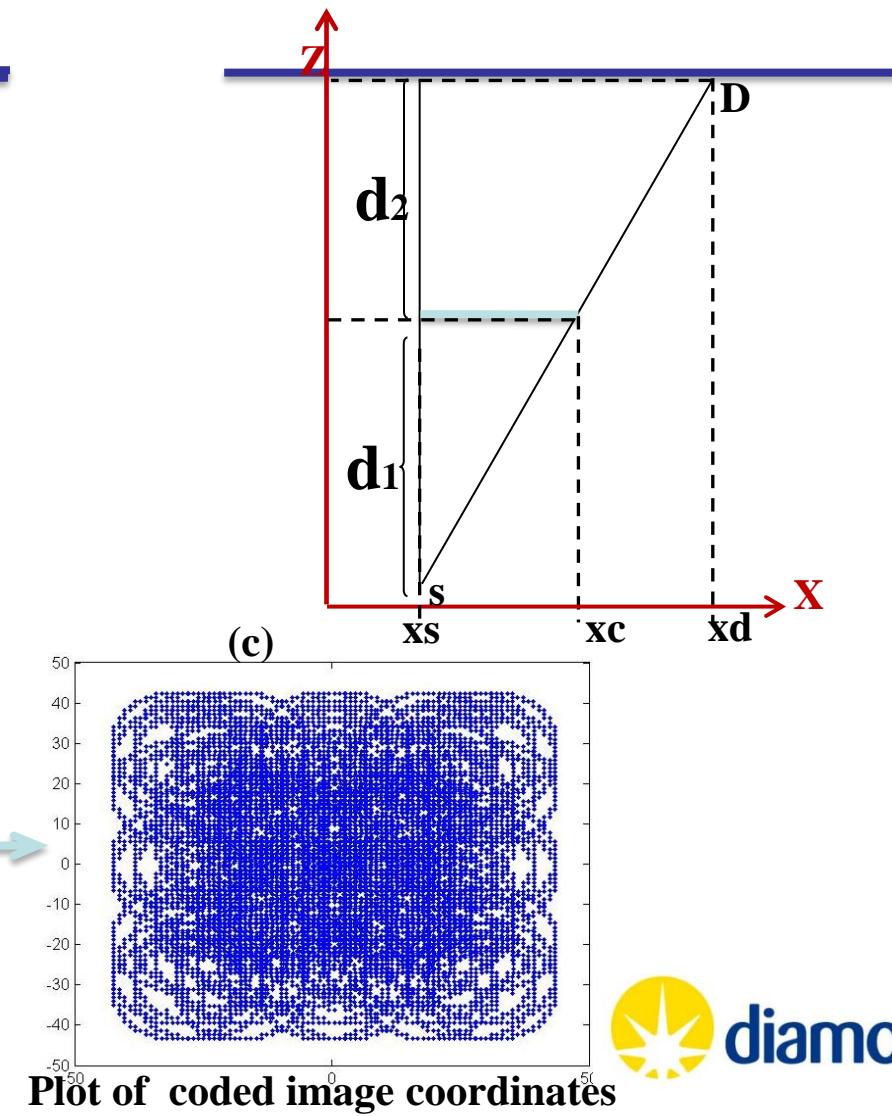
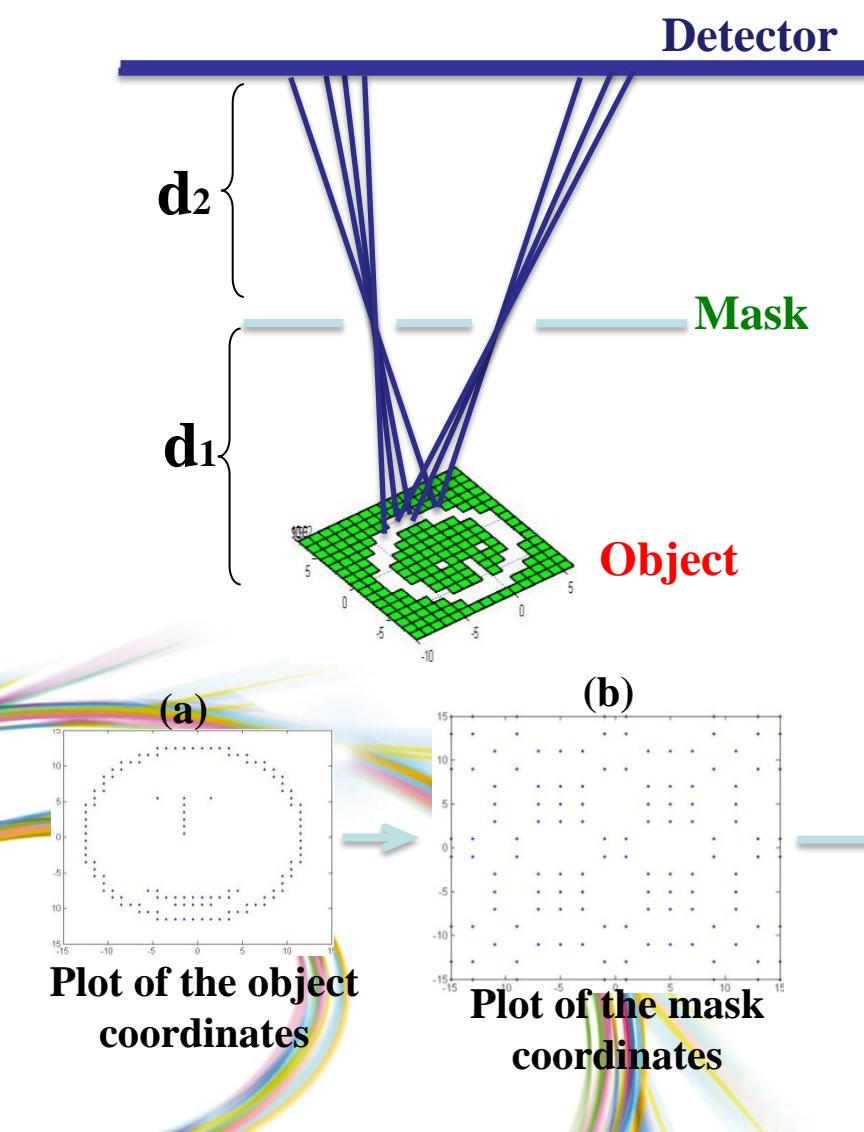
Focal length = 150 mm
Aperture & lens height = 280 μm x 60 μm
Focused beam size: 225 nm fwhm



