

Momentum Slip-Stacking Simulations for SPS Ion Beams with Collective Effects

D. Quartullo, T. Argyropoulos, A. Lasheen

Acknowledgements:

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K. Iliakis, J. Repond and G. Rumolo*



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- Motivation
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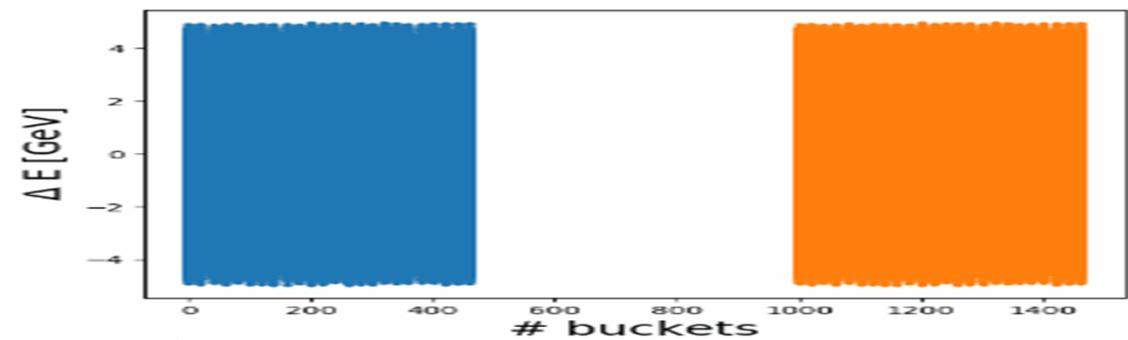


Motivation

- The HL-LHC requirement for ion beams is to double the peak luminosity after LIU Upgrade [1] increasing the number of bunches in the LHC
- The LIU baseline to achieve that is to decrease bunch spacing from 100 ns to 50 ns in SPS through slip-stacking (already used at Fermilab to double beam intensity [2])

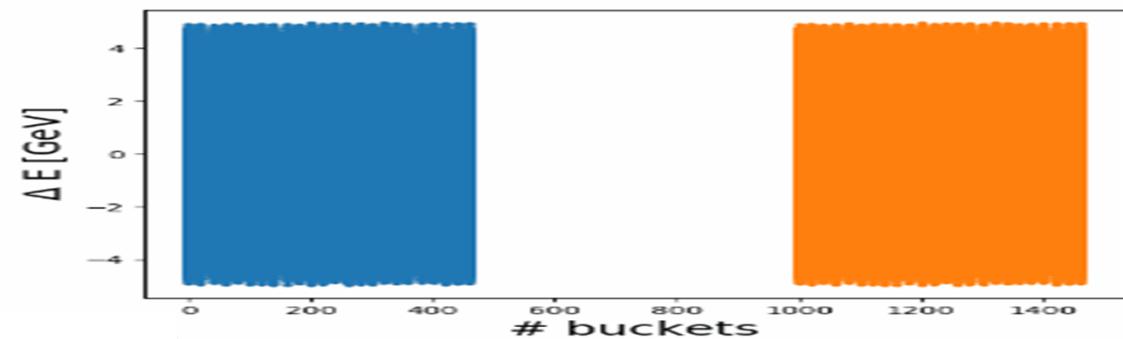
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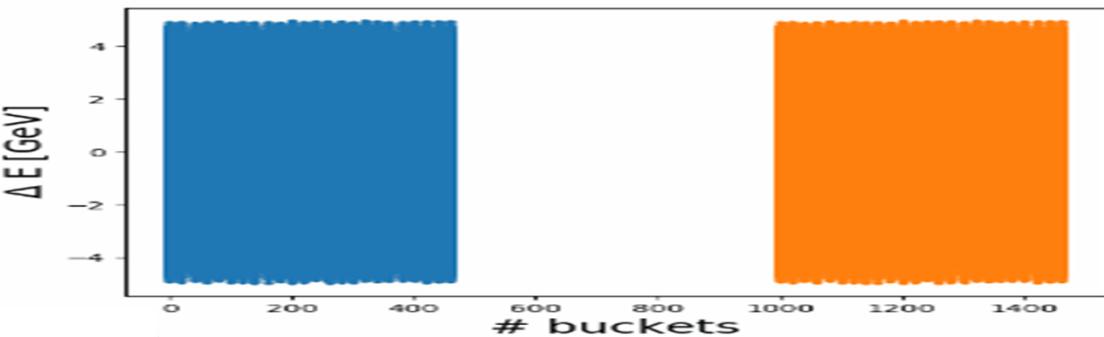
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In longitudinal phase space two batches are interleaved using two independent RF systems.

- In SPS slip-stacking can be tested only after Upgrade
 - Low Level RF of the 200 MHz RF system has to be upgraded
- Therefore simulations are the only means to check slip-stacking feasibility (see also [3])
- For the first time simulations (with the CERN BLonD code [4]) have been done using:
 - Full SPS longitudinal impedance model
 - Measured beam parameters
 - Optimization with respect to the most significant parameters involved

Slip-stacking principle

Fundamental
equations for slip-
stacking dynamics
(at constant
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$$\frac{\Delta f_{rf}}{f_{rf,0}} = -\eta_0 \frac{\Delta p}{p_0}$$

$$\frac{\Delta p}{p_0} = \gamma_{tr}^2 \frac{\Delta R}{R_0}$$

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Moving one bunch

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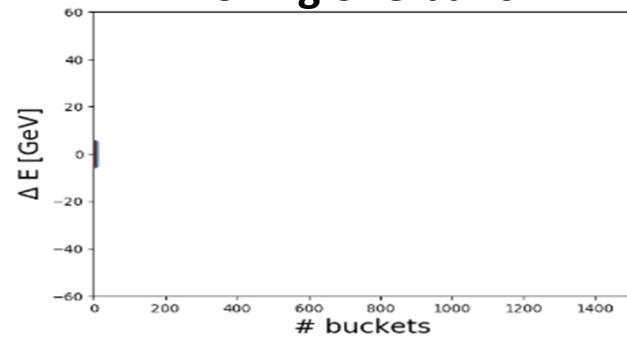
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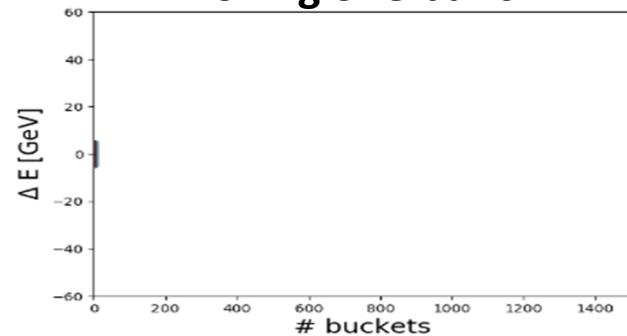
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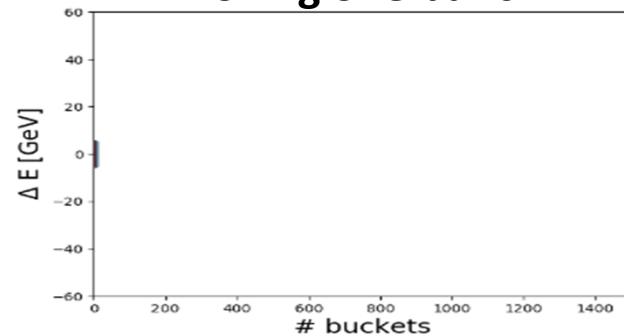
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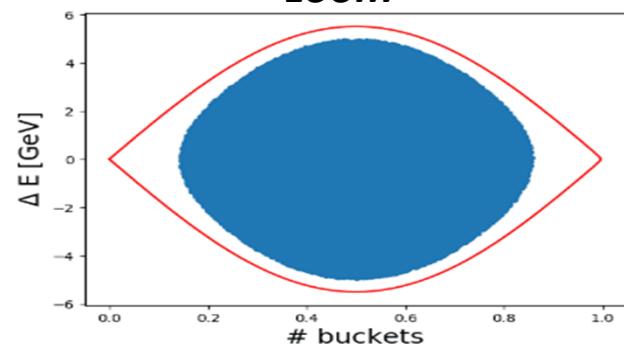
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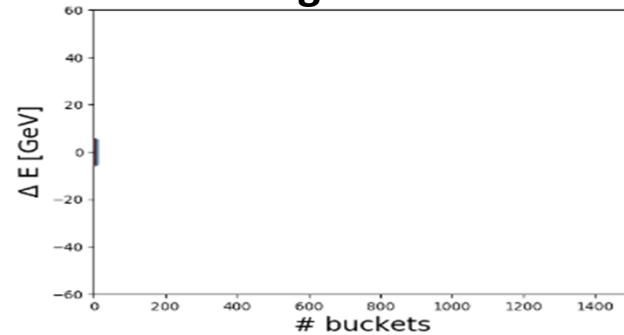
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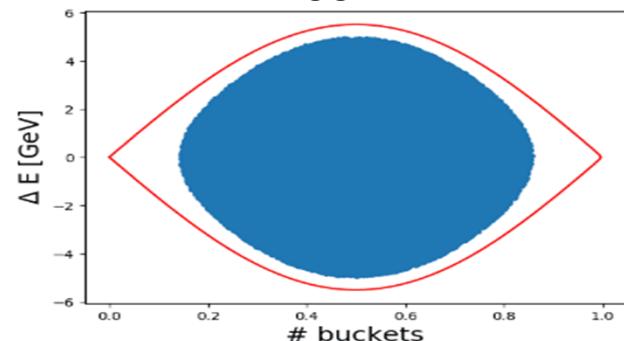
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zoom



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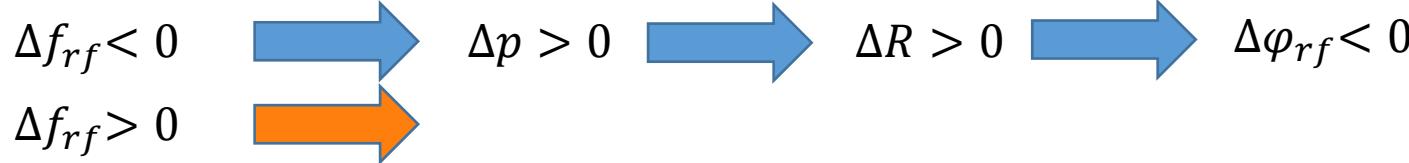
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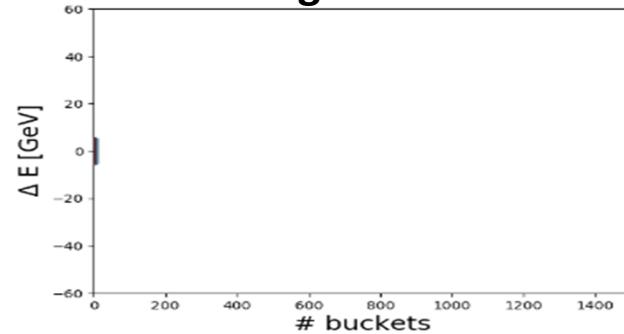
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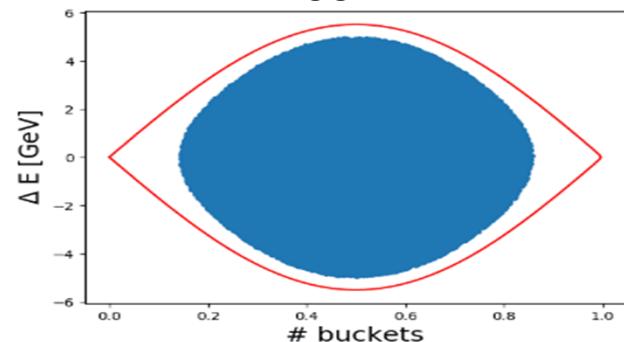
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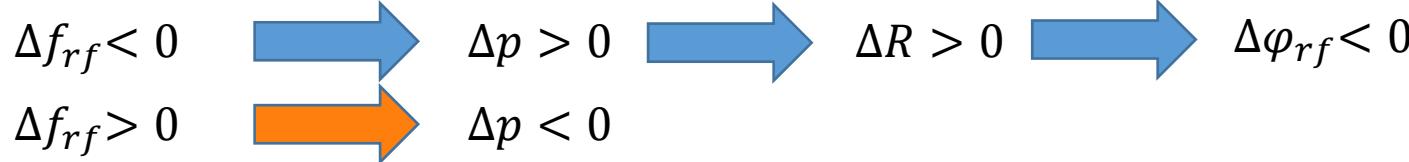
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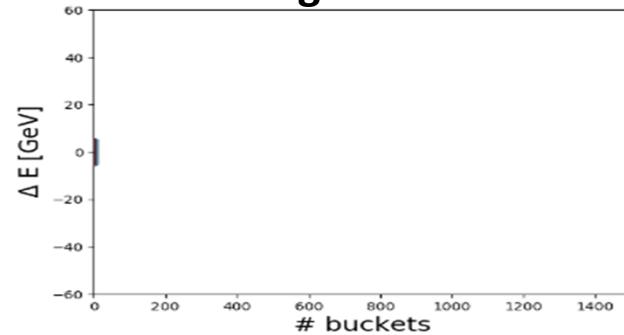
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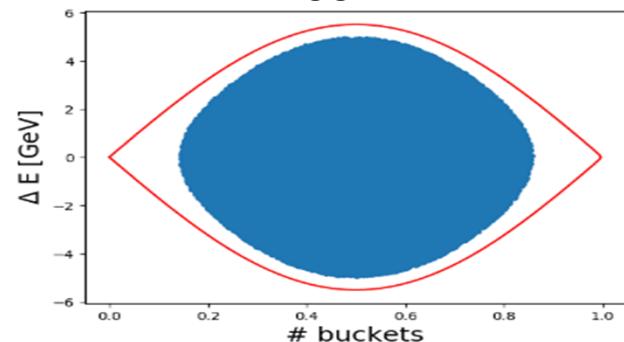
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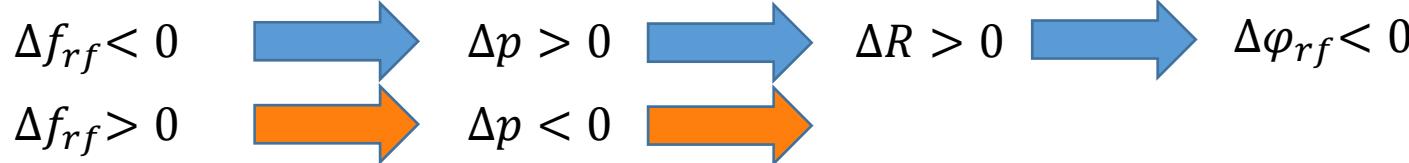
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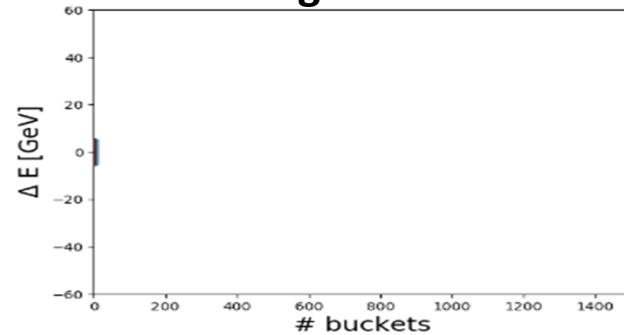
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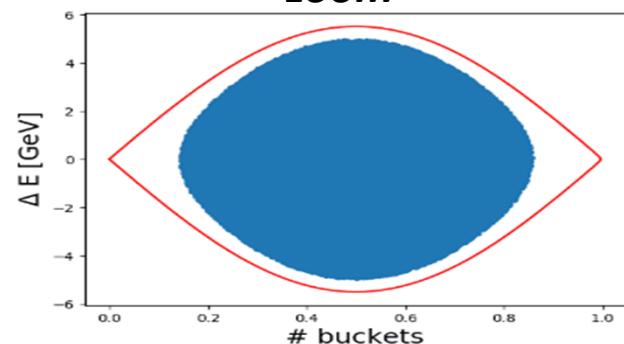
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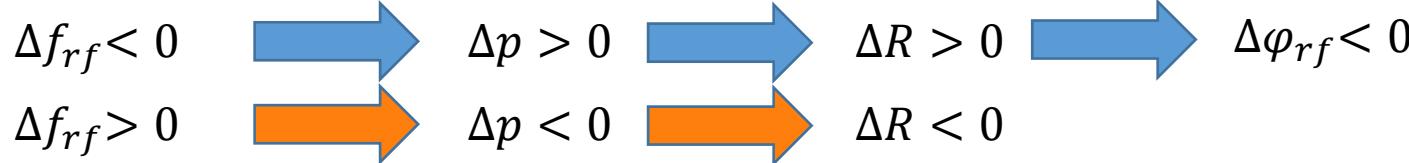
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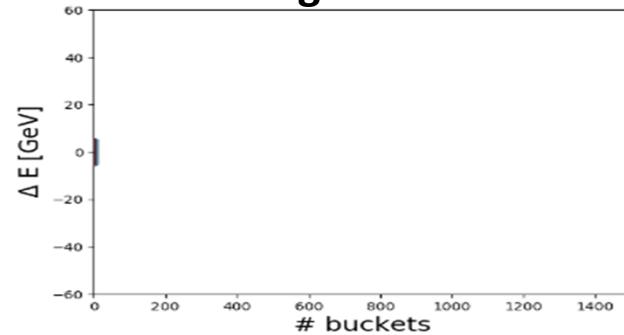
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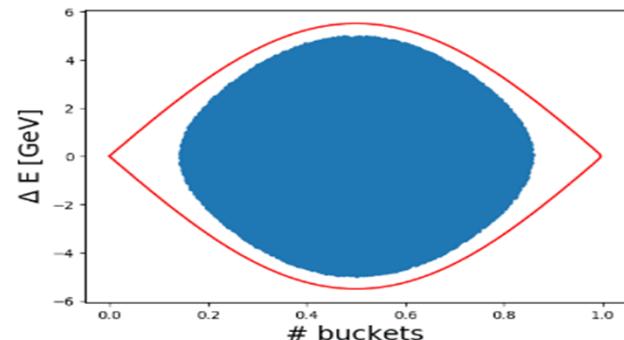
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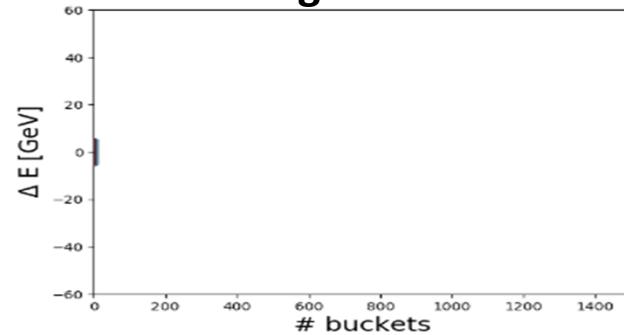
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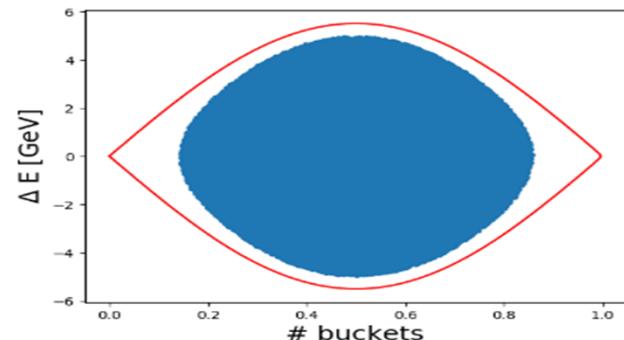
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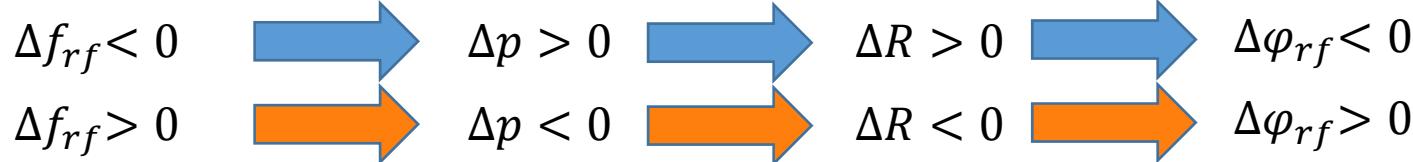
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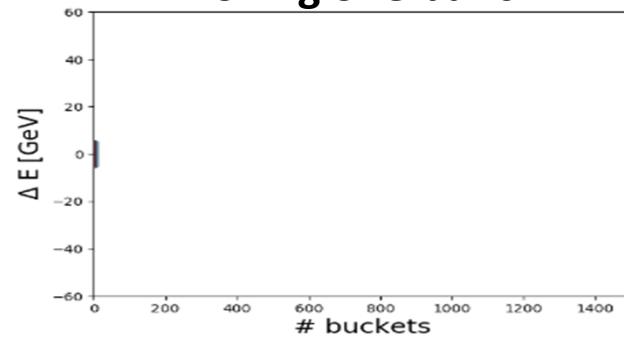
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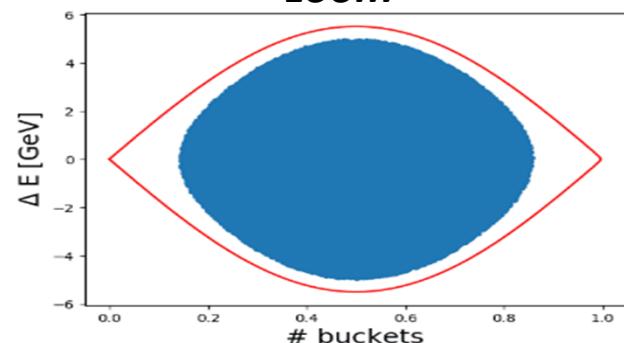
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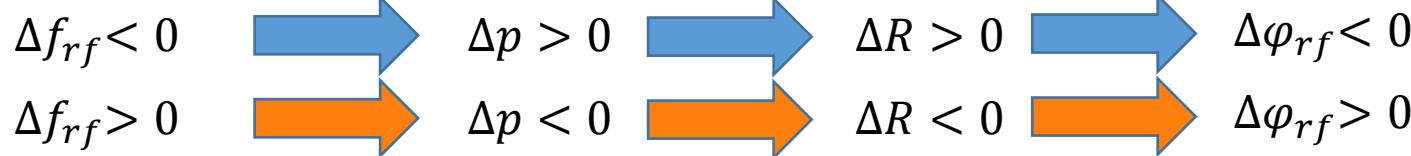
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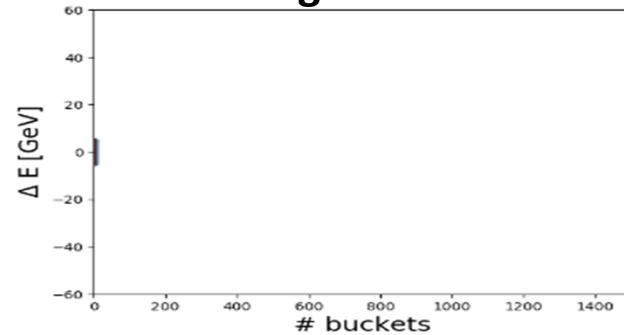
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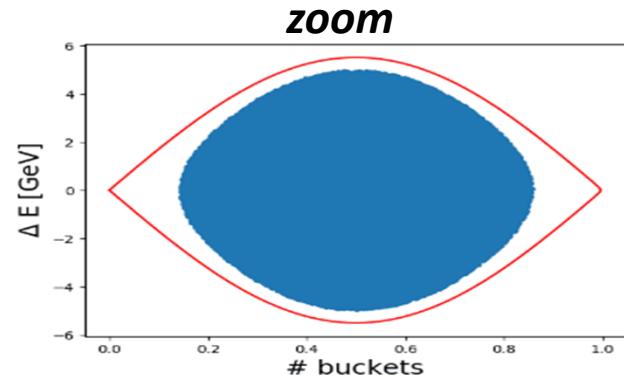
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Moving one bunch



Bringing closer two bunches



Slip-stacking principle

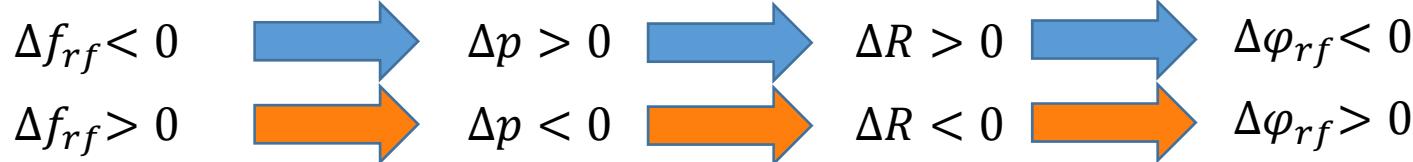
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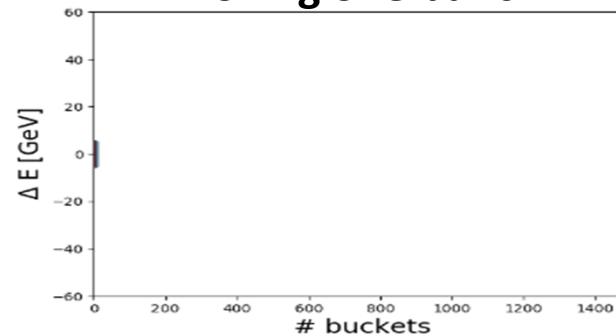
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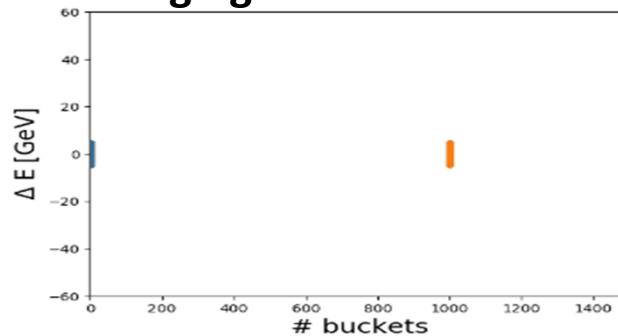
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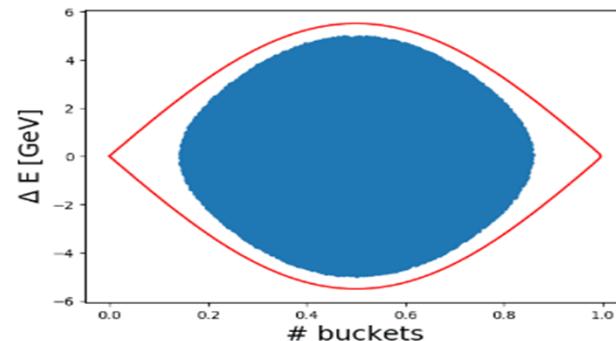
Moving one bunch



