



Transverse Beam Emittance Measurement by Undulator Radiation Power Noise

Ihar Lobach (University of Chicago)
IBIC 2021

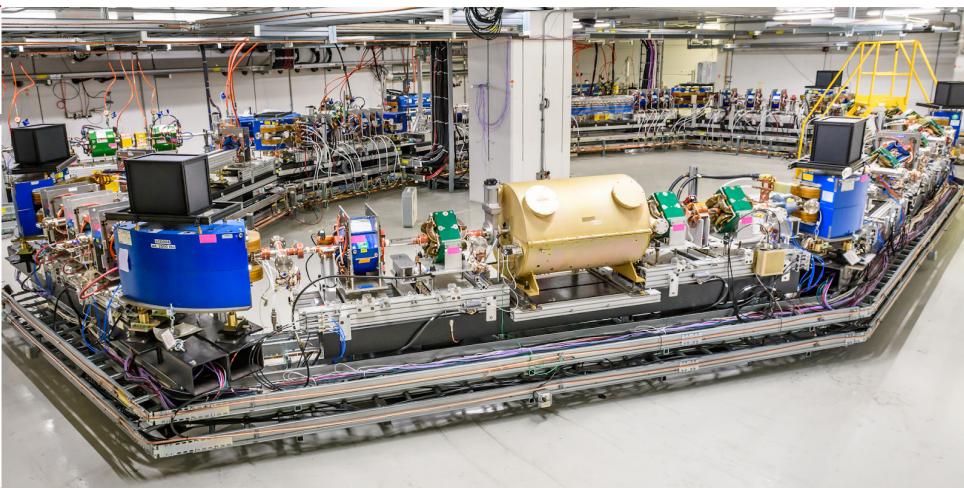
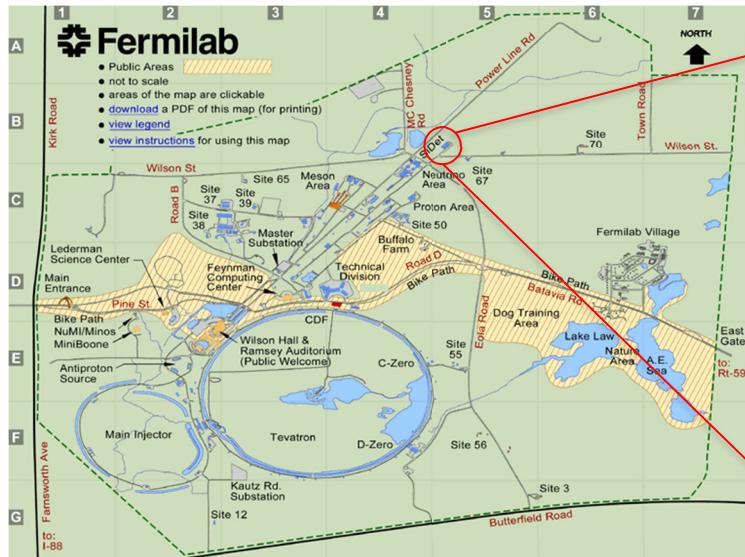


Ihar Lobach, Sergei Nagaitsev*, Valeri Lebedev, Aleksandr Romanov, Giulio Stancari*, Alexander Valishev, Aliaksei Halavanau, Zhirong Huang, Kwang-Je Kim

*dissertation advisors

Fermilab's Integrable Optics Test Accelerator (IOTA)

- First beam Aug 21, 2018



Primary purpose: accelerator science and technology research
(not production of radiation for users)

- Particles: electrons/protons
- Main experiments:
 - Nonlinear beam optics
 - Optical stochastic cooling

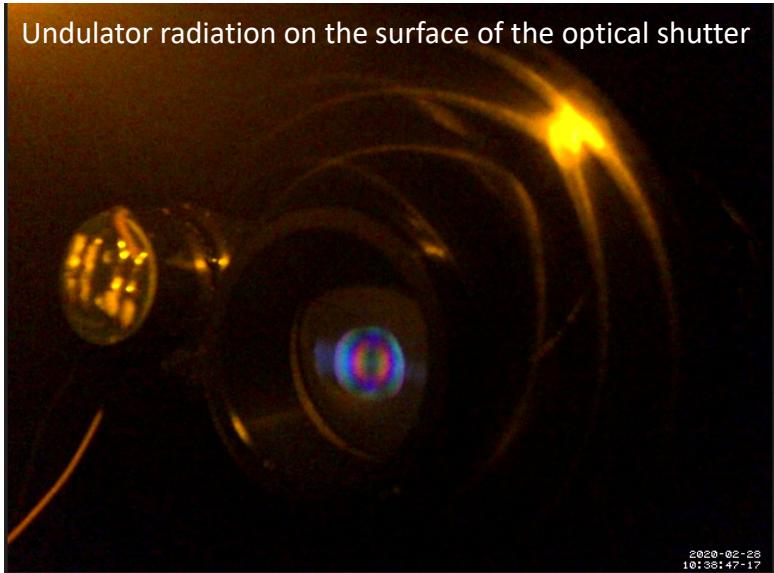
Circumference: 40 m (133 ns)
Electron energy: 100 MeV

Parameters of the undulator in IOTA

Many thanks to our collaborators from SLAC for providing the undulator



Undulator radiation on the surface of the optical shutter



Undulator:

- Number of periods: $N_u = 10.5$
- Undulator period length: $\lambda_u = 55 \text{ mm}$
- Undulator parameter (peak): $K_u = 1$
- Fundamental of radiation: 1.16 um
- Second harmonic: visible light

$$K_u = \frac{eB\lambda_u}{2\pi m_e c}$$

Layout of the undulator section in IOTA

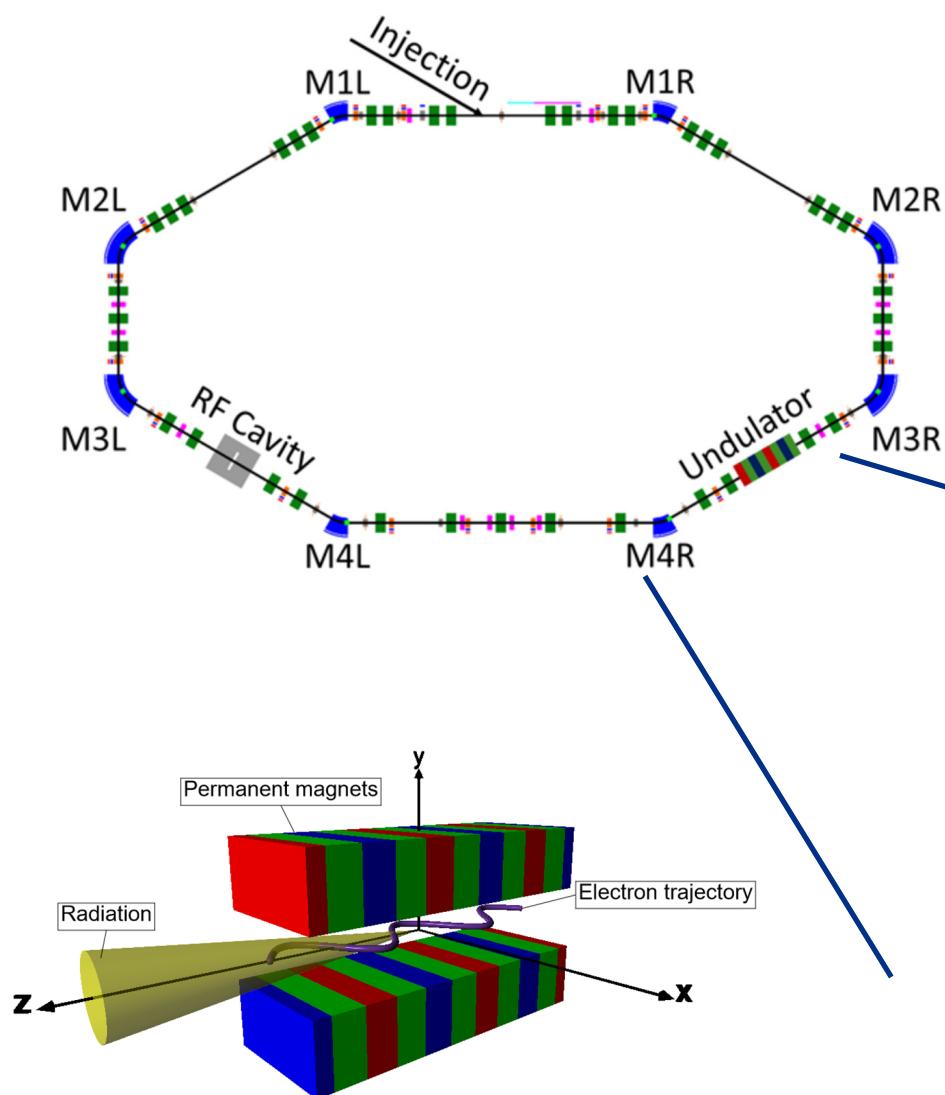
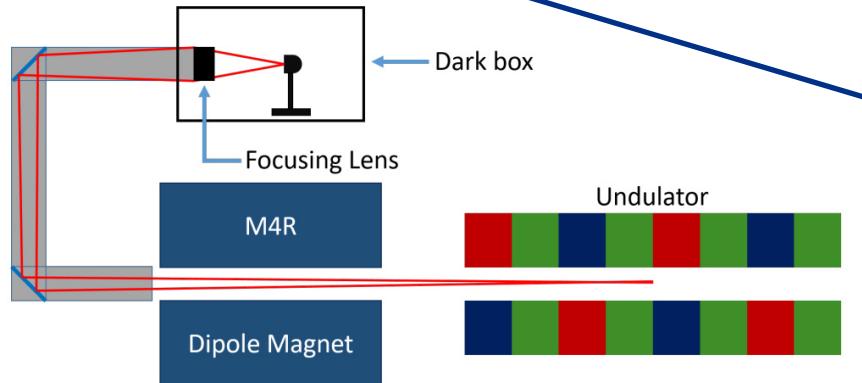
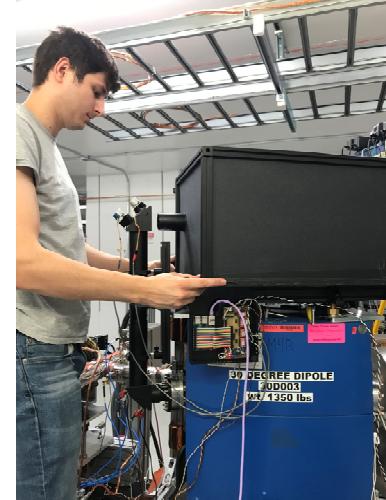