- Lucia Alianelli et al, *J. Synchrotron Rad.* **16** 325 (2009)
- Manoj Tiwari et al, *J. Synchrotron Rad.* **17** 237 (2010)
- Lucia Alianelli et al, *J. of Applied Physics* **108** 123107 (2010)
- Lucia Alianelli et al, *Optics Express* **19** 11120 (2011)



To deal with magnification and Field of view issues



Coded Apertures

- Coded Apertures:
 - grids, gratings, or other patterns of materials opaque to various wavelengths of light. By blocking and unblocking light in a known pattern, a coded "shadow" is cast upon a plane of detectors.
 - Using computer algorithms, properties of the original light source can be deduced from the shadow on the detectors.
 - Examples of coded apertures:
 - Uniformly Redundant Array (URA)
 - Optimized RAndom pattern (ORA)
 - Hexagonal URA (HURA)
 - Modified Uniformly Redundant Array (MURA)
 - Fresnel Zone Plate (FZP)
 - ...

Coded Apertures

- URA, MURA, HURA, etc.

all URAs are related by the fact that they can be constructed from pseudo-noise (PN) sequences. (A PN sequence is a special type of binary sequence with a two-valued periodic autocorrelation function

Definition of an URA (Fenimore *et al.*, APPLIED OPTICS, 17-3, p.337)

A is a $r \times s$ array with r,s prime numbers and $r - s = 2$

$$A(i, j) = \begin{cases} 0, & \text{if } i = 0 \\ 1, & \text{if } j = 0, i \neq 0 \\ 1, & \text{if } Q_r(i)Q_r(j) = 1 \end{cases}$$

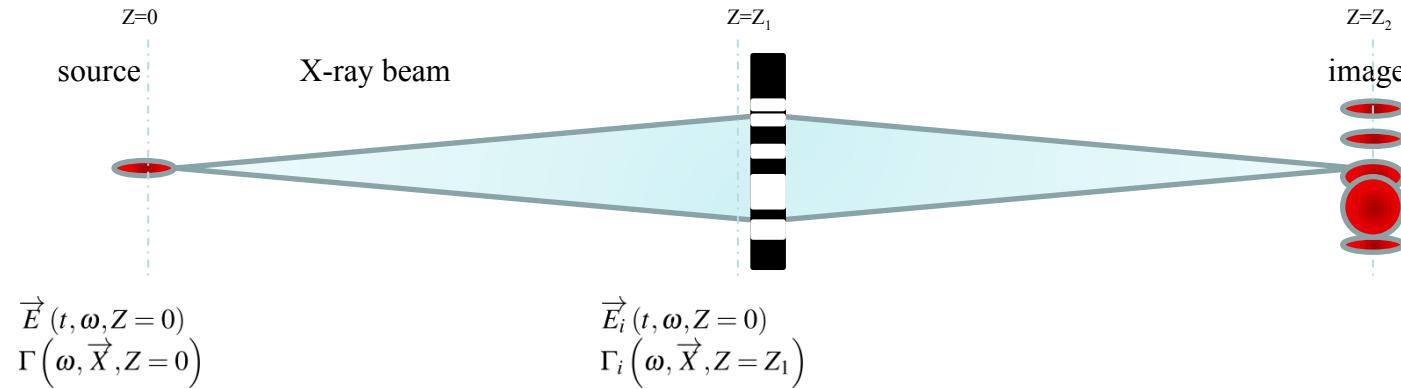
where the quadratic residue Q_r is:

$$Q_r(p) = \begin{cases} 1, & \text{if there exists an integer } x, 1 \leq x < r \\ & \text{such that } p = \text{mod}_r(x^2) \\ -1, & \text{otherwise} \end{cases}$$



Coded Apertures

- URA, MURA, HURA, ORA, etc.



$$I(x, y) = S(x, y) \otimes A(x, y) + N(x, y)$$

Shot resolution estimation

- Want to know, what is the chance that a beam of a certain size is misfit as one of a different size?
- Tend to be photon statistics limited. (Thus coded aperture.)
- So:
 - Calculate simulated detector images for beams of different sizes
 - “Fit” images pairwise against each other:
 - One image represents true beam size, one the measured beam size
 - Calculate χ^2/ν residuals differences between images:

N = # pixels/channels

n = # fit parameters (=1, normalization)

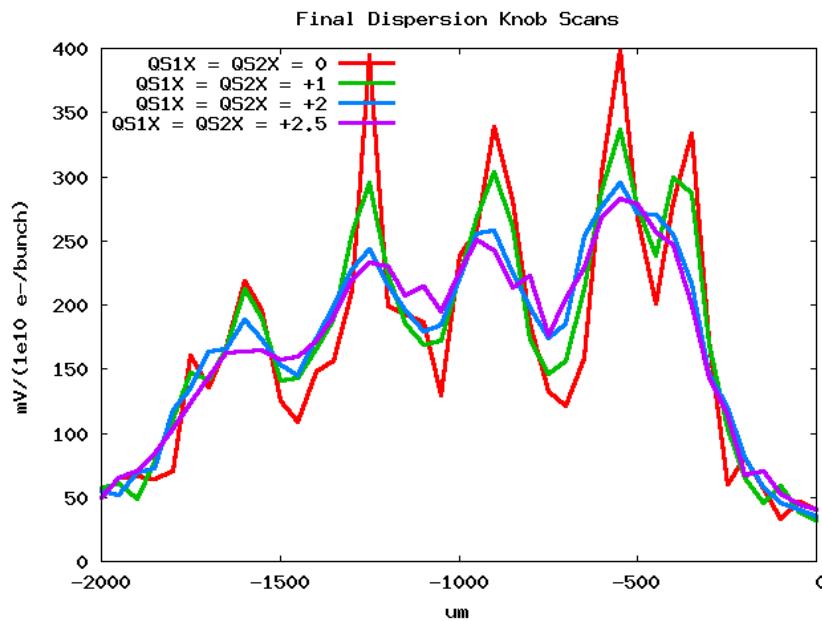
S_i = expected number of photons in channel i

$$\frac{\chi^2}{\nu} = \frac{1}{N-n-1} \sum_{i=1}^N \frac{[S'_i - S_i]^2}{\sigma_i^2},$$

