

Beam Dynamics issues for multi-pass ERLs

ERL workshop 07/19/2017

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Cornell Laboratory for
Accelerator-based Sciences and
Education (CLASSE)



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- b) halo dynamics
- c) HOM heating
- d) Intra-Beam Scattering
- e) Touschek scattering
- f) Rest Gas scattering
- g) Ion accumulation
 - i) optics changes
 - ii) nonlinear dynamics
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| f) Rest Gas scattering | |
| g) Ion accumulation | 3. Transport of damaged beam |
| i) optics changes | a) Phase space rotation for energy spread |
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→ All of the above, only worse!



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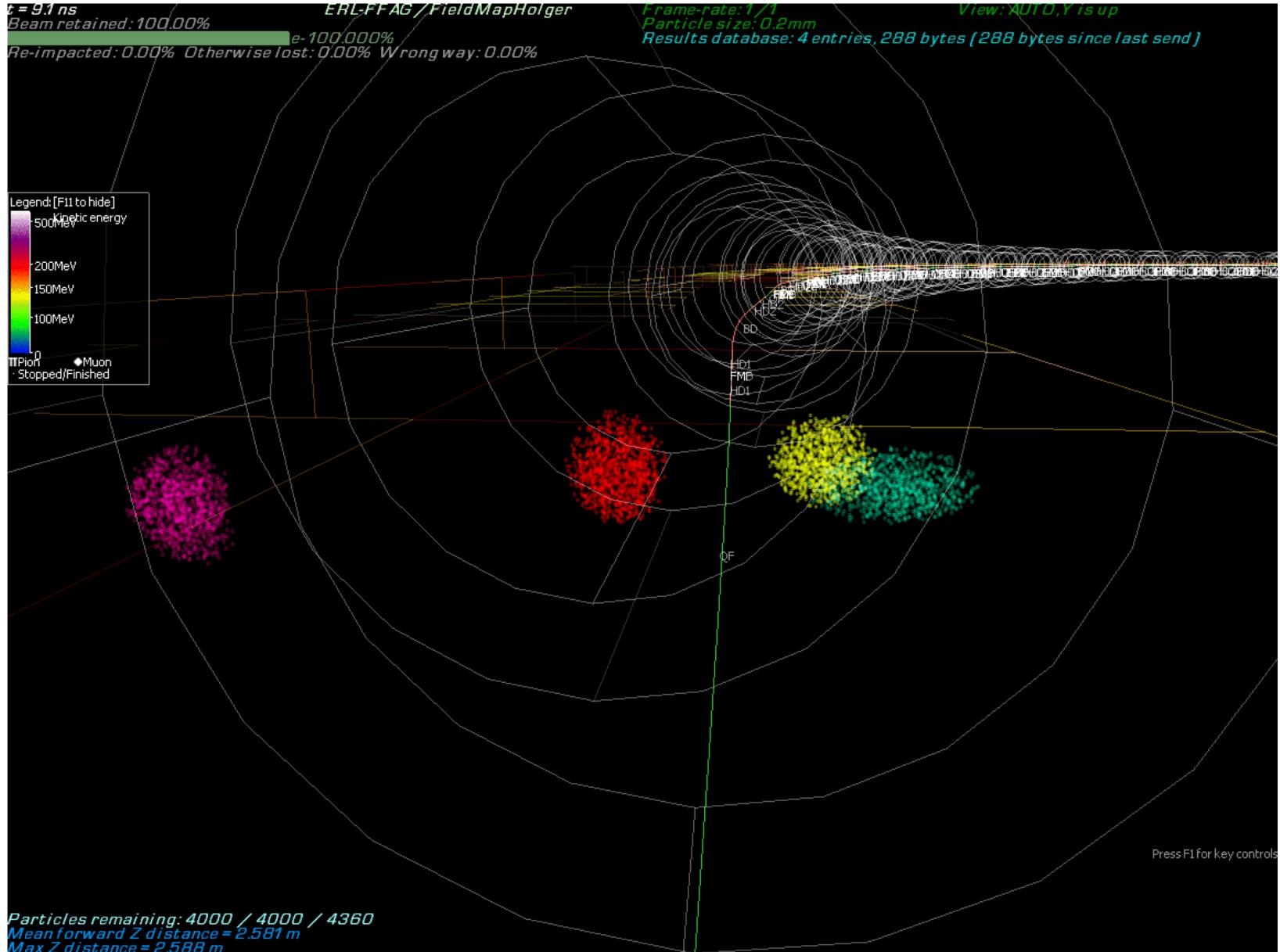
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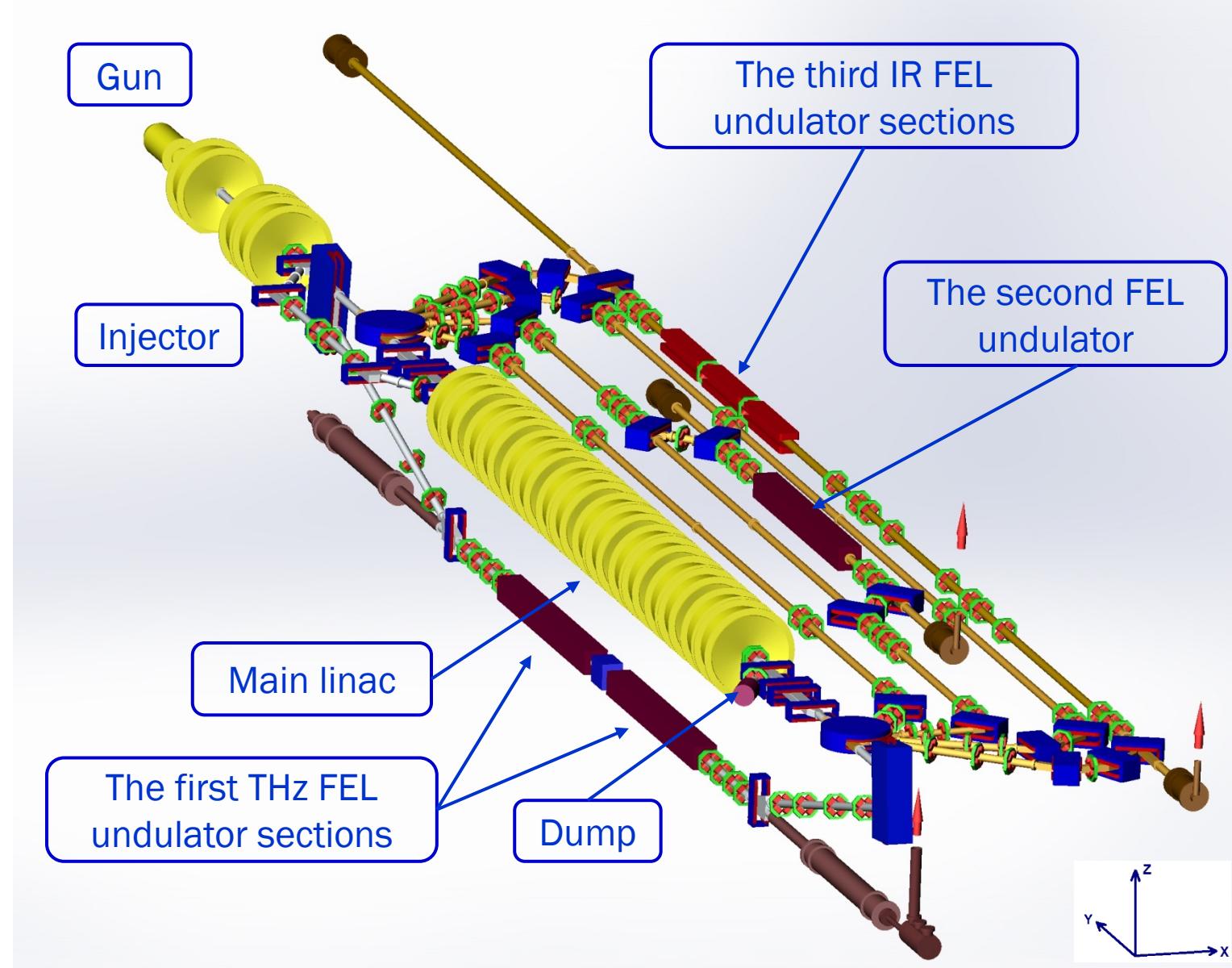
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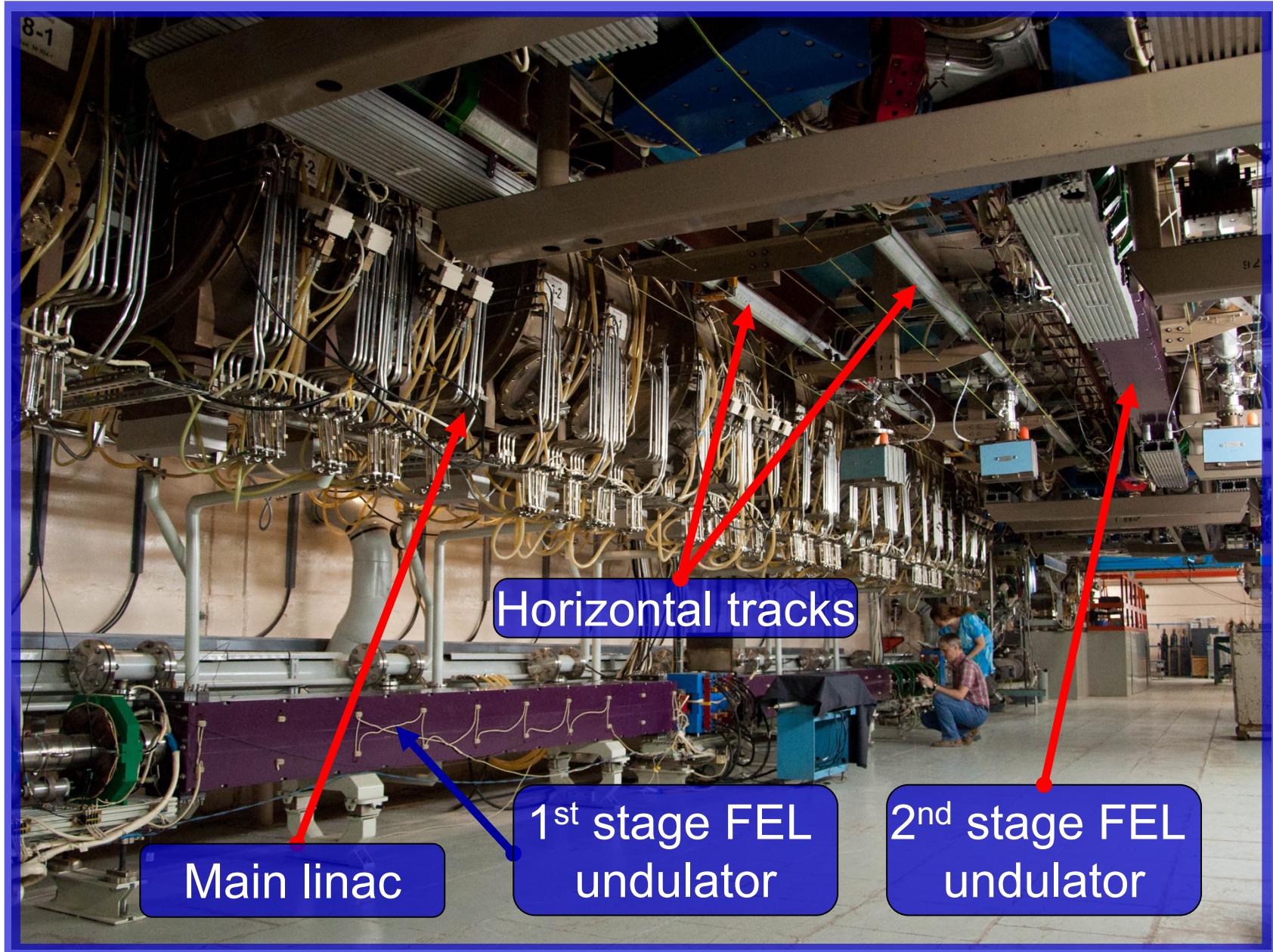
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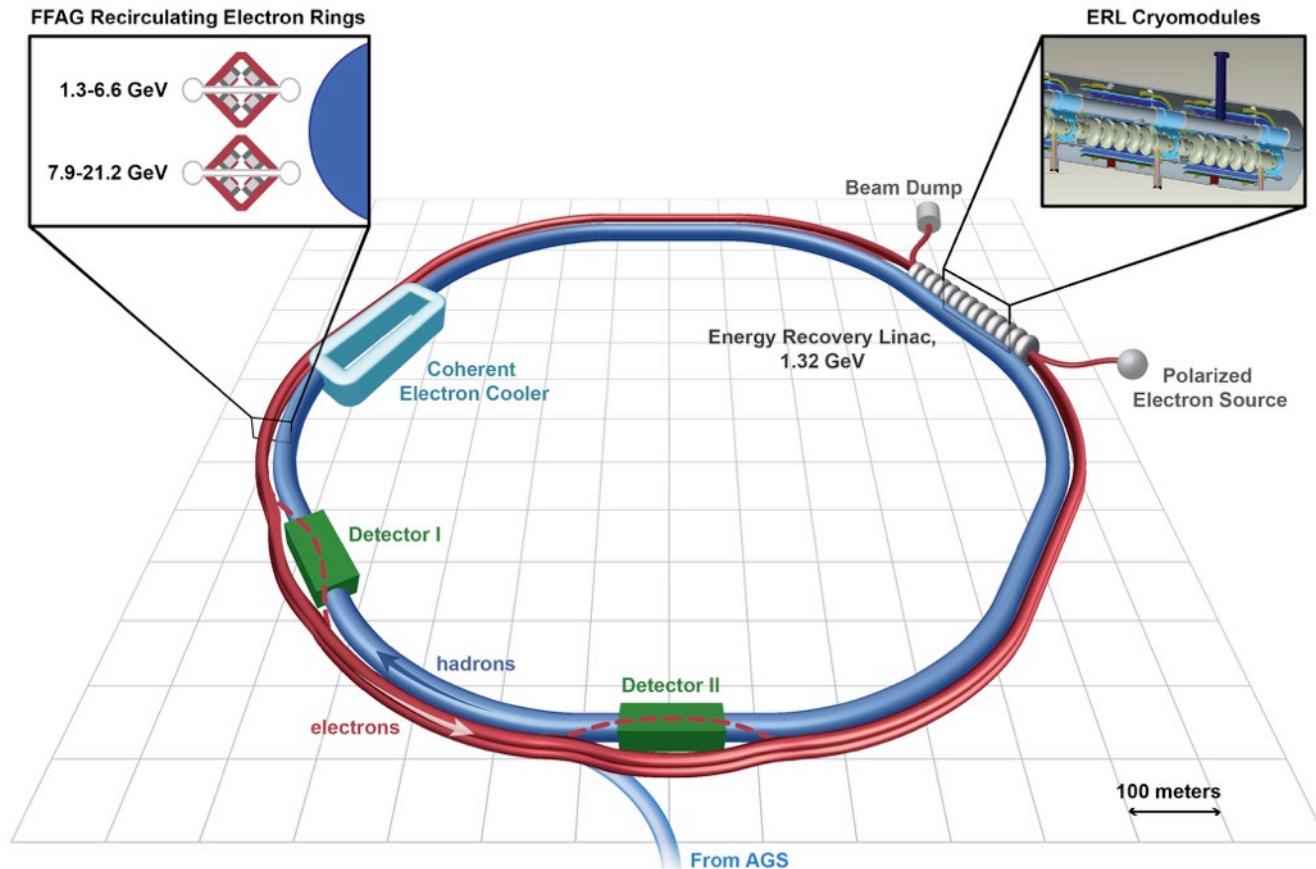
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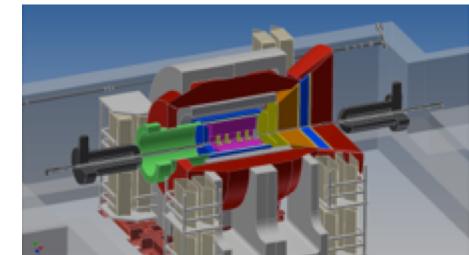




