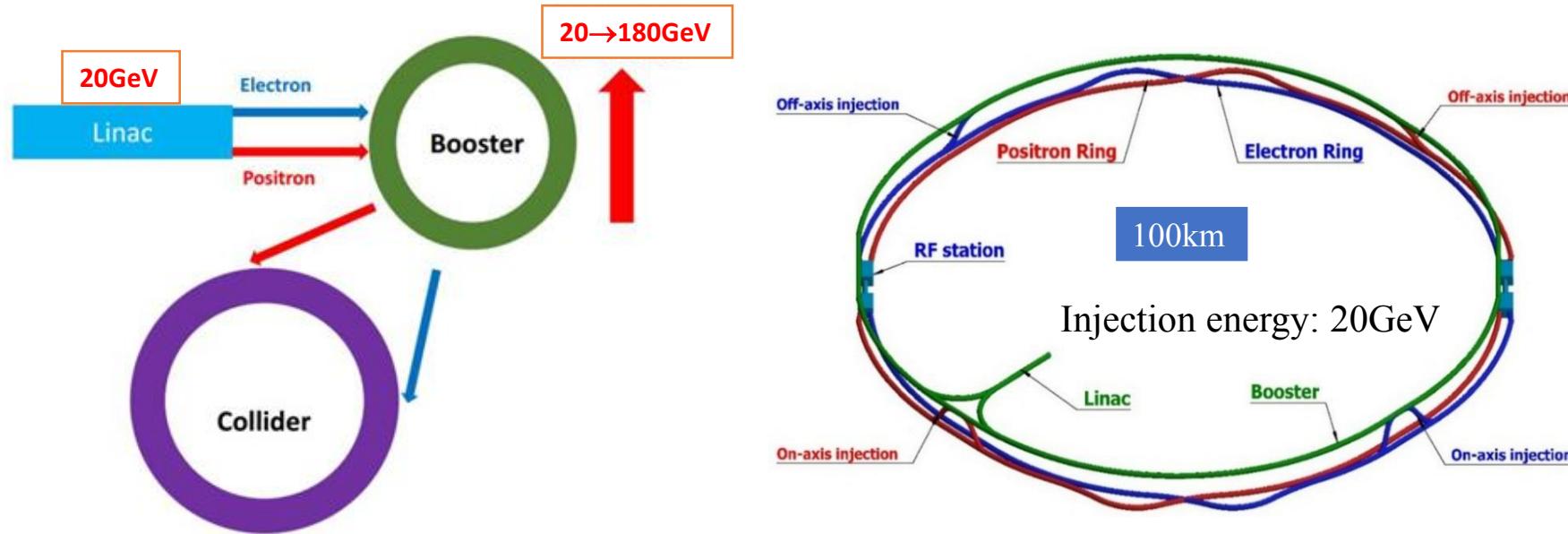


# CEPC booster lattice design

Dou Wang (IHEP)

on behalf of CEPC AP group

# CEPC injector chain

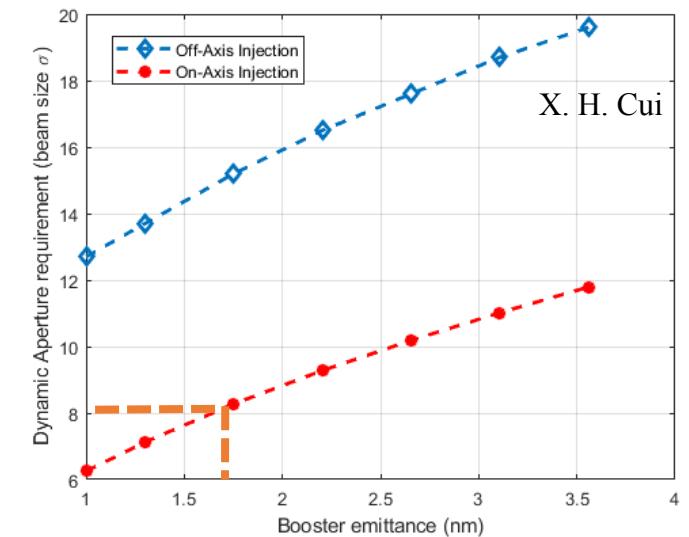


- 20 GeV linac provides electron and positron beams for booster.
- Top up injection for collider ring  $\sim 3\%$  current decay
- Booster is in the same tunnel as collider ring, above the collider ring, bypass in IR.
- Budget for transfer efficiency **90%: 95% for booster + 95% for transport lines.**
- Beam current threshold in booster is limited by RF system.
- Feedback systems (Transverse & longitudinal) are need to damp the instability at low energy.

# Requirement update for booster

Collider ring	Higgs (CDR)	Higgs (TDR)
Number of IPs	2	2
Energy (GeV)	120	120
Circumference (km)	100	100
SR loss/turn (GeV)	1.73	1.8
Half crossing angle (mrad)	16.5	
Piwnski angle	3.48	5.94
$N_e/\text{bunch} (10^{10})$	15.0	13.0
Bunch number	242	268
Beam current (mA)	17.4	16.7
SR power /beam (MW)	30	30
Bending radius (km)	10.7	10.2
Momentum compaction ( $10^{-6}$ )	11.1	7.1
$\beta_{IP} x/y$ (m)	0.36/0.0015	0.3/0.001
Emittance x/y (nm)	1.21/0.0024	0.64/0.0013
Transverse $\sigma_{IP}$ (um)	20.9/0.06	14.0/0.036
$\xi_x/\xi_y/IP$	0.018/0.109	0.015/0.11
$V_{RF}$ (GV)	2.17	2.20
$f_{RF}$ (MHz) (harmonic)	650 (216820)	
Nature bunch length $\sigma_z$ (mm)	2.72	2.3
Bunch length $\sigma_z$ (mm)	4.4	4.1
Energy spread (%) (SR/BS)	0.1/0.134	0.1/0.17
Energy acceptance requirement (%)	1.35	1.6
Energy acceptance by RF (%)	2.06	2.2
Lifetime due to beamstrahlung (min)	80	40
Lifetime (min)	25	20
$F$ (hour glass)	0.89	0.9
$L_{max}/IP (10^{34}\text{cm}^{-2}\text{s}^{-1})$	2.93	5.0

- Horizontal DA requirement of collider ring due to injection

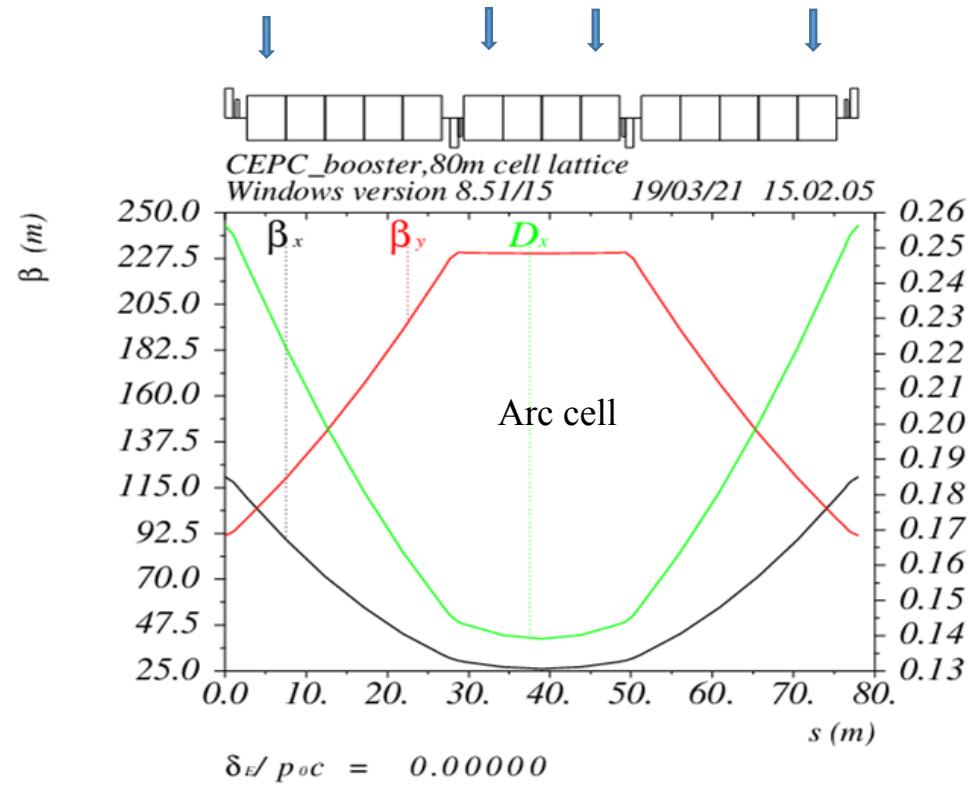


- Booster emittance @120 GeV <1.7nm (3.6nm in CDR)

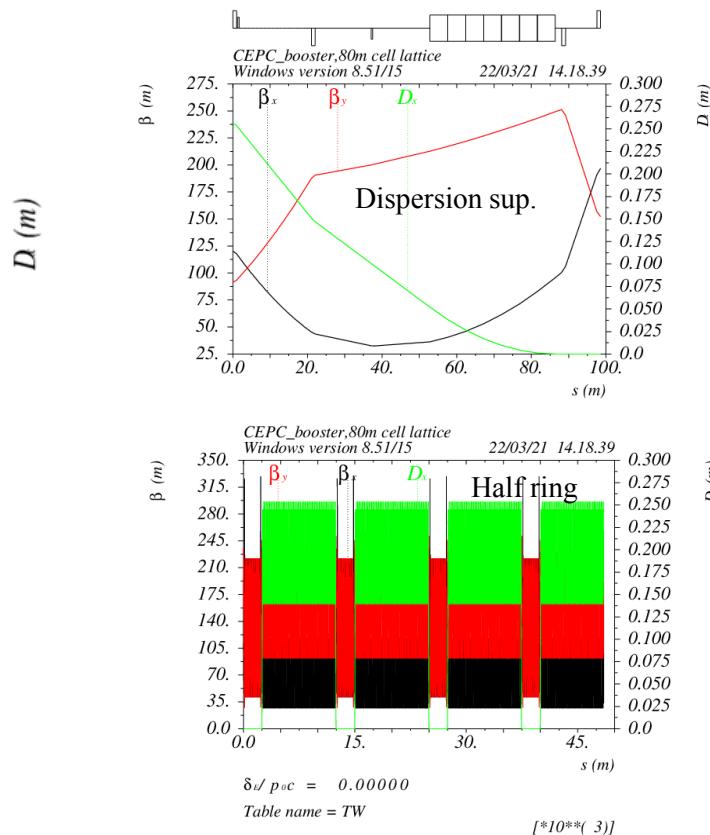
# Booster TDR optics

D. Wang, C. H. Yu, Y. M. Peng...

- TME like structure (cell length=78m)
- Interleave sextupole scheme
- Emittance@120GeV=1.26nm

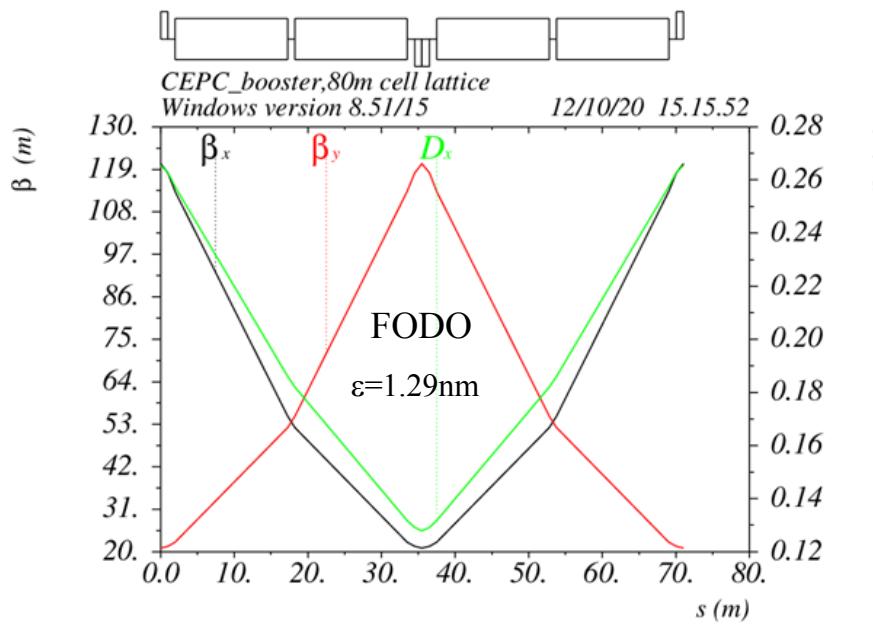


- Overall idea: uniform distribution for the Q
- Combined magnet (B+S) scheme possible
- Phase advance/cell: 100° (H) / 28° (V)