Bringing closer two bunches



zoom



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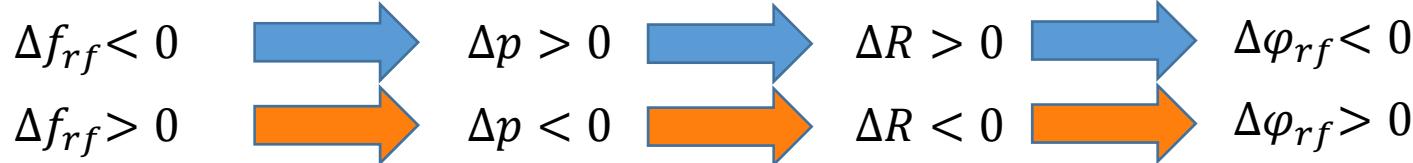
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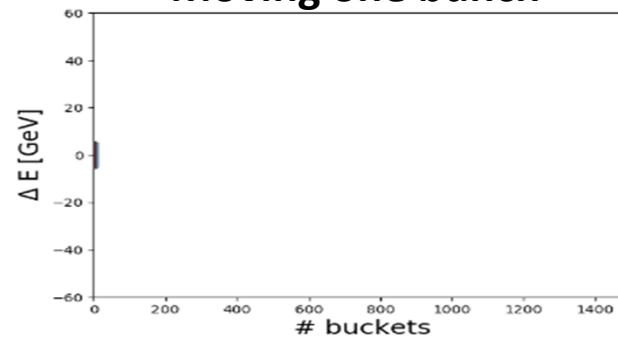
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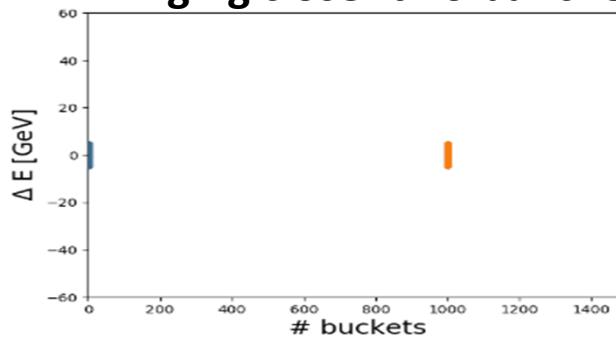
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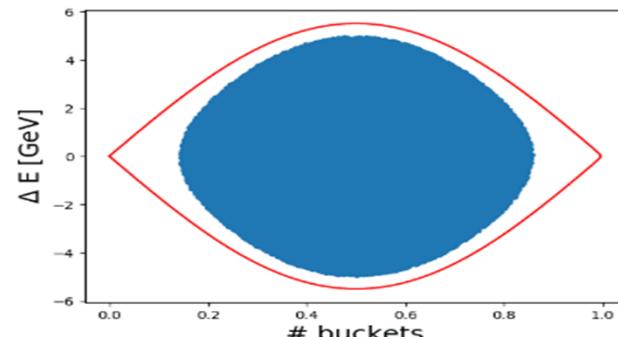
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Bringing closer two bunches



zoom



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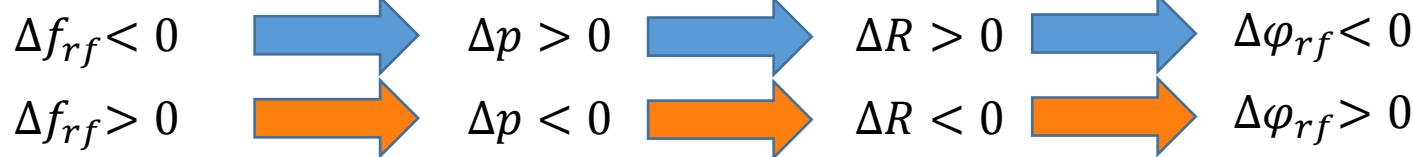
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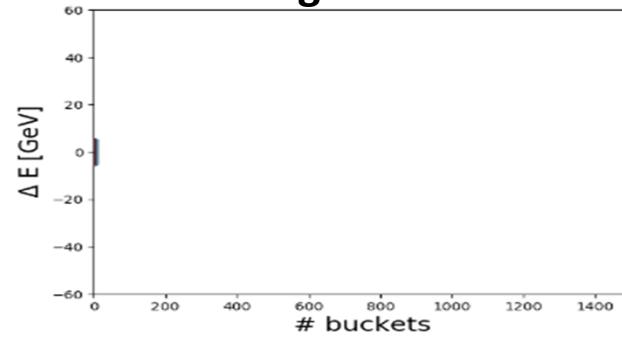
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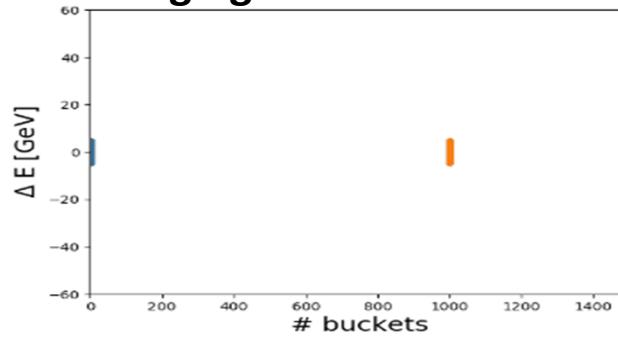
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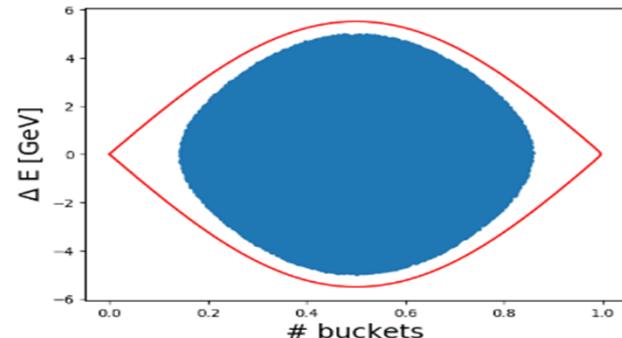
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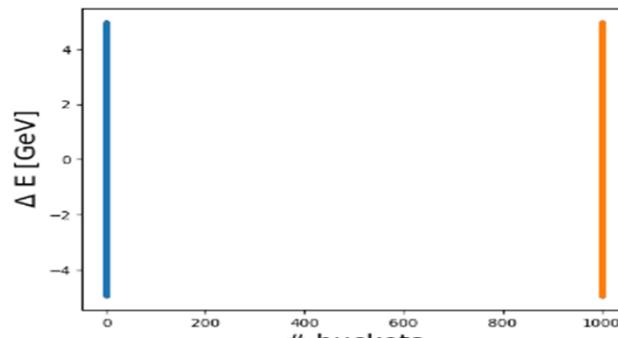
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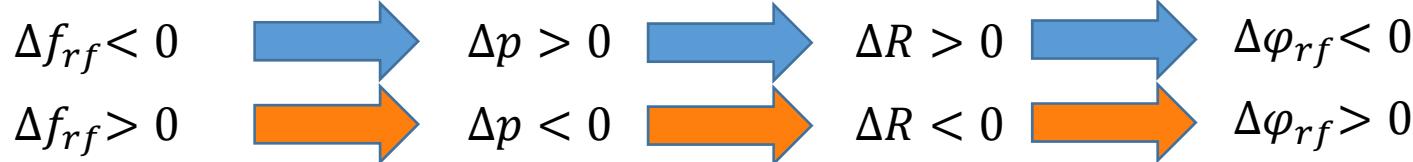
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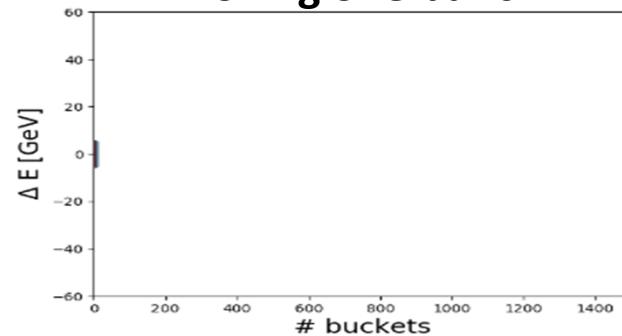
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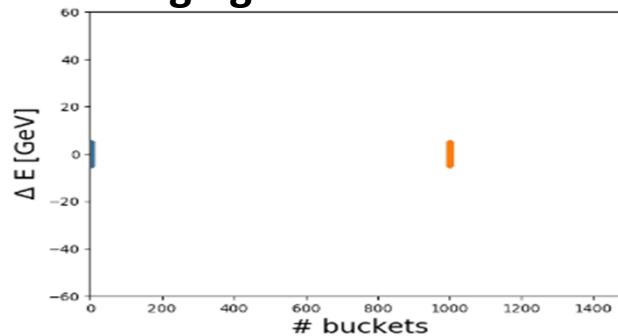
Examples above transition ($\eta_0 > 0$)



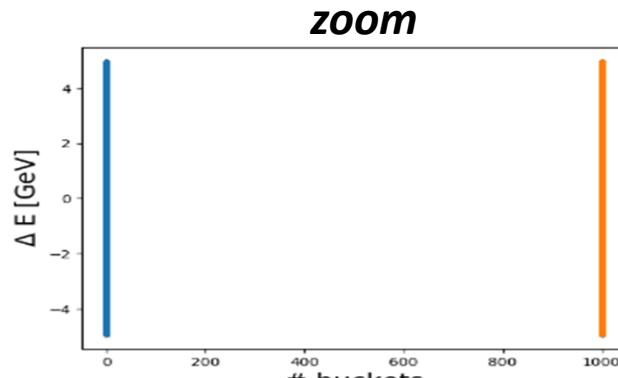
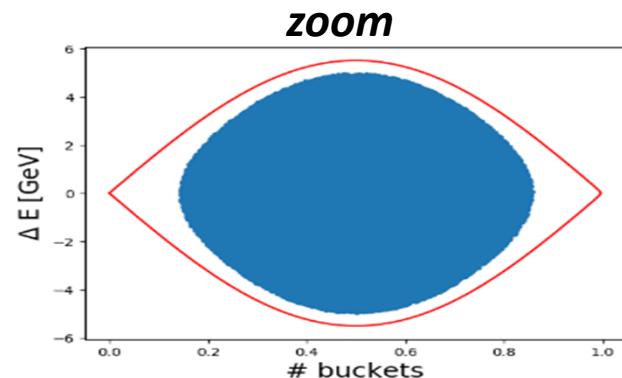
Moving one bunch



Bringing closer two bunches



Interleaving two batches



Slip-stacking principle

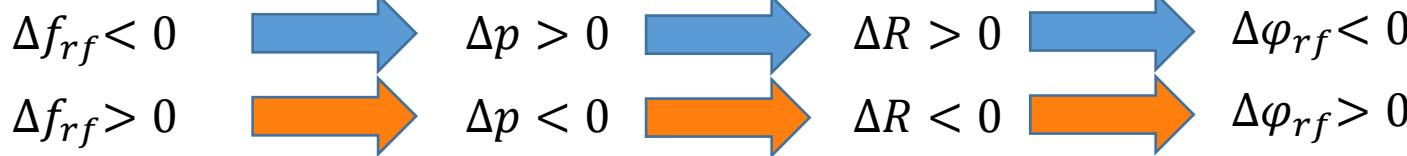
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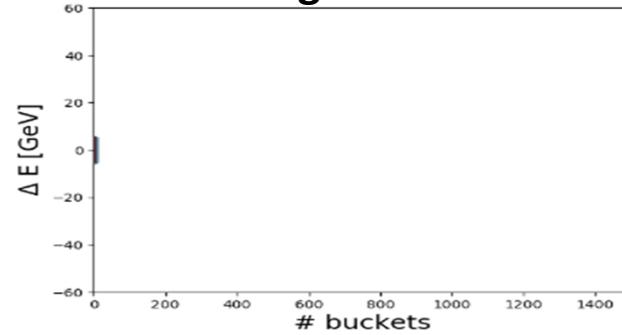
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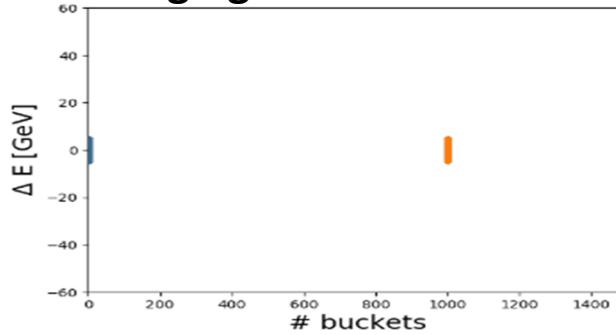
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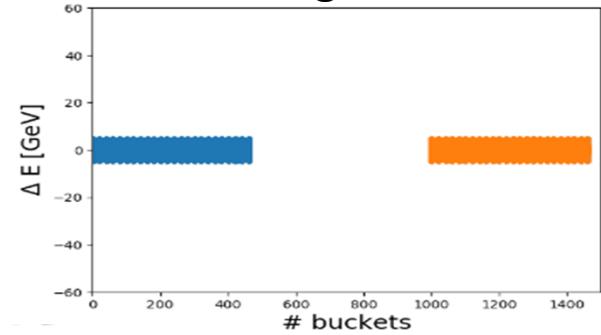
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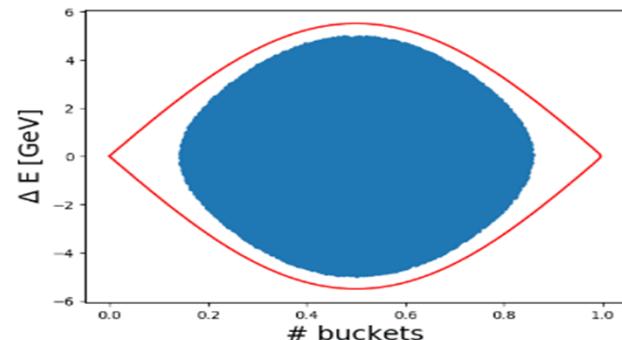
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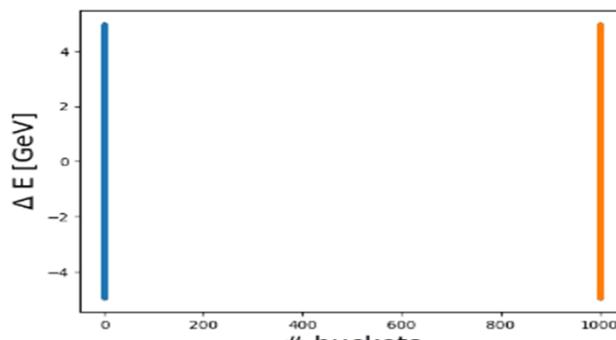
Interleaving two batches



zoom



zoom



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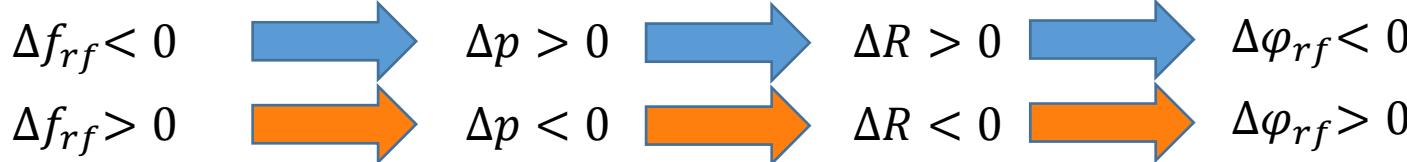
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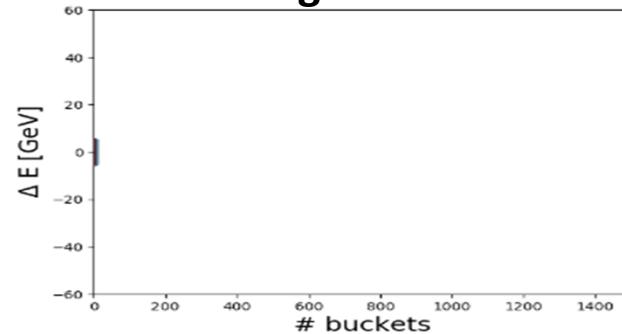
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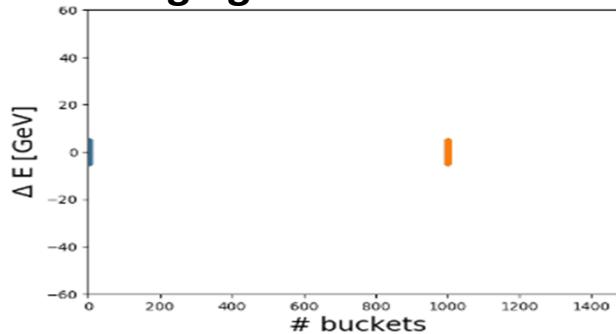
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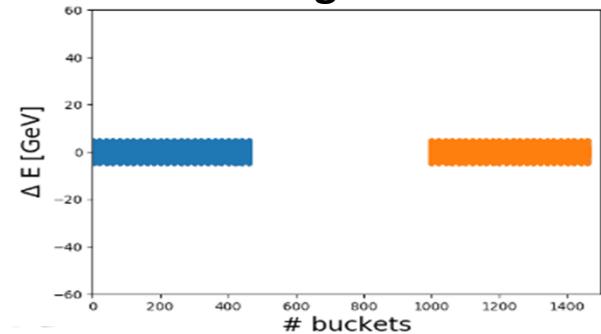
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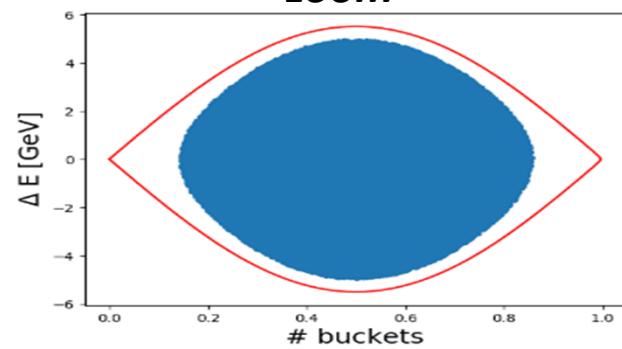
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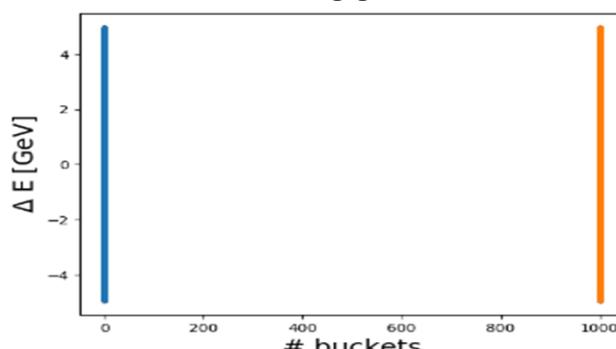
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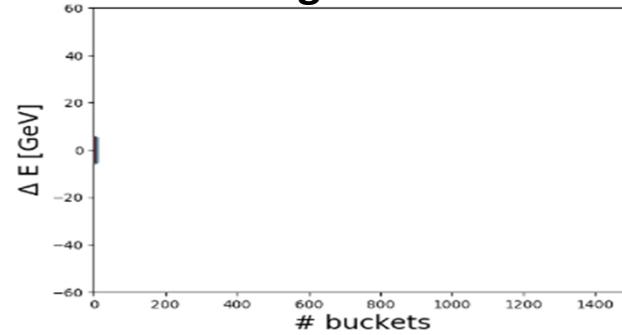
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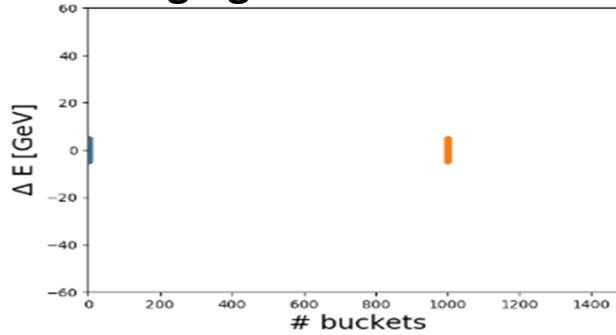
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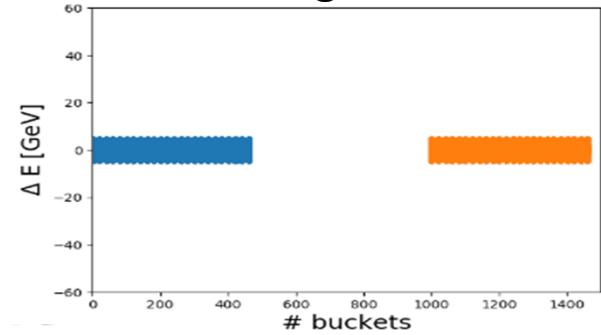
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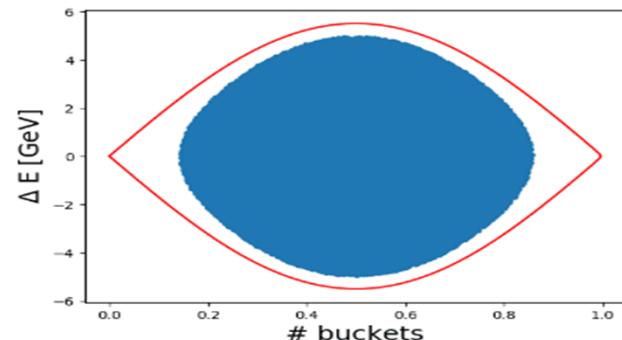
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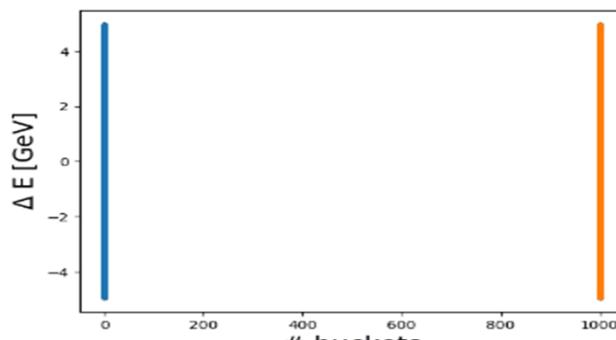
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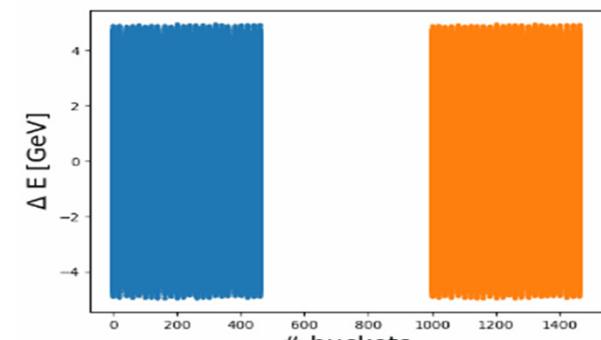
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Core synchrotron frequency and bucket half height
- It has been proven [5] that a lower limit for stable motion is defined by $\alpha = 4$