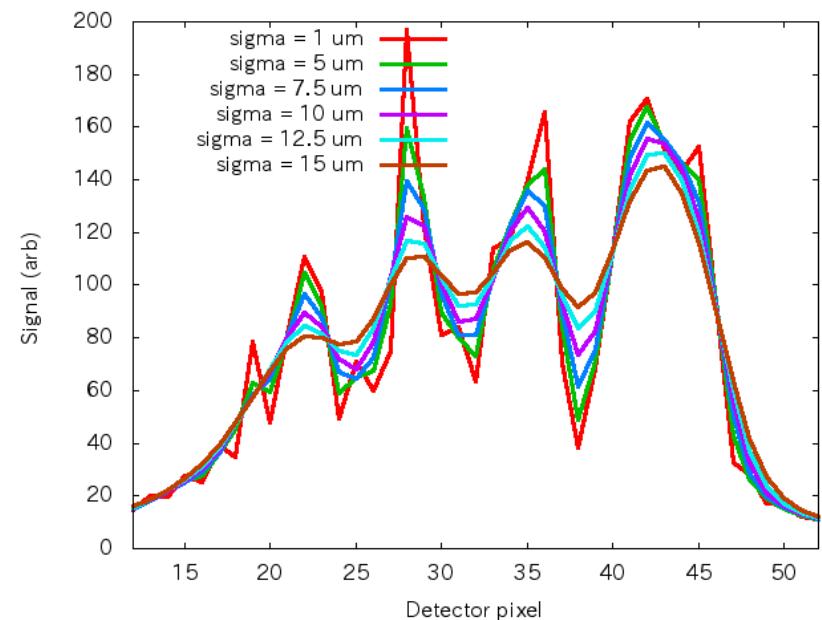
- Weighting function for channel i :
- Value of χ^2/ν that corresponds to a confidence interval of 68% is chosen to represent the 1-s confidence interval

Coded Aperture tests at ATF2

Data



Simulations



Used dispersion knob to change beam size

→Measured beams of 7.5 um or less with scanned-pixel (not single-shot) measurements

Why URA mask?

- Advantage over simple pinhole/slits:
 - Greater open aperture for single-shot measurements
 - Somewhat better resolution
 - Get some peak-valley ratios that help at smaller beam sizes.
 - Make use of more of the detector
- What about a simple equal-spaced array of pinholes/slits?
 - Flatter spatial frequency response
 - Better chance of reconstructing shape
 - Unique position determination (non-repeating pattern)
 - On the other hand, an equal-spaced array can offer tuned resolution over a narrower range of sizes
 - Array may be suitable for a very stable machine, such as a light source.
- For instability studies (e-cloud, e.g.) or other machine studies, or for a luminosity machine which is always running at the limit of stability, a URA mask promises reasonable performance over a range of bunch conditions.
- However, depending on the beam characteristics and measurements desired, URA is not necessarily the optimal pattern for a given measurement problem.
 - Other coded aperture patterns also currently under investigation

Concept of Coded Aperture Imaging

Courtesy of A. Haboub

- Coded aperture imaging allow lensless imaging at high photon energies and larger FOVs.
- Coded aperture imaging with fluorescent x-ray source, and an energy resolving CCD can yield to 3D elemental map of the sample.
- The detector response is

$$I(i, j) = O(i, j) \otimes A(i, j)$$

(1)

- Image reconstruction through post-processing

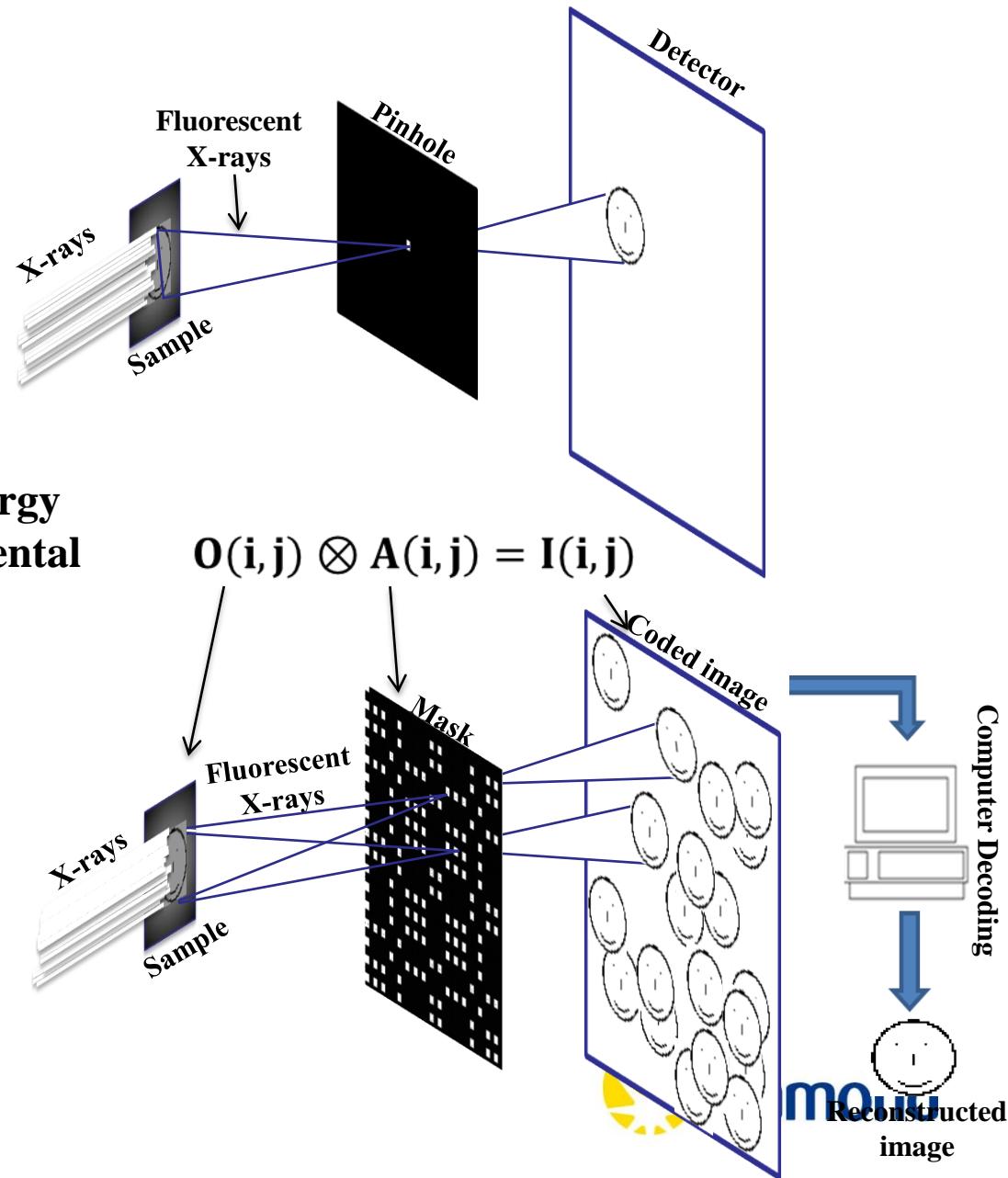
$$O'(i, j) = I(i, j) \otimes \tilde{A}(i, j)$$