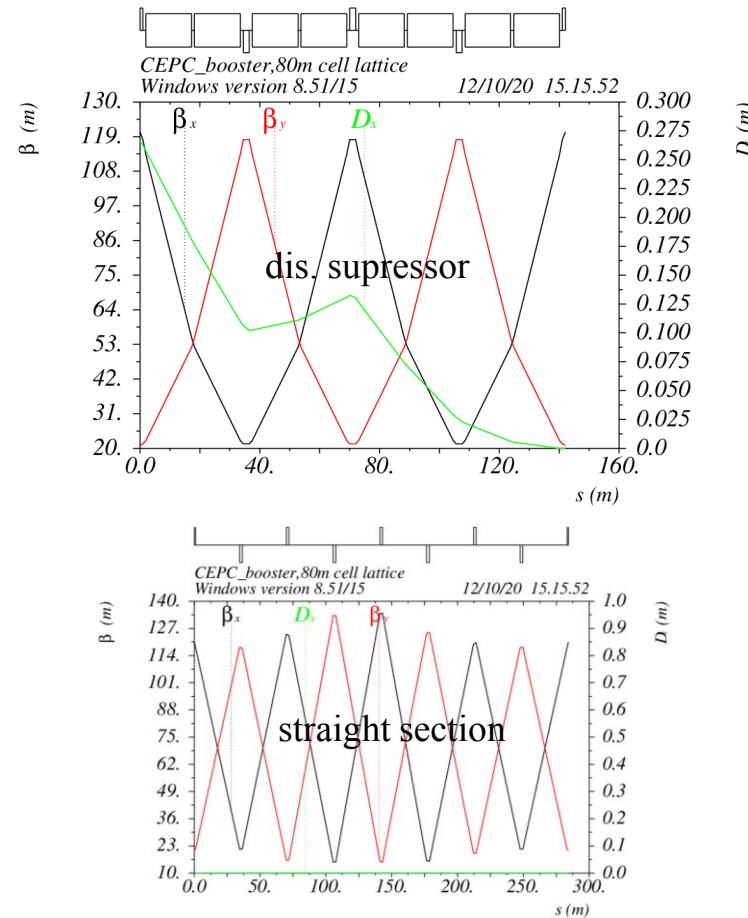


# Booster alternative optics

- FODO structure (cell length=70m)
- $90^\circ/90^\circ$  phase advance
- Non-interleave sextupole scheme
- Similar structure as CDR

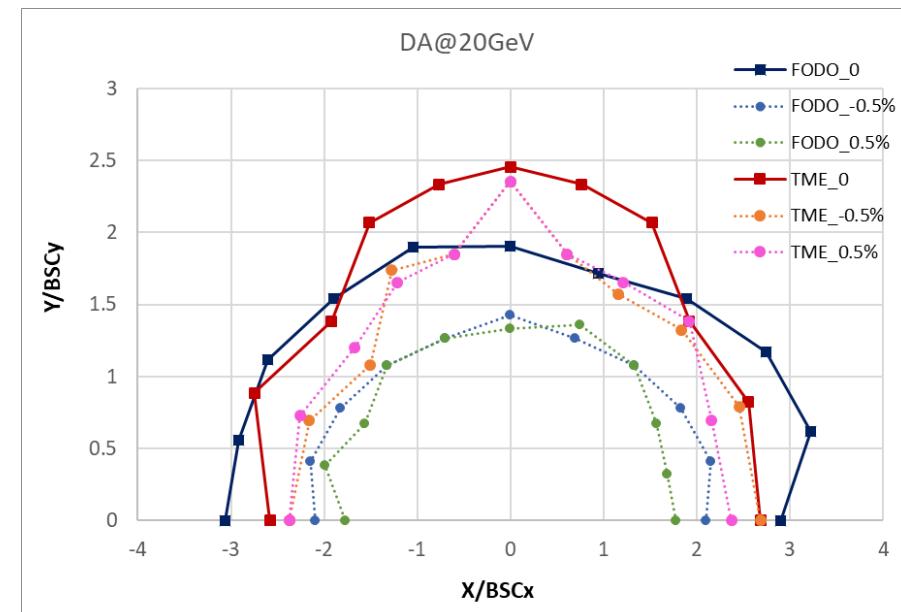
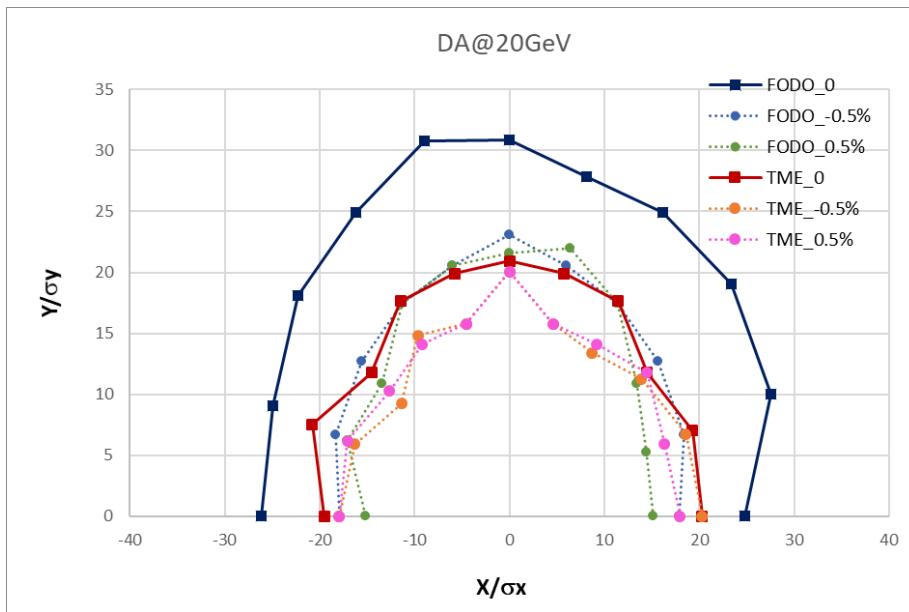


- Emittance@120GeV=**1.29nm**



# DA results @ 20GeV

- Booster energy: 20GeV~180GeV
- 20GeV:  $BSC_{xy} = (4\sigma_{xy} + 5\text{mm}) * 2$
- Inj. emittance from Linac: 10nm
- Energy spread from Linac: 0.16%



# DA results with errors and correction (w/o multipoles)

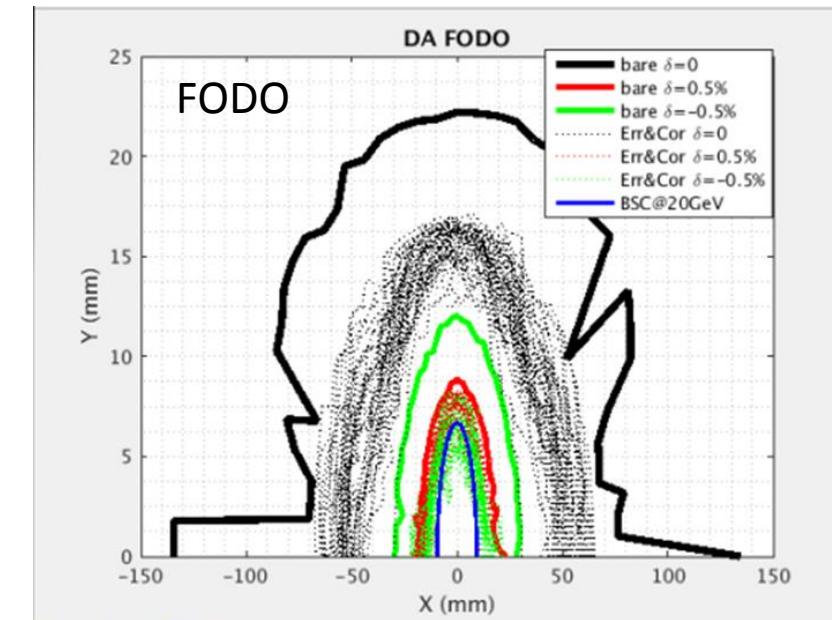
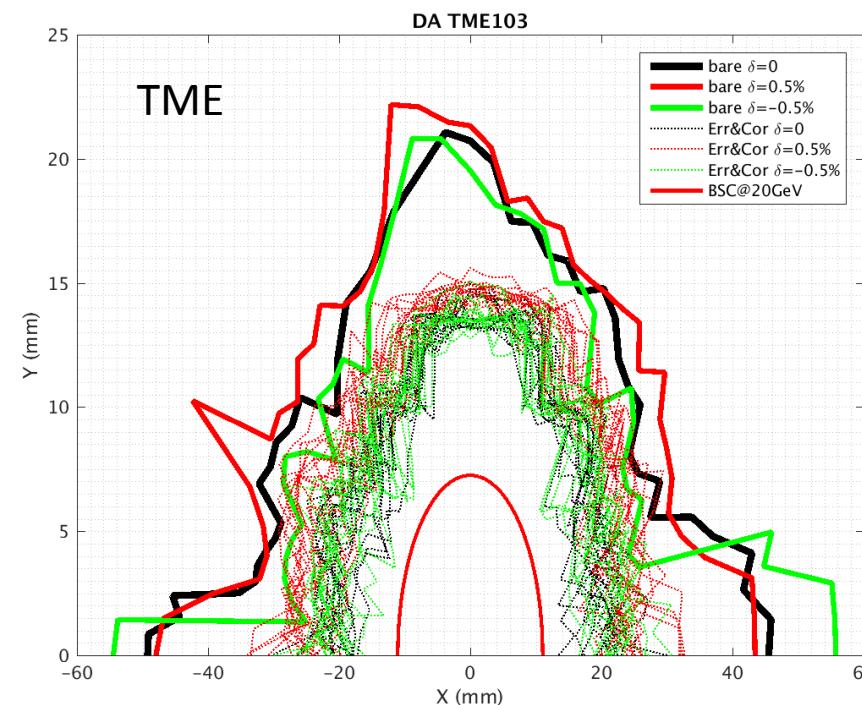
D. H. Ji

	Dipole	Quadrupole	Sextupole
<b>Transverse shift X/Y (μm)</b>	100	100	100
<b>Longitudinal shift Z (μm)</b>	100	150	100
<b>Tilt about X/Y (mrad)</b>	0.2	0.2	0.2
<b>Tilt about Z (mrad)</b>	0.1	0.2	0.2
<b>Nominal field</b>	1e-3	2e-4	3e-4

	Accuracy (m)	Tilt (mrad)	Gain	Offset w/ BBA(mm)
<b>BPM(10Hz)</b>	1e-7	10	5%	30e-3

➤ error correction (w/o SR effect)