photo credit Evan Angelico



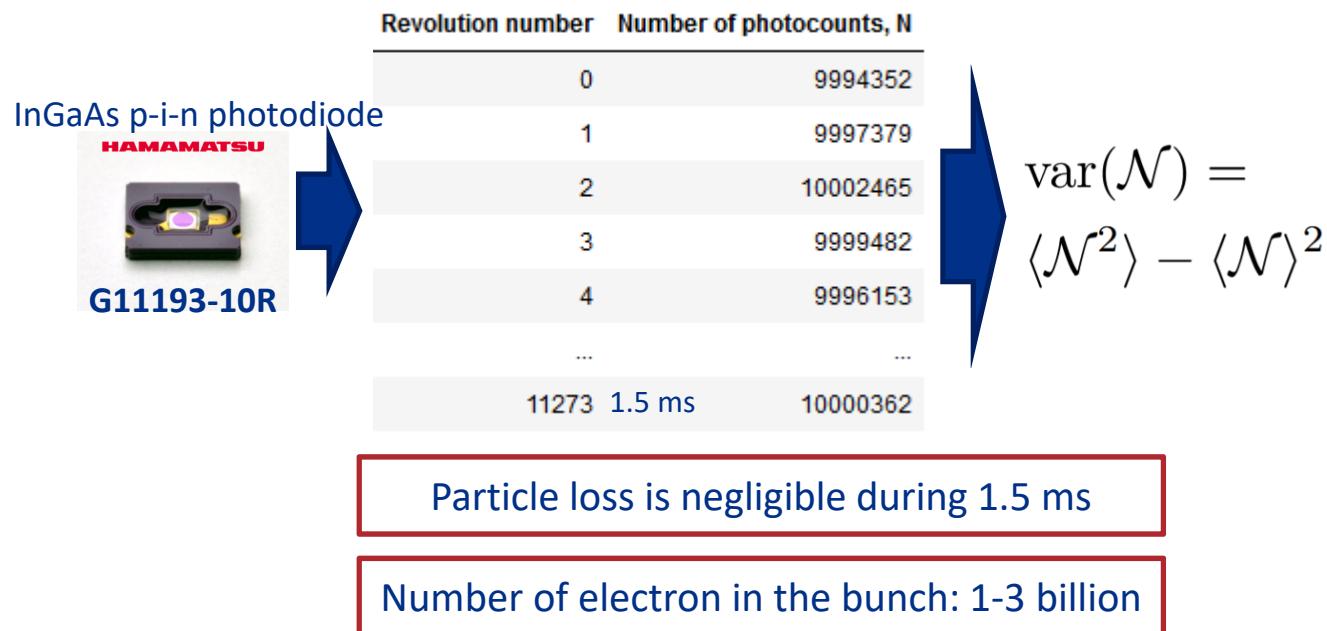
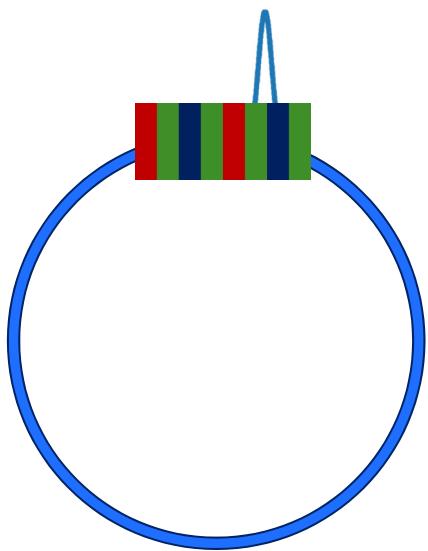
Previous research about statistical properties of synchrotron radiation

Both theoretical and experimental results:

- [1] M. C. Teich, T. Tanabe, T. C. Marshall, and J. Galayda, Statistical properties of wiggler and bending-magnet radiation from the Brookhaven Vacuum-Ultraviolet electron storage ring, Phys. Rev. Lett. **65**, 3393 (1990).
- [2] V. Sajaev, *Determination of longitudinal bunch profile using spectral fluctuations of incoherent radiation*, Report No ANL/ASD/CP-100935 (Argonne National Laboratory, 2000).
- [3] V. Sajaev, Measurement of bunch length using spectral analysis of incoherent radiation fluctuations, in *AIP Conf. Proc.*, Vol. 732 (AIP, 2004) pp. 73–87.
- [4] F. Sannibale, G. Stupakov, M. Zolotorev, D. Filippetto, and L. Jägerhofer, Absolute bunch length measurements by incoherent radiation fluctuation analysis, Phys. Rev. ST Accel. Beams **12**, 032801 (2009).
- [5] P. Catravas, W. Leemans, J. Wurtele, M. Zolotorev, M. Babzien, I. Ben-Zvi, Z. Segalov, X.-J. Wang, and V. Yakimenko, Measurement of electron-beam bunch length and emittance using shot-noise-driven fluctuations in incoherent radiation, Phys. Rev. Lett. **82**, 5261 (1999).
- [6] K.-J. Kim, Start-up noise in 3-D self-amplified spontaneous emission, Nucl. Instrum. Methods Phys. Res., Sect. A **393**, 167 (1997).
- [7] S. Benson and J. M. Madey, Shot and quantum noise in free electron lasers, Nucl. Instrum. Methods Phys. Res., Sect. A **237**, 55 (1985).
- [8] E. L. Saldin, E. Schneidmiller, and M. V. Yurkov, *The physics of free electron lasers* (Springer Science & Business Media, 2013).
- [9] C. Pellegrini, A. Marinelli, and S. Reiche, The physics of x-ray free-electron lasers, Rev. Mod. Phys. **88**, 015006 (2016).
- [10] W. Becker and M. S. Zubairy, Photon statistics of a free-electron laser, Phys. Rev. A **25**, 2200 (1982).
- [11] W. Becker and J. McIver, Fully quantized many-particle theory of a free-electron laser, Phys. Rev. A **27**, 1030 (1983).
- [12] W. Becker and J. McIver, Photon statistics of the free-electron-laser startup, Phys. Rev. A **28**, 1838 (1983).
- [13] T. Chen and J. M. Madey, Observation of sub-Poisson fluctuations in the intensity of the seventh coherent spontaneous harmonic emitted by a RF linac free-electron laser, Phys. Rev. Lett. **86**, 5906 (2001).
- [14] J.-W. Park, *An Investigation of Possible Non-Standard Photon Statistics in a Free-Electron Laser*, Ph.D. thesis, University of Hawaii at Manoa (2019).