(2)

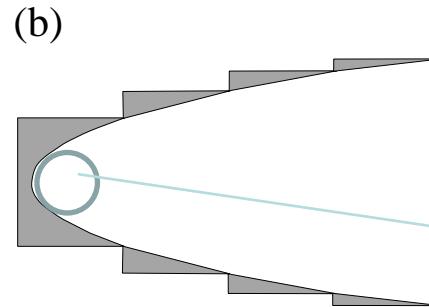
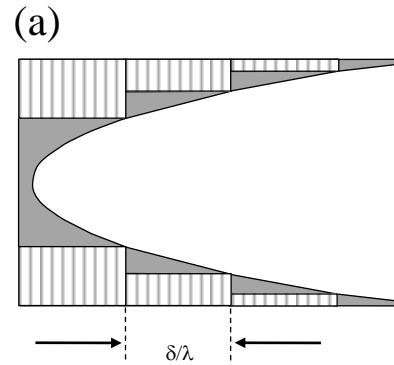
$$A(i, j) \otimes \tilde{A}(i, j) = \delta$$

(3)

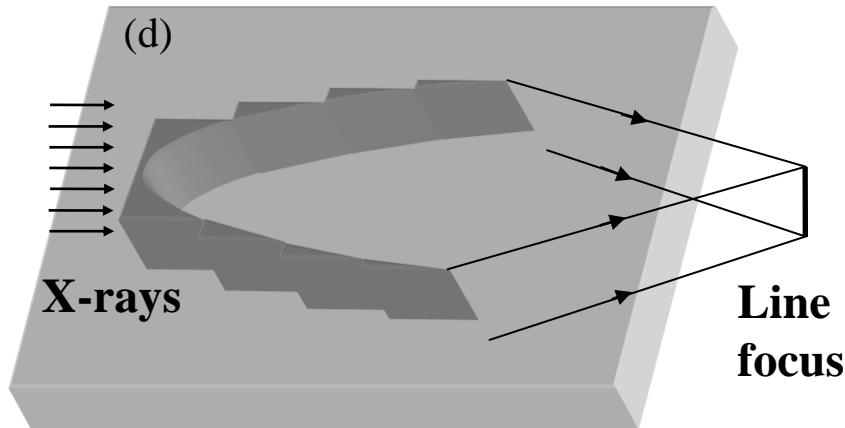
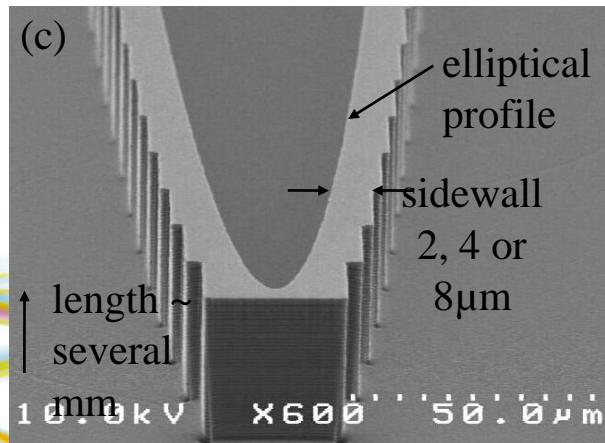
Magnification >1



Kinoform lenses



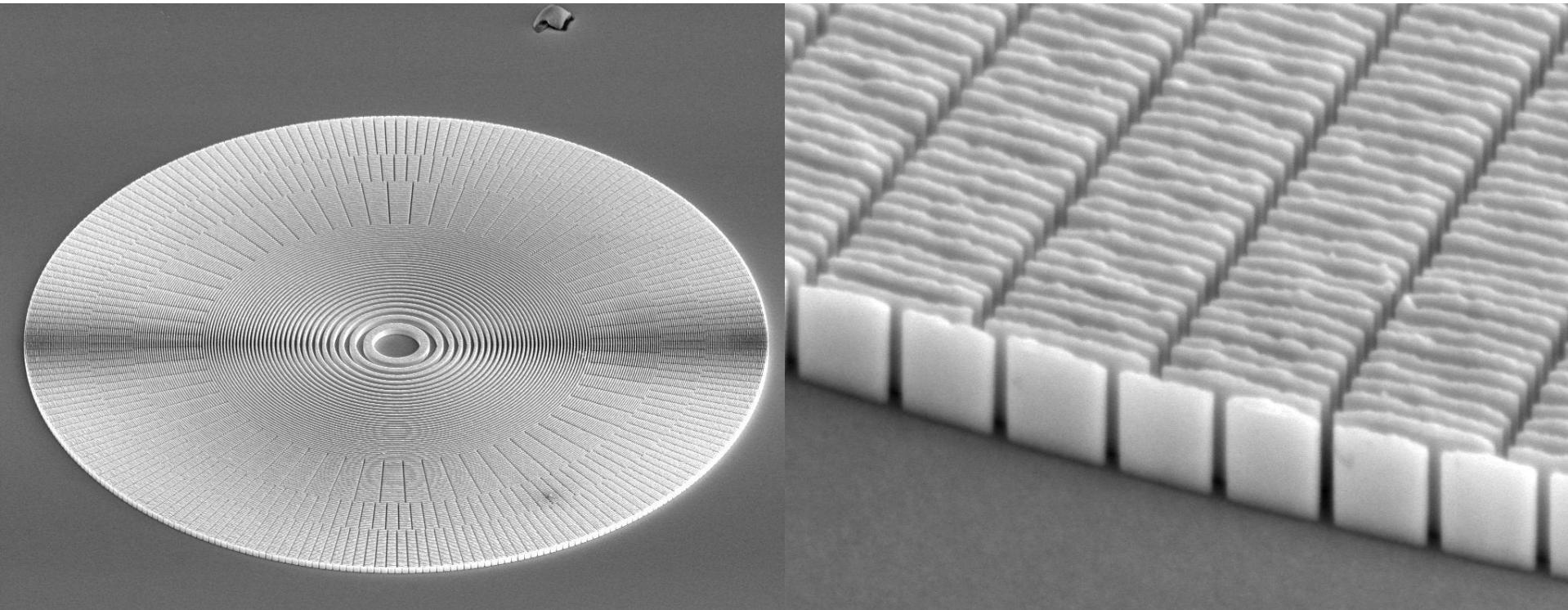
$$f = \frac{R}{\delta}$$
$$R \sim 1 \mu m$$



