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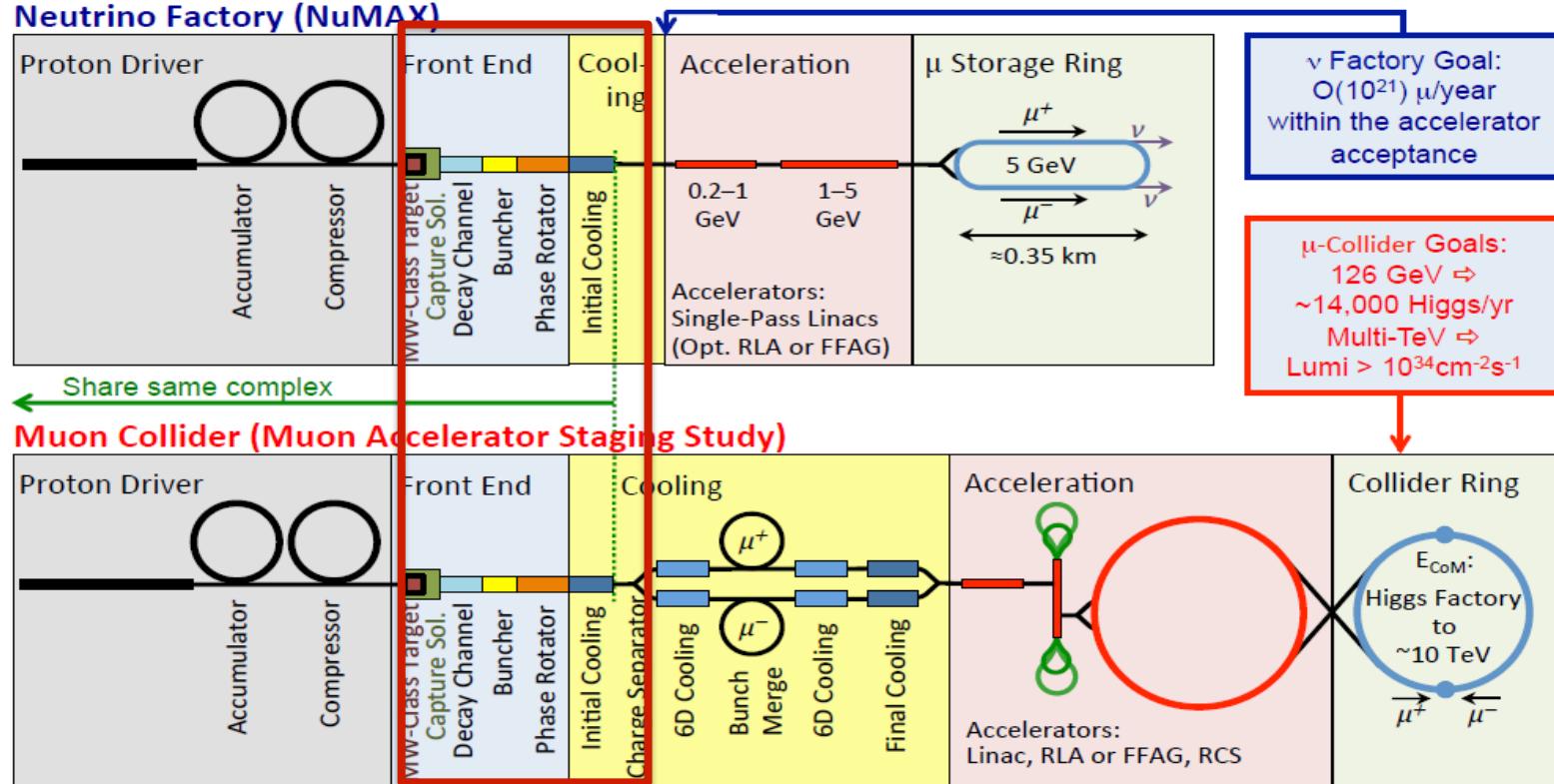
Progress of Front End Design and FOFO Snake

David Neuffer, Y. Alexahin FNAL

Outline

- **Front end design**
 - Baseline configuration
 - Buncher Phase Rotator
 - Cooler options
- **HFOFO “Snake” properties**
 - Design Concepts
 - Example (IBS)
 - Simulation
- **Variations**
 - cold muon source

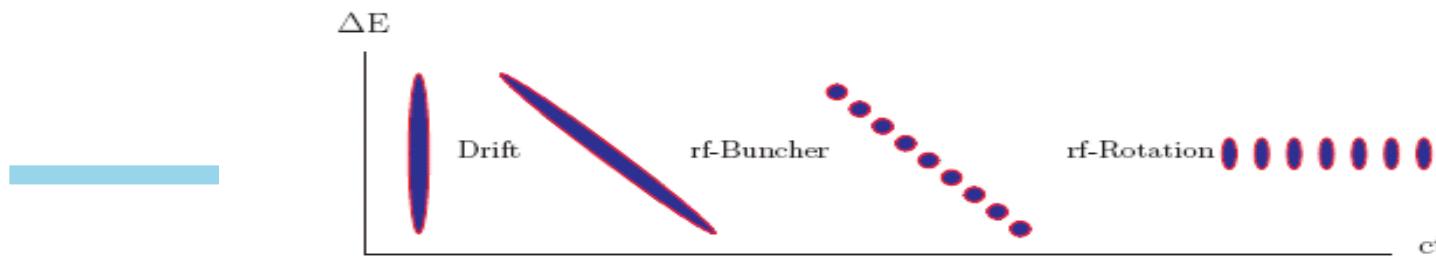
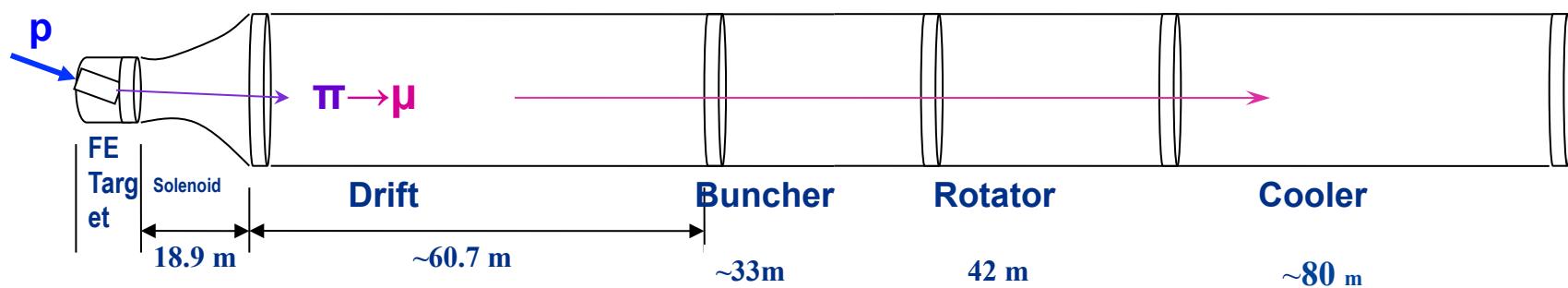
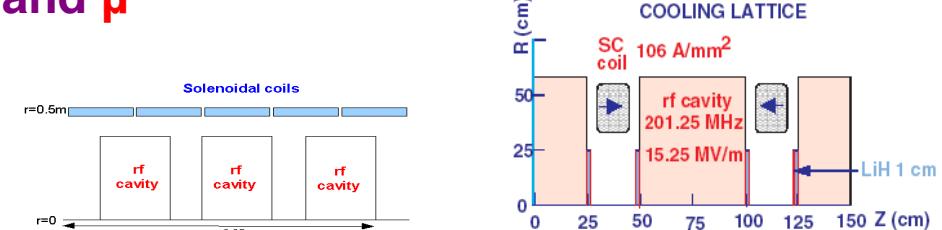
Front End and Initial Cooling