Experiment idea

Fundamental of the undulator
radiation 1.16 um



The initial goal was to systematically study $\text{var}(\mathcal{N})$ as a function of the electron bunch parameters (charge, size, shape, divergence)

Then, we realized that we could reverse this procedure and infer the electron bunch parameters from the measured $\text{var}(\mathcal{N})$

Outline

- Theoretical consideration
- Details about the apparatus and measurement procedure
- Measurements of the fluctuations
- Measurements of electron beam emittances via the fluctuations

Theoretical predictions

$$\text{var}(\mathcal{N}_{\text{ph}}) = \langle \mathcal{N}_{\text{ph}} \rangle + \frac{1}{M} \langle \mathcal{N}_{\text{ph}} \rangle^2$$

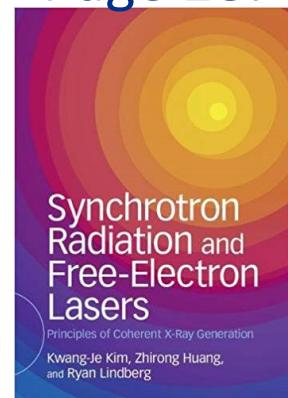
Discrete quantum
nature of light
(Poisson fluctuations)



Turn-to-turn variations in
relative electron positions
and directions of motion

M is conventionally called the number
of coherent modes

Page 28:

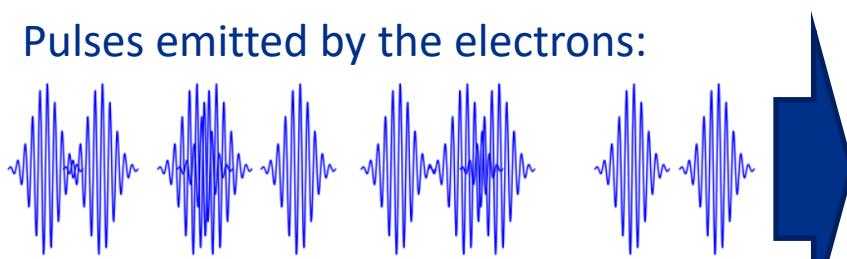


Origin of the second term

$$\text{var}(\mathcal{N}_{\text{ph}}) = \langle \mathcal{N}_{\text{ph}} \rangle + \frac{1}{M} \langle \mathcal{N}_{\text{ph}} \rangle^2$$

- Simplified 1D model:

Pulses emitted by the electrons:



$$W \propto \int dt \left| \sum_{i=1}^{n_e} E(t - t_i) \right|^2 = \int d\omega |E(\omega)|^2 \left| \sum_{i=1}^{n_e} e^{-i\omega t_i} \right|^2$$

The set of arrival times of the electrons $\{t_i\}$ is different during every revolution in the ring. Hence, the radiated energy W fluctuates from turn to turn. $\sigma_t = \sqrt{\langle t_i^2 \rangle - \langle t_i \rangle^2}$

$$|E(\omega)|^2 \propto e^{-\frac{(\omega - \omega_0)^2}{2\sigma_\omega^2}}$$



$$M = \sqrt{1 + 4\sigma_\omega^2 \sigma_t^2}$$

If we also consider transverse electron bunch dimensions and a Gaussian angular radiation profile:

$$M = \sqrt{1 + 4\sigma_k^2 \sigma_z^2} \sqrt{1 + 4k_0^2 \sigma_{\theta_x}^2 \sigma_x^2} \sqrt{1 + 4k_0^2 \sigma_{\theta_y}^2 \sigma_y^2}$$

- F. Sannibale, et al, *Phys. Rev. ST AB*, 12, 032801 (2009)
- I. Lobach, et al, *Phys. Rev. Accel. Beams*, 23, 090703 (2020)

Realistic case

In general, M is a function of

- Detector's angular acceptance
- Detector's spectral sensitivity, polarization sensitivity
- Spectral-angular properties of the radiation (undulator or bending magnet)
- Electron bunch density distribution over $x, y, z, x', y', \delta_p$

x', y', δ_p

We accounted for this part for the first time

Featured in Physics

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Measurements of undulator radiation power noise and comparison with *ab initio* calculations

Ihar Lobach, Sergei Nagaitsev, Valeri Lebedev, Aleksandr Romanov, Giulio Stancari, Alexander Valishev, Aliaksei Halavanau, Zhirong Huang, and Kwang-Je Kim

Phys. Rev. Accel. Beams **24**, 040701 – Published 1 April 2021

Physics See synopsis: Using Fluctuations to Measure Beam Properties



The obtained expression is very complex and includes a multidimensional integral:

$$\frac{1}{M} = (1 - 1/n_e) \frac{\sqrt{\pi} \int dk d^2\phi_1 d^2\phi_2 d^2r' \mathcal{P}_k(r', \phi_1 - \phi_2) \mathcal{I}_k(\phi_1, r') \mathcal{I}_k^*(\phi_2, r')}{\sigma_z^{\text{eff}} \langle \mathcal{N}_{\text{s.e.}} \rangle^2}, \quad (2)$$

with

$$\mathcal{P}_k(r', \phi_1 - \phi_2) = \frac{1}{4\pi\sigma_{x'}\sigma_{y'}} e^{-\frac{(x')^2}{4\sigma_{x'}^2} - \frac{(y')^2}{4\sigma_{y'}^2}} e^{-ik\Delta_x(\phi_{1x} - \phi_{2x})x' - ik\Delta_y(\phi_{1y} - \phi_{2y})y'} e^{-k^2\Sigma_x^2(\phi_{1x} - \phi_{2x})^2 - k^2\Sigma_y^2(\phi_{1y} - \phi_{2y})^2}, \quad (3)$$

$$\mathcal{I}_k(\phi, r') = \sum_{s=1,2} \eta_{k,s}(\phi) \mathcal{E}_{k,s}(\phi) \mathcal{E}_{k,s}^*(\phi - r'), \quad (4)$$

$$\langle \mathcal{N}_{\text{s.e.}} \rangle = \sum_{s=1,2} \int dk d^2\phi \eta_{k,s}(\phi) |\mathcal{E}_{k,s}(\phi)|^2, \quad (5)$$

where $s = 1, 2$ indicates the polarization component, n_e is the number of electrons in the bunch, $k = 2\pi/\lambda$ is the magnitude of the wave vector; $\phi = (\phi_x, \phi_y)$, $\phi_1 = (\phi_{1x}, \phi_{1y})$ and $\phi_2 = (\phi_{2x}, \phi_{2y})$ represent angles of direction of the radiation in the paraxial approximation. Hereinafter, x and y refer to the horizontal and the vertical axes, respectively, and

$$\sigma_z^{\text{eff}} = 1 / \left(2\sqrt{\pi} \int \rho^2(z) dz \right) \quad (6)$$

where $\rho(z)$ is the electron bunch longitudinal density distribution function, $\int \rho(z) dz = 1$, and σ_z^{eff} is equal to the rms bunch length σ_z for a Gaussian bunch; $r' = (x', y')$ represents the direction of motion of an electron at the radiator center, relative to a reference electron; $\sigma_{x'}$ and $\sigma_{y'}$ are the rms beam divergences, $\sigma_{x'}^2 = \gamma_x \epsilon_x + D_{x'}^2 \sigma_p^2$, $\sigma_{y'}^2 = \gamma_y \epsilon_y$; $\Sigma_x^2 = \epsilon_x / \gamma_x + (\gamma_x D_x + D_{x'} \alpha_x)^2 \beta_x \epsilon_x \sigma_p^2 / \sigma_{x'}^2$, $\Sigma_y^2 = \epsilon_y / \gamma_y$, $\Delta_x = (\alpha_x \epsilon_x - D_x D_{x'} \sigma_p^2) / \sigma_{x'}^2$, $\Delta_y = \alpha_y / \epsilon_y$, where $\alpha_x, \beta_x, \gamma_x, \alpha_y, \beta_y, \gamma_y$ are the Twiss parameters of an uncoupled focusing optics in the synchrotron radiation

$$\mathcal{E}_{k,s}(\phi) = \sqrt{\frac{\alpha k}{2(2\pi)^3}} \int dt \mathbf{e}_s(k) \cdot \mathbf{v}(t) e^{ickt - ik \cdot r(t)}$$

- Assumes known Twiss-functions

- Transversely Gaussian beam
- Arbitrary longitudinal density distribution

The code for numerical computation is available at <https://github.com/IharLobach/fur>



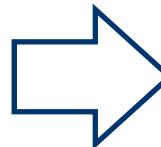
A remark about the quantum contribution

$$\text{var}(\mathcal{N}_{\text{ph}}) = \langle \mathcal{N}_{\text{ph}} \rangle + \frac{1}{M} \langle \mathcal{N}_{\text{ph}} \rangle^2$$

Quantum Classical

At negligible electron recoil the radiated field is in a **coherent state**:

PHYSICAL REVIEW VOLUME 131, NUMBER 6 15 SEPTEMBER 1963
Coherent and Incoherent States of the Radiation Field*
ROY J. GLAUBER



$$|\alpha\rangle = e^{-\frac{1}{2}|\alpha|^2} \sum_n \frac{\alpha^n}{\sqrt{n!}} |n\rangle$$

$$\text{var}(n) = \langle \alpha | (\hat{a}^\dagger \hat{a} - \langle n \rangle)^2 | \alpha \rangle = |\alpha|^2 = \langle n \rangle$$

A unified description leading to the above expression is possible within the framework of **quantum optics using the density operator formalism**:

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Statistical properties of spontaneous synchrotron radiation with arbitrary degree of coherence

Ihar Lobach, Valeri Lebedev, Sergei Nagaitsev, Aleksandr Romanov, Giulio Stancari, Alexander Valishev, Aliaksei Halavanau, Zhirong Huang, and Kwang-Je Kim