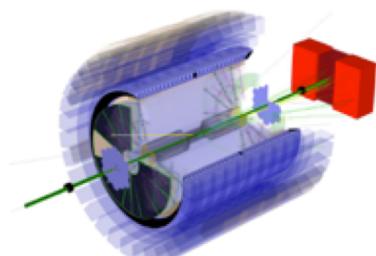




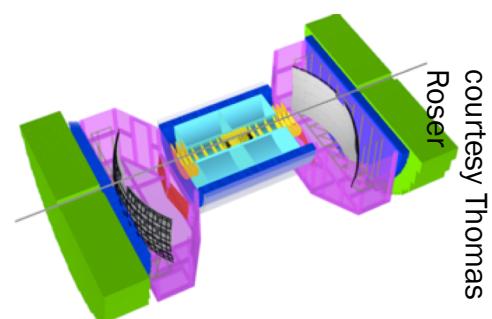
ePHENIX



eSTAR



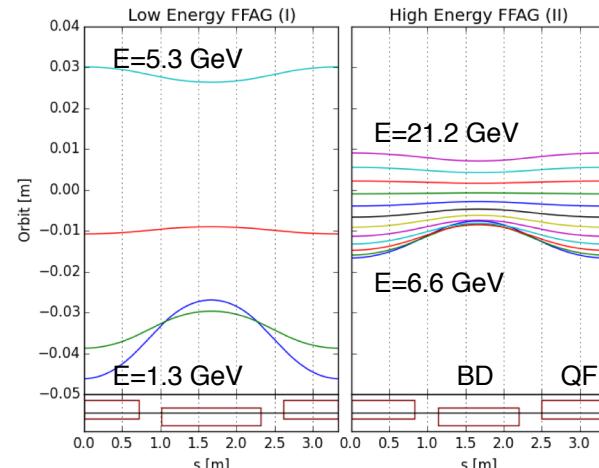
BeAST



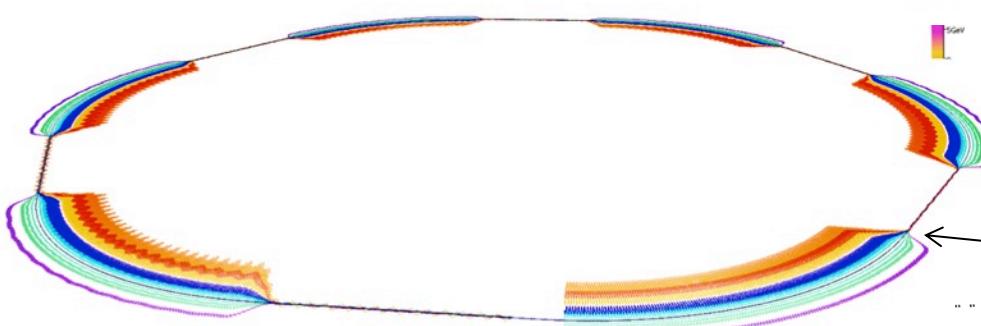
- $1.7 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$ for $\sqrt{s} = 127 \text{ GeV}$ (15.9 GeV e \uparrow on 255 GeV p \uparrow)
- $\times 10$ luminosity with modest improvements (coating of RHIC vacuum chamber)
- $\times 100$ luminosity with shorter bunch spacing (ultimate capability)



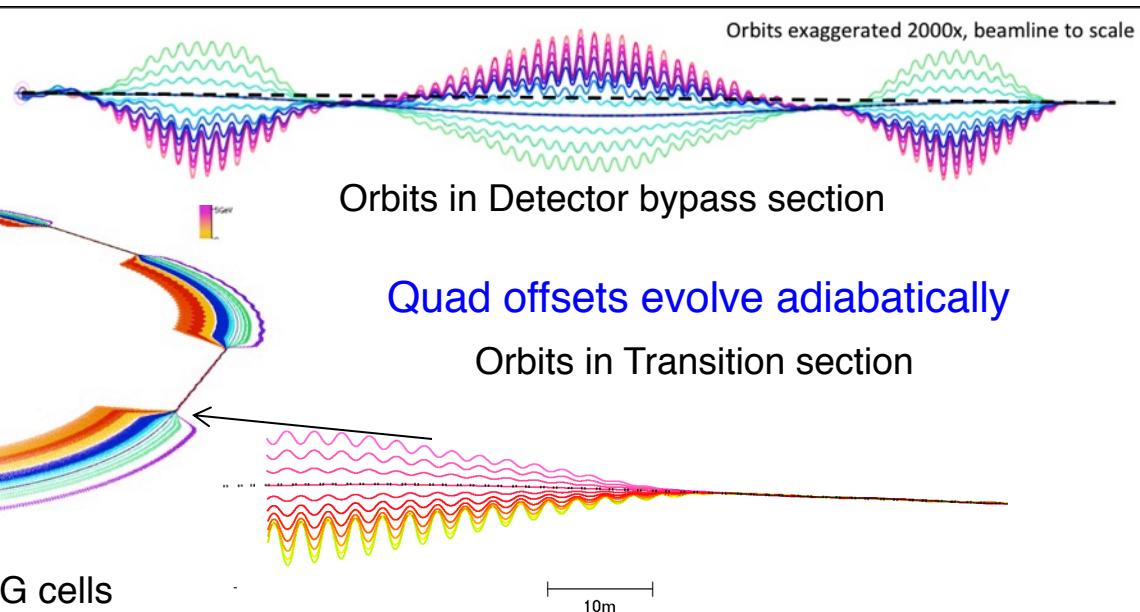
- eRHIC uses two FFAG beamlines to do multiple recirculations.
(FFAG-I: 1.3-5.4 GeV, FFAG-II: 6.6-21.2 GeV)
- All sections of a FFAG beamline is formed using a same FODO cell. Required bending in different sections is arranged by proper selection of the offsets between cell magnets (or, alternatively, with dipole field correctors).
- Permanent magnets can be used for the FFAG beamline magnets (no need for power supplies/cables and cooling).