- **From target to end of initial cooling**
 - capture and bunch $\pi \rightarrow \mu$; initial cooling for downstream
 - captures & cools both signs (μ^+ and μ^-)
- **Same system can be used for both ν factory and $\mu^+ \text{-} \mu^-$ collider**

IDS Neutrino Factory Buncher and ϕ -E Rotator

- Drift ($\pi \rightarrow \mu$)
- “Adiabatically” bunch beam first (weak 320 to 232 MHz rf)
- Φ -E rotate bunches – align bunches to ~equal energies
 - 232 to 202 MHz, 12MV/m
- Cool beam 201.25MHz
- Captures and Cools both μ^+ and μ^-



Buncher/Rotator Example

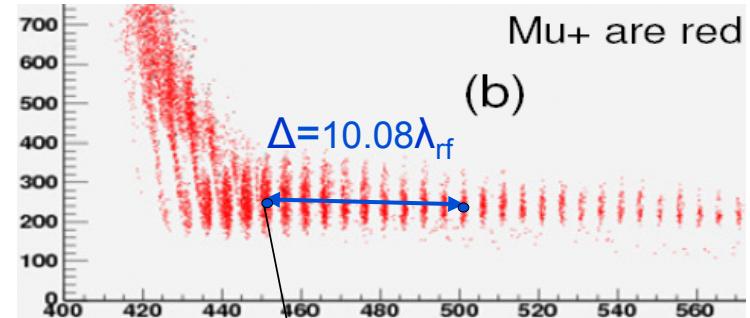
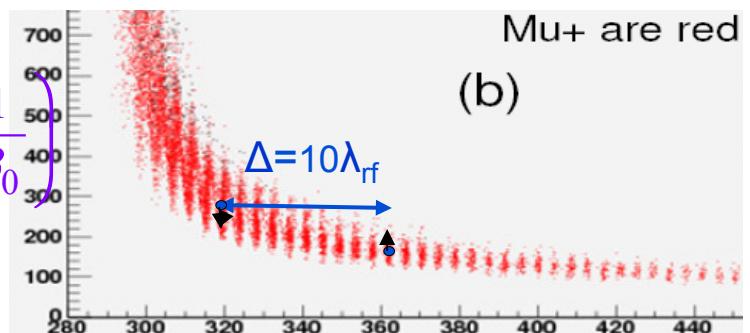
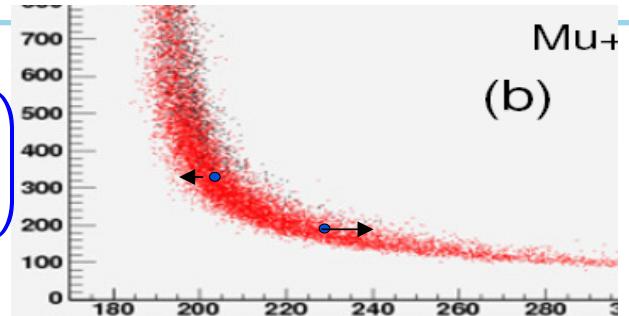
- **Drift** from target ~60m

- $\pi \rightarrow \mu$
- Beam lengthens

- **Buncher** (~30m)

- $N=10, P_0=280\text{MeV}/c, P_N=154\text{MeV}/c$
- $330 \rightarrow 235 \text{ MHz}$
- $V'=0 \rightarrow 10 \text{ MV/m}$

$$\delta(ct_i) = L \left(\frac{1}{\beta_i} - \frac{1}{\beta_0} \right)$$



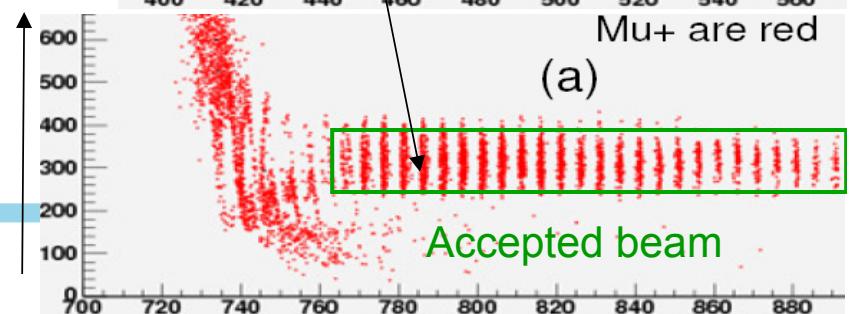
- **Rotator** (~35m)

- $N=10.08$ – accelerate/decelerate bunches
- $235 \rightarrow 202 \text{ MHz}, V'= 12 \text{ MV/m}$

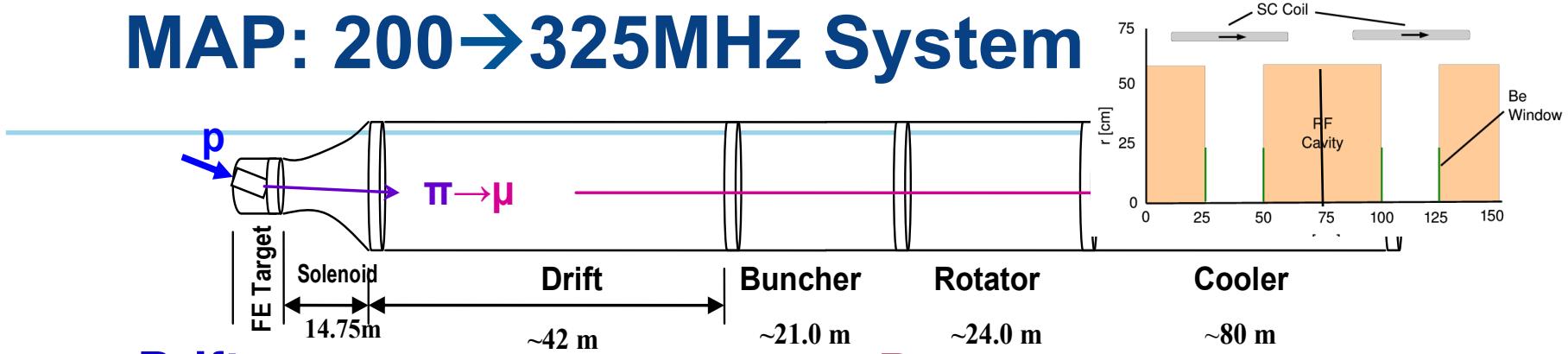
- **Cooler** (~80m)

- $201.25 \text{ MHz, ASOL lattice}$
- 15MV/m in rf cavities
- LiH or H₂ cooling

- Captures both μ^+ and μ^-



MAP: 200→325MHz System



- **Drift**
 - $20\text{T} \rightarrow 2\text{T}$
- **Buncher**
 - $P_o = 250\text{MeV}/c$, $P_N = 154 \text{ MeV}/c$; $N=12$
 - $V_{rf} : 0 \rightarrow 15 \text{ MV/m}$
 - $f_{RF} : 490 \rightarrow 365\text{MHz}$
- **Rotator**
 - $V_{rf} : 20\text{MV/m}$
 - $f_{RF} : 364 \rightarrow 326\text{MHz}$
 - $N=12.045$
- **Cooler**
 - $245 \text{ MeV}/c$, 325 MHz , 25 MV/m
 - LiH absorbers