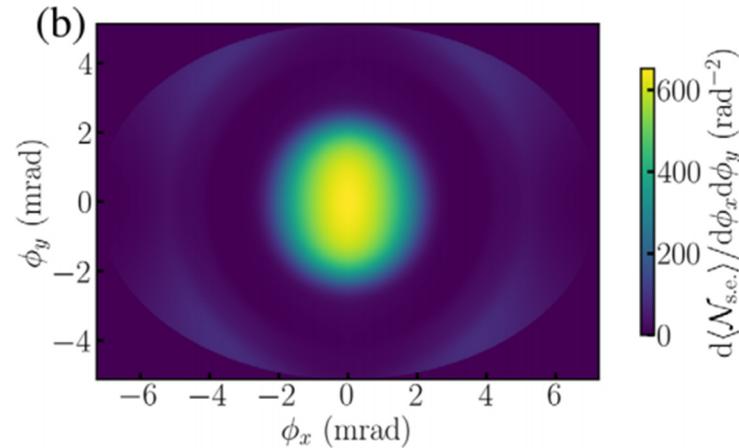
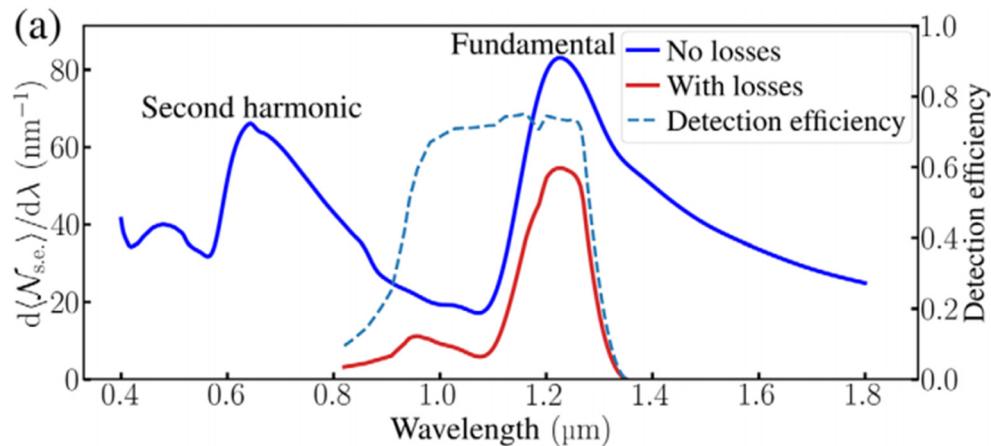
Phys. Rev. Accel. Beams **23**, 090703 – Published 11 September 2020



Fermilab

Details about the experiment

Spectral-angular radiation distribution



In our experiment:

#1 Detect the fundamental ($\approx 1.16 \text{ um}$). InGaAs p-i-n photodiode

#2 Wide band ($\approx 0.14 \text{ um FWHM}$). Large acceptance angle $> 1/\gamma$

(We use a focusing lens)

Simulated total intensity: 9.1×10^{-3} photoelectrons/electron

Measured: 8.8×10^{-3} photoelectrons/electron

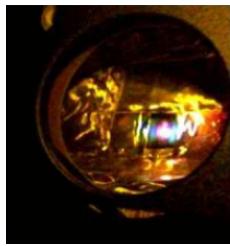
Details about the apparatus

InGaAs PIN photodiode

HAMAMATSU



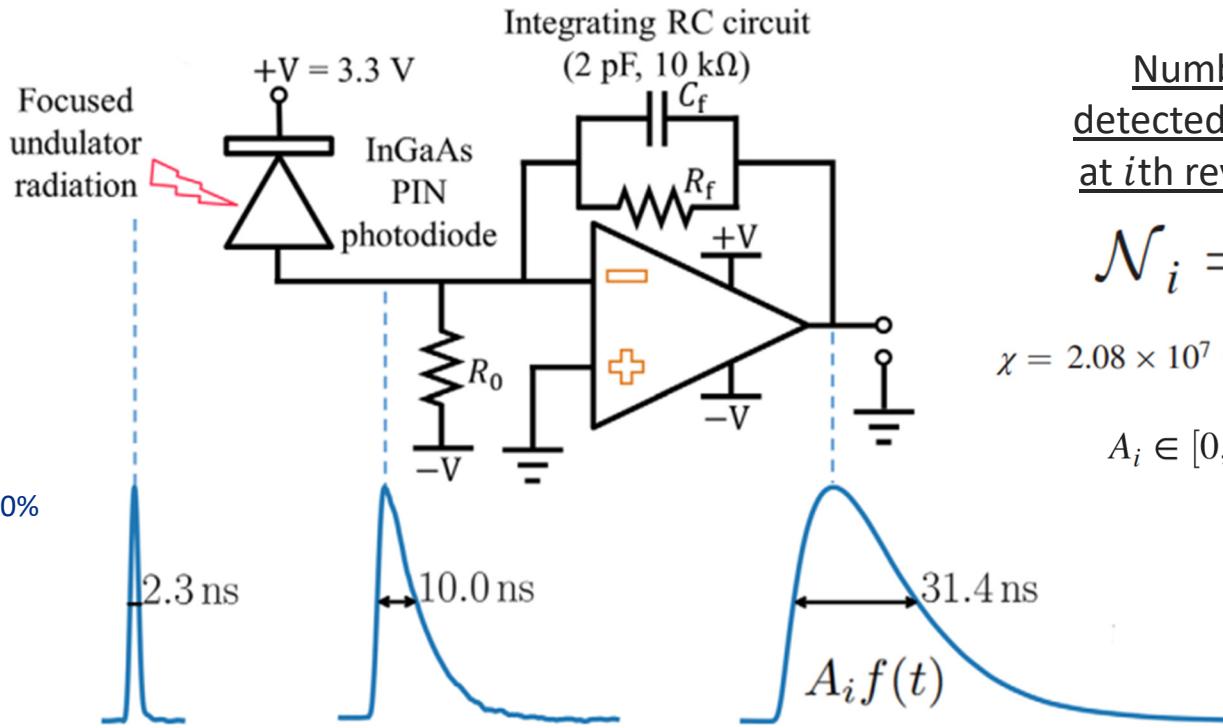
G11193-10R



Sensitive area: $\phi 1\text{mm}$

Quantum efficiency at $1.16\text{ }\mu\text{m}$: 80%

*the circuit was built by Greg Saewert



Number of detected photons at i th revolution:

$$\mathcal{N}_i = \chi A_i$$

$$\chi = 2.08 \times 10^7 \text{ photoelectrons/V}$$

$$A_i \in [0, 1.2] \text{ V}$$

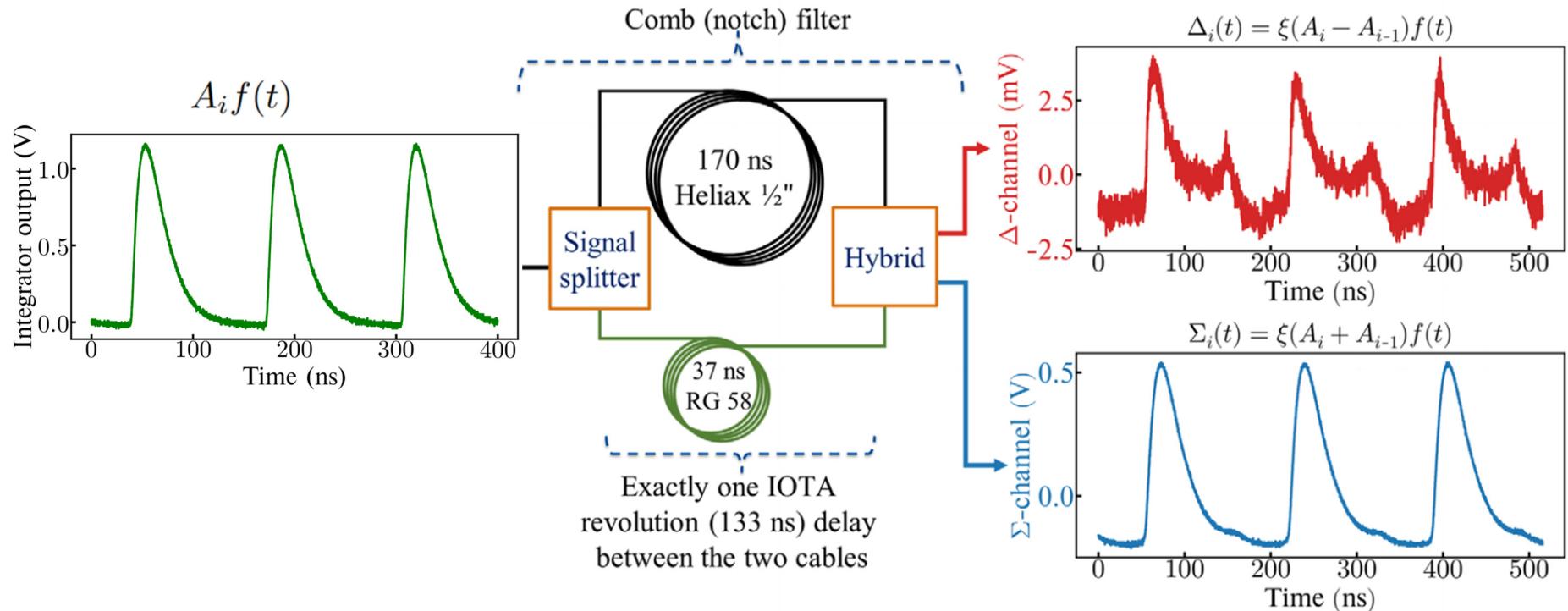
*Many thanks to Mark Obrycki, Peter Prieto, David Johnson, Todd Johnson and Greg Saewert for the equipment for the setup and for their help during our detector tests.