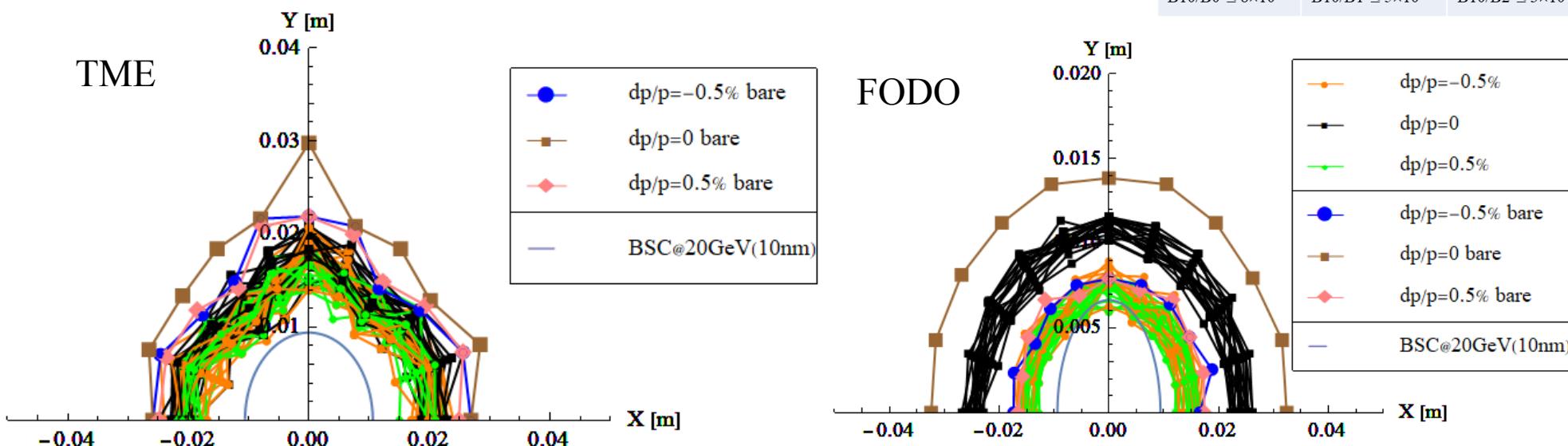
- Orbit correction
- Optics correction



# Multipole errors @ 20GeV

- Multipole errors only
- Multipole errors can not be corrected
- TME is chosen as the baseline for TDR.

dipole	quadrupole	sextupole
$B1/B0 \leq 2 \times 10^{-4}$		
$B2/B0 \leq 3 \times 10^{-4}$	$B2/B1 \leq 3 \times 10^{-4}$	
$B3/B0 \leq 2 \times 10^{-5}$	$B3/B1 \leq 1 \times 10^{-4}$	$B3/B2 \leq 1 \times 10^{-3}$
$B4/B0 \leq 8 \times 10^{-5}$	$B4/B1 \leq 1 \times 10^{-4}$	$B4/B2 \leq 3 \times 10^{-4}$
$B5/B0 \leq 2 \times 10^{-5}$	$B5/B1 \leq 1 \times 10^{-4}$	$B5/B2 \leq 1 \times 10^{-3}$
$B6/B0 \leq 8 \times 10^{-5}$	$B6/B1 \leq 5 \times 10^{-5}$	$B6/B2 \leq 3 \times 10^{-4}$
$B7/B0 \leq 2 \times 10^{-5}$	$B7/B1 \leq 5 \times 10^{-5}$	$B7/B2 \leq 1 \times 10^{-3}$
$B8/B0 \leq 8 \times 10^{-5}$	$B8/B1 \leq 5 \times 10^{-5}$	$B8/B2 \leq 3 \times 10^{-4}$
$B9/B0 \leq 2 \times 10^{-5}$	$B9/B1 \leq 5 \times 10^{-5}$	$B9/B2 \leq 1 \times 10^{-3}$
$B10/B0 \leq 8 \times 10^{-5}$	$B10/B1 \leq 5 \times 10^{-5}$	$B10/B2 \leq 3 \times 10^{-4}$



# DA results with errors and correction

D. H. Ji

	Dipole	Quadrupole	Sextupole
<b>Transverse shift X/Y (μm)</b>	100	100	-
<b>Longitudinal shift Z (μm)</b>	100	150	-
<b>Tilt about X/Y (mrad)</b>	0.2	0.2	-
<b>Tilt about Z (mrad)</b>	0.1	0.2	-
<b>Nominal field</b>	1e-3	2e-4	3e-4

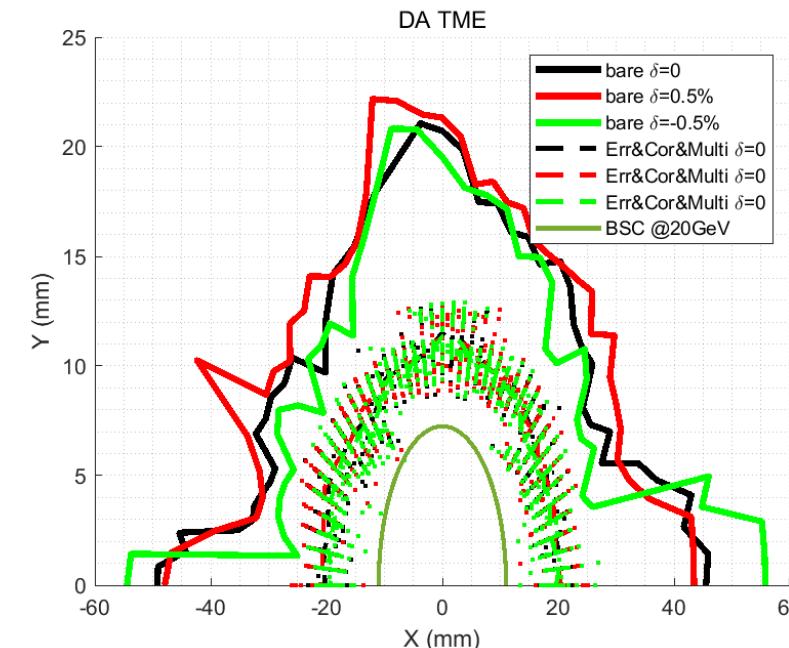
- Include multipole errors

dipole	quadrupole
$B_1/B_0 \leq 2 \times 10^{-4}$	
$B_2/B_0 \leq 5 \times 10^{-4}$	$B_2/B_1 \leq 3 \times 10^{-4}$
$B_3/B_0 \leq 2 \times 10^{-5}$	$B_3/B_1 \leq 2 \times 10^{-4}$
$B_4/B_0 \leq 8 \times 10^{-5}$	$B_4/B_1 \leq 1 \times 10^{-4}$
$B_5/B_0 \leq 2 \times 10^{-5}$	$B_5/B_1 \leq 1 \times 10^{-4}$
$B_6/B_0 \leq 8 \times 10^{-5}$	$B_6/B_1 \leq 5 \times 10^{-5}$
$B_7/B_0 \leq 2 \times 10^{-5}$	$B_7/B_1 \leq 5 \times 10^{-5}$
$B_8/B_0 \leq 8 \times 10^{-5}$	$B_8/B_1 \leq 5 \times 10^{-5}$
$B_9/B_0 \leq 2 \times 10^{-5}$	$B_9/B_1 \leq 5 \times 10^{-5}$
$B_{10}/B_0 \leq 8 \times 10^{-5}$	$B_{10}/B_1 \leq 5 \times 10^{-5}$

	Accuracy (m)	Tilt (mrad)	Gain	Offset w/ BBA(mm)
<b>BPM(10Hz)</b>	1e-7	10	5%	30e-3

- Orbit & Dispersion Correction (100 seeds)
  - Response Matrix (RM)+SVD
- Optics Correction (93 seeds)
  - RM + LOCO
- DA track in AT @20GeV

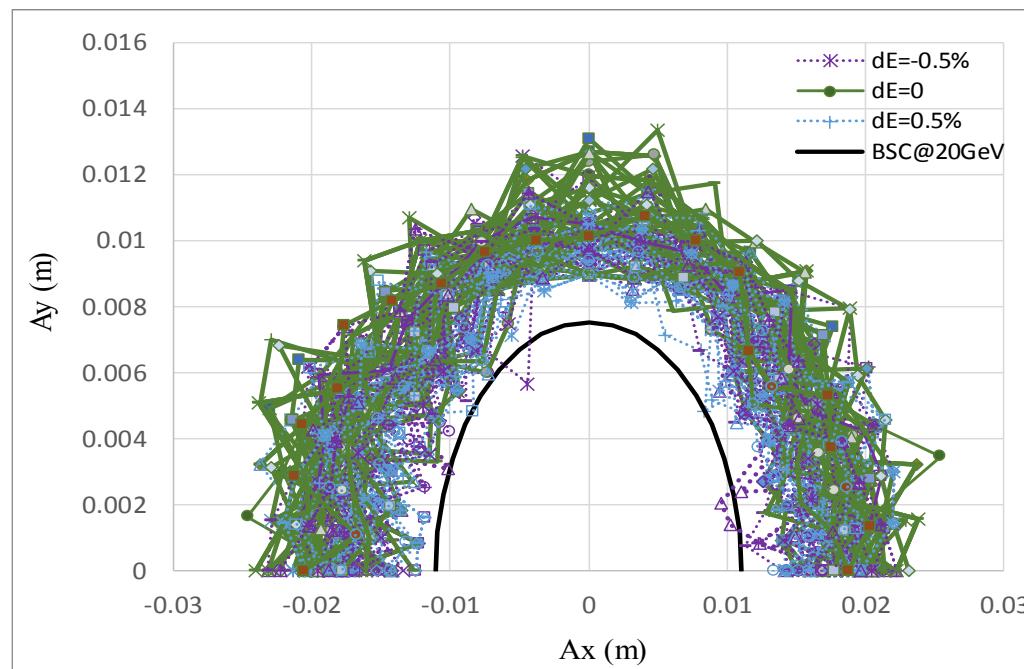
RMS	TME
Orbit (mm)	0.062/0.071
Beta Beating(%)	0.16/0.1
Δ Dispersion(mm)	1.2/3.3



# DA@20GeV

Dou Wang, Daheng Ji

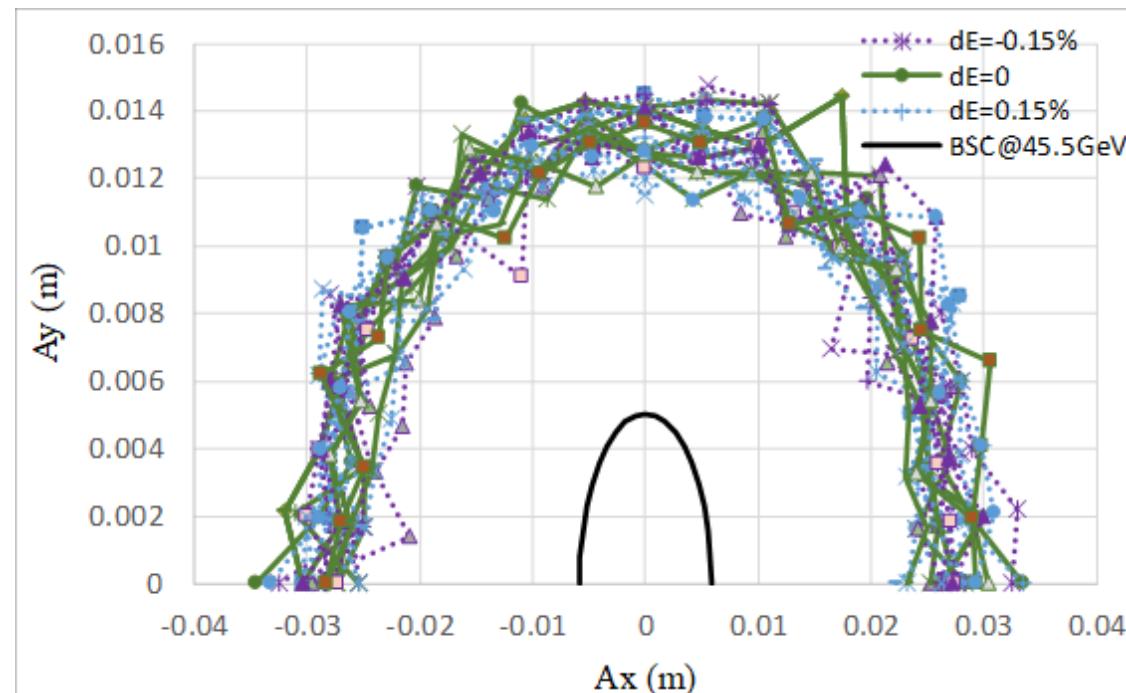
- Tracking by **SAD** (2500 turns)
- include errors (w. multipole errors)
- Include SR sawtooth orbit (without taper)
- Include SR damping & fluctuation
- On axis injection from Linac to booster
- BSC definition ( $\varepsilon_{inj}=10\text{nm}$ ):  
$$BSC_{x,y} = 2 \times (4 \cdot \sigma_{x,y} + 5\text{mm})$$
- Energy acceptance:  $3 \cdot \delta_{inj} = 0.48\%$