@S.Brooks, D.Trbojevic



Each of two eRHIC FFAGs contain 1066 FFAG cells





CBETA study topics important for eRHIC:

1) FFAG loops with a factor of 4 in momentum **aperture**.

- a) Precision, reproducibility, alignment during magnet and girder production.
- b) Stability of magnetic fields in a radiation environment.
- c) **Matching** and correction of multiple simultaneous **orbits**.
- d) **Matching** and correction of multiple simultaneous **optics**.
- e) **Path length control** for all orbits.

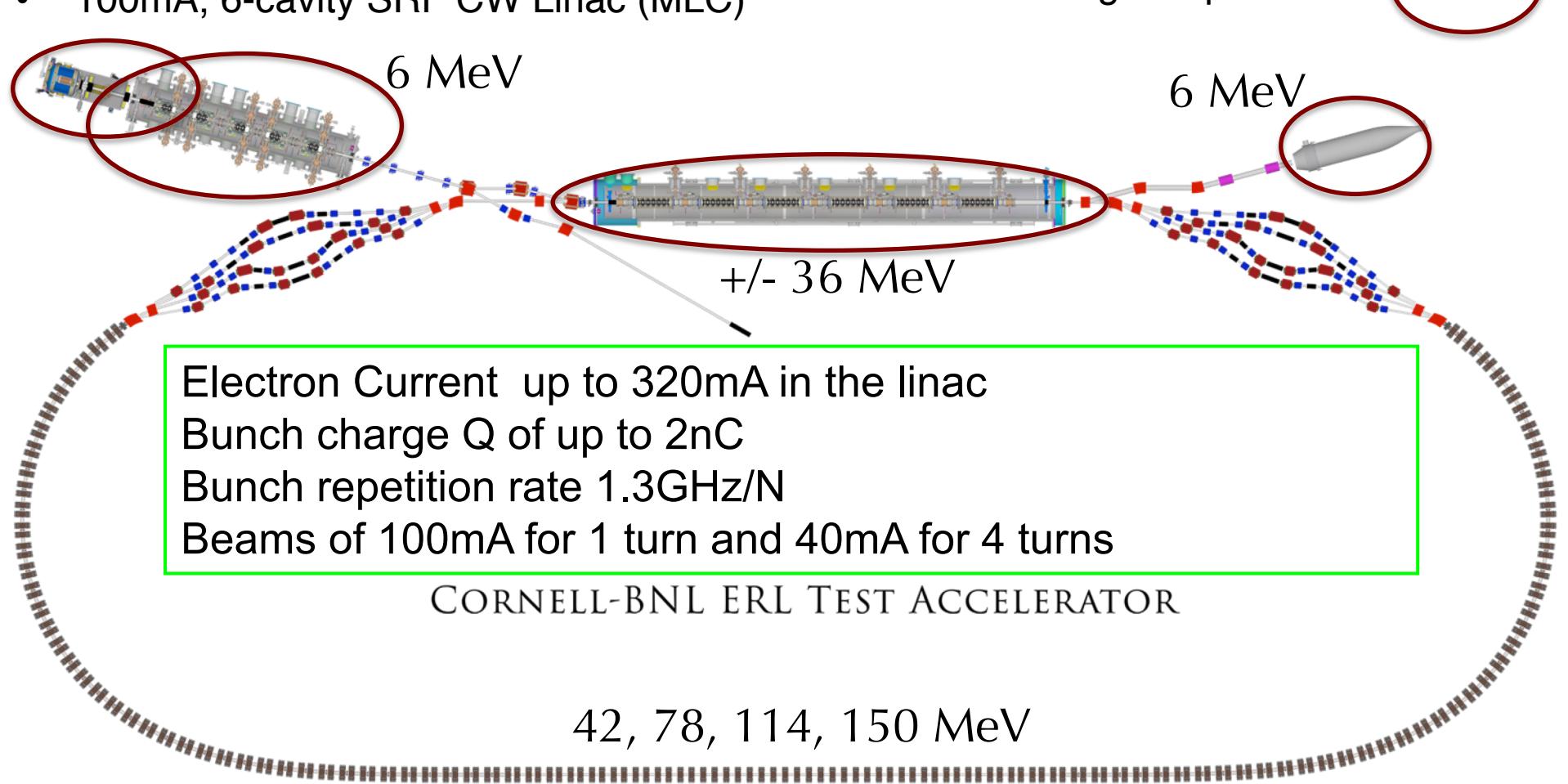
2) Multi-turn ERL operation with a large number of turns.

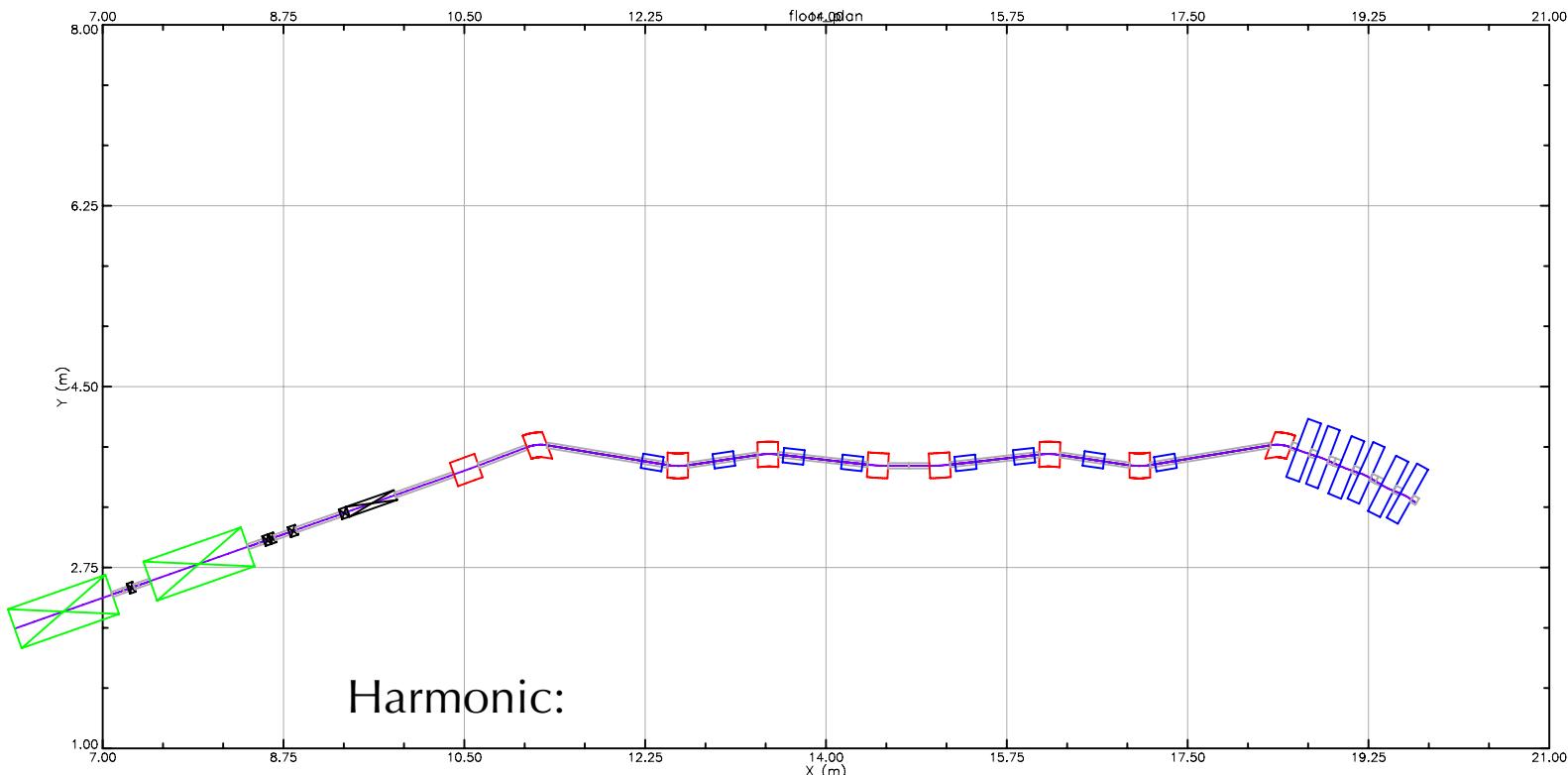
- a) **HOM damping**.
- b) **BBU limits**.
- c) **LLRF control and microphonics**.
- d) **ERL startup from low-power beam**.



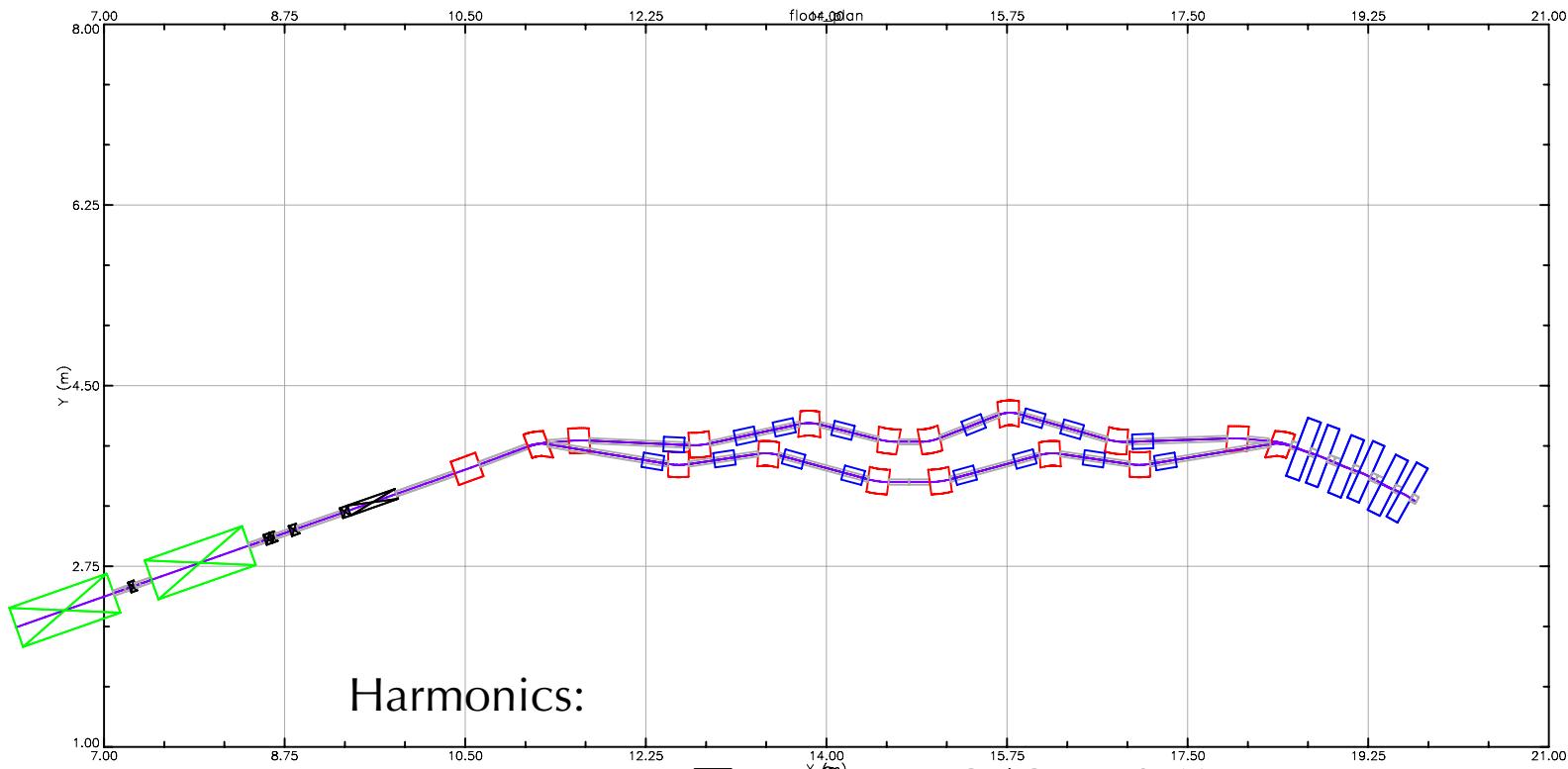
- Cornell DC gun
- 100mA, 6MeV SRF injector (ICM)
- 600kW beam dump
- 100mA, 6-cavity SRF CW Linac (MLC)