325 MHz – much more affordable than 200MHz

more compact, $\sim 1/2$ rf power

matches present/future power sources/ frequencies-ILC,

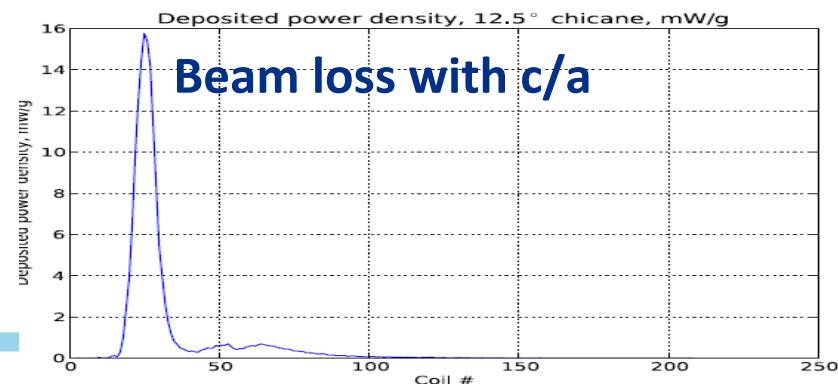
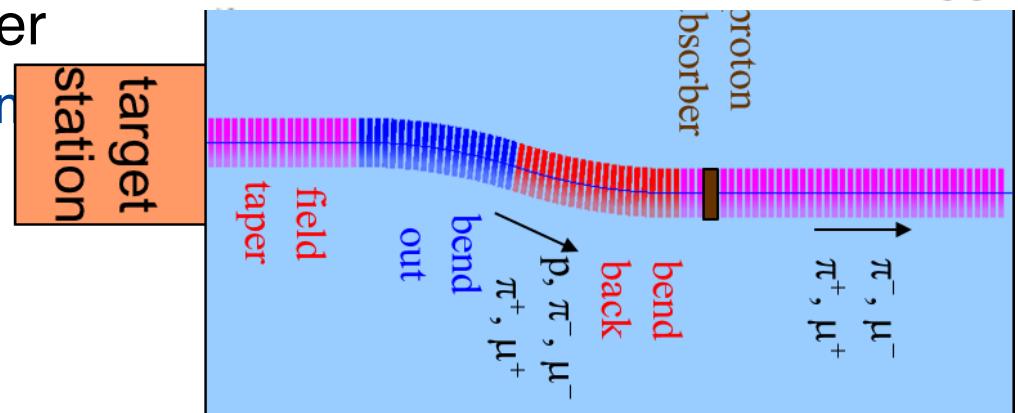
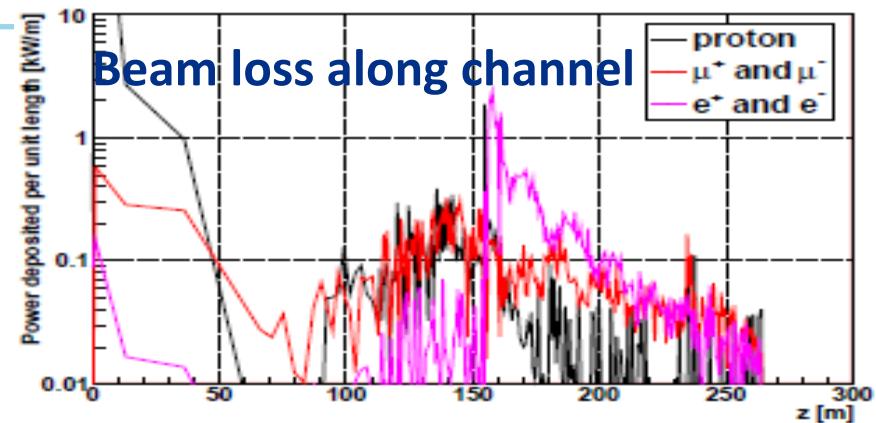
PIP II

but more bunches in bunch train for collider ($\sim 12 \rightarrow \sim 21$)



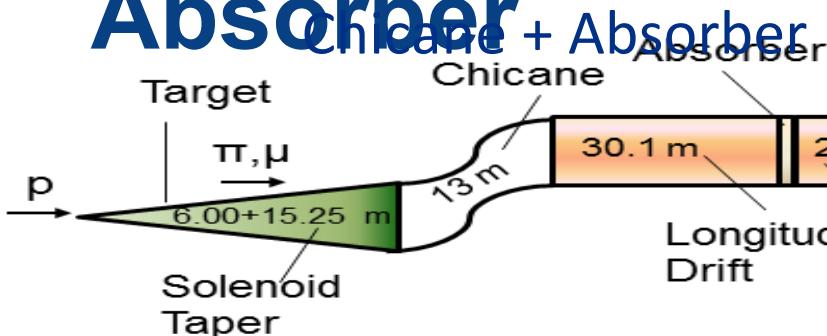
Problem: Beam Losses & Activation

- Beam Loss and Activation
 - 4MW p beam
 - 100 kW secondaries ..
 - ~kW/m losses in line
- Solution: Chicane and Absorber
 - Chicane: bend out ~15° 6.5m
 - bend back ~15° 6.5m
 - separates high-E particles
 - Absorber
 - ~10 cm Be
 - stops p, K, low-E
- Localizes beam-related losses to before buncher/rf

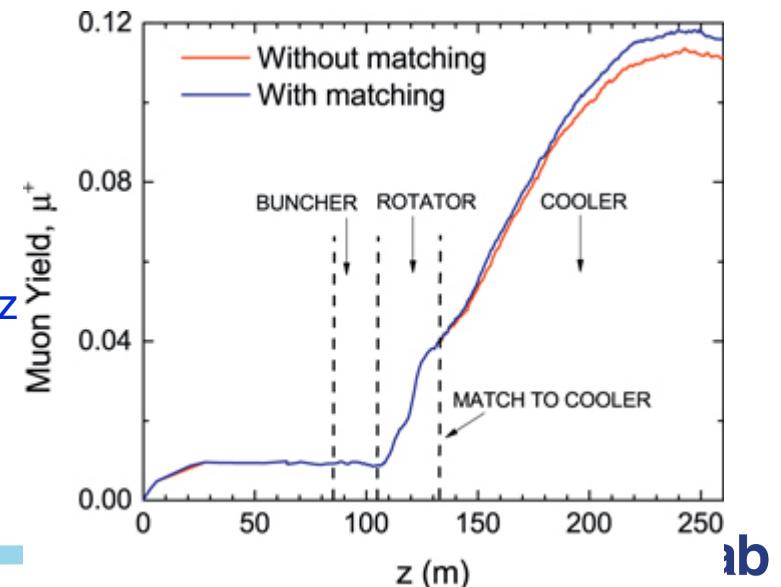
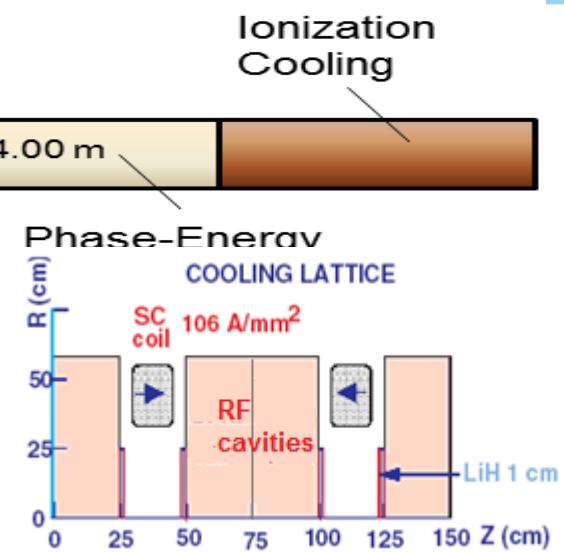