Schematic of a kinoform lens before (a) and after removal of redundant 2π phase-shifting material (b). **SEM micrograph of a Si kinoform lens depicting important parameters (c)**. Focusing action of a kinoform lens (d).

Au FZP for 8-12 keV photon energy

FZPs for sub 100-nm focusing

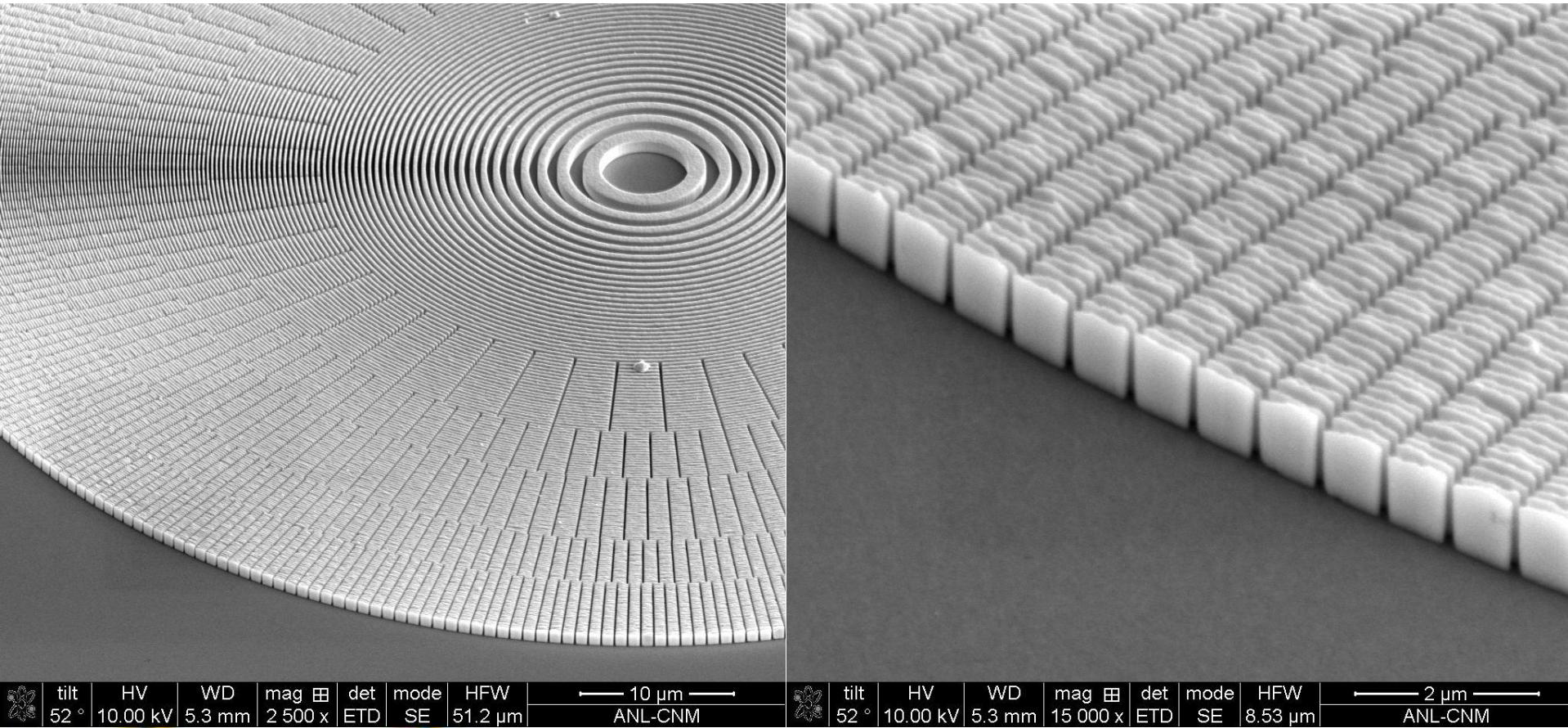


tilt | HV | WD | mag | det | mode | HFW | ————— 30 μm ————— tilt | HV | WD | mag | det | mode | HFW | ————— 2 μm —————
52° | 10.00 kV | 5.3 mm | 1 200 x | ETD | SE | 107 μm | ANL-CNM | 52° | 10.00 kV | 5.3 mm | 20 000 x | ETD | SE | 6.40 μm | ANL-CNM