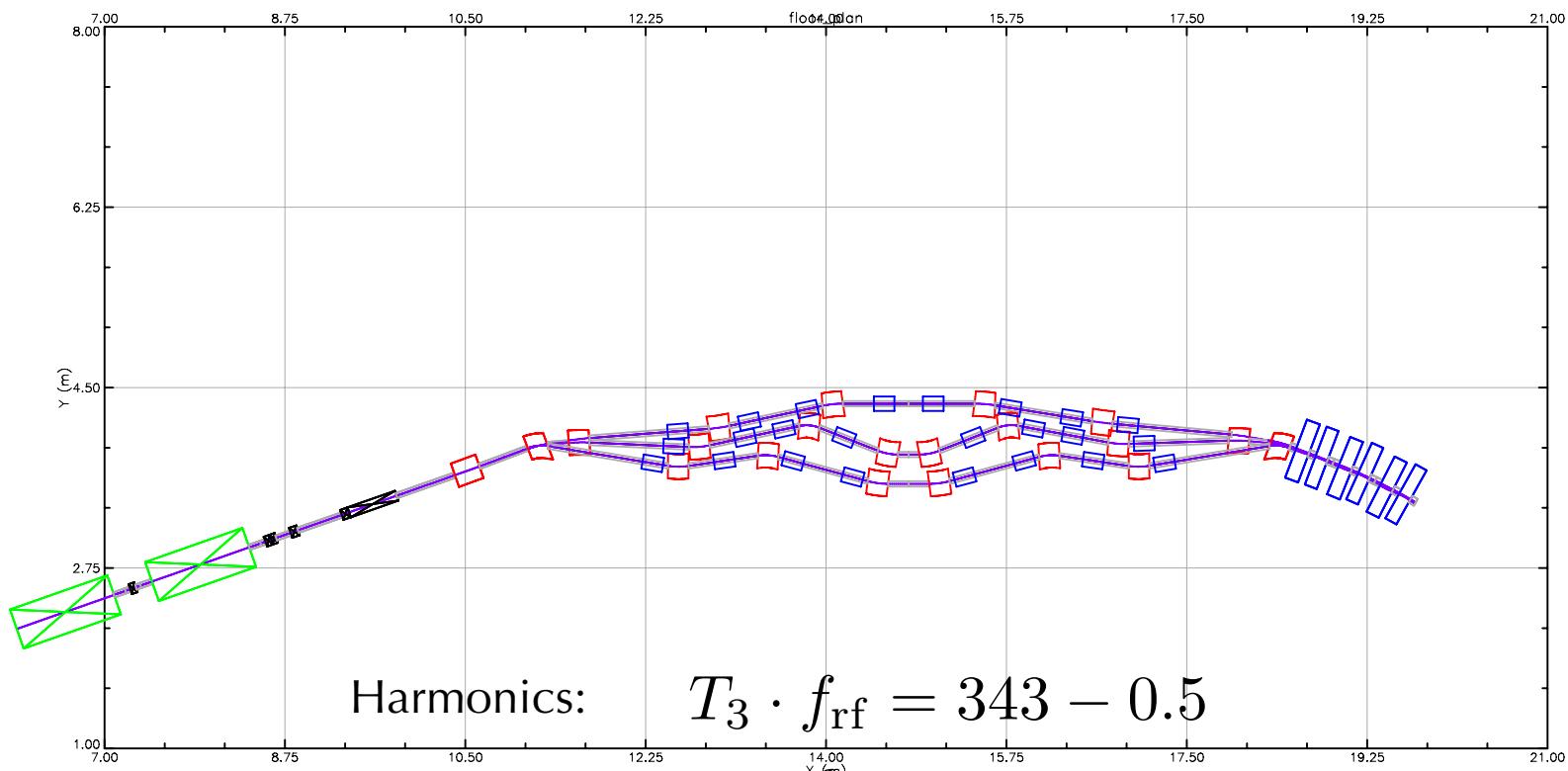
Existing components at Cornell





$$T_1 \cdot f_{\text{rf}} = 343 - 0.5$$

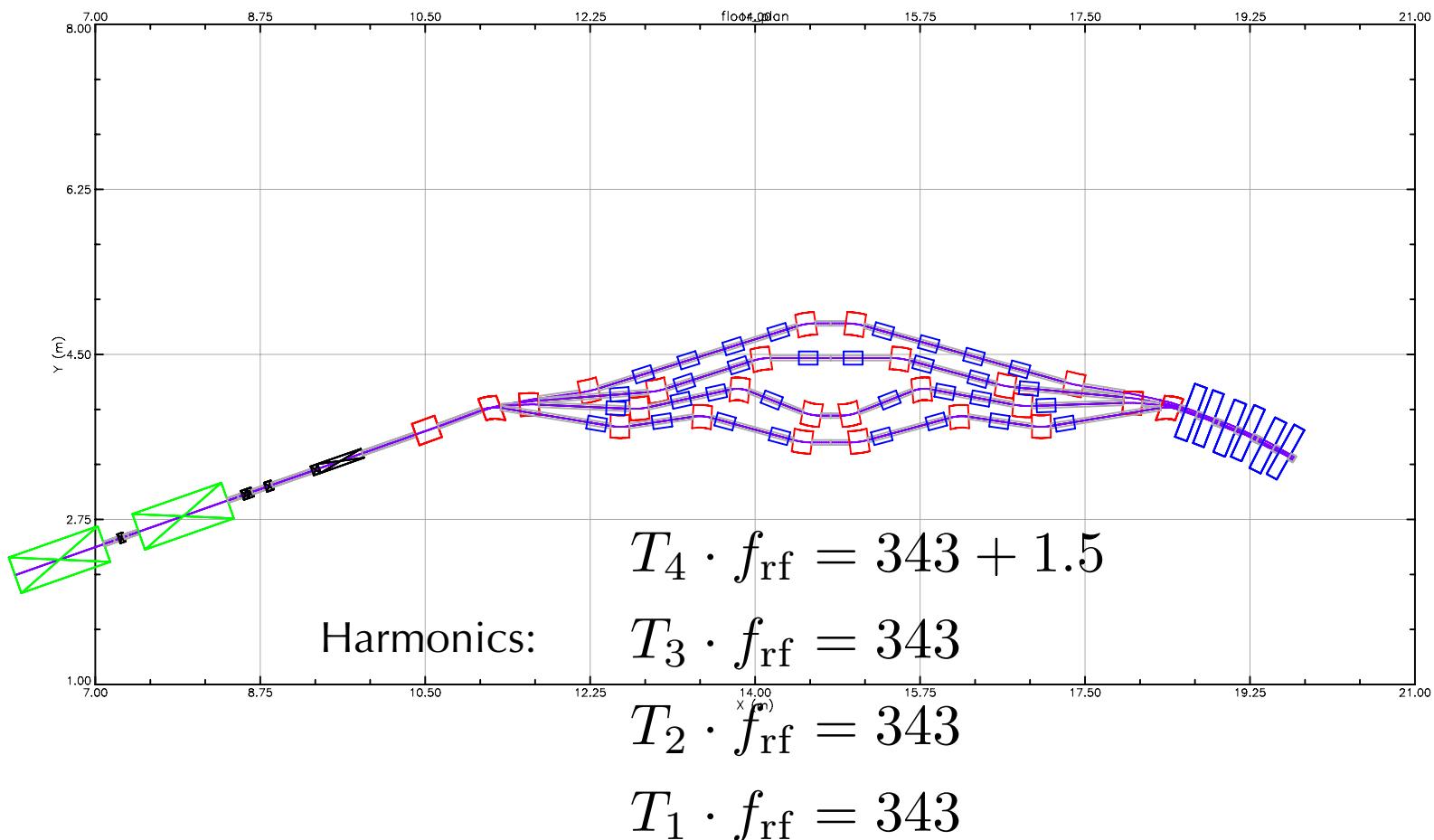




$$\text{Harmonics: } T_3 \cdot f_{\text{rf}} = 343 - 0.5$$

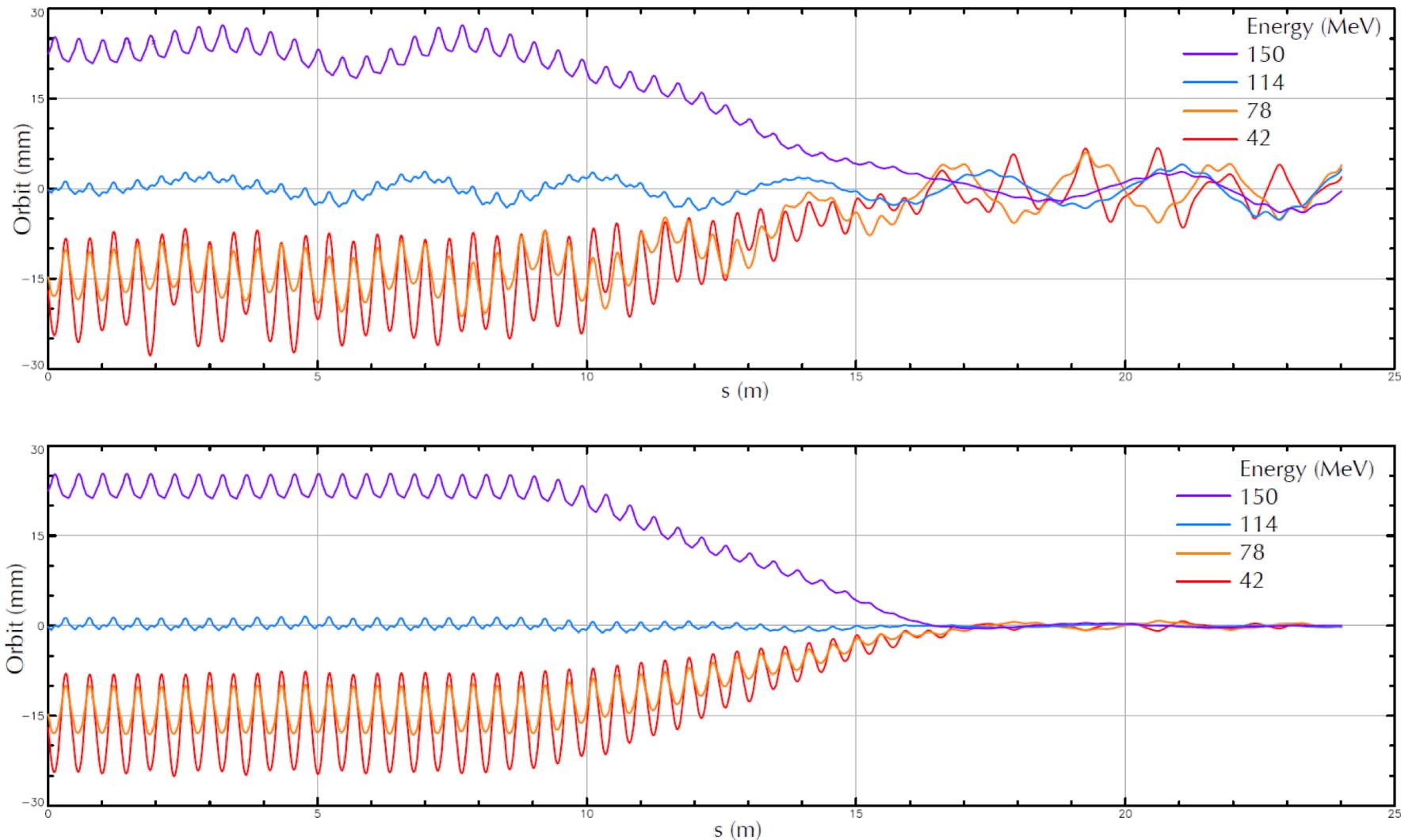
$$T_2 \cdot f_{\text{rf}} = 343$$

$$T_1 \cdot f_{\text{rf}} = 343$$





Orbit Correction of 4 Beams



Courtesy C. Mayes