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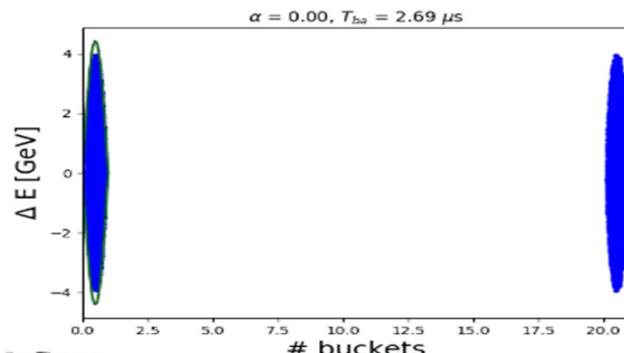
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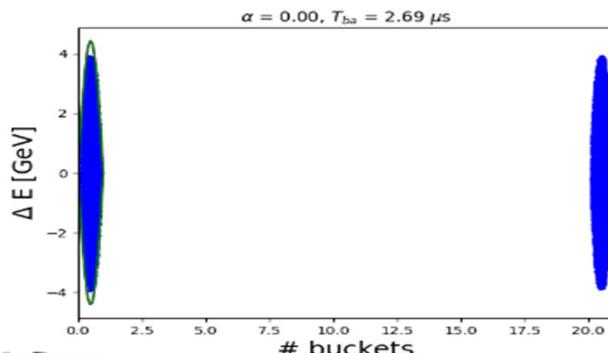
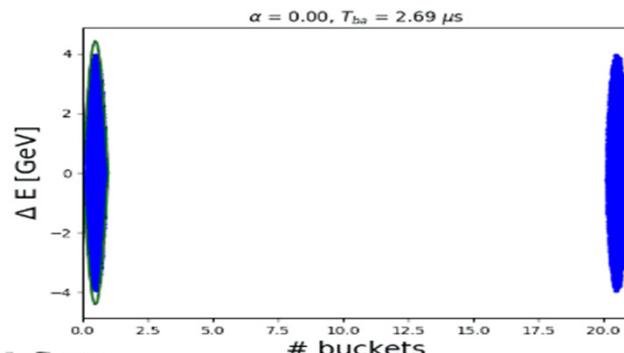
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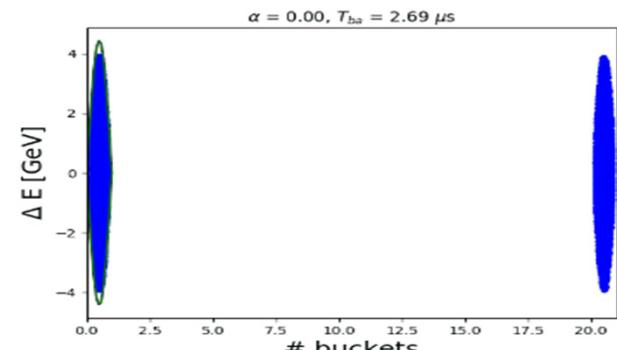
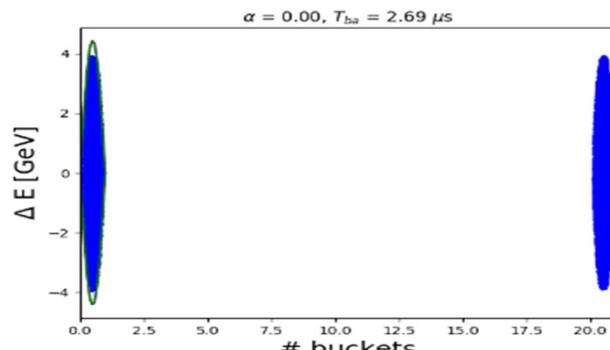
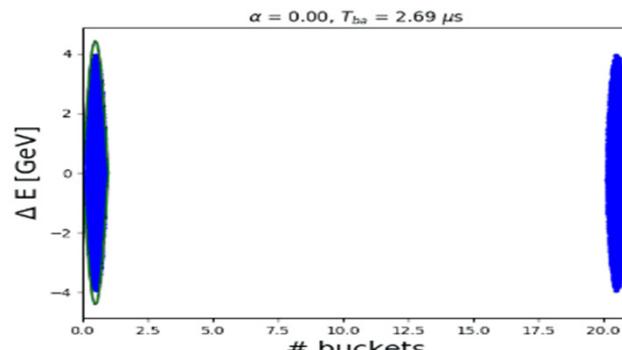
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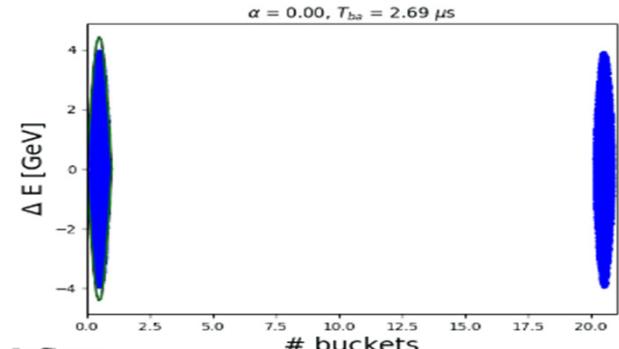
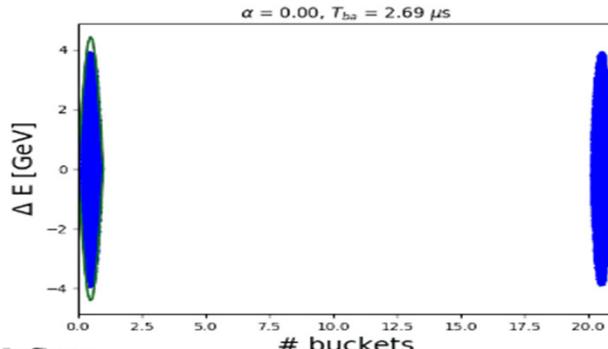
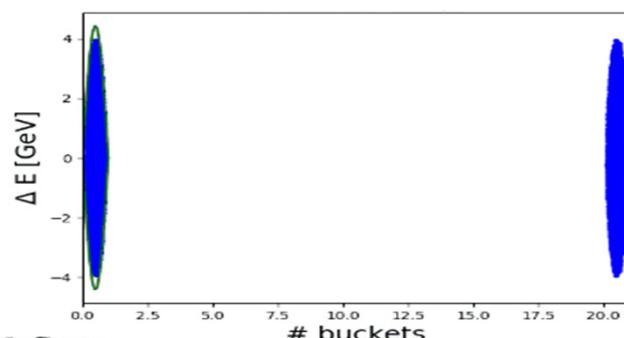
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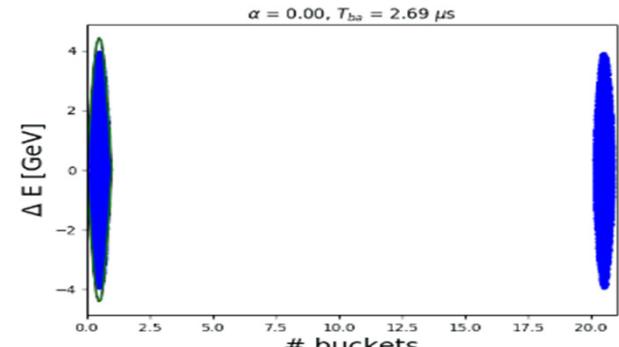
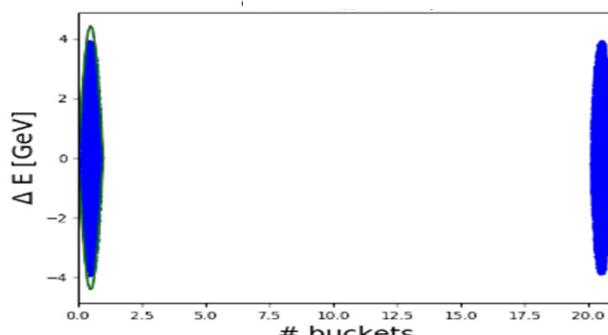
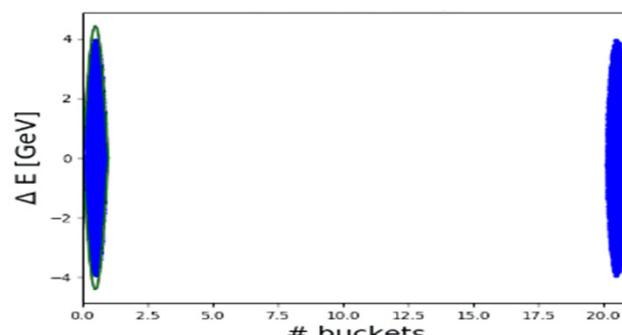
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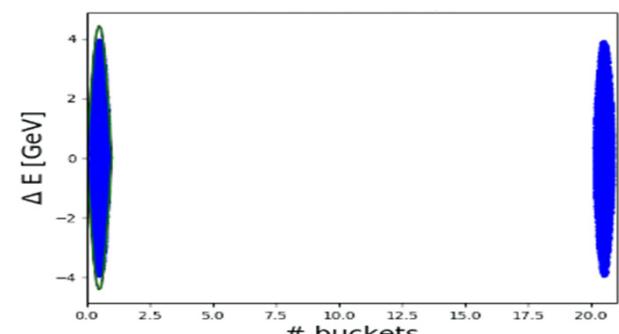
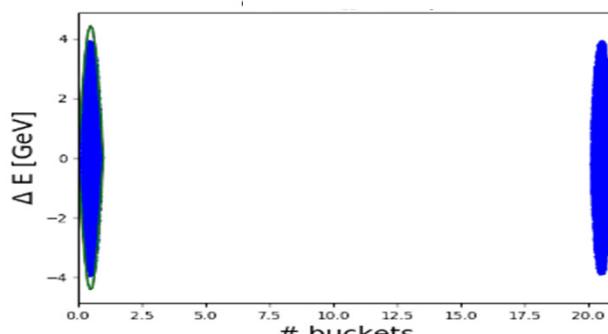
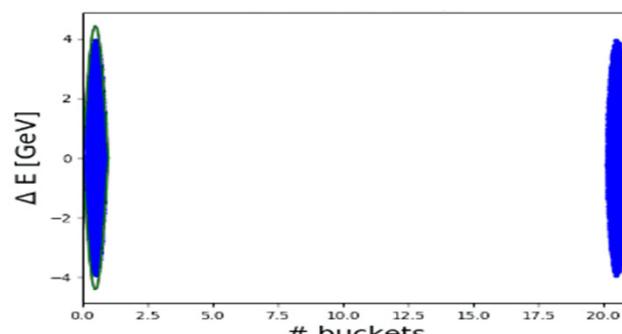
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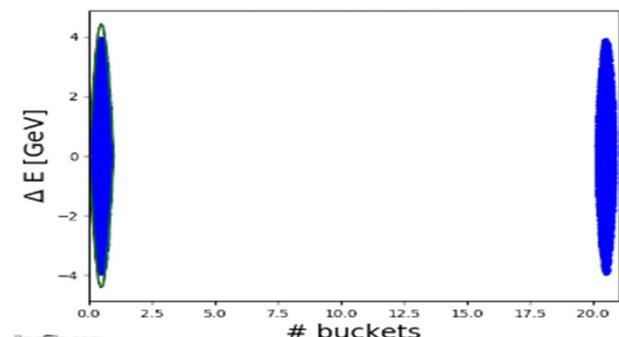
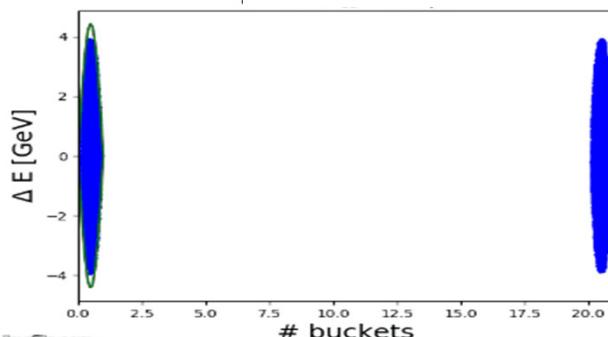
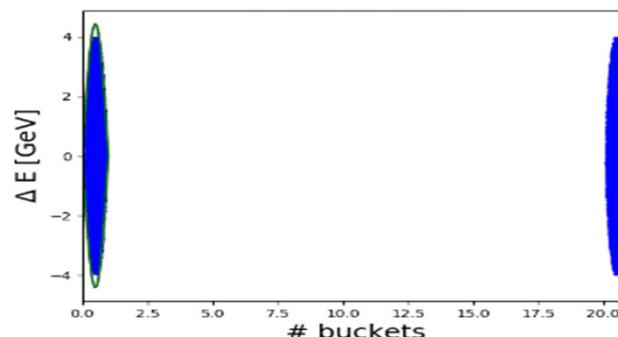
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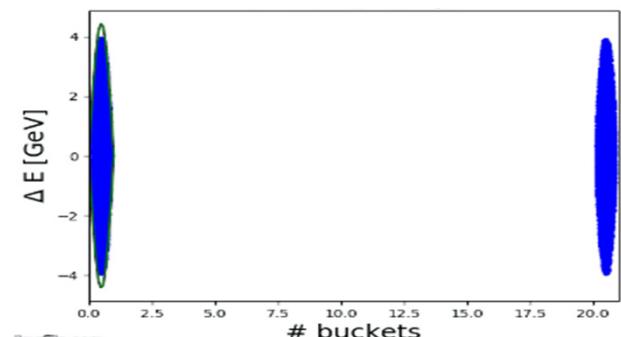
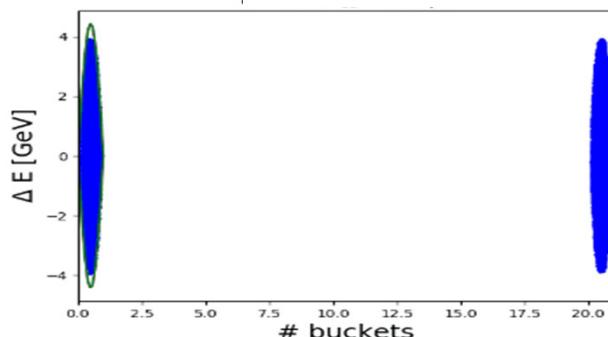
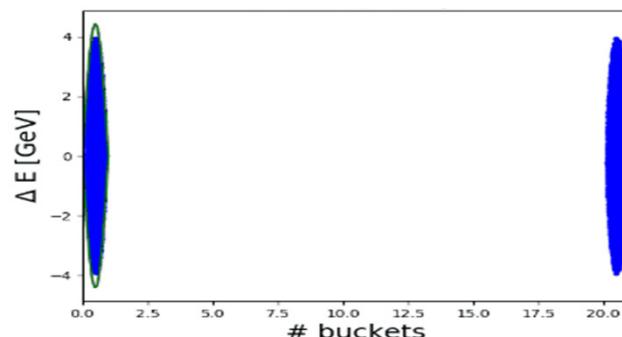
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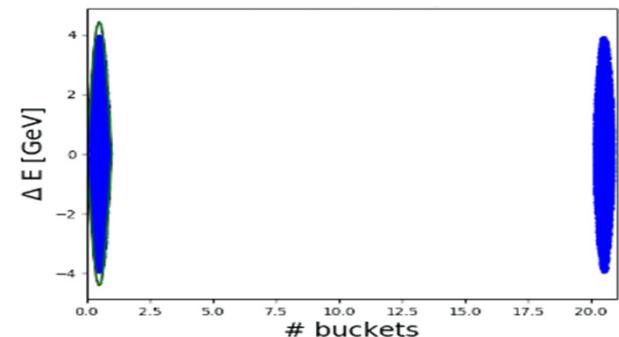
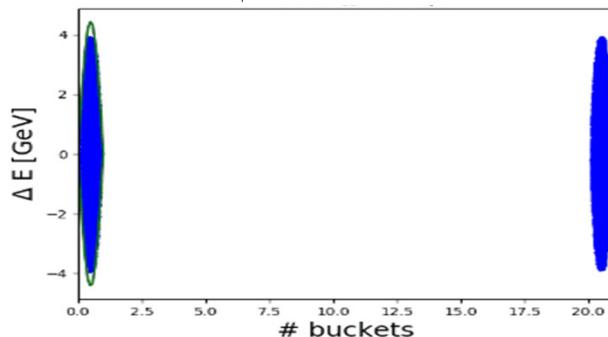
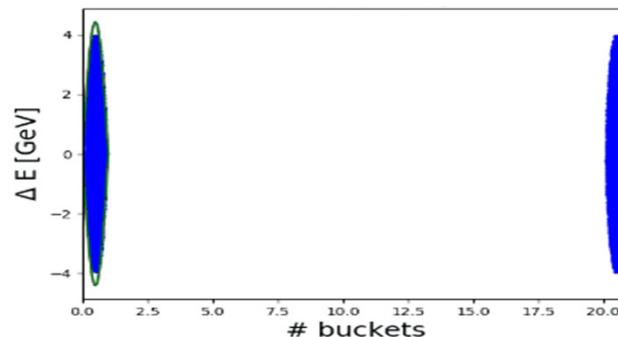
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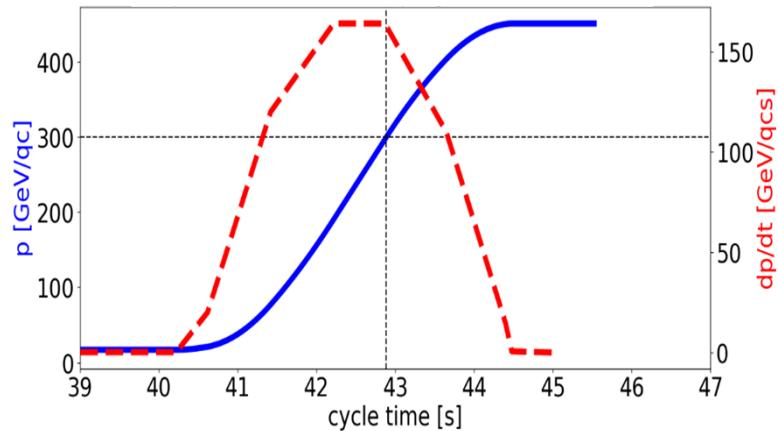
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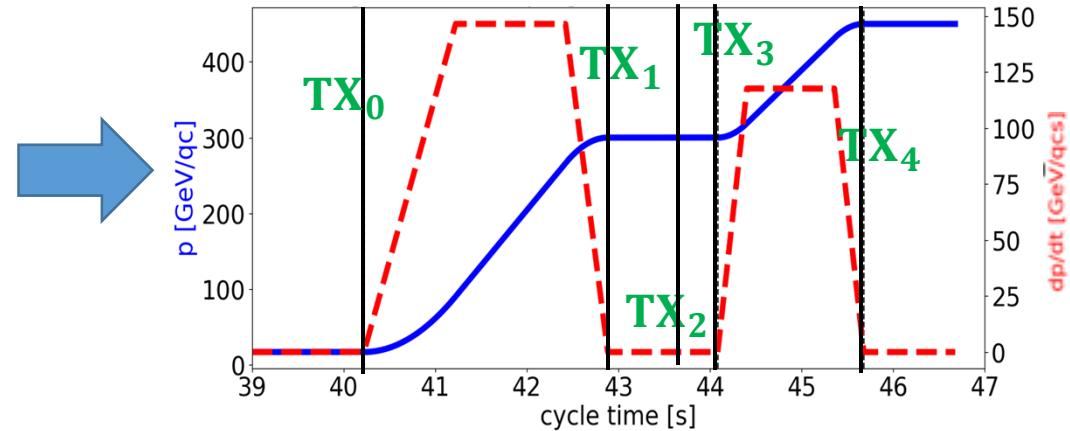
Slip-stacking energy in SPS

- At which energy should slip-stacking be performed?
 - Flat bottom: strong space charge effects, IBS and RF noise (observed during operation)
 - Flat top: uncaptured beam is transferred to the LHC and lowest instability threshold
 - **Intermediate energy plateau**: good compromise (the energy 300 GeV/qc is chosen)
- Only multiples of 1.2 s (PSB cycle length) can be added to the SPS cycle for slip-stacking
 - 1.2 s are added at 300 GeV/c (0.8 s for slip-stacking and 0.4 s for filamentation after recapture)

Operational momentum program and derivative



Momentum program with slip-stacking and derivative



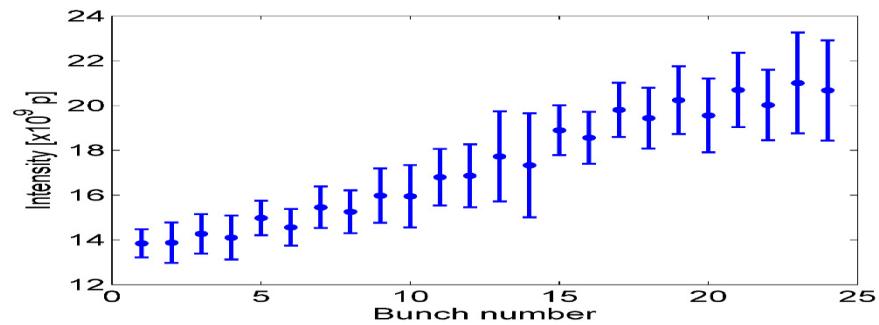
- Simulations started at TX_1 (beginning of slip-stacking)

U

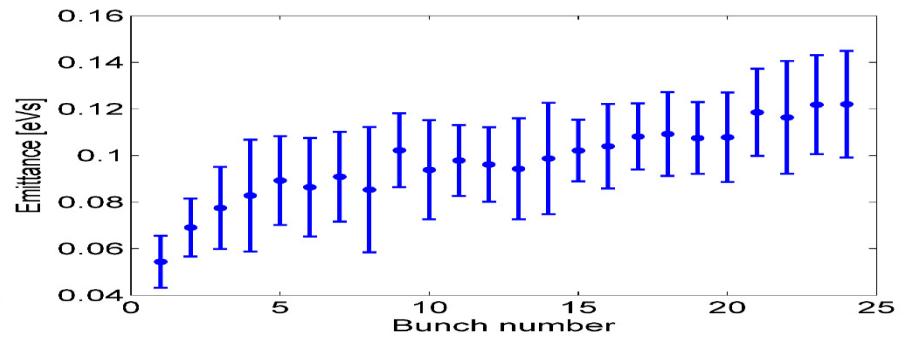
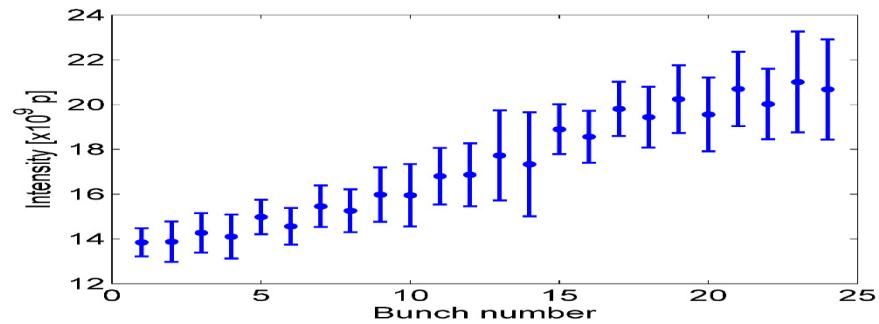


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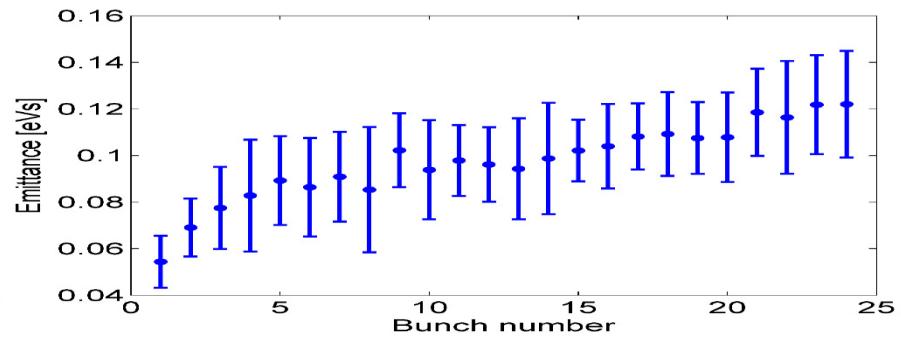
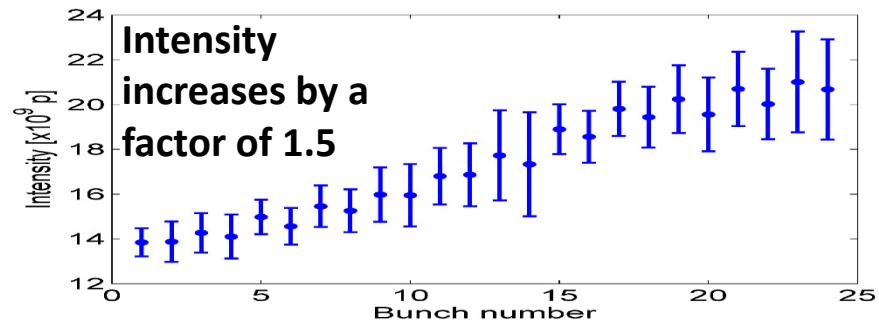
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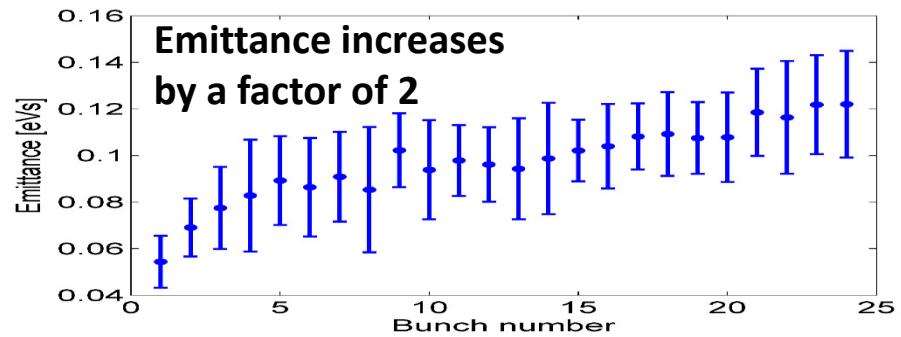
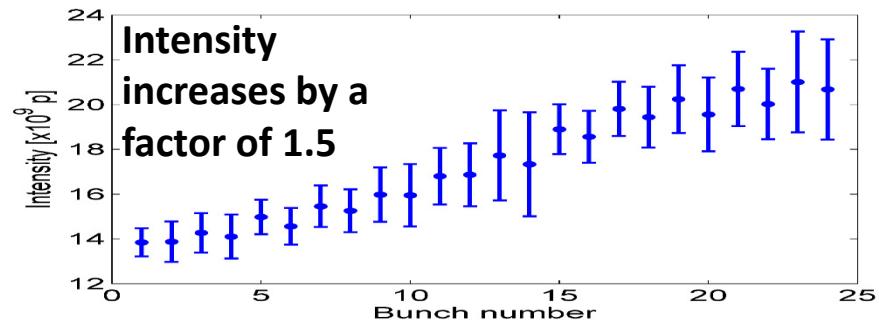
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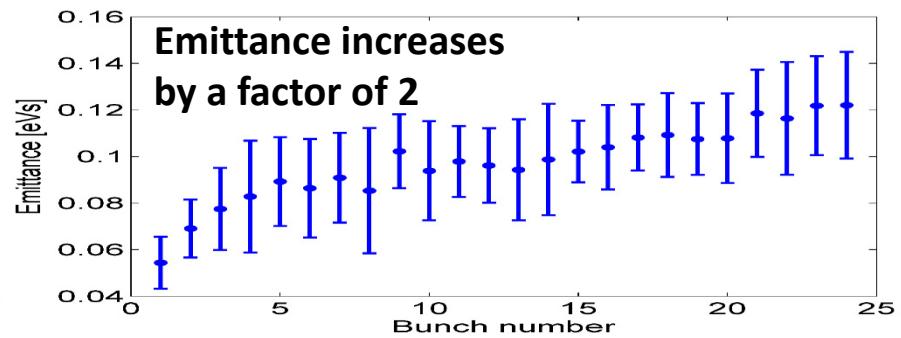
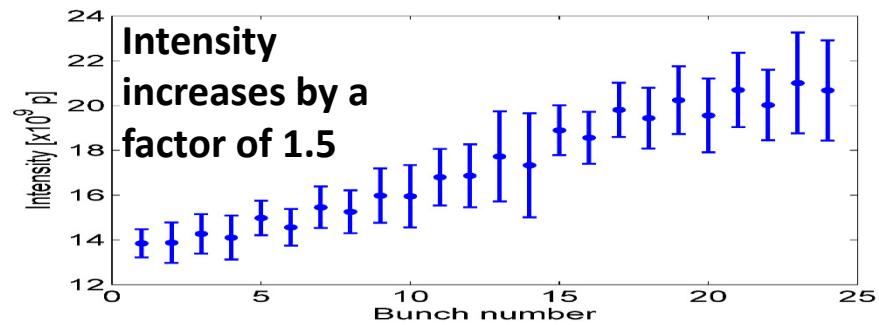


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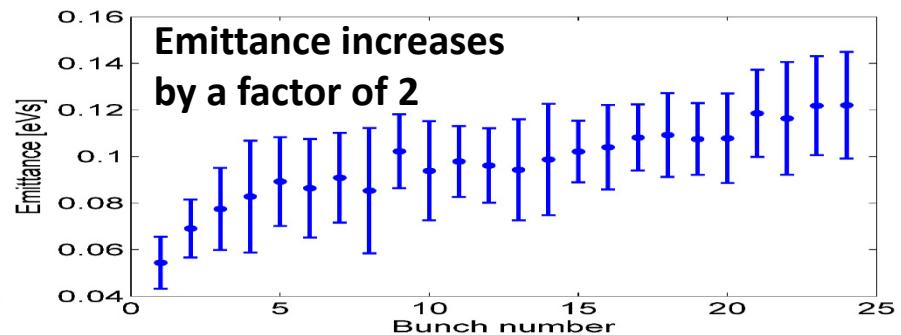
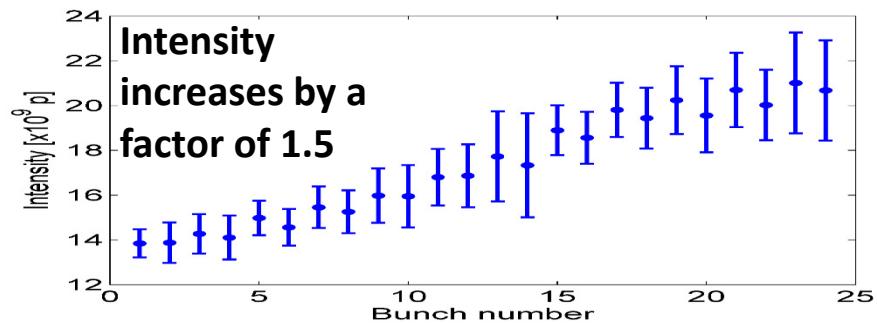
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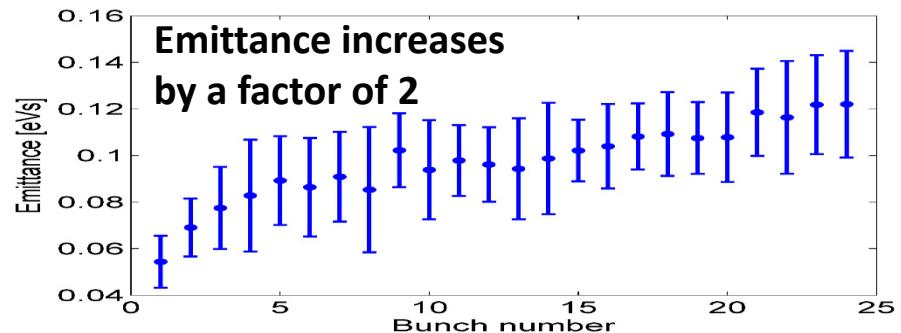
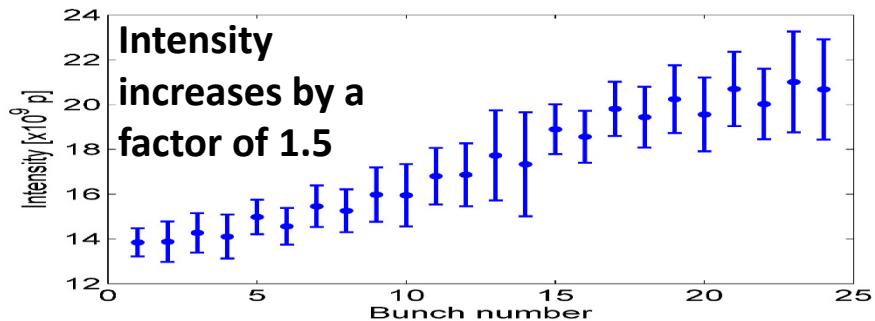
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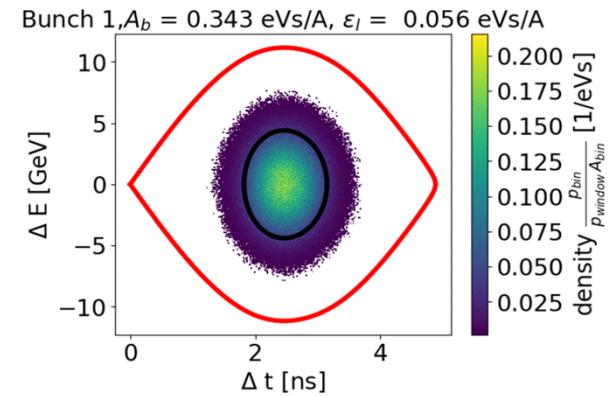
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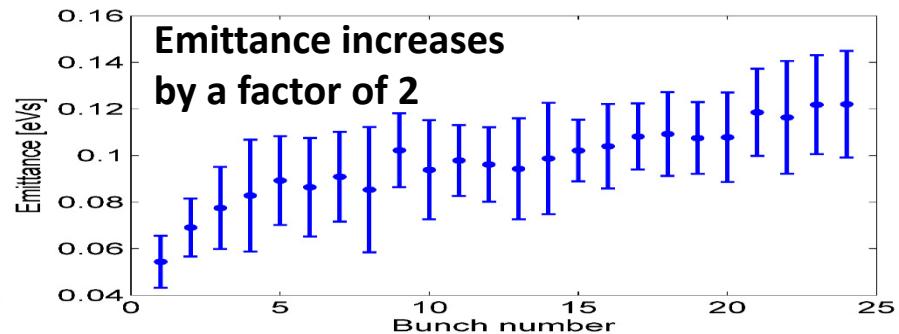
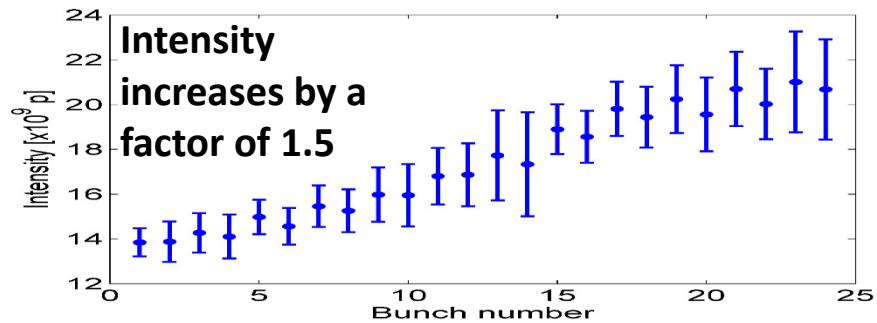