The expected relative fluctuation of A_i was very small $10^{-4} - 10^{-3}$ (rms). It was a big challenge to measure it.

*comparable to the resolution of our 8-bit scope

Comb (notch) filter

*the idea to use the comb filter was proposed by S. Nagaitev.
The components were provided by B.J. Fellenz, K. Carlson, and D. Frolov



Our comb filter had some imperfections:

- Cross-talk (< 1%)
- Small reflected pulse in one of the arms

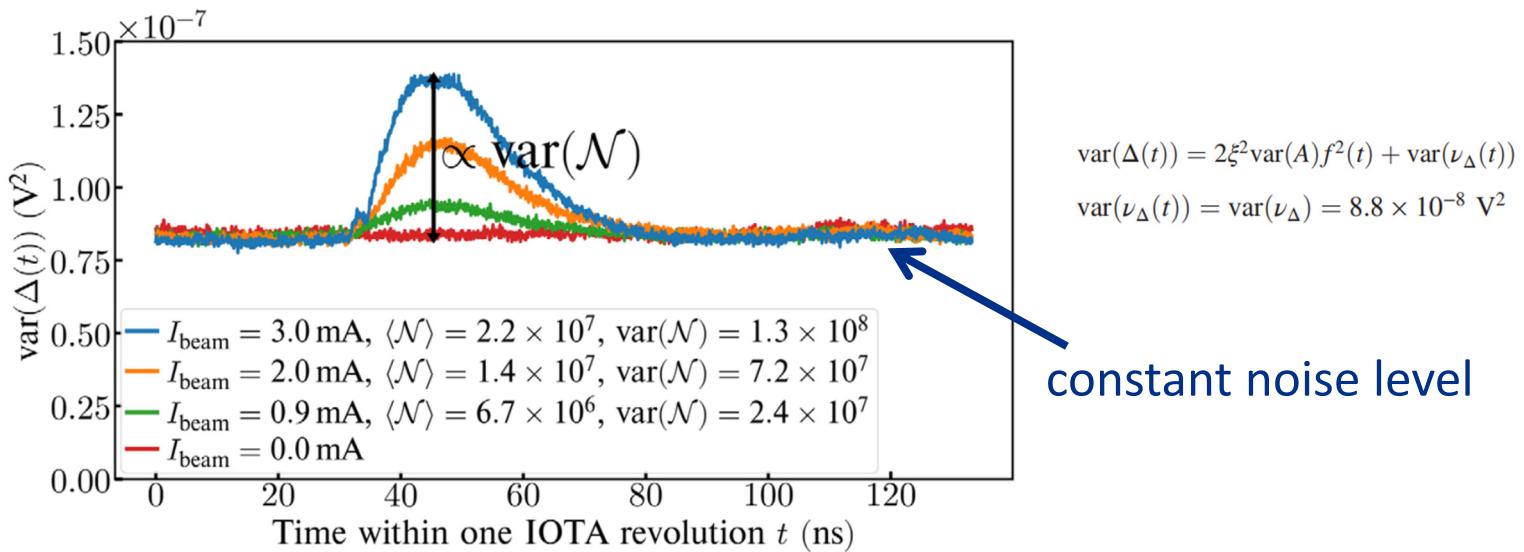
*they could be taken into account and did not affect final results

Noise filtering algorithm

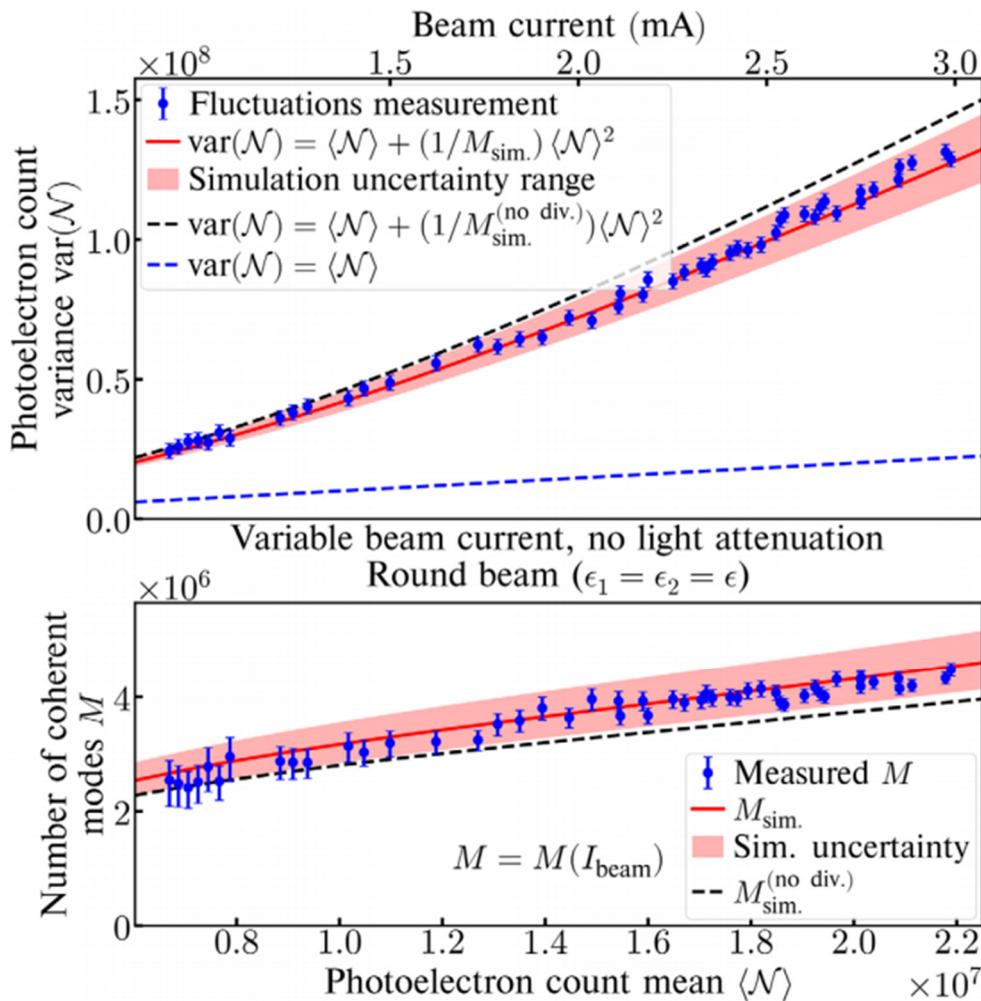
- The instrumental noise due to the oscilloscope's pre-amp and due to the integrator's op-amp was about 0.3 mV (rms)
- Therefore, signal-to-noise ratio was about 1

We had to use a special noise filtering algorithm.

For each time t within one IOTA revolution, calculate variance of Δ -signal for the 11000 revolutions:



Measurements and simulations



$$M = M(\epsilon_x, \epsilon_y, \sigma_p, \sigma_z^{\text{eff}})$$

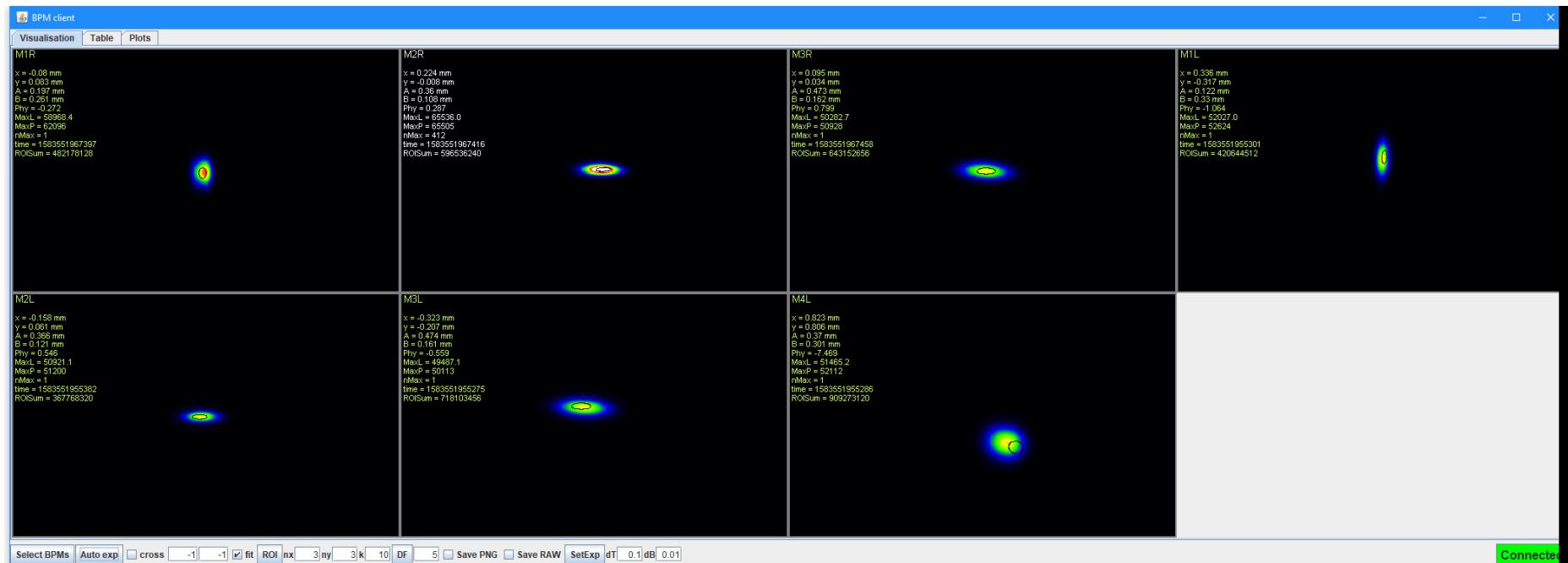
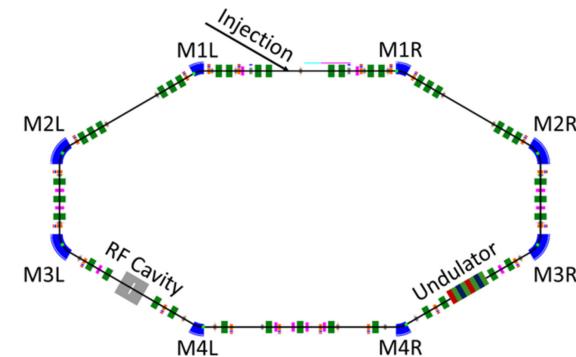
For the simulation,

- ϵ_x and ϵ_y were estimated using bending magnet synchrotron radiation monitors and known Twiss functions.
- σ_z^{eff} and σ_p were estimated using the wall-current monitor signal

Note that the simulation with beam divergence taken into account agrees better

Measurement of transverse bunch size: 7 synclight stations

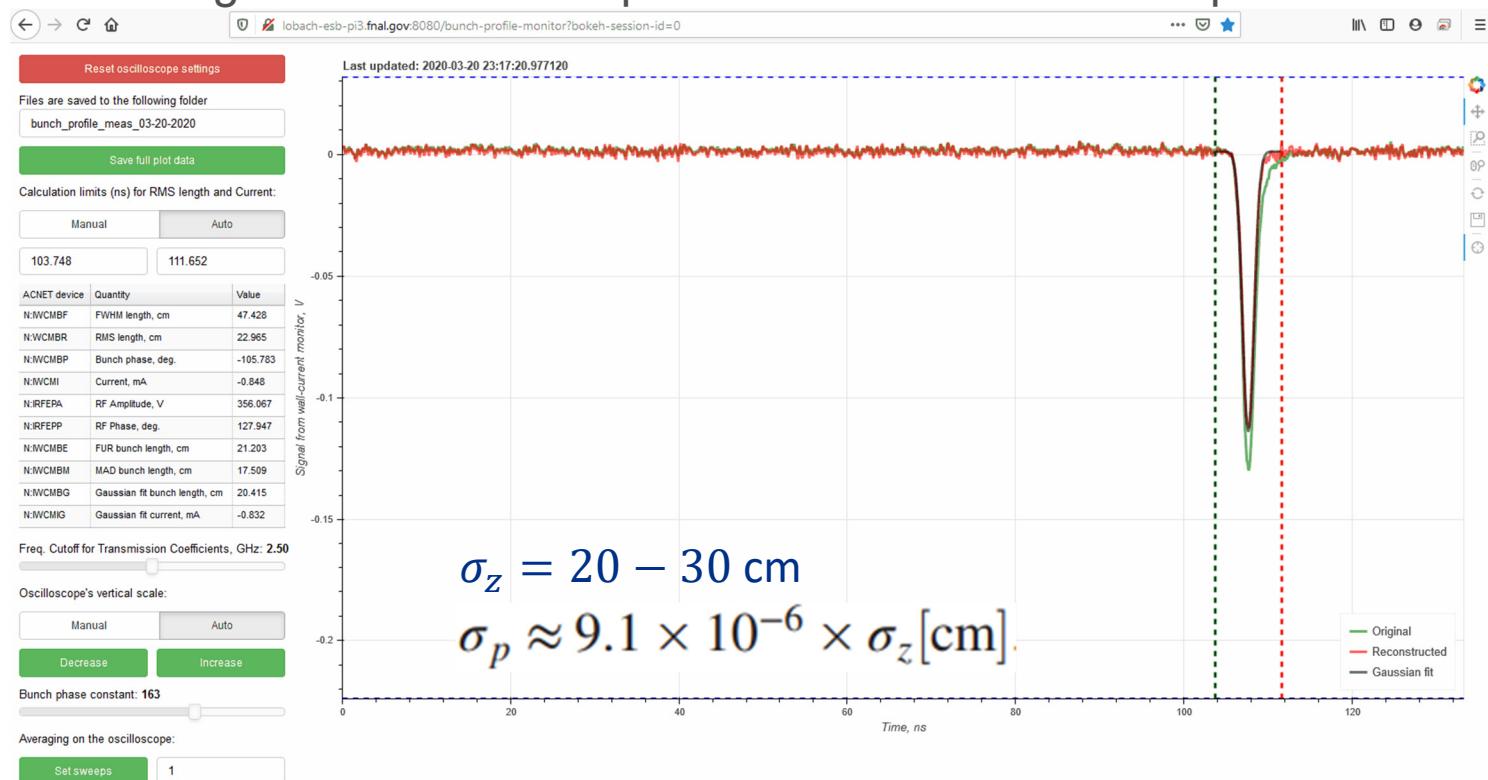
Bending magnet radiation (not undulator)



*built by A. Romanov, J. Santucci, G. Stancari, N. Kuklev, ...

Measurement of longitudinal bunch length and shape: Bunch length monitor

- Wall-current monitor → long cable → amplifier → oscilloscope
- The web-server runs on a Raspberry Pi on the Fermilab controls network. It receives the signal from the scope and applies the inverse of the transmission function of the long cable and the amplifier to reconstruct the shape of the electron bunch

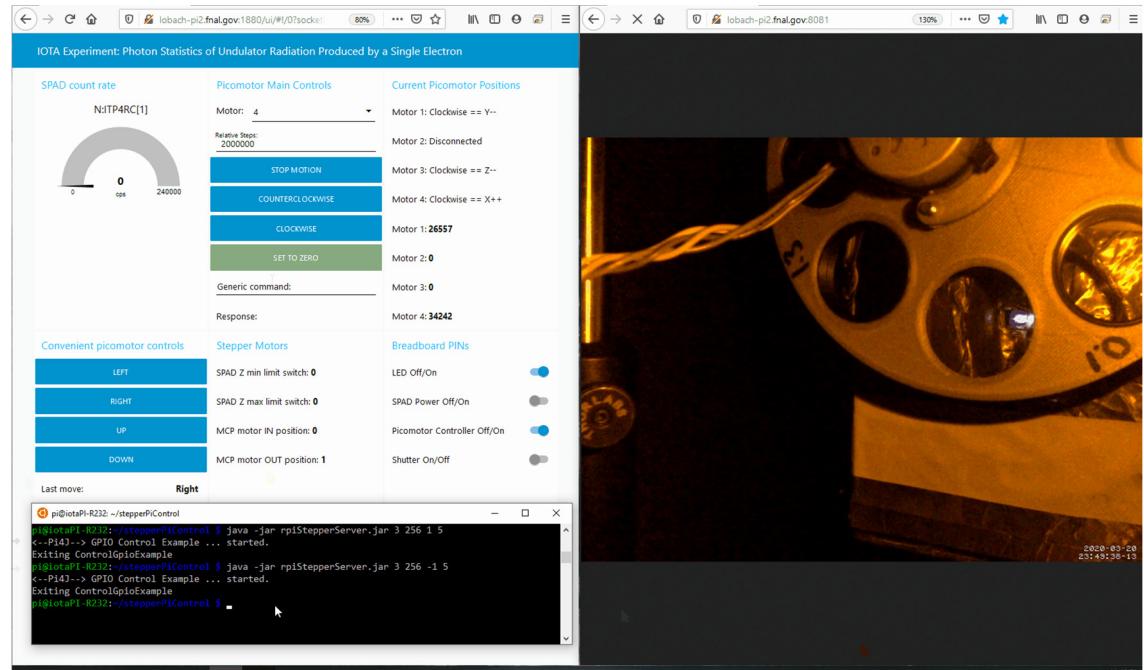


Valeri Lebedev and Kermit Carlson helped with measurement of the transmission function.
Dean Edstrom helped with network communication with the oscilloscope.