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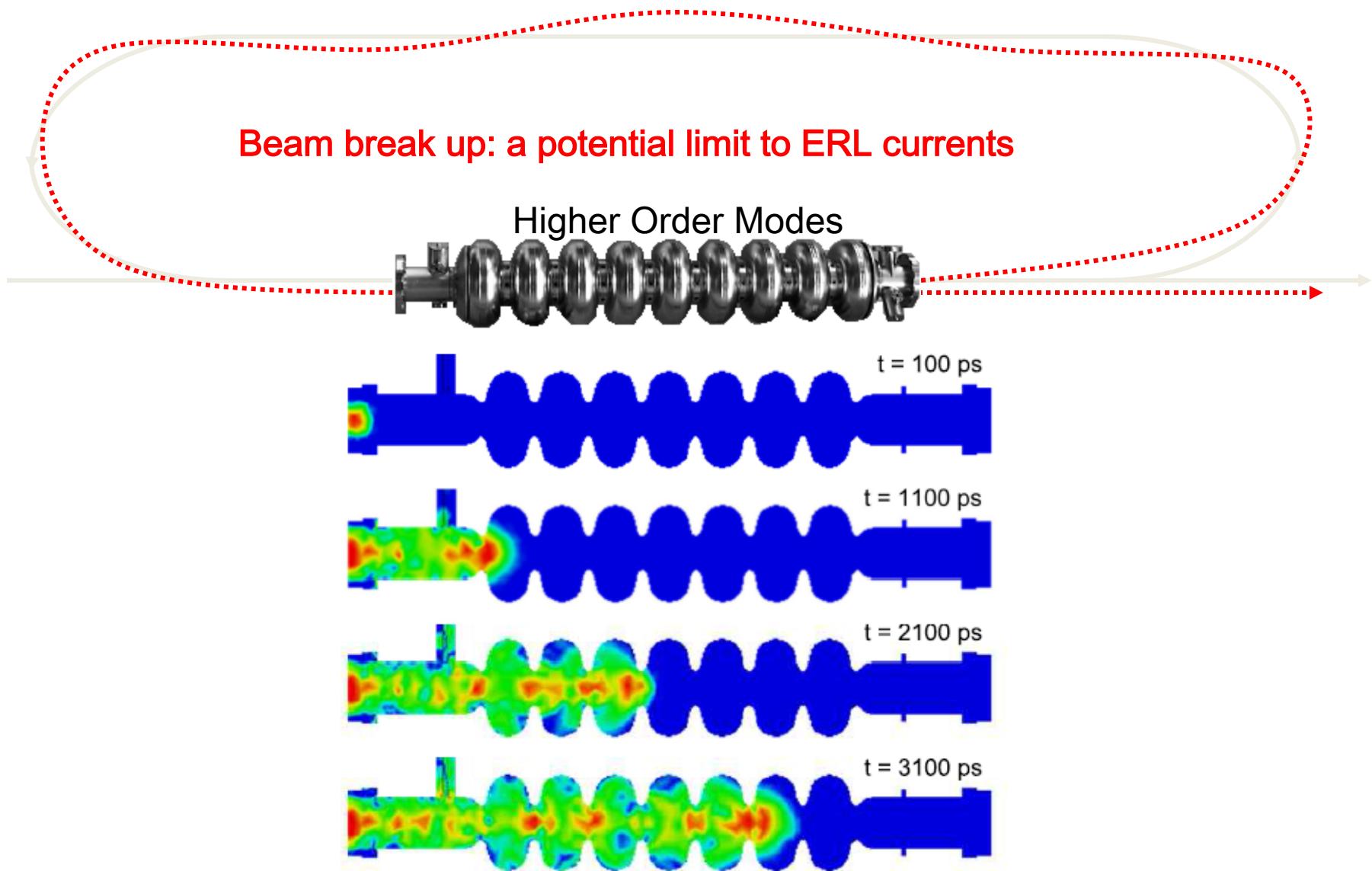
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$$V_x(t) = T_{12} \frac{e}{c} \int_{-\infty}^t W_x(t-t') V_x(t'-t_r) I(t') dt'$$



Beam break up: a potential limit to ERL currents

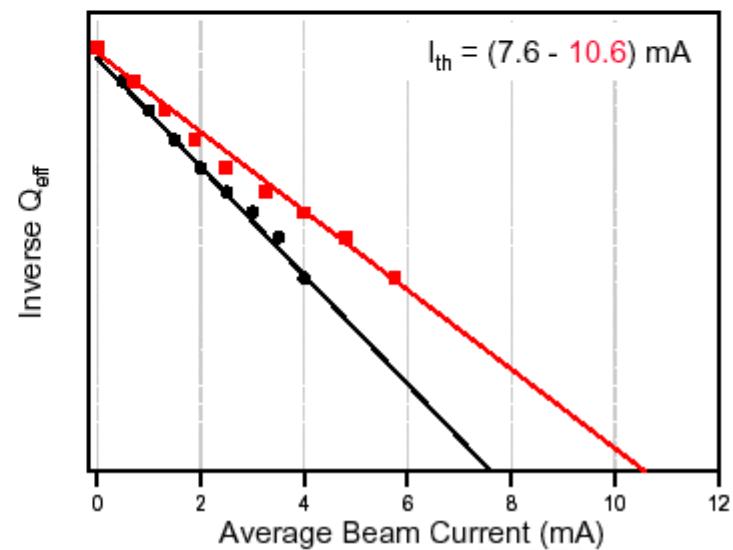
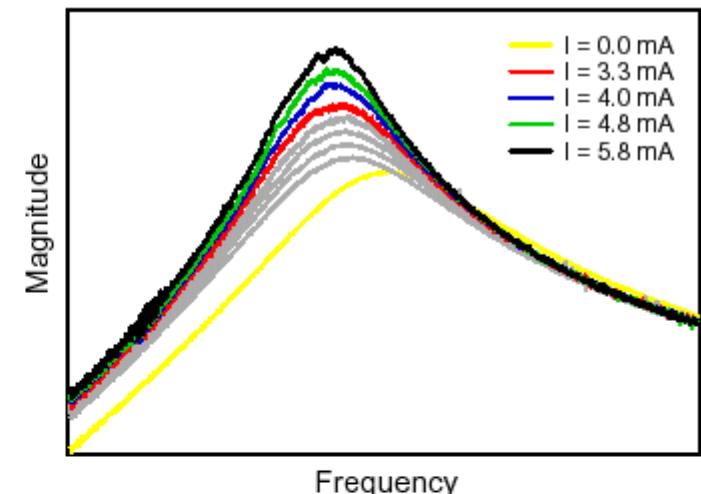
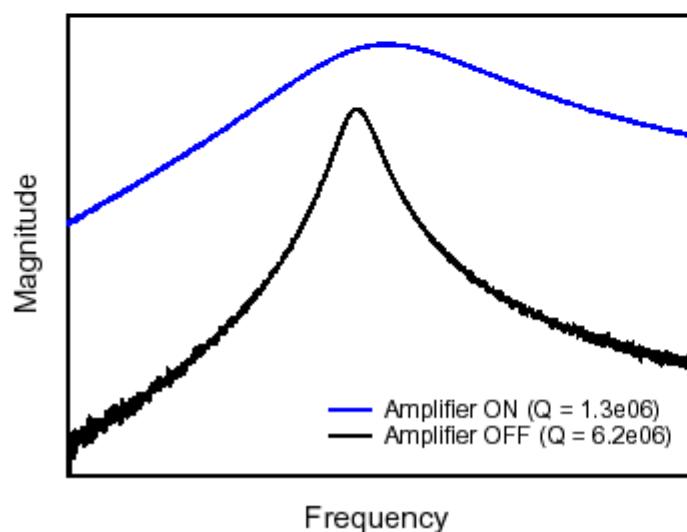


