

Ultrashort Pulse Generation and Superradiance in FELs

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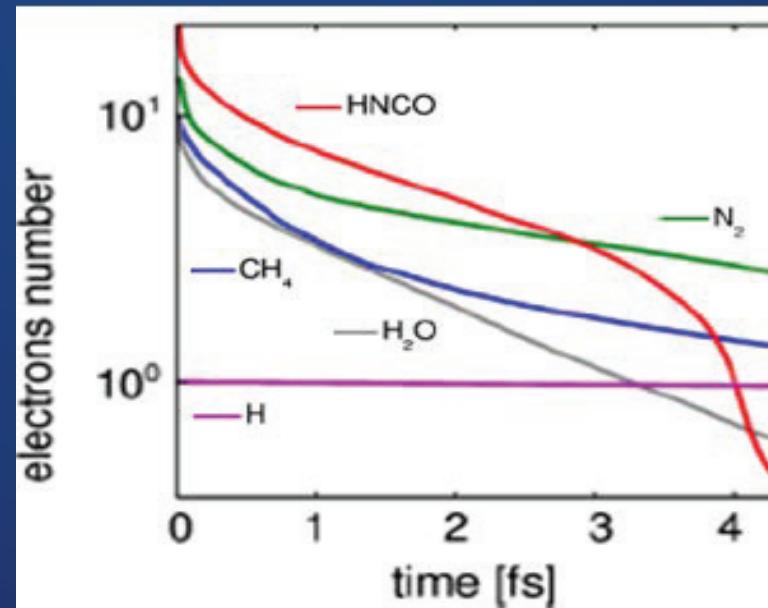
Outline

- Peak power and pulse duration limits in FEL amplifiers
- Methods to achieve single spike at saturation
- Saturation effects
 - Pulse shortening & power increase
 - Pulse splitting and tail formation after saturation
- Tail structure
 - FEL pulse splitting into head (L_+) and tail (L_-) modes after saturation
- Tail suppression

Motivation: Single-Shot Isolated-Molecule Imaging

- Key issues:
 - Time scale (sub-fs): Acquiring single shot images before radiation damage/Coulomb explosion of the sample takes place
 - Spatial resolution: Resolving the structure of proteins that cannot be crystallized in single-molecule level
 - High Intensity: $1.3 \cdot 10^{11}$ photon/pulse at $P=150$ GW, $\lambda=0.4$ nm with $\sigma_{t-FWHM}=400$ as
- Such conditions can be met by XFEL with peak power of multi-GW and sub-femtosecond temporal duration

Number of “bounded” electrons versus time of molecules illuminated by XFEL radiation with power $P=150$ GW and $\lambda = 0.4$ nm

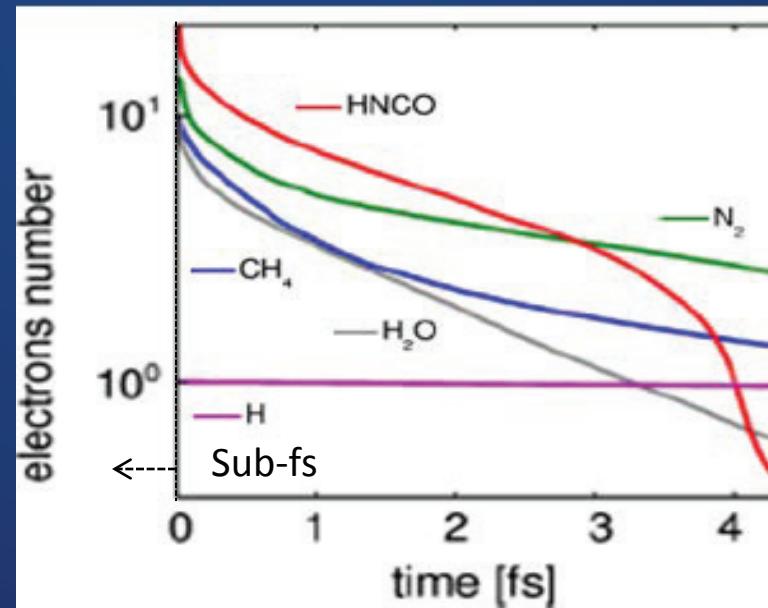


A. Fratalocchi and G. Ruocco
PRL 106, 105504 (2011)

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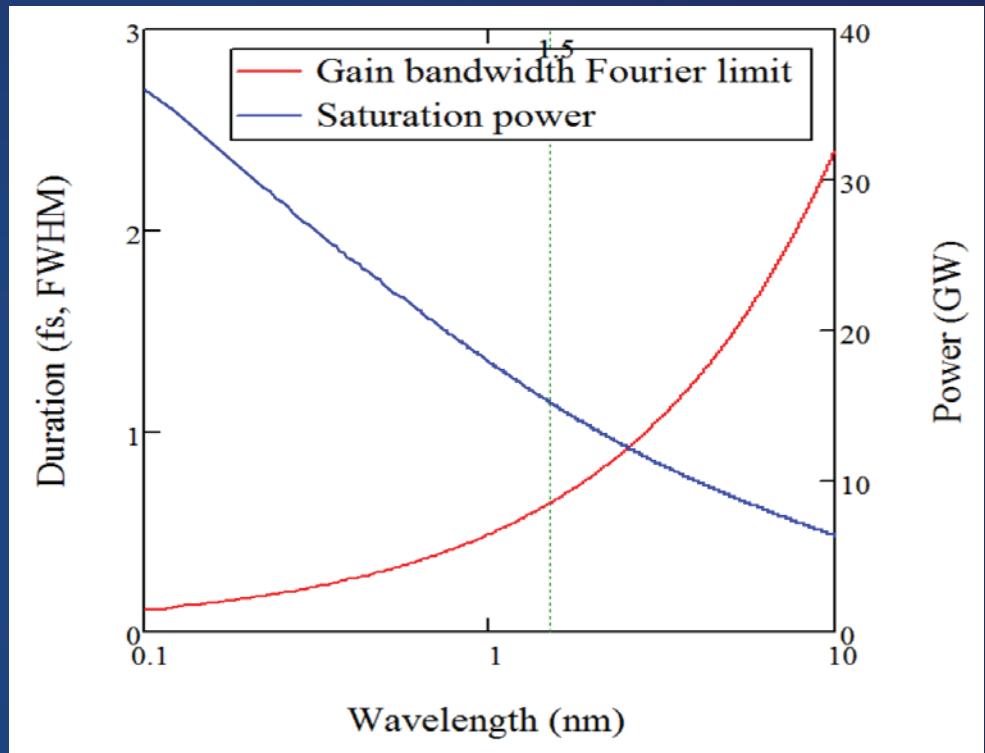
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Single spike:Peak Power and Pulse Duration Limits at FEL Saturation (no taper)

- Limit by saturation:
 - Power 20 to 40 GW at $\lambda = 0.1$ nm
- Limit by gain bandwidth
 - Pulse duration down to 100 fs (FWHM)
- In order to meet the sub-fs –multi-GW (*tens of*) of peak power we get close to the gain bandwidth limit and to saturation
- It is possible to get to this condition



- Period 3.3 cm
- $K = 3.5$
- $\epsilon_n = 0.5$ mm-mrad
- Reasonable assumptions of I_{pk} and β
- L. H. Yu, S. Krinsky, Phys. Rev. A. 35 3406-3422 (1987)
- M. Xie LINAC 1995

Methods to Achieve Single Spike at Saturation

- A few ways to trigger the formation of a single spike :
 - Short electron bunch single spike
J. Rosenzweig et al, NIMA 593(2008)
 - Chirp + Taper
200 as (FWHM) and 100 GW in $\lambda \sim 1\text{\AA}$ (sim) *E. Saldin et al, PRST-AB 9, 050702 (2006)*
 E_{out} increases >10 times in single spike SASE at $\lambda \sim 540\text{nm}$ (exp) *L. Giannessi et al, PRL 106, 144801 (2011)*
 - Slotted foil
Sub-fs 10GW x-ray pulse *P. Emma et al. PRL 92, 074801 (2004)*
 - Multi-foil + Electron Delay
500as (FWHM) and 1TW at $\lambda \sim 1\text{\AA}$ (sim) *E. Prat and S Reiche PRL 114, 244801 (2015)*
 - Fresh bunch self-seeding
50 GW, 9 fs at 5.5keV *C. Emma et al, APL 110, 154101 (2017)*
 - Chirp + Taper + Fresh bunch self-seeding
0.5TW and 260as (FWHM) at $\lambda = 1.5\text{nm}$ *S. Huang et al, PRAB 19, 080702 (2016)*
- When the short pulse reaches saturation -> superradiance

Saturation of the single spike

- When the peak power exceeds ρP_e



- Superradiance*
 - Modification of the pulse properties due to the electron longitudinal synchrotron oscillations.
 - Scaling relations**: $P_L \propto z^2$, $E_L \propto z^{3/2}$, $\sigma_t \propto z^{-1/2}$

*R. Bonifacio, B. W. J. Mc Neil, P. Pierini, PRA 40, 4467 (1989)

R. Bonifacio, L. De Salvo Souza, P. Pierini, N. Piovella, NIM A296, 358 (1990)

** see: L. Giannessi, P. Musumeci, S. Spampinati, JAP 98, 043110 (2005)

Experiments: Watanabe et al. PRL 98, 034802 (2007)

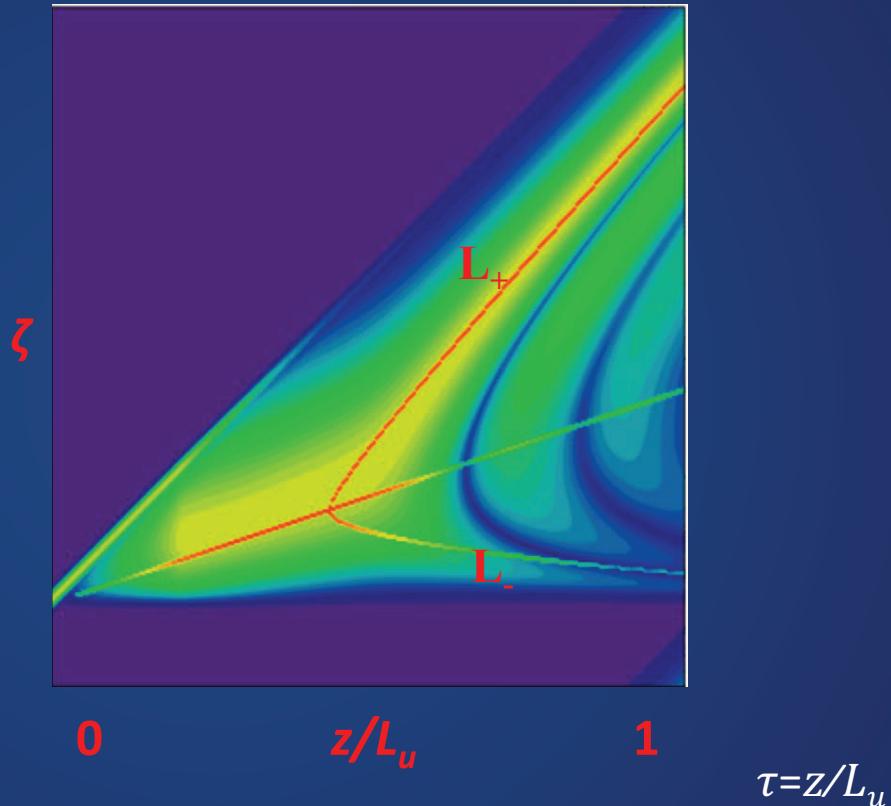
SPARC, Frascati: PRL 106, 144801 (2011) – PRL 108, 164801 (2012) – PRL 110, 044801 (2013)

MOVIE 1 AND MOVIE 2

What happens when single spike reaches saturation

Pulse Splitting and Tail Formation

- Local saturation condition is met
- P_{sr} exceeding saturation and increasing as $\propto z^2$
- σ_t shortening as $\propto z^{-1/2}$
- It is desired to get into the superradiance regime (indicated by L_+) with higher power and shorter pulse length
- Once getting into the saturation, the tail is formed
- The **pulse length is determined by the structure between L_+ and L_-** , both from the same origin of pulse splitting.