325 “Collider” w Chicane/

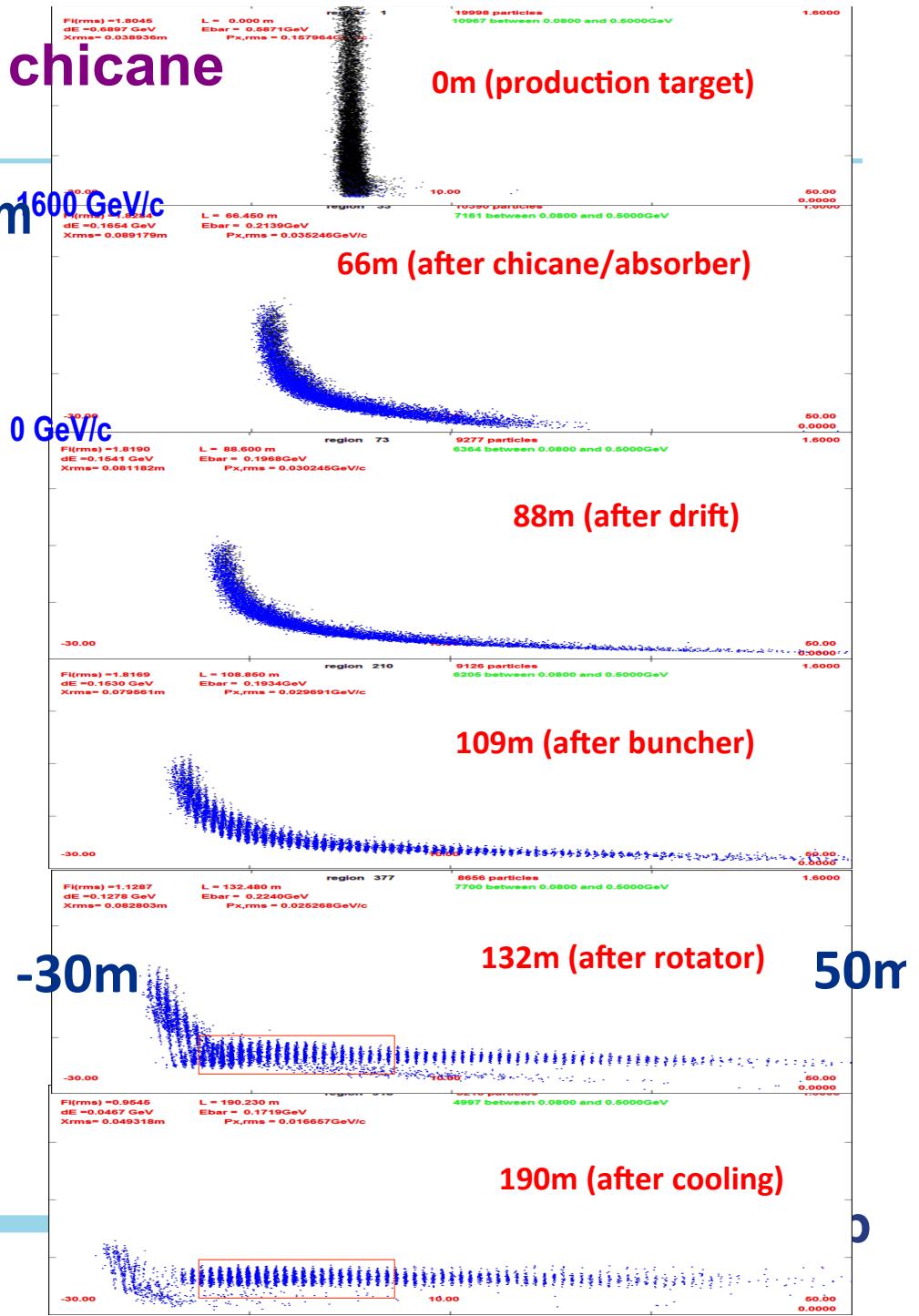
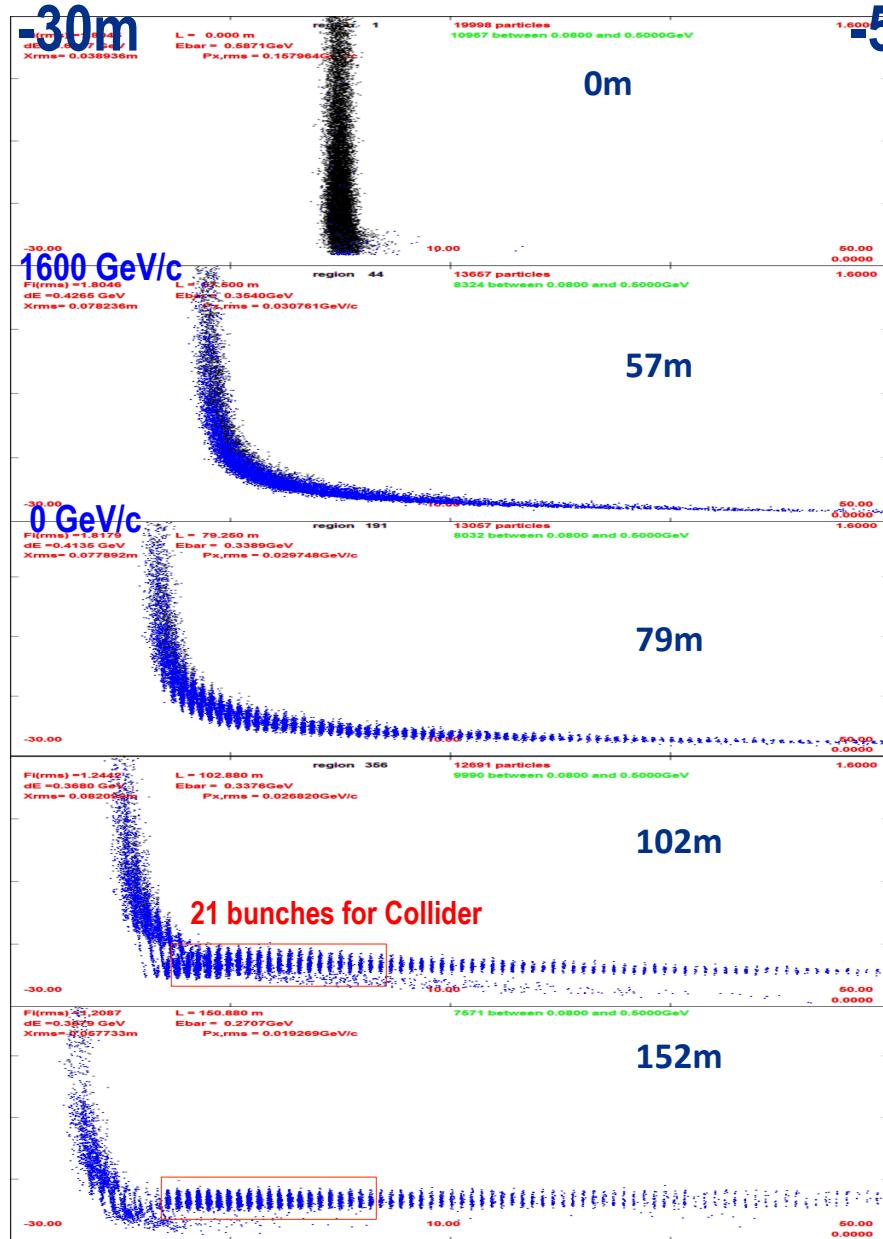
Absorber



- Add chicane
 - $6.5\text{m} \rightarrow +15^\circ, 6.5\text{m} -15^\circ$
- Add 30 m drift after chicane to absorber
 - $6.5\text{m} \rightarrow +15^\circ, 6.5\text{m} -15^\circ$
- Rematch
 - particle 1-283 MeV/c $\rightarrow 250$
 - particle 2-194 MeV/c $\rightarrow 154$
 - Bunch ($N=12$) $0 \rightarrow 15 \text{ MV/m}$: $496 \rightarrow 365 \text{ MHz}$
 - Rotate ($N=12.045$) – 20MV/m : $365 \rightarrow 326.5 \text{ MHz}$
 - Cool -325MHz -25 MV/m
- Obtain $\sim 0.1 \text{ } \mu^+ \text{ and } \mu^-/\text{p}$