Au FZP, D = 100 μm, dr = 100 nm, t ~ 900 nm

Au FZP for 8-12 keV photon energy

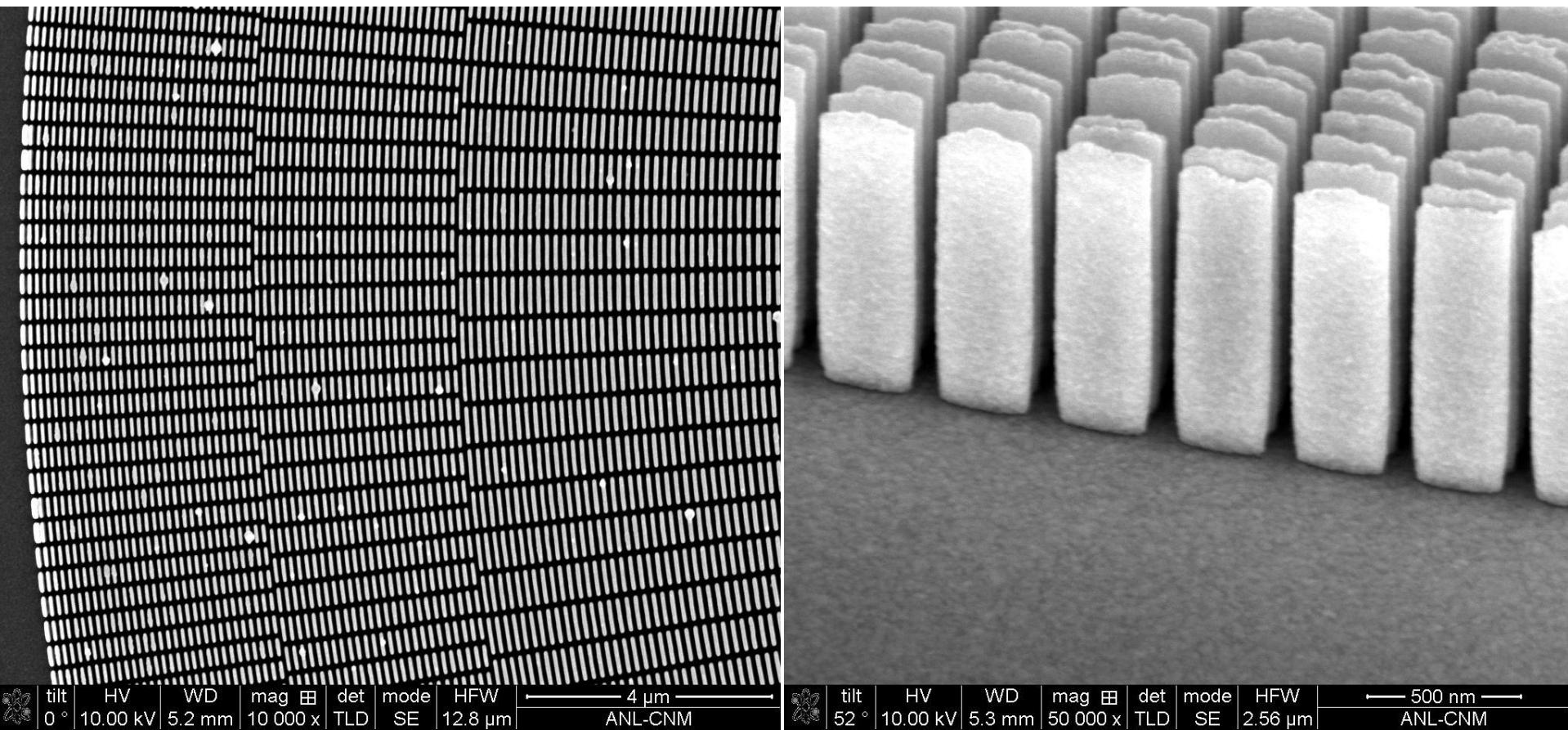
FZPs for sub 100-nm focusing



Au FZP, D = 100 μm, dr = 80 nm, t ~ 900 nm

Au FZP for 8-12 keV photon energy

FZPs for sub 100-nm focusing



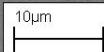
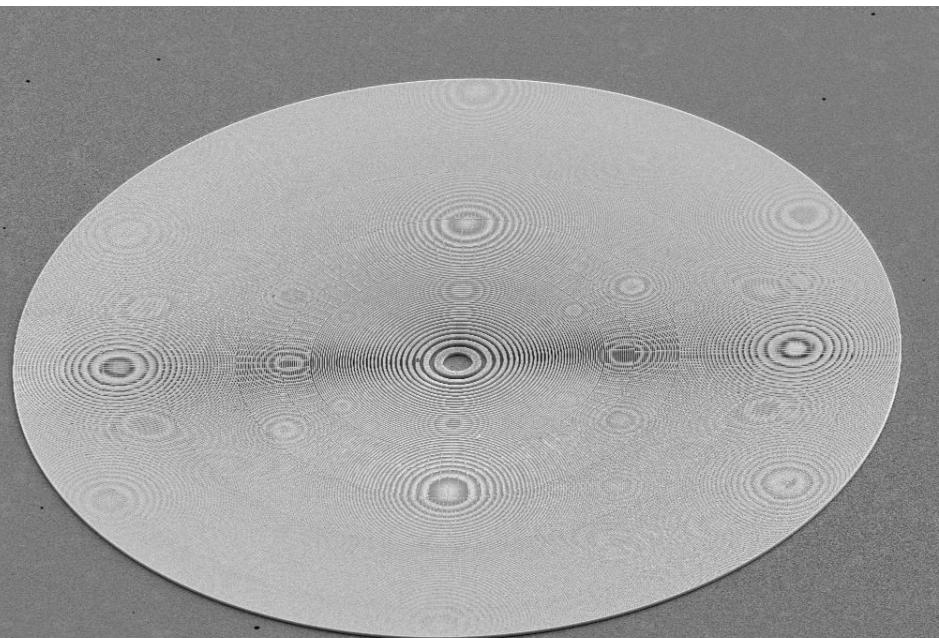
Au FZP, D = 100 μm, dr = 60 nm, t ~ 1100 nm

Ir-HSQ Fresnel Zone Plates for Hard X-rays made at PSI (6—10 keV)