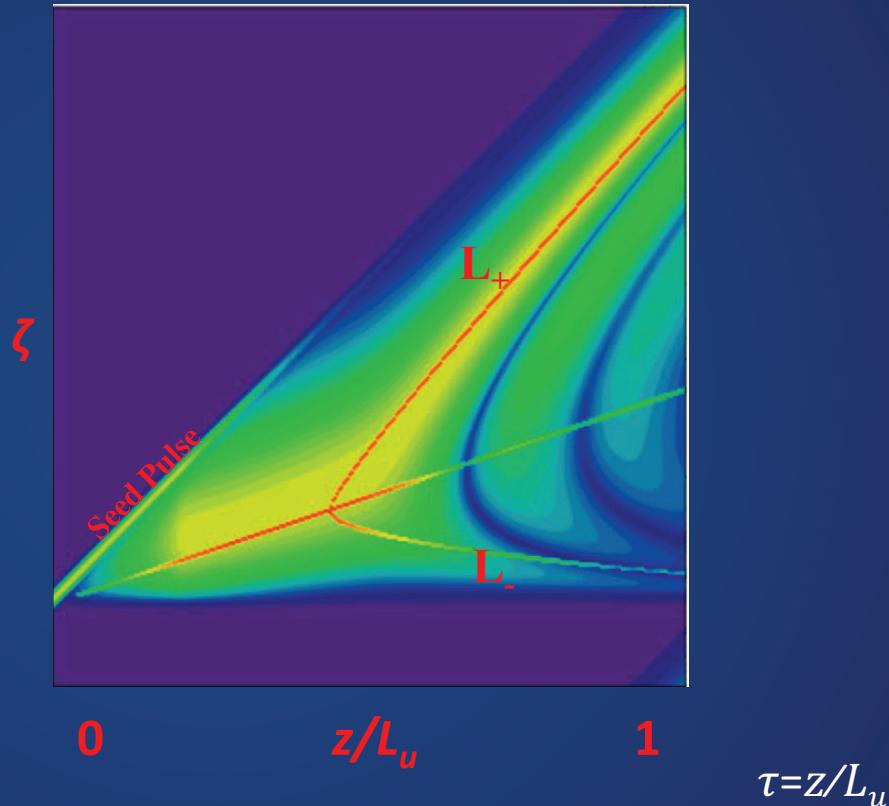


Longitudinal profile of the radiation field amplitude along the e- beam coordinate ζ as it propagates along the undulator with coordinate τ

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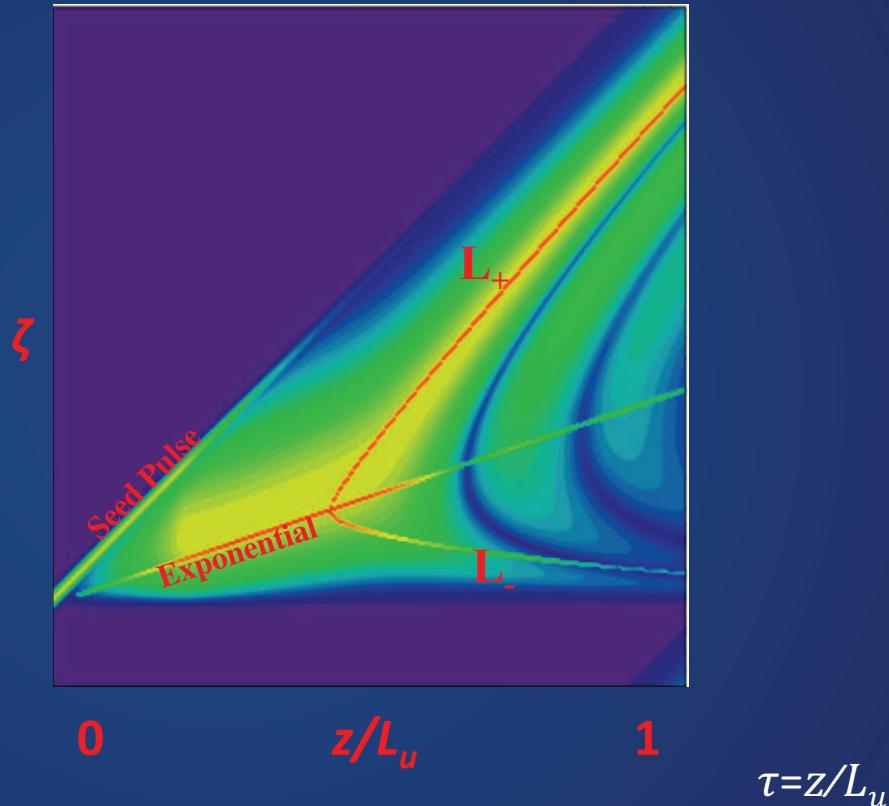


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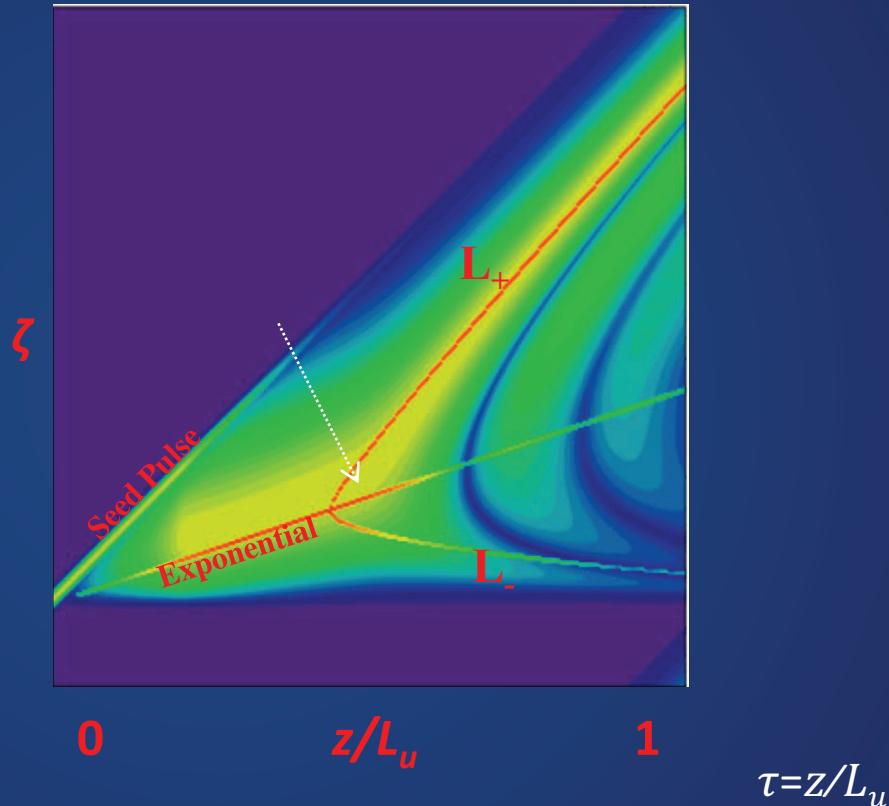


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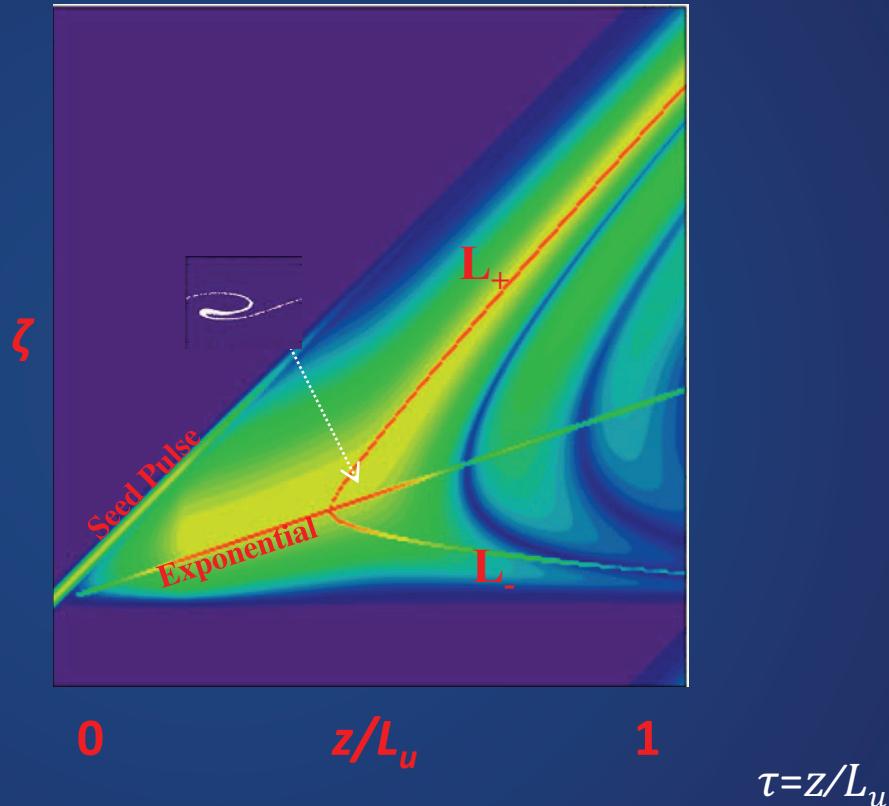


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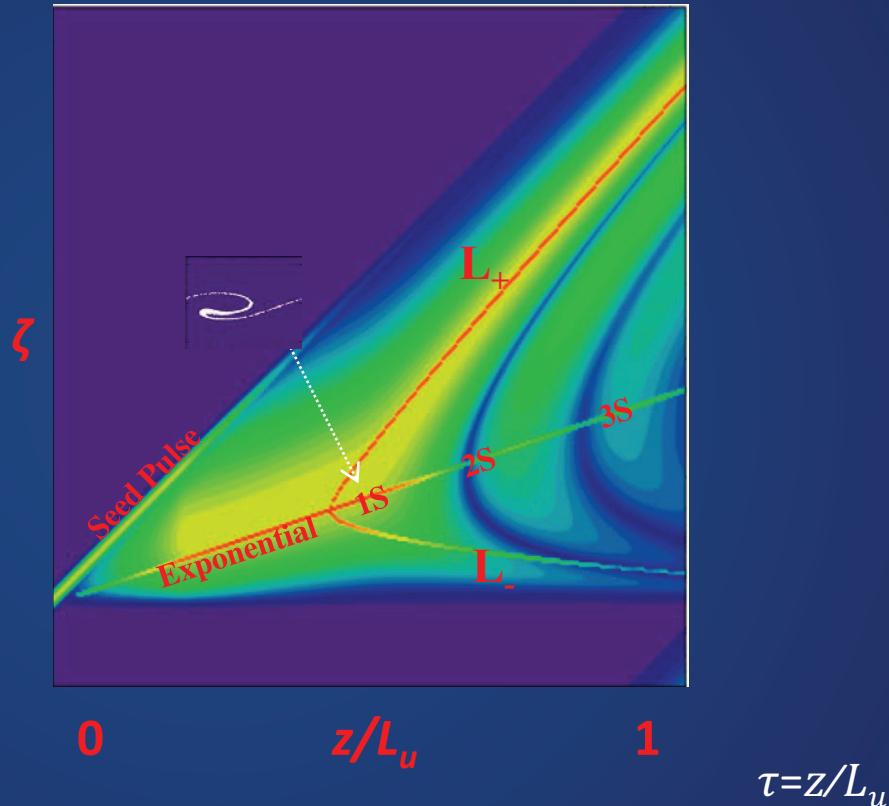


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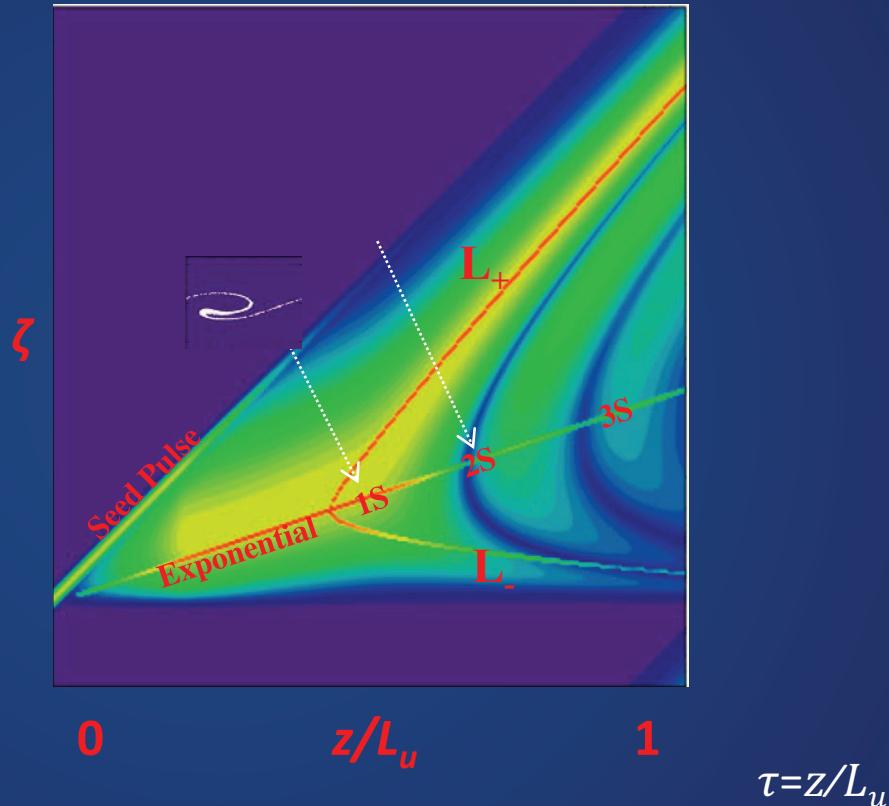