# DA@45GeV

Dou Wang, Daheng Ji

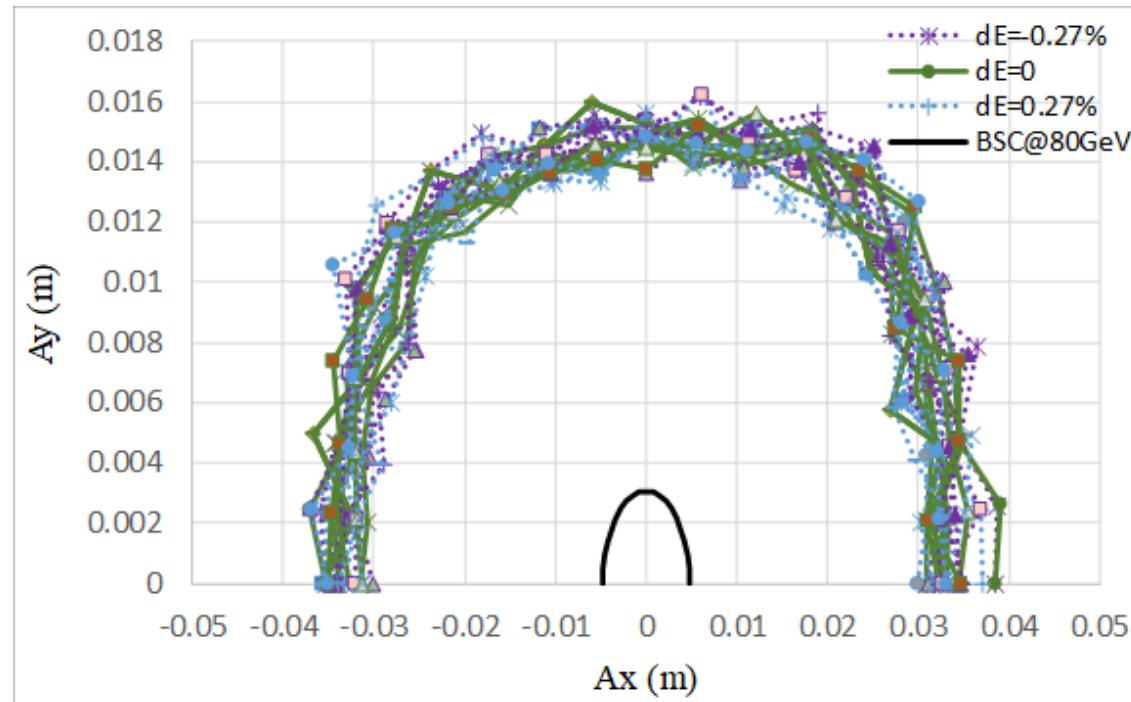
- Tracking by **SAD** (1200 turns)
- include errors (w. multipole errors)
- Include SR sawtooth orbit (without taper)
- Include SR damping & fluctuation
- Off axis injection from booster to collider
- BSC definition ( $\varepsilon_x=0.18\text{nm}$ ,  $\varepsilon_y=\varepsilon_x * 1\%$ ):  
$$BSC_{x,y} = 2 \times (4 \cdot \sigma_{x,y} + 5\text{mm})$$
- Energy acceptance:  $4 * \delta = 0.15\%$



# DA@80GeV

Dou Wang, Daheng Ji

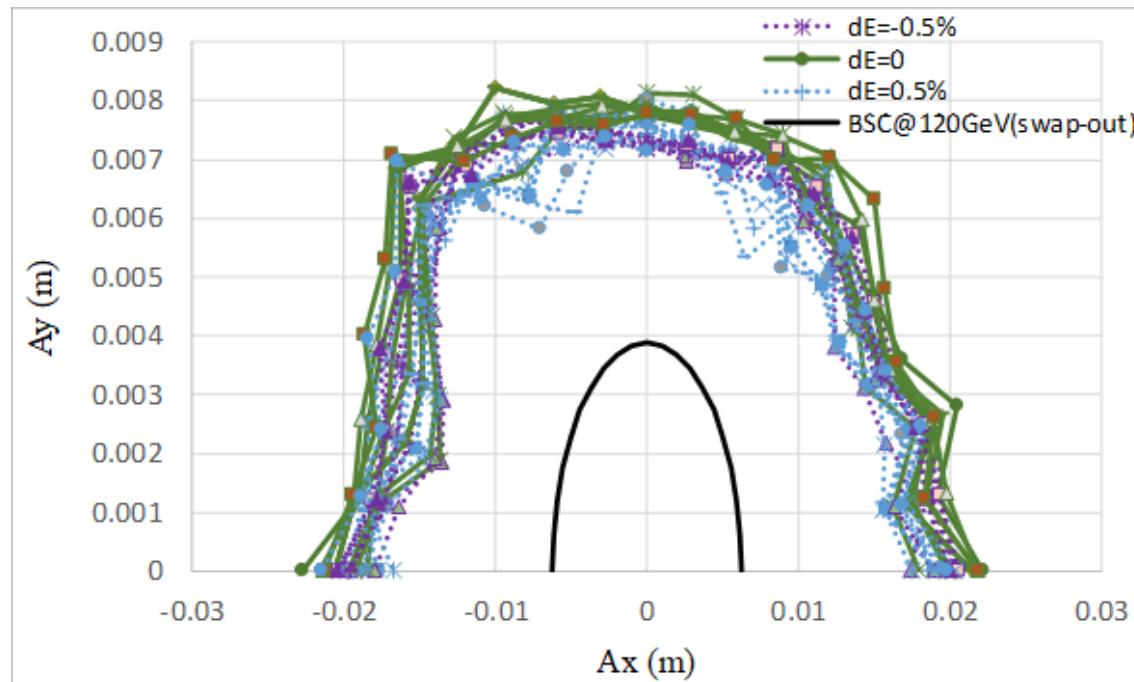
- Tracking by **SAD** (500 turns)
- include errors (w. multipole errors)
- Include SR sawtooth orbit (without taper)
- Include SR damping & fluctuation
- Off axis injection from booster to collider
- BSC definition ( $\varepsilon_x=0.56\text{nm}$ ,  $\varepsilon_y=\varepsilon_x * 1\%$ ):  
$$BSC_{x,y} = 2 \times (5 \cdot \sigma_{x,y} + 3\text{mm})$$
- Energy acceptance:  $4 * \delta = 0.27\%$



# DA@120GeV

Dou Wang, Daheng Ji

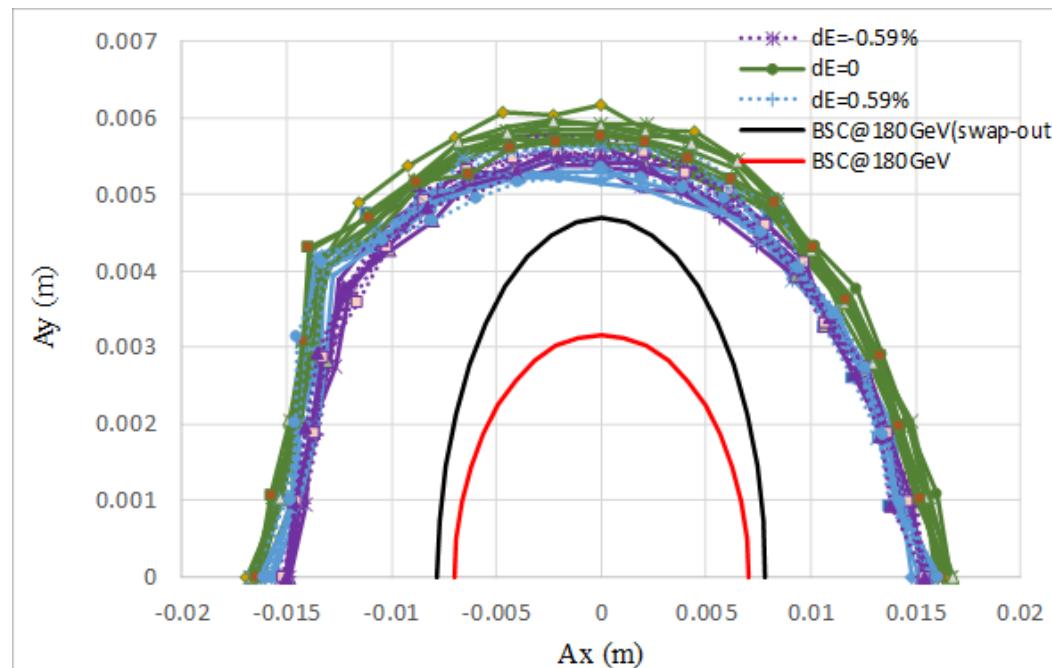
- Tracking by **SAD** (250 turns)
- include errors (w. multipole errors)
- Include SR sawtooth orbit (without taper)
- Include SR damping & fluctuation
- On axis injection from booster to collider
- BSC definition ( $\varepsilon_x = 1.26\text{nm}$ ,  $\varepsilon_y = \varepsilon_x * 1\%$ ):  
 $BSC_x = 2 \times (6 \cdot \sigma_x + 3\text{mm})$     $BSC_y = 2 \times (39 \cdot \sigma_y + 3\text{mm})$
- Energy acceptance:  $5 * \delta = 0.5\%$



# DA@180GeV

Dou Wang, Daheng Ji

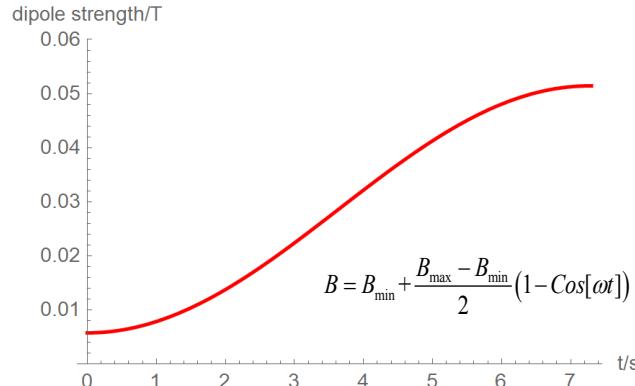
- Tracking by **SAD** (150 turns)
- include errors (w. multipole errors)
- Include SR sawtooth orbit (**with taper**)
- Include SR damping & fluctuation
- Keep possibility for on axis injection to collider
- BSC definition ( $\varepsilon_x = 2.84\text{nm}$ ,  $\varepsilon_y = \varepsilon_x * 1\%$ ):
  - $BSC_x = 2 \times (6 \cdot \sigma_x + 3\text{mm})$   $BSC_y = 2 \times (50 \cdot \sigma_y + 3\text{mm})$
  - $BSC_{x,y} = 2 \times (5 \cdot \sigma_{x,y} + 3\text{mm})$
- Energy acceptance:  $4 * \delta = 0.59\%$