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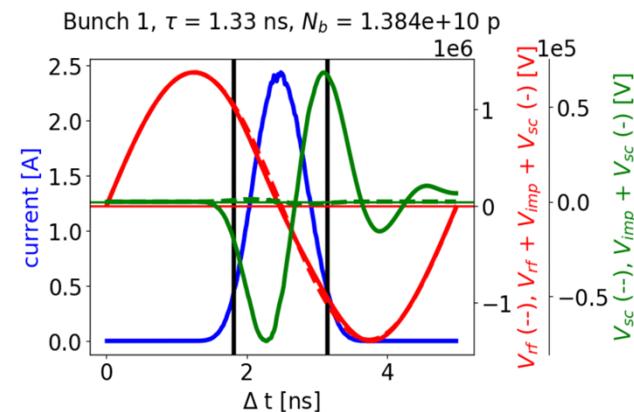
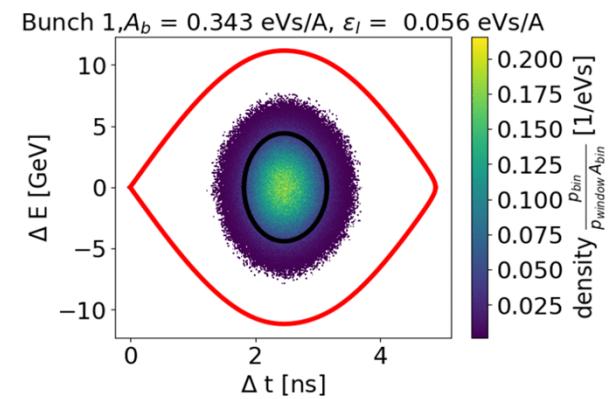


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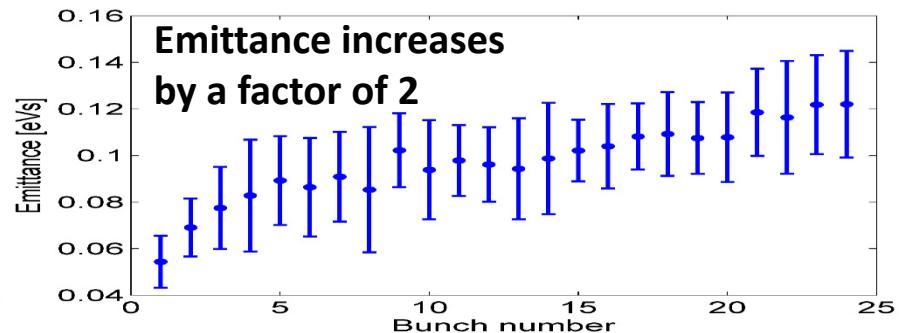
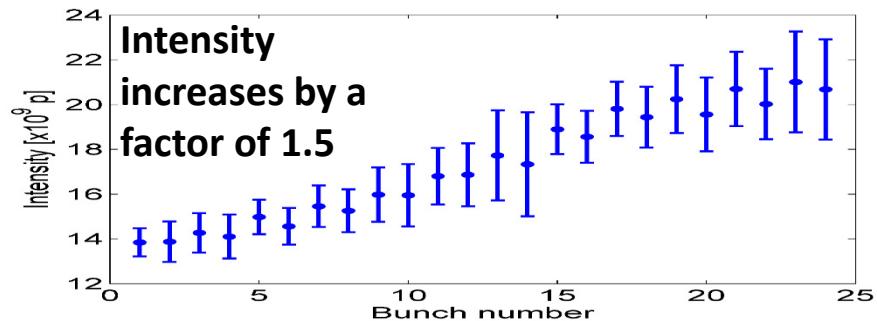


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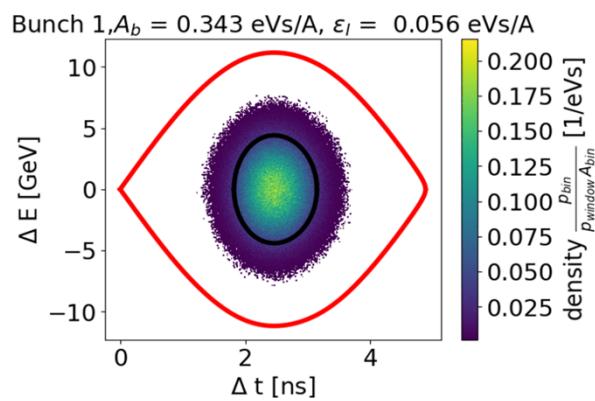


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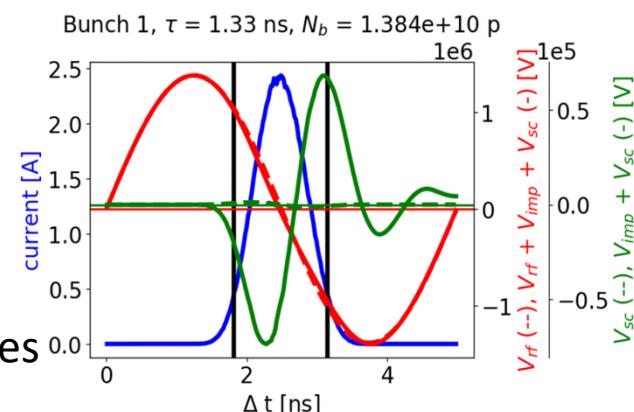


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EXAMPLE

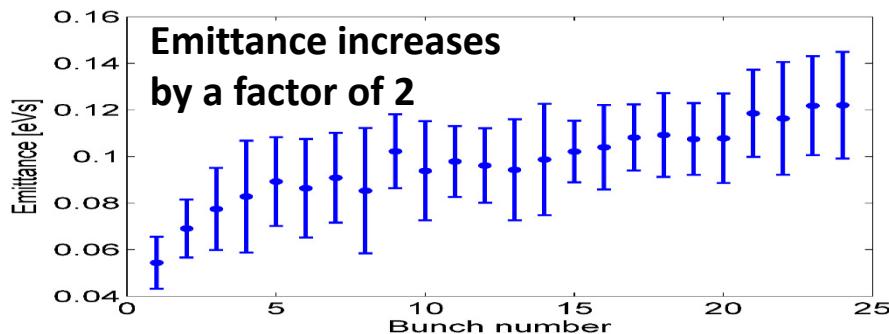
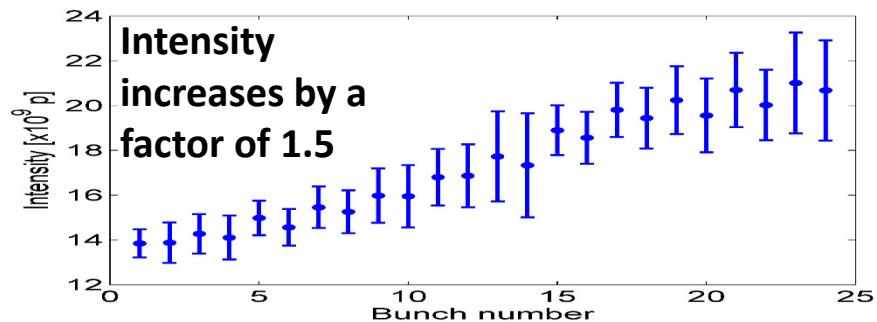
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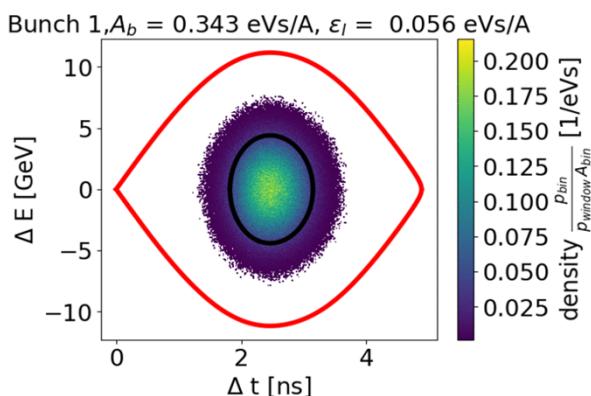
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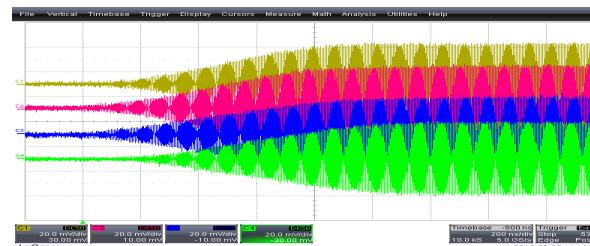
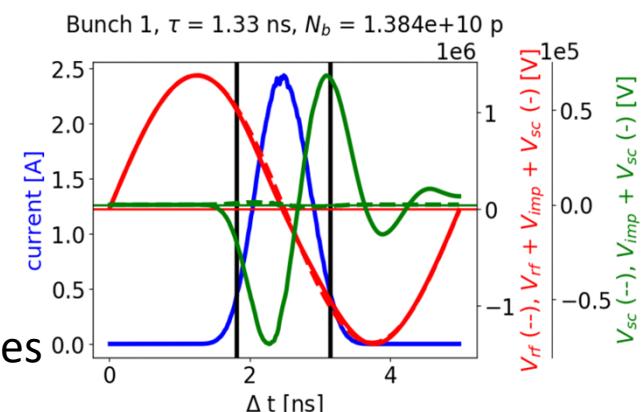


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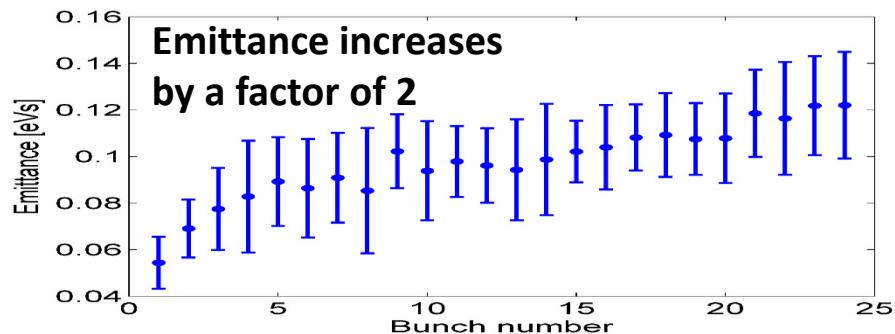
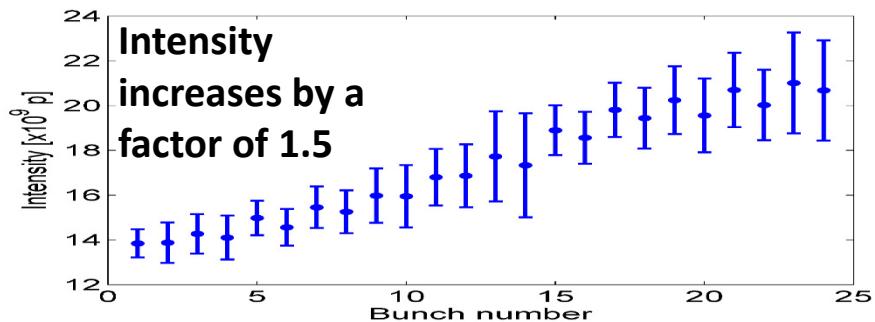
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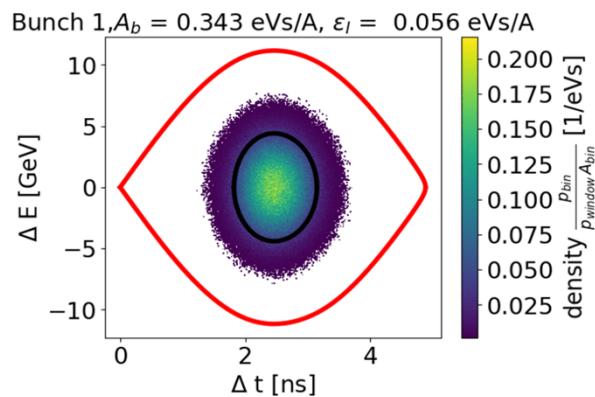


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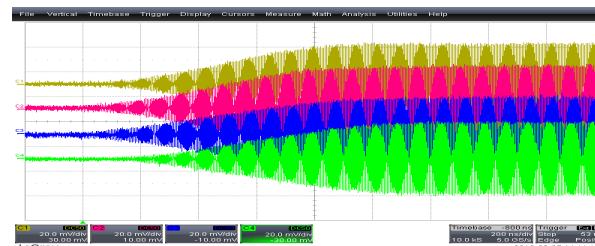
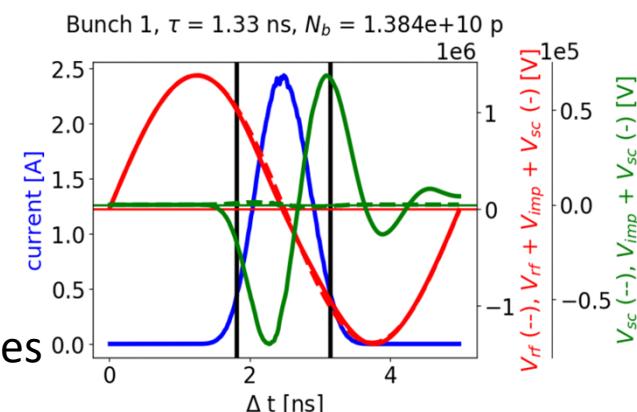


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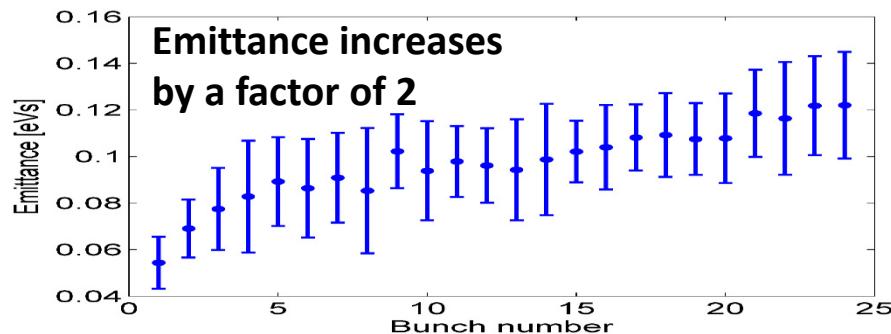
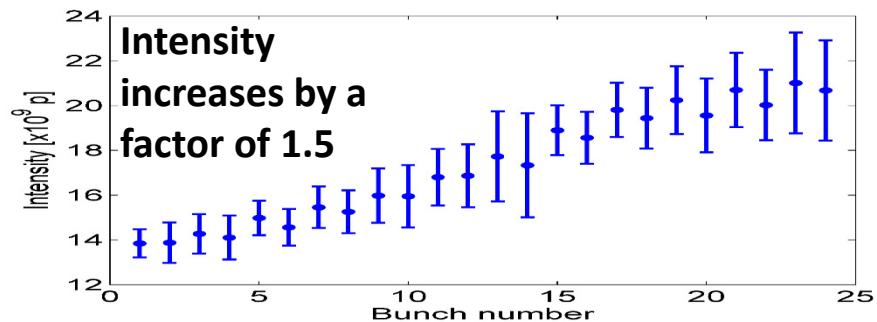


Measurements of cavity voltage rise during batch passage (courtesy T. Bohl)

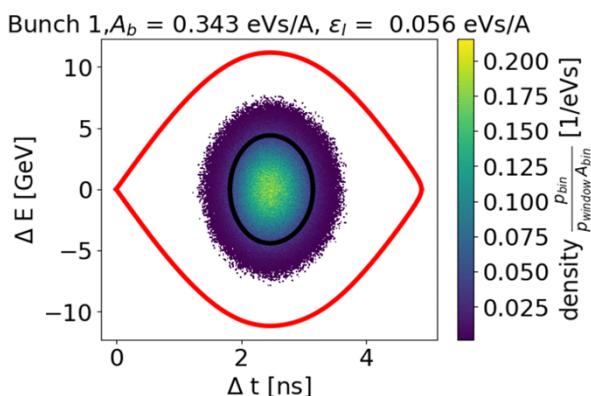
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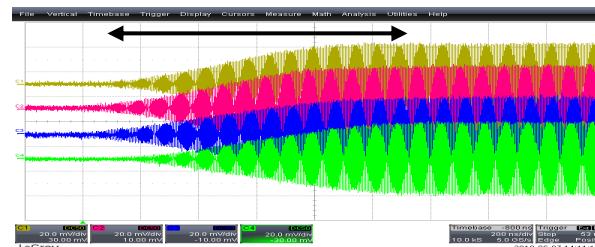
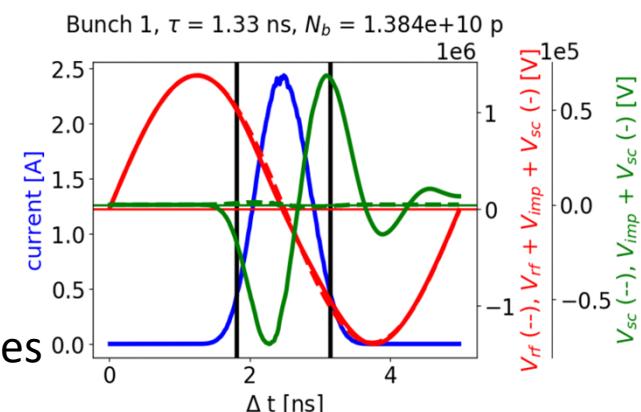


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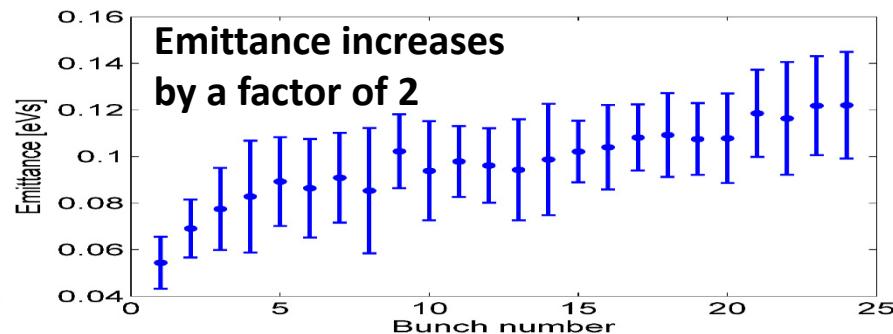
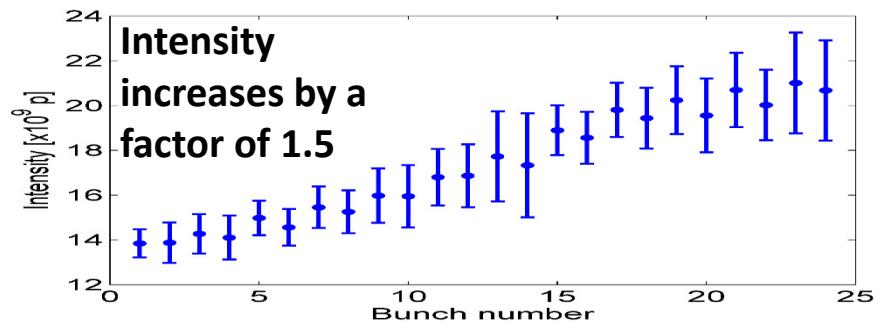


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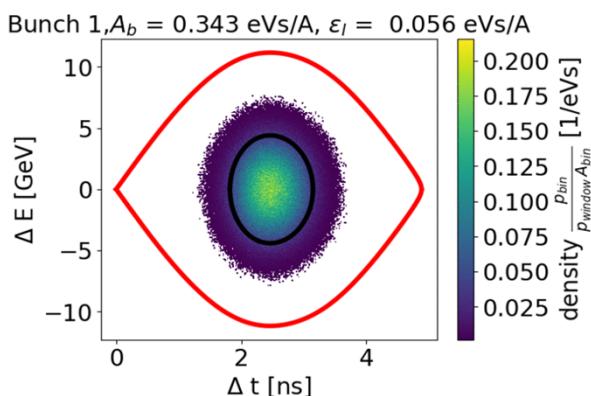
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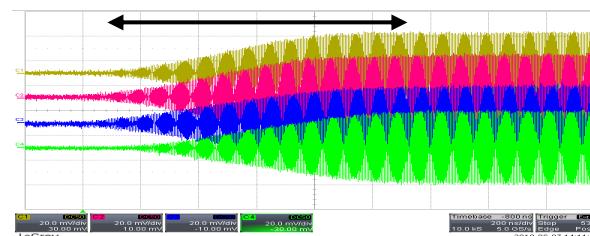
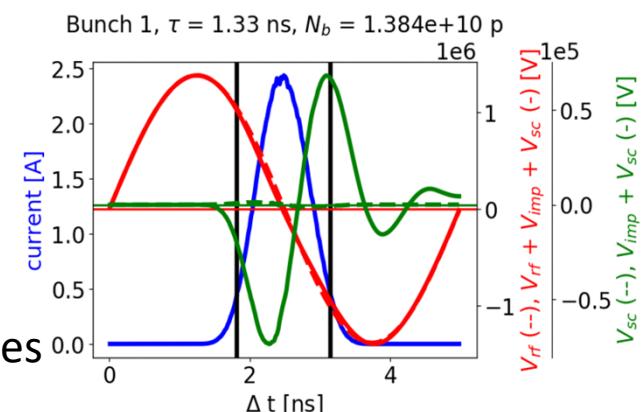


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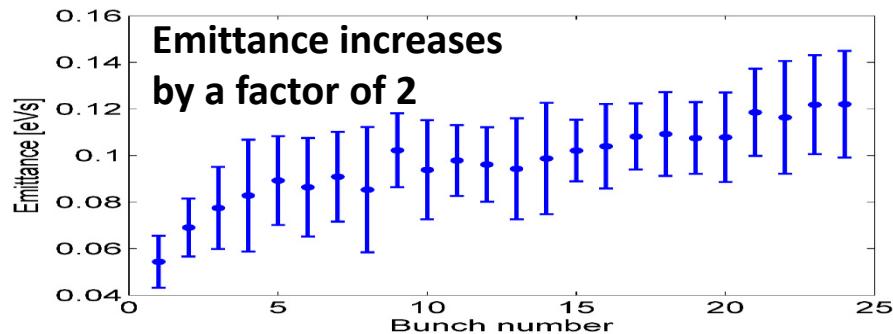
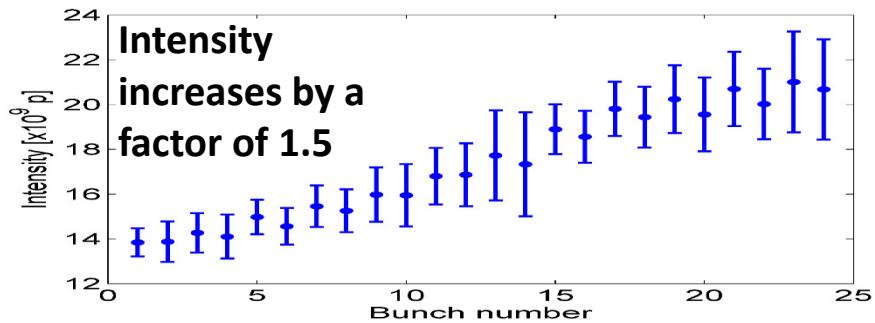
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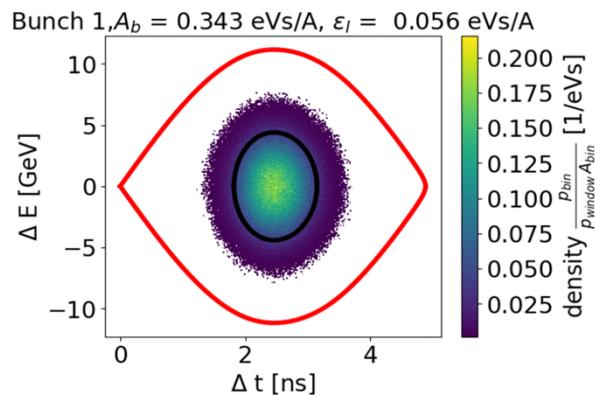
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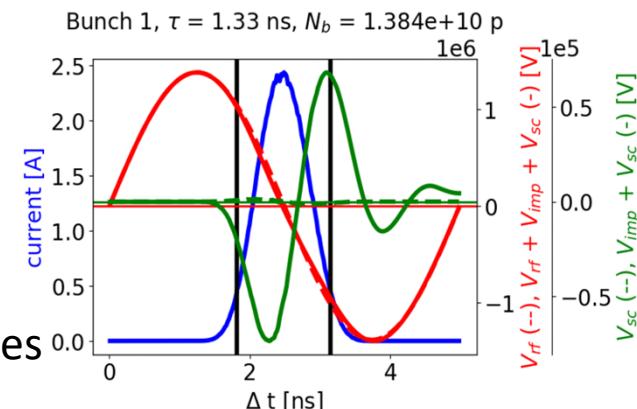