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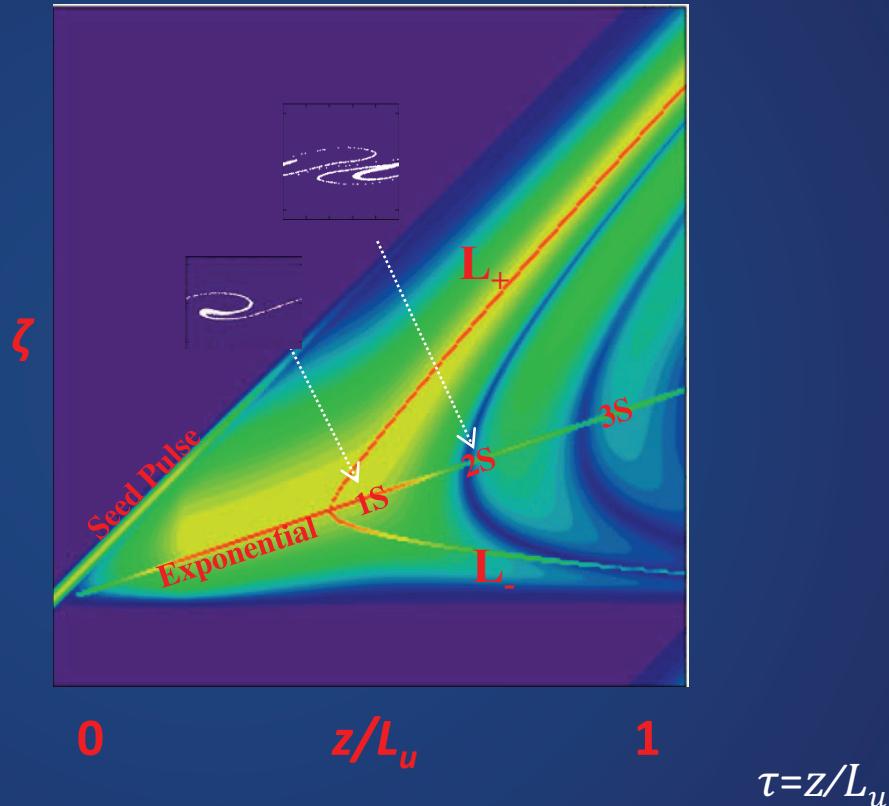


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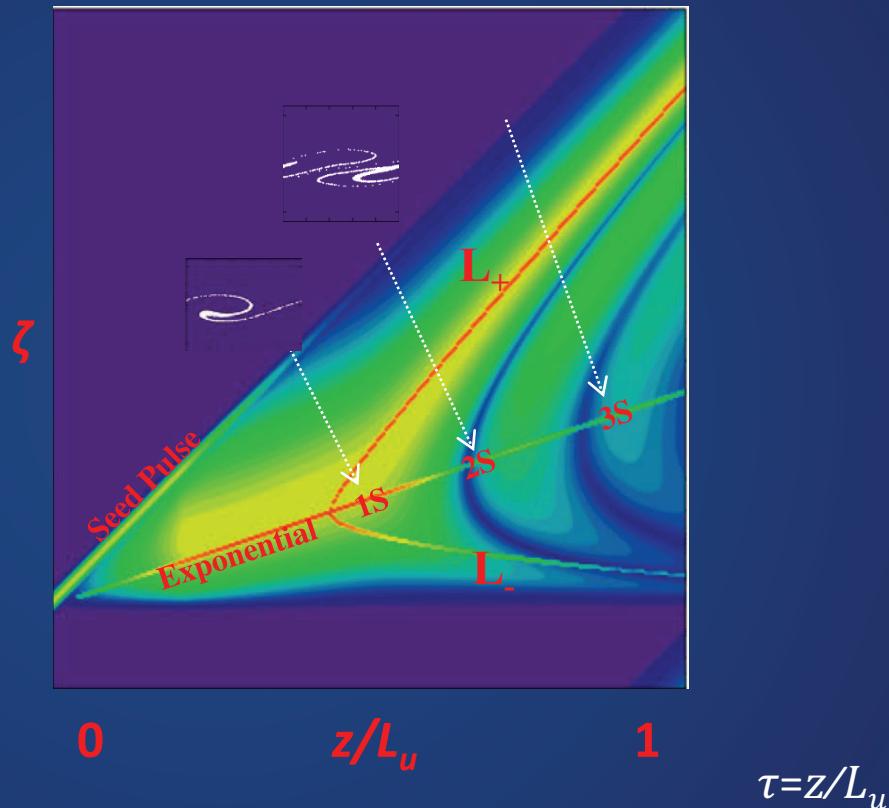


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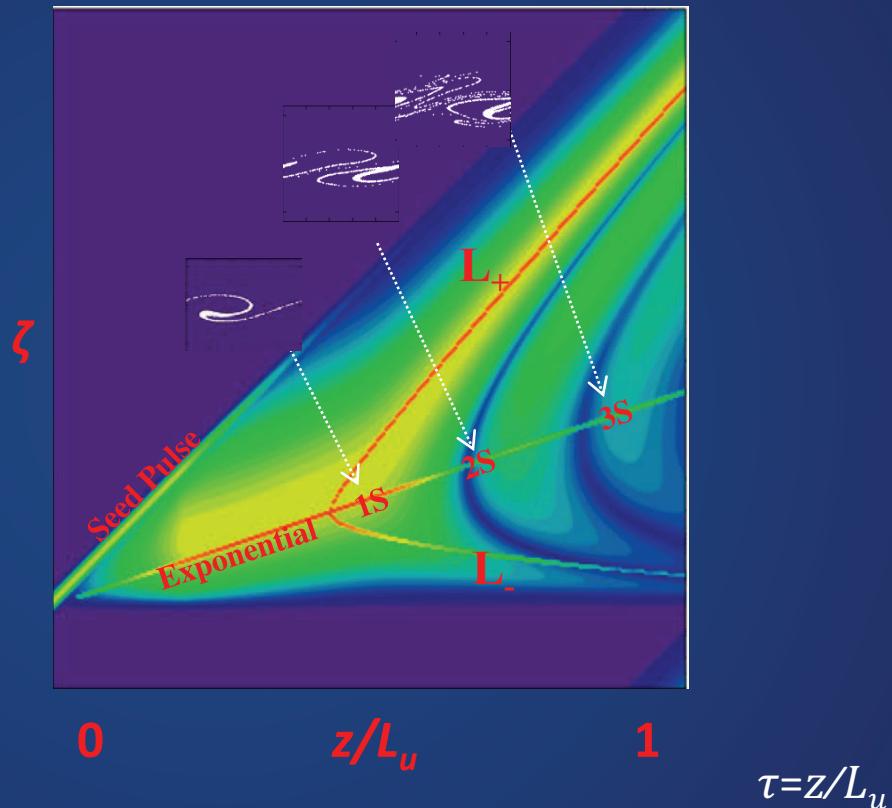


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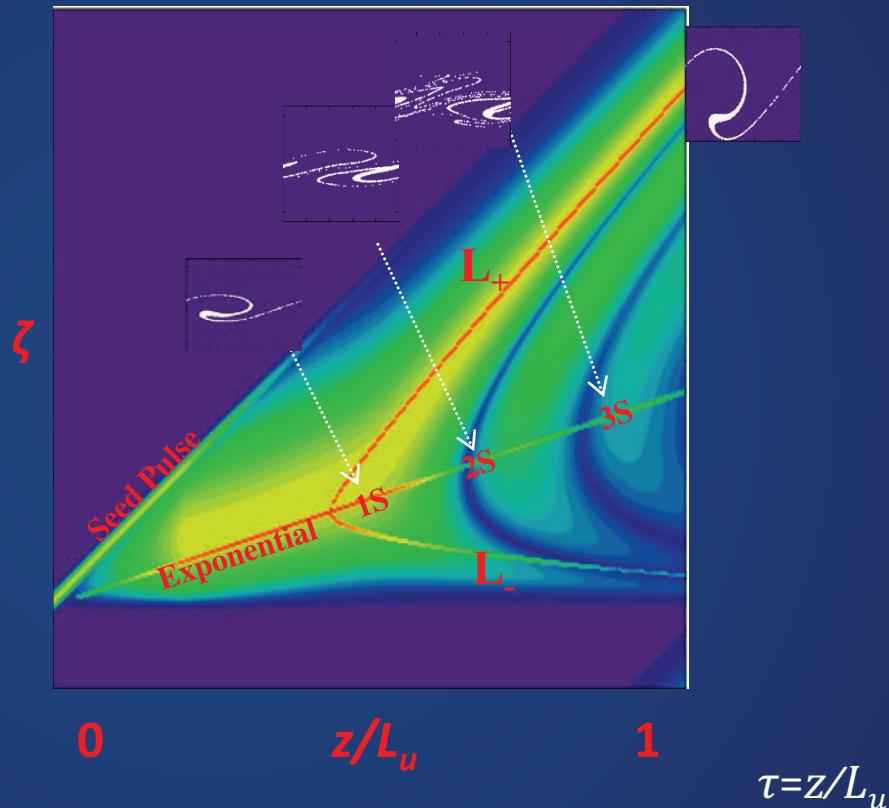


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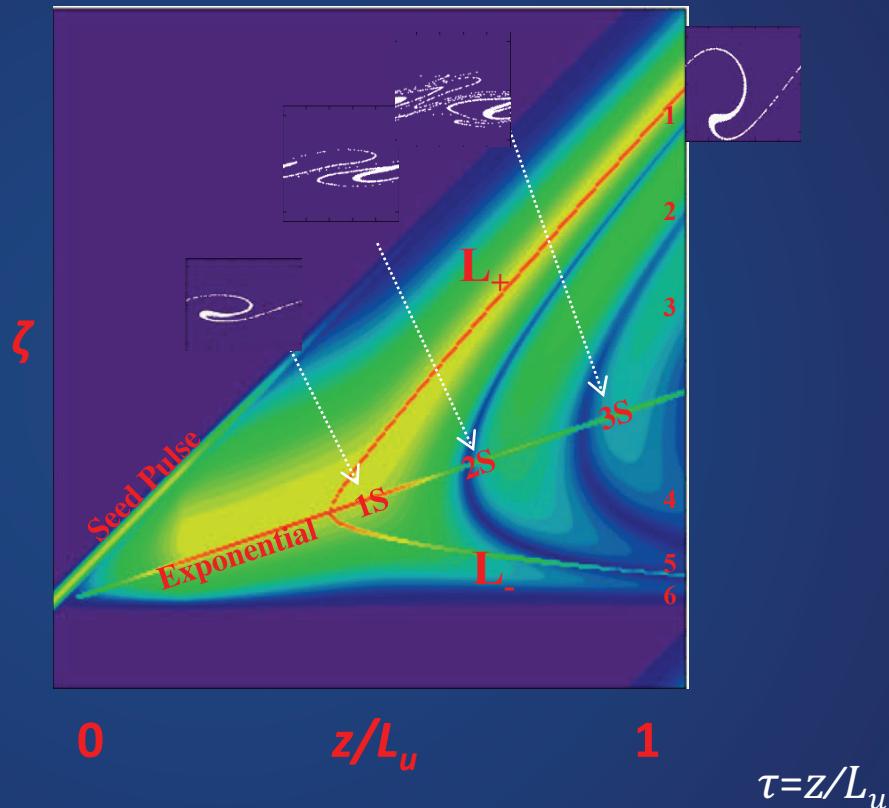


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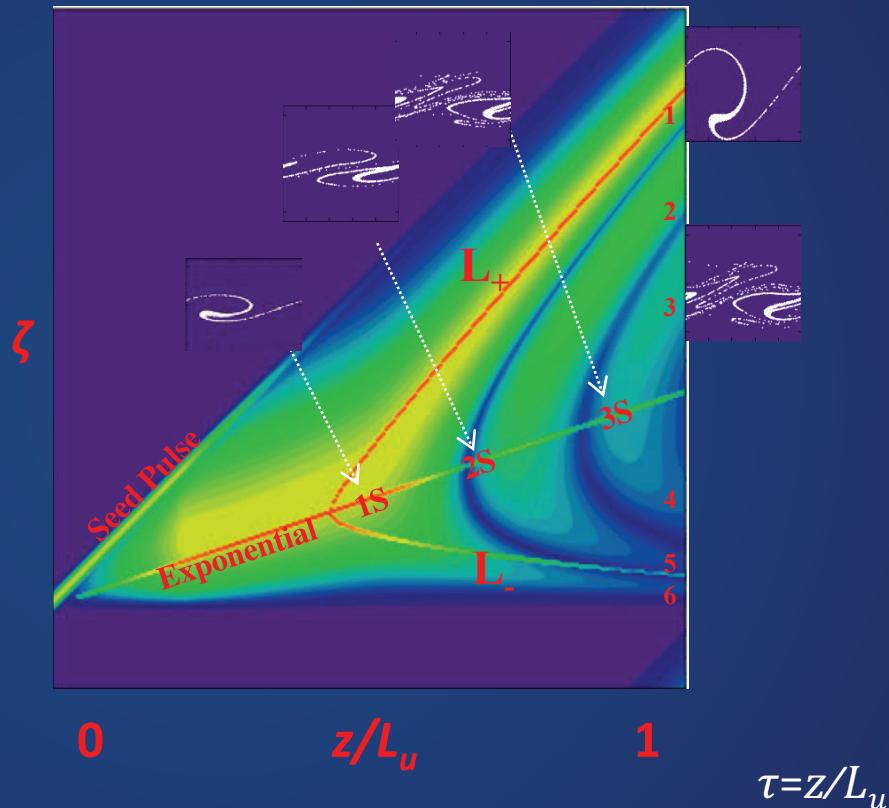