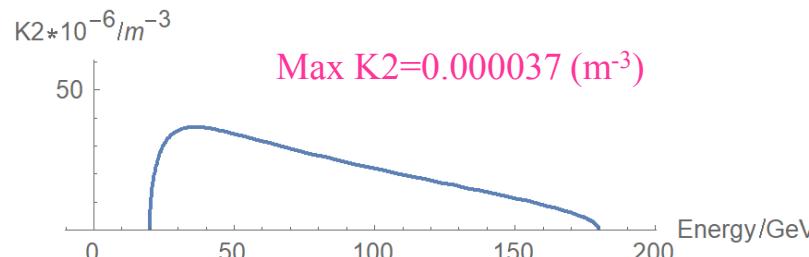
# Eddy current effect

Dou Wang, Yuemei Peng,  
Daheng Ji

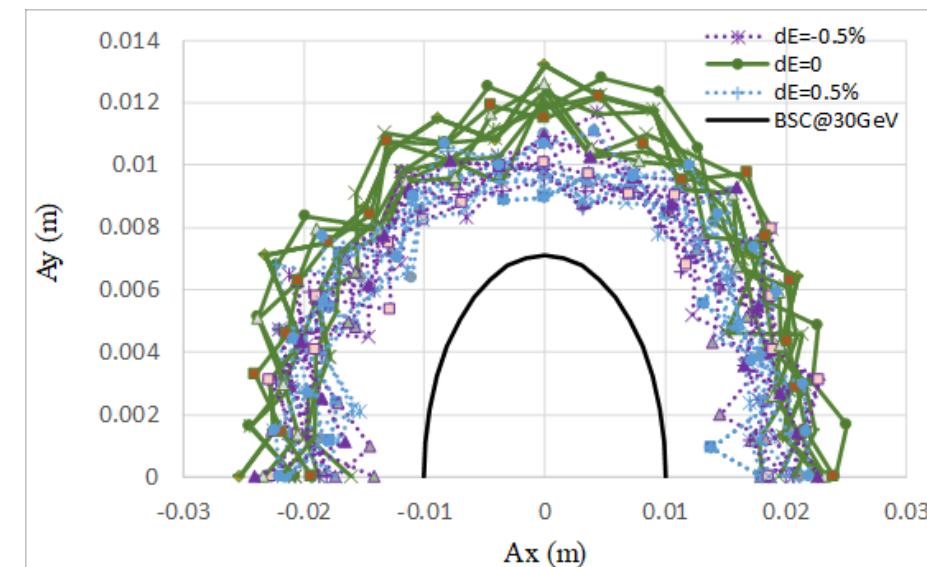
- Dedicated ramping curve to control the maximum K2.



- Analytical estimation for eddy effect\*
- K2 reaches max at 30GeV.



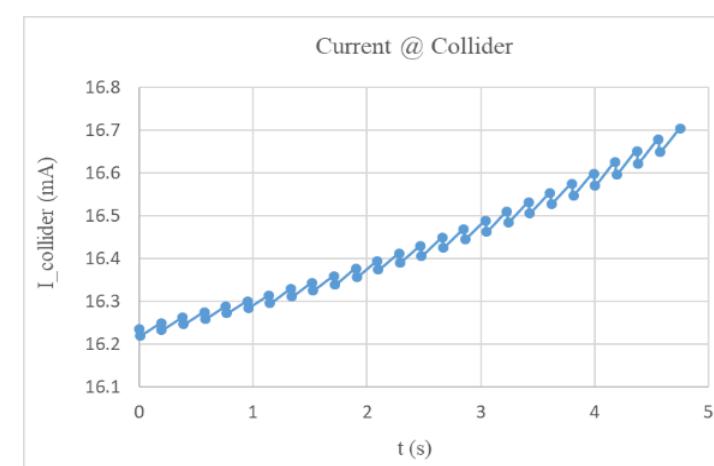
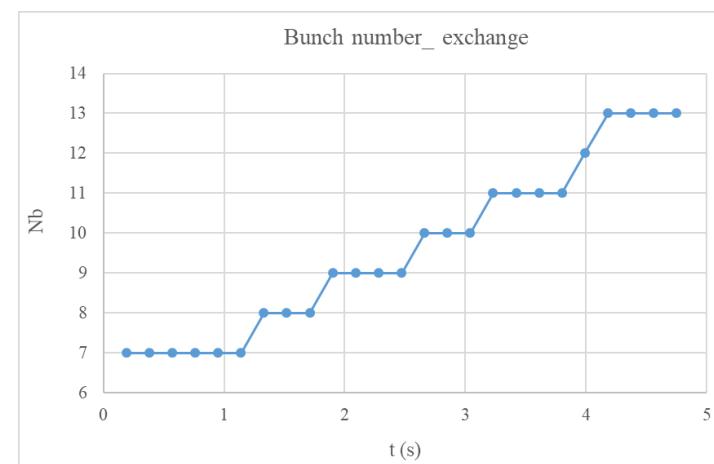
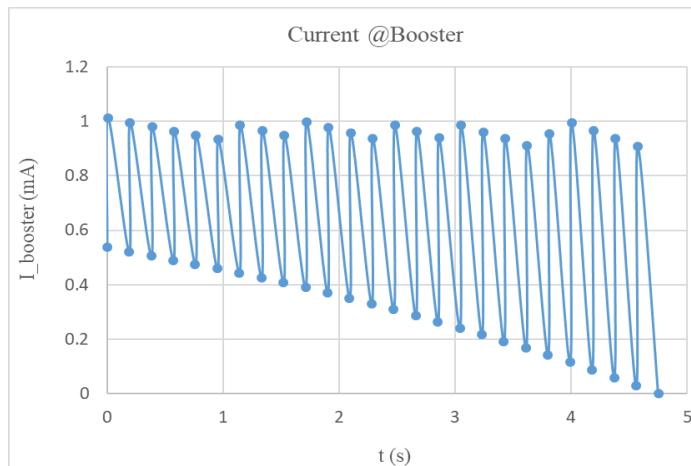
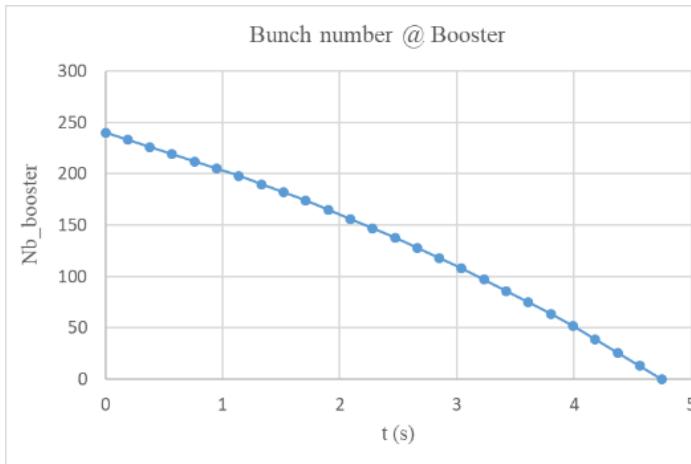
- Al beam pipe (round shape)
  - inner diameter: 55mm, thickness: 2mm
- Dynamic chromaticity is not corrected.
  - Sextupole field is attached to dipole
- DA tracking including eddy effect and error effects
- Independent sext. (~100) — chromaticity adjustment



\*Yuan Chen et al., Analytical expression development for eddy field and the beam dynamics effect on the CEPC booster, IJMPA, Vol. 36, No. 22 (2021) 2142010

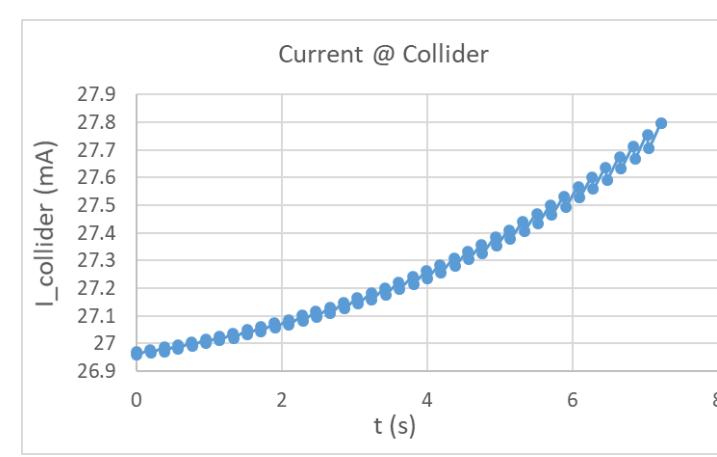
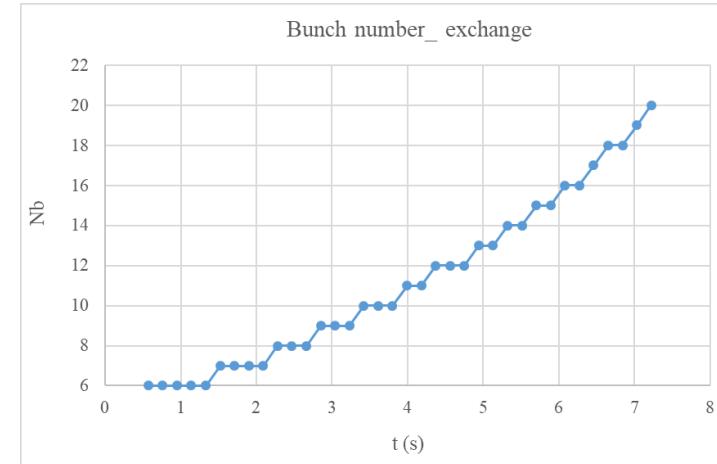
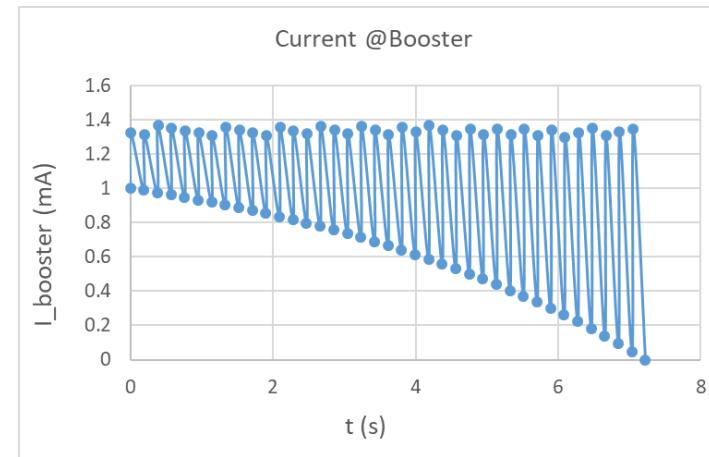
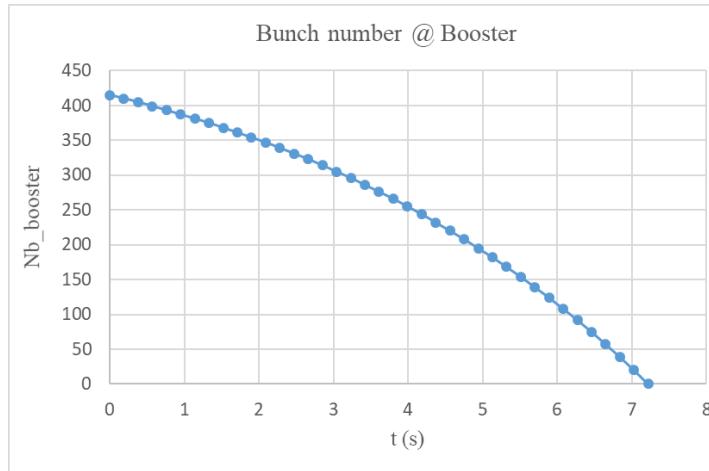
# On-axis injection at Higgs energy

- Swap-out injection
- Current threshold in booster: 1A
- Current decay for collider: 3% (top up mode)
- 4 damping times to merge the bunches in booster



# On-axis injection at Higgs energy (50MW upgrade)

- Swap-out injection
- Current threshold in booster: 1.4 A
- Current decay for collider: 3% (top up mode)
- Small upgrade for the RF power source