$$V_x(t) = T_{12} \frac{e}{c} \int_{-\infty}^t W_x(t-t') V_x(t'-t_r) I(t') dt'$$



Recall... $I_{threshold} \propto \frac{1}{Q_{HOM}}$

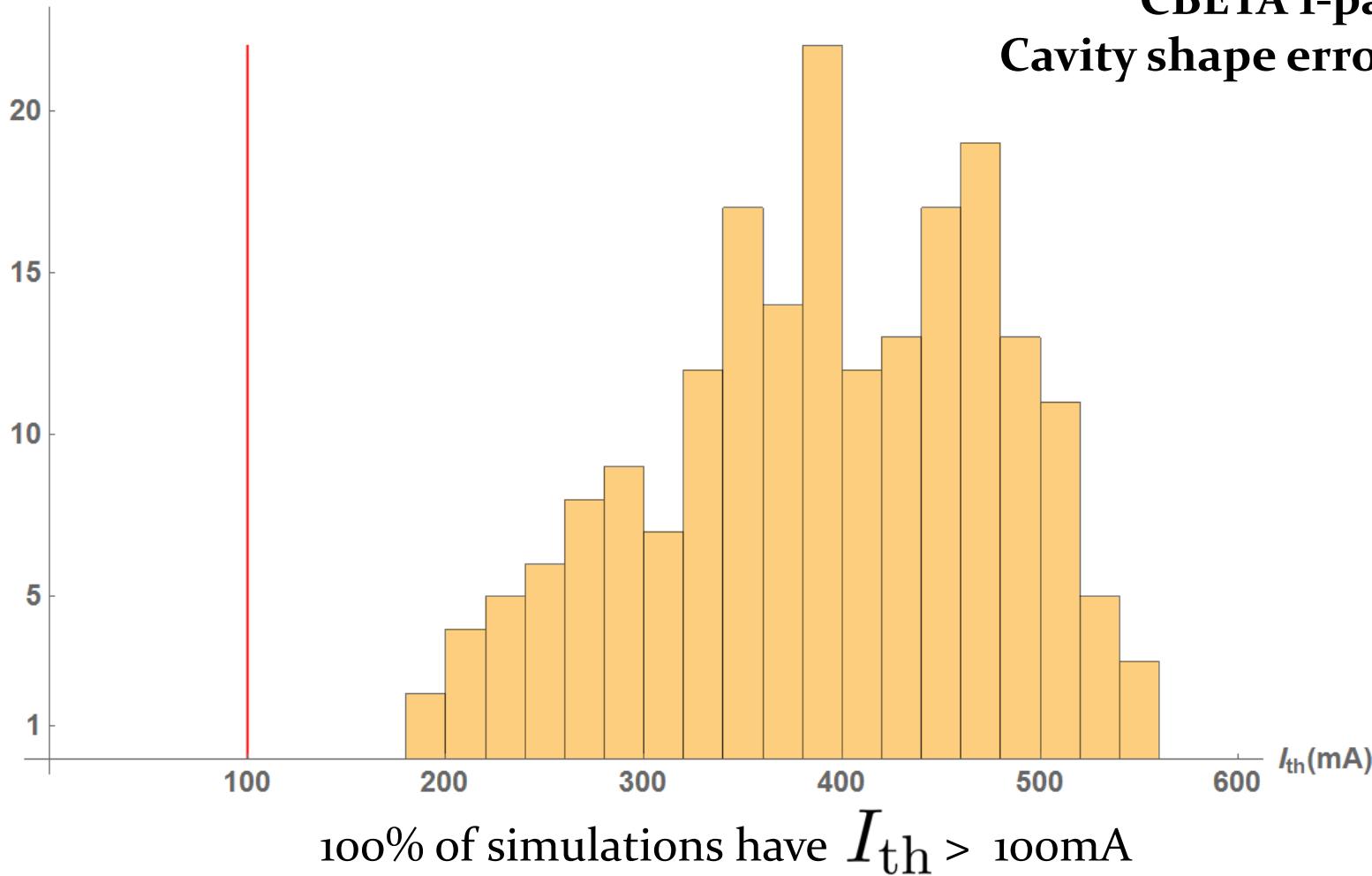
- Damping circuit easily reduced the Q of the 2106 MHz mode by a factor of 5
(Above a factor of about 10, the system becomes sensitive to external disturbances)
- The threshold is increased accordingly: from 2 mA to ~10 mA

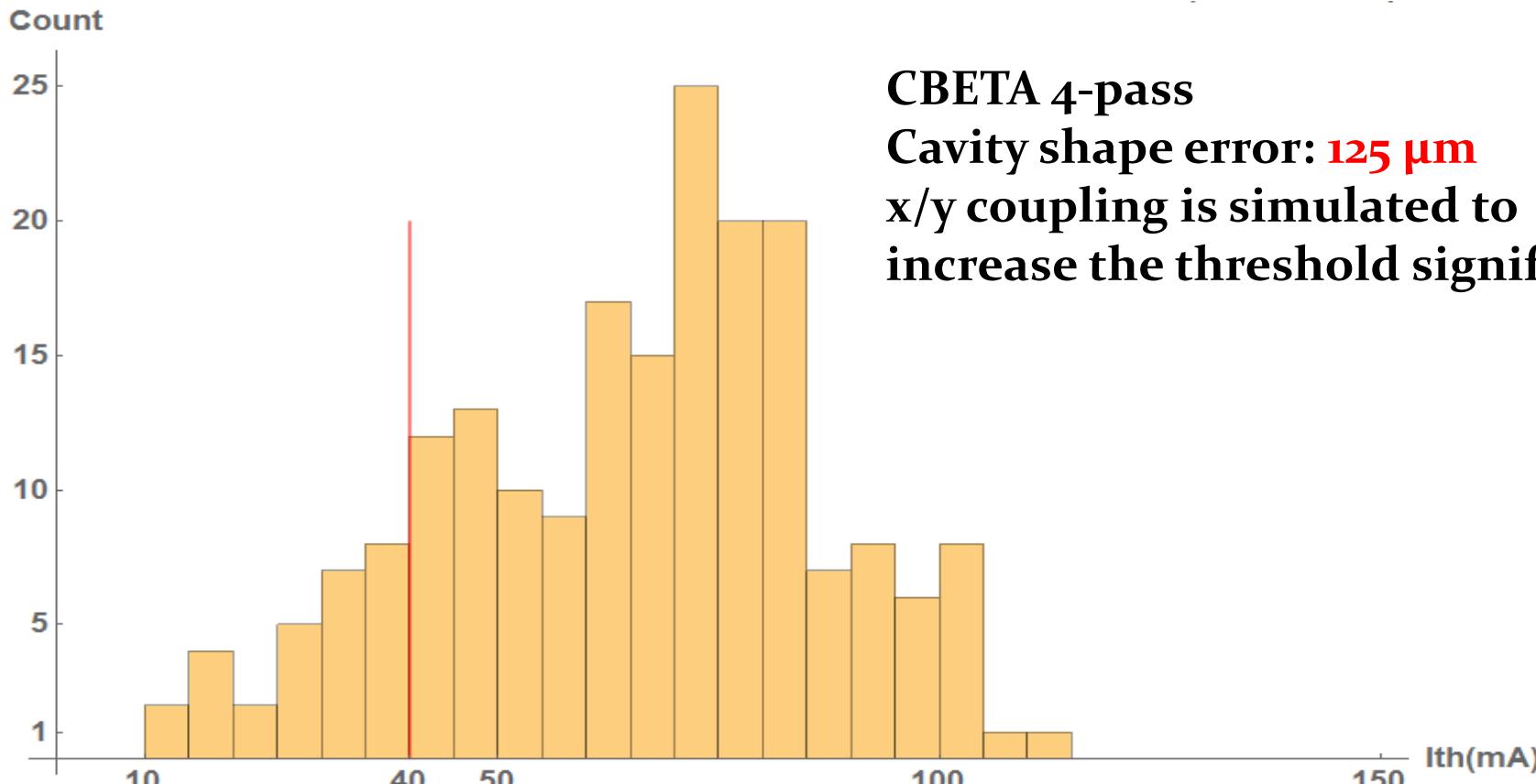




Count

CBETA 1-pass
Cavity shape error: 125 μm





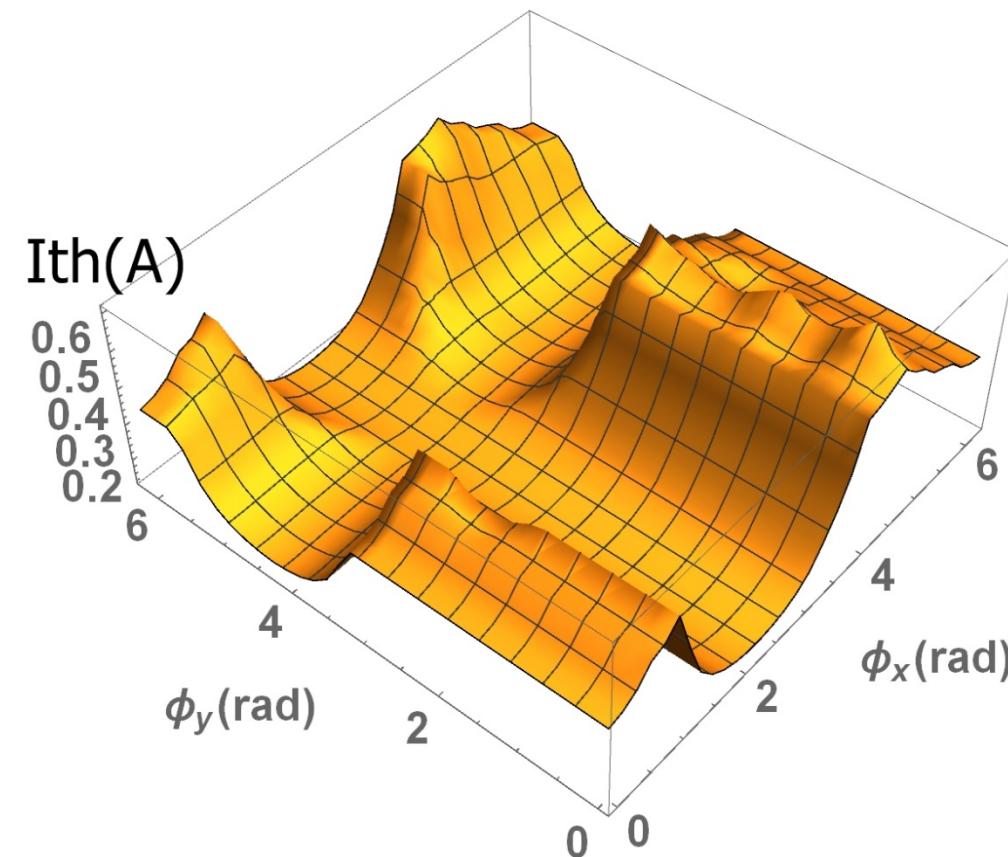
CBETA 4-pass
Cavity shape error: 125 μ m
x/y coupling is simulated to increase the threshold significantly