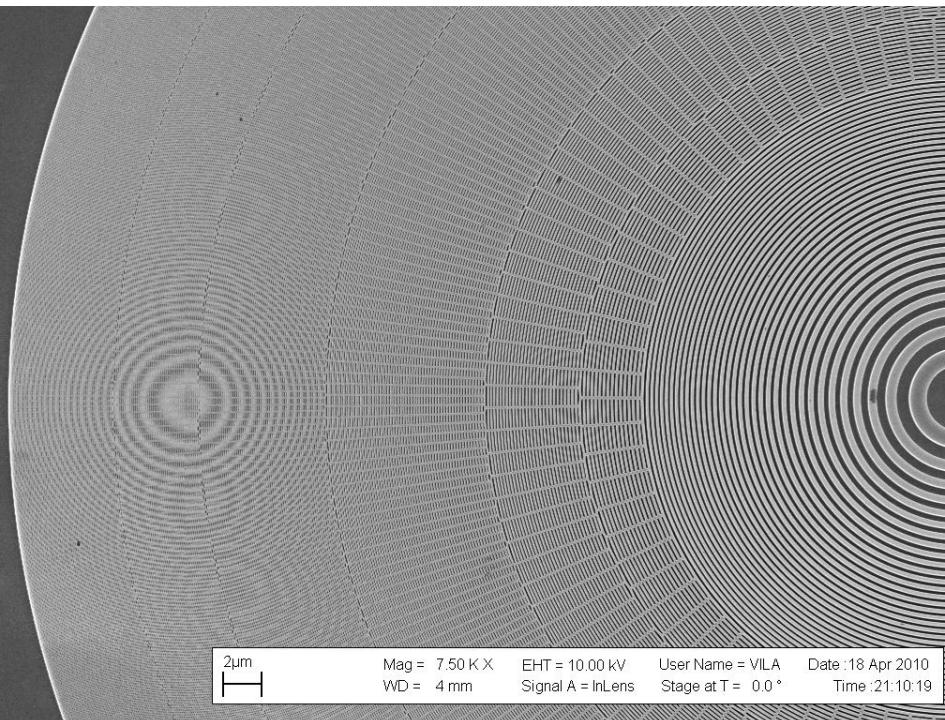
Diameter, D = 150 and 100 μm

Outermost zone width, $dr = 20$

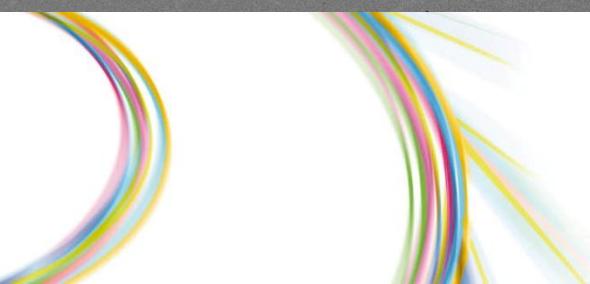
Zone thickness, $t \sim 500\text{--}600 \text{ nm}$



Mag = 3.50 K X
WD = 10 mm
EHT = 10.00 kV
Signal A = SE2
User Name = VILA
Stage at T = 50.0 °
Date : 18 Apr 2010
Time : 20:57:38



Mag = 7.50 K X
WD = 4 mm
EHT = 10.00 kV
Signal A = InLens
User Name = VILA
Stage at T = 0.0 °
Date : 18 Apr 2010
Time : 21:10:19