# Beam beam instability for on-axis injection

Yuan Zhang

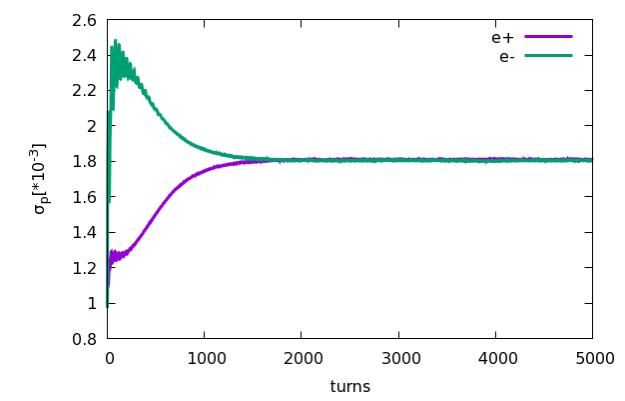
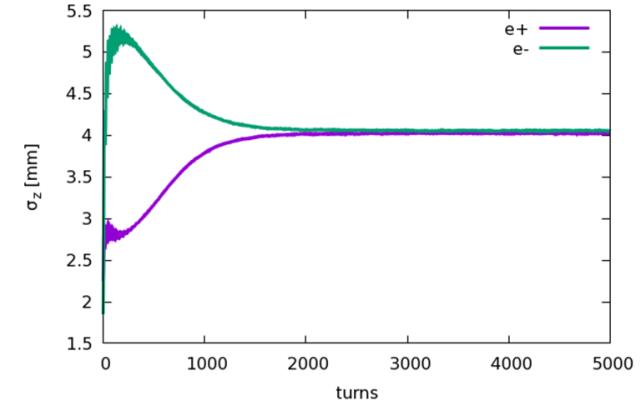
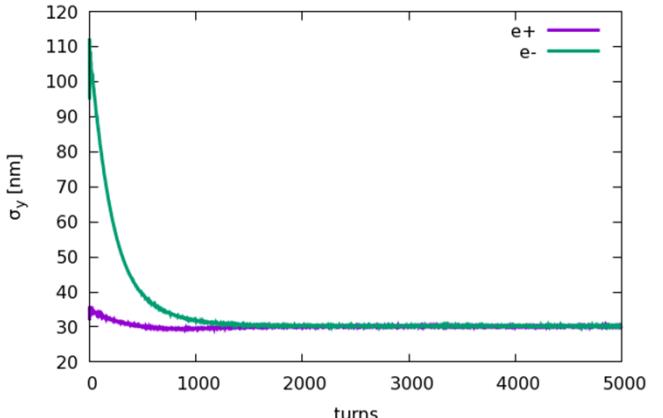
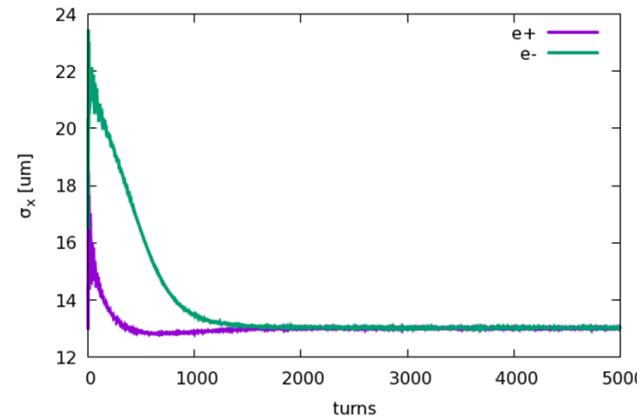
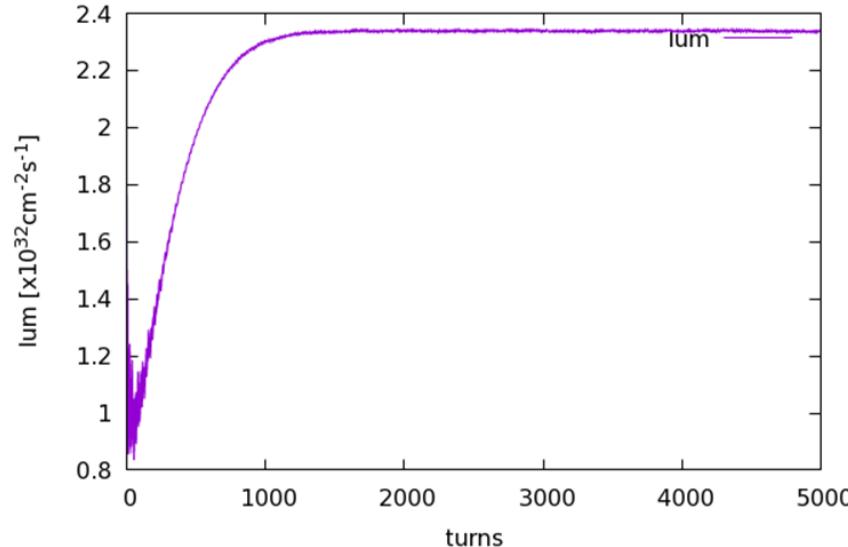
- ❖ Collision stability check for on-axis injection scheme at 120GeV

○ e- ( $N_e = 14 \times 10^{10}$ )

○ e+ ( $N_e = 14 \times 10^{10}$ )

- Emittance X = 1.26nm
- Energy spread = 0.1%
- Bunch length=1.85mm
- Coupling=1.0%

- Emittance X = 0.64nm
- Energy spread = 0.1%
- Bunch length=2.25mm
- Coupling=0.2%



# Dipole reproducibility requirement@20GeV

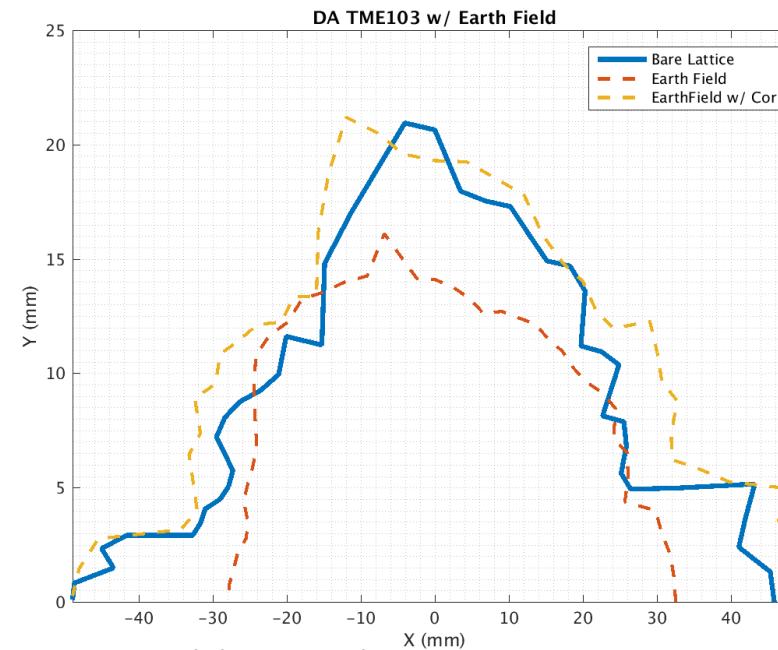
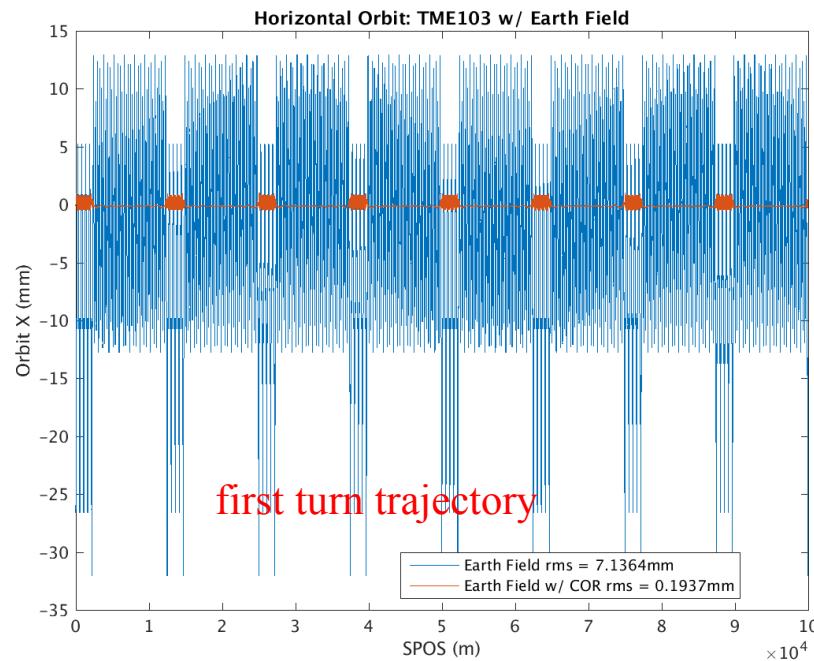
- Increase/decrease the strength of all the dipoles by the same amount.
- Evaluate the influence: working point, closed orbit, DA, energy acceptance
- Working point should not pass through the lower order resonance
- Small shrink for dynamic aperture
- Reproducibility requirement for dipoles: ~0.04%
- Stability requirement for power supply: ~0.01%
- Dipole field error tolerance slightly loser than 10GeV.

	original	+0.01%	-0.01%	+0.03%	-0.03%	+0.05%	-0.05%
nux	321.271	321.234	321.308	321.158	321.383	321.084	321.458
nuy	117.193	117.166	117.220	117.112	117.274	117.058	117.328
$\Delta x$ (um)	0	-26	26	-77	77	-130	130
DA (%)	100	95	100	97	95	97	95

# Effect of earthfield @20GeV

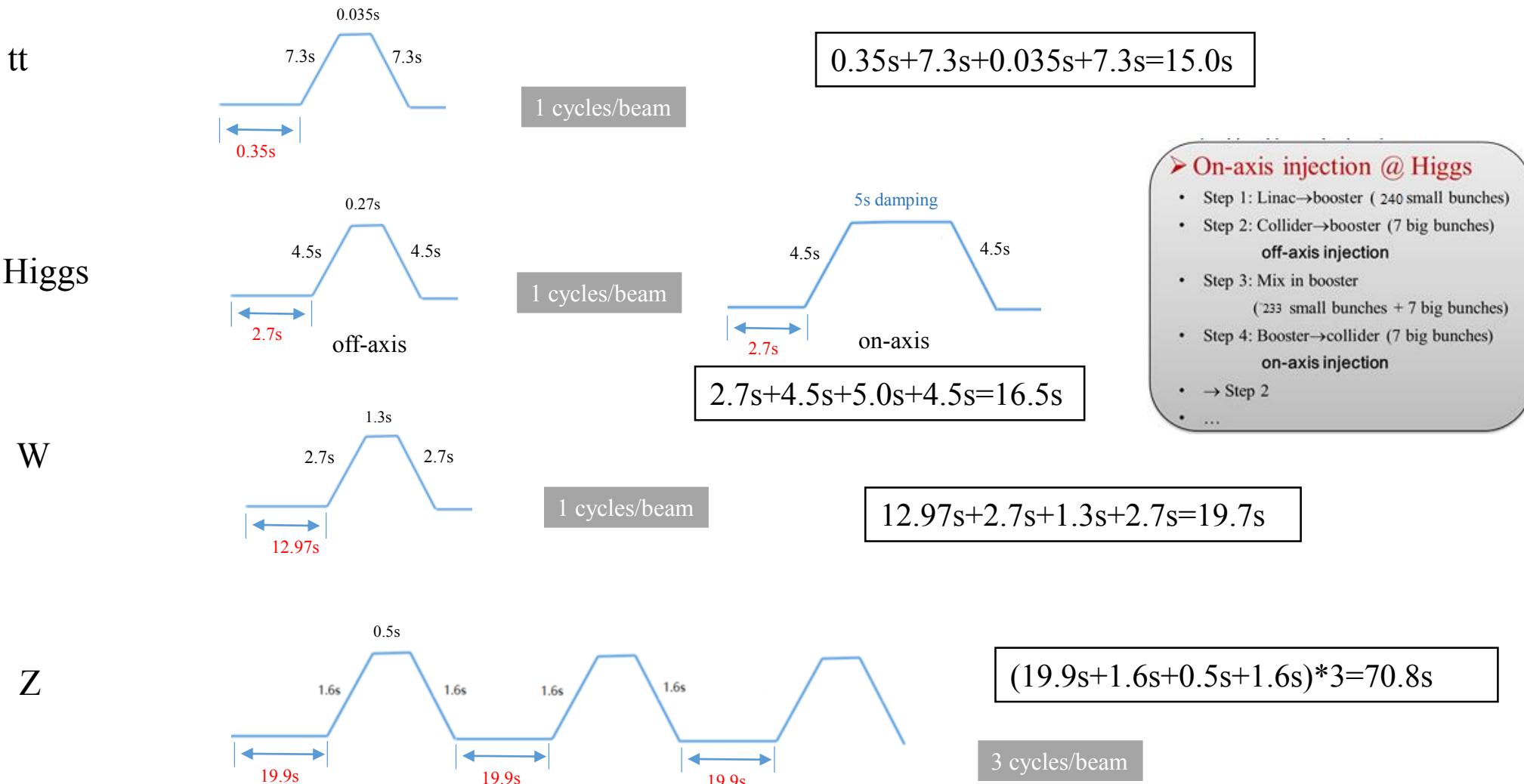
D. H. Ji, D. Wang

- ~20% vacuum pipe (drift) is exposed in earthfield directly.
- treat drifts as week dipole to simulate the effect of earthfield
- Assume earthfield: **0.6 gauss** (simple model: perpendicular component only )
- Working point can be corrected by weaken the dipoles systematically (-0.07%)
- Earthfield problem can be solved by global orbit correction.