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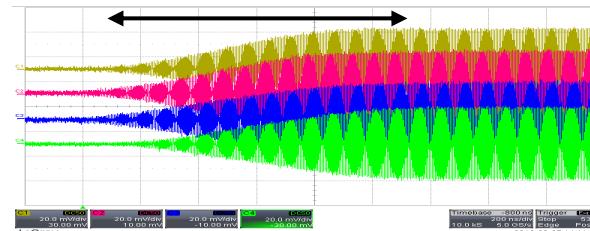


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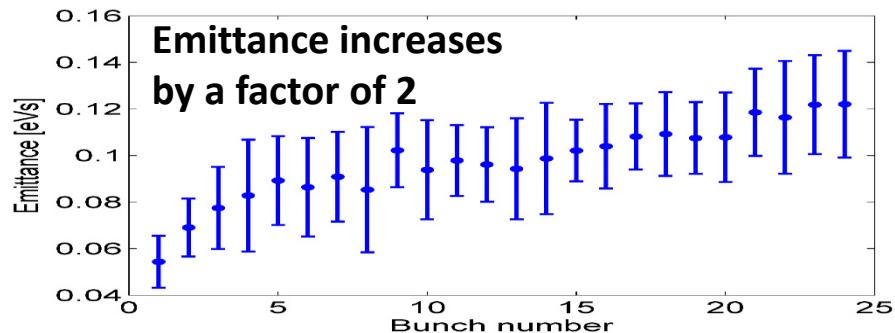
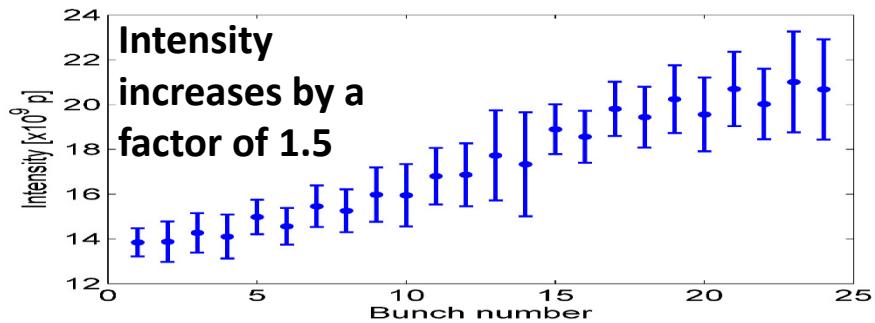
- The two batches are separated by large $T_b = 2.7 \mu\text{s}$ ($T_b^{th} = 1 \mu\text{s}$)
 - In this way $\alpha \gg 4$ when $T_b = T_b^{th}$ and adiabaticity is preserved



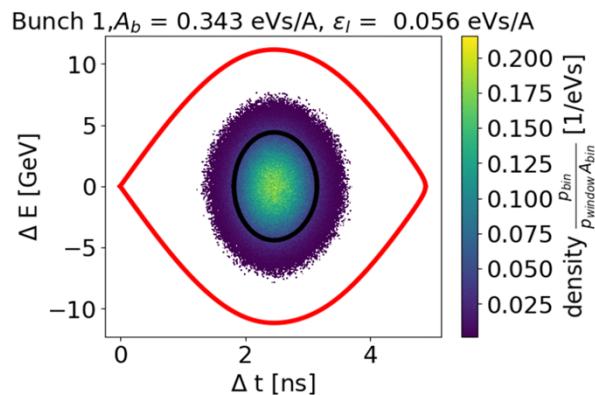
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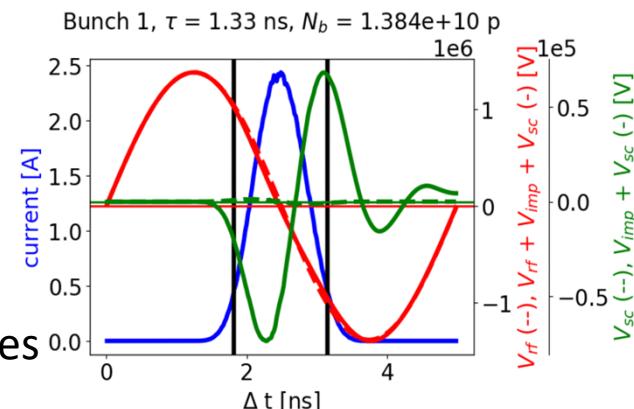


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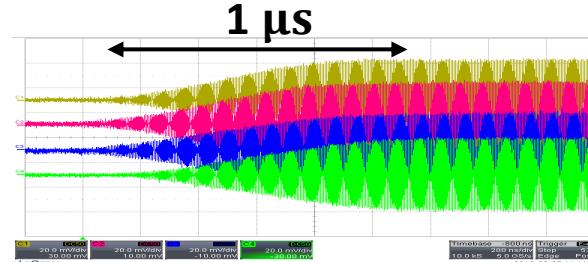


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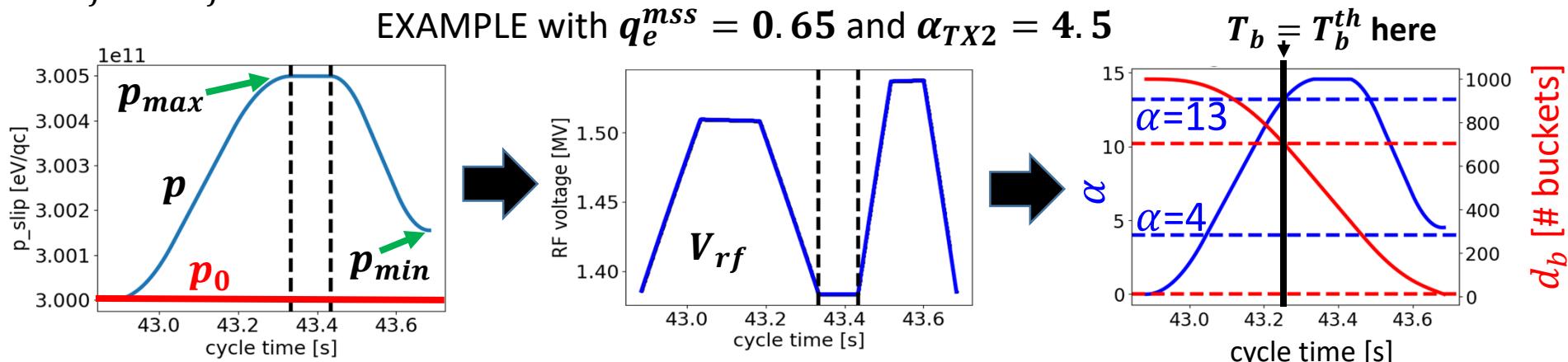


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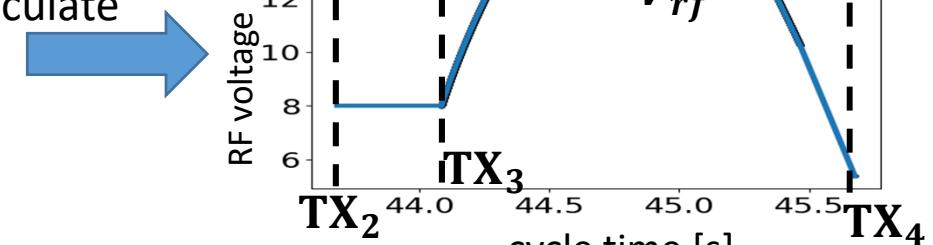
Design of RF programs



- The RF voltage program during slip-stacking is calculated from the momentum program for constant filling factor of bucket in energy q_e^{mss}
- The batches move in opposite directions relative to $\Delta E=0$ ($f_{rf}^1 + f_{rf}^2 = 2f_{rf,0}$, $V_{rf}^1 = V_{rf}^2$)



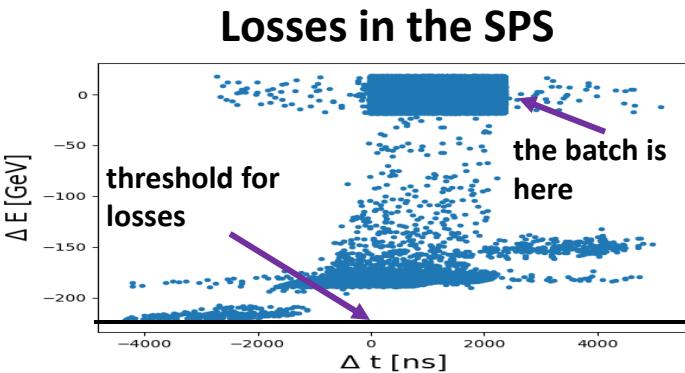
- The capture voltage V_{rf}^{rc} is used in $[TX_2, TX_3]$, then the filling factor in energy at TX_3 of the highest emittance bunch is computed and used to calculate the voltage program in $[TX_3, TX_4]$.



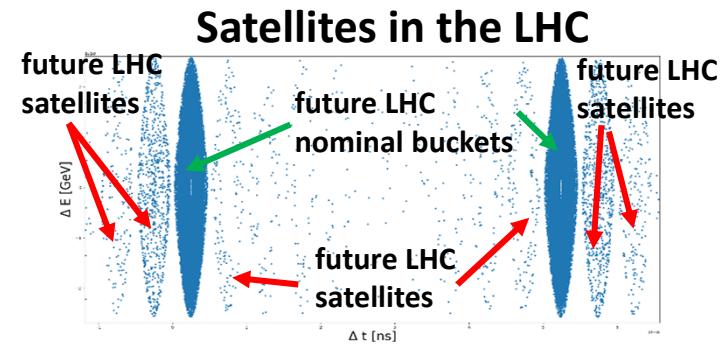
- At flat top two options are considered:
 - V_{rf} is increased adiabatically to 15 MV (**bunch compression**).
 - V_{rf} is increased in few turns to 15 MV (**bunch rotation**).

Constraints and optimizations

- Two constraints to take into account
 - $L_{tot} < 5\%$ (total losses due to momentum slip-stacking, LIU constraint)
 - $\tau_{max} < 1.65\text{ ns}$ (maximum bunch length at SPS extraction, 400 MHz LHC buckets cannot accept more)
- We divide the total losses in $L_{tot} = L_{SPS} + S_{LHC}$



EXAMPLE

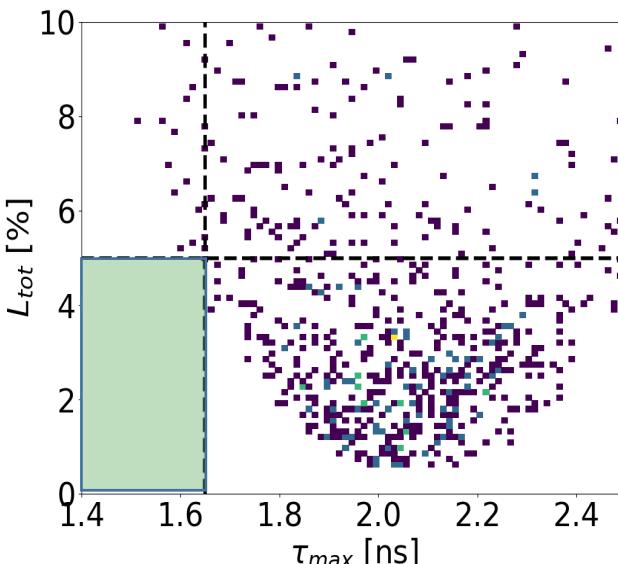


- With all the assumptions given before, simulations are completely defined fixing α_{TX2} , q_e^{mss} , V_{rf}^{rc} and the RF manipulation at flat top (**compression or rotation**)
 - It is important to find the combinations which give the lowest L_{tot} and τ_{max} (optimal solutions)
 - The dynamics are too complex to rely only on qualitative studies
 - Parameter scan: α_{TX2} (3.5->8), q_e^{mss} (0.45->9), V_{rf}^{rc} (1 MV->9 MV)
- The Q20 optics ($\gamma_{tr}=18$) is currently used in operation (detailed analysis)
 - The other two optics (Q22, $\gamma_{tr}=20$), (Q26, $\gamma_{tr}=23$) are briefly mentioned

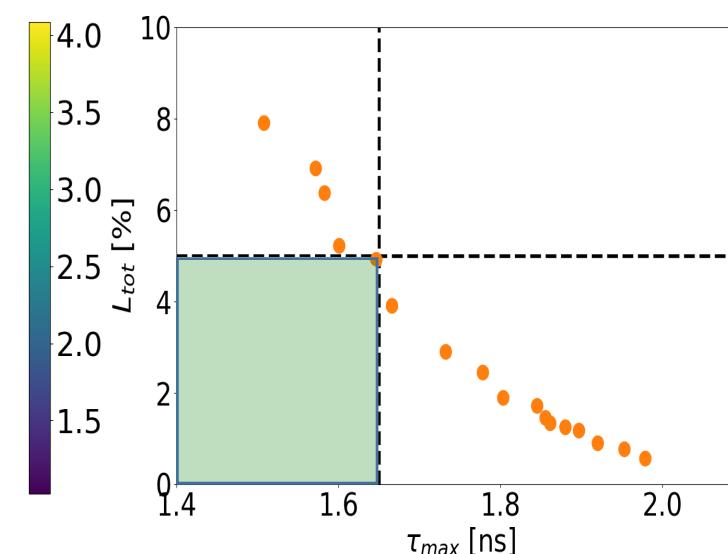
Q20 optics: bunch compression



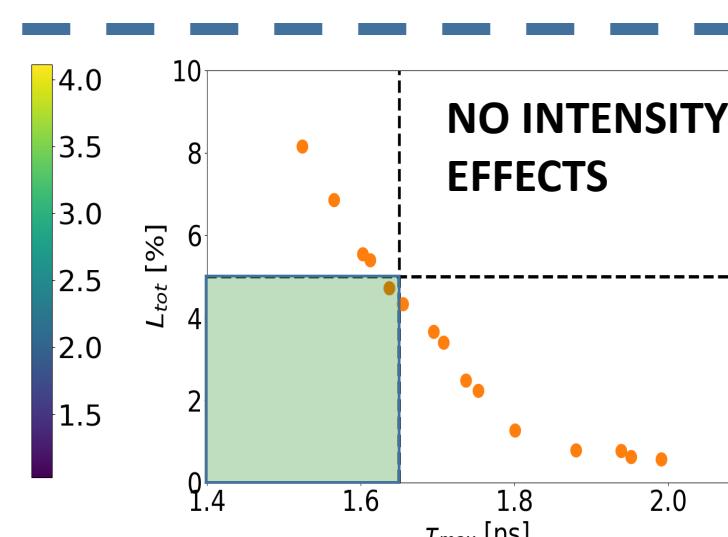
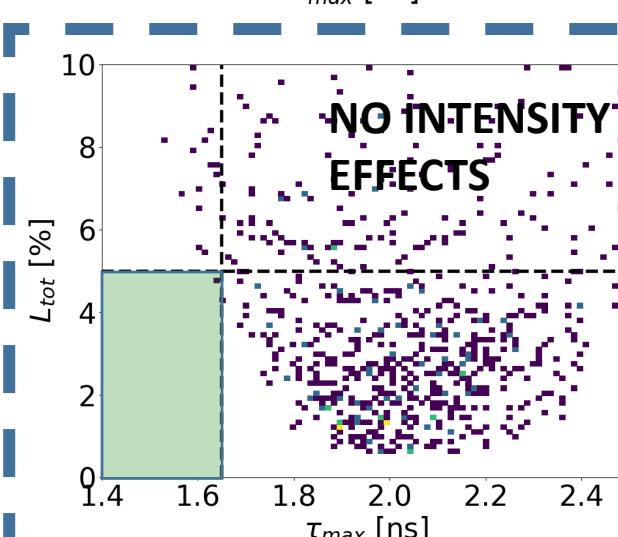
Scan results



Optimal solutions



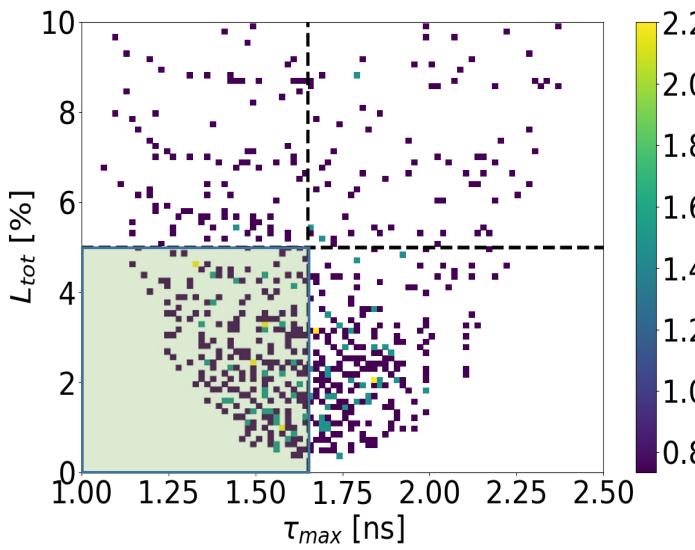
- Constraints are practically not satisfied
- Strong limitation on τ_{max} rather than on L_{tot}



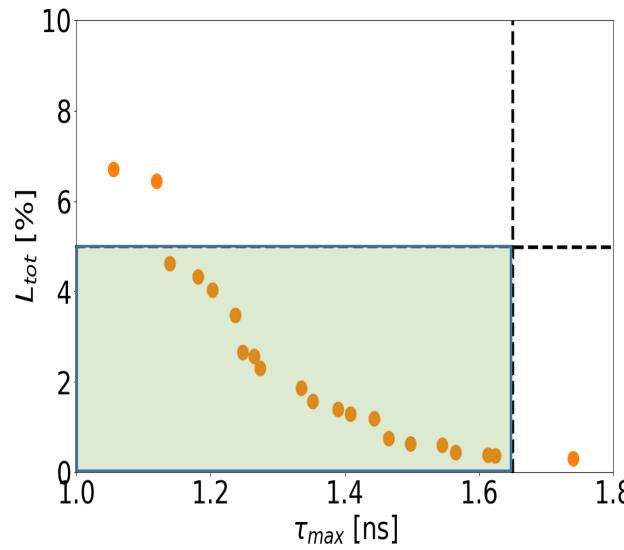
- No significant difference if intensity effects are off
- Intensity effects don't cause additional losses or blow-up

Q20 optics: bunch rotation

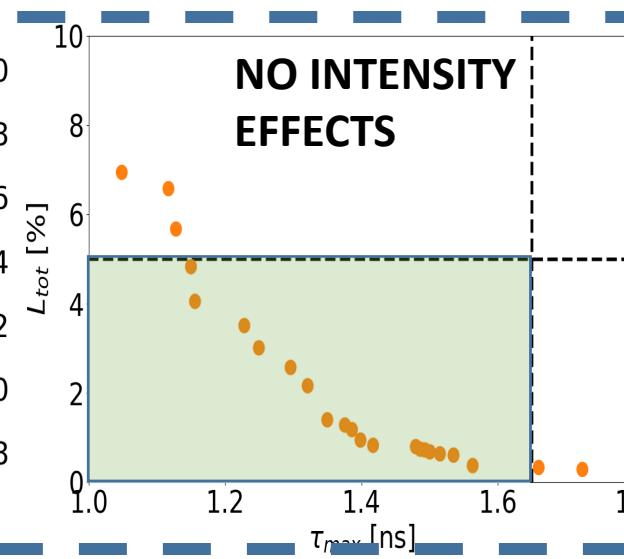
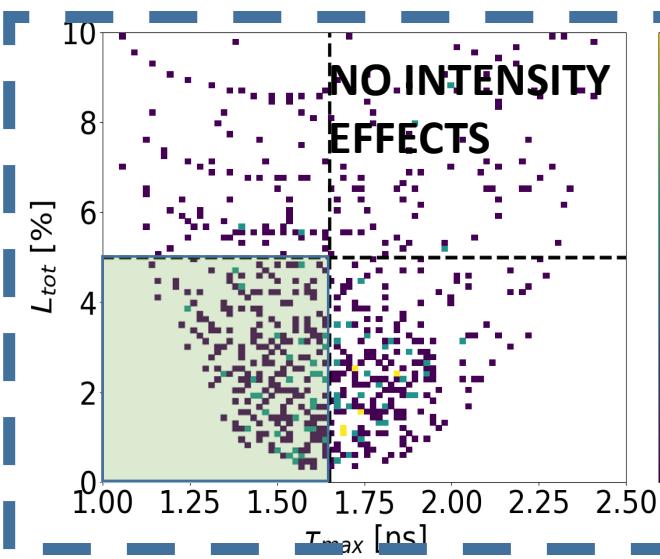
Scan results



Optimal solutions



- Bunch rotation allows to significantly reduce τ_{max} without increasing L_{tot}
- Constraints satisfied by half of the combinations
- However 'S' shape at extraction could complicate transmission into LHC

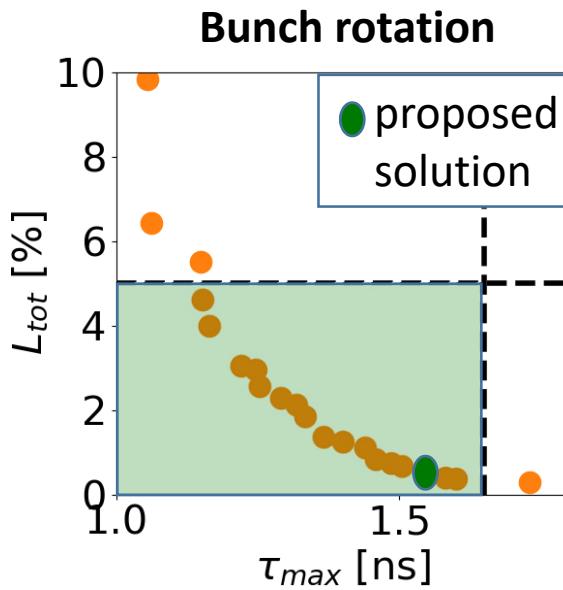


- Again no significant difference if intensity effects are off

Q20 optics: proposed solution



- Only bunch rotation can fulfil the requirements.
- Giving priority to loss reduction and keeping some safety margin for the bunch length we propose the following combination (see also the **Appendix** for more detailed analysis)



The solution largely fulfills LIU requirements

- $L_{tot} = 0.43\%$
- $\tau_{max} = 1.55\text{ ns}$
- $S_{LHC} = 0.13\%$
- $L_{SPS} = 0.30\%$
- $\alpha_{TX2} = 4.5$
- $q_e^{mss} = 0.65$
- $V_{rf}^{rc} = 8\text{ MV}$
- Low q_e^{mss} helps limiting the losses in SPS during slip-stacking
- Low q_e^{mss} and $\alpha_{TX2} > 4$ helps limiting influence of chaotic motion in $\Delta E = 0$ making S_{LHC} low

The solution is feasible

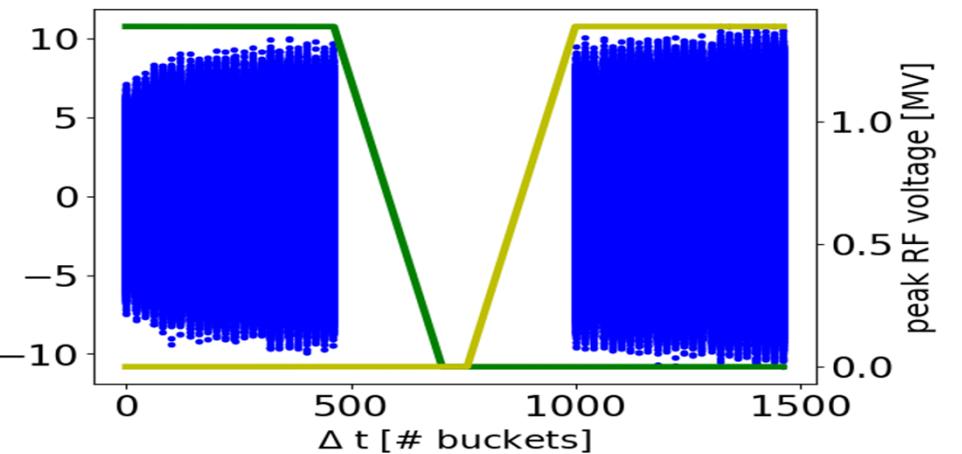
- $\Delta R_{max}^{mss} = 8\text{ mm} < 20\text{ mm}$ (one-side aperture limitation)
- $\Delta f_{rf,max}^{mss} = 1\text{ kHz} \ll 1\text{ MHz}$ (200 MHz TWC bandwidth)
- $V_{rf}^{max} = 14.6\text{ MV} < 15\text{ MV}$ (available peak voltage)

Proposed solution: slip-stacking

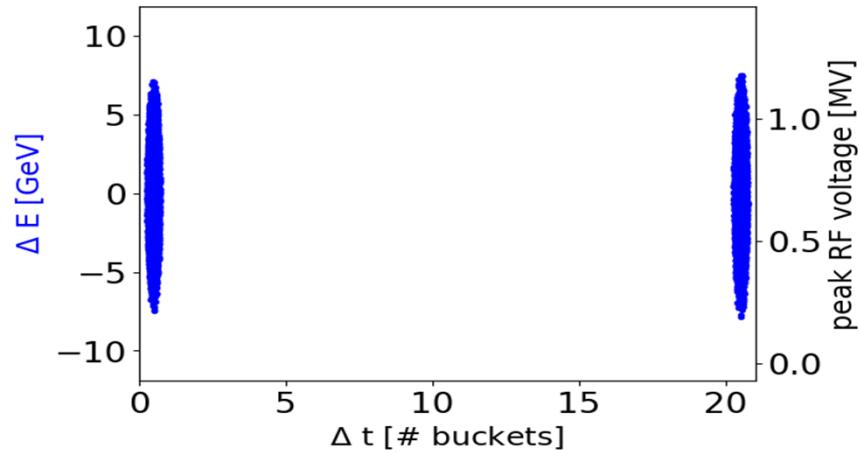


General frame, V_{rf}^1 , V_{rf}^2

ΔE [GeV]



Zoom on first two bunches



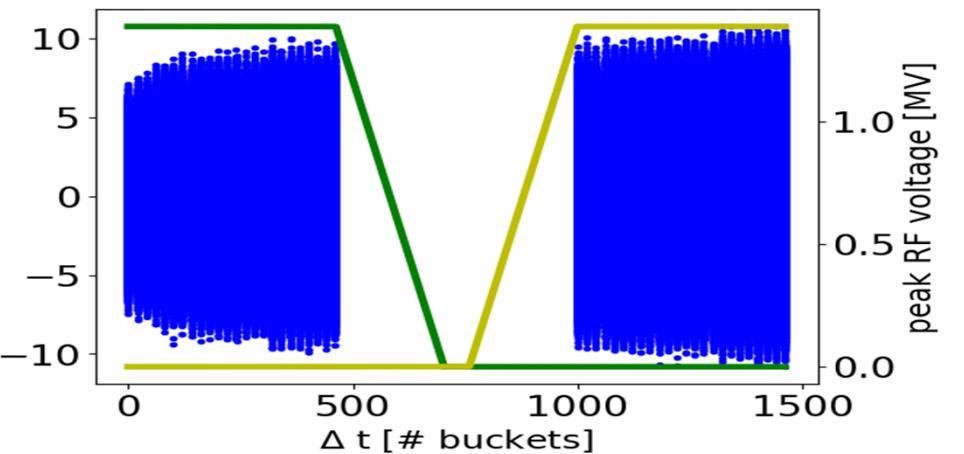
- As expected only few particle lost during slip-stacking ($q_e^{mss} = 0.65$)
- Low impact of chaotic motion in $\Delta E = 0$ ($\alpha_{TX2} = 4.5$)