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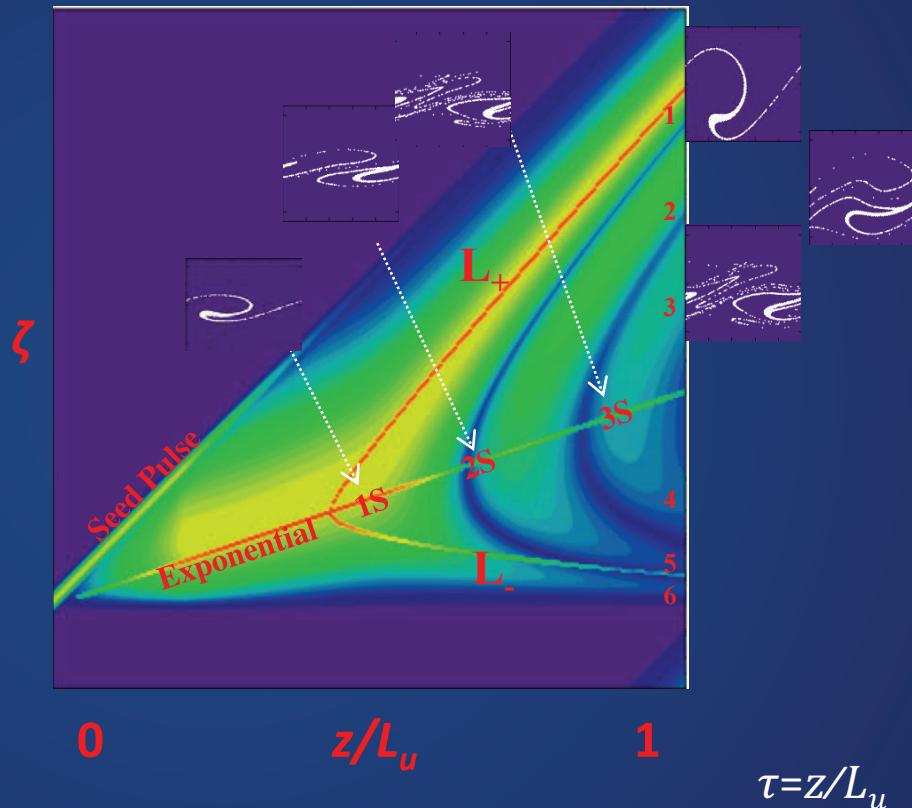


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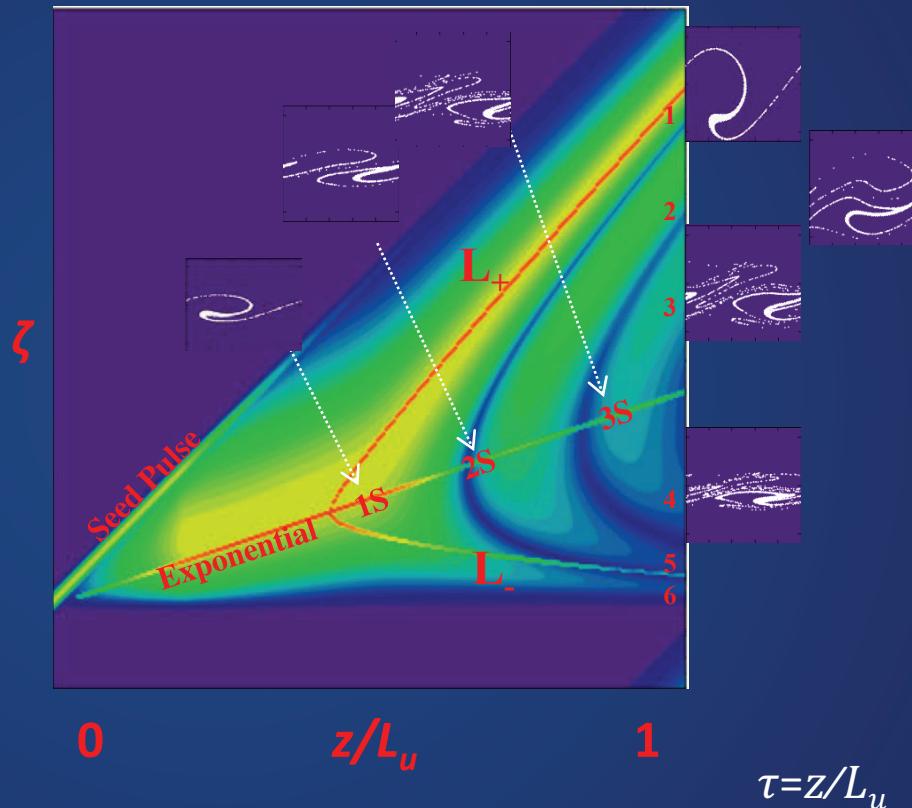


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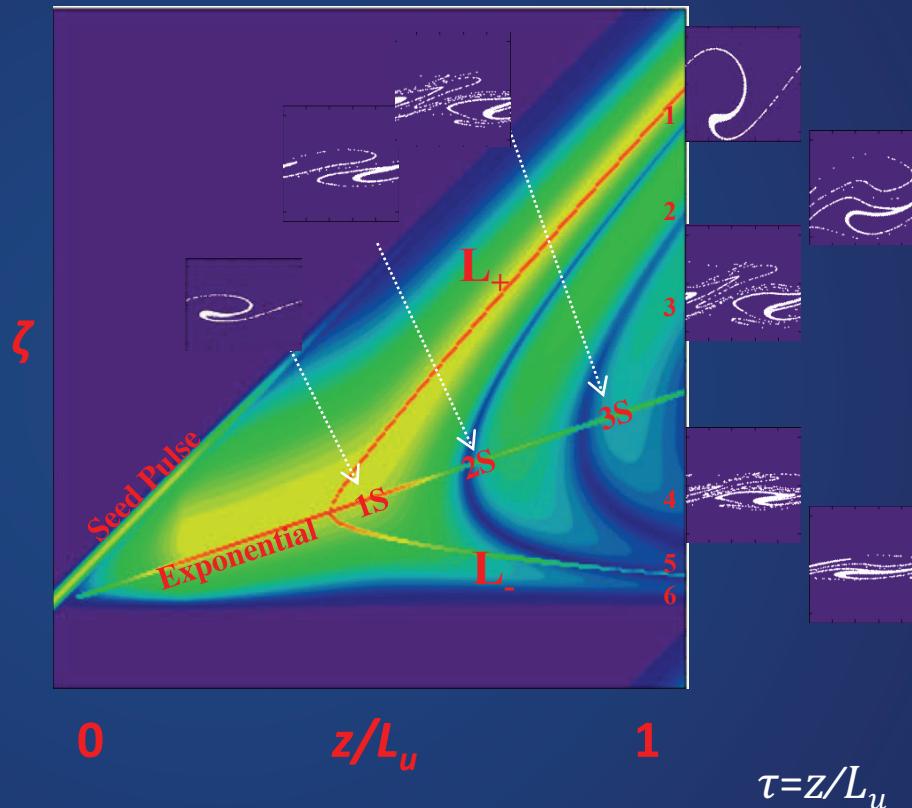


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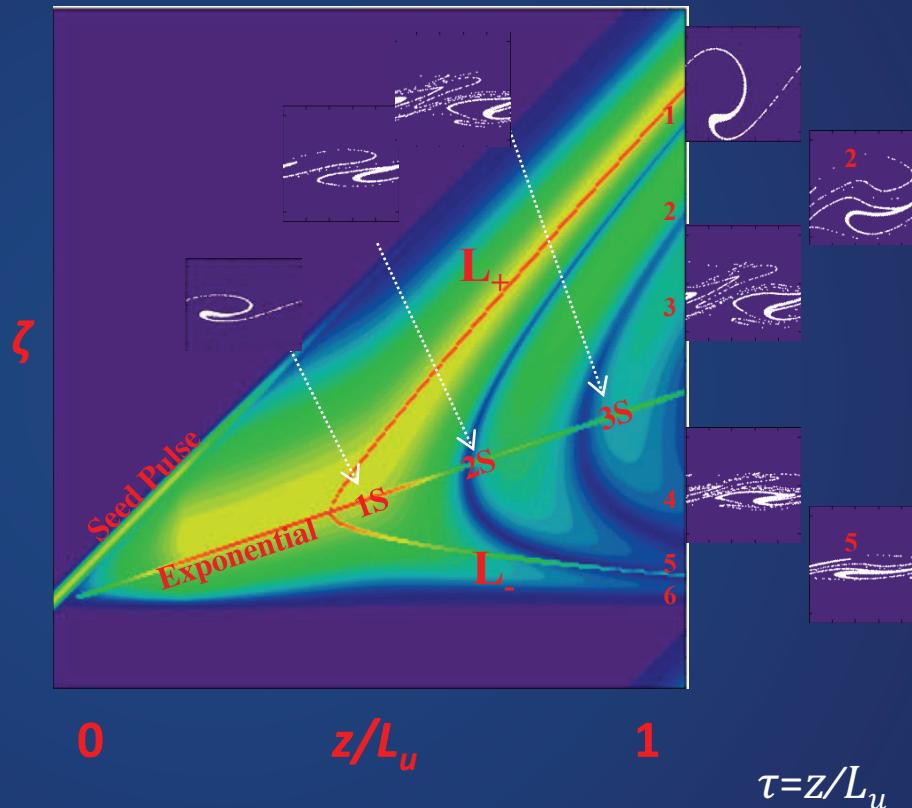


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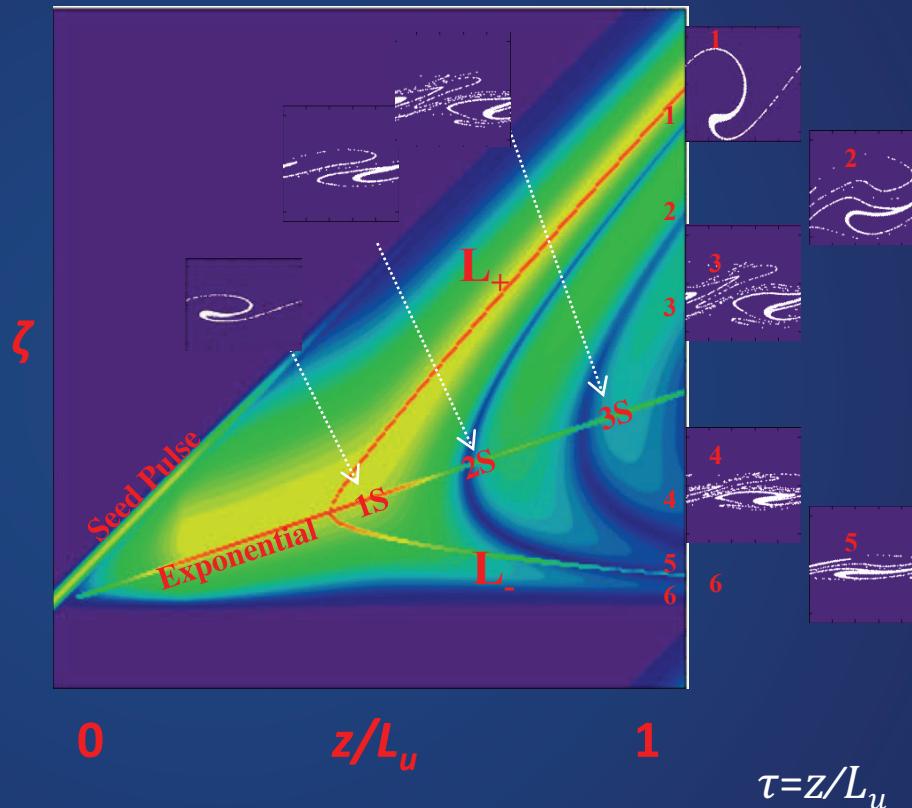


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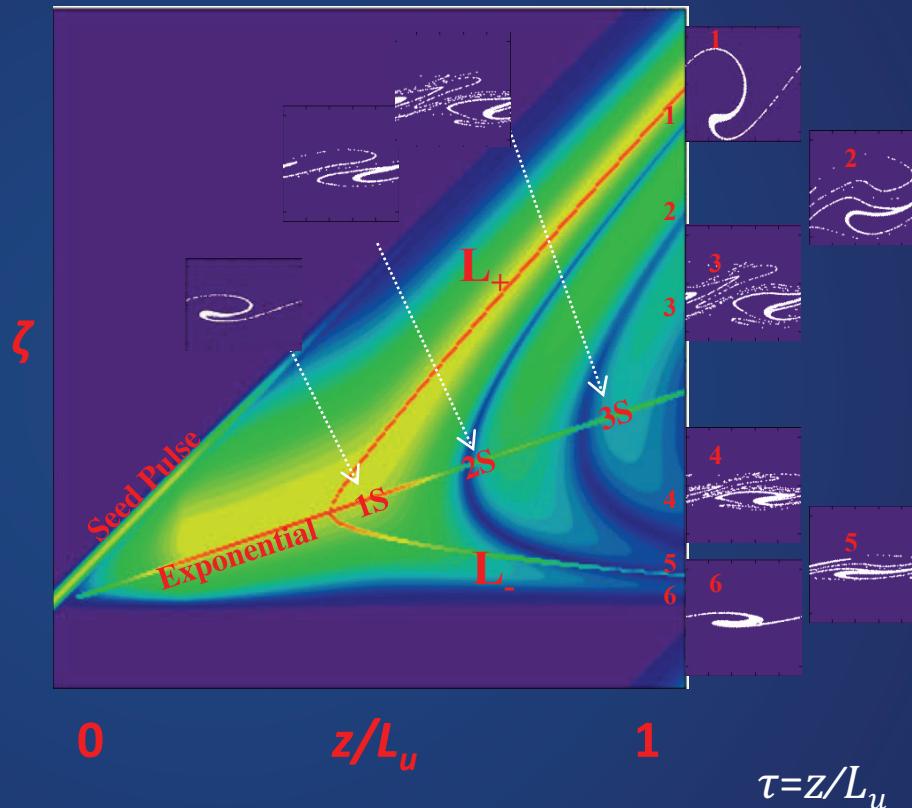