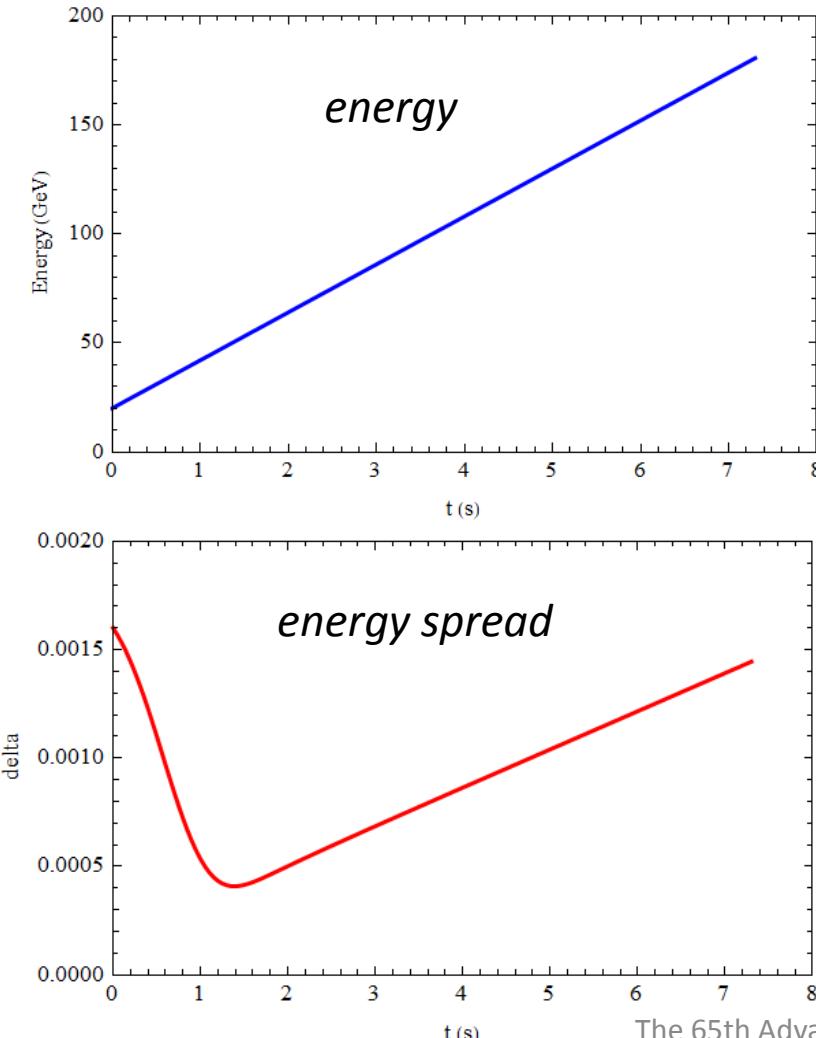
# Booster ramping scheme

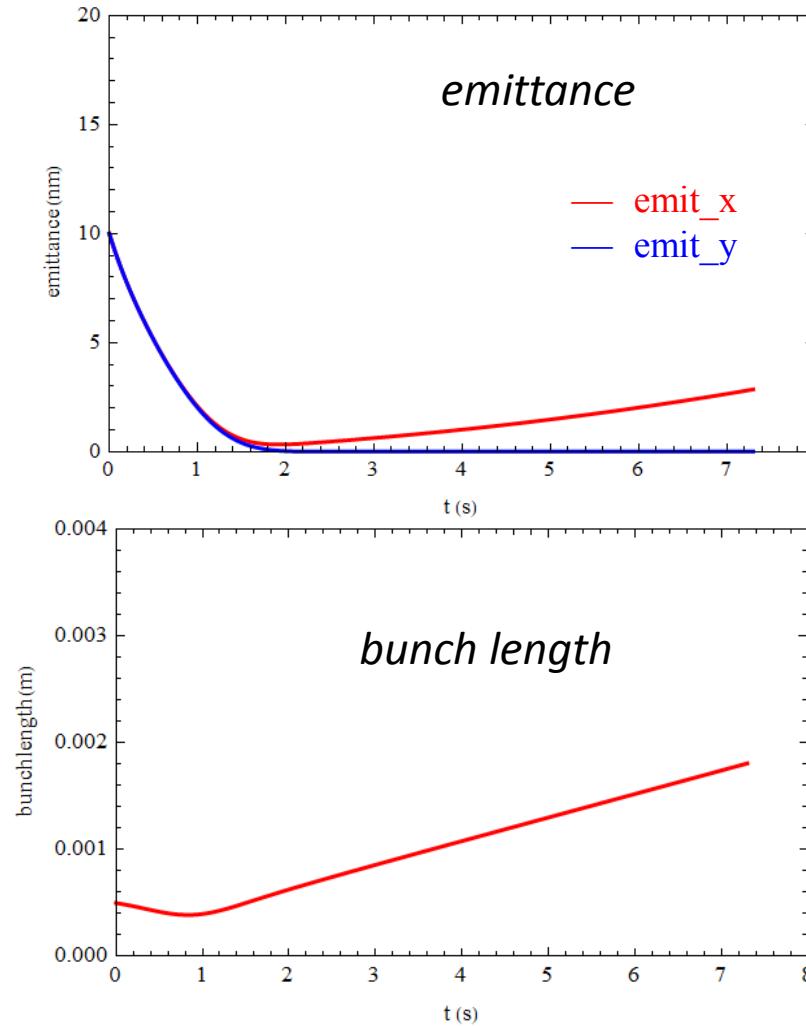
Dou Wang, Xiaohao Cui



# Beam parameter evolution

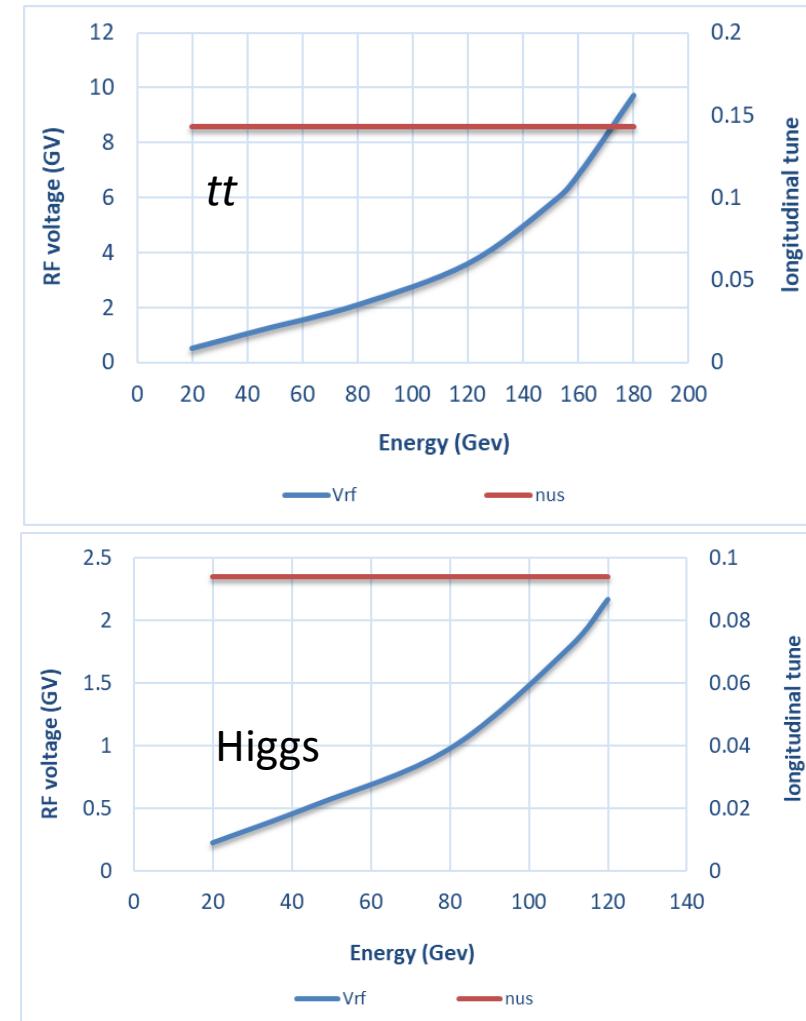
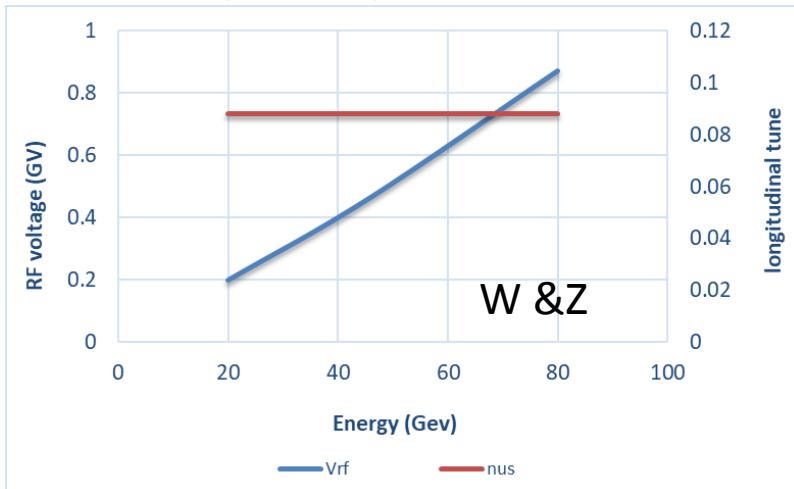
- Injection emittance: 10nm @20GeV
- Beam parameters reach balance after 60GeV.