Proposed solution: slip-stacking

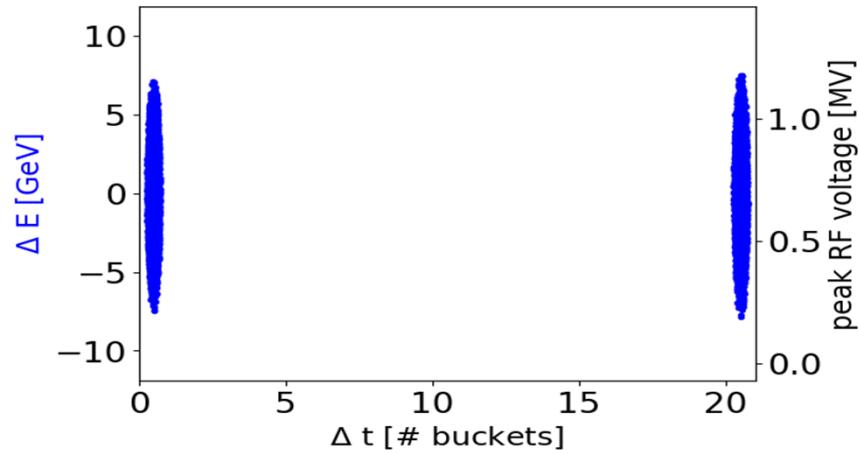


General frame, V_{rf}^1 , V_{rf}^2

ΔE [GeV]



Zoom on first two bunches



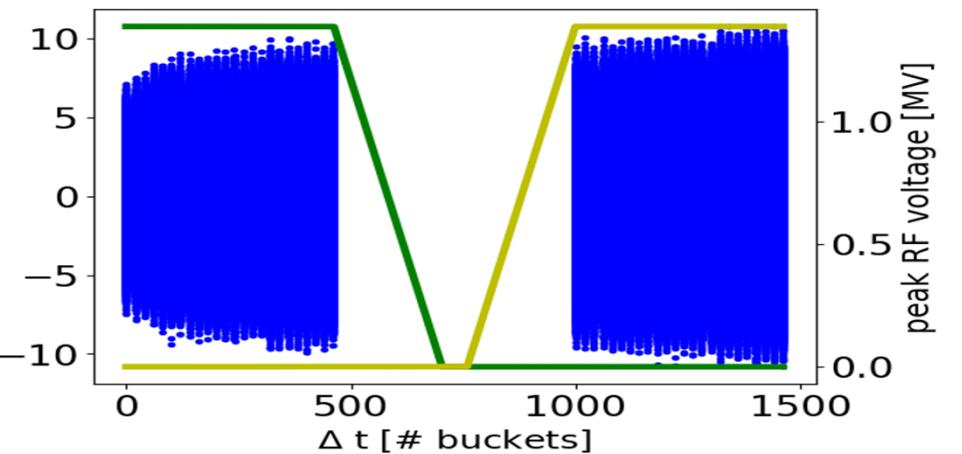
- As expected only few particle lost during slip-stacking ($q_e^{mss} = 0.65$)
- Low impact of chaotic motion in $\Delta E = 0$ ($\alpha_{TX2} = 4.5$)

Proposed solution: slip-stacking

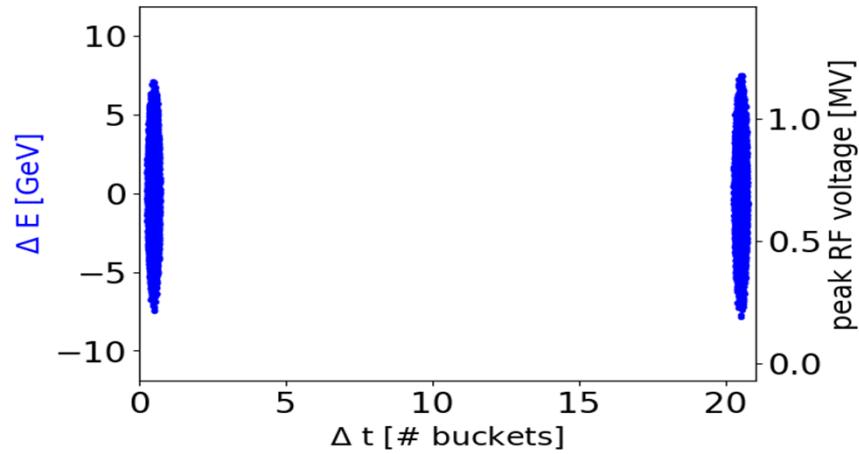


General frame, V_{rf}^1 , V_{rf}^2

ΔE [GeV]



Zoom on first two bunches



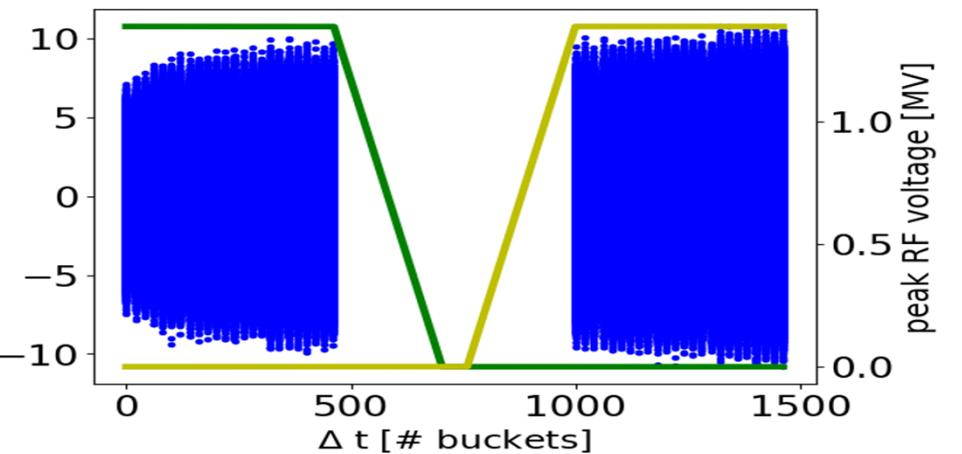
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Proposed solution: slip-stacking

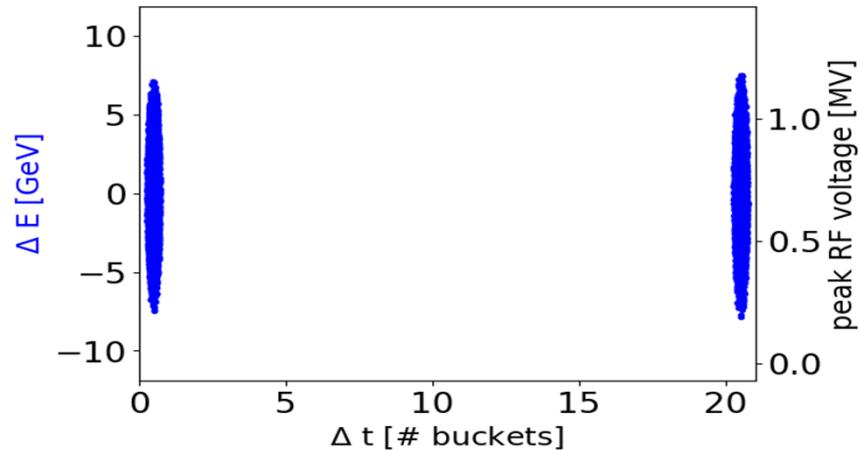


General frame, V_{rf}^1 , V_{rf}^2

ΔE [GeV]



Zoom on first two bunches



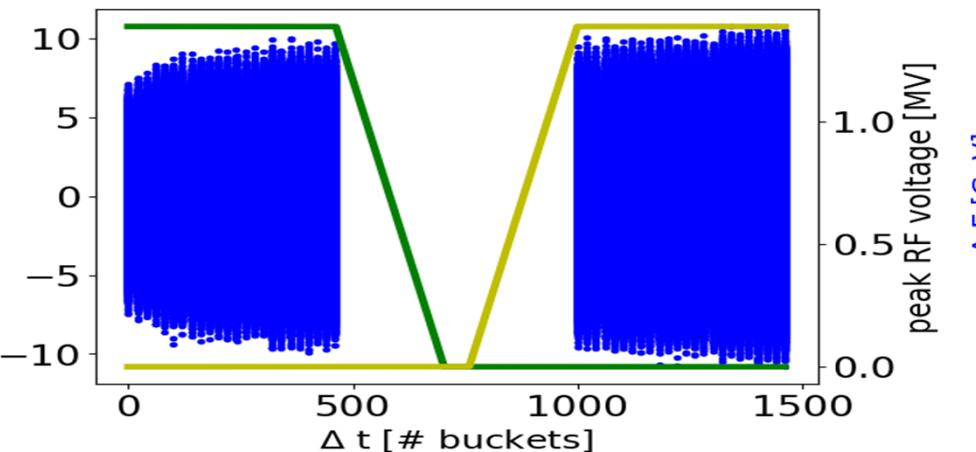
- As expected only few particle lost during slip-stacking ($q_e^{mss} = 0.65$)
- Low impact of chaotic motion in $\Delta E = 0$ ($\alpha_{TX2} = 4.5$)

Proposed solution: slip-stacking

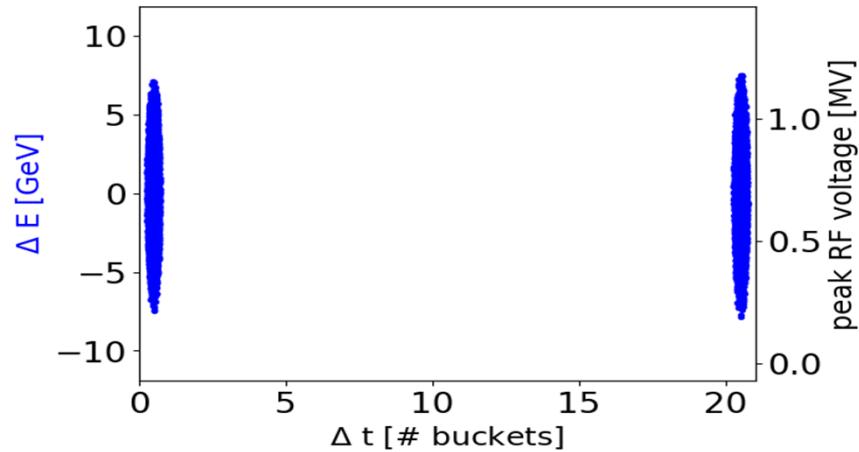


General frame, V_{rf}^1 , V_{rf}^2

ΔE [GeV]



Zoom on first two bunches

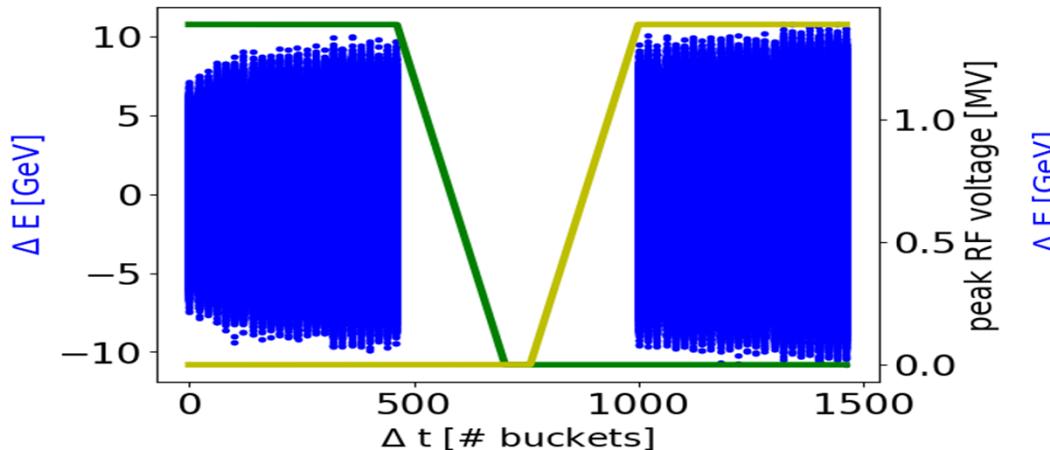


- As expected only few particle lost during slip-stacking ($q_e^{mss} = 0.65$)
- Low impact of chaotic motion in $\Delta E = 0$ ($\alpha_{TX2} = 4.5$)
- RF perturbation causes resonances at the end of slip-stacking (even without intensity effects)
 - Predicted by theory [2]

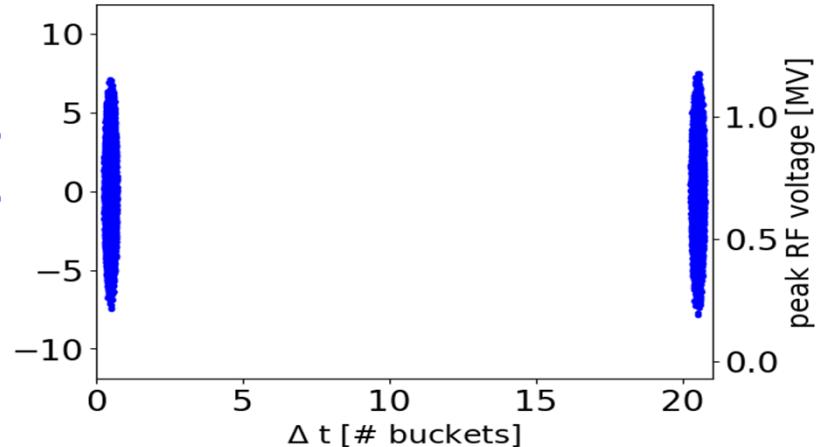
Proposed solution: slip-stacking



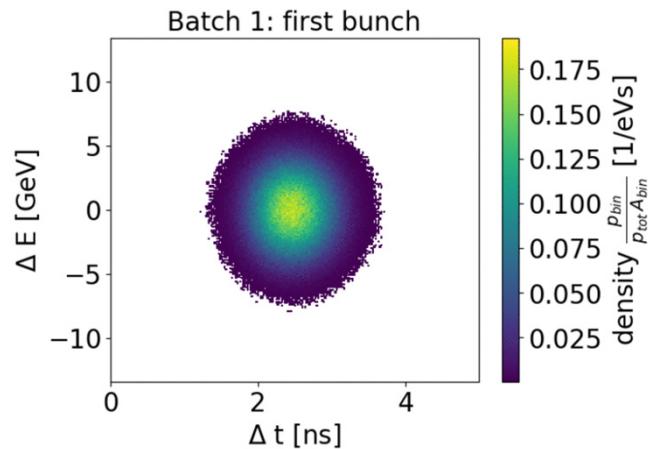
General frame, V_{rf}^1 , V_{rf}^2



Zoom on first two bunches



- As expected only few particle lost during slip-stacking ($q_e^{mss} = 0.65$)
- Low impact of chaotic motion in $\Delta E = 0$ ($\alpha_{TX2} = 4.5$)

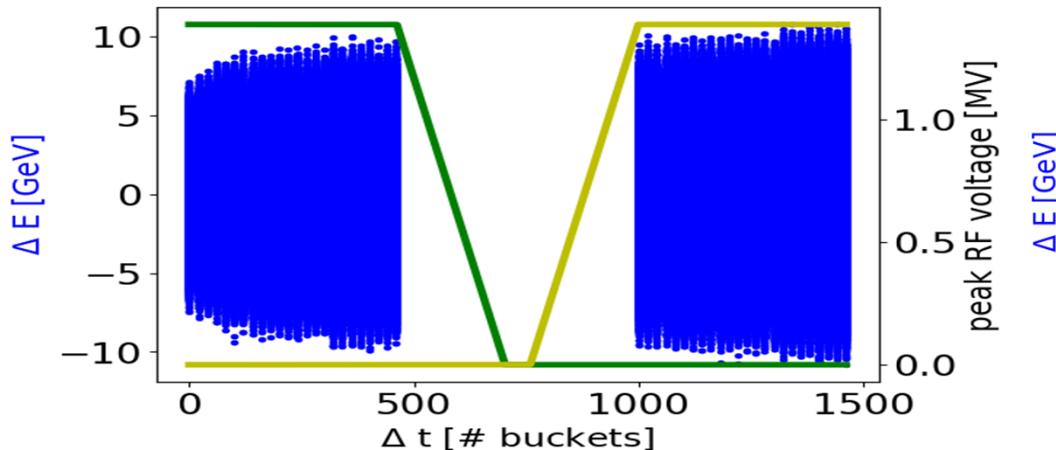


- RF perturbation causes resonances at the end of slip-stacking (even without intensity effects)
 - Predicted by theory [2]

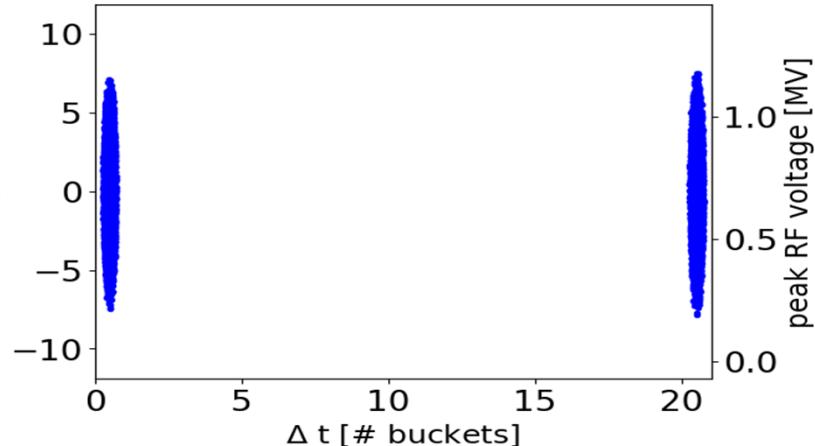
Proposed solution: slip-stacking



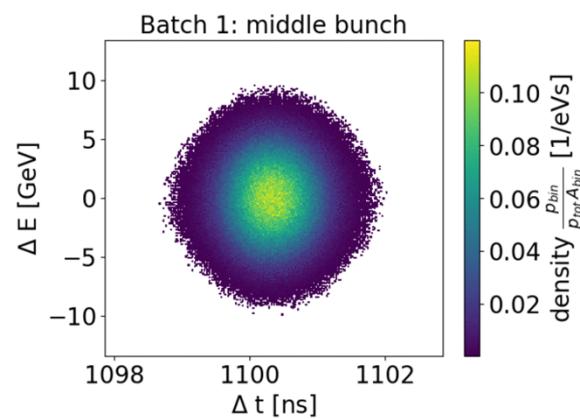
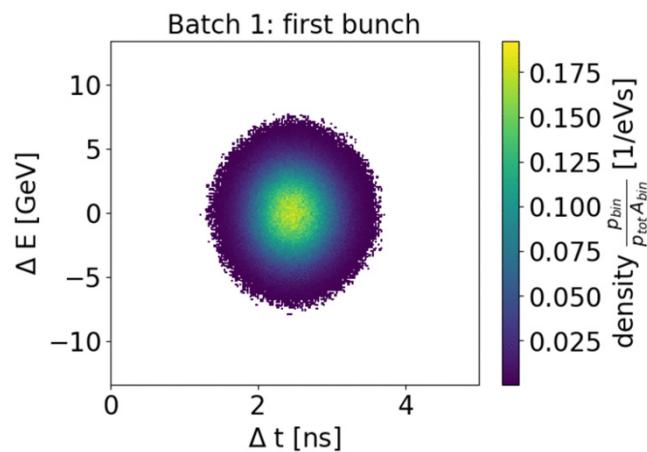
General frame, V_{rf}^1 , V_{rf}^2



Zoom on first two bunches



- As expected only few particle lost during slip-stacking ($q_e^{mss} = 0.65$)
- Low impact of chaotic motion in $\Delta E = 0$ ($\alpha_{TX2} = 4.5$)

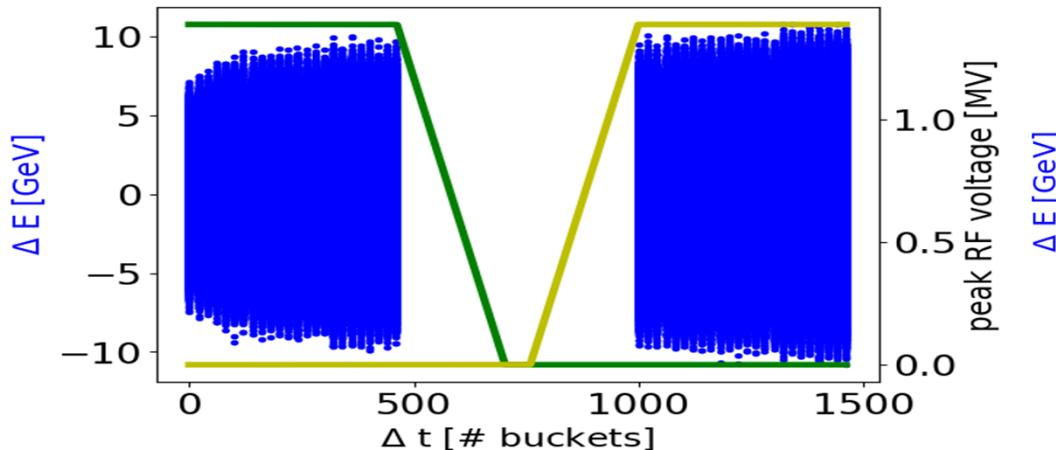


- RF perturbation causes resonances at the end of slip-stacking (even without intensity effects)
 - Predicted by theory [2]

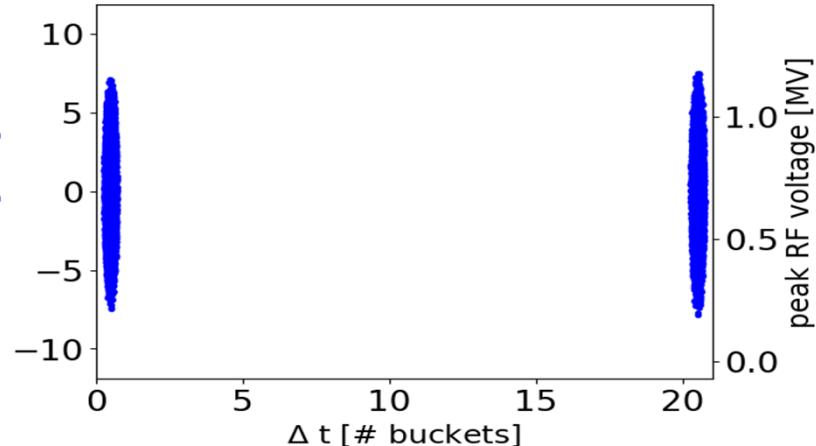
Proposed solution: slip-stacking



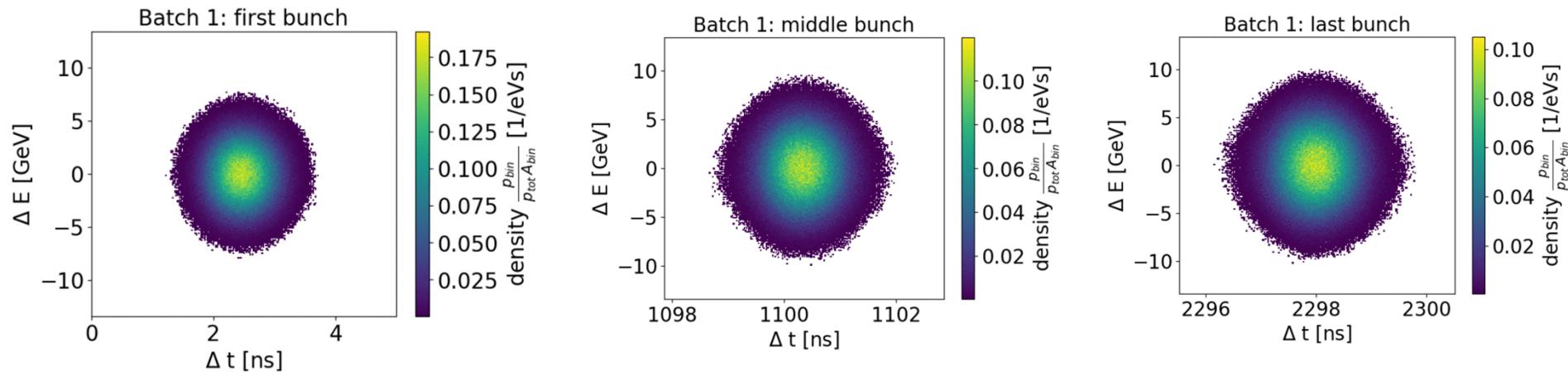
General frame, V_{rf}^1 , V_{rf}^2



Zoom on first two bunches



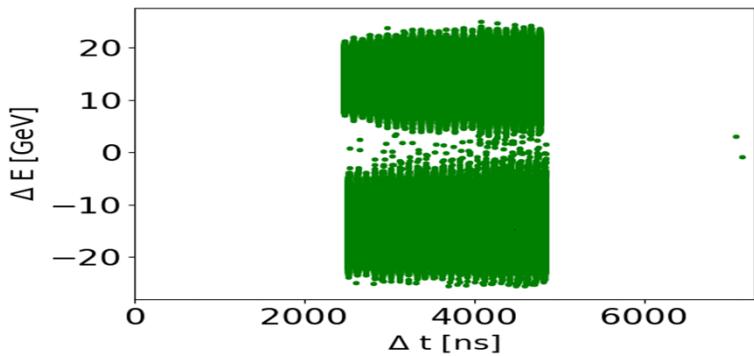
- As expected only few particle lost during slip-stacking ($q_e^{mss} = 0.65$)
- Low impact of chaotic motion in $\Delta E = 0$ ($\alpha_{TX2} = 4.5$)



- RF perturbation causes resonances at the end of slip-stacking (even without intensity effects)
 - Predicted by theory [2]

Proposed solution: capture and ramp

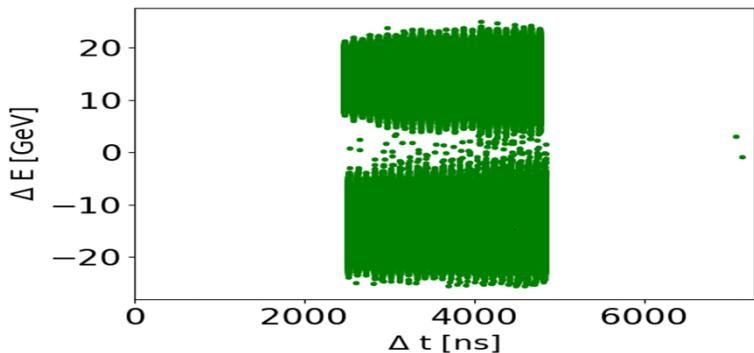
General frame bunches are yellow at TX_3