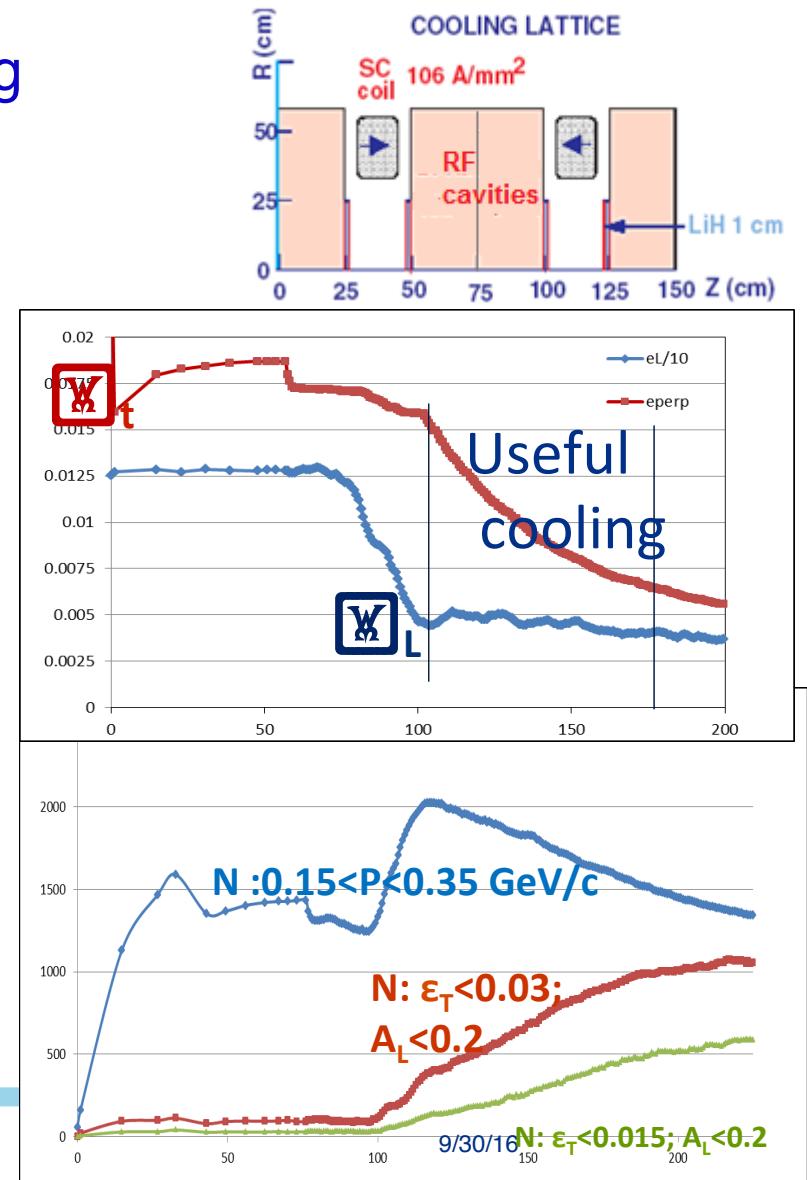


Compare without/with chicane



Cooling Section – “2-D” cooling only

- Baseline Initial cooling system
 - from IDS Neutrino Factory cooling
 - Consists of rf & LiH absorbers & Alternating Solenoid focusing
- Cools transverse emittance
 - $\sim \mathcal{W}_t : 0.016 \rightarrow 0.0065 \text{ m}$
 - $\mathcal{W}_L : 0.04 \rightarrow \sim 0.03 \text{ m}$
 - no longitudinal cooling (scraping)
- $\sim 0.1\mu / 8\text{GeV p}$ within acceptance
 - most beam outside acceptance scraped away

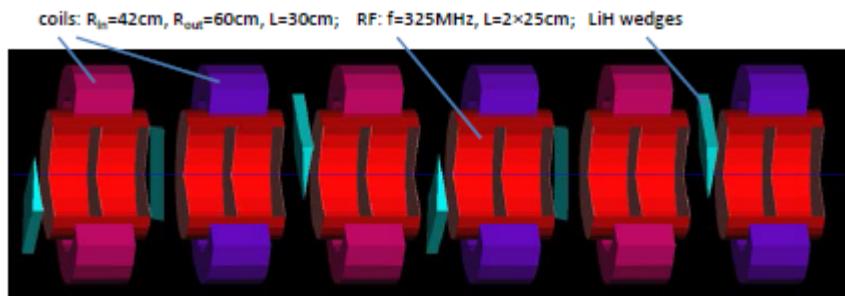


Vacuum rf or Gas-filled rf?

- Initial design was for vacuum rf within $B = \sim 2T$ solenoids
 - rf gradient limited within magnetic fields (?)
 - gas-filled rf does not breakdown
 - (but has plasma loading effect)
- Front end can have gas-filled rf
 - same performance as with vacuum rf
 - need a bit higher gradient to compensate energy loss in gas
 - With higher density gas and higher gradient
 - can have some cooling in buncher/rotator
 - better performance
- Would like to increase $B \rightarrow 3T$

“FOFO Snake” initial cooling [Y. Alexahin et al.]

- Motivation
 - Obtain front end 6-D cooling
 - equal cooling in x and y
 - cyclotron and drift modes
 - For both μ^+ and μ^-
 - Dispersion+wedge would only cool one sign ...
 - (we thought ...)
- Principles
 - Alternating solenoid cooling
 - resonance dispersion
 - tilts in solenoids
 - Longitudinal cooling from path length (E_μ)

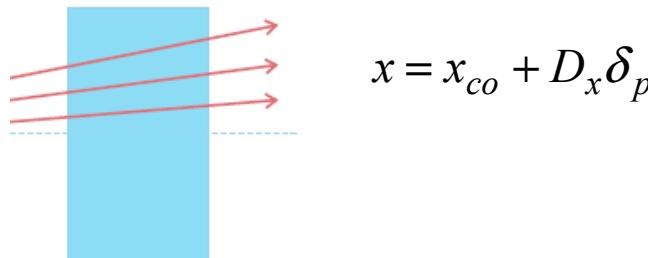


$$D_x = \frac{d x_{co}}{d \delta_p} \approx -\pi Q'_x x_{co} \cot(\pi Q_x)$$

Basic Principles of “FOFO Snake”

- Alternating Solenoid field
 - Equal cooling of transverse modes
 - cyclotron/drift modes exchange at each flip
- Resonance Dispersion generation
 - solenoid tilts generate helical orbit/dispersion
 - $x_{co} \sim 1/\sin(\pi Q_x)$; $D_x = \frac{d x_{co}}{d \delta_p} \approx -\pi Q'_x x_{co} \cot(\pi Q_x)$
 - larger compaction factor if tune $\sim N + \delta$
- Longitudinal cooling in flat absorbers due to D'