Neutral density (ND) filters

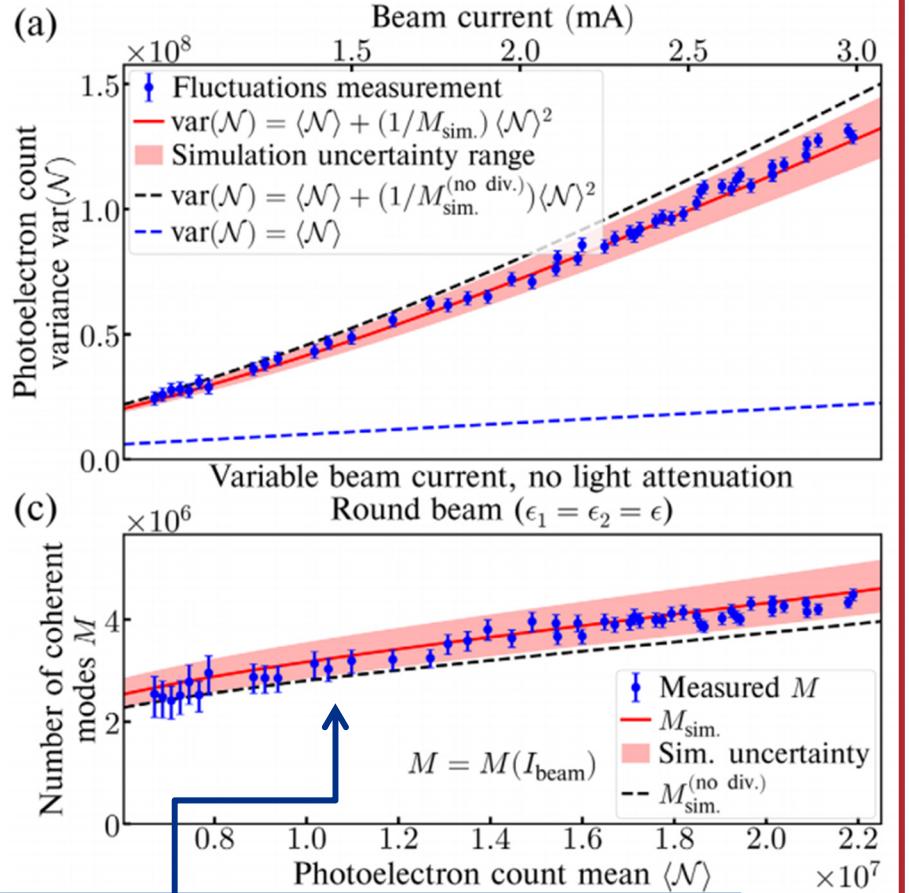
- ND filter is a filter that has constant attenuation in a wide spectral range
- ND filter does not change the number of coherent modes M , however, it does change the average number of detected photons $\langle \mathcal{N} \rangle$

Remote controls for the apparatus

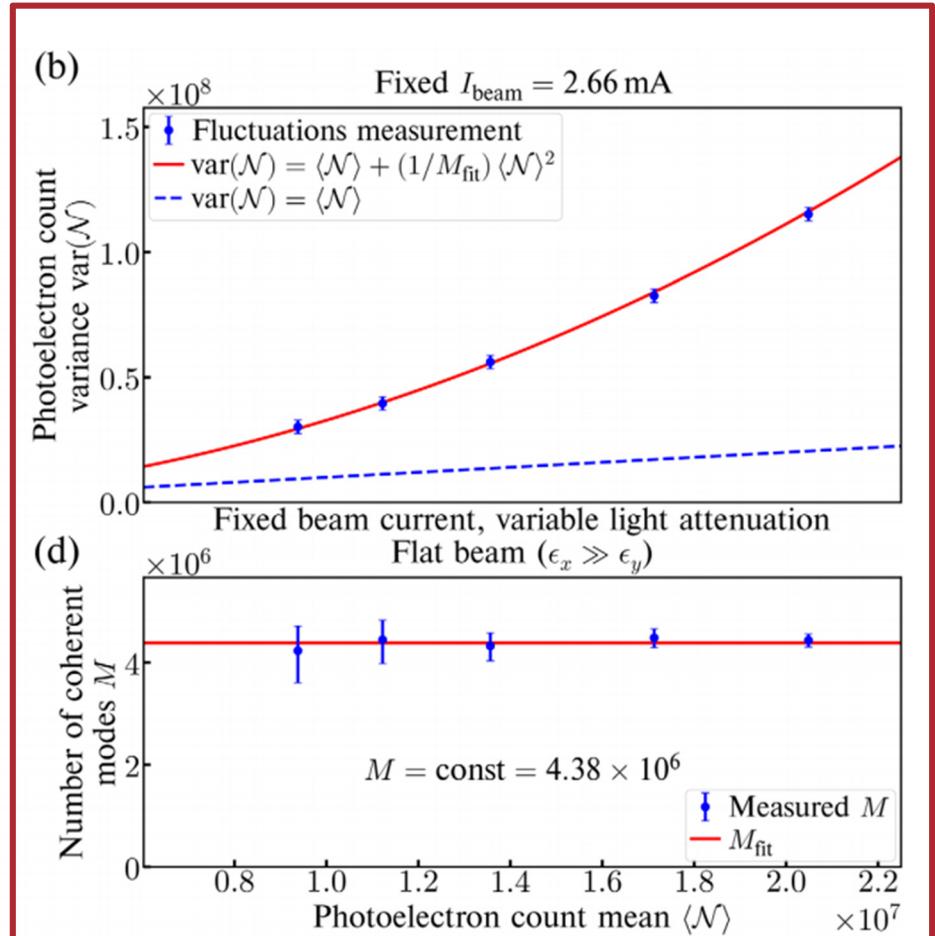


The filter wheel was built
by Sasha Romanov

Measurements with ND filters (right-hand side)



$\epsilon_x, \epsilon_y, \sigma_z^{\text{eff}}, \sigma_p$ change with the beam current due to intrabeam scattering and interaction of the bunch with its environment. Therefore, M changes too.



Reconstruction of transverse emittances from the measured $\text{var}(\mathcal{N})$

Featured in Physics

Editors' Suggestion

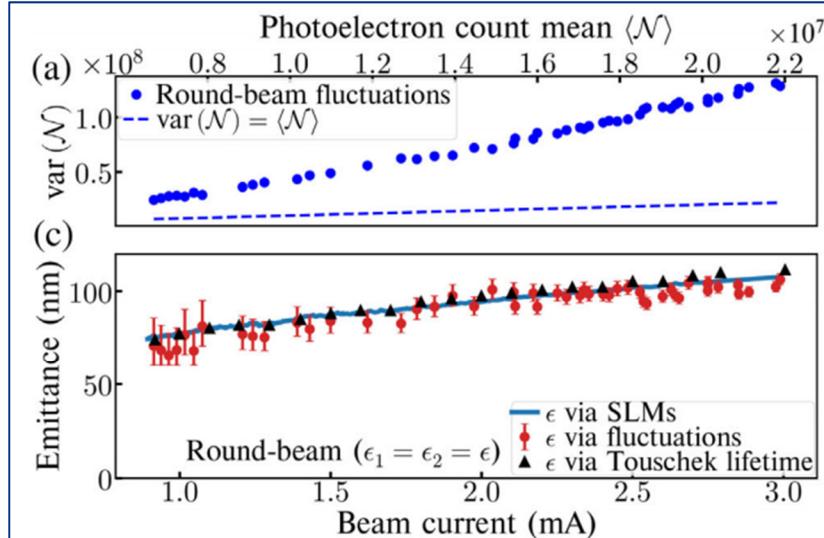
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Transverse Beam Emittance Measurement by Undulator Radiation Power Noise

Ihar Lobach, Sergei Nagaitsev, Valeri Lebedev, Aleksandr Romanov, Giulio Stancari, Alexander Valishev, Aliaksei Halavanau, Zhirong Huang, and Kwang-Je Kim
Phys. Rev. Lett. **126**, 134802 – Published 1 April 2021