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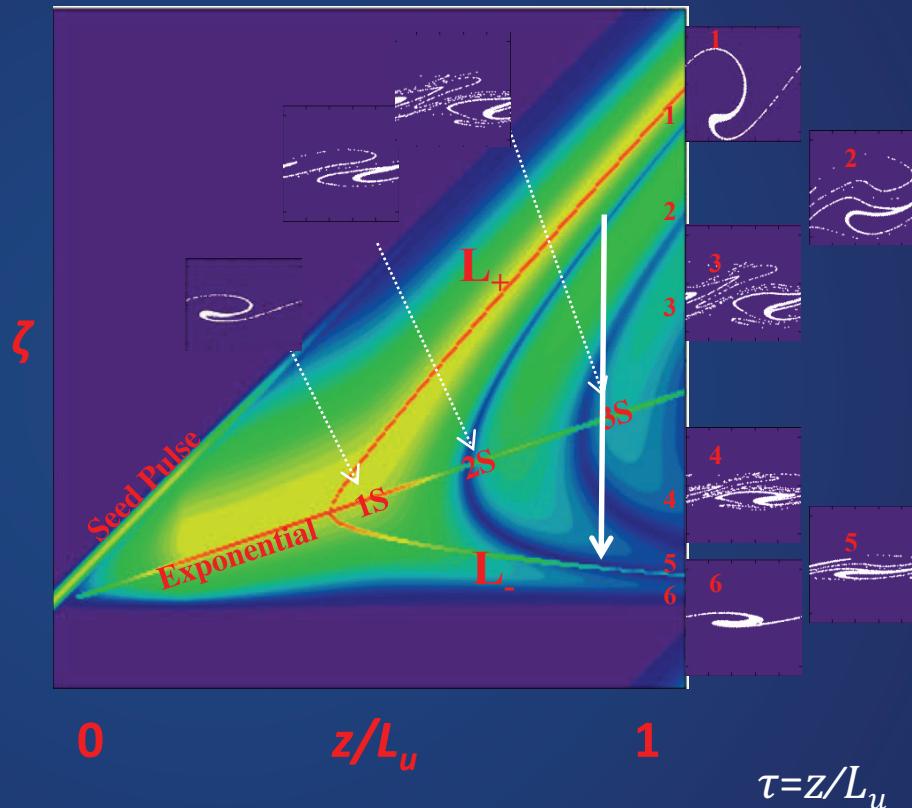


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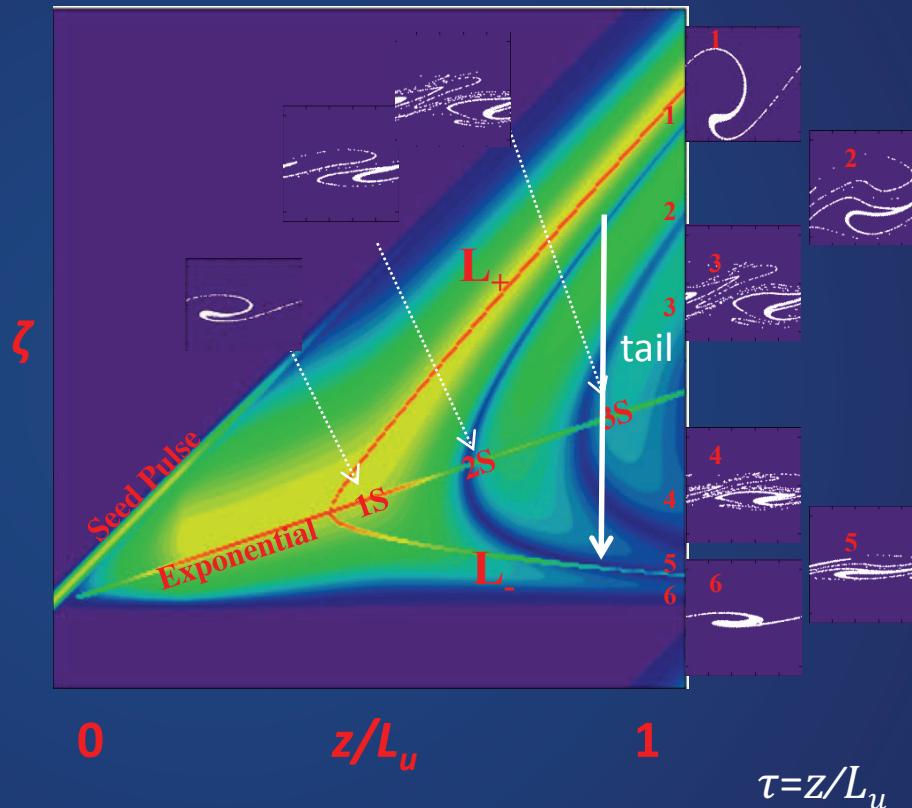


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Single electron FEL

Notes

- Pulse duration is determined by the slippage distance over $\frac{1}{2}$ synchrotron period, i.e. $\frac{1}{2}$ the Fourier limit of a pulse with bandwidth
- Secondary π peaks induced by residual bunching
- Peak amplitudes decaying with beam energy spread
- Phase shift of π between peaks
- Secondary peak in the tail, the trailing edge is still reaching saturation
- Peak propagation speed ... see next

Peaks position

Condition for saturation $P(z) = P_0 \exp \left\{ -\frac{[\zeta - vz]}{2\sigma_\zeta^2} + \frac{z}{L_g} \right\} = P_s \simeq 1.6 \rho_{fel} P_E$

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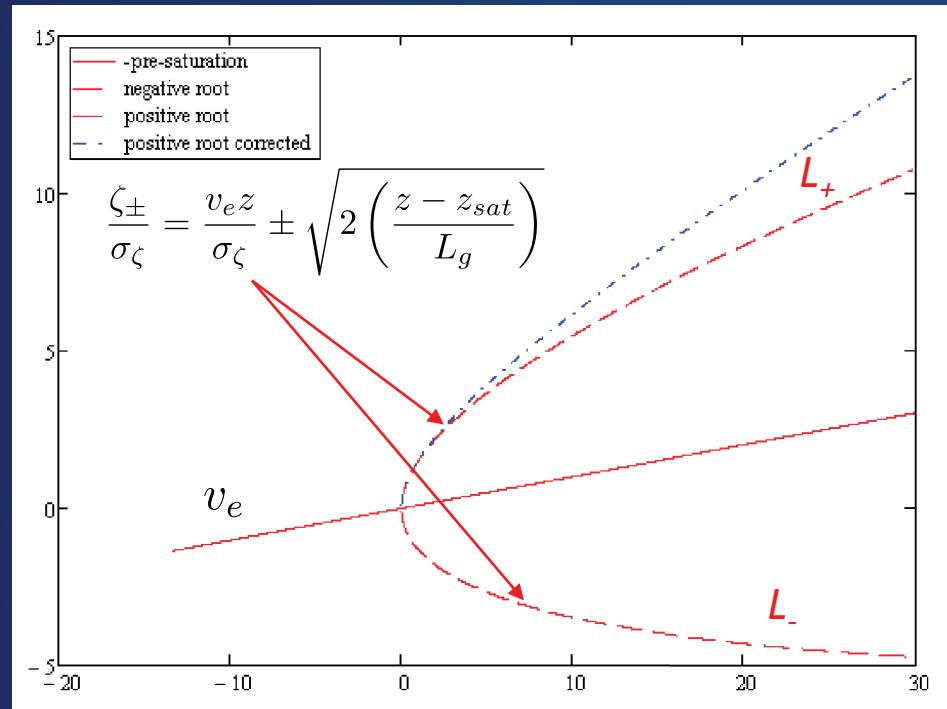
Peak velocity

$$v = \begin{cases} v_e = \lambda_0 / 3\lambda_u \\ v_s = \lambda_0 / \lambda_u \end{cases}$$

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Two roots are plotted as solid lines indicated by L_+ and L_-



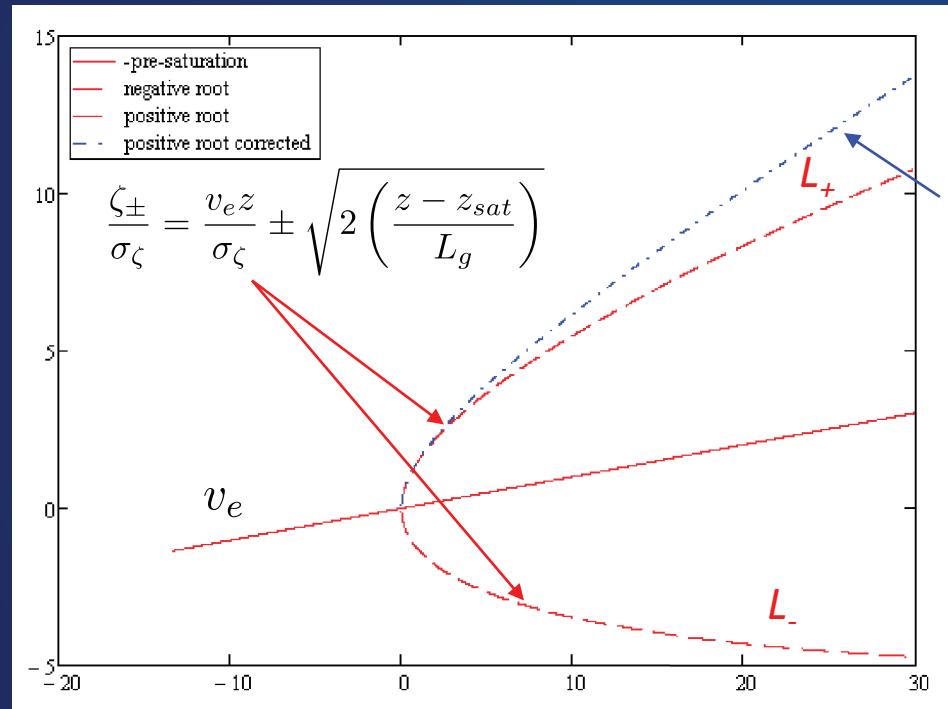
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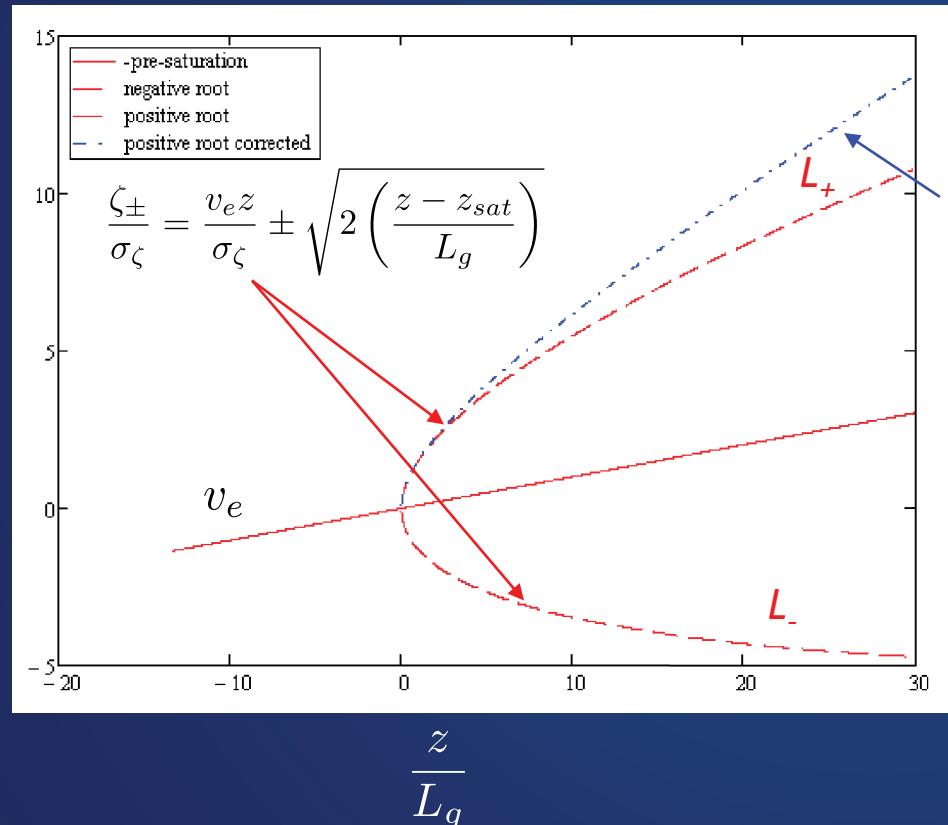
$$\frac{\zeta_+}{\sigma_\zeta} = \sqrt{\left(\frac{v_s z}{\sigma_\zeta}\right)^2 + 2\left(\frac{z - z_{sat}}{L_g}\right) + 2\frac{v_e z}{\sigma_\zeta} \sqrt{2\left(\frac{z - z_{sat}}{L_g}\right)}}$$