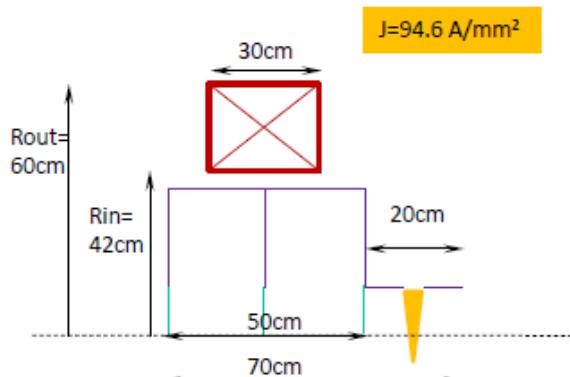
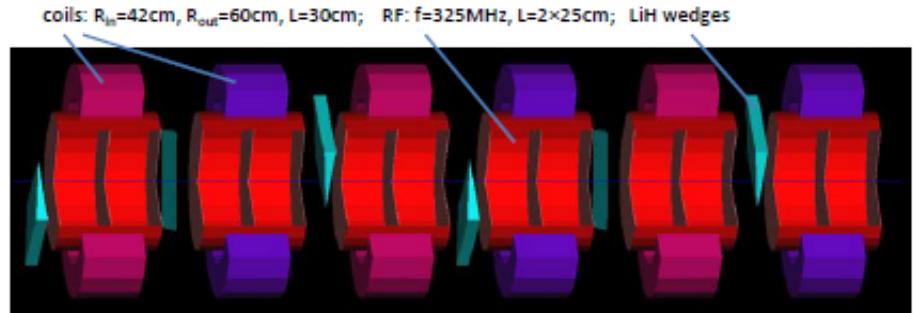
- path length (δ_p)



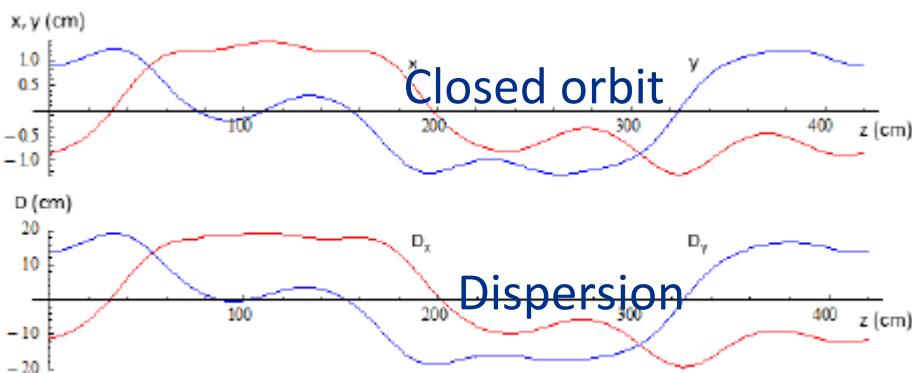
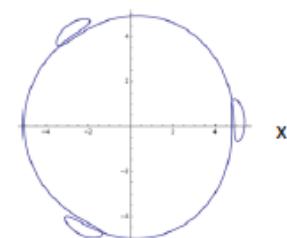
- initially without wedge absorbers

Baseline 325 Mhz cooler example

- 6 cell period
 - 4.2m, $B_{\max}=3.7\text{T}$
 - $\beta_t \sim 0.6\text{m}$
 - 325MHz rf, 25 MV/m
 - 2.5 mrad Tilts
- Gas filled (1/5 Liquid H₂ density)
 - (slabs could also be used)
 - with LiH wedges



Single Cell

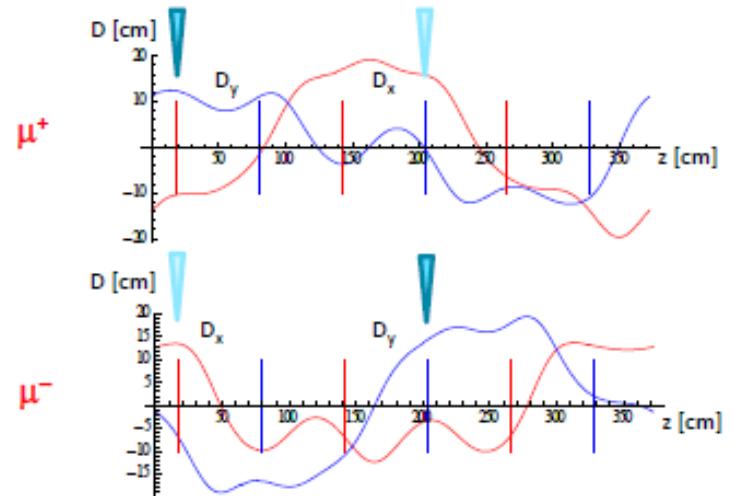
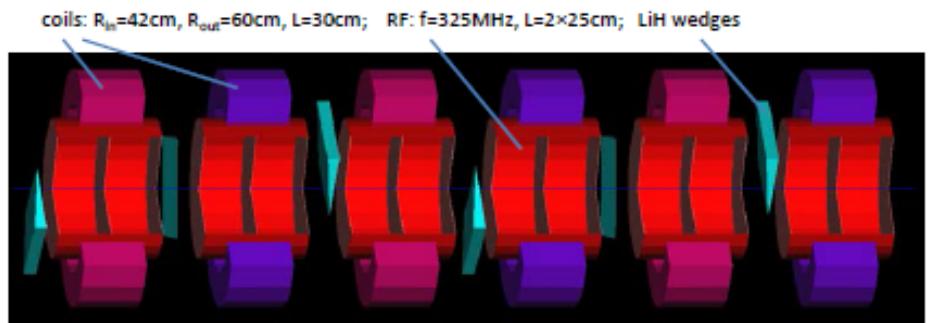


FODO snake properties

- 2.5 mrad tilts oriented at
- $\phi_k = \frac{4\pi}{3}, 0, \frac{2\pi}{3}, \frac{4\pi}{3}, 0, \frac{2\pi}{3}$ from vertical
- Wedges follow similar rotation
 - Are placed to **cool both signs**: μ^+ and μ^-
- Eigen values, equilibrium ϵ

Mode	I	II	III
Tune	$1.2271 + 0.0100 i$	$1.2375 + 0.0036 i$	$0.1886 + 0.0049 i$
Emittance (mm)	2.28	6.13	1.93

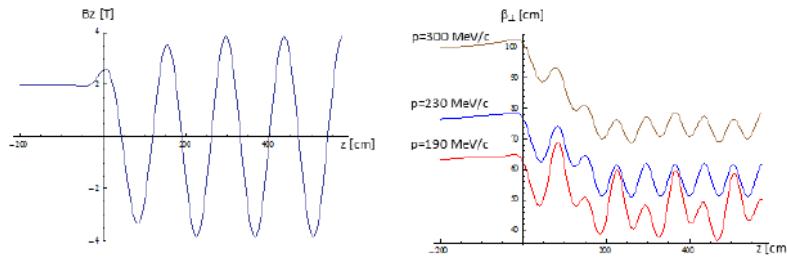
- not balanced in x, y – (add quad)
- Total cooling channel is
~30 cells (126 m)



Dispersion and two vertical wedge absorbers:
the left works for μ^+ while the right works for μ^-

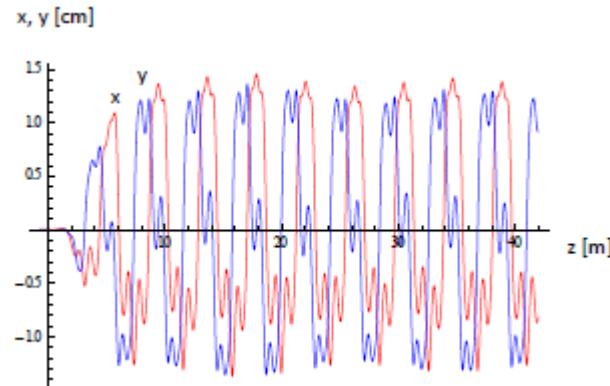
Matching from upstream Rotator

- Transverse Optics match
 - constant solenoid to ASOL

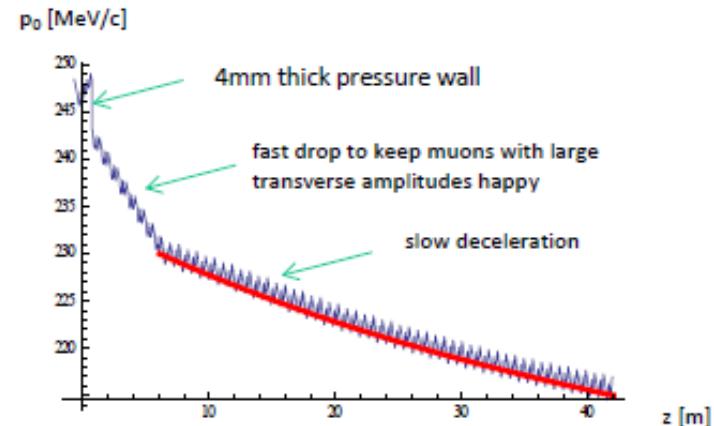


Magnetic field in the transition area (left) and β -function for constant momentum (right)