100% of simulations have $I_{th} > 100$ mA

86% of simulations have $I_{th} > 40$ mA



I_{th}

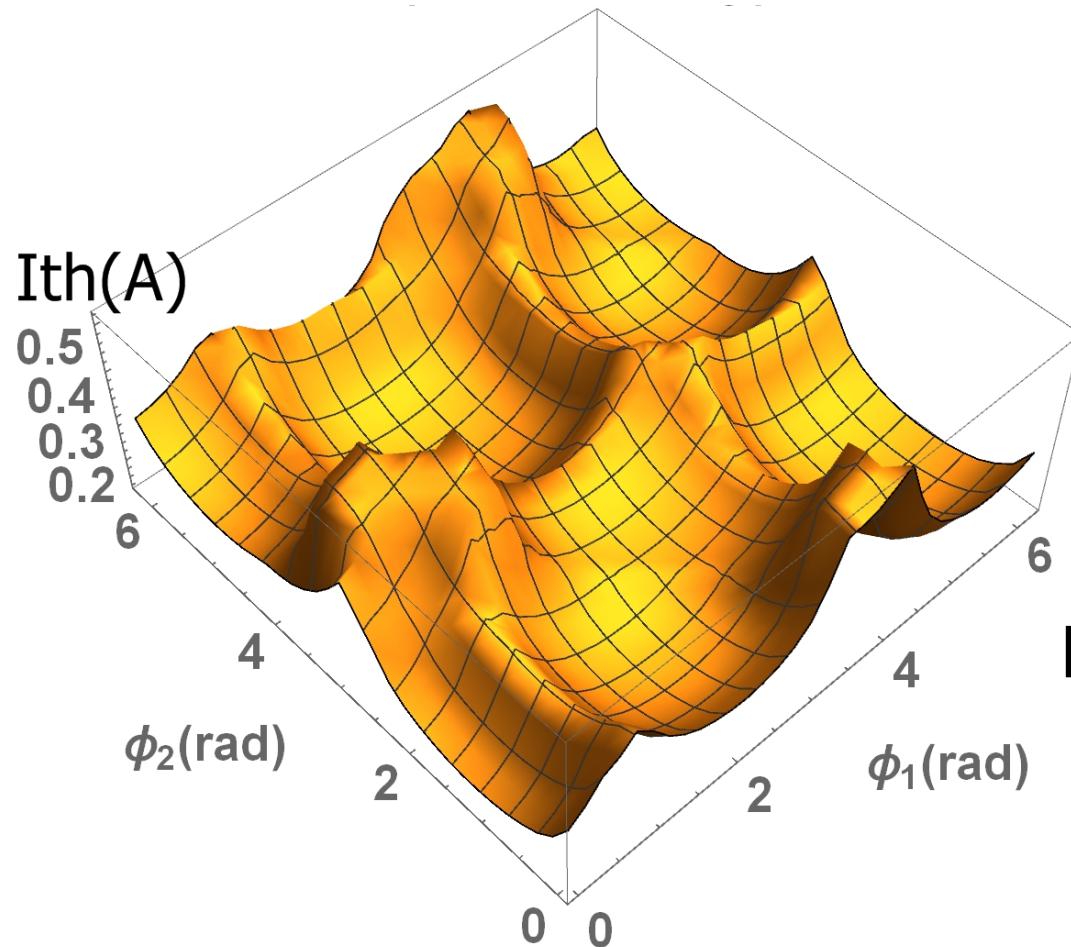


Min = 140 mA
Max = 611 mA
nominal = 342 mA

I_{th} results can improve significantly



I_{th}

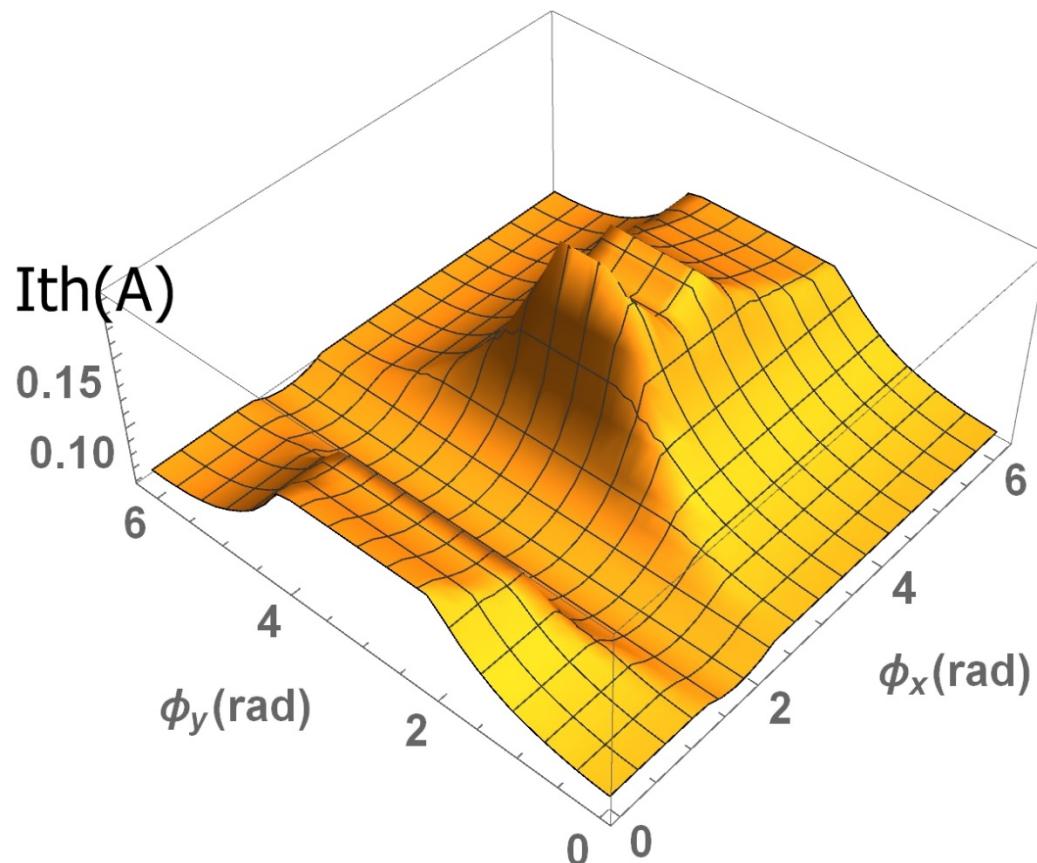


Min = 140 mA
Max = 520 mA
nominal = 342 mA

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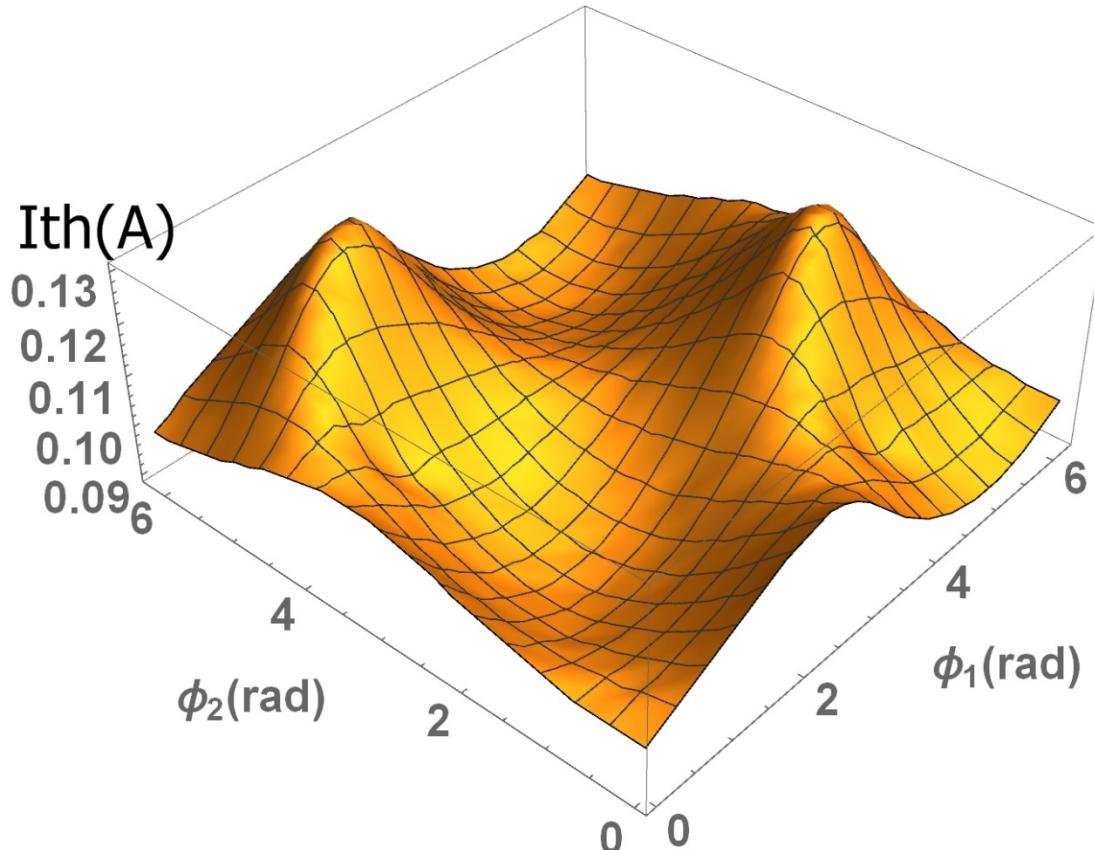


I_{th}



Min = 61 mA
Max = 193 mA
Nominal = 69 mA

I_{th} results can improve

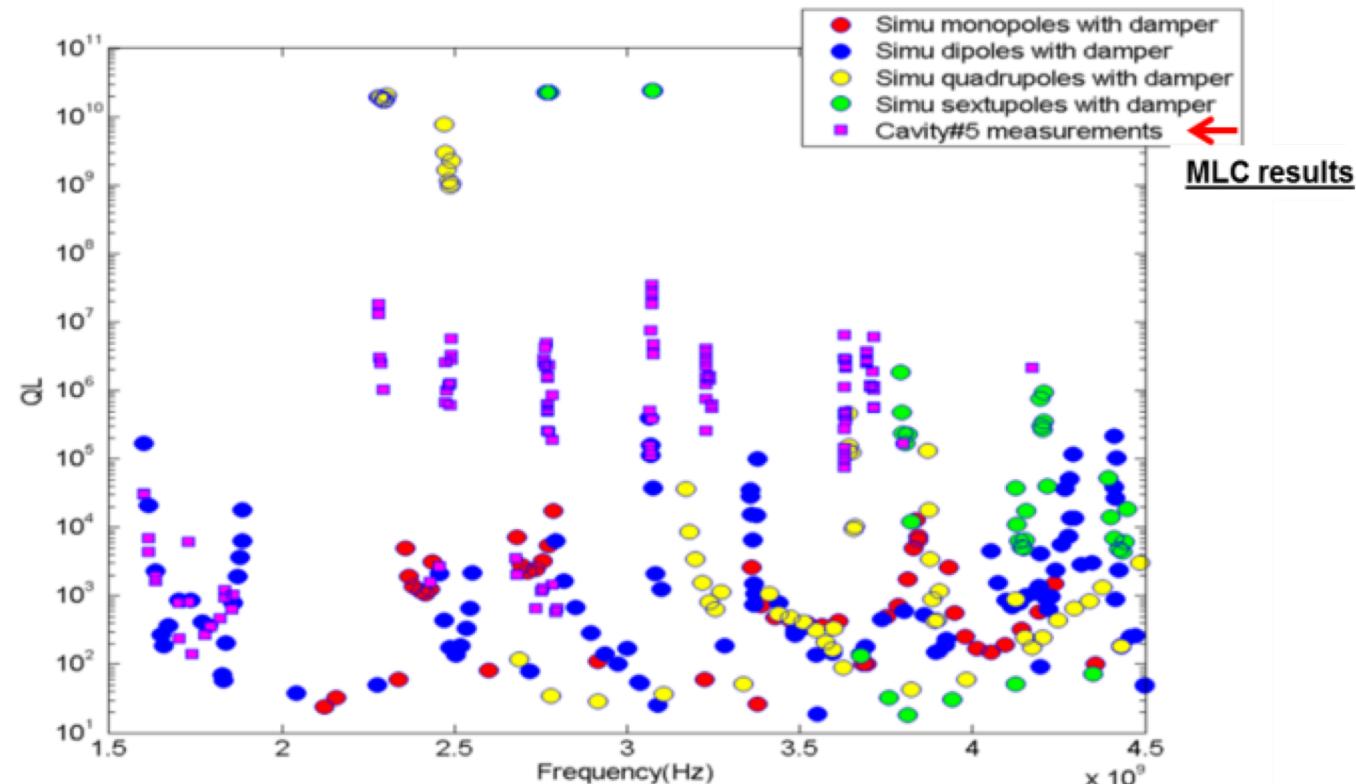
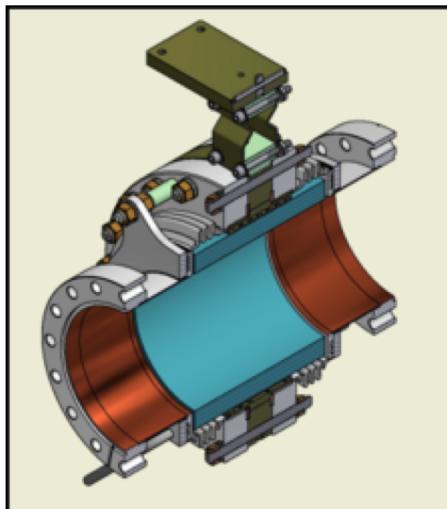