Corrected for saturation

Peaks position

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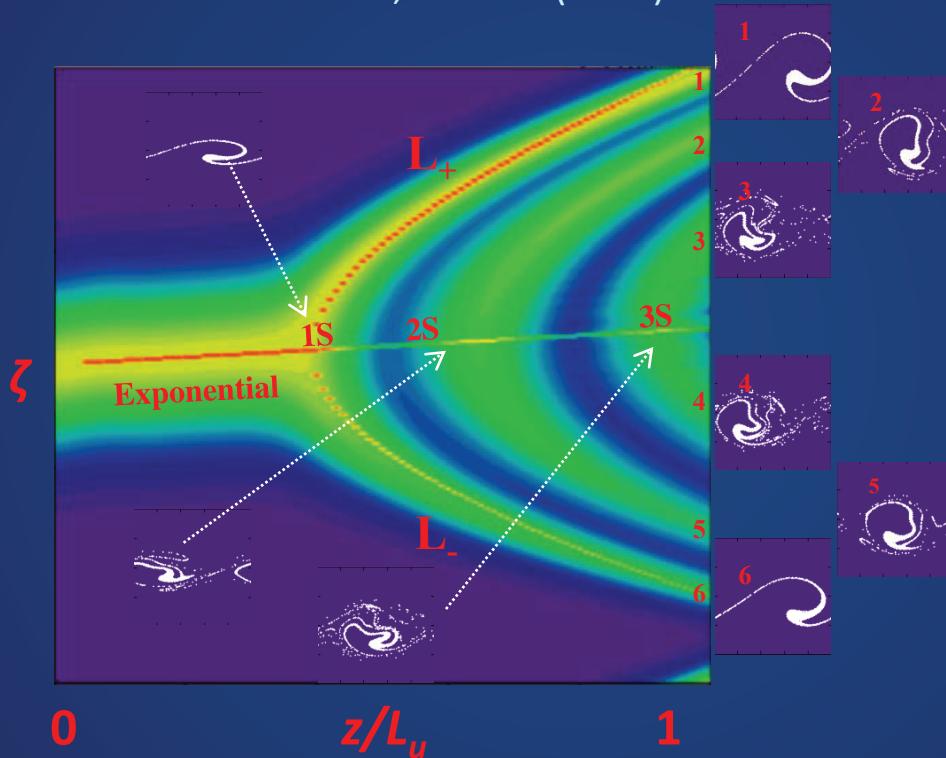
Corrected for saturation

Group velocity of the head mode is obtained by differentiating L_+ with respect to z

The correlation of the tail structure with the longitudinal phase space of the e-beam - Long seed, two symmetric roots

Pulse splitting in short wavelength seeded FEL

M. Labat *et al* PRL 103, 264801 (2009)

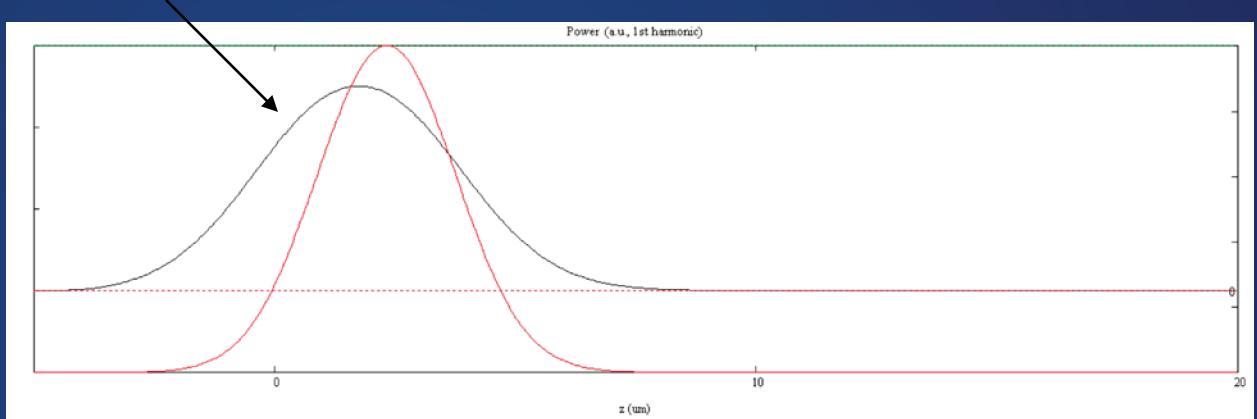


Length of the tail is given by $L_+ - L_-$

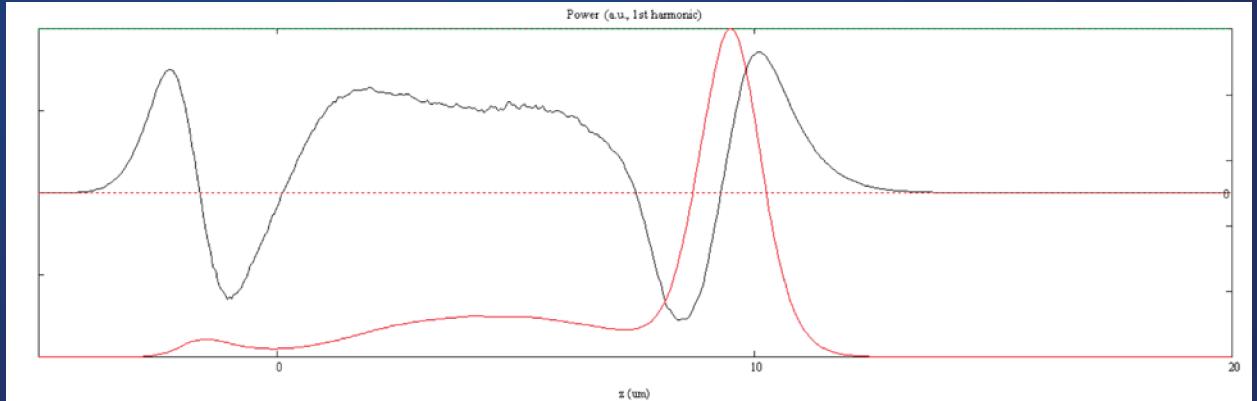
Local gain

Exponential gain

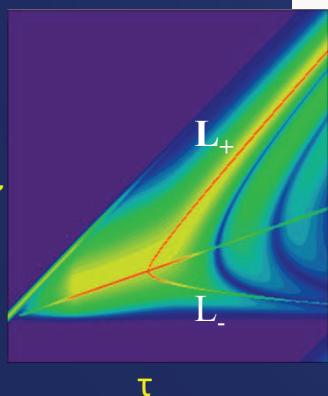
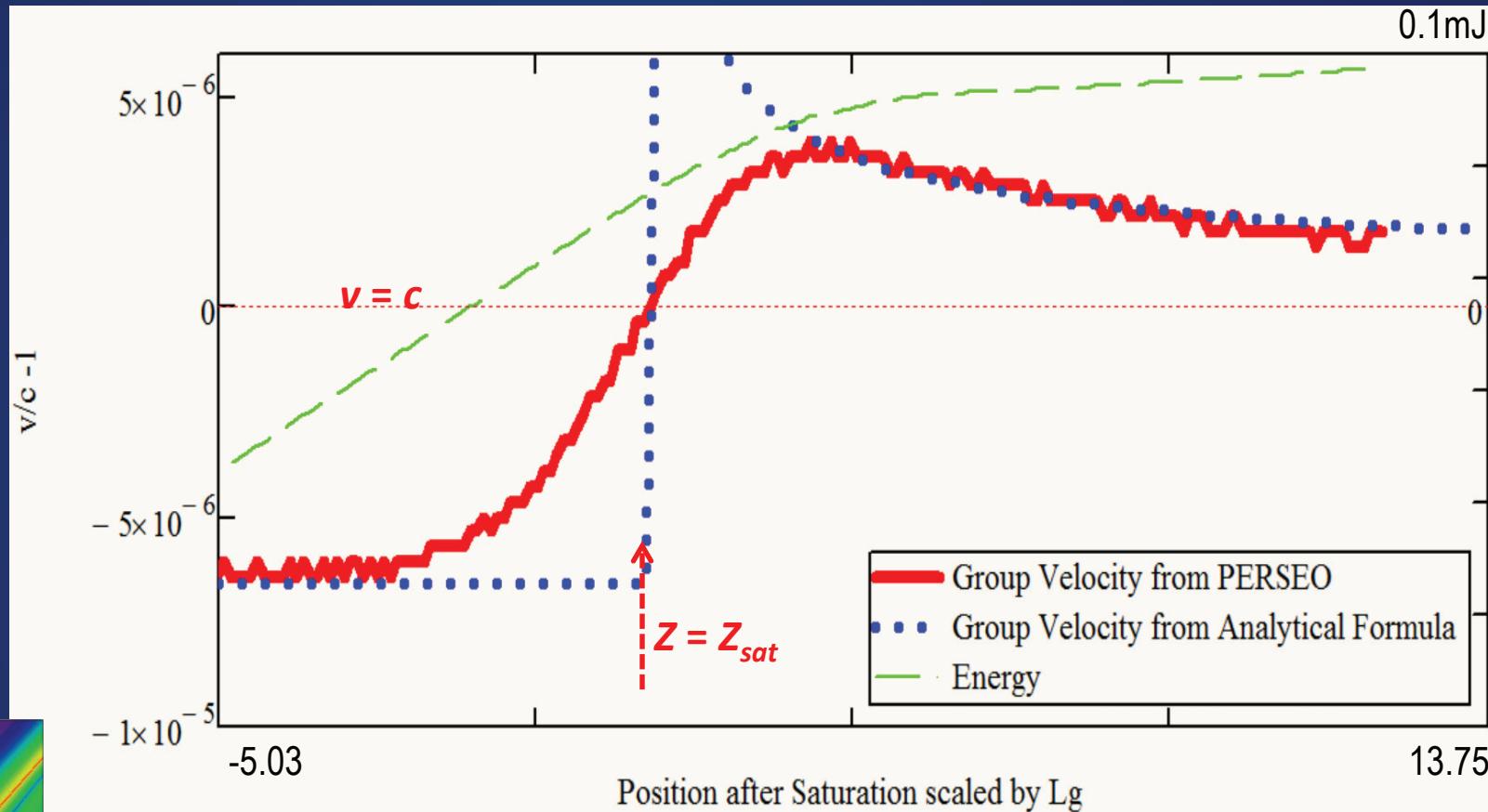
Im. ref. Index



Superradiance

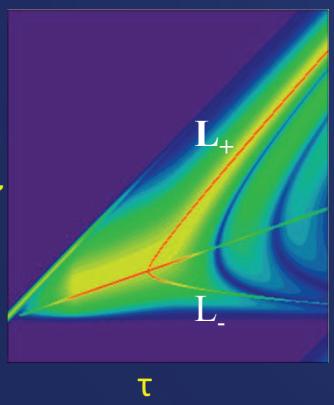
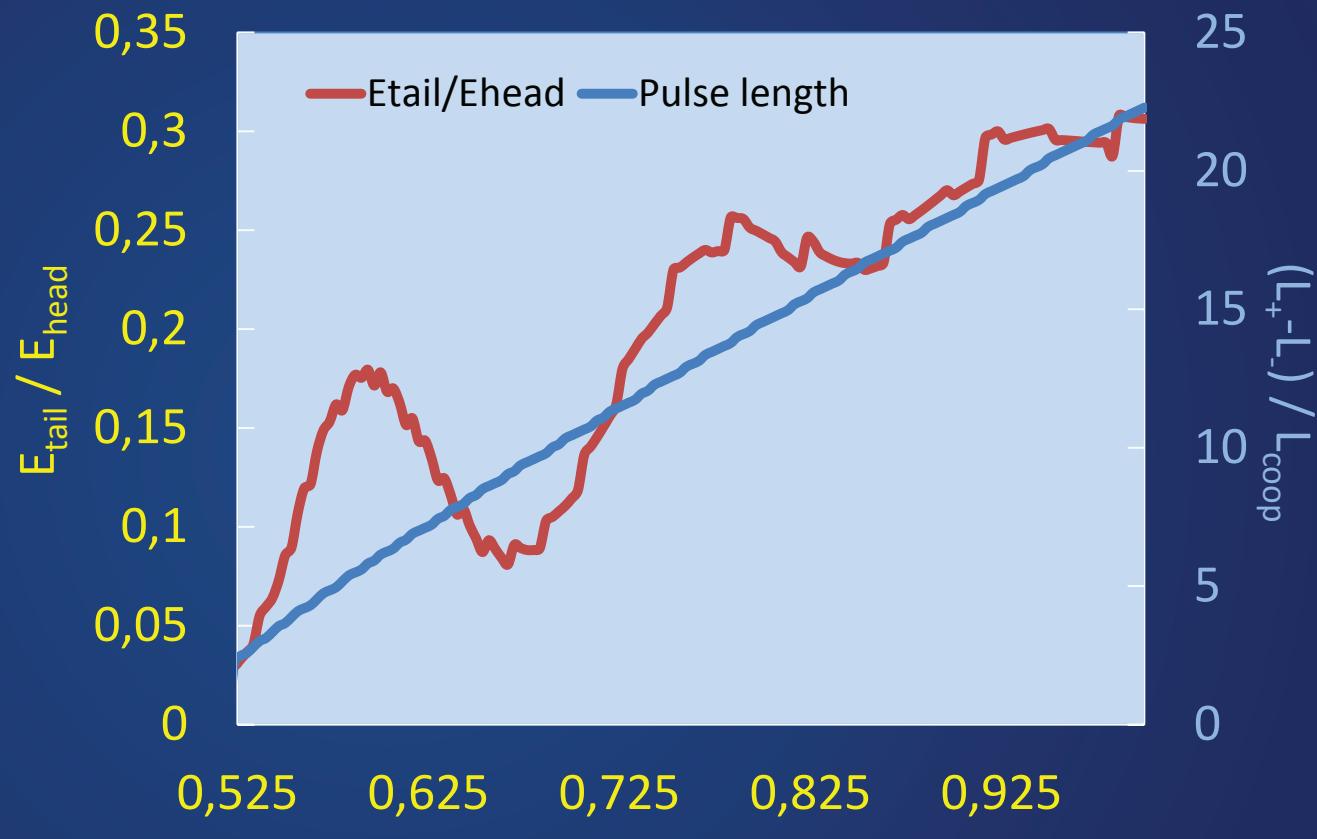