- Helical Orbit match
 - tilts of solenoids 3-9

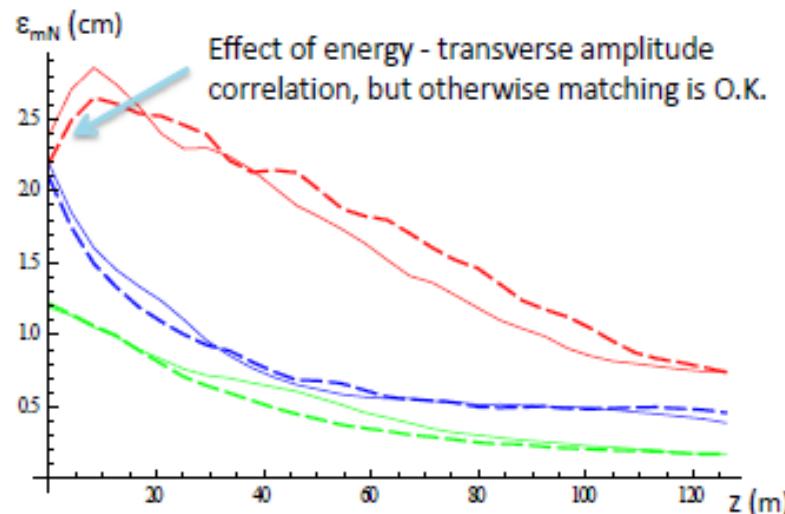


- Longitudinal momentum match
 - gradual deceleration

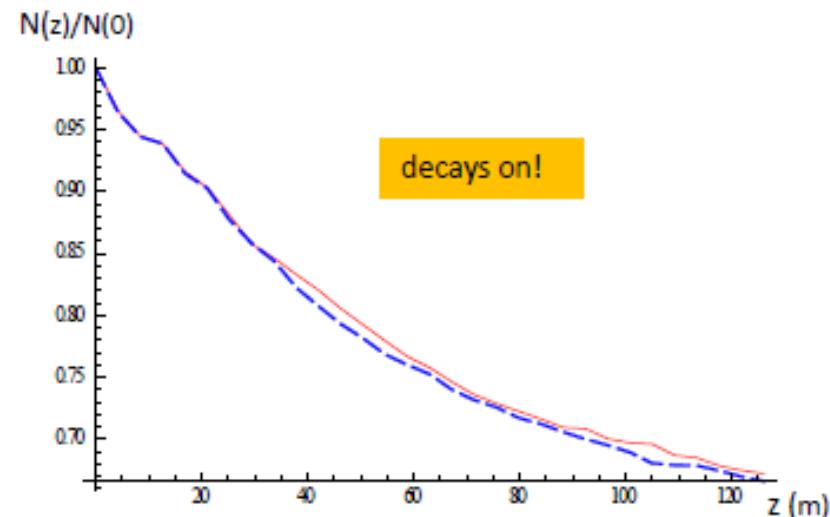


- phases readjusted to compensate for amplitude/momentun correlation

Cooling & Transmission (G4BL)



Normalized emittances (cm) from Gaussian fit:
 μ^+ - solid lines, μ^- - dashed lines.



Transmission as a ratio of the number of muons in the Gaussian core: red solid line - μ^+ , blue dashed line - μ^- .

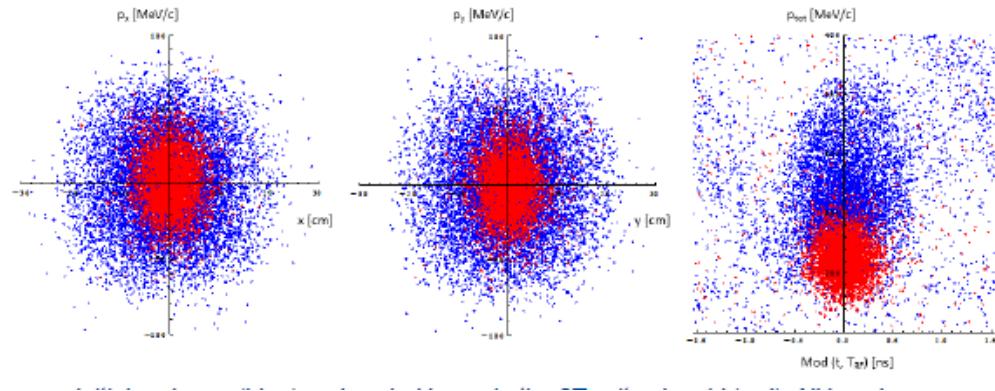
Final/Initial values (Gaussian fit):

	$N^{(\text{total})}$	$N^{(150 < p < 360)}$	$N^{(\text{core})}$	$p^{(\text{cut})}$, MeV/c	$\epsilon_{mN}, \text{ cm}$			
μ^+	5378/11755	5167/7998	5010/7329	208.2/248.0	0.19/1.19	0.36/2.19	0.76/2.38	0.051/6.22
μ^-	5896/12396	5743/9020	5499/8248	207.7/248.8	0.16/1.22	0.46/2.10	0.72/2.19	0.051/5.59

Results and discussion

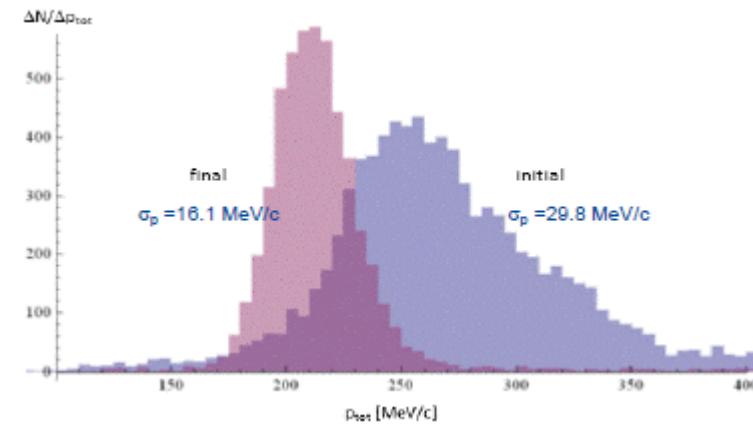
- **Beam phase space**

- before (blue)
- after (red)