- Few losses due to recapture and acceleration of higher emittance bunches

Proposed solution: capture and ramp

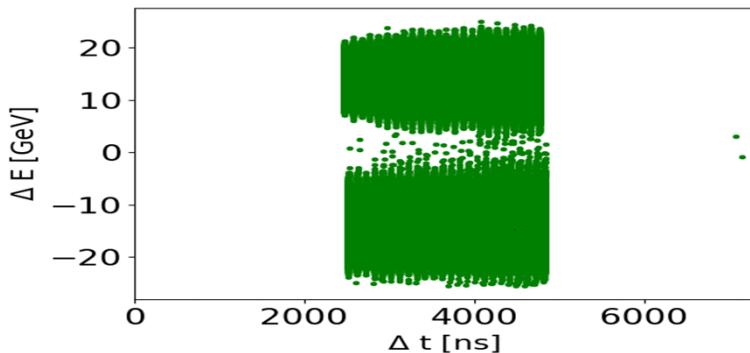
General frame bunches are yellow at TX_3



- Few losses due to recapture and acceleration of higher emittance bunches
- Hollow bunches due to mismatch in recapture bucket (even without int. effects)
- **Dense area in phase space never filaments for shorter bunches (only with int. effects, see Appendix)**

Proposed solution: capture and ramp

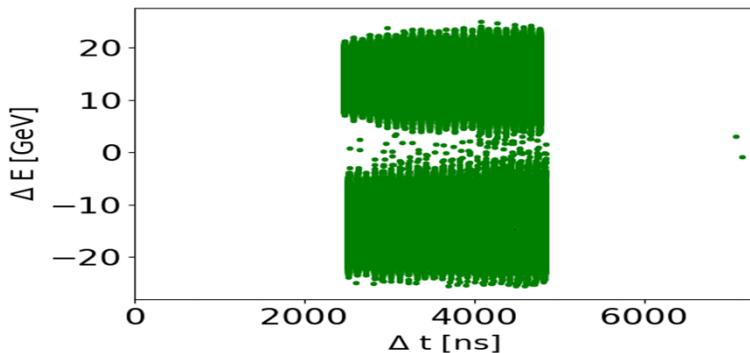
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Proposed solution: capture and ramp

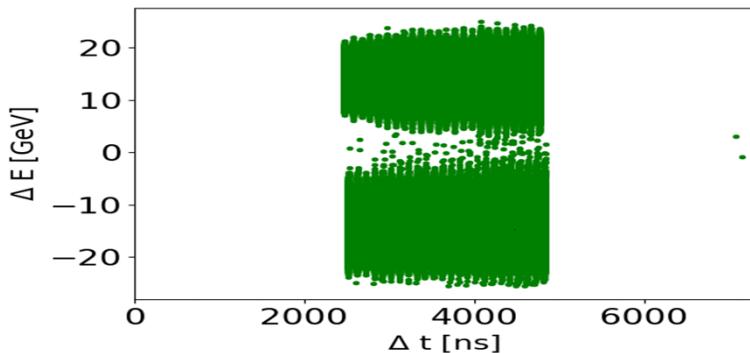
General frame bunches are yellow at TX_3



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Proposed solution: capture and ramp

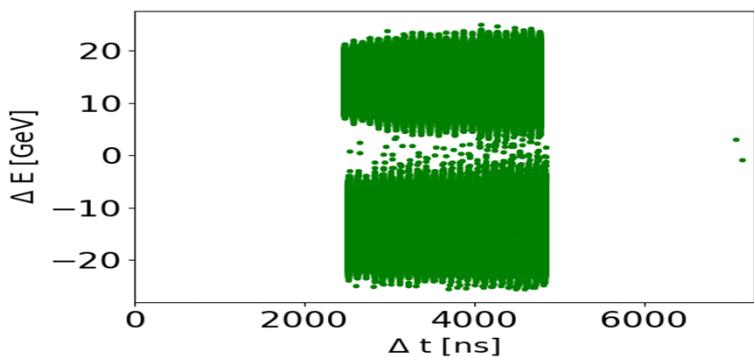
General frame bunches are yellow at TX_3



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- **Dense area in phase space never filaments for shorter bunches (only with int. effects, see Appendix)**

Proposed solution: capture and ramp

General frame bunches are yellow at TX_3

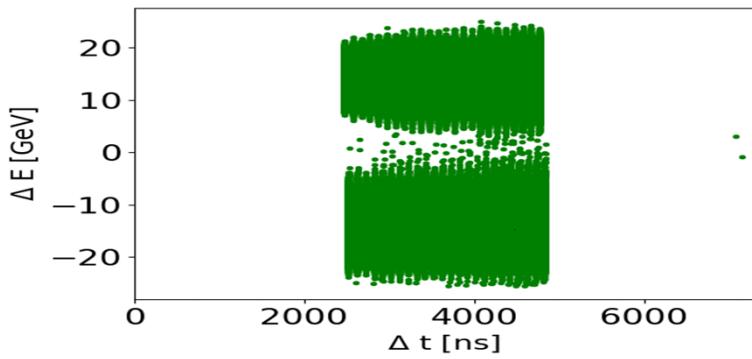


- Few losses due to recapture and acceleration of higher emittance bunches
- Hollow bunches due to mismatch in recapture bucket (even without int. effects)
- **Dense area in phase space never filaments for shorter bunches (only with int. effects, see Appendix)**

Middle bunch

Proposed solution: capture and ramp

General frame bunches are yellow at TX_3

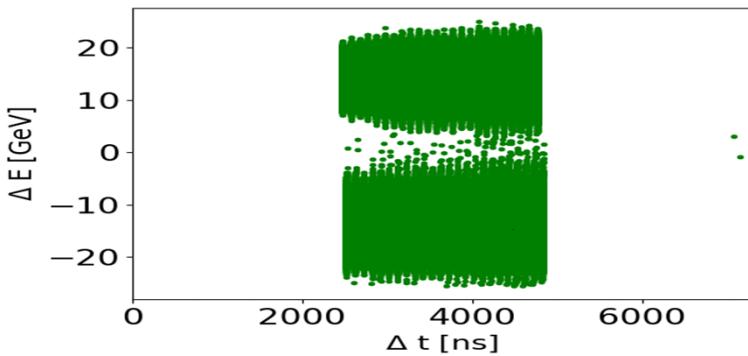


- Few losses due to recapture and acceleration of higher emittance bunches
- Hollow bunches due to mismatch in recapture bucket (even without int. effects)
- Dense area in phase space never filaments for shorter bunches (**only with int. effects, see Appendix**)

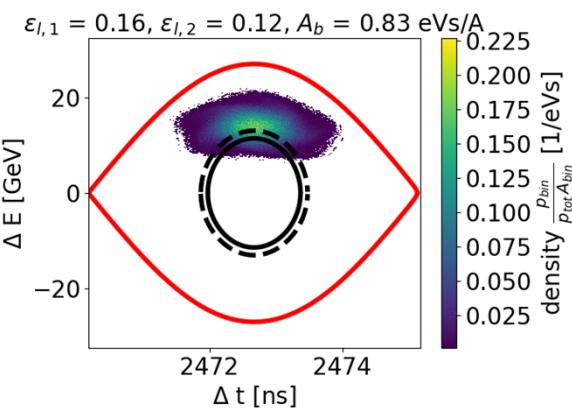
Middle bunch

Proposed solution: capture and ramp

General frame bunches are yellow at TX_3



First bunch



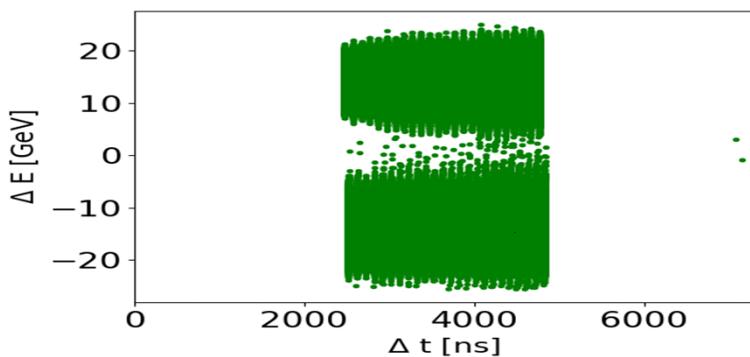
Middle bunch

- Few losses due to recapture and acceleration of higher emittance bunches
- Hollow bunches due to mismatch in recapture bucket (even without int. effects)
- **Dense area in phase space never filaments for shorter bunches (only with int. effects, see Appendix)**

Proposed solution: capture and ramp

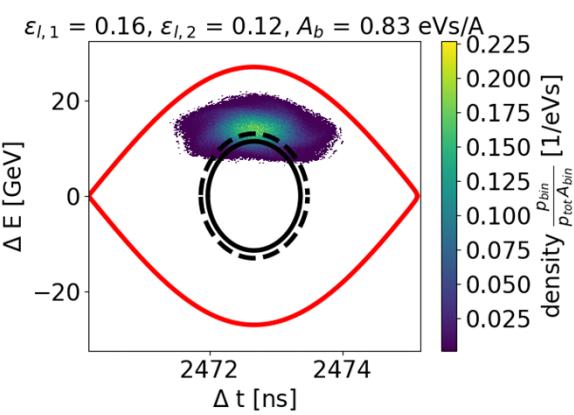


General frame bunches are yellow at TX_3

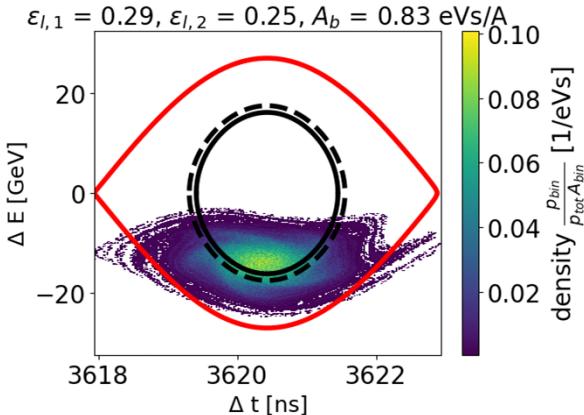


- Few losses due to recapture and acceleration of higher emittance bunches
- Hollow bunches due to mismatch in recapture bucket (even without int. effects)
- Dense area in phase space never filaments for shorter bunches (**only with int. effects, see Appendix**)

First bunch



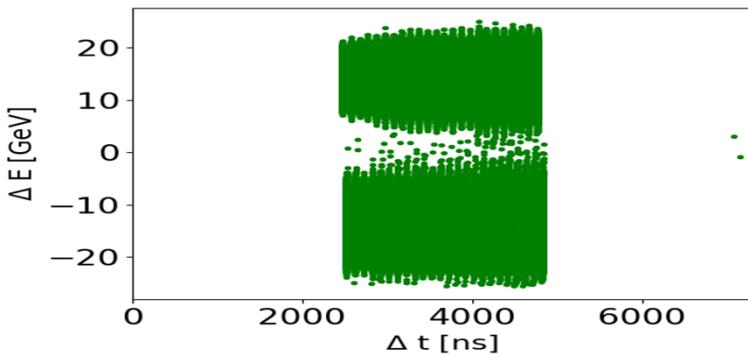
Middle bunch





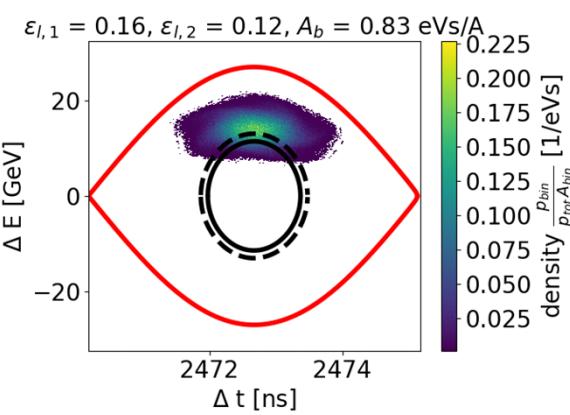
Proposed solution: capture and ramp

General frame bunches are yellow at TX_3

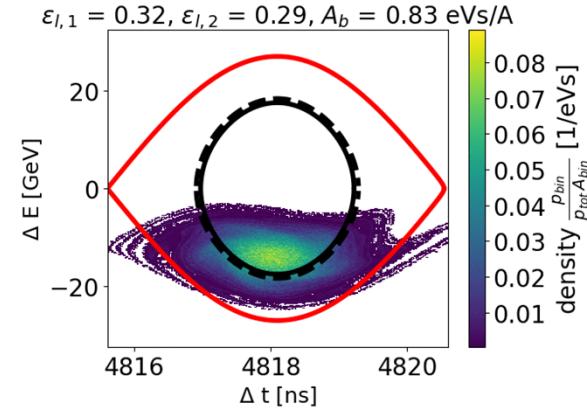
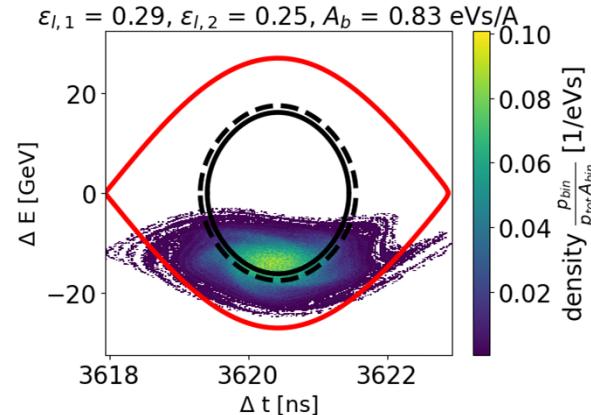


- Few losses due to recapture and acceleration of higher emittance bunches
- Hollow bunches due to mismatch in recapture bucket (even without int. effects)
- Dense area in phase space never filaments for shorter bunches (**only with int. effects, see Appendix**)

First bunch



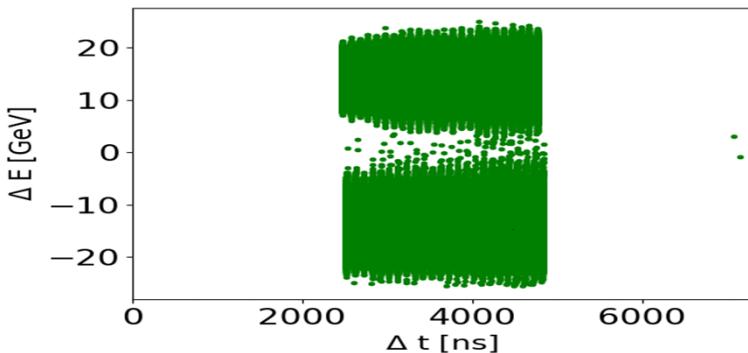
Middle bunch



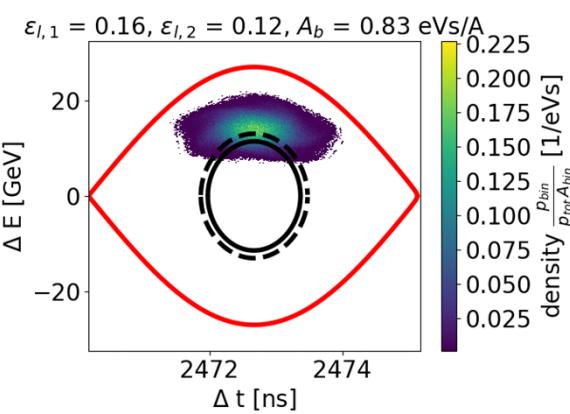


Proposed solution: capture and ramp

General frame bunches are yellow at TX_3

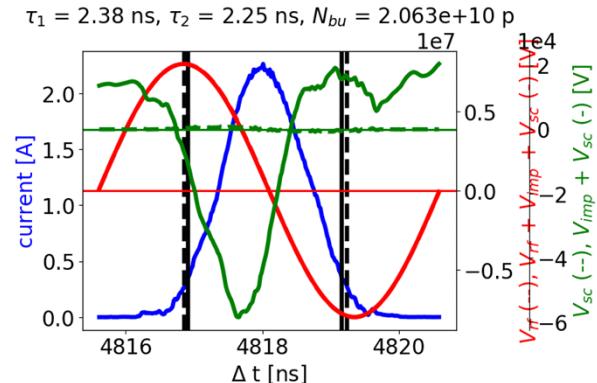
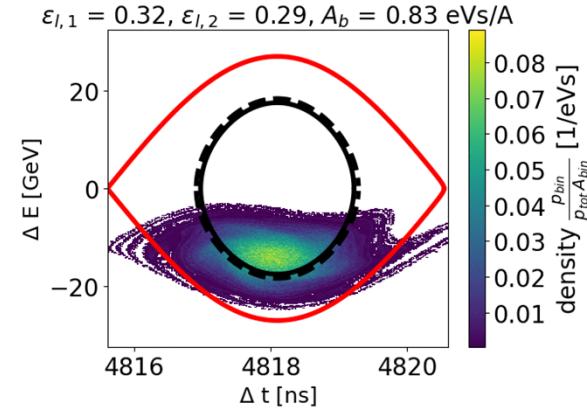
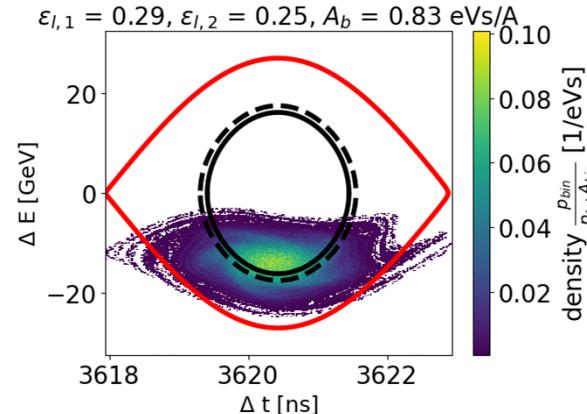


First bunch



- Few losses due to recapture and acceleration of higher emittance bunches
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- Dense area in phase space never filaments for shorter bunches (only with int. effects, see Appendix)**

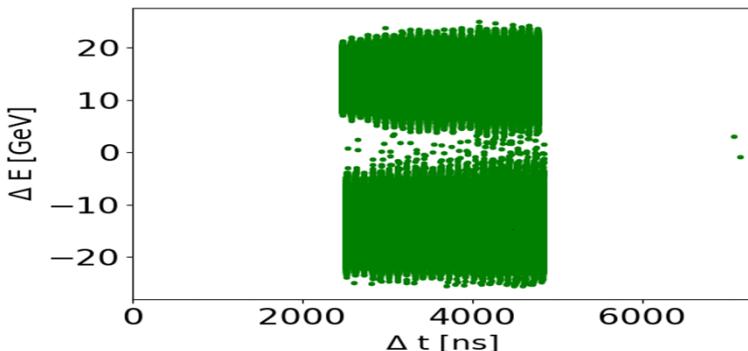
Middle bunch



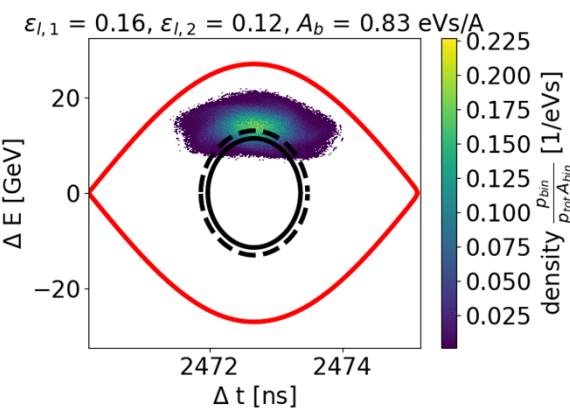


Proposed solution: capture and ramp

General frame bunches are yellow at TX_3

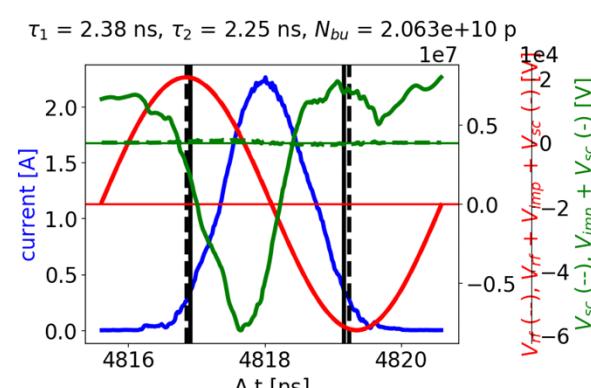
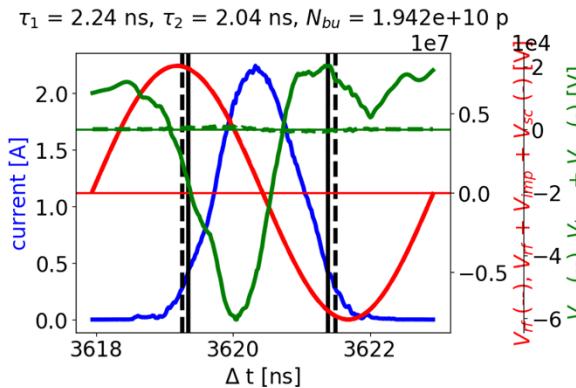
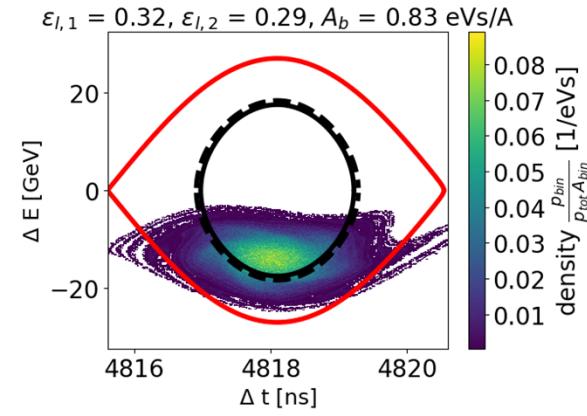
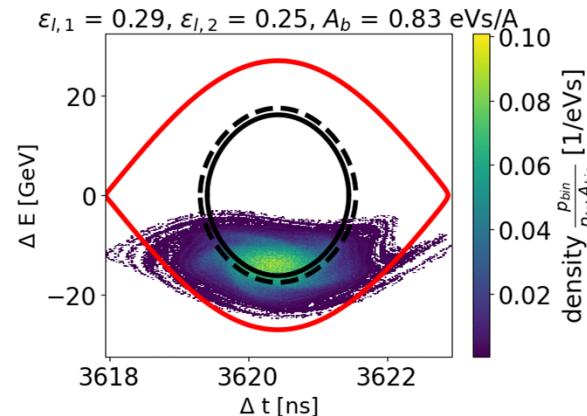


First bunch



- Few losses due to recapture and acceleration of higher emittance bunches
- Hollow bunches due to mismatch in recapture bucket (even without int. effects)
- Dense area in phase space never filaments for shorter bunches (**only with int. effects, see Appendix**)

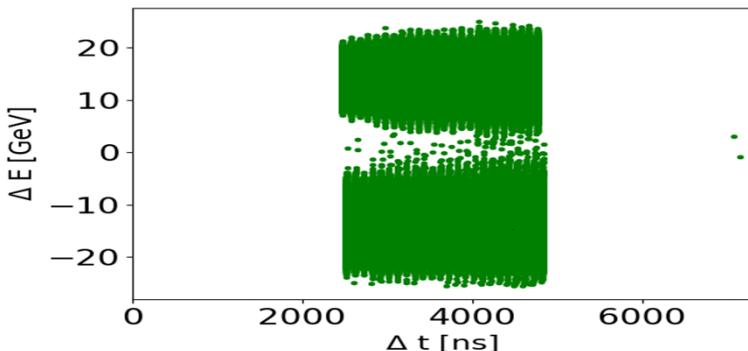
Middle bunch



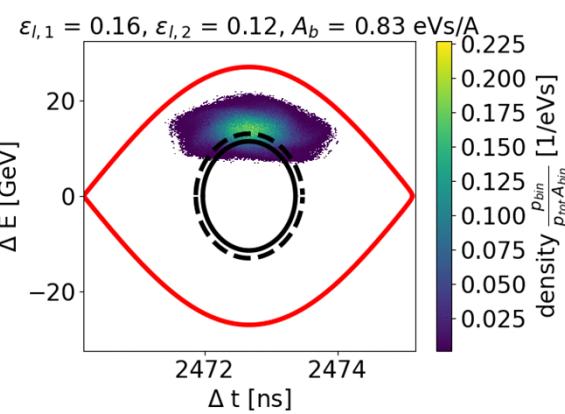


Proposed solution: capture and ramp

General frame bunches are yellow at TX_3

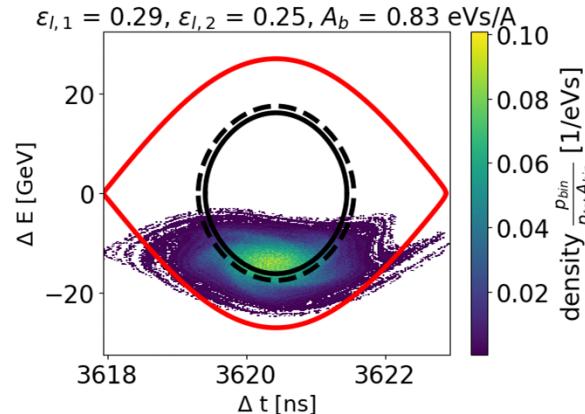


First bunch

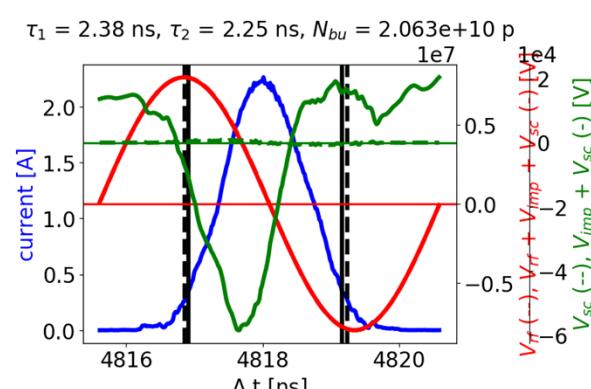
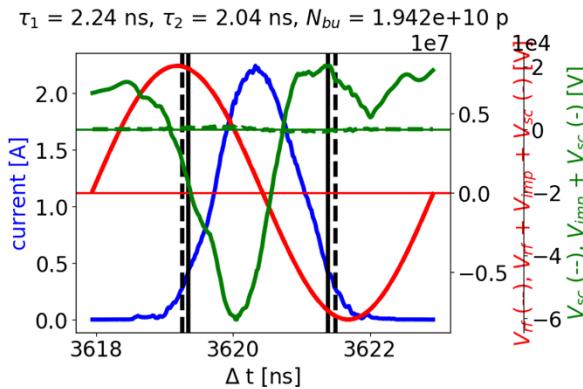
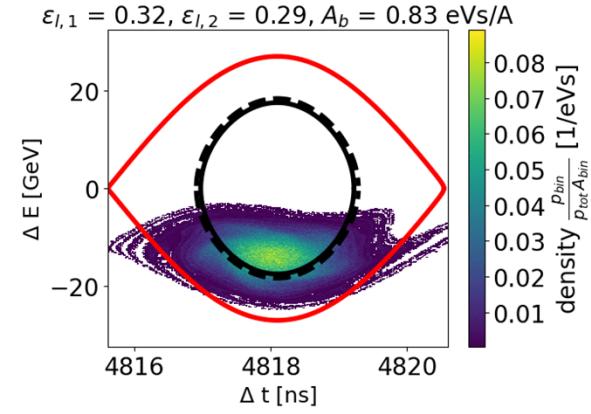


- Few losses due to recapture and acceleration of higher emittance bunches
- Hollow bunches due to mismatch in recapture bucket (even without int. effects)
- Dense area in phase space never filaments for shorter bunches (**only with int. effects, see Appendix**)