Head Peak Moving at Superluminal Speed



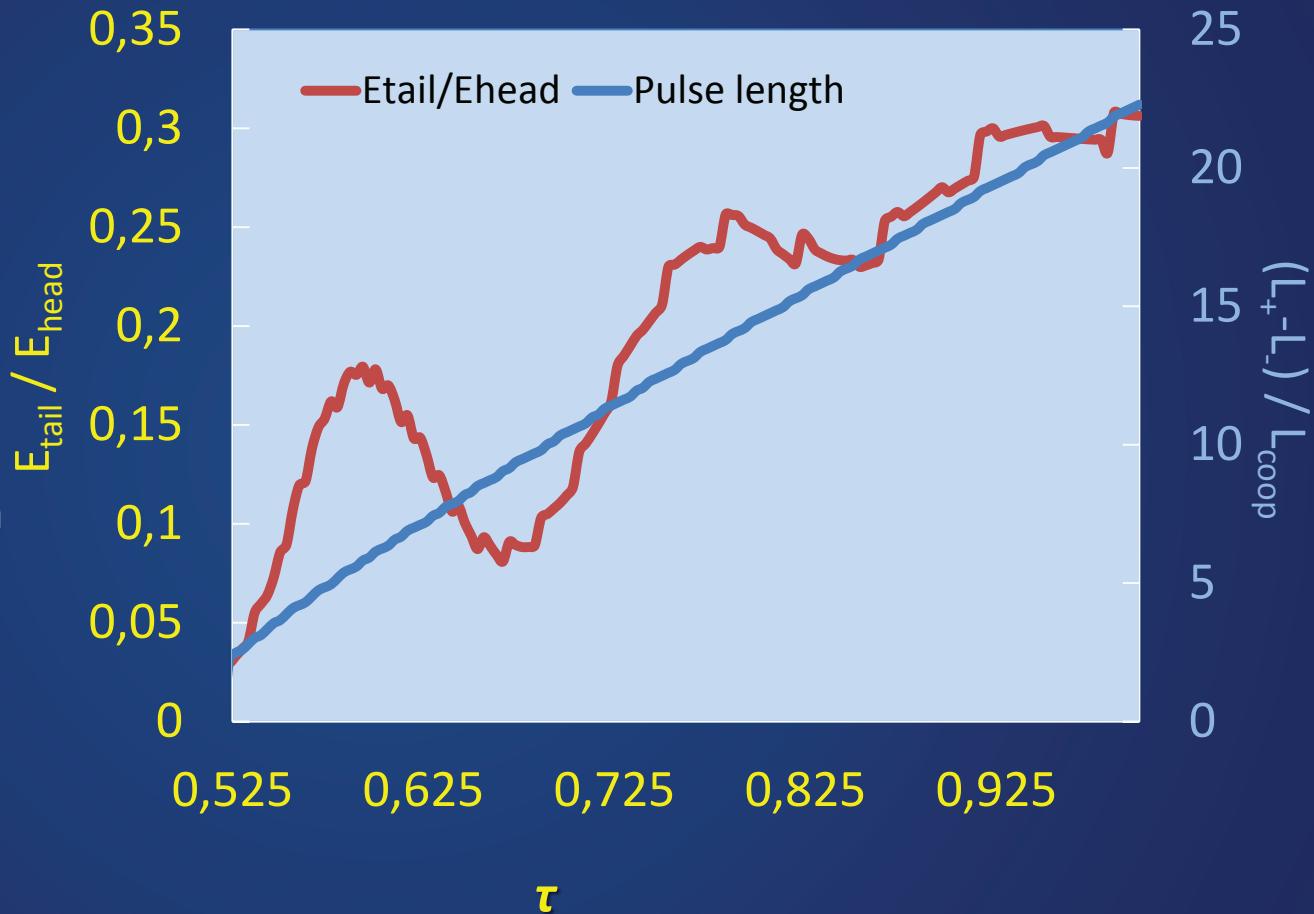
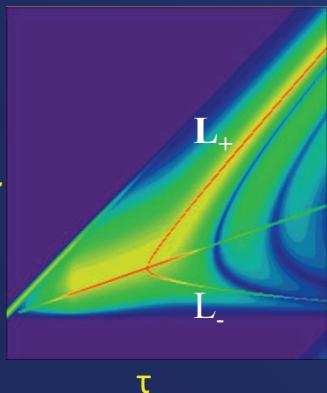
No causality violation, gain distortion, «information» is already distributed

Tail after saturation: E_{tail} is $\sim 30\%$ of E_{main} and pulse is lengthening ~ 10 times

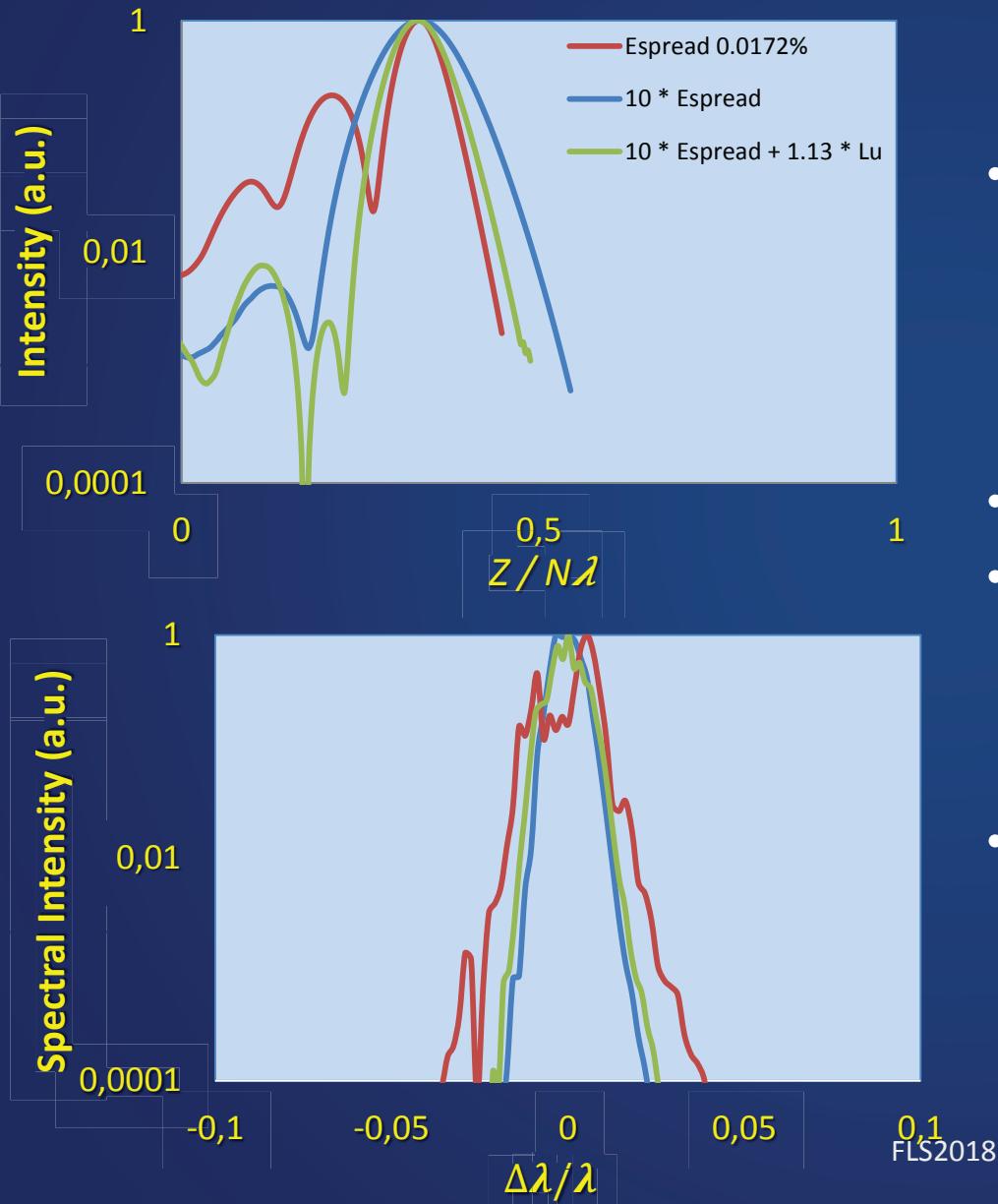


Tail after saturation: E_{tail} is $\sim 30\%$ of E_{main} and pulse is lengthening ~ 10 times

- Tail can have a significant amount of energy, $\sim 30\%$ of the main pulse
- Pulse length ($L_+ - L_-$) gets longer ~ 10 times
- The presence of the tail increases pulse duration and reduces the signal to noise ratio

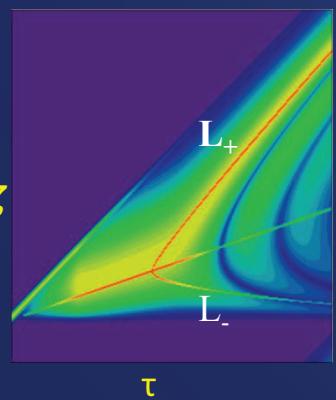
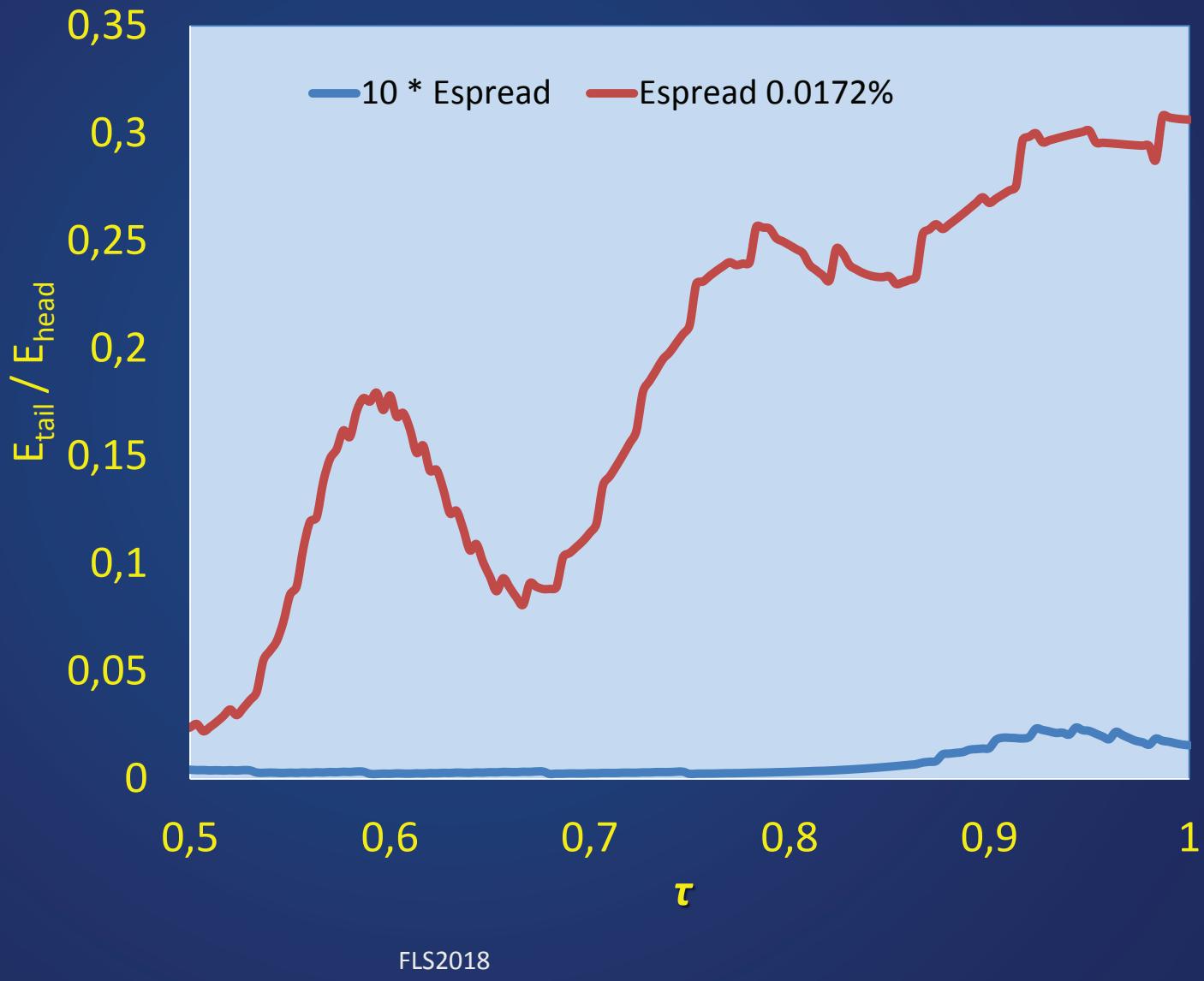