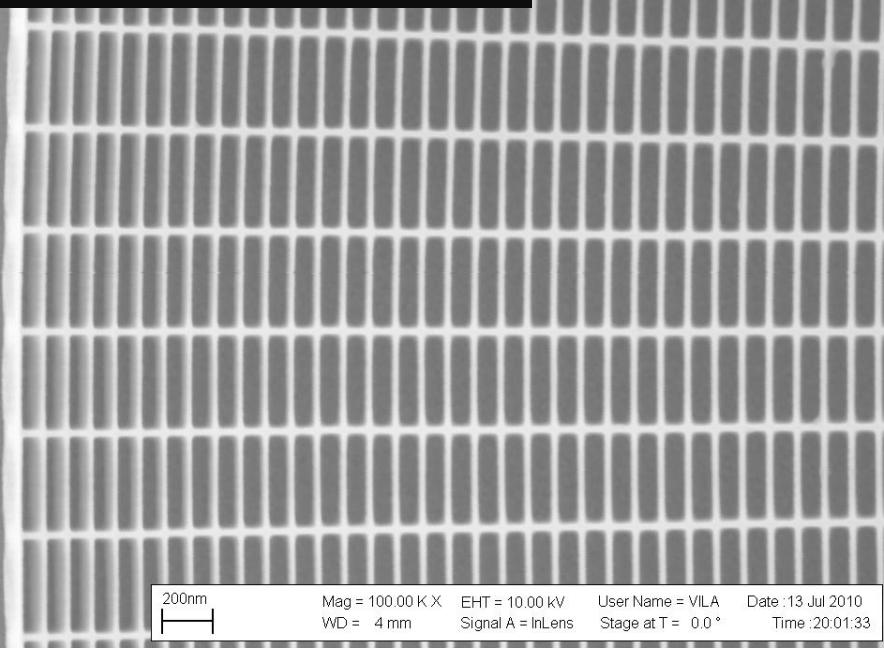


J. Vila-Comamala et al., Nanotechnology (2010)

J. Vila-Comamala et al., Optics Express (2011)



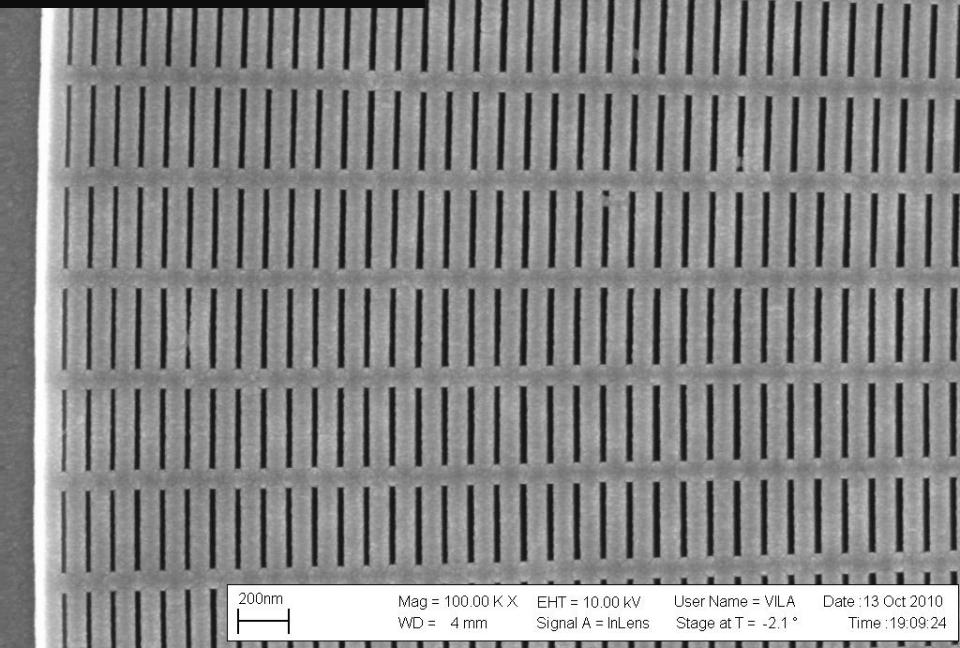
25 nm lines / 100 nm period in HSQ



200nm

Mag = 100.00 K X EHT = 10.00 kV User Name = VILA Date :13 Jul 2010
WD = 4 mm Signal A = InLens Stage at T = 0.0 ° Time :20:01:33

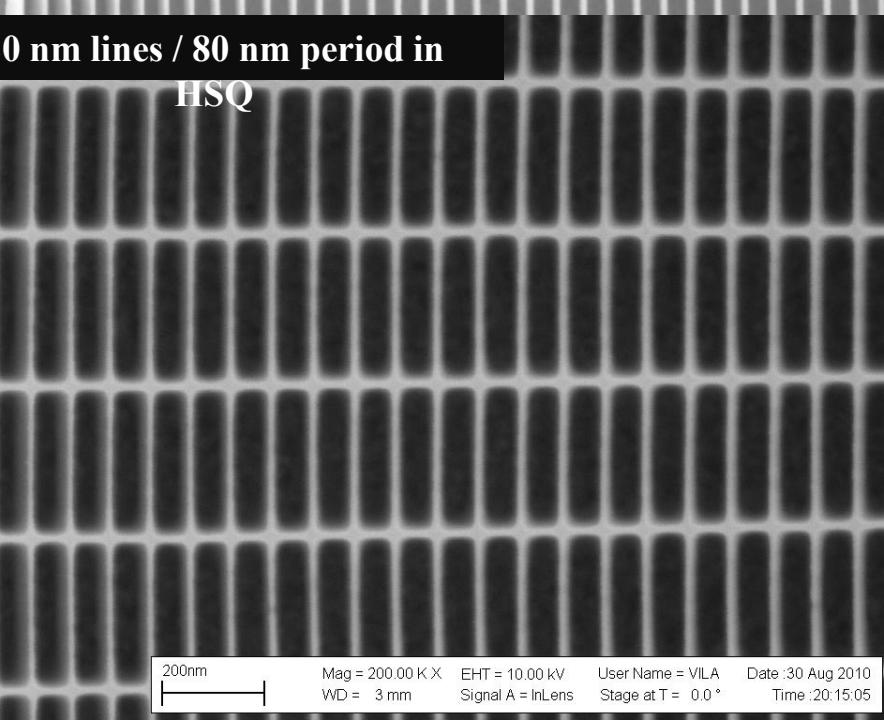
25 nm lines/spaces in Ir



200nm

Mag = 100.00 K X EHT = 10.00 kV User Name = VILA Date :13 Oct 2010
WD = 4 mm Signal A = InLens Stage at T = -2.1 ° Time :19:09:24

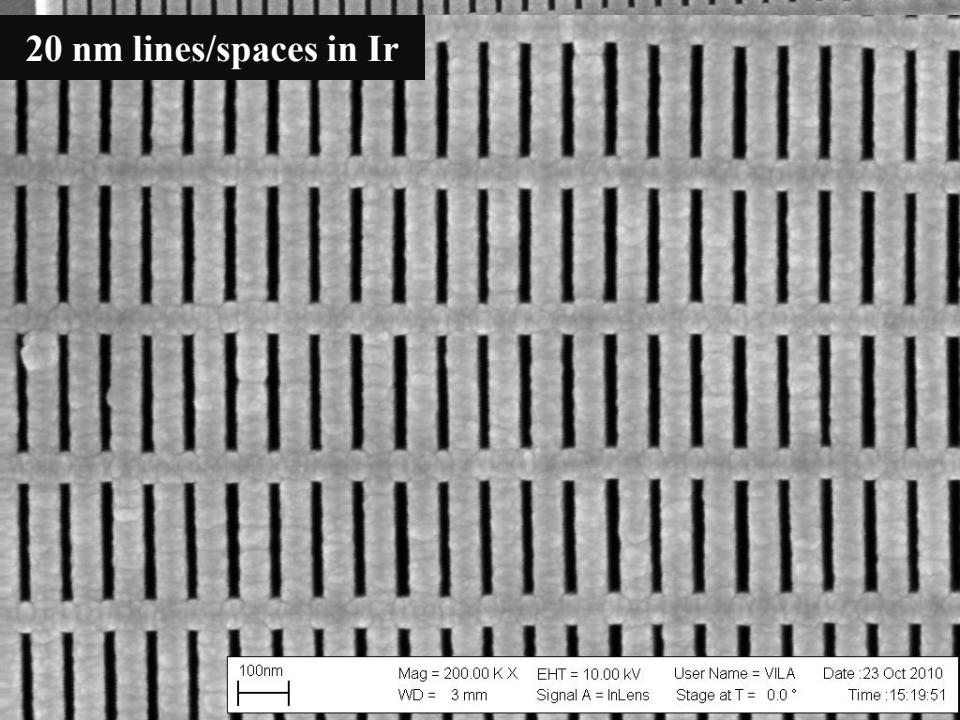
20 nm lines / 80 nm period in HSQ



200nm

Mag = 200.00 K X EHT = 10.00 kV User Name = VILA Date :30 Aug 2010
WD = 3 mm Signal A = InLens Stage at T = 0.0 ° Time :20:15:05

20 nm lines/spaces in Ir



100nm

Mag = 200.00 K X EHT = 10.00 kV User Name = VILA Date :23 Oct 2010
WD = 3 mm Signal A = InLens Stage at T = 0.0 ° Time :15:19:51