Min = 89 mA
Max = 131 mA
Nominal = 69 mA

I_{th} results can improve

Conclusion: In 1-path ERLs the benefit from coupling and phase optimization can be significant. In multi-turn ERLs this benefit is much diminished.

Current limits from HOMs



Dipole HOMs on MLC were strongly damped below $Q \sim 10^4$.
Consistent with HTC and simulation results.

HTC results were:

- **HOM heating: currents are limited to < 40mA in CBETA**
- **BBU no HOM limits BBU to below 100mA in one turn**



The fundamental theory paper [1] solved the BBU time-delay integral equation by Laplace transform techniques.

$$V(t) = \int_{-\infty}^t W(t - \tau) I(\tau) V(\tau - T) d\tau$$

But with the special form of exponentially damped wake fields

$$W(t) = e^{-kt} \sin \omega t$$

One can transform to a time-delay differential equation

$$V''(t) = \omega I(t) V(t - T) - 2kV'(t) - (k^2 + \omega^2)V(t)$$

Which is now accessible to a set of theories for such equations, especially those for
Delay Differential Equations (DDEs) with periodic coefficients.

- [1] G.H. Hoffstaetter, I. Bazarov, Physical Review ST-AB, Volume 7, 54401 (May 2004)
- [2] Delay-Coupled Mathieu Equations in Synchrotron Dynamics, A. Bernstein and R. Rand, Journal of Applied Nonlinear Dynamics, 5(3):337-348 (2016)



Don't forget that there is

(A) Transverse Dipole BBU that is often considered and there are good codes

(B) Longitudinal BBU

- contained in the BMAD simulation code
- It is important because they excite monopole (accelerating) modes with very large Q
- Is minimized by T56=0 for all cavity couplings
- Phase and time-of-flight tricks need to be checked against this instability.

(C) Quadrupole BBU

- Is important because the frequencies of the lowest order Quadrupole modes are below the first higher order dipole modes. Their Q can therefore be extremely large.

(D) Higher-order multipole BBU: Check out the simple scaling formulas in [1]

- Is usually benign if (C) is ok. But it can be important for similar reasons at (C).

[1] Recirculative BBU, G.H. Hoffstaetter in A. Chao, M. Tigner, Accelerator Handbook.



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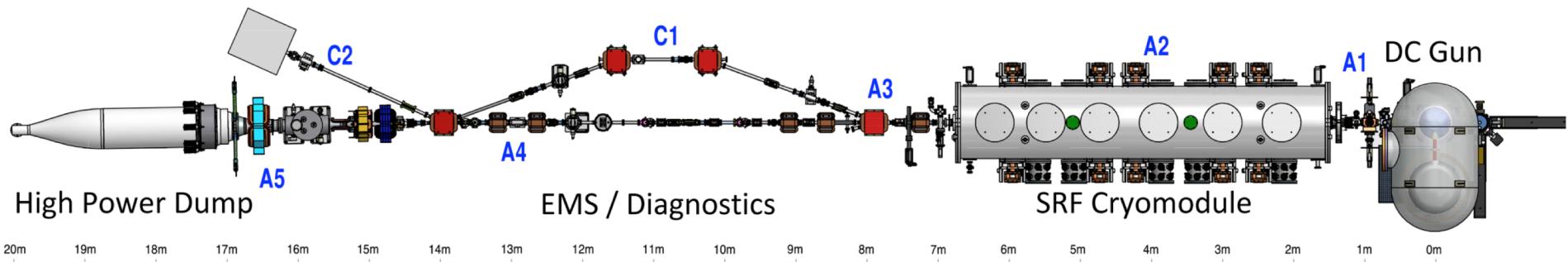
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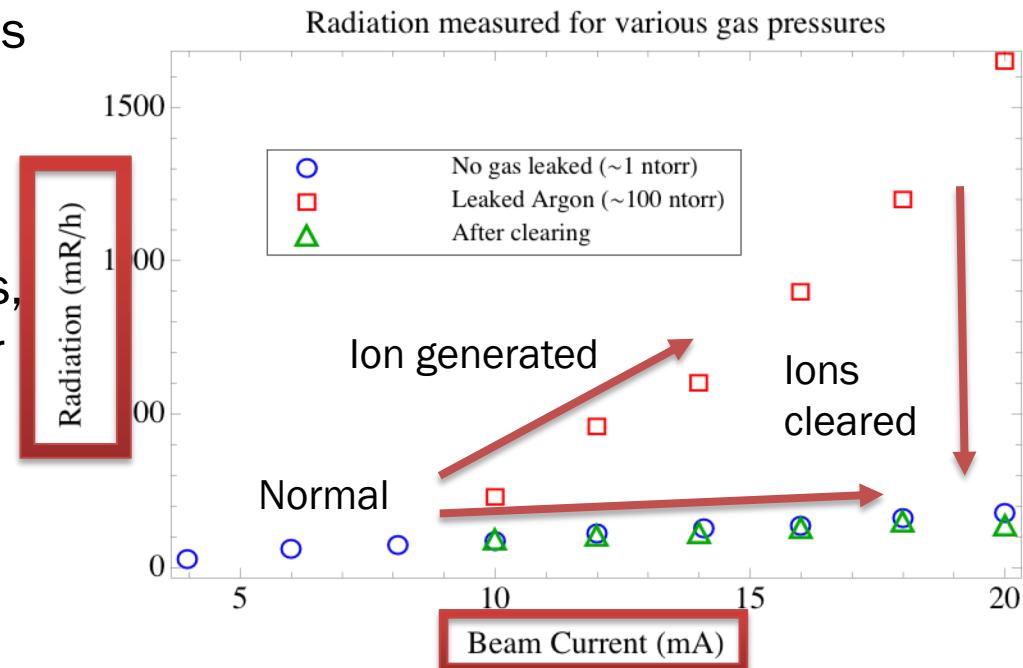
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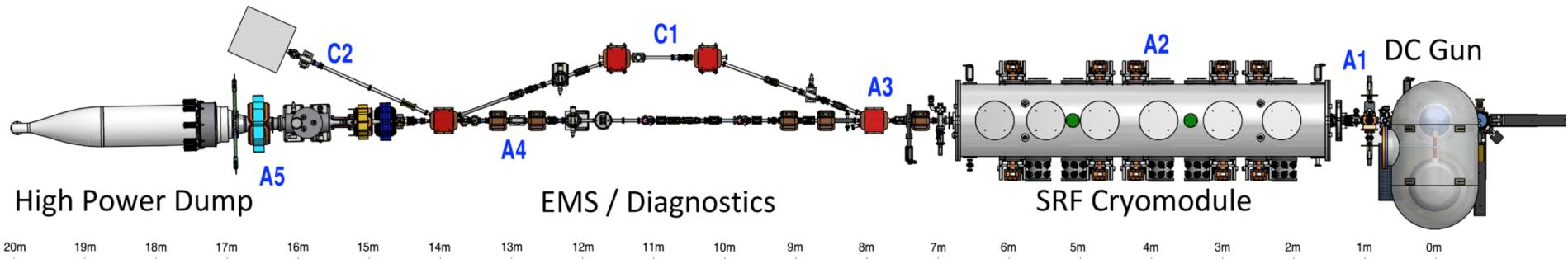


Observed ion trapping multiple times

- 1) During 75 mA, 5 MeV runs, ion clearing electrode reduced background radiation by > 50%
- 2) During low energy 350 keV runs, intermittent trips vanished after using clearing electrode

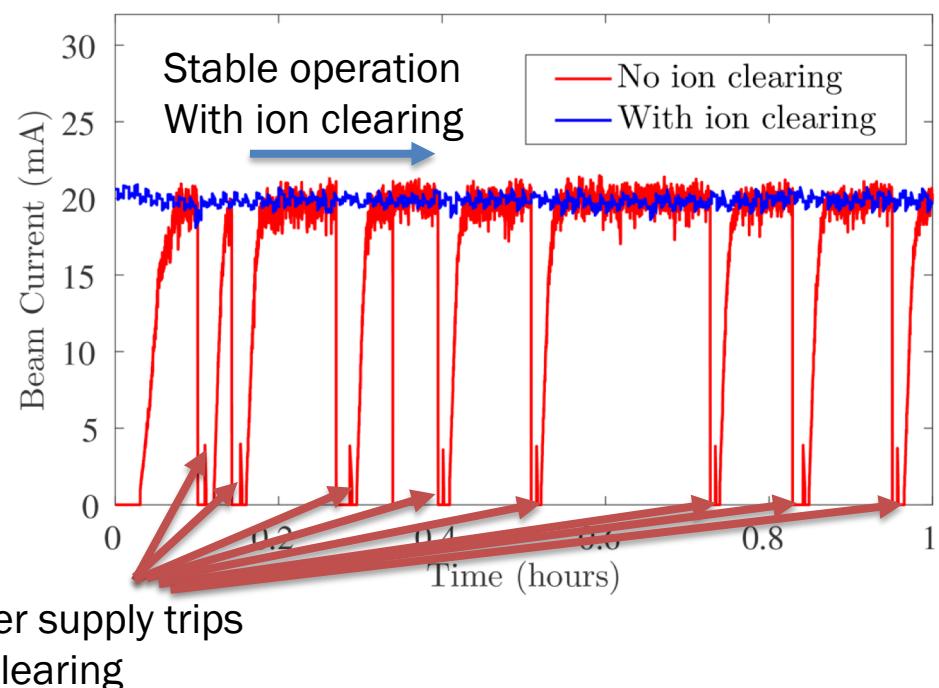


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