Suppress tail via increasing the energy spread

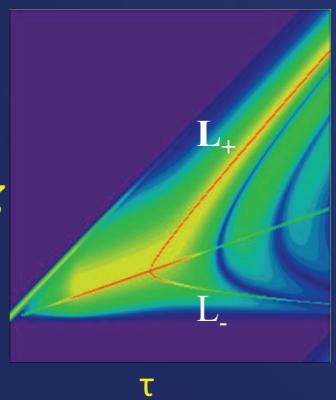
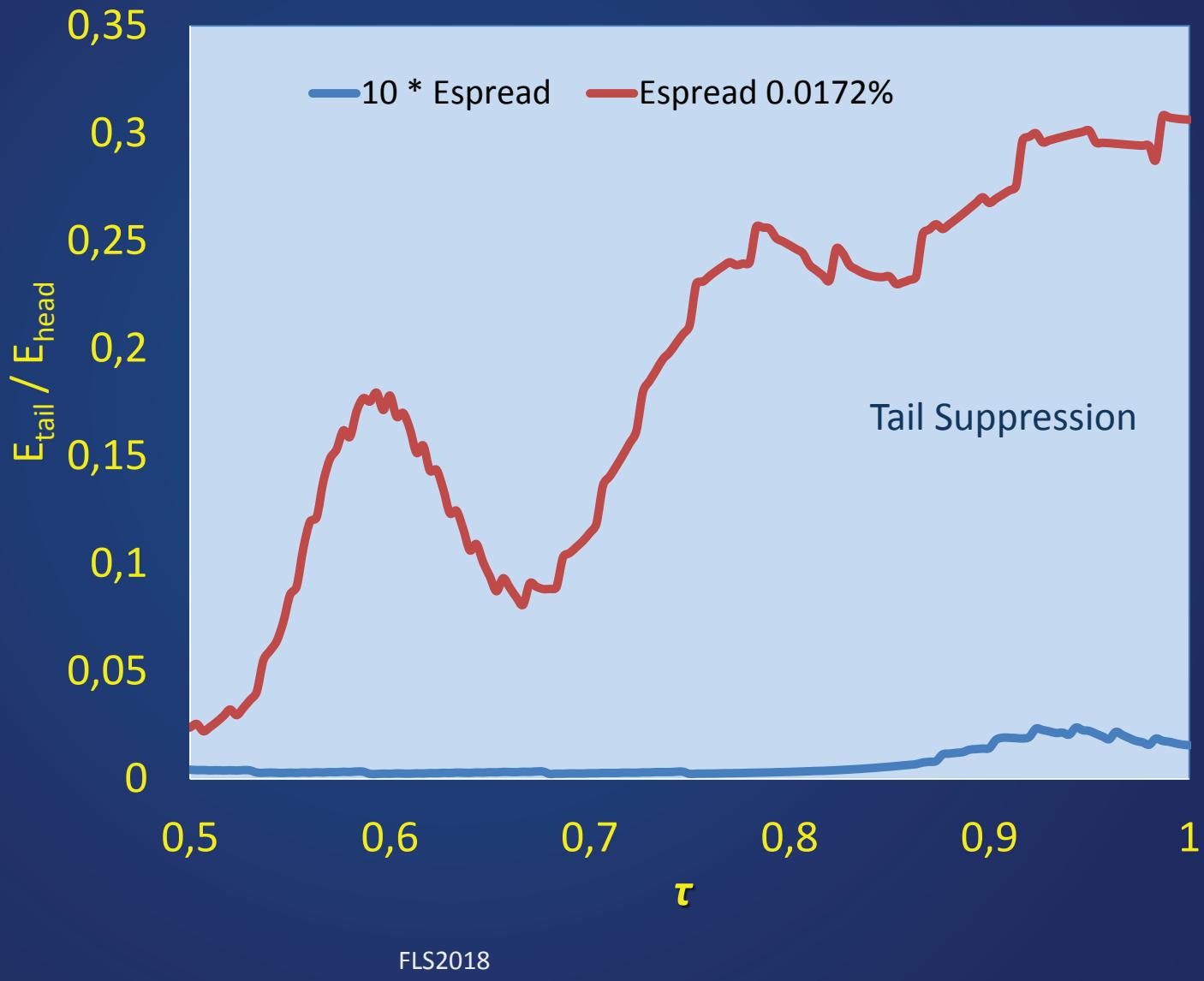


- The laser heater suppressing micro-bunching instability may be considered to increase the energy spread (σ_E/E) to suppress the tail to (< 1%) of the main pulse
- Time-bandwidth product (<0.7)
- A substantial reduction in the total pulse duration accompanied by an increase of the pulse longitudinal coherence
- Reduction in spectral broadening

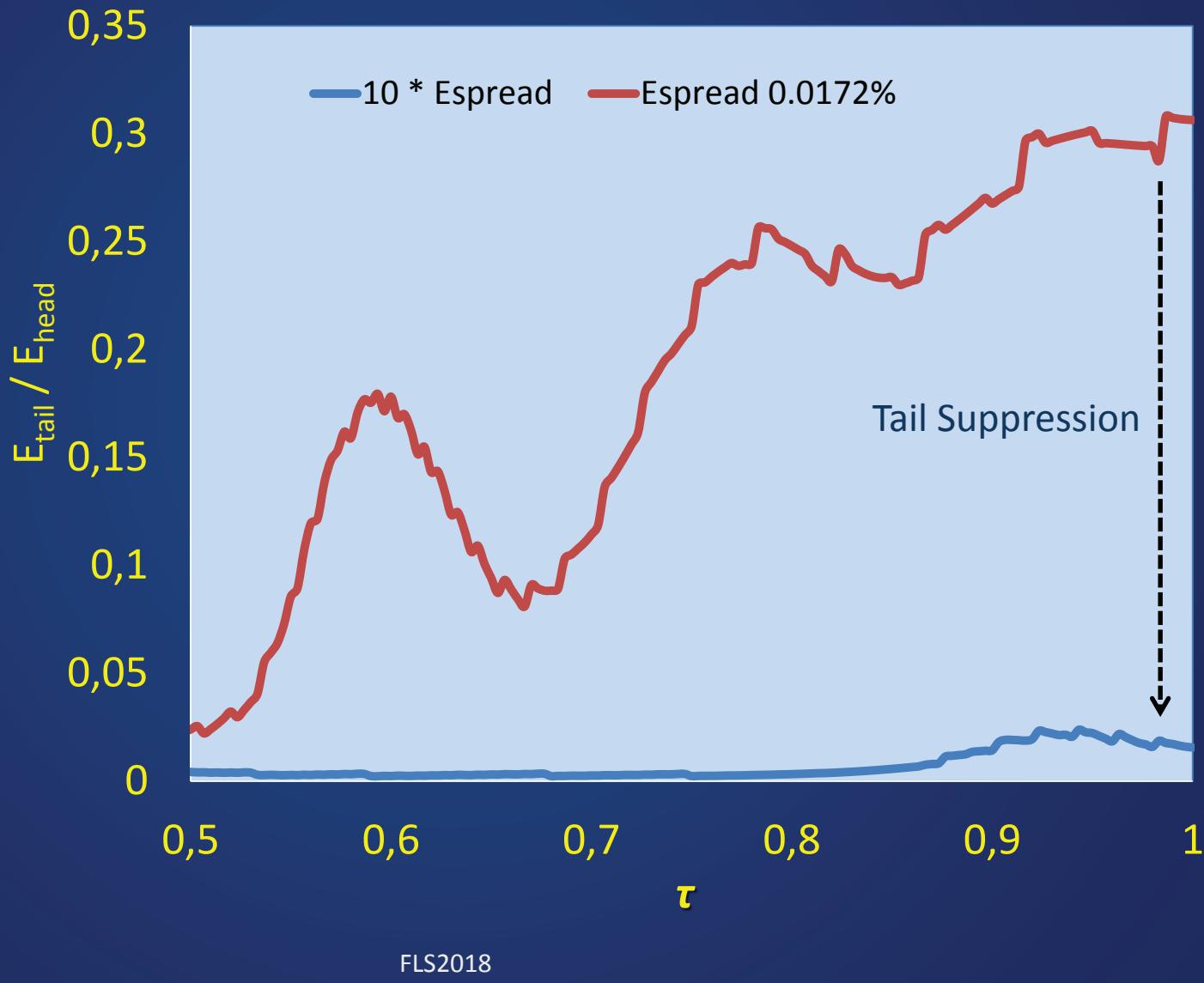
E_{tail}/E_{main} Reduction (~20 times) after Tail Suppression



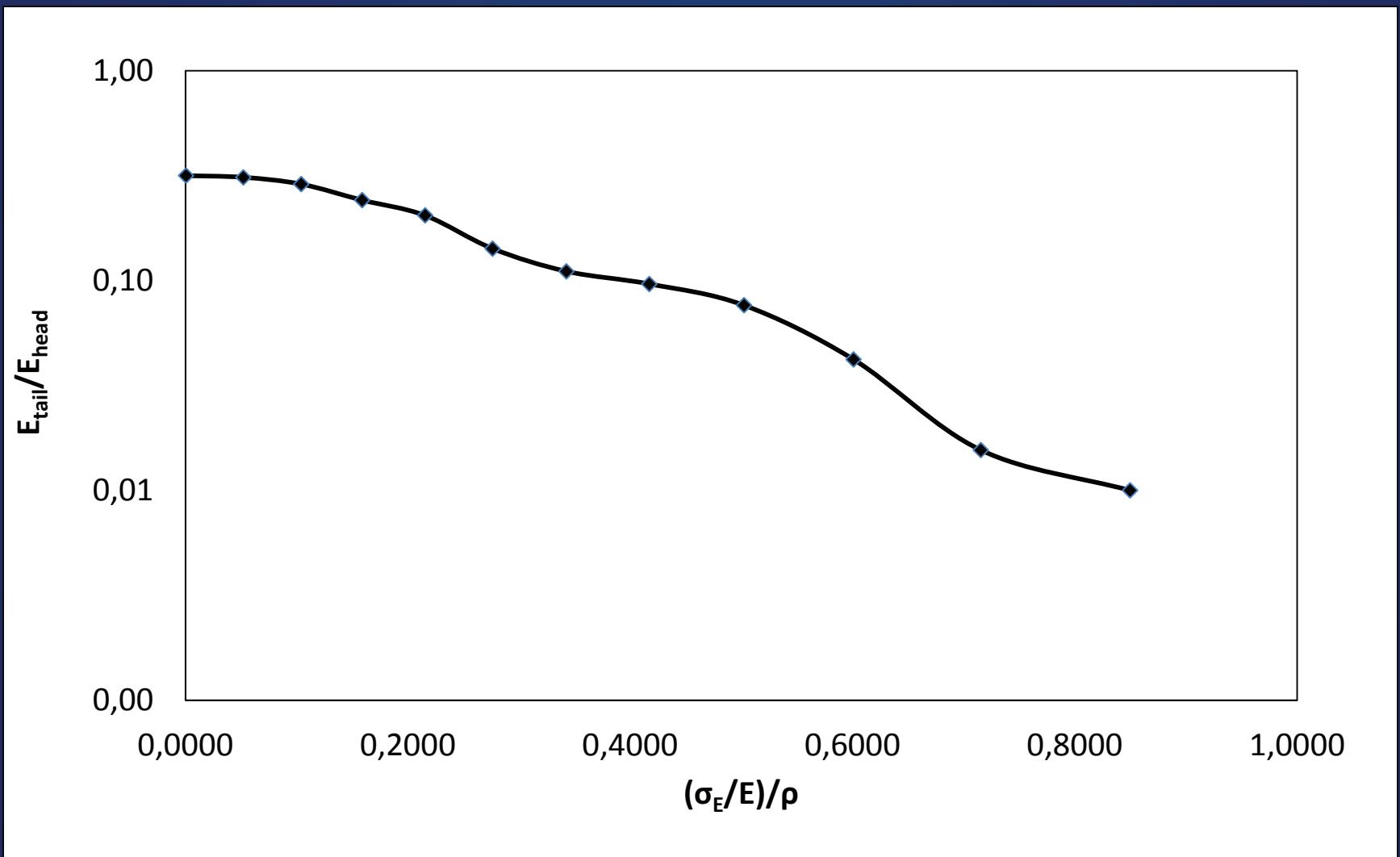
E_{tail}/E_{main} Reduction (~20 times) after Tail Suppression



E_{tail}/E_{main} Reduction (~20 times) after Tail Suppression



E_{tail}/E_{main} as a function of $(\sigma_E/E)/\rho$



Summary

- Time-resolved single-shot imaging of isolated molecules or non-periodic structures requires an XFEL with peak power at multi-GW level and sub-femtosecond temporal duration → **FEL operating in single spike - superradiant regime**
- When single spike reaches saturation, pulse splits and tail is formed. We studied this process in ideal conditions, "flat" beam parameters, no taper
- Peak of **the pulse propagates at superluminal speed**
The **tail is constituted by a train of pulses with both transverse and longitudinal coherence and decaying amplitudes**
- **Suppressing the tail to <1% of the main pulse**, can be achieved by inducing additional energy spread. Observed a factor of 10 reduction in the pulse duration and a factor of 20 reduction in $E_{\text{tail}}/E_{\text{main}}$