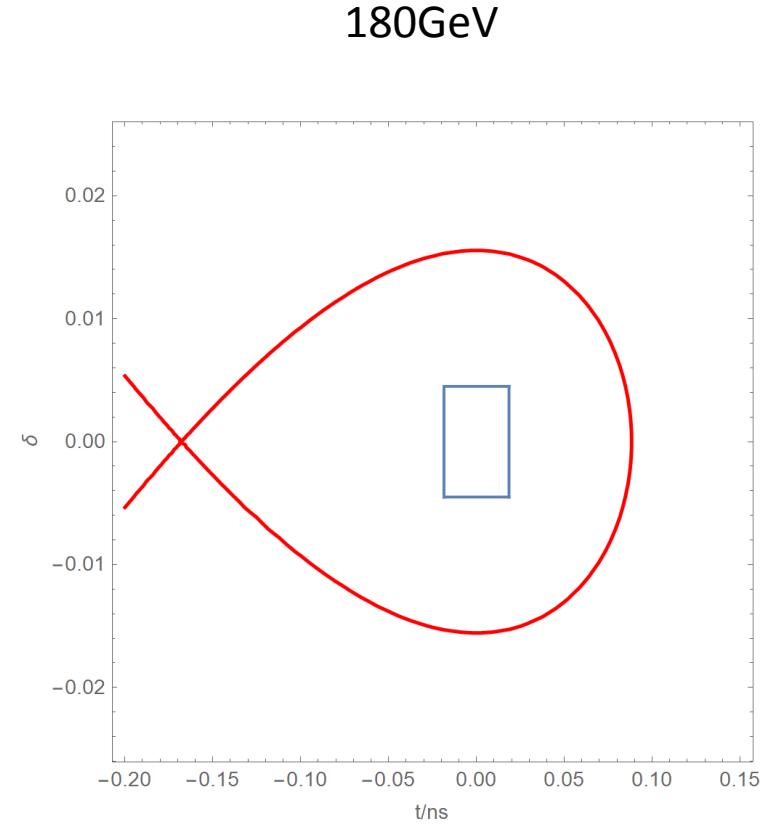
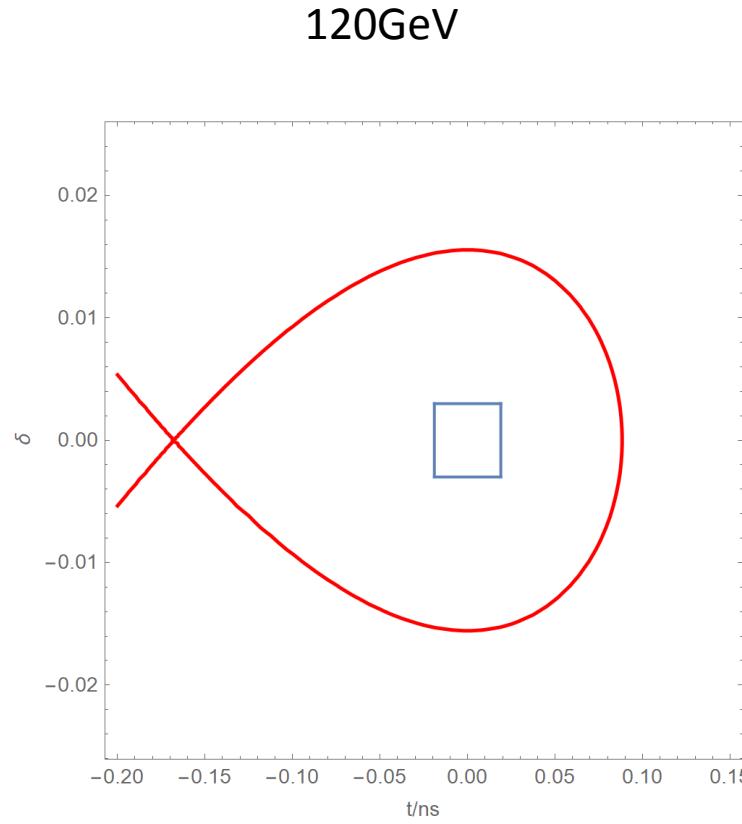
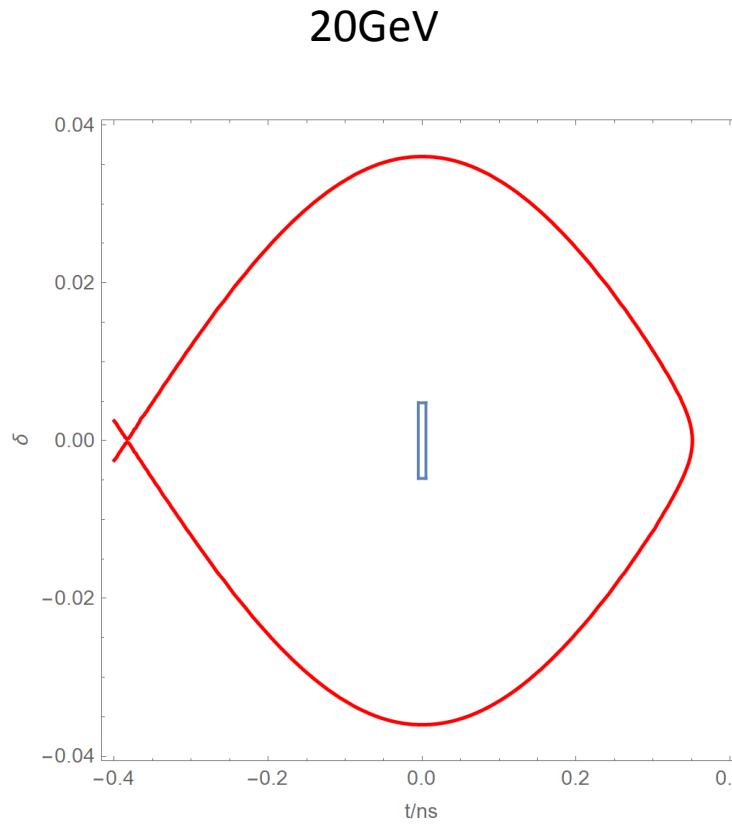
# RF ramping curve

- Different RF ramping curve for each energy mode (constant  $\nu_s$ )
  - $\nu_s$  for  $t\bar{t}$ : 0.14
  - $\nu_s$  for Higgs: 0.094
  - $\nu_s$  for W & Z: 0.088
- Max RF voltage @ $t\bar{t}$  determined by longitudinal quantum lifetime & DA.
  - $\eta_{RF} \sim 12 \times \delta$
  - VRF (180GeV)=9.8GV



# Longitudinal acceptance

- $\pm 3$  times of sigma for the longitudinal beam size



# Optics parameter comparison

D. H. Ji, W. Kang

Lattice	FODO 0 (CDR)	FODO 1	TME (combine magnets)
Emittance X (nm) @120GeV	3.57	1.29	1.26
Momentum compaction ( $\times 10^{-5}$ )	2.44	1.18	1.12
Tunes	[263.201/261.219]	[353.180/353.280]	[321.271/117.193]
Quad amount	2110	2816	3458
Quad Strength (K1L rms)	0.0383	0.0407	0.0259
Sext amount	512	896	96
Sexts Strength (K2L rms)	0.179	0.4091	0.0492
H Corrector	1053	1408	1218
V Corrector	1054	1408	2240
BPM	2108	2816	3458
Power consumption of magnets@120GeV (MW) (max/average)	15/6		12.1/4.8

➤ Magnets' cost of TME is lower than FODO 1

- Less independent sextupole for TME
- Quadrupole strength of TME is lower

➤ TME is less sensitive to error effects

- Weaker quad/sex strength

➤ TME has lower magnets' power consumption

# Booster power consumption @Higgs

- The technical systems with changes are considered.
- The power consumption of TDR is lower than CDR with much lower emittance.

Technical system	CDR [MW]		TDR [MW]		Budget increment [MW]	
	max	average	max	average	max	average
Magnet system	15	6	12.1	4.8	-2.9	-1.2
Power supply	10.04	4.02	6.62	2.65	-3.42	-1.37
RF system						
RF power source	3.95	0.15	4.45	1.44	0.5	1.29
Beam Instrumentation	0.6	0.6	0.72	0.72	0.12	0.12
...						
total		20.97		19.81	-5.7	-1.16

# Booster power consumption @Z

- The technical systems with changes are considered.
- The power consumption of TDR almost same as CDR with much lower emittance.

Technical system	CDR [MW]		TDR [MW]		Budget increment [MW]	
	max	average	max	average	max	average
Magnet system	2.14	1.28	1.72	0.69	-0.42	-0.59
Power supply	2.48	0.99	1.88	0.75	-0.6	-0.24
RF system						
RF power source	0.5	0.04	1.13	0.084	0.63	0.044
Beam Instrumentation	0.6	0.6	0.72	0.72	0.12	0.12
...						
total		9.7		9.034	-0.27	-0.666

# Booster TDR parameters

- Injection energy:  $10\text{GeV} \rightarrow 20\text{GeV}$
- Max energy:  $120\text{GeV} \rightarrow 180\text{GeV}$
- Lower emittance — new lattice ([TME](#))

Injection		<i>t</i>	<i>H</i>	<i>W</i>	<i>Z</i>
Beam energy	GeV		20		
Bunch number		35	268	1297	3978
Threshold of single bunch current	$\mu\text{A}$	5.79	4.20		3.92
Threshold of beam current (limited by coupled bunch instability)	mA			27	
Bunch charge	nC	1.1	0.78	0.81	0.87
Single bunch current	$\mu\text{A}$	3.4	2.3	2.4	2.65
Beam current	mA	0.12	0.62	3.1	10.5
Growth time (coupled bunch instability)	ms	1690	358	67	19.4
Energy spread	%		0.016		
Synchrotron radiation loss/turn	MeV		1.3		
Momentum compaction factor	$10^{-5}$		1.12		
Emittance	nm		0.035		
Natural chromaticity	H/V		-372/-269		
RF voltage	MV	531.0	230.2	200.0	
Betatron tune $v_x/v_y$			321.23/117.18		
Longitudinal tune		0.14	0.0943	0.0879	
RF energy acceptance	%	5.9	3.7	3.6	
Damping time	s		10.4		
Bunch length of linac beam	mm		0.5		
Energy spread of linac beam	%		0.16		
Emittance of linac beam	nm		10		

Extraction		<i>t</i>	<i>H</i>	<i>W</i>	<i>Z</i>	
		Off axis injection	Off axis injection	On axis injection	Off axis injection	Off axis injection
Beam energy	GeV	180		120	80	45.5
Bunch number		35	268	261+7	1297	3978
Maximum bunch charge	nC	0.99	0.7	20.3	0.73	0.8
Maximum single bunch current	$\mu\text{A}$	3.0	2.1	61.2	2.2	2.4
Threshold of single bunch current	$\mu\text{A}$	91.5		70	22.16	9.57
Threshold of beam current (limited by RF system)	mA	0.3		1	4	16
Beam current	mA	0.11	0.56	0.98	2.85	9.5
Growth time (coupled bunch instability)	ms	16611	2359	1215	297.8	49.5
Bunches per pulse of Linac		1	1	1	2	
Time for ramping up	s	7.3	4.5	2.7	1.6	
Injection duration for top-up (Both beams)	s	30.0	23.3	32.8	39.4	141.6
Injection interval for top-up	s	65	38	155	153.5	
Current decay during injection interval				3%		
Energy spread	%	0.15	0.099	0.066	0.037	
Synchrotron radiation loss/turn	GeV	8.45	1.69	0.33	0.034	
Momentum compaction factor	$10^{-5}$			1.12		
Emittance	nm	2.83	1.26	0.56	0.19	
Natural chromaticity	H/V		-372/-269			
Betatron tune $v_x/v_y$			321.27/117.19			
RF voltage	GV	9.7	2.17	0.87	0.46	
Longitudinal tune		0.14	0.0943	0.0879	0.0879	
RF energy acceptance	%	1.78	1.59	2.6	3.4	
Damping time	ms	14.2	47.6	160.8	879	
Natural bunch length	mm	1.8	1.85	1.3	0.75	
Full injection from empty ring	h	0.1	0.14	0.16	0.27	1.8

\*Diameter of beam pipe is 55mm for re-injection with high single bunch current @120GeV.

# Summary

- Booster energy range is enlarged in TDR. ( $10\text{GeV}/120\text{GeV} \rightarrow 20\text{GeV}/180\text{GeV}$ )
- Update booster design with smaller emittance in TDR— support for CEPC high lum. scheme
  - TME structure with combined magnets (B+S)
  - DA with error effects fulfill the requirements
  - Booster parameters update — consistent with CEPC TDR parameters at 4 energy
- 30GeV injection is under consideration for the cost saving.
  - The non-oriented silicon laminations for the iron dominated dipole magnet can be used at 30GeV.