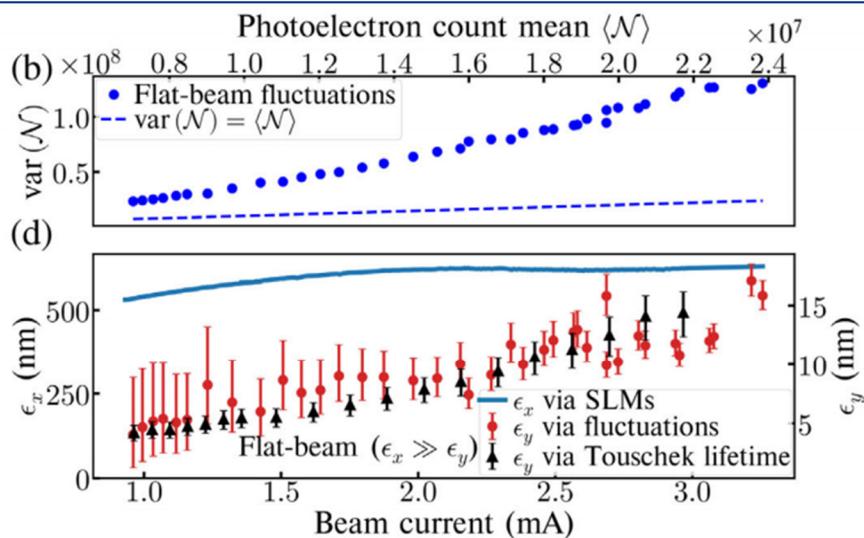
We verified our method with a “round” beam, whose emittances could be independently measured by synchrotron radiation monitors, (a) and (c):



Strong coupling



Then, we used our fluctuations-based method to measure the unknown small vertical emittance of a “flat” beam, (b) and (d):



Uncoupled



Limitations (or strengths?)

- The fluctuations must not be dominated by the Poisson noise

$$\langle \mathcal{N} \rangle \lesssim \frac{1}{M} \langle \mathcal{N} \rangle^2 \quad \rightarrow \quad \frac{\langle \mathcal{N} \rangle}{M} = \alpha \left(\frac{\pi}{2} \right)^{\frac{3}{2}} F_h(K_u) \frac{\gamma^2 N_u^2 n_e}{\sigma_x \sigma_y \sigma_z k_0^3} \gtrsim 1$$

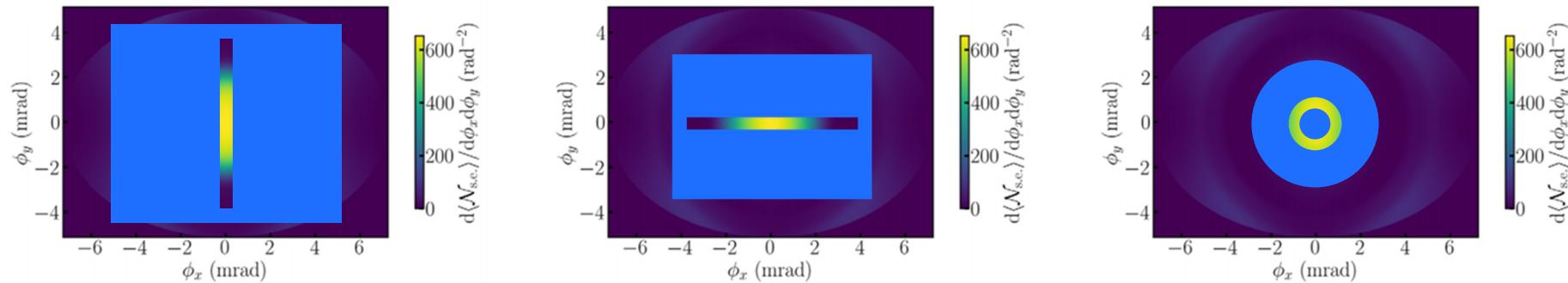
- M must be sensitive to changes in σ_x, σ_y (ϵ_x, ϵ_y)

$$\sigma_x, \sigma_y \gtrsim \sqrt{2L_u \lambda_0} / (4\pi)$$



The sensitivity of this technique improves with shorter wavelength. Therefore, this technique may be particularly beneficial for existing state-of-the-art and next-generation low-emittance high-brightness ultraviolet and x-ray synchrotron light sources. For instance, this technique can measure $\epsilon_x \approx \epsilon_y \approx 30$ pm in the Advanced Photon Source Upgrade at Argonne.

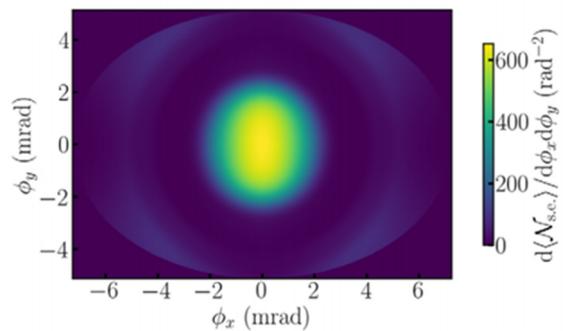
Usage of slits and masks



- Measurement of fluctuations with slits or masks would allow measurement of more than one electron bunch parameter.

$$M = \sqrt{1 + 4\sigma_k^2\sigma_z^2} \sqrt{1 + 4k_0^2\sigma_{\theta_x}^2\sigma_x^2} \sqrt{1 + 4k_0^2\sigma_{\theta_y}^2\sigma_y^2}$$

Original angular distribution:



Conclusions

- Turn-to-turn undulator radiation power fluctuations have two contributions: (1) quantum due to discrete nature of light and (2) classical due to variations in relative electron positions and directions of motion.
- We derived the second contribution, accounting for electron beam divergence, for the first time.
- We obtained a good agreement for the fluctuations $\text{var}(\mathcal{N})$ between measurements and calculations.
- The process can be reversed, i.e., the measured fluctuations $\text{var}(\mathcal{N})$ can be used to infer the transverse electron beam emittances. This method can be especially useful for low-emittance high-brightness ultraviolet and x-ray synchrotron light sources.

Thesis advisors:

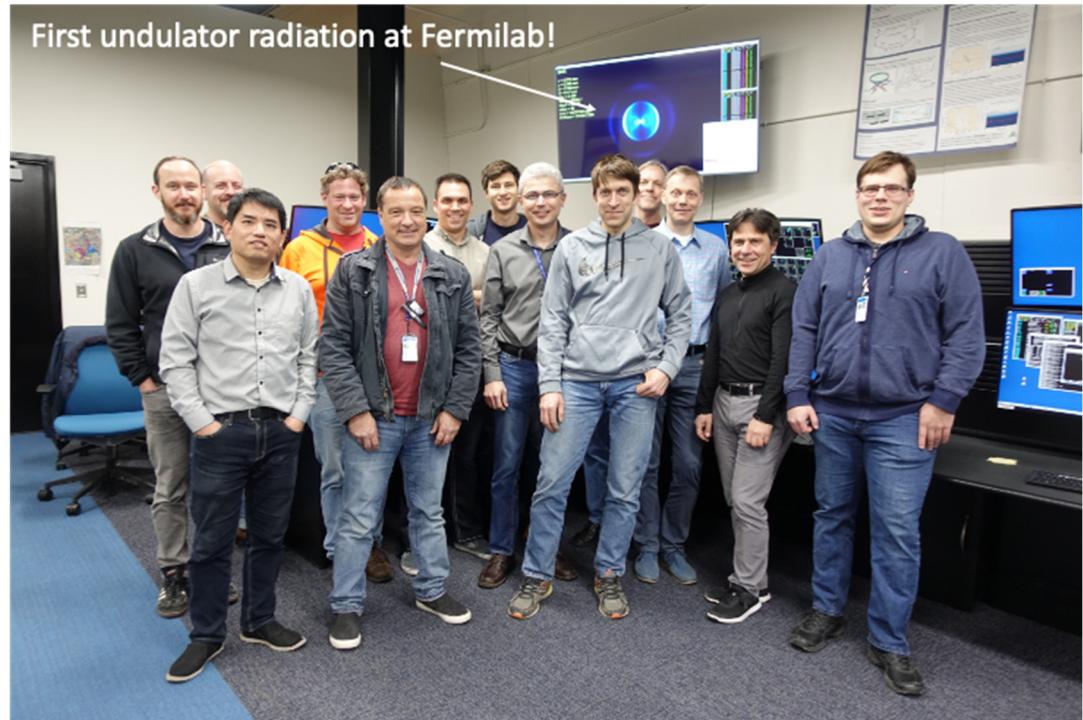


Sergei Nagaitsev
(UChicago/Fermilab)



Giulio Stancari
(Fermilab)

IOTA team:



Aleksandr Romanov and Alexander Valishev tuned the ring and the beam. Mark Obrycki, James Santucci, Wayne Johnson, Dean Edstrom, and Kermit Carlson helped build the apparatus. Greg Saewert constructed the photodiode detection circuit and provided the test light source. Brian Fellenz, Daniil Frolov, David Johnson, and Todd Johnson provided some equipment and assisted during our detector tests. We had useful discussions about theoretical description with Valeri Lebedev and our collaborators from SLAC --- Aliaksei Halavanau and Zhirong Huang --- who also kindly provided the undulator.

Thank you for your attention!