Middle bunch



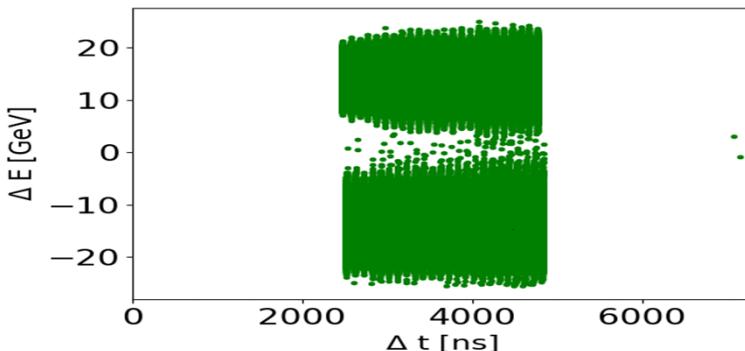
Last bunch



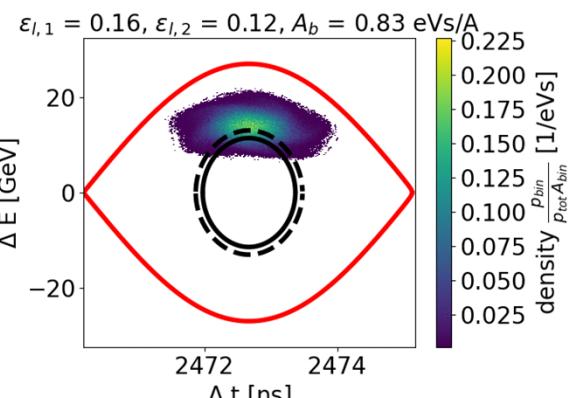


Proposed solution: capture and ramp

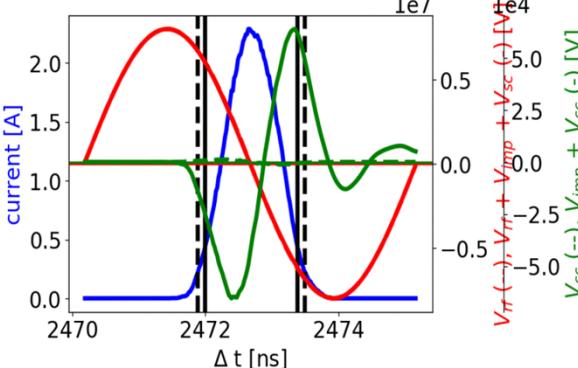
General frame bunches are yellow at TX_3



First bunch

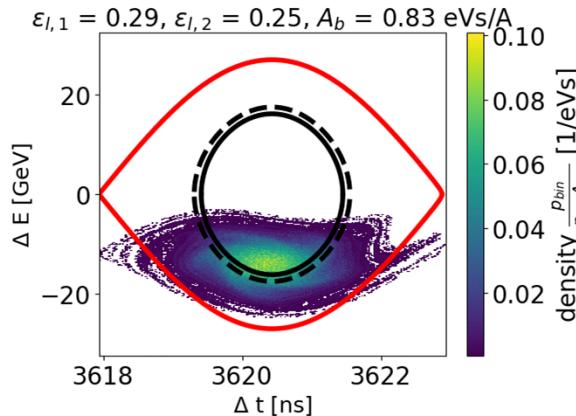


$$\tau_1 = 1.61 \text{ ns}, \tau_2 = 1.39 \text{ ns}, N_{bu} = 1.384 \times 10^{10} \text{ p}$$

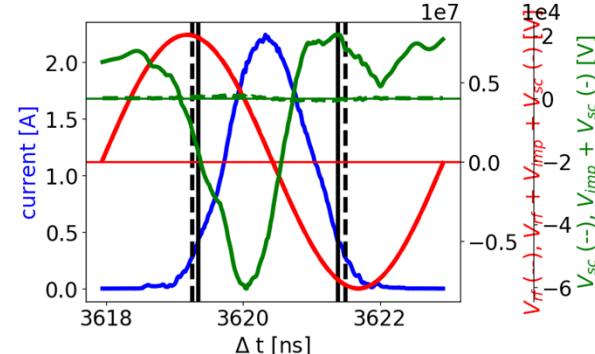


- Few losses due to recapture and acceleration of higher emittance bunches
- Hollow bunches due to mismatch in recapture bucket (even without int. effects)
- Dense area in phase space never filaments for shorter bunches (**only with int. effects, see Appendix**)

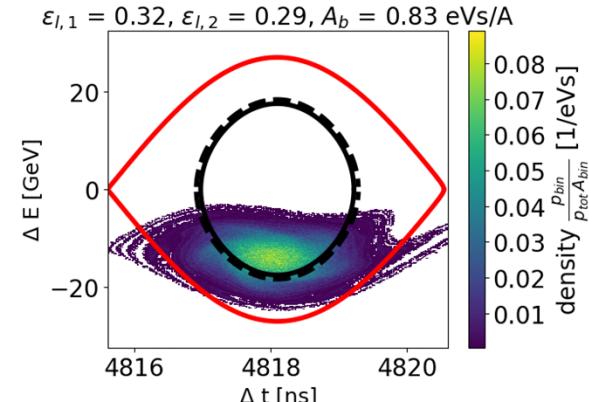
Middle bunch



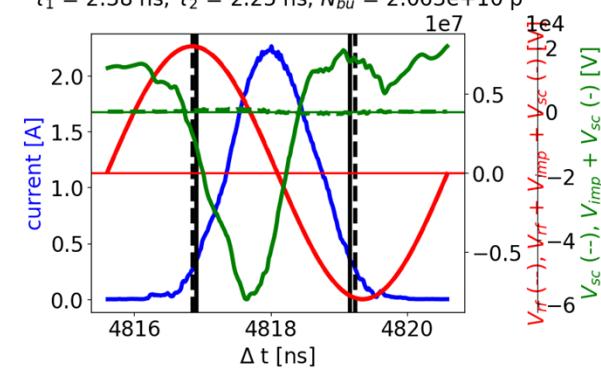
$$\tau_1 = 2.24 \text{ ns}, \tau_2 = 2.04 \text{ ns}, N_{bu} = 1.942 \times 10^{10} \text{ p}$$



Last bunch



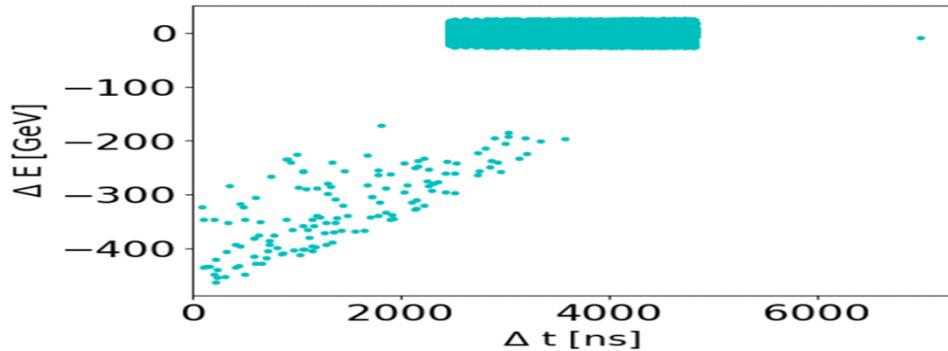
$$\tau_1 = 2.38 \text{ ns}, \tau_2 = 2.25 \text{ ns}, N_{bu} = 2.063 \times 10^{10} \text{ p}$$



Proposed solution: flat top

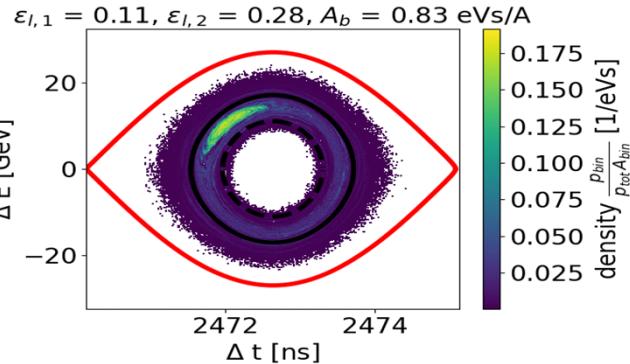


General frame

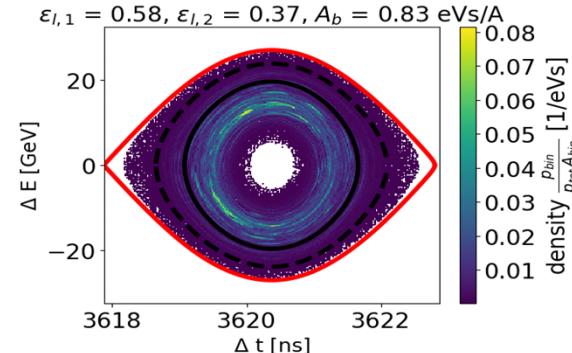


- The dense area remains up to bunch rotation (shortest bunch)
- Structure also for middle and last bunches but less strong

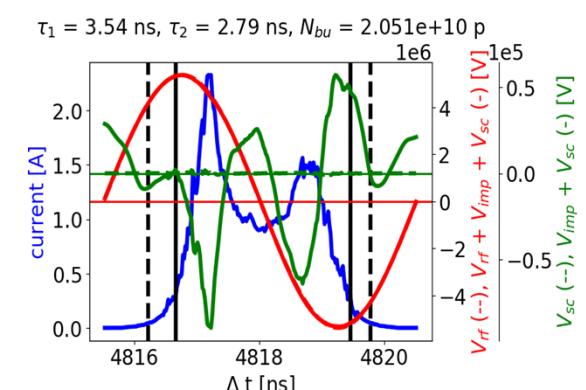
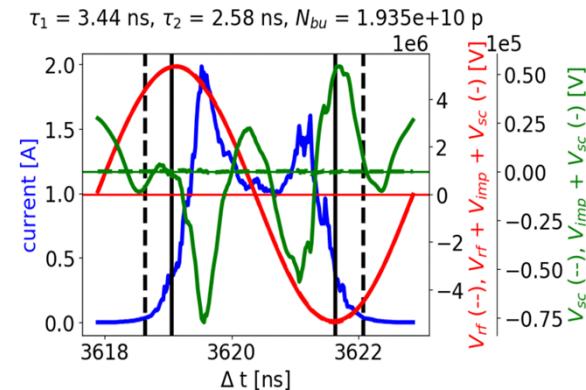
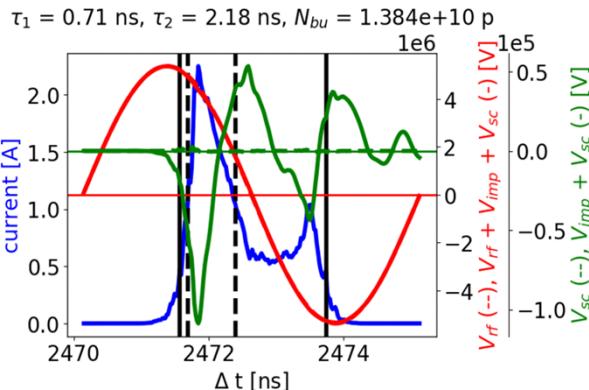
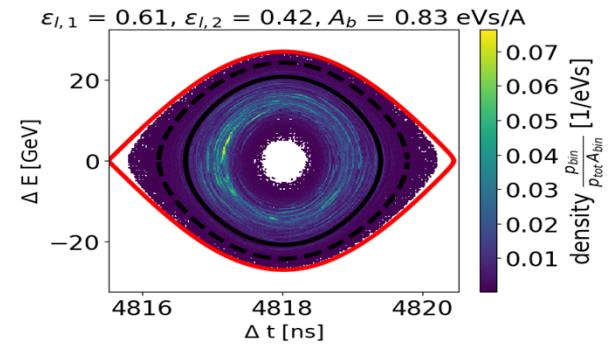
First bunch



Middle bunch



Last bunch

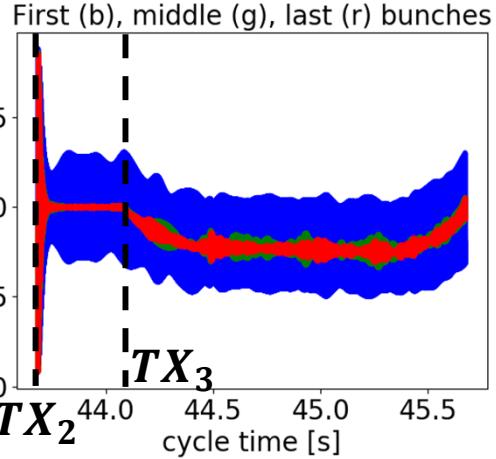


Loss of Landau damping

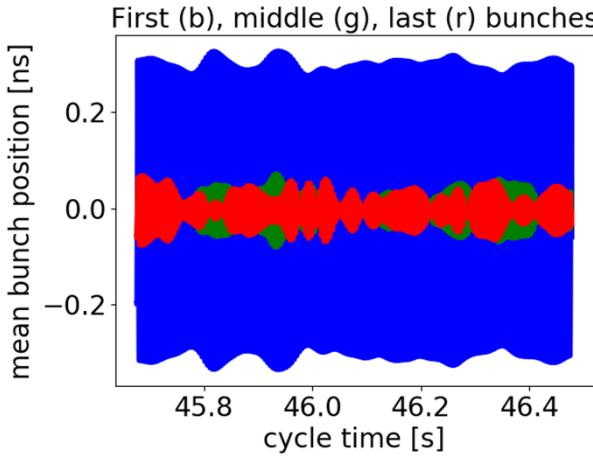


Dipole oscillations with intensity effects

Recapture and ramp



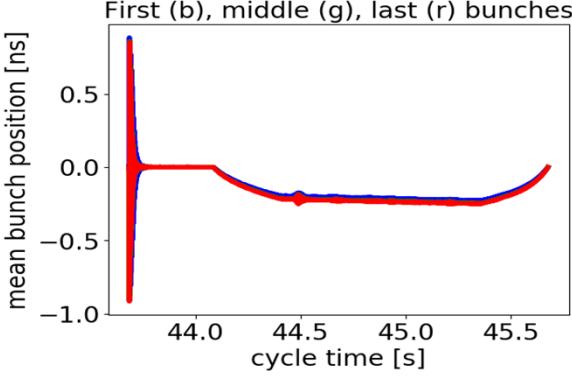
Flat top



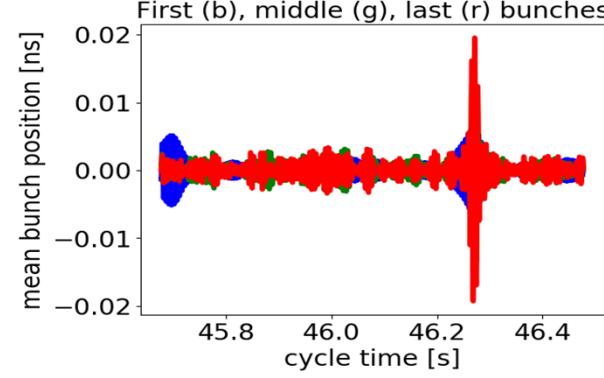
- Large dipole oscillations never damp
- Shortest bunch: amplitude 10% relative to bucket length, LLD at TX_2
- Longest bunch: amplitude 2%, LLD not at TX_2 but at TX_3

Dipole oscillations without intensity effects

Recapture and ramp



Flat top



- Very small dipole oscillations for all bunches
- Amplitude only 0.2 % relative to bucket length

LLD analytical estimations

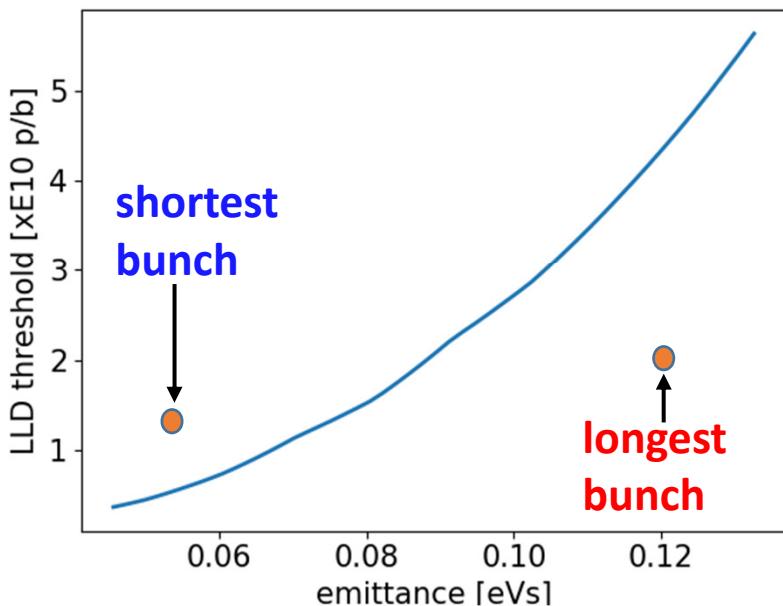


LLD threshold formula

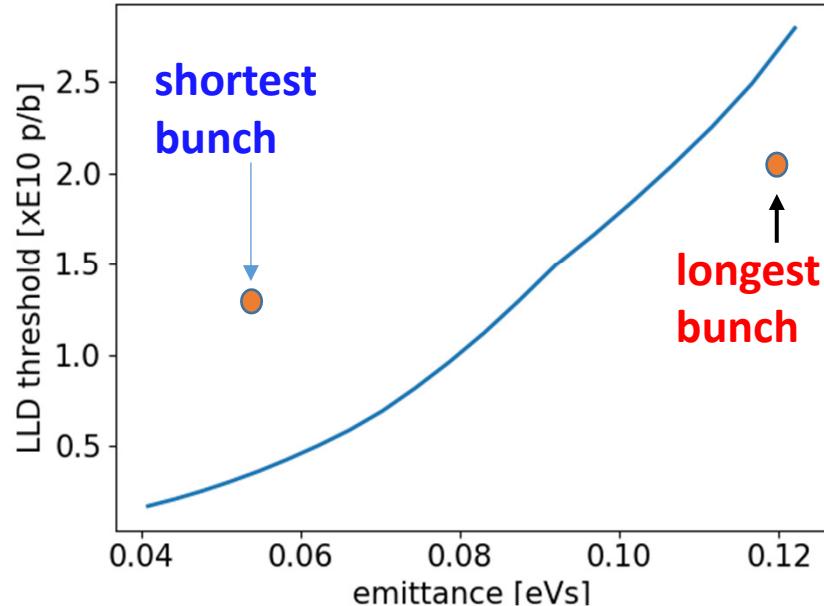
$$N_b < \frac{|\eta|E}{q^2\beta^2} \frac{\tau}{ImZ/n} \left(\frac{\Delta E}{E} \right)^2 \frac{\Delta \omega_s}{\omega_s}$$

$Im Z/n = 3\Omega$ [6]

$V_{rf} = 1.5$ MV (during slip-stacking)



$V_{rf} = 8$ MV (at recapture)

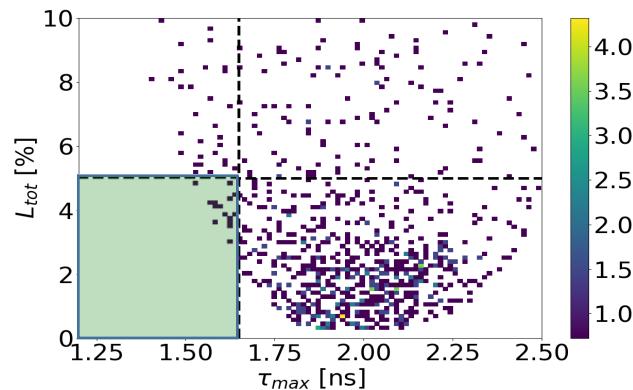


- LLD for shortest bunches even using ‘low’ RF voltage during slip-stacking
- Analytical estimations confirm what seen in simulations
 - LLD for **shortest bunch** at recapture
 - Not LLD for **longest bunch** at recapture

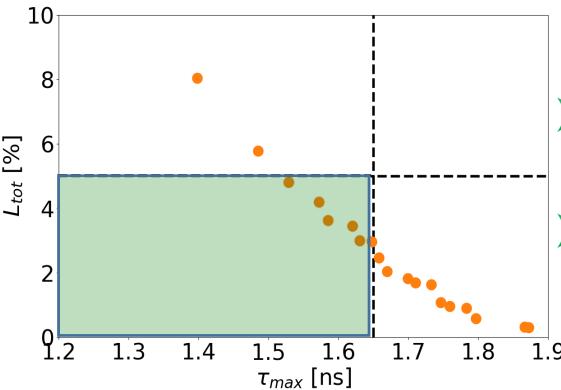
Q22 and Q26: bunch compression

- Lower η_0 \rightarrow lower $q_e^{mss} \propto \eta_0^{1/4}$ \rightarrow significant lower L_{SPS} and S_{LHC}
 \rightarrow we can allow some losses (for example S_{LHC}) to bring batches closer to each other and have a lower τ_{max} which satisfies the requirement

Scan results

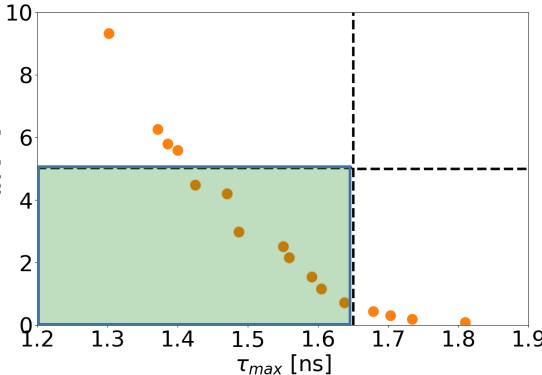
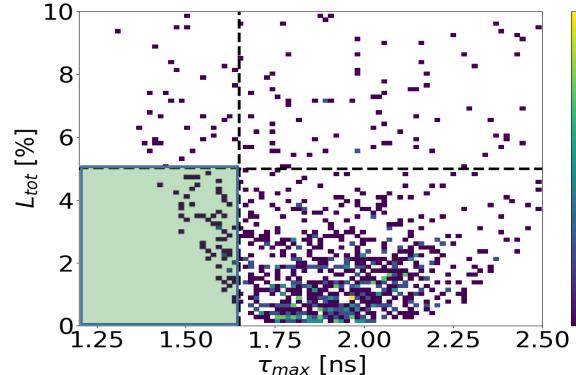


Optimal solutions



Q22

- On average lower L_{tot} and τ_{max} than Q20 optics
- Acceptable margin for constraint fulfillment



Q26

- On average lower L_{tot} and τ_{max} than Q22 optics
- Constraints even better satisfied

- However Q22 and Q26 are more sensitive to IBS and transverse space charge



Conclusions



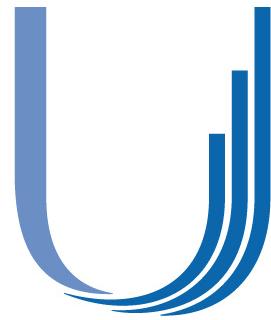
Conclusions

- Momentum slip-stacking for LHC ion beams in SPS after LIU upgrade is fundamental to fulfil the HL-LHC requirements.
- The optimum parameters involved in this complicated beam manipulation have been suggested through simulations.
- An accurate impedance model and realistic beam parameters have been used.
- Simulations show that momentum slip-stacking can be applied under certain conditions, providing at extraction the beam parameters required by the LIU project.
- Intensity effects do not increase losses or bunch length at SPS extraction.
- However loss of Landau damping was observed
 - Analytical estimations confirm what found in simulations
 - Further studies are needed to find possible cures



References

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- [2] J. Eldred, “Slip-Stacking Dynamics for High-Power Proton Beams at Fermilab.” PhD thesis, 2015.
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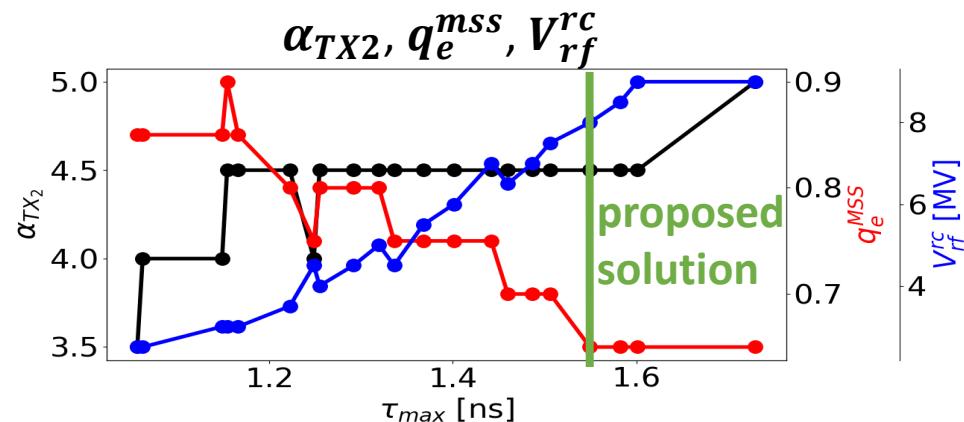
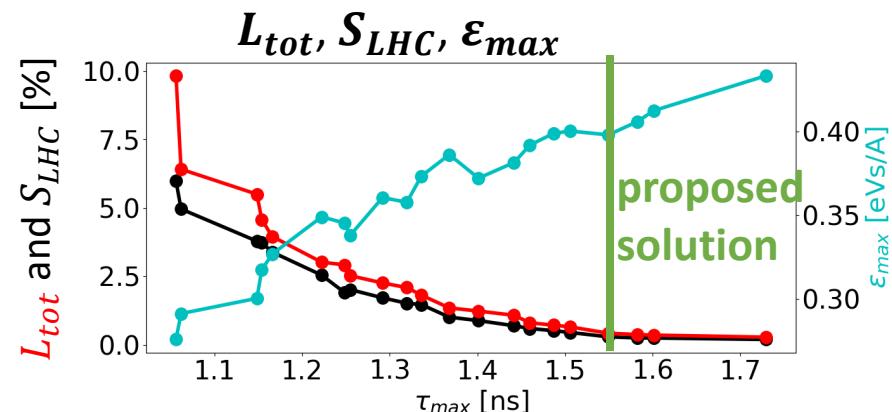


LHC Injectors Upgrade

THANK YOU FOR YOUR ATTENTION!



APPENDIX 1. Parameter behaviours for the optimal solutions (Q20 optics, rotation)



- All optimal solutions have roughly the same α_{TX2} as expected
 - Different configurations with same α_{TX2} are similar from a slip-stacking perspective
- $\alpha_{TX2} \approx 4$, because 4 is the lower limit for stability and the solutions are optimal
 - $\alpha_{TX2} = 4.5$ is preferable (margin due to highest emittance bunches filling the bucket)
- Qualitatively, a **lower τ_{max}** implies
 - **Lower ϵ_{max}** (lower emittance for lower bunch length at extraction)
 - **Lower V_{rf}^{rc}** (bucket area after recapture has to decrease)
 - **Lower ΔE_b** (otherwise particles outside the recapture bucket will be lost)
 - **Higher S_{LHC}** (stronger perturbations due to lower ΔE_b)
 - **Lower H_b and $V_{rf,1}$** (α_{TX2} is roughly constant)
 - **Higher q_e^{mss}** (it scales as $V_{rf,1}^{-1/4}$)
 - **Higher L_{SPS}** (due to higher q_e^{mss}) and L_{tot}

APPENDIX 2. Proposed solution: capture and ramp, no intensity effects

- Without intensity effects the hollow bunches are uniform
- The two peaks of the line density have the same height