- **Longitudinal distributions**

- momentum spread reduced by factor of ~ 2



Comparison to 2-D cooling

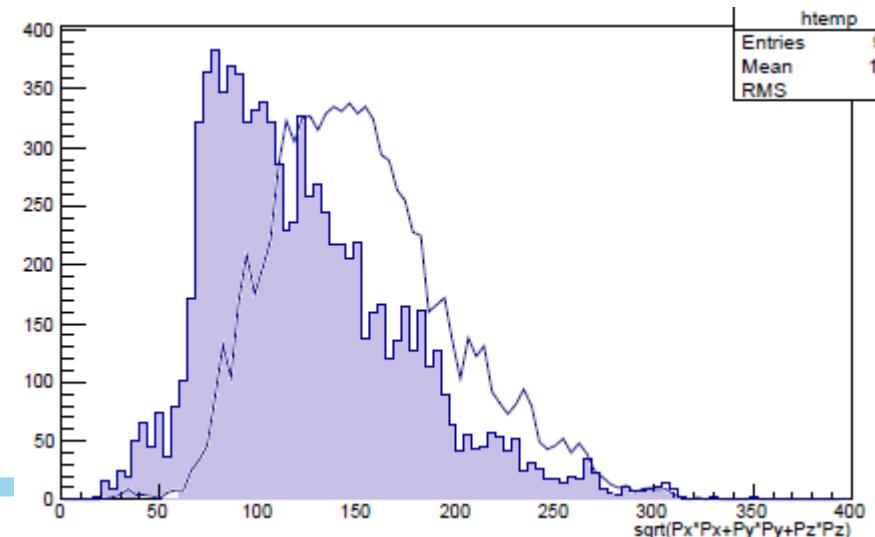
- Cools in 3-D
 - ε_1 : $2.2 \rightarrow 0.4$ cm ; ε_2 : $1.2 \rightarrow 0.2$ cm; ε_L : $2.4 \rightarrow 0.7$ cm
 - ε_t : $1.7 \rightarrow 0.6$ (2D)
- More Cooling (than 2-D baseline)
 - but longer channel & stronger focusing
 - up to 120m; B_{\max} $2.8 \rightarrow 3.7$ T
- Initial Acceptance a bit less than 2-D cooling channel
 - $\sim 10\%$
- Better match to downstream systems
 - from longitudinal cooling ...

Front End with Helical FOFO cooler preferred

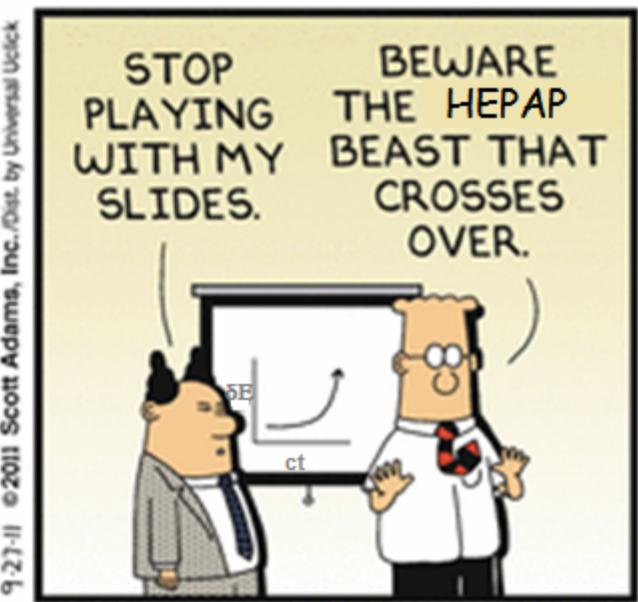
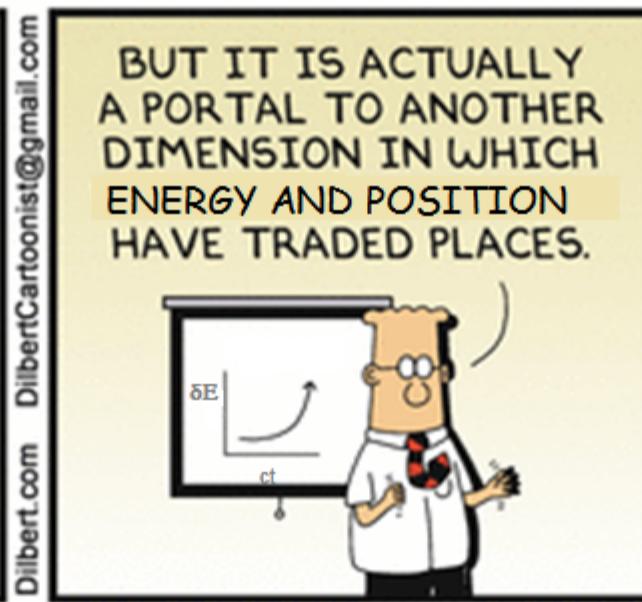
- **Smaller momentum spread bunches will fit into downstream components more easily**
 - Acceleration transition $325 \rightarrow 650$ MHz can occur earlier
 - at ~ 1 GeV/c for nu-Factory \rightarrow “NuMAX” scenario
 - Cooling transition $325 \rightarrow 650$ for collider sooner ...
 - losses reduced; separation of μ^+ and μ^- easier ...
- **Deceleration to a lower energy muon beam (mu2e?) easier, with fewer losses**

To Do

- Write-up current status for JINST volume
- Variations / Improvements -- ?
- Scale back to low-energy applications
 - smaller, lower field system capturing at 150 MeV/c
 - 50m → 25m
 - → 100 MeV/c
 - ~0.05 μ/p



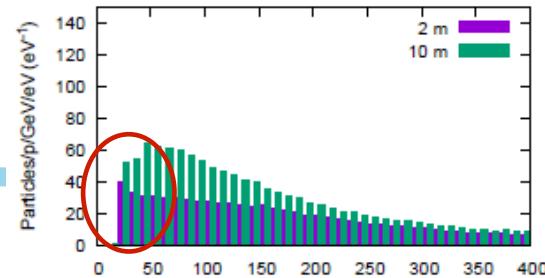
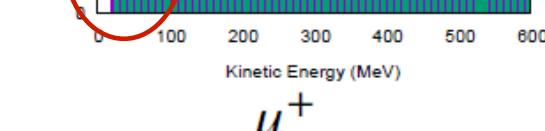
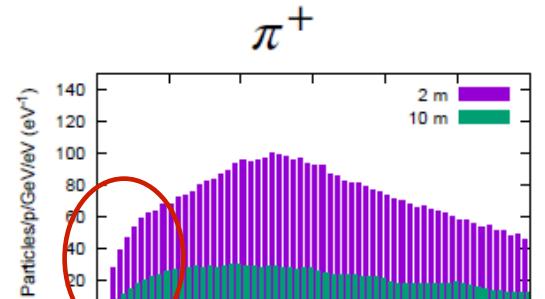
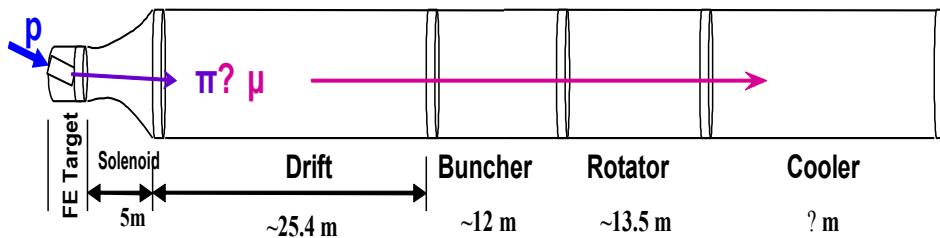
Summary



Backup slides

Low-E capture

- Capture at low momentum
 - prepare beam for low-E μ experiment
- Somewhat scaled back version of front end
 - 30.4m drift
 - shorter buncher /rotator
 - 12m / 13.5m
 - 0 → 15 MV/m, 15 MV/m
 - vacuum rf
 - $B=2T$
- Parameters
 - 150 MeV/c ... 100 MeV/c reference particles
 - 77.8 // 39.8 MeV
- Bunch to 150 MeV/c
- Cooling at 2T (1-D cooling)



simulation of low-E buncher

➤ Used Ding initial beam

- initial beam cut off at ~70 MeV/c
 - 21 MeV kinetic energy
- bunch train formed

